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# Lattice Dynamics of $\beta$ - $\text{V}_2\text{O}_5$ : Raman Spectroscopic Insight into the Atomistic Structure of a High-Pressure Vanadium Pentoxide Polymorph

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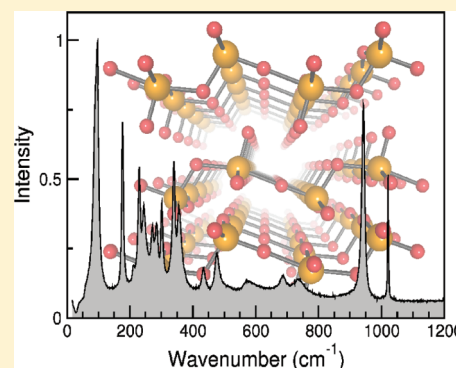
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**ABSTRACT:** We report here the Raman spectrum and lattice dynamics study of a well-crystallized  $\beta$ - $\text{V}_2\text{O}_5$  material prepared via a high-temperature/high-pressure (HT/HP) route, using  $\alpha$ - $\text{V}_2\text{O}_5$  as the precursor. Periodic quantum-chemical density functional theory calculations show good agreement with the experimental results and allow one to assign the observed spectral features to specific vibrational modes in the  $\beta$ - $\text{V}_2\text{O}_5$  polymorph. Key structure–spectrum relationships are extracted from comparative analysis of the vibrational states of the  $\beta$ - $\text{V}_2\text{O}_5$  and  $\alpha$ - $\text{V}_2\text{O}_5$  structures, and spectral patterns specific to the basic units of the two  $\text{V}_2\text{O}_5$  phases are proposed for the first time. Such results open the way for the use of Raman spectroscopy for the structural characterization of vanadium oxide-based host lattices of interest in the field of lithium batteries and help us to greatly understand the atomistic mechanism involved in the  $\alpha$ -to- $\beta$  phase transition of vanadium pentoxide.



## 1. INTRODUCTION

Pentavalent vanadium-based frameworks attract much attention because of their outstanding structural flexibility and their chemical and physical properties suitable for catalytic and electrochemical applications.<sup>1–3</sup> The ambient-pressure form of vanadium pentoxide ( $\alpha$ - $\text{V}_2\text{O}_5$ ) has a layered structure with orthorhombic symmetry (space group  $Pmmn$ ) consisting of  $\text{VO}_5$  square pyramids sharing edges and corners.<sup>4</sup> The structure is well adapted to the reversible incorporation of guest  $\text{Li}^+$  ions, and since the 1970s, the  $\alpha$ - $\text{V}_2\text{O}_5$  polymorph is recognized as an attractive material for applications in electrochromic thin film devices and as a cathode in lithium batteries because of its high energy density and retention capacity upon cycling.<sup>5–11</sup> The valence state of V atoms is known to be extremely sensitive to the chemical environment, and such chemical versatility may lead to a variety of structures containing different building units and exhibiting tunable physical properties. In this regard, high-pressure/high-temperature (HP/HT) synthesis routes are promising ways to obtain novel  $\text{V}_2\text{O}_5$  polymorphs, particularly for potential electrochemical applications.

The first HP modification of  $\text{V}_2\text{O}_5$  (prepared at  $P = 4\text{--}6$  GPa and  $T = 650$  °C) was reported by Suzuki et al.<sup>12</sup> Later, Volkov et al.<sup>13</sup> reproduced the same HP phase of  $\text{V}_2\text{O}_5$ , named the  $\beta$  phase. Making use of the results of quenching experiments at 600 °C and between 3.5 and 9 GPa, Volkov et al.<sup>13</sup> determined by X-ray diffraction (XRD) measurements that the structure of the  $\beta$  phase is tetragonal. In situ Raman spectroscopic experiments by Grzechnik<sup>14</sup> performed in the pressure range 7–10 GPa and at room temperature (RT) revealed qualitative changes in the Raman spectrum of the  $\text{V}_2\text{O}_5$  sample, especially in the V–O stretching region. The author concluded that a new phase appeared and coexisted with the  $\alpha$ - $\text{V}_2\text{O}_5$  starting material; the phase was found to return to the starting orthorhombic material upon pressure release. A few years later, Loa et al.<sup>15</sup> performed similar RT experiments by employing synchrotron radiation for detecting structural changes. The authors observed a pronounced structural disorder under

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elevated pressure and suggested that the correct determination of the new phase necessitates the simultaneous application of HT and HP.

In 2001, two different groups<sup>16,17</sup> published their findings on the  $V_2O_5$  phases investigated at HT/HP, and both reported the existence of the  $\beta$ - $V_2O_5$  phase with orthorhombic symmetry. Filonenko and Zibrov<sup>16</sup> performed quenching experiments and found the  $\beta$  phase up to 7.5 GPa/900 °C, which returns to the  $\alpha$  phase at atmospheric pressure and a temperature of 400 °C. Kusaba et al.<sup>17</sup> showed the presence of the  $\beta$  phase at 6 GPa/500 °C from quenching experiments and at 4.5 GPa/350 °C from in situ experiments. Later, Filonenko et al.<sup>18</sup> reexamined the  $\beta$  phase of  $V_2O_5$  using XRD, neutron diffraction, and high-resolution transmission electron microscopy experiments and found the structure to be monoclinic. The authors established that the  $\beta$ - $V_2O_5$  structure is built up of infinite chains made of quadruple units of edge-sharing  $VO_6$  octahedra along the  $b$  axis. The chains are linked by sharing corners of two octahedra along the  $c$  axis, which leads to a  $V_4O_{10}$ -layered composition, with the layers parallel to the (100) plane. Weak interactions, similar to those in  $MoO_3$ , hold the layers together. Preliminary electrochemical experiments showed that this new monoclinic  $\beta$ - $V_2O_5$  polymorph behaves as a reversible lithium intercalation compound delivering a specific capacity of 250 mAh/g at a C/3.5 rate.<sup>19</sup> More recently, the  $V_2O_5$  phase diagram was revisited in a wide  $P$ – $T$  range (pressures up to 29 GPa and temperatures up to 1500 °C), providing two HP/HT modifications of  $V_2O_5$  ( $\beta$ - and  $\delta$ - $V_2O_5$ ) having well-defined stability ranges in the phase diagram.<sup>20</sup>

Structural distinctions between the  $\alpha$ - and  $\beta$ - $V_2O_5$  polymorphs must become apparent in their vibrational spectra, and the Raman spectroscopy provides a fast, reliable, and nondestructive means of studying these differences. Furthermore, Raman spectroscopy turned out to be a very efficient tool to follow the structural changes under operation conditions for a wide range of transition-metal oxides used as electrode materials for lithium batteries.<sup>26</sup> The Raman spectra of  $\alpha$ - $V_2O_5$  were thoroughly studied both experimentally<sup>21–23</sup> and theoretically.<sup>22,24,25</sup> In addition, Raman studies of the  $\alpha$ - $V_2O_5$ /Li system as a pure thin film and as a composite powder electrode were carried out<sup>27–30</sup> and were recently extended to the  $\beta$ - $Na_{0.33}V_2O_5$ /Li system.<sup>31</sup>

On the other hand, much less attention was paid to the  $\beta$ - $V_2O_5$  structure. Up to now, the in situ recorded Raman spectrum at ambient temperatures reported in ref 14 was the only reliable experimental information on vibrational states of  $\beta$ - $V_2O_5$ . However, Raman peaks in this spectrum are markedly large because of strong inhomogeneous broadening due to size/strain effects of pressure gradients in the cells.<sup>15</sup> In the present work, the thermal annealing under pressure is expected to yield a grain coarsening and well-crystallized  $\beta$ - $V_2O_5$  with a low level of remaining stress, which results in a better quality spectrum.

