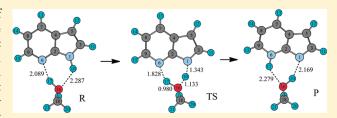


# Solvent Effects in the Excited-State Tautomerization of 7-Azaindole: A Theoretical Study

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**ABSTRACT:** The solvent effect often changes the mechanism of a chemical reaction. Experimental studies of the excited-state tautomerization of 7-azaindole (7AI) suggested that the intrinsic reactions occur via the concerted triple and double proton transfer mechanisms in the gas and liquid phases, respectively. Theoretical study is required to understand how the solvent effect changes the mechanism; however, such studies have rarely been performed in the excited-state. In this study, systematic



quantum mechanical calculations were performed to study the excited-state tautomerization of 7AI in methanol. Electronic structures and energies for the reactant, transition state, and product were computed at the complete active space self-consistent field levels with the second-order multireference perturbation theory (MRPT2) to consider the dynamic electron correlation. The IEFPCM and SM8 methods were used to include solvent effect in the excited and ground-state calculations, respectively. The excited-state double proton transfer (ESDPT) in 7AI-CH<sub>3</sub>OH and the triple proton transfer (ESTPT) in 7AI-(CH<sub>3</sub>OH)<sub>2</sub> both occur via a concerted but asynchronous mechanism. The ESTPT barrier was smaller than the activation energy of solvent reorganization; however, the amount of 7AI-(CH<sub>3</sub>OH)<sub>2</sub> in methanol is very small because the complex formation is entropically very unfavorable. Therefore, the ESTPT is not an important path. The MRPT2 barrier of ESDPT was 2.8 kcal/mol, which agrees very well with the experimental value. The MRPT2 barrier of deuterium (D) transfer is larger than the activation energy of solvent reorganization; therefore, the intrinsic D transfer is rate-limiting, while the proton transfer must compete with solvent reorganization. The time-dependent density functional theory (TDDFT) was also used for comparison. Most TDDFT methods used in this study failed to predict transition state structures or barriers of the excited-state tautomerization. Additionally, the TDDFT levels failed to predict correct dipole moments in the excited-state, which produced an unreliable solvent effect on barrier heights.

# 1. INTRODUCTION

Proton and hydrogen-atom transfer is of key importance to the redox (oxidation-reduction) reactions in many chemical and biological processes, to the proton transport via membranespanning proteins, and to the proton relay system in enzymes. In particular, prototropic tautomerisms of DNA base-pairs have attracted much interest for many years 1-5 since they are related to UV-induced gene mutation. However, it is difficult to monitor the proton transfer in real DNA base pairs because of their conformational complexities and poor spectroscopic properties. Therefore, 7-azaindole (7AI) is utilized as a model compound to mimic the DNA base pair, and the proton transfer in 7AI dimers has been extensively studied. 7AI contains a hydrogen bond donor site (N-H) and an acceptor site (=N-) and displays simple hydrogen-bonding structures upon dimerization and complexation with water and/or alcohols. Proton transfer in the cyclic hydrogen-bonded complexes of amphoteric aromatic molecules with water and/or alcohol, such as 7AI or 7-hydroxyquinoline (7HQ), has also been studied extensively  $^{6-16}$ since it can mimic the proton relay system in enzymes and proton transport in membranes. $^{17-20}$  Consequently, a detailed understanding of the multiple proton transfer mechanism at the molecular level might provide insight into these complicated chemical and biological processes.<sup>21,2</sup>

A large number of proton transfer reactions in hydrogenbonded complexes of 7AI with water have been studied in the gas phase as well as in the condensed phase.<sup>23–28</sup> The multipleproton transfer in 7AI complexes bound to alcohol in the gas phase and in solution was thoroughly studied in order to reveal the proton transfer dynamics in complicated molecular systems such as enzymes and proteins. The ESDPT of a 7AI-CH<sub>3</sub>OH complex was observed in the condensed phase, and a two-step model for the tautomerization was proposed.<sup>29</sup> In this model, the photoexcited 7AI-CH<sub>3</sub>OH undergoes solvent reorganization into the optimal precursor by forming a cyclic hydrogen-bonded complex followed by intrinsic double proton transfer. This model is widely accepted as the mechanism of the excited-state double proton transfer (ESDPT) in 7AI-alcohol complexes in the condensed phase and is also valid for 7HQ-alcohol complexes. The ESDPT of 7AI-CH<sub>3</sub>OH in methanol solution was very fast; its time constant was 124 ps at 293 K at an Arrhenius activation energy of 2.32 kJ/mol.<sup>29</sup> This activation energy is quite close to the viscosity activation energies of bulk methanol. Moog and Maronchlli<sup>29</sup> pointed out that the large-amplitude solvent motion is

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important in the formation of the cyclic conformer; however, such motion could not be entirely rate-limiting because if it were, no kinetic isotope effect (KIE) would be observed. However, the experimental KIE was  $\sim 3.^{29}$  Those authors also observed that proton transfer rate depends more on the hydrogen-bond donating ability of the solvent than it does on solvent viscosity, and the KIE decreases as the temperature decreases, which support the multistep mechanism of the excited-state tautomerization where no single step is entirely rate-limiting.

Chen et al.<sup>30</sup> reported that two protons were involved in the excited-state tautomerization of 7AI in methanol solution based on the proton inventory experiments showing the linear plot of  $\left(k_{\rm n}/k_{\rm 0}\right)^{1/2}$  vs n, where  $k_{\rm 0}$  and  $k_{\rm n}$  are tautomerization rate constants in methanol and in a mixture of protiated and deuterated methanol with mole fraction n in  $CH_3OD$ , respectively. They also proposed a concerted mechanism for the intrinsic proton transfer step based on the analysis of the rule of geometric mean in KIEs. One of the underlying assumptions in these experiments is that the intrinsic proton (and deuterium) transfer step is ratelimiting, and the force constants of all protons in-flight during the concerted reaction are the same at the transition state (TS). However, this assumption fails when the intrinsic proton transfer step is not rate-limiting or when the multiproton transfer is highly asynchronous so that the force constants of protons in-flight are not the same at the TS.

