See discussions, stats, and author profiles for this publication at: https://www.researchgate.net/publication/229046806

# Mott-Schottky and Charge-Transport Analysis of Nanoporous Titanium Dioxide Films in Air

Δ	R	Т	1	(	1	F	i	n	Т	Ή	IF	10	1	Ш	R	Ν	12	١L		۱(	Ε	P	Н	۱١	V	SI	(	. Δ	П	(		Н	F	N	11	ς	Т	Ē	V	(	٠,	M	1	١F	5	$\Gamma$	Н	-	1	10	١7	7
$\overline{}$	w	·		·	_	_	- 1	11	- 1		41-	 , (	,,	JI	1	I١	1	۱L	~	"				ш	ı	וכ			۱∟	٠,	_		_	. I V	ш	-		11	·	٠.	_	ľ	_	N١	١,	L			Δι.	v	, ,	

Impact Factor: 4.77 · DOI: 10.1021/jp068354l

CITATIONS READS

37 63

### 4 AUTHORS, INCLUDING:



Marius Nanu thin film factory

35 PUBLICATIONS 799 CITATIONS

SEE PROFILE



Joop Schoonman

**Delft University of Technology** 

605 PUBLICATIONS 8,929 CITATIONS

SEE PROFILE

## Mott-Schottky and Charge-Transport Analysis of Nanoporous Titanium Dioxide Films in Air

## Ryan O'Hayre,\*,† Marian Nanu,‡ Joop Schoonman,‡ and Albert Goossens‡

Department of Metallurgical and Materials Engineering, Colorado School of Mines, 1500 Illinois Street, Golden, Colorado 80401, and Delft Institute for Sustainable Energy, Delft University of Technology, 2628 BL Delft, The Netherlands

Received: December 5, 2006; In Final Form: January 26, 2007

We investigate the electrical properties of air-filled nanoporous TiO<sub>2</sub> films through Mott-Schottky (MS) and current-voltage (IV) analyses. Films of varying thickness and varying TiO<sub>2</sub> particle size are examined. Dark IV analysis indicates formation of an asymmetric Schottky-barrier junction between the nanoporous TiO<sub>2</sub> film and a graphite back contact. Upon increasing the film thickness and decreasing the particle size, diode rectification deteriorates while series resistance increases; these phenomena are attributed to resistive hopping charge transport between TiO2 particles. Dramatic differences in the dark-IV extrapolated resistance of comparable thickness 300 and 9 nc films indicate that the transport physics may be substantially different between these two types of films in the dark. An effective medium model is developed that appropriately describes the dark MS data, indicating that the TiO<sub>2</sub> film behaves as a pure dielectric in the depletion region and that the internal surface area of the film does not contribute to the capacitance. Upon UV illumination, photodoping increases the TiO<sub>2</sub> film conductivity. Fermi-level splitting results in an ohmic graphite contact and current flow is generally limited by carrier transport rather than charge transfer to the contact. IV analysis based on a space charge limited current model provides mobility estimates of  $\sim 1.7-3.4 \times 10^{-4}$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> for the 9 nm diameter  $\text{TiO}_2$  particle films and  $\sim 1.8 - 3.5 \times 10^{-4} \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for 300 nm diameter  $\text{TiO}_2$ particle films under AM 1.5 illumination. The close agreement between the illuminated-IV extrapolated electron mobility for both the 9 and 300 nm diameter TiO<sub>2</sub> particles suggests that the transport physics are likely similar in both films when illuminated.

#### I. Introduction

The low cost, ease of fabrication, wide availability, and high stability of porous nanocrystalline TiO<sub>2</sub> has led to its increasing deployment in a variety of functional applications. For example, it is extensively used in dye-sensitized solar cells (DSSCs), 1,2 photocatalysis and photoelectrochemistry, 3,4 electrochromics,5 and sensors.<sup>6,7</sup> Despite its widespread application, the electrical properties of porous nanocrystalline TiO<sub>2</sub> are still poorly understood. Characterization and interpretation is complicated by structural disorder, high surface area, and the influence of defects.<sup>8,9</sup> So far, most studies have focused on the properties of nanoporous TiO2 films when immersed in an electrolyte, since this reflects the situation experienced in DSSCs and in most other applications. 10-19 A general consensus has emerged from these TiO2/electrolyte studies, yielding the following conclusions: (1) Surface states at the TiO<sub>2</sub>/electrolyte interface strongly influence the electrical behavior of the system, affecting both charge-transport and recombination processes. (2) Mobile ionic species in the liquid electrolyte effectively screen the TiO<sub>2</sub> from any macroscopic electric fields, leading to the dominance of diffusion-based transport of electrons within the nanoporous TiO<sub>2</sub> film. (3) The low intrinsic conductivity of the TiO<sub>2</sub> film in combination with field screening means that under depletion conditions the potential drop across the nanoporous TiO2 film should be sharply localized to the substrate/TiO<sub>2</sub> interface. These conclusions have important ramifications for catalytic and photovoltaic applications of nanocrystalline  ${\rm TiO_2/electrolyte}$  systems.