The Raman spectra measured by Balog et al.<sup>20</sup> on postquench samples retrieved from HP/HT experiments did not show any marked distinction from the spectra of the starting  $\alpha$ - $V_2O_5$  material, although the presence of HP/HT phases was inferred from the XRD experiments. Density functional theory (DFT) calculations confirmed the stability of the  $\beta$  structure<sup>32</sup> and provided a theoretical Raman spectrum<sup>33</sup> of the material that generally agrees with the experimental spectra reported in ref 14. These calculations also ascertained the symmetry assignment of the observed Raman peaks, but the

atomistic pattern of the vibrational modes was not presented, and as a consequence, no structure–spectrum relationship was proposed.

This paper reports the results of a combined experimental and computational study of the  $\beta$ - $V_2O_5$  polymorph. A well-crystallized  $\beta$ - $V_2O_5$  sample was prepared at HT/HP conditions, and its structure was completely characterized by XRD measurements. A high-quality Raman spectrum of the sample was obtained, and DFT calculations allowed one to assign all of the observed spectral peaks to the vibrational modes of the structure. A comparison of the  $\beta$ - $V_2O_5$  and  $\alpha$ - $V_2O_5$  vibrational states is provided and leads to the clear identification of spectral features related to the presence of specific structural basic units in the two  $V_2O_5$  polymorphs.

## 2. EXPERIMENTS AND COMPUTATIONS

**2.1. Experimental Part.** A commercial (Aldrich)  $\alpha$  polymorph of  $V_2O_5$  was subjected to 8 GPa pressure and a temperature of 800 °C for 1 h in a belt-type press. After the pressure and temperature were applied for 1 h, the vessel was quenched to RT while pressure was slowly released. Starting and resulting samples were examined by scanning electron microscopy (SEM) on a JEOL 6400 microscope equipped with an EDAX Inc. energy-dispersive X-ray detector for microanalysis.

The resulting sample was also examined by XRD performed with a Bruker D8 high-resolution powder X-ray diffractometer equipped with an MBraun PSD-S0 M position-sensitive detector. Monochromatic  $Cu\ K\alpha_1$  ( $\lambda = 1.5406$  Å) radiation obtained with a germanium primary monochromator was used. The treatment of the diffraction data was carried out using the *FullProf* program.<sup>34</sup> The structure of the  $\beta$ - $V_2O_5$  phase reported in ref 18 was employed as a starting model; isotropic thermal parameters and constraints in V–O distances were used to keep the number of the parameter low and to ensure stability of the fitting procedure.

The Raman spectra were measured with a LaBRAM HR 800 (Jobin–Yvon–Horiba) Raman microspectrometer including edge filters and equipped with a back-illuminated charge-coupled device detector (Spex CCD) cooled by the Peltier effect to 200 K. A He:Ne laser (632.8 nm wavelength) was used as the excitation source. The spectra were registered in the backscattering geometry with a spectral resolution of  $0.5\text{ cm}^{-1}$ . A 100 $\times$  objective was used to focus the laser beam to a spot of  $1\text{ }\mu\text{m}^2$  size on the sample surface. To avoid local heating of the sample, the power of the laser beam was adjusted to 0.2–0.5 mW with neutral filters of various optical densities.

**2.2. Computational Details.** The vibrational states of the two  $V_2O_5$  polymorphs were computed with the CASTEP program<sup>35</sup> using density functional perturbation theory (DFPT).<sup>36</sup> The calculations were carried out within the local density approximation (LDA) to DFT and employed Troullier–Martins norm-conserving pseudopotentials.<sup>37</sup> The plane-wave energy cutoff of 35 Ha was used, and the Brillouin zone integration was done over a  $2 \times 4 \times 2$  grid of points chosen according to the Monkhorst–Pack scheme in the irreducible part of the Brillouin zone. The positions of atoms in the unit cell were optimized with the lattice parameters fixed at their experimental values prior to calculation of the vibrational spectral characteristics. This option was favored over complete geometry optimization because a test calculation of the  $\alpha$ - $V_2O_5$  structure with optimization of both the atomic positions and the lattice parameters, in particular, resulted in a value of the  $c$  parameter that was by 14% too small compared to its experimental value. This finding is in a line with that of Zhou and He<sup>25</sup> and is explained by the fact that the LDA fails to correctly describe weak interactions responsible for long V–O contacts (ca. 2.7 Å) between the layers in the structure. A recent computational study by Londero and Schröder<sup>38</sup> showed that dispersion-corrected exchange–correlation functionals need to be used to mimic the interplane spacing in the  $\alpha$  polymorph of vanadium pentoxide.

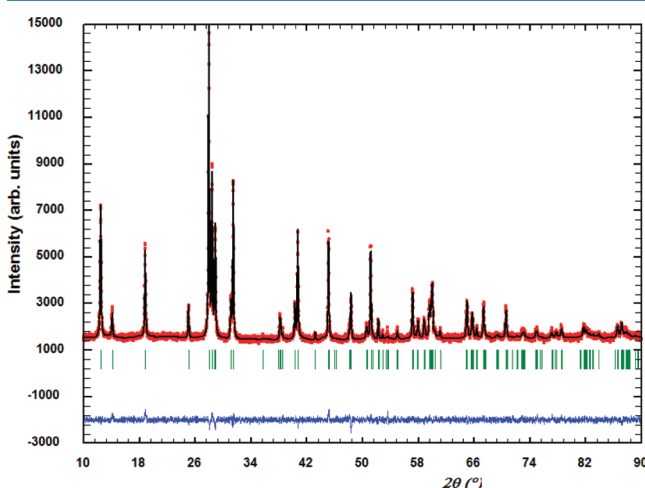
The Raman activity of the vibrational modes was computed within DFPT as described in ref 39. To obtain the Raman scattering

intensities, the Raman activities of the vibrational modes were multiplied by Bose–Einstein factors corresponding to the experimental conditions (temperature and wavelength of exciting radiation).