Very recently, Sekiya et. al<sup>9,10</sup> have studied the excited-state proton transfer of 7AI-(CH<sub>3</sub>OH)<sub>n</sub> (n=1-3) in the gas phase. However, no evidence of tautomer formation has been obtained for 7AI-(CH<sub>3</sub>OH)<sub>n</sub> (n=1,3), except for 7AI-(CH<sub>3</sub>OH)<sub>2</sub>, which could be attributed to a tautomerization rate too slow to be observed in the visible fluorescence spectrum. In the condensed phase, however, the ESDPT was reported to occur only in 7AI-CH<sub>3</sub>OH as described above.<sup>30</sup> Although the excited-state triple proton transfer (ESTPT) in 7AI-(CH<sub>3</sub>OH)<sub>2</sub> occurs in solution, no KIE would be observed if the solvent reorganization is rate-limiting; therefore, it would be difficult to obtain such experimental evidence. Thus, a systematic theoretical study is required to rationalize these results as very few theoretical studies have been performed for the excited-state tautomerization of 7AI in methanol solution.

In the present article, we report high level quantum mechanical data on the tautomerization of the 7AI-CH3OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> complexes in bulk methanol. The structures and energetics of the reactants, TS, and products were calculated and compared with the experimental results. The complete active space self-consistent field (CASSCF) methods were applied to calculate the structures and energies of the 7AI-methanol complexes. The CASSCF energies were corrected by considering the dynamics electron correlation. The time-dependent density functional theory (TDDFT) has recently been successfully used to study excited-states for many systems; however, most of the studies were focused on the spectroscopic properties. To understand the kinetics and mechanisms of a reaction in the excitedstate, detailed information about structures, energies, and vibrational frequencies of reactants and transition states are essential. The TDDFT calculations for excited-state reaction barriers have rarely been performed, particularly for the condensed phase. Thus, there is great interest in determining which functionals are most successful for studying excited-state reactions. In this study, five TDDFT methods, which contained hybrid functional, longrange correction (LC), and empirical dispersion functionals, were used to systematically investigate the excited-state tautomerization reactions in solution.

#### 2. COMPUTATIONAL DETAILS

Reactant, product, and TS geometries of the excited state proton transfer reaction in the 7AI-(CH<sub>3</sub>OH)<sub>n</sub> (n=1,2) complexes were fully optimized at the TDDFT and CASSCF level with 6-31G(d,p), 6-311G(d,p), and 6-311+G(d,p) basis sets using the Gaussian09 program. At the CASSCF level, the active space, which is an essential component of the calculation, includes four  $\pi$  bonds, four corresponding antibonding orbitals, and one nitrogen lone pair, resulting in an active space of 10 electrons in 9 orbitals, which was denoted as CASSCF(10,9). Vibrational frequencies were also calculated using a similar procedure. Single-point energy calculations were performed using the second-order multireference perturbation theory (MRPT2) for stationary points. All MRPT2 calculations were performed using the GAMESS program. <sup>32</sup>

Analytic TDDFT gradients were calculated using the variational TDDFT formulation of Furche and Ahlrichs.<sup>33</sup> Several different exchange-correlation DFT potentials were used in the systems, including Becke's three-parameter Lee-Yang-Parr hybrid functionals (B3LYP),<sup>34</sup> Handy and co-workers' longrange corrected version of B3LYP using the Coulomb-attenuating method (CAM-B3LYP),<sup>35</sup> long-range-corrected version of BLYP (LC-BLYP),<sup>36</sup> hybrid functional of Truhlar and Zhao (M06-2X),<sup>37</sup> and the latest functional from Head-Gordon and co-workers, which included empirical dispersion (WB97XD).<sup>36</sup> The polarizable continuum model calculations were performed using the integral equation formalism (IEFPCM)<sup>38-40</sup> at the TDDFT and CASSCF levels to investigate the mechanism of tautomerization in methanol for the excited state. In the IEFPCM calculations, all hydrogen atoms have their individual spheres, and the atomic radii from the UFF force field were scaled by 1.1. The geometries of the reactant, product, and TS were completely optimized in solution. Currently, the solvent effect is not implemented in the MRPT2 calculations. Therefore, the gas phase MRPT2 energies and the solvation energies at the CASSCF level were used to estimate the MRPT2 energies in methanol.

Geometries of the reactants in the 7AI- $(CH_3OH)_n$  (n=1,2) complexes in the ground state were also optimized with the M06-2X density functional<sup>37</sup> and the 6-31+G(d, p) basis set both in the gas phase and in solution. The solvation effect was predicted using the SM8 model.<sup>41</sup> The SM8 calculations require partial atomic charges, which were obtained using the CM4M charge model. These calculations for solvent effect were carried out using the locally modified Gaussian03<sup>42</sup> suite of electronic structure programs.<sup>43,44</sup> The basis set superposition error (BSSE) was corrected for the complex formation energies using the Boys and Bernardi counterpoise correction scheme.<sup>45</sup> We assumed that the BSSE in the gas phase would be the same as that in solution. In the free energy of solvation, a standard state correction of 1.89 kcal/mol at 298 K was included for transfer from an ideal gas of 1 atm to an ideal solution at a liquid phase concentration of 1 mol L<sup>-1</sup>.

