

Internal Surface Area Evaluation of Carbon Nanotube with GCMC Simulation-Assisted N₂ Adsorption

T. Ohba[†] and K. Kaneko^{*,†,‡}

Physical Chemistry, Material Science, Graduate School of Natural Science and Technology, Chiba University, 1-33, Yayoi, Inage, Chiba 263-8522, Japan, and Venture Business Laboratory, Chiba University, 1-33, Yayoi, Inage, Chiba 263-8522, Japan

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The N₂ adsorption on the internal and external surfaces of single-walled carbon nanotubes of the continuous model at 77 K was compared with that on the structureless graphite surface with grand canonical Monte Carlo (GCMC) simulation. The inapplicability of the BET analysis for evaluation of the surface area of the internal and external surfaces of the nanotube was explicitly shown and the reason was explained with the monolayer structure difference. The ordinary α_s -plot analysis using the standard isotherm of the flat graphite surface did not provide a reasonable method for the internal surface area. However, if we adopt the adsorption isotherm of the internal surface of the pore width being large enough to remove the enhanced potential effect, the subtracting pore effect method (SPE-IC method) using its α_s -plot gave an accurate surface area for the internal surface except for the pore width = 2 nm. The cause for the inapplicability of BET analysis was discussed with the radial distribution function of the monolayer.

1. Introduction

Recently, carbon nanotubes have gathered much attention both from fundamental science and technological interests.^{1–3} Carbon nanotubes have intraparticle pores whose width is in the range of micropores and mesopores which have been recommended by IUPAC;^{4,5} the term “nanopores” covering both micropores and small mesopores will be used in this article. As carbon nanotubes have basically a well-defined crystalline structure, high-resolution transmission electron microscopic (HR-TEM) observation can be used to determine the nanopore structures such as the internal surface area and pore width of the intraparticle pores. However, the obtained nanotube samples have heterogeneities in the primary crystal size and their assembly structure. Also, many carbon nanotube samples have amorphous carbon and metal impurity particles. Therefore, it is not easy to determine the average information on the pore structure from HR-TEM observation. Gas adsorption has contributed to providing information on average pore structures of less-crystalline porous materials such as activated carbon.^{6–8} As to activated carbon having slit-shaped micropores, the subtracting pore effect (SPE) method using high-resolution α_s -plot is quite helpful to determined the pore parameters such as surface area, pore volume, and slit width.^{9–11} The fundamental basis was obtained by grand canonical Monte Carlo (GCMC) simulation for the slit-shaped pores. In the case of the cylindrical pores, formation of the monolayer structure on the internal pore walls is quite different from adsorption in the slit pores due to the serious packing restriction.¹² Therefore, we wonder whether or not the SPE method for the slit-shaped pores can be applied

to the cylindrical nanopores.¹² If the SPE method for the slit-shaped micropores is not available for the cylindrical nanopores, there is no experimental method for evaluation of cylindrical nanopore structures. Although the BET method has been widely used in the porosity evaluation, it is well-known that the routine application provides markedly erroneous information even in the slit-shaped micropores. Accordingly, the effectiveness of the SPE method for the cylindrical nanopores must be studied.

In this work, we calculated the N₂ adsorption isotherm in the intraparticle nanopore and on the external surface of a single-walled carbon nanotube (SWNT) with GCMC simulation and constructed an α_s -plot to propose the best evaluation method of the pore structural parameters for the cylindrical pores. The proposed method is applied to the experimental data of single-walled carbon nanohorn (SWNH), providing the porosity. Also, this method can be applicable to new carbon materials prepared by use of the zeolite template.¹³ The principle can be widely applied even to new mesoporous silicas which have been widely studied.^{14–19}

2. Simulation

The N₂ adsorption isotherms at 77 K were calculated with GCMC simulation on the internal and external single-walled graphite tube as a function of pore width H from 1.5 to 8.0 nm using the following potential function.

The 12-6 Lennard-Jones potential $\phi_{ff}(r)$ for the fluid–fluid interaction at an intermolecular distance r using a single-center approximation can be calculated as follows:

$$\phi_{ff}(r) = 4\epsilon_{ff} \left[\left(\frac{\sigma_{ff}}{r} \right)^{12} - \left(\frac{\sigma_{ff}}{r} \right)^6 \right] \quad (1)$$

Here ϵ_{ff} and σ_{ff} are the N₂–N₂ potential well depth ($\epsilon_{ff}/k_B = 104.2$ K) and the effective diameter ($\sigma_{ff} = 0.3632$ nm), respectively. The structureless function was used for calculation

* Author to whom correspondence should be addressed at Department of Chemistry, Faculty of Science, Chiba University, 1-33 Yayoi, Inage, Chiba 263-8522, Japan. Fax: 81-43-290-2788. E-mail: kaneko@pchem2.s.chiba-u.ac.jp.