### 3. RESULTS AND DISCUSSION

**3.1. Structure.** SEM examination of commercial  $\alpha$ -V<sub>2</sub>O<sub>5</sub> shows that it consists of large aggregates of particles with a wide distribution in size (up to 50  $\mu$ m). The HT/HP treatment yields a  $\beta$ -V<sub>2</sub>O<sub>5</sub> sample with much smaller aggregates of particles not exceeding 10  $\mu$ m. We have checked the resulting sample's composition by energy-dispersive spectrometry by analyzing up to 15 particles. The V/O ratio was equal to 2:5 within the experimental error, which confirms the stoichiometric nature of HP-V<sub>2</sub>O<sub>5</sub>. Furthermore, the sample was verified to be single phase because all of the particles showed the same composition.

The XRD pattern of the quenched sample is shown in Figure 1. All of the diffraction peaks can be assigned to the monoclinic



**Figure 1.** Profile refinement of the XRD pattern corresponding to a sample prepared at a pressure of 8 GPa and a temperature of 1073 K for 1 h in a belt-type press. Red circles: observed pattern. Black line: calculated pattern. Blue line: difference between observed and calculated. The Bragg peaks are indicated by vertical bars.

unit cell previously proposed for the HP form of V<sub>2</sub>O<sub>5</sub>.<sup>18,32</sup> The final unit cell parameters (space group  $P2_1/m$ ) are  $a = 7.1016(3)$  Å,  $b = 3.5668(1)$  Å,  $c = 6.2742(3)$  Å, and  $\beta = 90.121(3)^\circ$ , and these values are in very good agreement with those determined in previous studies.<sup>18,32</sup>

The microstructural features of the sample were determined by the two-step procedure proposed by Langford.<sup>40</sup> We found

an average isotropic crystallite diameter of 374(5) Å and a low level of remaining stress. Thus, the prepared  $\beta$ -V<sub>2</sub>O<sub>5</sub> is a well-crystallized and ordered material with low strain effects (for comparison see, for instance, ref 41).

Table 1 compares the fractional coordinates of atoms in the unit cell of the  $\beta$ -V<sub>2</sub>O<sub>5</sub> structure obtained in the present study with those given in ref 18 and with the coordinates of atoms optimized in the DFT calculations. The agreement with the literature data is good, and the differences between the two experimental sets of coordinates are explained by the fact that XRD measurements performed in the present work are less precise, especially in locating light O atoms, than the experimental data reported by Filonenko et al.<sup>18</sup> using neutron diffraction. Nevertheless, the results of XRD measurements unambiguously point to the fact that the prepared HP/HT sample is indeed the  $\beta$  phase of vanadium pentoxide. Given the above arguments, the following discussion of the structure  $\beta$ -V<sub>2</sub>O<sub>5</sub> makes use of the structural data reported in ref 18.

It is common to consider the structure of V<sub>2</sub>O<sub>5</sub> polymorphs as an arrangement of VO<sub>x</sub> polyhedra. Such a representation of the  $\alpha$ -V<sub>2</sub>O<sub>5</sub> structure built of VO<sub>5</sub> polyhedra is shown in Figure 2a. A similar view of the  $\beta$ -V<sub>2</sub>O<sub>5</sub> structure in which the V atoms are considered 6-fold-coordinated is given in Figure 2b. In both structures, the VO<sub>x</sub> polyhedra share their edges and corners, thus forming layers that are stacked along the  $z$  direction and are held together by relatively weak interactions. This structure representation, however, is not fully justified from the crystal chemistry viewpoint because it considers V–O contacts longer than 2 Å as valence bonds.

On the other hand, if considering only contacts with lengths of less than 2 Å as “true” bonds, one can highlight the similarities and differences in the arrangement of structural entities in the crystal lattices of the two V<sub>2</sub>O<sub>5</sub> polymorphs. Such a representation of the  $\alpha$ - and  $\beta$ -V<sub>2</sub>O<sub>5</sub> structures is displayed in Figure 3.

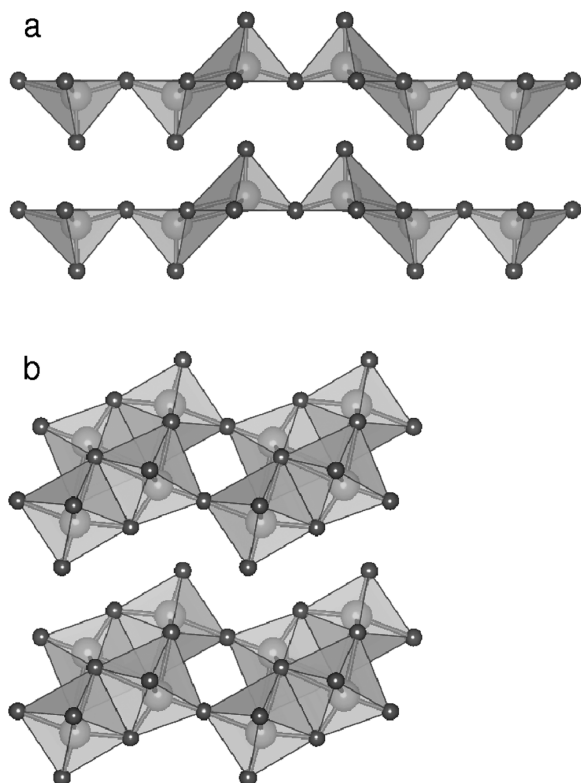
One sees that both structures are built of [V<sub>2</sub>O<sub>5</sub>] units. Three types of V–O bonds with lengths of less than 2 Å can be identified in the units (Table 2): vanadyl V–O<sub>1</sub> bonds ( $d_1$ ), V–O<sub>3</sub> bonds ( $d_2$ ) forming V–O<sub>3</sub>–V bridges in the  $xz$  planes, and V–O<sub>2</sub> bonds ( $d_3$ ) forming V–O<sub>2</sub>–V bridges oriented along the  $y$  direction. The arrangement of the [V<sub>2</sub>O<sub>5</sub>] units via the  $d_3$  bonds results in [V<sub>2</sub>O<sub>5</sub>]<sub>∞</sub> chains running in the  $y$  direction, and the chains are interconnected by V–O<sub>2</sub> contacts ( $d_4$ ) longer than 2 Å, which are shown in Figure 3a by dashed lines. As the point symmetry changes from  $D_{2h}$  in  $\alpha$ -V<sub>2</sub>O<sub>5</sub> to  $C_{2h}$  in  $\beta$ -V<sub>2</sub>O<sub>5</sub>, the crystallographic sites of V, O<sub>1</sub>, and O<sub>2</sub> atoms split into two nonequivalent groups distinguished by subscripts a and b in Figure 3b,c. In  $\beta$ -V<sub>2</sub>O<sub>5</sub>, V<sub>a</sub>–O<sub>2b</sub> and V<sub>b</sub>–O<sub>2a</sub> contacts link the chains of two V<sub>2</sub>O<sub>5</sub> layers in the  $z$  direction (cf. the dashed lines