#### 3. RESULTS AND DISCUSSION

**3.1.** Ground-State 7AI-(CH<sub>3</sub>OH)<sub>n</sub> (n = 1, 2) Complexes in Solution. The excited-state protropic tautomerization for 7AI in bulk solvents  $^{6,29,46-48}$  implies that solvation plays a key role in the proton transfer process. The excited-state tautomerization of 7AI in alcohols has been discussed as a two-step process. The first step involves solvent reorganization to form a cyclic

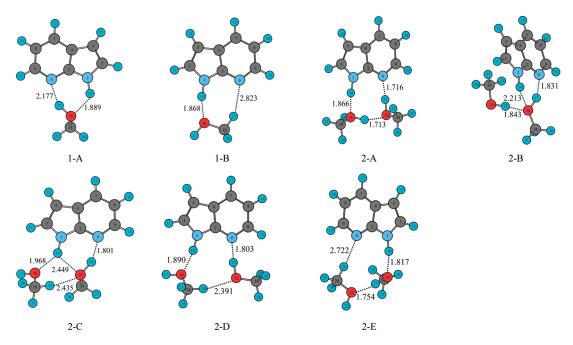


Figure 1. Ground-state H-bonded complexes in the  $7AI-(CH_3OH)_n$  (n = 1, 2) complex in methanol optimized at the M06-2X/SM8/6-31+ G(d,p) level.

hydrogen-bonded 7AI-alcohol complex, while the second step is an intrinsic proton transfer.

If the solvent motion was rate-limiting, no significant kinetic isotope effect (KIE) would be expected. However, KIEs for excited-state tautomerization have been observed in 7AI complexes with various alcohols, and Moogs et al.<sup>29</sup> suggested that both solvent reorganization and the intrinsic proton transfer step could determine the reaction rate. Since the ESDPT is very fast, the hydrogen-bonded complexes, either cyclic or noncyclic, should be present in solution before the excitation. Therefore, it is necessary to investigate what kind of hydrogen-bonded complex is most likely to be formed in solution. We used the M06-2X method for the liquid-phase calculations, which has been successfully used to reproduce the structures and energies of hydrogen-bonded complexes 37,49,50 as well as the solvation energies using the SM8 model with class IV charges. 51 The MP2/ 6-311+G(d,p) level using the IEFPCM was also used for comparison.

Several ground-state conformers of 7AI- $(CH_3OH)_n$  (n = 1, 2) complexes were optimized at the M06-2X/6-31+G(d,p) and MP2/6-311+G(d,p) levels in the gas phase and in methanol, and M06-2X structures in methanol are shown in Figure 1. For 7AI- $CH_3OH$ , two stable hydrogen-bonded complexes were obtained both in the gas phase and in solution: one with cyclic H-bonds and the other with a single H-bond between the N-H group of 7AI and O in methanol and a weak H-bond between a methyl proton and the pyridinum N of 7AI. The former and later are denoted as 1-A and 1-B, respectively, in the figure. We could not find the 1-B structure without the weak H-bond even in methanol solution. We also tried to find a stable structure with a single

H-bond between OH and the pyridinum N of 7AI; however, no such structure was found because all calculations led to the cyclic 1-A structure shown in Figure 1. For 7AI-(CH<sub>3</sub>OH)<sub>2</sub>, there are many possible conformers with cyclic or noncyclic H-bonds. Among them, five of the most energy stable complexes, which were denoted as 2-A—2-E, are depicted in Figure 1: 2-A has an eight-membered cyclic H-bonded structure; 2-B has a six-membered cyclic H-bonded structure (similar to 1-A) with an additional H-bond donating CH<sub>3</sub>OH; 2-C has one CH<sub>3</sub>OH forming an H-bond from the N—H of 7AI and the other CH<sub>3</sub>OH forms a cyclic H-bond similar to that in 1-A; 2-D has two CH<sub>3</sub>OH molecules (with a weak H-bond between them), one donating an H-bond to N and the other accepting a bond from the N—H of 7AI; 2-E has one CH<sub>3</sub>OH forming an H-bond with the N—H of 7AI and the other forming a bond with CH<sub>3</sub>OH.

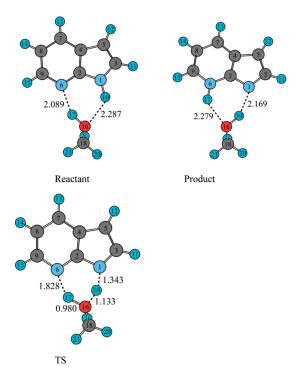
The formation energies of the above conformers in the gas phase and in solution are listed in Table 1. The formation enthalpies ( $\Delta H_{\rm HB}$ ) of 1-B at 0 K are 3.0 and 1.6 kcal/mol higher than those of 1-A at the M06-2X/6-31+G(d,p) level in the gas phase and in methanol, respectively. At the MP2 level, the difference in the  $\Delta H_{\rm HB}$  value between 1-A and 1-B is 2.8 and 1.3 kcal/mol in the gas phase and in methanol, respectively. These results indicate that 1-A is energetically more stable than 1-B both in the gas phase and in solution. Among the five conformers of  $7AI-(CH_3OH)_2$ , 2-A is energetically most stable both in the gas phase and in solution, and this structure has been confirmed by observing the IR-UV ion-dip spectrum. 52 For the cyclic 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> conformers (1-A and 2-A), the  $\Delta H_{\rm HB}$  values at the M06-2X/6-31+G(d,p) level are -9.8 and -20.2 kcal/mol, respectively, in the gas phase, and -3.82 and -9.48 kcal/mol, respectively, in methanol. These results indicate that the latter is energetically more favorable both in the gas phase and in solution.

The predicted formation enthalpies ( $\Delta H_{HB}$ ) and free energies ( $\Delta G$ ) in solution at the two different levels of M06-2X/SM8/6-31+G(d,p) and MP2/IEFPCM/6-311+G(d,p) agree quite well

Table 1. Ground-State Formation Energies (kcal/mol) of Various  $7AI-(CH_3OH)_n$  (n = 1,2) Complexes in the Gas Phase and in Methanol <sup>a</sup>