[†] Physical Chemistry, Material Science, Graduate School of Natural Science and Technology.

[‡] Venture Business Laboratory.

of the interaction potential of an N₂ molecule with a single-walled graphite tube.^{20,21}

$$\phi_{\text{sf}} = 4\rho\epsilon_{\text{sf}}[\sigma_{\text{sf}}^{12}I_6 - \sigma_{\text{sf}}^6I_3] \quad (2)$$

where ϵ_{sf} and σ_{sf} are fitted parameters of the N₂-carbon potential depth and effective diameter, respectively, which were obtained using the Lorentz–Berthelot rules. ρ is the number density of carbon atom. I_3 and I_6 are given by eqs 3 and 4.

$$I_6 = \frac{63\pi^2}{128a^{10}(1-\beta^2)^{10}}F\left(-\frac{9}{2}, -\frac{9}{2}, 1; \beta^2\right) \quad (3)$$

$$I_3 = \frac{3\pi^2}{4a^4(1-\beta^2)^4}F\left(-\frac{3}{2}, -\frac{3}{2}, 1; \beta^2\right) \quad (4)$$

Here $\beta = r/a$ and F is a hypergeometric function. Also the 10-4-3 potential for an atom was used for the flat surface.²²

$$\phi_{\text{sf}}(z) = A \left[\frac{2(\sigma_{\text{sf}})^{10}}{5(z)^5} - \left(\frac{\sigma_{\text{sf}}}{z}\right)^4 - \frac{\sigma_{\text{sf}}^4}{3\Delta_{\text{C}}(z + 0.61\Delta_{\text{C}})^3} \right] \quad (5)$$

where A is $2\pi\sigma_{\text{sf}}^2\epsilon_{\text{sf}}\rho\Delta_{\text{C}}$, z is the vertical distance of the molecule from the graphite surface, and Δ_{C} is the interlayer distance of the graphite.

The cylindrical pore width w , which is determined by potential calculation, is associated with the diameter H at the carbon atom position, as given by eq 6. The w must be the effective pore width which can be determined experimentally.²³

$$w = H - (2z_0 - \sigma_{\text{ff}}), \quad z_0 = 1.325\sigma_{\text{sf}} \quad (6)$$

where z_0 is the distance of the closest approach between an N₂ molecule and graphitic surface. In the case of N₂ adsorption, w (nm) can be given by $(H - 0.57)$ (nm).

The established GCMC simulation method gave the adsorption isotherms of N₂ at 77 K.^{24–27} The random movement, creation, and removal of molecules make new configurations. They are accepted when they obey Metropolis's sampling scheme in proportion to $\exp(-\Delta E/kT)$ where ΔE is the change of total energy in the system. Each step of the scheme in GCMC simulation was calculated 3×10^6 cycles.

3. Results and Discussion

3.1. Interaction Potential Profiles. Figure 1 shows the interaction potential profiles of the N₂ molecule with internal and external surfaces of single-walled carbon nanotube for $H = 2.0, 3.0$, and 5.0 nm. There are two potential minima across the pore wall: the internal potential minimum is much deeper than the external one. The interaction potential depth for the internal surface does not sensitively change with the pore width H . The internal surface has a deeper potential minimum than the external surface. The potential depth of the internal surface is almost constant in these pore width ranges, whereas that of the external surface becomes deeper with the increase of the pore width. As the potential depth difference is nearly 800 K at least, we can expect that molecular adsorption processes on the internal and external surfaces should be quite different from each other.

3.2. Adsorption Isotherms of N₂ on Internal Surface and Their BET Analysis. The N₂ adsorption isotherms on the internal wall are shown as a function of H . The adsorption isotherms for $H \leq 3$ nm are representative of Type I. The adsorption isotherms for $H > 3$ nm have a gradual step after