Despite the extensive research on TiO<sub>2</sub>/electolyte systems, however, far fewer studies have characterized the properties of porous nanocrystalline TiO<sub>2</sub> films in ambient air. 8,20-22 Such research is needed, because air-based measurements are more likely to reflect the conditions presented by nonelectrolyte applications of nanoporous TiO2 (like some sensor applications, <sup>23</sup> or the recently developed 3D nanocomposite inorganic solar cell<sup>24,25</sup>). It should be expected that the electrical behavior of nanoporous TiO2 will change significantly in the absence of an electrolyte, due to the loss of ion screening and changes in interfacial chemistry. For example, in air and vacuum based studies of nanoporous TiO<sub>2</sub>, Nelson et al. observed significant changes in the electron transport and recombination behavior when varying the environmental conditions.<sup>8,20</sup> They attributed these effects primarily to electron scavenging by surface absorbed species. In a separate study, Konenkamp observed reduced electron mobility in air-filled nanoporous TiO<sub>2</sub> films compared to electrolyte filled films.<sup>22</sup> He hypothesized that charge transfer or surface passivation at the TiO2/electrolyte interface may decrease the available trap states in electrolyte filled films compared to the air-filled case.

In this paper, the electrical properties of air-filled nanoporous  $TiO_2$  films are further defined through Mott–Schottky (MS) and current–voltage (IV) analyses in dark and IV analysis under illumination. Films of varying thickness and varying  $TiO_2$ 

<sup>\*</sup> Address correspondence to this author. E-mail: rohayre@mines.edu.

<sup>†</sup> Colorado School of Mines.

<sup>‡</sup> Delft University of Technology.

TABLE 1: Characteristics of Samples Used in the Study

sample	crystallite size (nm)	nanoporous layer thickness (nm)
DL only	N/A	N/A
300nc-50nm	300	50
300nc-130nm	300	130
300nc-350nm	300	350
300nc-1100nm	300	1100
9nc-350nm	9	350
9nc-850nm	9	850
9nc-1150nm	9	1150

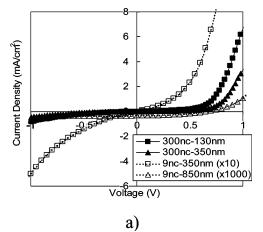
particle size are investigated. MS analysis as a function of film thickness is used to elucidate the distribution of the electric field in air-filled nanoporous  ${\rm TiO_2}$  films, while IV analysis provides insight into the charge-transport mechanisms and electron mobility.

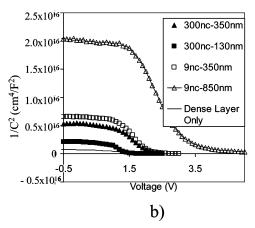
#### **II. Experimental Section**

Nanoporous TiO<sub>2</sub> film structures in the configuration glass/ TCO/TiO<sub>2</sub>/graphite were prepared as follows. To eliminate the possibility of shorting, a thin ( $\sim$ 200 nm) dense underlayer of anatase TiO<sub>2</sub> was first deposited onto transparent conductive oxide (TCO) coated glass substrates via the spray pyrolysis technique (described in detail in ref 25). Nanoporous TiO<sub>2</sub> film coatings were subsequently deposited via the doctor blade technique from commercially available precursor pastes (Solaronix, Inc.). Two different film types containing 9 and 300 nm TiO<sub>2</sub> nanocrystallites, respectively, were prepared. These will be referred to as 9nc and 300nc film types throughout this paper. By varying the viscosity of the precursor pastes via dilution with ethanol, films of varying thickness were produced  $(0.05-1.15 \mu m)$ . Table 1 provides a summary of the samples used in this study. Sample 9nc-350nm in Table 1, for example, was a 350 nm thick film prepared from 9 nm diameter TiO<sub>2</sub> nanocrystallites. The "DL only" sample consisted of only the spray-coated dense TiO<sub>2</sub> layer without an overlying nanoporous

After annealing at 450 °C for 6 h in air to remove organics, circular graphite electrodes (19.6 mm<sup>2</sup> in area) were applied to the top surfaces of the films. The graphite electrodes were painted onto the samples with conductive graphite ink. Electrode size was defined with use of a stencil mask. The graphite ink contained graphite flakes of approximately 30  $\mu$ m diameter. In all electrical measurements, the top graphite electrode served as the working electrode, while the bottom TCO film served as the counter/reference electrode. Thus in forward bias, the graphite film was positive relative to the TCO electrode. Electron microscope cross-sectional images showed that graphite penetration into the nanoporous TiO<sub>2</sub> film was not a problem due to the large grain size ( $\sim$ 30  $\mu$ m) of the graphite. Therefore, to a reasonable approximation, the contact geometry could be considered planar. For all samples, film thickness was quantified with a Detak 6M profilometer (Veeco Instruments). Porosity, determined by measuring the weight and film dimensions of witness samples, was estimated to be 56% ( $\pm$ 5%) for the 9nc films and 66% ( $\pm$ 3%) for the 300nc films. In both cases, within experimental error, porosity was independent of film thickness. For the thinnest (50 and 130 nm) film samples employing the 300 nm crystallites, porosity was not a meaningful descriptor since these films provided only partial surface coverage.