**Table 1.** Fractional Coordinates of Atoms in the Unit Cell of the  $\beta$ -V<sub>2</sub>O<sub>5</sub> Structure<sup>a</sup>

	expt, ref 18			expt, present work			DFT, present work		
	$x/a$	$y/b$	$z/c$	$x/a$	$y/b$	$z/c$	$x/a$	$y/b$	$z/c$
V <sub>a</sub>	0.2773	0.25	0.2557	0.2852	0.25	0.2566	0.2823	0.25	0.2619
V <sub>b</sub>	0.0998	0.25	0.8103	0.1035	0.25	0.8070	0.0980	0.25	0.8064
O <sub>1a</sub>	0.4914	0.25	0.3248	0.4943	0.25	0.3280	0.5004	0.25	0.3245
O <sub>1b</sub>	0.8241	0.75	0.4374	0.8043	0.75	0.4429	0.8255	0.75	0.4450
O <sub>2a</sub>	0.1992	0.75	0.2627	0.1910	0.75	0.2521	0.1926	0.75	0.2578
O <sub>2b</sub>	0.9693	0.25	0.1464	0.9686	0.25	0.1548	0.9708	0.25	0.1409
O <sub>3</sub>	0.3012	0.25	0.9576	0.3100	0.25	0.9349	0.3014	0.25	0.9631

<sup>a</sup> $R_p = 3.64$ ,  $R_{wp} = 4.48$ ,  $R_{exp} = 2.38$ ,  $\chi^2 = 3.55$ , and Bragg  $R$  factor = 3.61.





**Figure 2.** Polyhedral views in the  $xz$  projection of  $\alpha$ - $V_2O_5$  (a) and  $\beta$ - $V_2O_5$  (b) structures.

in Figure 3b). Furthermore, half of the vanadyl  $d_1$  bonds in the  $\beta$ - $V_2O_5$  structure lose their terminal character and transform into highly asymmetric  $V_a-O_{1b}-V_b$  bridges. The long  $V_a-O_{1b}$  contacts shown in Figure 3b,c by dotted lines connect the chains in the  $x$  direction. In addition, the  $V_a-O_3-V_b$  bridges become asymmetric.

This structural information provides an indispensable basis for the interpretation of the vibrational spectroscopic pattern of the  $V_2O_5$  polymorphs.

**3.2. Raman Spectra.** Both of the  $\alpha$ - and  $\beta$ - $V_2O_5$  crystal structures contain two formula units per unit cell. According to the group symmetry analysis, 21 Raman-active phonon modes of the  $\alpha$ - and  $\beta$ - $V_2O_5$  polymorphs are distributed over the irreducible symmetry representations as follows:

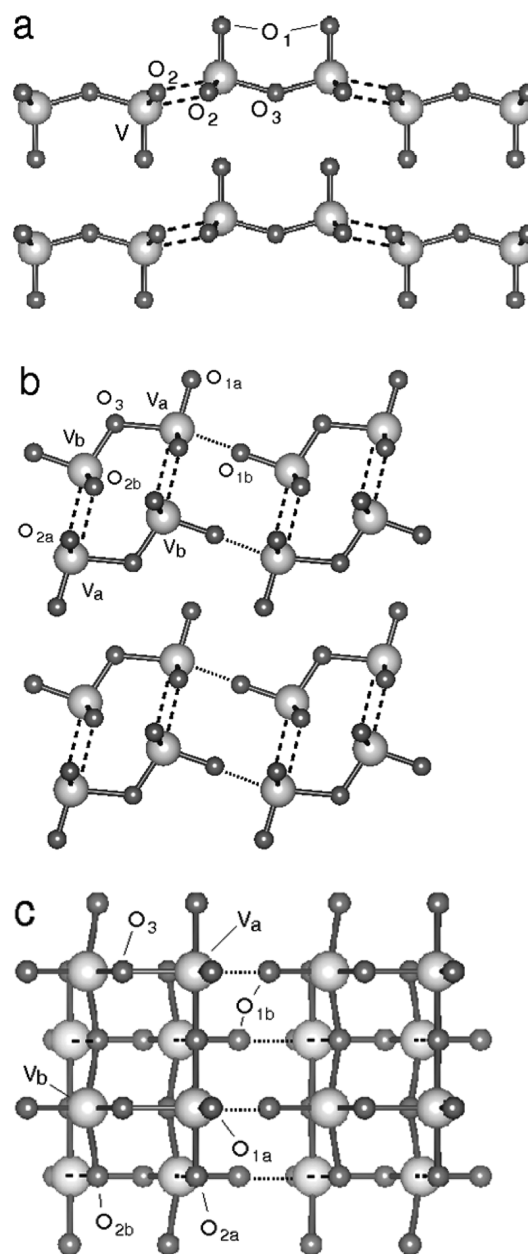
$$\alpha\text{-}V_2O_5(D_{2h}): \Gamma_{\text{Raman}} = 7A_g + 7B_{2g} + 3B_{1g} + 4B_{3g}$$

$$\beta\text{-}V_2O_5(C_{2h}): \Gamma_{\text{Raman}} = 14A_g + 7B_g$$

For the  $\alpha$ - $V_2O_5$  structure, vibrational modes involving atomic displacements in the  $xz$  plane belong to  $A_g$  and  $B_{2g}$  species, and the modes combine into the  $A_g$  representation in the  $\beta$ - $V_2O_5$  lattice. Similar symmetry distribution is valid for the out-of-plane vibrations with  $y$  displacements, which belong to  $B_{1g}$  and  $B_{3g}$  species in  $\alpha$ - $V_2O_5$  and merge into the  $B_g$  representation in  $\beta$ - $V_2O_5$ .

The experimental Raman spectrum of the  $\beta$ - $V_2O_5$  sample is shown in Figure 4a, while Figure 4b presents the Raman spectrum of the  $\alpha$ - $V_2O_5$  material.

The Raman spectrum of  $\beta$ - $V_2O_5$  exhibits a series of well-resolved peaks, many of which have not been observed previously in the in situ RT/HP experiments<sup>14</sup> and have become evident in the present work. This is related to the



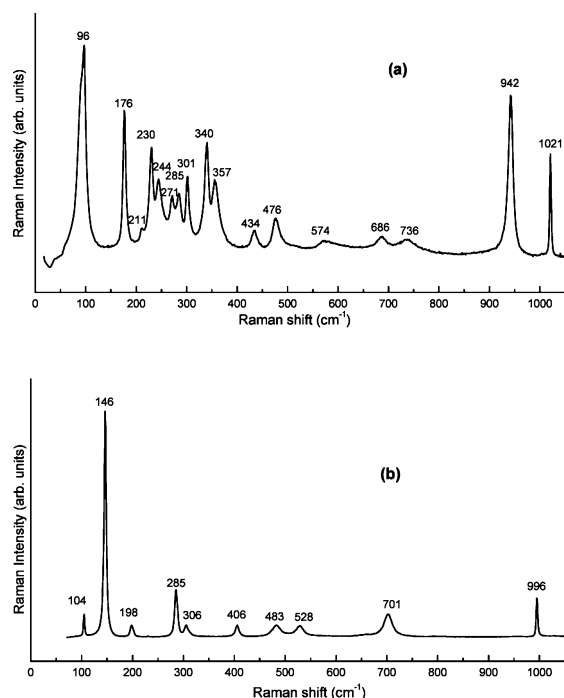
**Figure 3.** Views of the  $\alpha$ - $V_2O_5$  (a) and  $\beta$ - $V_2O_5$  (b and c) structures with contacts longer than 2 Å shown as dashed and dotted lines (see the text for details). Images a and b are in the  $xz$  projection. Image c is in the  $xy$  projection.