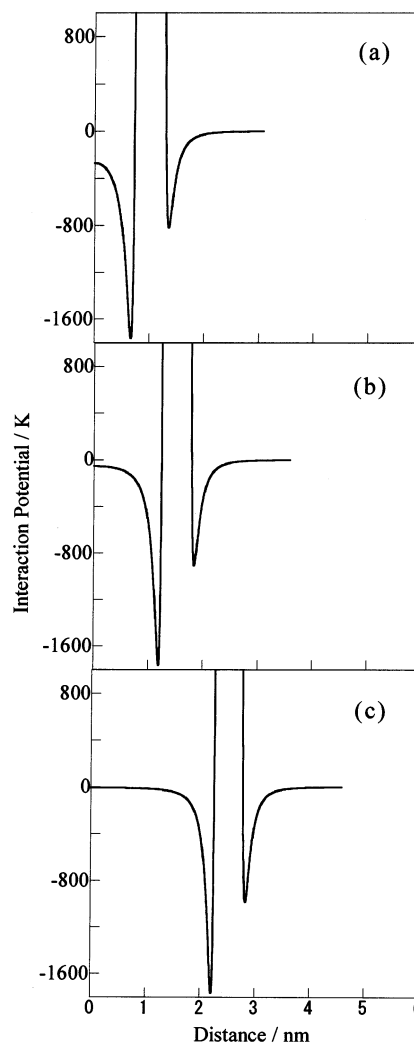


Figure 1. Potential profiles for distance from center in tube in $H = 2.0$ nm (a), 3.0 nm (b), and 5.0 nm (c).

the vertical uptake at the initial stage, as shown in Figure 2a. The interaction potential between an N₂ molecule with the cylindrical wall is more enhanced compared with the slit pore. Hence, a steep jump below $P/P_0 = 10^{-5}$ is observed even for $H = 3$ nm, as shown in Figure 2b.

The routine BET analysis has been applied to the adsorption isotherm in the P/P_0 range of 0.05 to 0.35. Figure 3 shows the BET plots. The linearity of the BET plot in the P/P_0 range of 0.05 to 0.35 is not good, suggesting the presence of the enhanced molecular potential field different from that of the flat graphite. The adsorption data below $P/P_0 = 0.05$ give a good linear BET plot. The monolayer is completely formed even at $P/P_0 = 0.05$, as shown in the snapshots of Figure 10.

Then, the usage of the adsorption data below $P/P_0 = 0.05$ is reasonable for the BET analysis. The BET surface areas a_{BET} determined from adsorption data in the P/P_0 ranges of 0.05–0.35 and 0–0.05 are compared with the surface area geometrically determined a_{geo} . The a_{geo} was calculated using the effective pore width w given by eq 6. The a_{geo} of the internal space is expressed by $\pi w \times \text{unit cell length } l$ of the carbon nanotube. The a_{geo} of the external surface is given by $\pi(H + 0.61) \times l$ (unit: nm) which will be shown later. Figure 4 shows the change of the ratio of a_{BET} to a_{geo} with physical width H for the internal surface for both P/P_0 ranges. Both P/P_0 ranges do not give a simple relation. The ratio of $a_{\text{BET}}/a_{\text{geo}}$ in the P/P_0 range of 0.05 to 0.35 has no constant region and changes from

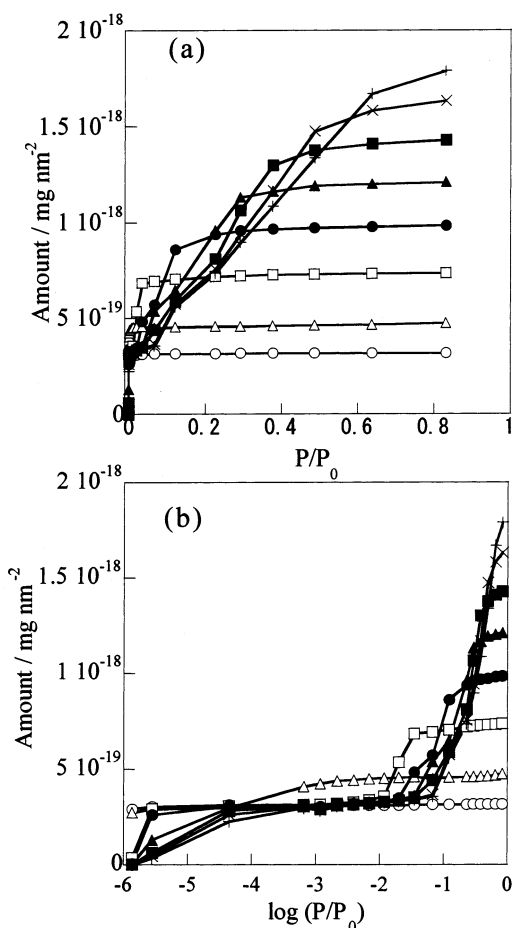


Figure 2. Adsorption isotherms of N₂ in internal pore (a) and log plots (b). \circ : $H = 1.5$ nm, Δ : $H = 2.0$ nm, \square : $H = 3.0$ nm, \bullet : $H = 4.0$ nm, \blacktriangle : $H = 5.0$ nm, \blacksquare : $H = 6.0$ nm, \times : $H = 7.0$ nm, and $+$: $H = 8.0$ nm.