IV measurements were performed in the dark and in the light with a Princeton Applied Research 273 potentiostat/galvanostat. For measurements in the light, illumination was provided with





**Figure 1.** Dark IV curves (a) and corresponding dark MS curves (b) for selected 9nc and 300nc samples. The current—density values for the 9nc-350nm and 9nc-850nm IV curves have been amplified by a factor of 10 and 1000, respectively, for clarity.

a calibrated AM 1.5 solar simulator (Solar Constant 1200, K.H. Steuernagel Lichttechnik GmbH). MS measurements were acquired with a Solartron 1255 FRA in combination with a Princeton Applied Research 283 potentiostat/galvanostat. In all cases, a 10 mV sinusoidal excitation signal was employed to interrogate the capacitance. Capacitance was determined from single-frequency measurements at high frequency by assuming a simple series RC circuit model for the system. Capacitances calculated by using this approach were similar to capacitances extracted from full impedance spectrum fits (measured in the range 1 MHz-1 Hz). Furthermore, the capacitances calculated from single-frequency measurements did not significantly vary in the range 1 MHz-10 kHz. All data presented in this paper are from 100 kHz measurements. Area normalized capacitance values (units of F/cm<sup>2</sup>) are employed in all equations and data results throughout. All measurements were made at room temperature and ambient humidity (T = 20 °C, RH  $\approx 60\%$ ).

#### III. Results and Discussion

**A. Dark IV** Analysis. Figure 1a presents typical dark IV responses for a series of 9nc and 300nc TiO<sub>2</sub> films of varying thickness. In all cases, an asymmetric, Schottky-barrier response is observed. Mott—Schottky measurements (presented in the next section) suggest that the rectifying junction occurs between the nanoporous TiO<sub>2</sub> film and the graphite back contact. We believe that the front contact (between F-doped SnO<sub>2</sub> and the spray deposited TiO<sub>2</sub> film) is ohmic, although recent reports suggest

TABLE 2: Dark IV Characteristics of the Investigated

sample	G (mS/cm <sup>2</sup> )	$R (\Omega \text{ cm}^2)$	n	$J_{\rm o}~({\rm mA/cm^2})$
DL only	0.385	19.2	3.2	$1.1 \times 10^{-3}$
300nc-50nm	0.06	14.4	2.7	$3 \times 10^{-5}$
300nc-130nm	0.17	21.3	3.1	$1 \times 10^{-4}$
300nc-350nm	0.06	14.9	2.6	$2.0 \times 10^{-5}$
300nc-1100nm	0.47	53.5	12	$4 \times 10^{-2}$
9nc-350nm	0.2	532	4.2	$9.5 \times 10^{-3}$
9nc-850nm	0.001	2860	8.1	$5 \times 10^{-6}$

that this junction can also induce a Schottky-barrier response.<sup>26</sup> Our assignment of the recitifying junction to the graphite contact is bolstered by the fact that symmetric test cells of the configuration TCO/TiO2/TCO show ohmic behavior while symmetric test cells of the configuration graphite/TiO<sub>2</sub>/graphite show diode behavior.

The IV curves presented in Figure 1a can be analyzed by using a modified Schottky barrier diode-equation approach. In this approach, we assume that the current is limited by thermionic emission over the Schottky barrier, while neglecting tunneling or diffusion modifications. This assumption is reasonable over the voltage range ( $\pm 1$  V) presented in Figure 1. While tunneling and diffusion are not considered, we find it necessary to take into account series resistance (R) and shunt (G)conductance losses, using a modified diode approach as described in ref 27:

$$J = J_{o} \exp\left[\frac{e}{nkT}(V - RJ) - 1\right] + GV - J_{sc}$$
 (1)

In this equation, n is the diode ideality factor, e is the electron charge, k is Boltzmann's constant, T is temperature, and  $J_0$  is the exchange current. This equation assumes that the shunt conductance (G) is in parallel with the series combination of the diode plus the series resistance (R). Thus, G experiences the full voltage drop V, and the current flowing through the shunt conductance is given by G\*V (rather than G\*\*[V-RJ]). We feel that this model adequately reflects the physical situation in our samples, since the shunt-conduction pathway likely corresponds to pinholes/shorts in our films that short both the TiO<sub>2</sub> layer and the diode interface. Applying eq 1 to the experimentally measured IV data permits values for R, G, n, and  $J_0$  to be extracted for all samples listed in Table 1. The results of this analysis are presented in Table 2.

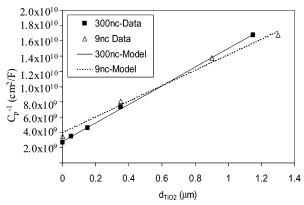
The resistance term, R, represents a "lumped" resistance associated with the bulk resistance associated with both the nanporous and dense TiO2 film layers, the measurement leads, and the TCO and graphite electrodes. For the 300nc samples, R is relatively constant (between 14 and 21  $\Omega$  cm<sup>2</sup>) for film thicknesses between 0 and 350 nm. The nanoporous film in these cases consists of isolated "clumps" or islands of TiO2 nanoparticles dispersed on the dense TiO<sub>2</sub> substrate layer (this clumping is strongly indicated by Detak profilometer measurements of the thin 300nc films). The nanoporous layer "thickness", in this case, thus represents a mixing between the height of the nanoparticle clumps (~300 nm high) and zero thickness (where the dense layer is not covered by nanoparticles). In these films, because the film thickness is smaller than the particle size, conduction likely occurs through discontinuities in the nanoporous film. Series resistance in this domain is therefore controlled by the characteristics of the underlying dense TiO2 layer. In the 300nc-1100nm sample, the nanoporous TiO<sub>2</sub> film thickness is greater than the particle size and additional series resistance is incurred due to interparticle hopping charge transport through the nanoporous film. R increases com-