**Table 2.** Characteristic Interatomic Distances (in Å) in  $\alpha$ - and  $\beta$ - $V_2O_5$  According to the Experimental Data Reported in References 4 and 18

$\alpha$ -V <sub>2</sub> O <sub>5</sub> <sup>4</sup>			$\beta$ -V <sub>2</sub> O <sub>5</sub> <sup>18</sup>			
d <sub>1</sub>	V–O <sub>1</sub>	1.586	V <sub>a</sub> –O <sub>1a</sub>	1.583	V <sub>b</sub> –O <sub>1b</sub>	1.649
d <sub>2</sub>	V–O <sub>3</sub>	1.780	V <sub>a</sub> –O <sub>3</sub>	1.881	V <sub>b</sub> –O <sub>3</sub>	1.705
d <sub>3</sub>	V–O <sub>2</sub>	1.878	V <sub>a</sub> –O <sub>2a</sub>	1.871	V <sub>b</sub> –O <sub>2b</sub>	1.872
d <sub>4</sub>	V–O <sub>2</sub>	2.021	V <sub>a</sub> –O <sub>2b</sub>	2.296	V <sub>b</sub> –O <sub>2a</sub>	2.176

microstructure of the sample because thermal annealing under pressure led to a well-crystallized  $\beta$ - $V_2O_5$  sample with a low level of remaining stress.

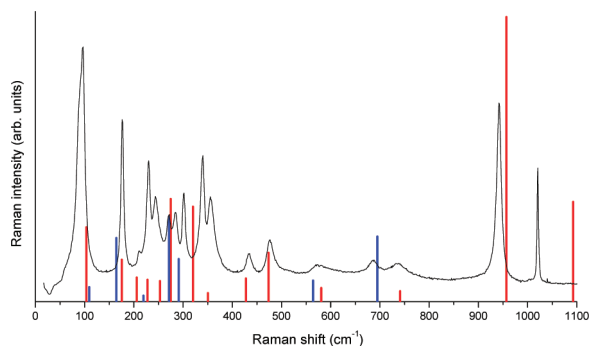
The following features can be observed:



**Figure 4.** Raman spectra: (a)  $\beta$ - $V_2O_5$  sample prepared at a pressure of 8 GPa and a temperature of 1073 K for 1 h in a belt-type press; (b)  $\alpha$ - $V_2O_5$  precursor.

- (i) Two intense and sharp peaks in the high-frequency region at 942 and 1021  $\text{cm}^{-1}$ ,
- (ii) Two large peaks located at 686 and 736  $\text{cm}^{-1}$ ,
- (iii) A large peak with a maximum at 574  $\text{cm}^{-1}$  and a wide shoulder reaching 620  $\text{cm}^{-1}$  from the high-frequency side,
- (iv) Two peaks at 434 and 476  $\text{cm}^{-1}$ ; note that only one peak at ca. 450  $\text{cm}^{-1}$  was observed in ref 14.
- (v) A number of well-resolved peaks below 400  $\text{cm}^{-1}$  with the most intense features at 96, 176, 230, 244, 271, 285, 301, 340, and 357  $\text{cm}^{-1}$ . Note that only ill-defined bands with an intense peak at ca. 80  $\text{cm}^{-1}$  were observed in this region in ref 14.

The calculated spectrum of  $\beta$ - $V_2O_5$  is shown in Figure 5, where it is compared with the experimental one. The spectrum



**Figure 5.** Experimental (black) and computed (color bars) Raman spectra of the  $\beta$ - $V_2O_5$  sample. Red and blue bars stand for the  $A_g$  and  $B_g$  vibrational modes, respectively.

well agrees with the theoretical spectrum reported in ref 33.

Table 3 compares the positions of the peaks in the experimental

**Table 3.** Experimental and Calculated Frequencies and Maximum Atomic Amplitudes of Raman-Active Phonon Modes of the  $\beta$ - $V_2O_5$  Structure

frequency		symmetry	max atomic amplitudes <sup>a</sup>		
expt	calcd		x	y	z
96	103.5	$A_g$	$L_1-L_2$		
96	109.3	$B_g$		$V_a-V_b$	
176	164.7	$B_g$		$L_1-L_2$	
176	175.4	$A_g$	$O_3$		$V_a$
211	205.6	$A_g$	$O_{1a}$		
211	219.8	$A_g$		$O_{1a}$	
230	227.6	$B_g$			$L_1-L_2$
244	252.9	$A_g$			$O_{1b}$
271	271.8	$B_g$		$O_3$	
285	274.9	$A_g$	$O_{2a}, O_{2b}$		
301	291.3	$B_g$		$O_{1b}$	
340	320.4	$A_g$			$O_{2b}$
357	350.2	$A_g$	$O_{2a}$		$O_{1b}$
434	427.7	$A_g$	$O_{2b}$		
476	473.4	$A_g$			$O_{2a}, O_{2b}$
574	581.0	$A_g$	$O_3$		
574	564.2	$B_g$		$O_{2a}, O_{2b}$	
686	695.2	$B_g$		$O_{2a}, O_{2b}$	
736	741.3	$A_g$			$O_3$
942	957.0	$A_g$	$O_{1b}$		
1021	1092.5	$A_g$		$O_{1a}$	

<sup>a</sup> $L_1$  and  $L_2$  denote translations of neighboring layers.

and computed spectra and proposes the assignment of observed Raman peaks to specific vibrational modes, based on the results of the calculations. One can notice a systematic overestimation of the computed vibrational frequencies in the region above 500  $\text{cm}^{-1}$ , which is inherent to the level of theory used. One can also observe that the intensities of some peaks in the low-frequency part of the spectrum are not well reproduced. Nevertheless, a good general correspondence between the spectra allows interpretation of the measured spectral pattern.