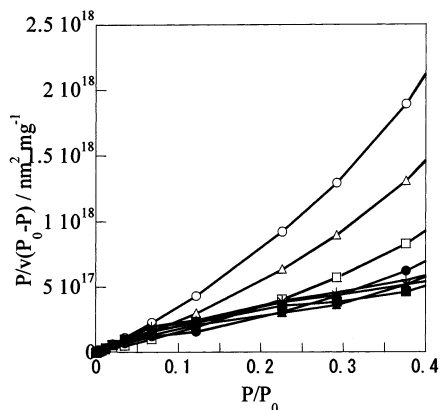


Figure 3. BET plots of N₂ in internal pore. \circ : $w = 1.5$ nm, Δ : $w = 2.0$ nm, \square : $w = 3.0$ nm, \bullet : $w = 4.0$ nm, \blacktriangle : $w = 5.0$ nm, \blacksquare : $w = 6.0$ nm, \times : $w = 7.0$ nm, and $+$: $w = 8.0$ nm.

0.75 to 3.2. The snapshots, which will be shown in Figure 10 later, give the cause for the great deviation from unit. In this P/P_0 range, multilayer adsorption proceeds. Hence, the second layer structure and the presence of the enhanced third or fourth layer formation gives rise to the overestimation of the surface area with the BET analysis. On the other hand, $a_{\text{BET}}/a_{\text{geo}}$ vs pore width H below 0.05 of P/P_0 has an almost constant value of 1.2 for the pore width greater than 4.5 nm, although it varies from 1.1 to 2.3 for the H value less than 4.5 nm. In this case, an enhanced second layer formation occurs for narrow pores, inducing a greater $a_{\text{BET}}/a_{\text{geo}}$ value below $H = 4$ nm, while the

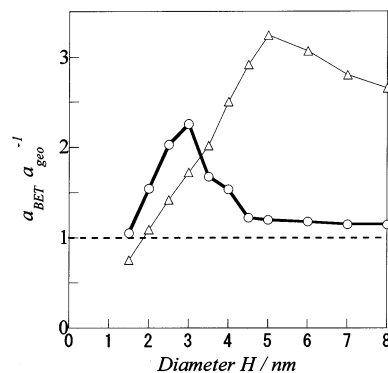


Figure 4. Ratio of a_{BET} to a_{geo} with physical width H for the internal surface area. Here a_{BET} is determined from $P/P_0 = 0-0.05$: \circ and $P/P_0 = 0.05-0.35$: Δ .

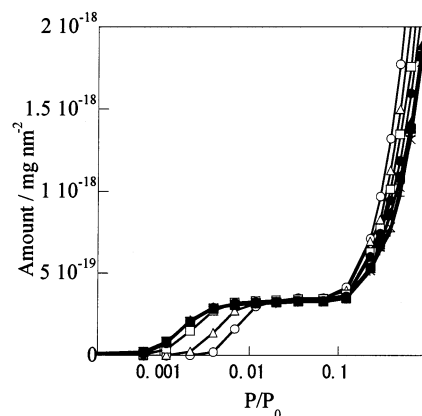


Figure 5. Adsorption isotherms of N₂ in external pore. \circ : $H = 1.5$ nm, Δ : $H = 2.0$ nm, \square : $H = 3.0$ nm, \bullet : $H = 4.0$ nm, \blacktriangle : $H = 5.0$ nm, \blacksquare : $H = 6.0$ nm, \times : $H = 7.0$ nm, and $+$: $H = 8.0$ nm.

monolayer having the closed packing structure cannot be formed for pores of $H > 4$ nm, giving a slight deviation from unit. Hence a_{BET} from the adsorption data below $P/P_0 = 0.05$ should be more favorable. However, the evaluation of the internal surface area of carbon nanotube with BET method is seriously erroneous.

3.3. Adsorption Isotherms of N₂ on External Surfaces and Their BET Analysis. Figure 5 shows adsorption isotherms on the external surface. The larger the pore width H , the lower the step position in the low-pressure region. On the contrary, the smaller the pore width, the lower the rising pressure above 0.1 of P/P_0 . The adsorption isotherm on the external surface is insensitive to the pore width compared with adsorption on the internal surface, which comes from the weaker molecule-surface interaction than that on the internal surface. The fitting of the adsorption isotherm to the BET equation was not good for the whole P/P_0 range. Although the linearity is worse than that for the internal surface, the a_{BET} was determined; $a_{\text{BET}}/a_{\text{geo}}$ against physical width H is shown in Figure 6. The ratio from the adsorption data of $P/P_0 = 0.05-0.35$ decreases from 3.7 to 1.8 with the increase of H from 1.5 to 8.0 nm. Then the routine BET analysis must not be used in this case, too.