mensurately. In the 9nc samples, R is even higher, and is dominated by the resistance of the nanoporous TiO<sub>2</sub> film. We have previously observed similar transport behavior trends in comparable nanoporous TiO<sub>2</sub> films.<sup>28</sup> There are several possible reasons for the significantly increased series resistance associated with the 9nc films: (1) increased resistance due to the significantly increased number of interparticle junctions, (2) increased resistance due to an increase in shallow traps, (3) increased resistance due to an increase in deep traps, and (4) increased resistance due to a decrease in donor density. The first two factors would effectively decrease the electron mobility, while the last two factors would decrease the effective carrier concentration. Trends in the other IV parameters, such as G, and  $J_0$ , are not clearly resolved, although the diode ideality factor (n) increases substantially in the thickest films.

B. Dark MS Analysis. Representative MS curves for the samples discussed above are provided in Figure 1b. For all samples, the plateau capacitance  $(C_p)$  attained in the reverse bias (depletion) region is inversely proportional to the nanoporous TiO2 film thickness. An effective medium model provides a good fit to the experimental data, indicating that the TiO<sub>2</sub> film behaves as a pure dielectric in the depletion region and that the internal surface area of the film does not contribute to the capacitance. (In other words, the electric potential drops uniformly across the nanoporous film.) Accounting for the measured porosity of the TiO<sub>2</sub> film and correcting for the dense TiO<sub>2</sub> underlayer, the effective dielectric capacitance may be calculated as

$$C_{\rm p}^{-1} = \left(\frac{\epsilon_0 \epsilon_{\rm eff}}{d_{\rm ncTiO_2}}\right)^{-1} + \left(\frac{\epsilon_0 \epsilon_{\rm TiO_2}}{d_{\rm DLTiO_2}}\right)^{-1} \tag{2}$$

where the first term gives the capacitive contribution from the nanoporous TiO<sub>2</sub> layer (thickness  $d_{ncTiO_2}$ ) and the second term gives the capacitive contribution from the dense TiO2 underlayer (thickness  $d_{DLTiO_2}$ ). In this equation,  $\epsilon_0$  is the permittivity of free space,  $\epsilon_{\rm eff}$  is the effective dielectric constant of the nanoporous  $TiO_2$  film, and  $\epsilon_{TiO_2}$  is the dielectric constant of the dense  $TiO_2$  film.  $\epsilon_{eff}$  accounts for the porosity of the nanoporous TiO2 film through a statistical weighting function that takes into account the relative contributions from  $\epsilon_{TiO_2}$  and  $\epsilon_{\rm air}$  based on the relative volume fractions of the two components. There are several effective medium theories that provide formulas for this statistical weighing function, including the Bruggeman theory,<sup>29</sup> the Maxwell-Garnett theory,<sup>30</sup> and the Landau-Lifshitz/Looyenga model<sup>31,32</sup> (see ref 33 for an excellent discussion of the various effective medium theories). Although the Bruggeman theory is perhaps the most widely used, it is best applied in situations where the ratio of the dielectric constants for the two components is less than 20. Since air has a dielectric constant of 1 and TiO2 has a dielectric constant of  $\sim$ 50, application of the Bruggeman theory proves problematic (fluctuations in the local value of  $\epsilon$  become unacceptably large). Likewise, it is difficult to use Maxwell-Garnett theory, which applies for binary systems in the limit where the volume fraction of one of the materials is small (less than 0.15). The porosity of our nanoporous films is between 56% and 66%, and therefore the volume fractions of both components are greater than 0.15. A third theory, the Landau-Lifshitz/Looyenga model, proves applicable to the nanoporous TiO<sub>2</sub> film. Furthermore, Theiss<sup>34</sup> has shown that the Landau-Lifshitz/Looyenga model is more topologically appropriate for porous materials than either the Bruggeman or Maxwell-Garnett models. For a two-component system consisting of air



**Figure 2.** Inverse depletion capacitance  $(C_p^{-1})$  versus nanoporous  $\text{TiO}_2$  layer thickness for the 9nc and 300nc films. Depletion capacitance decreases with increasing nanoporous  $\text{TiO}_2$  film thickness and can be fit to an effective medium capacitance model (linear fits).

and TiO2, the Landau-Lifshitz/Looyenga model yields

$$\epsilon_{\text{eff}} = \left[ \left( \epsilon_{\text{TiO}_2}^{1/3} - \epsilon_{\text{air}} \right) (1 - \phi) + \epsilon_{\text{air}}^{1/3} \right]^3 \tag{3}$$

where  $\phi$  is the porosity (volume fraction of air),  $\epsilon_{\rm air}$  is the dielectric constant of air,  $(1-\phi)$  is the volume fraction of the nanocrystalline TiO<sub>2</sub> phase, and  $\epsilon_{\rm TiO_2}$  is the dielectric constant of bulk TiO<sub>2</sub>. (Lacking evidence otherwise, we assume that the bulk dielectric constant for TiO<sub>2</sub> is the same for the nanocrystalline and dense phases, although of course it must be modified by the porosity for the case of the nanoporous layer.)