Now we turn to assignment of the most prominent spectral features. It is instructive to begin with the  $\alpha$  phase of the vanadium pentoxide structure. This consideration will facilitate the subsequent interpretation of the spectral pattern of the more complicated  $\beta$  polymorph. Taking into account the structural data collected in Table 2, one can expect to find four lines in the high-wavenumber region of the Raman spectrum of  $\alpha$ - $V_2O_5$  that correspond to four different bond stretching modes ( $\nu$ ) with frequency relationships

$$\nu(d_4) < \nu(d_3) < \nu(d_2) < \nu(d_1)$$

Furthermore, the  $O_2$  and  $O_3$  atoms are located in symmetric V–O–V bridges and, therefore, the  $\nu(d_2)$  and  $\nu(d_3)$  modes split into symmetric (s) and antisymmetric (as) components. Only  $\nu_{as}(\text{V–O–V})$  modes are genuine bond-stretching modes because the  $\nu_s(\text{V–O–V})$  modes are coupled with the  $\delta(\text{V–O–V})$  bending modes and thus have markedly lower frequencies. Consequently, one can detail the above relationship as follows:

$$\nu_s(d_2) < \nu_s(d_3) < \nu(d_4) < \nu_{as}(d_3) < \nu_{as}(d_2) < \nu(d_1)$$

The experimental Raman spectrum of  $\alpha$ - $V_2O_5$  (Figure 4b) has four Raman peaks at 996, 701, 528, and 482  $\text{cm}^{-1}$ , which were assigned to the  $\nu(d_1)$ ,  $\nu_{as}(d_3)$ ,  $\nu(d_4)$ , and  $\nu_s(d_2)$  modes, respectively<sup>24,25,28</sup> (Table 4). The missing  $\nu_{as}(d_2)$  mode is not

Table 4. Frequencies and Assignments of High-Frequency Raman-Active Phonon Modes of the  $\alpha$ -V<sub>2</sub>O<sub>5</sub> and  $\beta$ -V<sub>2</sub>O<sub>5</sub> Structures

$\alpha$ -V <sub>2</sub> O <sub>5</sub>		$\beta$ -V <sub>2</sub> O <sub>5</sub>			
		max atomic amplitudes			assignment
expt frequency	assignment <sup>24,25,28</sup>	expt frequency	x	y	
528	$\nu(d_4)$	476			$\nu_s(V_b-O_{2a})$
483	$\nu_s(d_2)$	574	O <sub>3</sub>		$\nu(V_a-O_3)$
		574		O <sub>2a</sub> , O <sub>2b</sub>	$\nu_{as}(V_b-O_{2b}-V_b)$
701	$\nu_{as}(d_3)$	686		O <sub>2a</sub> , O <sub>2b</sub>	$\nu_{as}(V_a-O_{2a}-V_a)$
	$\nu_{as}(d_2)$	736			$\nu(V_b-O_3)$
996	$\nu(d_1)$	942	O <sub>1b</sub>		$\nu(V_b-O_{1b})$
		1021			$\nu(V_a-O_{1a})$

observed because of its low intensity. This feature is related to the structural peculiarity of the  $\alpha$ -V<sub>2</sub>O<sub>5</sub> structure, where the V–O<sub>3</sub>–V bridges are almost linear (cf. Figure 3a) and the  $\nu_{as}(d_2)$  mode, being formally Raman-active, has very low Raman activity because of a compensation effect. A theoretical prediction of the frequency of this quasi-silent mode based on a force-field model gave a value of 848 cm<sup>−1</sup>;<sup>22</sup> recent DFT calculations predicted higher values of 936<sup>24</sup> or 1010 cm<sup>−1</sup>.<sup>25</sup> Regardless the exact value of the  $\nu_{as}(d_2)$  wavenumber, one sees that the Raman features in the high-frequency part of the spectrum of the  $\alpha$ -V<sub>2</sub>O<sub>5</sub> structure can be assigned to the variation of specific structural elements with the use of structural information and common spectroscopic wisdom. It is noteworthy that such an analysis for the low-frequency part of the spectrum is much more difficult because the vibrational modes with frequencies in this region contain important contributions of angle-bending coordinates and involve the dynamics of larger structural entities.

Now we turn to the discussion of the vibrational states of  $\beta$ -V<sub>2</sub>O<sub>5</sub>. The differences between the  $\alpha$ - and  $\beta$ -V<sub>2</sub>O<sub>5</sub> structures discussed above are obviously expected to manifest themselves in the vibrational spectra, and given the above structural information, one can await the following changes in the spectrum of the  $\beta$ -V<sub>2</sub>O<sub>5</sub> structure compared with that of the  $\alpha$ -V<sub>2</sub>O<sub>5</sub> polymorph:

- Because half of the V–O<sub>1</sub> bonds lose their terminal character, a new peak related to the  $\nu(V_b-O_{1b})$  vibration has to appear at a lower frequency.
- Because of the asymmetry of the V–O<sub>3</sub>–V bridges in the  $\beta$  phase, the  $\nu_s(V-O_3-V)$  and  $\nu_{as}(V-O_3-V)$  modes have to be replaced by the  $\nu(V_a-O_3)$  and  $\nu(V_b-O_3)$  modes.
- Two B<sub>g</sub> modes related to  $\nu_{as}(V-O_2-V)$  vibrations must split into  $\nu_{as}(V_a-O_{2a}-V_a)$  and  $\nu_{as}(V_b-O_{2b}-V_b)$  modes.

Analysis of the experimental Raman spectrum of  $\beta$ -V<sub>2</sub>O<sub>5</sub> in Figure 4a and of the peak assignments given in Table 4 shows that the observed spectral pattern of the HP phase of vanadium pentoxide indeed follows these expectations:

- The spectrum of the  $\beta$  phase has two lines at 942 and 1021 cm<sup>−1</sup> assigned to the  $\nu(V_b-O_{1b})$  and  $\nu(V_a-O_{1a})$  modes, respectively, instead of one line at 996 cm<sup>−1</sup> corresponding to the  $\nu(d_1)$  mode in the spectrum of the  $\alpha$  phase.
- The  $\nu_{as}(d_2)$  and  $\nu_s(d_2)$  modes inherent to the vibrations of the bridging O<sub>3</sub> atoms in the  $\alpha$  phase become the  $\nu(V_b-O_3)$  and  $\nu(V_a-O_3)$  modes in the  $\beta$  structure. The former gives rise to the Raman line at 736 cm<sup>−1</sup>, while the latter contributes to the wide spectral feature centered at 574 cm<sup>−1</sup>.

- The Raman line at 700 cm<sup>−1</sup> due to the  $\nu_{as}(d_3)$  mode in the  $\alpha$  phase splits into two Raman lines in the  $\beta$  phase: the first one,  $\nu_{as}(V_a-O_{2a}-V_a)$ , is related to the line at 686 cm<sup>−1</sup>, and the second one,  $\nu_{as}(V_b-O_{2b}-V_b)$ , contributes to the signal at 574 cm<sup>−1</sup>.
- The Raman line at 528 cm<sup>−1</sup> corresponding to the  $\nu(d_4)$  mode in the spectrum of  $\alpha$ -V<sub>2</sub>O<sub>5</sub> undergoes a downward shift to 476 cm<sup>−1</sup> in the  $\beta$  phase. This line can now be attributed to the  $\nu(V_b-O_{2a})$  mode because the V<sub>a</sub>–O<sub>2b</sub> contacts are too long (~2.3 Å) to give rise to a characteristic normal vibration. A signal due to variation of the latter contacts is hidden in a host of low-frequency modes.