3.4. Simulated α_s -Plot and SPE Method for Adsorption on Internal Surface. As the BET analysis cannot be applied to nanotube systems, an optimum method must be developed. As the SPE method using the high-resolution α_s -plot can provide the accurate surface area of the slit pore of $w \geq 0.6$ nm, the applicability of the SPE method to the cylindrical pore must be studied. Construction of the α_s -plot needs the standard adsorption isotherm. Here there are two possibilities for the standard

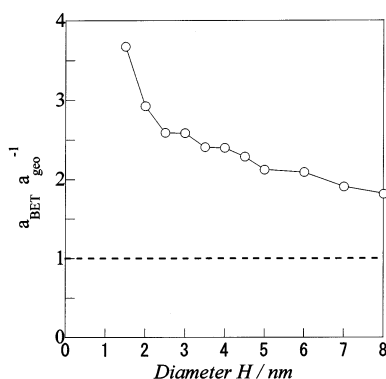


Figure 6. Ratio of a_{BET} to a_{geo} for the internal surface with physical width H in the P/P_0 range of 0.05 to 0.35.

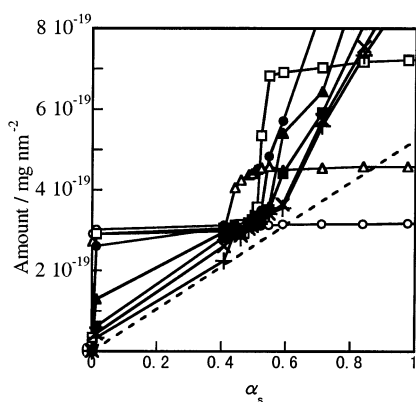


Figure 7. α_s -plots for adsorption on internal surface from the standard adsorption isotherm of the flat surface (dashed line). \circ : $H = 1.5$ nm, \triangle : $H = 2.0$ nm, \square : $H = 3.0$ nm, \bullet : $H = 4.0$ nm, \blacktriangle : $H = 5.0$ nm, \blacksquare : $H = 6.0$ nm, \times : $H = 7.0$ nm, and $+$: $H = 8.0$ nm.

adsorption isotherm. One is to use the adsorption isotherm on the flat graphite surface. Another is to adopt the adsorption isotherm on the internal surface of a relatively large pore width. Then, we used two simulated adsorption isotherms on the flat graphite surface and the internal surface of $H = 8$ nm as the standard adsorption isotherm. Figure 7 shows the constructed α_s -plots from the standard adsorption isotherm of the flat surface. Here the broken line indicates adsorption on the flat surface whose surface area is known. When the simulated α_s -plot has a linear region overlapping the broken line, the slope of the linear region leads to the accurate surface area. There are two upward deviations below and above $\alpha_s = 0.44$, although all α_s -plots deviate upward from the reference line expressed by the broken line. Some of the upward deviated α_s -plots in the low α_s region cross each other at $\alpha_s = 0.44$. However, α_s -plots do not cross or overlap the reference line except for $H = 2.0$ nm. Therefore, it is difficult to remove the enhanced adsorption and to determine the linear relation in this case.

Figure 8 shows the α_s -plot constructed from the standard adsorption isotherm of the internal surface of $H = 8.0$ nm. The α_s -plot has an upward deviation below or above $\alpha_s = 0.32$ except for $H = 2.0$ nm. All α_s -plots other than that for $H = 2.0$ nm cross the reference line at $\alpha_s = 0.32$. Hence the enhanced adsorption effect can be removed using the line passing both of the origin and the adsorption point at $\alpha_s = 0.32$. Thus, we can determine precisely the internal surface area from the slope of the line except for $H = 2.0$ nm. Therefore, the surface area from this method, which may be denoted the subtracting pore effect method for the internal surface of cylindrical pores using the standard isotherm on the internal surface of great H (SPE-IC method), is superior to that from the method using the

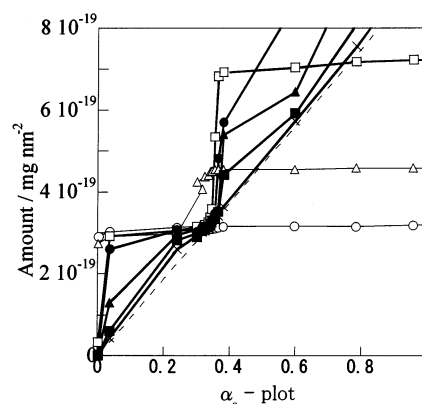


Figure 8. α_s -plots from the standard adsorption isotherm in $H = 8.0$ nm. \circ : $H = 1.5$ nm, \triangle : $H = 2.0$ nm, \square : $H = 3.0$ nm, \bullet : $H = 4.0$ nm, \blacktriangle : $H = 5.0$ nm, \blacksquare : $H = 6.0$ nm, and \times : $H = 7.0$ nm.