By combining eqs 2 and 3, the experimental capacitance data for both the 9nc and 300nc films can be modeled. Figure 2 provides a comparison between the experimental data and model fit for both sets of films. For the 9nc crystallites, the best model fit is obtained with  $\epsilon_{\text{TiO}_2} = 45$ , while for the 300nc crystallites, the best model fit is obtained with  $\epsilon_{\text{TiO}_2} = 65$ . In both cases,  $\epsilon_{\text{air}}$  is assumed equal to one. Both values fall within the range reported for nanocrystalline anatase TiO<sub>2</sub> and conform to the generally observed trend of decreasing dielectric constant with decreasing crystallite size. <sup>35-38</sup>

As the data in Figure 2 reveal, the much larger internal surface area presented by the 9nc films compared to the 300nc films has no effect on  $C_p$ . The fact that  $C_p^{-1}$  is linearly dependent on film thickness but independent of particle size strongly justifies the effective medium interpretation.

Like the plateau capacitance, the apparent flat-band voltages extracted from the MS plots in Figure 1b also depend on film thickness. The apparent flat-band voltage increases with increasing nanoporous  $\text{TiO}_2$  film thickness. This flat-band voltage offset effect can be modeled by assuming that the nanoporous  $\text{TiO}_2$  film remains in the depleted (dielectric) state even at high voltages, so that band bending first occurs only in the dense  $\text{TiO}_2$  layer. Thus, as the nanoporous  $\text{TiO}_2$  film thickness increases, a correspondingly larger amount of voltage is dropped across this region. For band bending in a single n-type semiconductor layer, the Mott—Schottky equation expresses the linear relationship between  $C^{-2}$  and applied voltage (V):

$$C^{-2} = \frac{2}{\epsilon_0 \epsilon e N_D} \left( V_{\text{fb}} - V - \frac{kT}{e} \right) \tag{4}$$

where e is the electron charge ( $e = 1.6 \times 10^{-19}$  C),  $N_{\rm D}$  is the donor density in the semiconductor (cm<sup>-3</sup>), V is the applied voltage, and  $V_{\rm fb}$  is the flat-band voltage. For a two-layer system, where  $\epsilon$  and  $N_{\rm D}$  may be different for each layer, the Mott–Schottky expression can be modified as<sup>37</sup>

$$C^{-2} = \left(1 - \frac{\epsilon_1 N_{\rm D1}}{\epsilon_2 N_{\rm D2}}\right) \left(\frac{d_1}{\epsilon_0 \epsilon_1}\right)^2 + \frac{2}{\epsilon_0 \epsilon_2 e N_{\rm D2}} (V_{\rm fb} - V) \quad (5)$$

where subscripts 1 and 2 refer to the two layers of the system, respectively, and  $N_{\rm D1} < N_{\rm D2}$ . For the two-layer nanoporous  ${\rm TiO_2}$  + dense  ${\rm TiO_2}$  system, we assign  $\epsilon_1$ ,  $N_{\rm D1}$ , and  $d_1$  to the nanoporous  ${\rm TiO_2}$  film and  $\epsilon_2$  and  $N_{\rm D2}$  to the dense  ${\rm TiO_2}$  film. Again, it is necessary to account for the effect of porosity in the nanoporous region, therefore

$$\epsilon_1 = \left[ \left( \epsilon_{\text{TiO}_2}^{1/3} - \epsilon_{\text{air}} \right) (1 - \phi) + \epsilon_{\text{air}}^{1/3} \right]^3 \tag{6}$$

$$N_{\rm D1} = (1 - \phi)N_{\rm D,ncTiO_2} \tag{7}$$

where  $\epsilon_1$  is calculated by using the Landau—Lifshitz/Looyenga effective medium model, a simple linear rule-of-mixtures model is applied to estimate  $N_{\rm D1}$  (simple porosity volume correction), and  $N_{\rm D,ncTiO_2}$  represents the donor density in the TiO<sub>2</sub> particles.

For the nanoporous film to remain in depletion while band bending occurs in the dense film, the donor density in the nanoporous layer must be much lower than the donor density in the dense layer (in other words,  $N_{\rm D1} \ll N_{\rm D2}$ ). This is reasonable, especially since the porosity of the nanoporous layer will certainly dilute the effective volumetric donor density (as per eq 7). Inserting the condition  $N_{\rm D1} \ll N_{\rm D2}$  into eq 5 yields

$$C^{-2} = \left(\frac{d_1}{\epsilon_0 \epsilon_1}\right)^2 + \frac{2}{\epsilon_0 \epsilon_2 e N_{D2}} (V_{fb} - V) \tag{8}$$