		M06-2X/6-31+G(d,p)		MP2/6-311+G(d,p)				
	$\Delta E_{ m HB}$	$\Delta H_{ m HB}(0~{ m K})$	$\Delta G(298 \text{ K})$	$\Delta E_{ m HB}$	$\Delta H_{\mathrm{HB}}(0\ \mathrm{K})$	$\Delta G(298 \text{ K})$		
1-A	-11.4 (-5.63)	-9.76 (-3.82)	-0.12 (3.86)	-10.2 (-5.50)	-8.45 (-4.08)	1.16 (3.27)		
1-B	-7.65 (-4.22)	-6.65(-2.25)	1.60 (5.02)	-6.89(-3.80)	-5.62(-2.83)	3.56 (3.88)		
2-A	-23.0 (-13.4)	-20.2 (-9.46)	-2.30(6.54)	-20.2 (-12.2)	-16.8 (-9.18)	2.46 (6.22)		
2-B	$-19.1\ (-10.3)$	-16.2 (-6.43)	2.42 (9.53)	-15.8 (-9.61)	-12.3 (-6.27)	7.51 (9.81)		
2-C	-18.0 (-9.93)	-15.4(-6.79)	4.34 (8.57)	-14.1 (-8.96)	-11.3 (-6.52)	7.16 (8.05)		
2-D	-18.0 (-9.85)	-15.4 (-6.81)	4.32 (8.56)	-13.7 (-8.06)	-10.8 (-5.46)	7.59 (8.79)		
2-E	-17.0 (-9.56)	-14.3 (-6.49)	4.38 (7.80)	-14.6 (-7.93)	-11.4(-5.23)	7.66 (9.36)		

<sup>&</sup>lt;sup>a</sup> Numbers in parentheses are for the methanol solution. The SM8 and IEFPCM methods were used at the M06-2X and MP2 levels, respectively. The structures of 1-A, 1-B, 2-A, 2-B, 2-C, 2-D, and 2-E are shown in Figure 1.



**Figure 2.** Reactant, product, and transition state of the ESDPT in the 7AI-CH<sub>3</sub>OH complex in methanol at the CASSCF(10,9)/6-311G-(d,p) level.

with each other. In the gas phase, the  $\Delta G$  values of 1-A and 2-A at the M06-2X level are both negative, and 2-A has a 2.2 kcal/mol smaller value, which suggests that both conformers are present in the gas phase, while 2-A is more preferable. However, in methanol solution, neither complex has negative free energies of formation; 2-A has a 2.7 kcal/mol larger  $\Delta G$  value than 1-A. The formation of 2-A is entropically very unfavorable even in solution. Therefore, there is no abundance of cyclic H-bonded complexes in solution. Equilibrium constants for the formation of 7AI-CH<sub>3</sub>OH can be rewritten as

$$\frac{[7AI \cdot CH_3OH]}{[7AI]} = K_{eq}[CH_3OH] = f$$
 (1)

which can be used to estimate the fraction of a cyclic complex in bulk methanol. The fraction of 1-A obtained using the equilibrium constant (from the formation free energy) and the molar

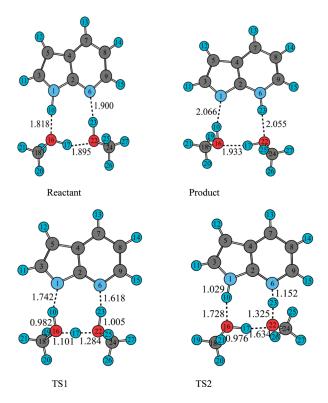


Figure 3. Reactant, product, and two transition states (TS1 and TS2) of the ESTPT in the 7AI- $(CH_3OH)_2$  complex in methanol at the CASSCF-(10,9)/6-311G(d,p) level.

concentration of bulk methanol was 0.036, which means that only 3.6% of 1-A is generated in a given methanol solution of 7AI at 298 K. In the 7AI complexes with two CH<sub>3</sub>OH groups, only 1% of the composition would be the cyclic 2-A conformer in the ground state. This result agrees very well with the previous Monte Carlo and molecular dynamics studies, 53,54 which is consistent with the two step model involving the formation of the cyclic complex after excitation. As a result, solvent reorganization plays a very important role in the above process.

Before excitation, most 7AI molecules were assumed to be solvated in a manner that blocks the double proton transfer. However, we were unable to find such complexes in abundance in bulk methanol. Among single-methanol complexes, 1-B blocks the double proton transfer, but its free energies of formation in

Table 2. Selected Bond Distances (Å) of Reactant, Product, and Transition States for the Excited-State Proton Transfer Optimized at the CASSCF(10,9) Level in  $Methanol^a$ 

		7AI-CH₃OH								
		reactant			product					
	r(H <sub>10</sub> -	-O <sub>16</sub> )	$r(H_{17}-N_6)$	r(N <sub>1</sub> -	r(N <sub>1</sub> -H <sub>10</sub> )					
6-31G(d,p)	2.26	2.261		2.261 2.081			2.161			
6-311G(d,p)	2.28	37	2.089	2.1	69	2.279				
		transition state								
	$r(N_1-H_{10})$		$r(H_{10}-O_{16})$	r(O <sub>16</sub> -	r(O <sub>16</sub> -H <sub>17</sub> )					
6-31G(d,p)	1.341		1.139	0.990		1.763				
6-311G(d,p)	1.343 (1.	1.343 (1.299)		1.133 (1.174) 0.980 (1		1.828 (1.605)				
	7AI-(CH <sub>3</sub> OH) <sub>2</sub>									
		reactant			product	product				
	$r(H_{10}-O_{16})$ $r(O_{22}-H_{17})$		r(H <sub>23</sub> -N <sub>6</sub> )	r(N <sub>1</sub> -H <sub>10</sub> )	$r(O_{16}-H_{17})$	r(O <sub>22</sub> -H <sub>23</sub> )				
6-31G(d,p)	1.817	1.874	1.879	2.055	1.920	2.045				
6-311G(d,p)	1.818	1.818 1.895		2.066	1.933	2.055				
		transition state								
	r(N <sub>1</sub> -H <sub>10</sub> )	$r(H_{10}-O_{16})$	$r(O_{16}-H_{17})$	$r(H_{17}-O_{22})$	r(O <sub>22</sub> -H <sub>23</sub> )	r(H <sub>23</sub> -N <sub>6</sub> )				
6-31G(d,p)TS1	1.700	0.991	1.087	1.312	1.014	1.593				
6-311G(d,p)TS1	1.742 (1.548) 0.982 (1.027)		1.101 (1.045)	1.284 (1.385)	1.005 (1.009)	1.618 (1.599)				
6-31G(d,p)TS2	1.031	1.723	0.982	1.614	1.322	1.156				
6-311G(d,p)TS2	311G(d,p)TS2 1.029 (1.067) 1.728 (1.529) 0.976		0.976 (1.018)	1.634 (1.451)	1.325 (1.416)	1.152 (1.103)				
<sup>a</sup> Numbers in parentl	heses are the bond dis	stances in the gas pha	se.							