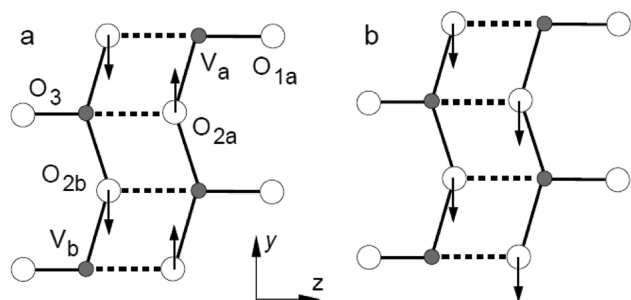
The above results allow us to propose fingerprints permitting identification of the  $\alpha$ - and  $\beta$ -V<sub>2</sub>O<sub>5</sub> polymorphs with the help of Raman spectroscopy:

- Raman lines around 900 cm<sup>−1</sup> correspond to the stretching vibrations of vanadyl V=O bonds. A number of such lines indicate the number of nonequivalent vanadyl bonds. It is one for the  $\alpha$  phase and two for the  $\beta$  phase.
- The appearance of two Raman peaks at 736 and 686 cm<sup>−1</sup> is characteristic of the  $\beta$ -V<sub>2</sub>O<sub>5</sub> polymorph. The peak at 736 cm<sup>−1</sup> points to the presence of the asymmetric V–O<sub>3</sub>–V bridge in the  $\beta$ -V<sub>2</sub>O<sub>5</sub> structure. In the  $\alpha$  phase, the vibrations localized within the symmetric and quasi-linear V–O<sub>3</sub>–V bridge manifest themselves as one single  $\nu_s(d_2)$  mode located at 482 cm<sup>−1</sup>, whereas in the  $\beta$  phase, the change of the bridge geometry leads to the appearance of two Raman-active modes at 736 and 574 cm<sup>−1</sup>.

The second fingerprint peak at 686 cm<sup>−1</sup> corresponds to a  $\nu_{as}(V_a-O_2-V_a)$  mode of B<sub>g</sub> symmetry, while the other  $\nu_{as}(V_b-O_2-V_b)$  B<sub>g</sub> mode contributes to the Raman signal at 574 cm<sup>−1</sup>. The origin of such a large frequency splitting between the two B<sub>g</sub> modes is worth a special comment because similar  $\nu_{as}(V-O_2-V)$  modes of B<sub>1g</sub> and B<sub>3g</sub> symmetry in the  $\alpha$ -V<sub>2</sub>O<sub>5</sub> structure have almost equal frequencies of 700 cm<sup>−1</sup>. The 110 cm<sup>−1</sup> splitting between the B<sub>g</sub> modes in the  $\beta$  structure cannot be explained by the difference in the lengths of the V<sub>a</sub>–O<sub>2a</sub> and V<sub>b</sub>–O<sub>2b</sub> bonds, which are equal to 1.871 and 1.872 Å, respectively. Furthermore, both modes involve equal contributions of the  $\nu_{as}(V_a-O_{2a}-V_a)$  and  $\nu_{as}(V_b-O_{2b}-V_b)$  oscillations.

The splitting can readily be understood by considering the structure of the  $\beta$ -V<sub>2</sub>O<sub>5</sub> phase and the displacement of atoms in the two modes. The structure of the vanadium oxide polymorph is characterized by short

$O_{2a} \cdots O_{2b}$  contacts of 2.52 and 2.49 Å in the experimental data and DFT calculations, respectively. Therefore, one might expect a strong influence of O–O interactions on the frequencies of modes with large vibrational amplitudes of the O atoms. Parts a and b of Figure 6



**Figure 6.** Displacements of O atoms in the two  $B_g$  modes with calculated frequencies of  $695\text{ cm}^{-1}$  (a) and  $564\text{ cm}^{-1}$  (b) of the  $\beta$ - $V_2O_5$  structure. O and V atoms are shown by white and gray circles, respectively. V–O contacts longer than 2 Å are shown by dashed lines.

show atomic displacements of atoms in the  $B_g$  modes experimentally observed at  $686$  and  $574\text{ cm}^{-1}$ , respectively. One sees that the high-frequency mode involves displacements of  $O_2$  atoms in the opposite direction, whereas the atoms move in the same direction in the low-frequency mode. Therefore, the  $O_{2a} \cdots O_{2b}$  contacts change their length in the first mode, while they remain unchanged in the second one, and it is just this repulsive O–O interaction that accounts for the  $110\text{ cm}^{-1}$  splitting of the vibrational frequencies. It is noteworthy that a similar effect accounts for the features in the Raman spectrum of zircon.<sup>42</sup>

In the case of the  $\alpha$ - $V_2O_5$  structure, the two  $\nu_{as}(V-O_2-V)$  modes include antiparallel displacements of  $O_2$  atoms similar to those depicted in Figure 6a, and the frequencies of these two modes almost coincide.

- Finally, the origin of the large spectral band observed in the  $\beta$  phase at around  $600\text{ cm}^{-1}$  also merits special consideration. This band has a maximum at  $574\text{ cm}^{-1}$  and a wide high-frequency shoulder reaching  $620\text{ cm}^{-1}$ . Note that there are no Raman-active modes within this frequency interval in  $\alpha$ - $V_2O_5$ . Thus, this spectral feature could also serve as a fingerprint of the  $\beta$  structure. According to our calculations, there are two modes of different symmetry and of almost equal Raman activity within this frequency region: the  $A_g$  mode assigned to the  $\nu(V_a-O_3)$  vibration and the  $B_g$   $\nu_{as}(V_b-O_{2b}-V_b)$  mode with the atomic displacements shown in Figure 6b. The marked difference in the frequencies of these modes in our calculations ( $A_g$ ,  $581\text{ cm}^{-1}$ ;  $B_g$ ,  $564\text{ cm}^{-1}$ ) can explain the large width of the observed spectral band. Note that the results of ref 33 gave a much smaller frequency difference between these modes ( $A_g$ ,  $611\text{ cm}^{-1}$ ;  $B_g$ ,  $613\text{ cm}^{-1}$ ).

#### 4. CONCLUSIONS

A well-crystallized sample of the  $\beta$ - $V_2O_5$  polymorph obtained from the  $\alpha$ - $V_2O_5$  precursor via the HT/HP route was characterized by XRD, SEM, and Raman spectroscopy. A high-quality Raman spectrum is reported with new and well-resolved features, which definitely completes the previous

Raman pattern of the  $\beta$  phase of vanadium pentoxide;<sup>14</sup> these experimental data are complemented by periodic quantum-chemical DFT calculations. A good agreement between observed and computed Raman spectra was demonstrated, and the combination of theoretical and experimental techniques provides valuable information, permitting a reliable assignment of all observed spectral features. Comparative analysis of the Raman spectra and phonon states of the  $\beta$ - $V_2O_5$  phase with those of the parent  $\alpha$ - $V_2O_5$  structure has allowed us to identify for the first time spectral fingerprints specific to structural basic units of the two  $V_2O_5$  polymorphs. The established structure–spectrum correlations are expected to promote the use of Raman spectroscopy for characterization of more complex  $\beta$ - $V_2O_5$ -based structures such as  $\beta$ - $Na_{0.33}V_2O_5$  bronze used as a positive-electrode material in lithium batteries.<sup>31</sup>

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##### Notes

The authors declare no competing financial interest.