The "apparent" flat-band voltage,  $V_0$ , is obtained when  $C^{-2} = 0$ . Setting eq 8 equal to zero, inserting  $V_0$  for V, and solving for  $V_0$  produces

$$V_{o} = \left(\frac{\epsilon_{o}\epsilon_{2}eN_{D2}}{2}\right)\left(\frac{d_{1}}{\epsilon_{o}\epsilon_{1}}\right)^{2} + V_{fb}$$
 (9)

Thus, the apparent flat-band voltage  $(V_0)$  is offset from the real flat-band voltage  $(V_{\rm fb})$  by an amount that is proportional to the square of the nanoporous  $TiO_2$  layer thickness  $(d_1^2)$ . A quadratic fit to measured values of  $V_{\rm o}$  versus nanoporous TiO<sub>2</sub> layer thickness permits extraction of the real flat-band voltage as well as the donor density in the dense TiO2 layer, as shown in Figure 3. The fits shown in Figure 3 yield  $V_{\rm fb} = 1.7 \text{ V}$  and  $N_{\rm D2} = 2 \times 10^{15} \, {\rm cm}^{-3}$  for the 9nc TiO<sub>2</sub> samples and  $V_{\rm fb} = 1.65$ V and  $N_{\rm D2}=1.65\times 10^{15}~\rm cm^{-3}$  for the 300nc TiO<sub>2</sub> samples. Reassuringly, the values are similar for the two samples, which should be expected since they share the same dense TiO2 underlayer. The calculated donor density is considerably lower than typically observed in electrolyte-filled TiO<sub>2</sub> systems. In TiO<sub>2</sub>/electrolye systems, N<sub>D</sub> for spray-deposited TiO<sub>2</sub> is typically 10<sup>17</sup>-10<sup>19</sup> cm<sup>-3</sup>. <sup>39</sup> The low donor density calculated here may reflect the fact that these tests, which are conducted in air, lead to increased oxygen vacancy passivation compared to electrolytefilled TiO<sub>2</sub> experiments. The low donor density levels may also be a result of the prolonged air-annealing treatment at 450 °C employed after spray deposition.

The slope of the MS ( $C^{-2}$  vs V) plots in the space-charge region provides an independent measure of  $N_{\rm D2}$ . From these slopes, (see Figure 1b) average values of  $N_{\rm D2}=7\times10^{14}$  to  $3\times10^{15}$  cm<sup>-3</sup> are obtained. Although this range brackets the values provided by the model fit, the donor densities calculated from the MS slopes appear to show a systematic increase with decreasing nanoporous TiO<sub>2</sub> layer thickness. The nature of this remarkable relationship has not been investigated any further.

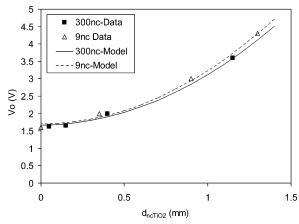


Figure 3. Apparent flat-band voltage  $(V_0)$  versus nanoporous  $TiO_2$ layer thickness for the 9nc and 300nc films. The apparent flat band voltage increases quadratically with the nanoporous TiO2 layer thickness. This behavior can be fit to a two-layer MS model assuming full depletion in the nanoporous TiO2 film (model fits indicated).

One possibility is that our assumption of  $N_{\rm D1} \ll N_{\rm D2}$  may be problematic. If  $N_{D1}$  and  $N_{D2}$  are similar, some mixture of band bending could occur. This may be particularly true for the thinner films, leading to systematic increase in the apparent MS slope with decreasing film thickness.

C. IV Analysis under Illumination. Under illumination, transport behavior changes significantly, as illustrated by the IV curves in Figure 4a. Under AM 1.5 illumination, the absolute magnitude of the current at a given voltage increases by almost a factor of 10 compared to the dark condition. This is a commonly observed effect in nanoporous TiO2 films and is attributed to photodoping of the TiO<sub>2</sub>. <sup>17,18</sup> Of the total AM 1.5 irradiation intensity of 1000 W/m<sup>2</sup>, approximately 5% is within the UV range. UV light with energy greater than the TiO<sub>2</sub> band gap (~3.2 eV) can be absorbed, leading to photogenerated charge carriers and thereby increasing the TiO<sub>2</sub> conductivity.

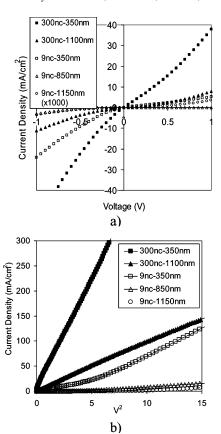
Also, the IV curves now show quasisymmetric rather than diode-like behavior. Diode analysis can no longer be used to interpret the transport behavior. Upon UV illumination the Fermi level splits in quasi-Fermi levels for electrons and holes. The presence of minority carriers (holes) changes the electrical contact with the graphite completely. Two nonblocking (ohmic) contacts are now present and current flow is limited by carrier transport rather than injection across a contact.

The hypothesis of carrier-transport limited current flow is supported by the J vs  $V^2$  analysis of the IV data, as presented in Figure 4b. The linear dependence of J as a function of  $V^2$ indicates that transport can be modeled by a space charge limited current (SCLC) process above a threshold voltage. Figure 5 recaptures the same IV data in log-log format to convey further details on the low-voltage IV dependence. For brevity, only the positive branches of the IV data are shown in Figures 4b and Figure 5; the negative branches show similar behavior.