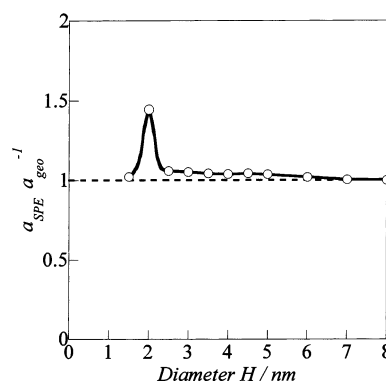


Figure 9. Ratio of a_{SPE} for a_{geo} with physical width from α_s plot used by simulated adsorption isotherm in $H = 8.0$ nm as standard isotherm.

isotherm on the flat surface as the standard isotherm. The difference of the packing state of molecules on the flat and internal surfaces is taken into account in the SPE-IC method. Then this SPE-IC method can evaluate the internal surface area without an enhanced adsorption effect by the pore potential.

The upward deviation of the α_s -plot stems from the enhanced adsorption on monolayer adsorption due to the strong molecule–pore wall interaction, compared with the internal surface of $H = 8.0$ nm. The a_{SPE} is determined after subtraction of adsorption due to the enhanced potential, and thereby the a_{SPE} must be close to a_{geo} . Figure 9 shows the a_{SPE} vs a_{geo} relation. a_{SPE} almost coincides with a_{geo} except for $H = 2$ nm. In the case of $H = 2$ nm, a_{SPE} is overestimated. This is because the molecule–pore interaction is strong enough to induce an accelerated secondlayer adsorption at the pressure corresponding to $\alpha_s = 0.32$. Although the a_{SPE} vs a_{geo} for the standard adsorption isotherm of the flat surface is not shown here, the a_{SPE} did not agree with a_{geo} . Therefore, a_{SPE} using the standard adsorption isotherm of $H = 8.0$ nm is strongly recommended for the internal surface area of the carbon nanotube. The practical determination method for evaluation of the internal surface area a_{SPE} is described by eq 7:

$$a_{\text{SPE}} = 0.71 \text{slope} [\text{m}^2 \text{g}^{-1}] \quad (7)$$

when we use the standard data of P/P_0 vs α_s for N_2 adsorption on the internal surface of $H = 8.0$ nm and adsorption amount is expressed by mg g^{-1} .

3.5. Monolayer Adsorbed State from Snapshot Analysis.

Figure 10 shows snapshots of N_2 adsorbed on the internal and external surfaces of carbon nanotubes of $H = 2.0$, 5.0 , and 8.0