solution are larger than that of 1-A. In two-methanol complexes, 2-D and 2-E block the triple proton transfer, but their formation free energies are smaller than that of 2-A. All these complexes are present less abundantly in bulk methanol than 1-A or 2-A. These results suggest that there may be no meaningful H-bonded conformers, which are abundantly present in solution, to block the proton transfer. Before the excitation of 7AI in bulk methanol, the formation of the H-bonded complexes seems to be random and dynamic rather than forming any meaningful equilibrated forms.

3.2. Excited-State Tautomerization of 7AI-(CH<sub>3</sub>OH)<sub>n</sub> (n = 1, 2) in Solution. 3.2.1. Structures of Reactants, Products, and Transition States at the CASSCF(10,9) Level. We preformed IEFPCM calculations for the cyclic reactant, TS, and product at the CASSCF levels to understand the solvent effect in the excited-state tautomerization. The cyclic complexes of reactant, product, and TS in solution were confirmed by frequency calculations. In the excited-state studies, we will discuss only the cyclic conformers of 7AI complexes from now on, so 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> represent the 1-A and 2-A conformers, respectively, unless mentioned otherwise. The optimized structures of 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> at the CASSCF(10,9)/6-311G(d,p) level in methanol are depicted in Figures 2 and 3, respectively, and some optimized geometrical parameters of 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> are listed in Table 2. In the gas phase structure of the 7AI-CH<sub>3</sub>OH complex at the CASSCF/6-311G(d,p) level, the H-bond distances of  $H_{10}-O_{16}$  and  $N_6-H_{17}$  in the reactant and  $N_1-H_{10}$  and  $O_{16}-H_{17}$  in the product were 2.154 and 2.127 Å and 2.199 and 2.187 Å, respectively. In methanol solution, the H<sub>10</sub>-O<sub>16</sub> H-bond in the reactant was 0.133 Å longer and N<sub>6</sub>-H<sub>17</sub> was 0.038 Å shorter than those in the gas phase. In the 7AI-CH<sub>3</sub>OH product, the N<sub>1</sub>-H<sub>10</sub> and O<sub>16</sub>-H<sub>17</sub> H-bonds became shorter and longer, respectively, in methanol. In other words, H-bonds with a nitrogen atom as an acceptor  $(N_1-H_{10})$  in the product and  $N_6-H_{17}$  in the reactant) shrank in methanol, whereas those with oxygen as an acceptor  $(H_{10}-O_{16})$  in the reactant and  $O_{16}-H_{17}$  in the product) were elongated. These results imply that the solvent effect could increase the excited-state basicity of the nitrogen atom in 7AI to generate slightly shorter and stronger H-bond. The bond distances in the gas phase TSs are also listed in Table 2. Compared to those in the the gas phase structure, the  $N_1 - H_{10}$ and N<sub>6</sub>-H<sub>17</sub> distances were increased in solution, whereas the  $H_{10}-O_{16}$  and  $O_{16}-H_{17}$  distances were decreased, which forms a CH<sub>3</sub>OH<sub>2</sub><sup>+</sup>-like moiety in part of the TS. No large changes were observed in the distances depending on the size of the basis sets.

In the reactant and product structures of  $7AI-(CH_3OH)_2$  at the CASSCF/6-311G(d,p) level, the H-bond distances in solution did not vary much from the corresponding gas phase values. Two TS structures for the ESTPT were found and are shown in Figure 3. In the first TS (denoted as TS1), the  $H_{10}$  moved more than halfway from the  $N_1$  to  $O_{16}$  atom with  $H_{17}$  and  $H_{23}$  barely moving. This generated a  $CH_3OH_2^+$ -like moiety in a portion of the TS (at  $O_{16}$ ). However, in the second TS (denoted as TS2),

Table 3. Tautomerization Energies, Barrier Heights, and Dipole Moments for the ESPT in  $7AI-CH_3OH$  and  $7AI-(CH_3OH)_2$  Complexes in Methanol <sup>a</sup>

				$\mu(D)$			
	$\Delta V^{\dagger}$	$\Delta E_{ m T}$	R	TS	P		
	7AI-C	H <sub>3</sub> OH					
CASSCF(10,9)/6-31G(d,p)	13.0 (10.7) [11.8]	-31.7 (-31.2)	2.38	7.76	2.35		
CASSCF(10,9)/6-311G(d,p)	11.6 (9.57) [10.6]	-32.0 (-31.5)	2.33	8.30	2.31		
$MRPT2/CASSCF(10,9)/6-31G(d,p)^{b}$	6.43 (4.06) [5.15]	-19.0(-18.5)					
$MRPT2/CASSCF(10,9)/6-311G(d,p)^{b}$	4.80 (2.78) [3.81]	$-18.4\ (-17.9)$					
	7AI-(CI	H <sub>3</sub> OH) <sub>2</sub>					
CASSCF(10,9)/6-31G(d,p)	12.5 (9.32) [10.4] <sup>c</sup>	-27.8 (-28.0)	7.43	9.39 <sup>c</sup>	2.43		
	$11.7 (8.14) [9.26]^d$			$10.1^{d}$			
CASSCF(10,9)/6-311G(d,p)	12.6 (9.58) [10.7] <sup>c</sup>	-27.1(-27.3)	7.55	9.77 <sup>c</sup>	2.49		
	$12.7 (9.07) [10.2]^d$			$10.1^{d}$			
$MRPT2/CASSCF(10,9)/6-31G(d,p)^{b}$	$4.94 (1.81) [2.93]^c$	-15.4 (-15.6)					
	$5.34(1.77)[2.89]^d$						
$MRPT2/CASSCF(10,9)/6-311G(d,p)^{b}$	$3.31 (0.27) [1.42]^c$	-14.8 (-15.0)					
	$7.05(3.43)[4.54]^d$						

 $<sup>^</sup>a$  The numbers in parentheses and brackets are the barrier heights of H and D transfers including zero-point energies, respectively. Energies are in kcal/mol.  $^b$  The energy includes nonelectrostatic terms.  $^c$  TS1.  $^d$  TS2.