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#### REFERENCES

- (1) Livage, J. *Chem. Mater.* **1991**, *3*, 578.
- (2) Chernova, N. A.; Roppolo, M.; Dillon, A. C.; Whittingham, M. S. *J. Mater. Chem.* **2009**, *19*, 2526.
- (3) Liu, Z.; Fang, G.; Wang, Y.; Bai, Y.; Yao, K.-L. *J. Appl. Phys. D: Appl. Phys.* **2000**, *33*, 2327.
- (4) Enjalbert, R.; Galy, J. *Acta Crystallogr.* **1986**, *C42*, 1467.
- (5) Whittingham, M. S. *Chem. Rev.* **2004**, *104*, 4271.
- (6) Murphy, D. W.; Christian, P. A.; Disalvo, F. J.; Waszczak, J. V. *Inorg. Chem.* **1979**, *18*, 2800.
- (7) Whittingham, M. S. *J. Electrochem. Soc.* **1976**, *126*, 315.
- (8) Wiesener, K.; Schneider, W.; Ilic, D.; Steger, E.; Hallmeir, K. H.; Brackmann, E. *J. Power Sources* **1978**, *20*, 157.
- (9) Delmas, C.; Cognac-Auradou, H.; Cocciantelli, J. M.; Ménétrier, M.; Doumerc, J. P. *Solid State Ionics* **1994**, *69*, 257.
- (10) Bates, J. B.; Gruzalski, G. R.; Dudney, N. J.; Luck, C. F.; Xiaohua, Y. *Solid State Ionics* **1994**, *70/71*, 619.
- (11) Cocciantelli, J. M.; Doumerc, J. P.; Pouchard, M.; Broussely, M.; Labat, J. *J. Power Sources* **1991**, *34*, 103.
- (12) Suzuki, T.; Saito, S.; Arakawa, W. *J. Non-Cryst. Solids* **1977**, *24*, 355.
- (13) Volkov, V. L.; Golovkin, V. G.; Fedyukov, A. S.; Zaynulin, Y. G. *Inorg. Mater.* **1988**, *24*, 1568. Translated from: *Izv. Akad. Nauk USSR Neorg. Mater.* **1988**, *24*, 1836.
- (14) Grzechnik, A. *Chem. Mater.* **1998**, *10*, 2505.
- (15) Loa, I.; Grzechnik, A.; Schwarz, U.; Syassen, K.; Hanfland, M.; Kremer, R. *J. Alloys Compd.* **2001**, *317/318*, 103.
- (16) Filonenko, V. P.; Zibrov, I. P. *Inorg. Mater.* **2001**, *37*, 953.
- (17) Kusaba, K.; Ohshima, E.; Syono, Y.; Kikegawa, T. *J. Cryst. Growth* **2001**, *229*, 467.
- (18) Filonenko, V. P.; Sundberg, M.; Werner, P.-E.; Zibrov, I. P. *Acta Crystallogr.* **2004**, *B60*, 375.
- (19) Arroyo-de Dompablo, M. E.; Gallardo-Amores, J. M.; Amador, U.; Moran, E. *Electrochem. Commun.* **2007**, *9*, 1305.



- (20) Balog, P.; Orosel, D.; Cancarevic, Z.; Schon, C.; Jansen, M. *J. Alloys Compd.* **2007**, 429, 87.
- (21) Clauws, P.; Vennik, J. *Phys. Status Solidi B* **1976**, 76, 707.
- (22) Abello, L.; Husson, E.; Repelin, Y.; Lucazeau, G. *Spectrochim. Acta* **1983**, 39, 641.
- (23) Clauws, P.; Broeckx, J.; Vennik, J. *Phys. Status Solidi B* **1985**, 131, 459.
- (24) Brazdova, V.; Ganduglia-Pirovano, M. V.; Sauer, J. *Phys. Rev. B* **2004**, 69, 165420.
- (25) Zhou, B.; He, D. *J. Raman Spectrosc.* **2008**, 39, 1475.
- (26) Baddour-Hadjean, R.; Pereira-Ramos, J. P. *Chem. Rev.* **2010**, 110, 1278.
- (27) Baddour-Hadjean, R.; Rackelboom, E.; Pereira-Ramos, J. P. *Chem. Mater.* **2006**, 18, 3548.
- (28) Baddour-Hadjean, R.; Pereira-Ramos, J. P.; Navone, C.; Smirnov, M. *Chem. Mater.* **2008**, 20, 1916.
- (29) Baddour-Hadjean, R.; Navone, C.; Pereira-Ramos, J. P. *Electrochim. Acta* **2009**, 54, 6674.
- (30) Baddour-Hadjean, R.; Marzouk, A.; Pereira-Ramos, J. P. *J. Raman Spectrosc.* **2011**, DOI: 10.1002/jrs.2984.
- (31) Baddour-Hadjean, R.; Bach, S.; Emery, N.; Pereira-Ramos, J. P. *J. Mater. Chem.* **2011**, 21, 11296.
- (32) Gallardo-Amores, J. M.; Biskup, N.; Amador, U.; Persson, K.; Ceder, G.; Moran, E.; Arroyo-de Dompablo, M. E. *Chem. Mater.* **2007**, 19, 5262.
- (33) Zhou, B.; Su, Q.; He, D. *Chin. Phys. B* **2009**, 18, 4988.
- (34) FullProf: Rodriguez-Carjaval, J. Satellite Meeting on Powder Diffraction of the XY Congress of the IUCr, Toulouse, France, 1990.
- (35) Clark, S. J.; Segall, M. D.; Pickard, C. J.; Hasnip, P. J.; Probert, M. J.; Refson, K.; Payne, M. C. *Z. Kristallogr.* **2005**, 220, 567.
- (36) Refson, K.; Clark, S. J.; Tulip, P. R. *Phys. Rev. B* **2006**, 73, 155114.
- (37) Troullier, N.; Martins, J. L. *Phys. Rev. B* **1991**, 43, 1993.
- (38) Londero, E.; Schröder, E. *Comput. Phys. Commun.* **2011**, 182, 1805.
- (39) Porezag, D.; Pederson, M. R. *Phys. Rev. B* **1996**, 54, 7830.
- (40) Langford, J. I. NIST Special Publication 846. Proceedings of the International Conference on Accuracy in Powder Diffraction II, Gaithersburg, MD, 1992.
- (41) Fuentes, A. F.; Boulahya, K.; Maczka, M.; Hanuza, J.; Amador, U. *Solid State Sci.* **2005**, 7, 343.
- (42) Lazarev, A. N., Mirgorodsky, A. P., Mazhenov, H. A. In *Vibrations of Oxide Lattices*; Lazarev, A., Ed.; Nauka Publishers: Leningrad, Russia, 1980; pp 72–99.