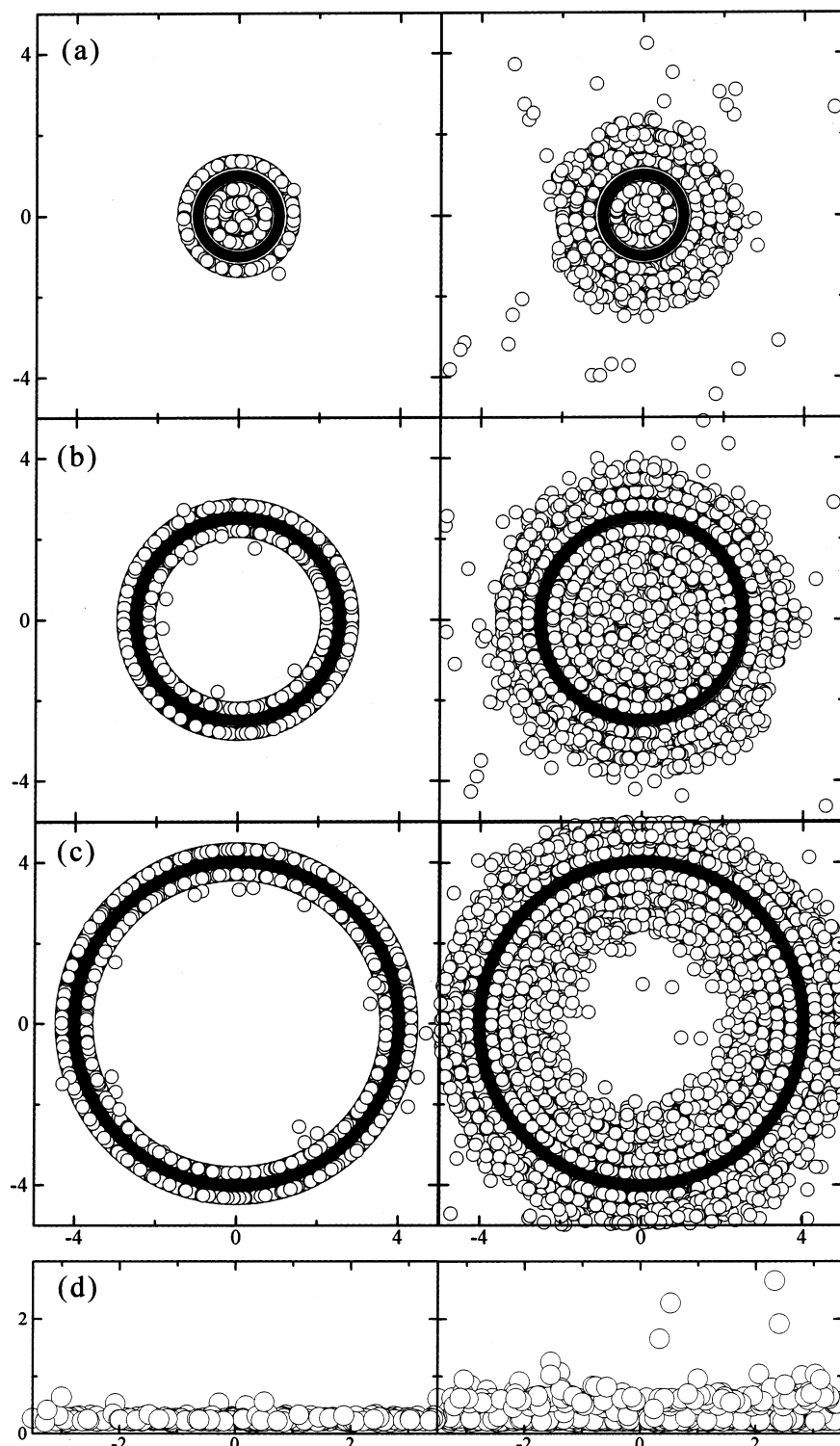


Figure 10. Snapshots of N_2 molecules adsorbed on the tube of $H = 2.0$ nm (a), 5.0 nm (b), and 8.0 nm (c), and on flat surface (d). Left side: $P/P_0 = 0.05$ and right side: $P/P_0 = 0.35$.

nm and those on the flat graphite surface for $P/P_0 = 0.05$ and 0.35 . The internal space of $H = 2.0$ nm is already filled with molecules even at $P/P_0 = 0.05$, whereas the monolayer is completed on the external surface. This adsorption behavior for $H = 2.0$ nm is far from larger pore cases, although adsorption processes on the internal surfaces of $H = 5.0$ and 8.0 nm are almost similar to that on the flat surfaces at $P/P_0 = 0.05$. However, even the internal space of $H = 5.0$ nm is filled with molecules at $P/P_0 = 0.35$, while that of $H = 8.0$ nm is not completely filled.

We compared the intermolecular structure of the monolayer on the internal surface with that on the flat surface using radial distribution function. Figure 11 shows the radial distribution function of monolayerly adsorbed molecules on the perimeter of the circular tube-wall as a function of H . The radial distribution function for the flat surface is also shown for comparison. Here the circumference of the circular surface of the internal tube-wall is stretched to the straight line. As molecules are more packed on a more concave wall of the tube, the intermolecular distance becomes larger on the stretched

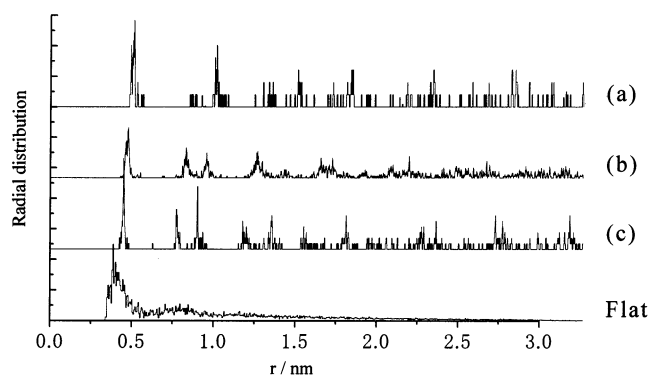


Figure 11. Radial distribution function of adsorbed molecules at right angles to carbon nanotubes in upper order to $H = 3.0, 4.0, 6.0$ nm, and flat surface.