Table 4. Selected Bond Distances (Å) of Reactant, Product, and Transition States for the Excited-State Proton Transfer in 7AI-CH $_3$ OH Calculated at the TDDFT Levels in Methanol

	rea	actant	product		
computational method	$r(H_{10}-O_{16})$	$r(H_{17}-N_6)$	r(N <sub>1</sub> -H <sub>10</sub> )	$r(O_{16}-H_{17})$	
B3LYP/6-31G(d,p)	1.939	1.809	1.933	2.049	
B3LYP/6-311+G(d,p)	2.013	1.851	1.954	2.130	
CAM-B3LYP/6-31G(d,p)	1.908	1.807	1.922	2.003	
CAM-B3LYP/6-311+G(d,p)	1.971	1.850	1.945	2.058	
LC- $BLYP$ / $6$ - $31G(d,p)$	1.884	1.798	1.900	1.950	
LC-BLYP/6-311+ $G(d,p)$	1.938	1.833	1.917	1.990	
M06-2X/6-31G(d,p)	1.943	1.824	1.982	2.025	
M06-2X/6-311+G(d,p)	2.010	1.870	1.984	2.100	
WB97XD/6-31G(d,p)	1.933	1.836	1.949	2.022	
WB97XD/6-311+ $G(d,p)$	2.015	1.854	1.854 1.948		
		transit	on state		
computational method	r(N <sub>1</sub> -H <sub>10</sub> )	$r(H_{10}-O_{16})$	r(O <sub>16</sub> -H <sub>17</sub> )	r(H <sub>17</sub> -N <sub>6</sub> )	
B3LYP/6-31G(d,p)	1.260	1.253	1.153	1.376	
B3LYP/6-311+G(d,p)	1.310	1.201	1.117	1.434	
CAM-B3LYP/6-31G(d,p)	1.277	1.224	1.121	1.412	
CAM-B3LYP/6-311+G(d,p)	1.329	1.175	1.091	1.473	
LC-BLYP/6-31G(d,p)	1.286	1.208	1.114	1.415	
LC-BLYP/6-311+ $G(d,p)$	1.332	1.167	1.093	1.460	
M06-2X/6-31G(d,p)	1.282	1.218	1.094	1.458	
M06-2X/6-311+G(d,p)	1.320	1.180	1.071	1.511	
WB97XD/6-31G(d,p)	1.289	1.208	1.111	1.424	
WB97XD/6-311+G(d,p)	1.342	1.159	1.079	1.490	

the  $H_{23}$  moved more than halfway from the  $O_{22}$  to the  $N_6$  atom, but  $H_{10}$  and  $H_{17}$  barely moved, resulting in a  $CH_3O^-$ -like moiety in a part of the TS (at  $O_{22}$ ). Two TSs of the concerted but highly asynchronous multiproton transfer in 7AI- $(H_2O)_2$  were previously

observed both in the gas phase and in water.<sup>28</sup> The methanol complex showed similar behavior in the ESTPT. Considering only one proton migrated substantially, while the other two barely moved, a stepwise mechanism with a possible intermediate was

Table 5. Selected Bond Distances (Å) of Reactant, Product, and Transition States for the Excited-State Proton Transfer in  $7AI-(CH_3OH)_2$  Calculated at the TDDFT Levels in Methanol

		reactant			product			
computational method	$r(H_{10} {-} O_{16})$	$r(O_{22}-H_{17})$	$r(H_{23}-N_6)$	$r(N_1 - H_{10})$	$r(O_{16}-H_{17})$	$r(O_{22}-H_{23})$		
B3LYP/6-31G(d,p)	1.690	1.674	1.679	1.806	1.729	1.827		
B3LYP/6-311+G(d,p)	1.733	1.727	1.729	1.834	1.770	1.866		
CAM-B3LYP/6-31G(d,p)	1.664	1.649	1.675	1.794	1.702	1.795		
CAM-B3LYP/6-311+G(d,p)	1.709	1.700	1.724	1.818	1.738	1.827		
LC-BLYP/6-31G(d,p)	1.638	1.613	1.661	1.766	1.661	1.749		
LC-BLYP/6-311+G(d,p)	1.685	1.662	1.705	1.783	1.692	1.778		
M06-2X/6-31G(d,p)	1.650	1.668	1.662	1.845	1.754	1.821		
M06-2X/6-311+G(d,p)	1.704	1.721	1.719	1.862	1.812	1.863		
WB97XD/6-31G(d,p)	1.695	1.704	1.705	1.826	1.751	1.816		
WB97XD/6-311+ $G(d,p)$	1.717	1.726	1.728	1.817	1.762	1.823		
		transit			tion state			
computational method	r(N <sub>1</sub> -H <sub>10</sub> )	r(H <sub>10</sub> -O <sub>16</sub> )	r(O <sub>16</sub> -H <sub>17</sub> )	r(H <sub>17</sub> -O <sub>22</sub> )	r(O <sub>22</sub> -H <sub>23</sub> )	r(H <sub>23</sub> -N <sub>6</sub> )		
B3LYP/6-31G(d,p)	1.118	1.447	1.104	1.341	1.349	1.164		
B3LYP/6-311+G(d,p)	1.094	1.508	1.094	1.356	1.477	1.103		
CAM-B3LYP/6-31G(d,p)	1.139	1.388	1.109	1.315	1.295	1.193		
CAM-B3LYP/6-311+G(d,p)TS1	1.382	1.124	1.122	1.296	1.097	1.428		
CAM-B3LYP/6-311+G(d,p)TS2	1.105	1.465	1.097	1.334	1.435	1.115		
LC-BLYP/6-31G(d,p)	1.251	1.222	1.129	1.271	1.159	1.319		
LC- $BLYP/6$ - $311$ + $G(d,p)$	1.370	1.127	1.130	1.275	1.100	1.415		
M06-2X/6-31G(d,p)	1.244	1.233	1.106	1.310	1.106	1.398		
		1.233 1.125	1.106 1.106	1.310 1.317	1.106 1.075	1.398 1.462		
M06-2X/6-31G(d,p)	1.244							
M06-2X/6-31G(d,p) M06-2X/6-311+G(d,p)	1.244 1.375	1.125	1.106	1.317	1.075	1.462		