The electron mobility in the nanoporous  $TiO_2$  ( $\mu_{ncTiO_2}$ ) can be estimated from the SCLC region at high voltage. The standard SCLC model may be applied assuming that the SCLC limitation occurs only within the nanoporous TiO2 layer, and neglecting the voltage loss across the dense TiO2 layer:

$$J = \frac{9}{8} \epsilon_0 \epsilon_{\text{eff}} \mu_{\text{eff}} \frac{V^2}{d_{\text{ncTiO}_2}}$$
 (10)

where  $\epsilon_{\rm eff}$  is defined as per eq 3,  $\mu_{\rm eff} = (1 - \phi)\mu_{\rm ncTiO_2}$ , V =



**Figure 4.** (a) IV curves and (b) the positive branch of the  $I-V^2$  curves, for selected 9nc and 300nc films under AM 1.5 illumination. IV curves under illumination show nearly symmetric response. In a  $V^2$  analysis, SCLC behavior is apparent at high voltages. Fits to a standard SCLC model permit extraction of electron mobility. The current-density values for the 9nc-1150nm IV curve have been amplified by a factor of 1000 for clarity.

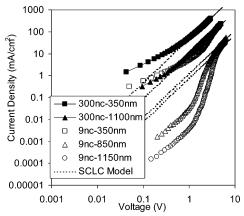


Figure 5. Log-log scale IV curves for selected 9nc and 300nc films under AM 1.5 illumination. The log-log analysis more clearly defines the onset voltage for the space charge limited current dependence. This onset voltage shifts to higher bias for thicker films.

applied voltage (volts), and all other terms are as previously defined. The resulting values of  $\mu_{\text{ncTiO}_2}$  are summarized in Table

The electron mobilities calculated from the SCLC model are roughly the same for both the 9nc and 300nc films and fall within the range reported in other recent experimental investigations.40,22

Observation of Figure 5 reveals that the simple interpretation of ohmic (barrier-free) transport at low voltage transitioning to SCLC transport at high voltage is problematic for the thicker

TABLE 3: SCLC Model Electron Mobility Estimates under AM 1.5 Illumination from the IV Data in Figure 4b

sample	$\mu_{\rm ncTiO_2}$ (cm <sup>2</sup> /Vs)
300nc-350nm 300nc-1100nm	$\begin{array}{c} 3.5 \times 10^{-4} \\ 1.8 \times 10^{-4} \end{array}$
9nc-350nm 9nc-850nm 9nc-1150nm	$\begin{array}{c} 1.7 \times 10^{-4} \\ 2.3 \times 10^{-4} \\ 3.4 \times 10^{-4} \end{array}$

9nc-850nm and 9nc-1150nm films. In these films, most of the UV light is absorbed in the bulk of the TiO<sub>2</sub> nanoporous films, and very little UV light reaches the TiO<sub>2</sub>/graphite interface. (Films are illuminated in a superstrate configuration, therefore the TiO<sub>2</sub>/graphite interface is farthest from the incident light.) In these thicker films, therefore, the Schottky-barrier thermionic emission process is still believed to limit the IV response at low bias (as evidenced by the steep-slope rise to SCLC behavior).

#### IV. Conclusions

MS analysis indicates that the air-filled nanocrystalline TiO<sub>2</sub> films investigated in this contribution are fully depleted over a wide potential window in the dark. This behavior is captured by an effective medium model that averages the properties of the TiO<sub>2</sub> and air regions without taking into account structural features of the composite such as particle size or internal surface area. Depletion capacitance is observed to be insensitive to particle size (i.e., it does not depend on internal surface area), strongly justifying the effective medium interpretation. For thick films and small particle sizes, transport characteristics are increasingly dominated by a large series resistance contribution. This increased resistance could be attributed to trapping effects, to doping effects, or simply to an increase in interparticlejunction "bottlenecks" between TiO2 particles. Dramatic differences in the dark-IV extrapolated resistance of comparable thickness 300nc and 9nc films indicate that the transport physics may be substantially different between these two types of films in the dark. Under illumination, conductivity improves substantially (this is attributed to photodoping) and the IV behavior is dominated by charge transport rather than charge injection. A space charge limited current model provides mobility estimates of  $\sim (1.7-3.5) \times 10^{-4} \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for both the 9 and 300 nm diameter TiO2 particle films under illumination. The close agreement in illuminated-IV extrapolated electron mobility between the 9 and 300 nm diameter TiO2 particles indicates that the transport physics are likely similar in both films when illuminated.

Acknowledgment. This material is based upon work supported by the National Science Foundation under Grant No. 0401817.

#### References and Notes

(1) O'Regan, B.; Grätzel, M. Nature 1991, 353, 737.