surface, as shown in Figure 11. Hence, the smaller the H value, the longer the distance to the nearest neighbor peak. The nearest neighbor distance for $H = 3.0$ nm is longer than that for the flat surface by 20%. This difference is an indication of the structural restriction for mutual packing in the monolayer, because the restriction for packing needs a larger area occupied by the adsorbed molecules. The second nearest neighbor distance for $H = 3.0$ nm is just twice that of the first nearest neighbor distance, suggesting the square packing on the real concave surface. The second nearest peak for $H = 4.0$ and 6.0 nm splits into two peaks, and thereby the molecular assembly of the monolayer for $H = 4.0$ and 6.0 nm should have a different symmetry from that for $H = 3.0$ nm. These peaks correspond to hexagonal closed packing and square packing, respectively. As the first and second nearest peaks of the flat surface are broader, the molecular packing should have flexibility. Therefore, the molecules in the internal space should have a more ordered structure compared with those on the flat surface, although they cannot form a close packing structure. Thus, the molecular structure for the monolayer on the internal surface of the carbon nanotube depends sensitively on the pore width, leading to a molecular structure different from that on the flat surface. These specific monolayer structures give rise to the situation that the ordinary BET analysis cannot be applied to evaluation of the internal surface of the carbon nanotubes.

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References and Notes

- (1) Scaife, S.; Kluson, P.; Quirke, N. *J. Phys. Chem. B* **2000**, *104*, 313.
- (2) Lastoskie, C.; Gubbins, K. E.; Quirke, N. *J. Phys. Chem.* **1993**, *97*, 4786.
- (3) Murata, K.; Kaneko, K. *Chem. Phys. Lett.* **2000**, *321*, 342.
- (4) Sing, K. S. W.; Everett, D. H.; Haul, R. A. W.; Moscon, L.; Pierotti, R. A.; Rouquerol, J.; Siemieniowska, T. *Pure Appl. Chem.* **1985**, *57*, 603.
- (5) Kaneko, K. *J. Membr. Sci.* **1994**, *96*, 59.
- (6) Kaneko, K. *Carbon* **2000**, *38*, 287.
- (7) Molina-Sabio, M.; Munecas, M. A.; Rodriguez-Reinoso, F.; MacEnaney, B. *Carbon* **1995**, *33*, 1777.
- (8) Seaton, N. A.; Walton, J. P. R. B.; Quirke, N. *Carbon* **1989**, *27*, 853.
- (9) Sing, K. S. W. *Carbon* **1989**, *27*, 25.
- (10) Kaneko, K.; Ishii, C. *Colloid Surf.* **1992**, *67*, 203.
- (11) Setoyama, N.; Suzuki, T.; Kaneko, K. *Carbon* **1998**, *36*, 1459.
- (12) Ohba, T.; Murata, K.; Kaneko, K.; Steele, W. A.; Kokai, F.; Takahashi, K.; Kasuya, D.; Yudasaka, M.; Iijima, S. *Nanoletters* **2001**, *1*, 371.
- (13) Ma, Z.; Kyotani, T.; Liu, Z.; Terasaki, O.; Tomita, A. *Chem. Mater.*, in press.
- (14) Llewellyn, P. L.; Grillet, Y.; Rouquerol, J.; Martin, C.; Coulomb, J.-P. *Surf. Sci.* **1996**, *352–354*, 468.
- (15) Kruk, M.; Jaroniec, M. *J. Phys. Chem. B* **1997**, *101*, 583.
- (16) Kruk, M.; Jaroniec, M.; Sayori, A. *Langmuir* **1997**, *13*, 6267.
- (17) Kruk, M.; Jaroniec, M.; Ryoo, R.; Kim, J. M. *Microporous Mater.* **1997**, *12*, 93.
- (18) Morishige, K.; Fujii, H.; Uga, M.; Kinukawa, D. *Langmuir* **1997**, *13*, 3494.
- (19) Jaroniec, M.; Kruk, M.; Olivier, J. P. *Langmuir* **1999**, *15*, 5410.
- (20) Steele, W. A.; Bojan, M. J. *Adv. Colloid Interface Sci.* **1998**, *153*, 7677.
- (21) Curtarolo, S.; Stan, G.; Cole, M. W.; Bojan, M. J.; Steele, W. A. *Phys. Rev. E* **1999**, *59*, 4402.
- (22) Steele, W. A. *Surf. Sci.* **1973**, *36*, 317.
- (23) Kaneko, K.; Cracknell, R. F.; Nicholson, D. *Langmuir* **1994**, *10*, 4606.
- (24) Lee, M.; Cahn, K.-Yu.; Nicholson, D.; Zara, S. *Chem. Phys. Lett.* **1999**, *307*, 89.
- (25) Seo, Y. G.; Kum, G. H.; Seaton, N. *J. Membr. Sci.* **2002**, *195*, 65.
- (26) Gavalda, S.; Kaneko, K.; Thomson, K. T.; Gubbins, K. E. *Colloid Surf. A* **2001**, *187–188*, 531.
- (27) Ohba, T.; Suzuki, T.; Kaneko, K. *Chem. Phys. Lett.* **2000**, *326*, 158.