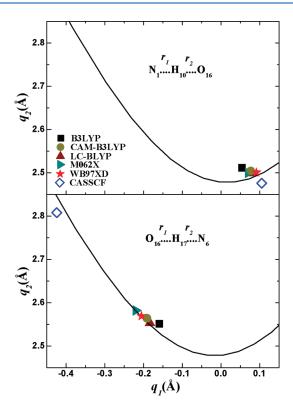
expected. However, all calculations to find this intermediate in methanol led to either the reactant or the product. Thus, these results suggest that there are potentially two concerted but asynchronous processes in the ESTPT. The solvent effect increased the  $N_1{-}H_{10}$  and  $N_6{-}H_{23}$  distances of TS1 and reduced the  $O_{16}{-}O_{23}$  distance by slightly moving  $H_{17}$  toward the center of two oxygen atoms to form a short and strong H-bond, which resulted in the larger ion-pair character of TS. In TS2, the  $O_{16}{-}H_{10}$  and  $O_{22}{-}H_{17}$  distances were increased in solution, but the  $O_{22}{-}H_{23}$  increased slightly, which probably increased the partial charge density of the  $CH_3O^-$ -like moiety in a part of the TS.

3.2.2. Energetics and Mechanism of the Excited-State Tautomerization in Solution. Barrier heights  $(\Delta V^{\dagger})$ , excited-state tautomerization energies  $(\Delta E_{\rm T})$ , and dipole moments  $(\mu)$  for the 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> complexes are listed in Table 3. Tautomerization energies and barrier heights were highly dependent on the dynamic electron correlation. The MRPT2 level predicted somewhat different tautomerization energies for 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> in methanol; the tautomerization of 7AI-CH<sub>3</sub>OH was more exoergic than that of 7AI-(CH<sub>3</sub>OH)<sub>2</sub>. The ZPE-corrected  $\Delta E_{\rm T}$  value of 7AI-CH<sub>3</sub>OH was 2.9 kcal/mol lower than that of 7AI-(CH<sub>3</sub>OH)<sub>2</sub> at the MRPT2 level using the 6-311G(d,p) basis sets, which means that the tautomerization of 7AI-(CH<sub>3</sub>OH)<sub>2</sub> is thermodynamically less favorable in methanol.

The  $\Delta V^{\dagger}$  values greatly depend on the dynamic electron correlation. In particular, the relative  $\Delta V^{\dagger}$  values of TS1 and

TS2 in 7AI-(CH<sub>3</sub>OH)<sub>2</sub> would not be correctly predicted unless the dynamic electron correlation with sufficiently large basis sets was used. The ZPE-corrected  $\Delta V^{\dagger}$  value of 7AI-CH<sub>3</sub>OH was only 2.8 kcal/mol at the MRPT2/6-311G(d,p) level in methanol. The activation energy of the solvent viscosity was 2.6 kcal/mol for methanol, <sup>29</sup> which is nearly the same as the  $\Delta V^{\dagger}$  value. This result suggests that the ESDPT is possible in solution at room temperature, while no tautomerization was observed in the gas phase, which is consistent with the experimental results. In the ESTPT of the 7AI-(CH<sub>3</sub>OH)<sub>2</sub> complex, the ZPE-corrected  $\Delta V^{\dagger}$ value of TS1 was 0.3 kcal/mol, which is 3.2 kcal/mol lower than that of TS2. This indicates that the ESTPT would occur preferably via TS1. The ZPE-corrected  $\Delta V^{\dagger}$  value of 7AI-(CH<sub>3</sub>OH)<sub>2</sub> was 2.5 kcal/mol lower than that of 7AI-CH<sub>3</sub>OH, which suggests that the ESTPT is approximately 70 times faster than the ESDPT in methanol without considering the tunneling

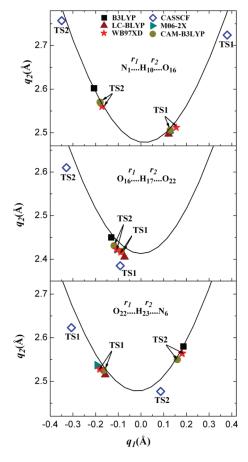
No experimental studies have reported the possibility of the ESTPT by forming cyclic H-bonded complexes with two CH<sub>3</sub>OH molecules in methanol. Proton inventory experiments showing the linear plot of  $\left(k_{\rm n}/k_0\right)^{1/2}$  vs n and the RGM in KIEs were used as evidence for the concerted two proton mechanism in the intrinsic proton transfer step by forming cyclic 7AI-CH<sub>3</sub>OH. The underlying assumption of the above experiments is that the force constants of the two protons in the concerted rate-limiting step are the same at the TS. However, this assumption fails when the multiproton transfer is highly asynchronous



**Figure 4.** Correlation of the H-bond distances  $q_2 = r_1 + r_2$  with the proton transfer coordinate  $q_1 = (1/2)(r_1 - r_2)$  for the 7AI-CH<sub>3</sub>OH complex in methanol. All points are for the transition states in S<sub>1</sub> optimized at the CASSCF/6-311G(d,p) and TDDFT/6-311+G(d,p) levels in solution. The solid lines designate the correlation that satisfies the conservation of the bond order.