- (2) Bach, U.; Lupo, D.; Comte, P.; Moser, J. E.; Weissörtel, F.; Salbeck, J.; Spreitzer, H.; Grätzel, M. Nature 1998, 395, 583.
- (3) Hoffmann, M. R.; Martin, S. T.; Choi, D. W.; Bahnemann, D. W. Chem. Rev. 1995, 65, 69.
- (4) Fujishima, A.; Kohayakawa, K.; Honda, K. J. Electrochem. Soc. 1975, 122, 1487.
- (5) Bechinger, C.; Ferrere, S.; Zaban, A.; Sprague, J.; Gregg, B. A. Nature 1996, 383, 608.
- (6) Topoglidis, E.; Cass, A. E. G.; Gilardi, G.; Sadeghi, S.; Beaumont, N.; Durrant, J. R. Anal. Chem. 1998, 70, 5111.
  - (7) Traversa, E. Sens. Actuators, B 1995, 23 (2-3), 135.
- (8) Eppler, A. M.; Ballard, I. M.; Nelson, J. Phys. E 2002, 14, 197. (9) Kelly, J. J.; Vanmaekelbergh, D. Electrochim. Acta. 1998, 43 (19-20), 2773.
- (10) Zaban, A.; Meier, A.; Gregg, B. A. J. Phys. Chem. B 1997, 101, 7985
- (11) Santiago, F. F.; Belmonte, G. G.; Bisquert, J.; Bogdanoff, P.; Zaban, A. J. Electrochem. Soc. 2003, 150 (6), E293.
- (12) Santiago, F. F.; Belmonte, G. G.; Bisquert, J.; Zaban, A.; Salvador, P. J. Phys. Chem. B 2002, 106, 334.
  - (13) Ruhle, S.; Dittrich, T. J. Phys. Chem. B 2005, 109, 9522.
- (14) Greijer-Angrell, H.; Boschloo, G.; Hagfeldt, A. J. Phys. Chem. B **2004**, 108, 12388.
- (15) Goossens, A.; Van der Zanden, B.; Schoonman, J. J. Chem. Phys. Lett. 2003, 331, 1-6.
  - (16) Boschloo, G.; Hagfeldt, A. J. Phys. Chem. B 2005, 109, 12093.
- (17) Fabregat-Santiago, F.; Bisquert, J.; Garcia-Belmonte, G.; Boschloo, G.; Hagfeldt, A. Sol. Energy Mater. Sol. Cells 2005, 87, 117.
- (18) Wang, Q.; Moser, J. E.; Grätzel, M. J. Phys. Chem. B 2005, 109,
- (19) van de Lagemaat, J.; Park, N. G.; Frank, A. J. J. Phys. Chem. B **2000**, 104, 2044.
- (20) Nelson, J.; Eppler, A. M.; Ballard, I. M. J. Photochem. Photobiol. A 2002, 148, 25.
- (21) Kytin, V. and Dittrich, T. H. Phys. Status Solidi A 2001, 185 (2), 461
  - (22) Konenkamp, R. Phys. Rev. B 2000, 61 (16), 11057.
- (23) Lin, H. M.; Keng, C. H.; Tung, C. Y. Nanostruct. Mater. 1997, 9 (1-8), 747.
- (24) Nanu, M.; Schoonman, J.; Goossens, A. Adv. Mater. (Weinheim, Germany) 2004, 16 (5), 453.
- (25) Nanu, M.; Schoonman, J.; Goossens, A. Nano Lett. 2005, 5 (9),
  - (26) Snaith H. J.; Grätzel, M. Adv. Mater. 2006, 18, 1910.
  - (27) Hegedus, S.; Shafarman W. N. Prog. Photovoltaics 2004, 12, 155.
- (28) O'Hayre, R.; Nanu, M.; Schoonman, J.; Goossens, A.;, Wang, Q.; Gratzel, M. Adv. Funct. Mater. 2006, 16, 1566.
  - (29) Bruggeman, D. A. G. Ann. Phys. (Leipzig) 1935, 24, 636.
- (30) Maxwell Garnett, J. C. Philos. Trans. R. Soc. London, Ser. A 1904, 203, 385.
- (31) Landau, L. D.; Lifshitz, E. M. In Electrodynamics of Continuous Media, 2nd ed.; Butterworth-Heinenann: Oxford, UK, 1984; p 42.
  - (32) Looyenga, H. Physica (Amsterdam) 1965, 31, 401.
  - (33) Spanier, J. E.; Herman, I. P. Phys. Rev. B 2000, 61 (15), 10437.
  - (34) Theiss, W. Adv. Solid State Phys. 1994, 33, 149.
- (35) Es-Souni, M.; Oja, I.; Krunks, M. J. Mater. Sci.: Mater. Electron. 2004, 15 (6), 341.
- (36) Garcia-Belmonte, G.; Kytin, V.; Dittrich, T. H.; et al. J. Appl. Phys. **2003**, 94 (8), 5261.
- (37) Van der Krol, R.; Goossens, A.; Schoonman, J. J. Electrochem. Soc. 1997, 144 (5), 1723.
- (38) Mo, C. M.; Zhang, L. D.; Wang, G. Z. Nanostruct. Mater. 1995, 6(5-8.), 823.
- (39) Cameron, P. J.; Peter, L. M. J. Phys. Chem. B 2003, 107 (51),
- (40) Kytin, V.; Dittrich, T. H.; Bisquert, J.; Lebedev, E. A.; Koch, F. Phys. Rev. B 2003, 68, 195308.