and/or the intrinsic proton transfer is not rate-limiting. Although the ESTPT in 7AI-(CH<sub>3</sub>OH)<sub>2</sub> occurs in solution, no KIE is observed if solvent reorganization is rate-limiting. In addition, the amount of ground-state 7AI-(CH<sub>3</sub>OH)<sub>2</sub> before excitation is very small in methanol. These results suggest that 7AI-CH<sub>3</sub>OH is generated in a larger quantity in the ground state than 7AI-(CH<sub>3</sub>OH)<sub>2</sub>, although the ESTPT in 7AI-(CH<sub>3</sub>OH)<sub>2</sub> occurs faster than the ESDPT in 7AI-CH<sub>3</sub>OH; therefore, the tautomerization path of the ESTPT seems to be unimportant. Moreover, the  $\Delta V^{\dagger}$  value of ESTPT via TS1 is lower than the activation energy of methanol viscosity; therefore, the tautomerization of 7AI-(CH<sub>3</sub>OH)<sub>2</sub> must be limited by solvent reorganization.

The experimental Arrhenius activation energy of the excitedstate tautomerization was 2.3 kcal/mol in methanol,<sup>29</sup> which is somewhat smaller than the  $\Delta V^{\dagger}$  value of 7AI-CH<sub>3</sub>OH. Considering the lack of tunneling effect in this study and the kinetics were mixed with solvent reorganization, the agreement between theory and experiment is quite good. The barrier heights of deuterium (D) transfer are also listed in Table 3. The  $\Delta V^{\dagger}$  value of D transfer in 7AI-CH<sub>3</sub>OH at the MRPT2 level using the 6-311G(d,p) basis set is 3.81 kcal/mol, which is 1.03 kcal/mol larger than that of the proton (H) transfer. The KIE estimated using these values without considering the tunneling effect is 5.87, which is larger than the experimental values. This value of KIE would be obtained only if H and D transfers were both ratelimiting. The smaller KIE value might be attributed to the slower H transfer rate that is limited by the solvent reorganization. This result also suggests that the intrinsic H transfer is not entirely



**Figure 5.** Correlation of the H-bond distances  $q_2 = r_1 + r_2$  with the proton transfer coordinate  $q_1 = (1/2)(r_1 - r_2)$  for the 7AI-(CH<sub>3</sub>OH)<sub>2</sub> complex in methanol. All points are for the transition states in S<sub>1</sub> optimized at the CASSCF/6-311G(d,p) and TDDFT/6-311+G(d,p) levels in solution. The solid lines designate the correlation that satisfies the conservation of the bond order.

rate-limiting (must be competing with solvent reorganization) in the excited-state tautomerization. The  $\Delta V^{\dagger}$  value of D transfer is larger than the activation energy of methanol viscosity; therefore, the intrinsic D transfer is rate-limiting. However, in the 7AI-(CH<sub>3</sub>OH)<sub>2</sub> complex, the  $\Delta V^{\dagger}$  value of D transfer is smaller than the activation energy of methanol viscosity; therefore, the solvent reorganization is still rate-limiting in this case.

3.2.3. Structures and Energetics at the TDDFT Level. In order to investigate which functionals are most successful for studying excited-state reactions, we tested five TDDFT methods, namely, B3LYP, CAM-B3LYP, LC-BLYP, M06-2X, and WB97XD. Geometric parameters of reactant, product, and transition states for 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> calculated at the TDDFT levels in methanol are listed in Tables 4 and 5, respectively. In order to explain kinetic properties, it is very important to correctly calculate the TS structure. In the TS, the ESDPT/ ESTPT occurred in a concerted but asynchronous way. Limbach et al. 55-57 defined the hydrogen bond coordinates  $q_1 = (1/2)$  $(r_{AH} - r_{BH})$  and  $q_2 = r_{AH} + r_{BH}$  to represent the correlation between  $r_{AH}$  and  $r_{BH}$  in many hydrogen-bonded complexes (A-H···B), which can be used to study the characteristics of TS, such as earliness or lateness, tightness or looseness, bond order, and asynchronicity. For a linear H-bond,  $q_1$  represents the distance of H from the H-bond center, and q2 represents the

Table 6. Tautomerization Energies, Barrier Heights, and Dipole Moments for the ESPT in 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> Calculated at the TDDFT Levels in Solution<sup>a</sup>

	7AI-CH₃OH				7AI-(CH <sub>3</sub> OH) <sub>2</sub>					
				$\mu(D)$				$\mu(D)$		
computational method	$\Delta \textit{V}^{\dagger}$	$\Delta E_{\mathrm{T}}$	R	TS	Р	$\Delta V^{\dagger}$	$\Delta E_{\mathrm{T}}$	R	TS	P
B3LYP/6-31G(d,p)	8.79 (4.23)	-15.5 (-15.1)	5.89	4.01	2.09	5.16 (0.46)	-13.4 (-12.7)	5.30	6.82	2.11
CAM-B3LYP/6-31G(d,p)	8.33 (4.13)	-16.2(-15.6)	5.42	4.30	2.18	5.11 (-0.09)	-14.0 (-13.1)	4.87	5.90	2.43
LC- $BLYP/6$ - $31G(d,p)$	8.04 (4.08)	-14.9(-14.2)	4.61	4.12	2.27	4.50 (-1.38)	-12.7(-11.7)	3.95	3.87	2.66
M06-2X/6-31G(d,p)	7.04 (3.47)	-16.8 (-16.1)	5.73	4.51	2.30	3.23 (-1.38)	-14.3 (-13.5)	5.19	4.75	3.07
WB97XD/6-31G(d,p)	9.77 (5.59)	-16.4(-15.9)	5.64	4.39	2.30	6.59 (1.48)	-14.2(-13.3)	5.15	6.62	3.02
B3LYP/6-311+G(d,p)	11.7 (7.54)	-13.7(-13.4)	5.93	4.54	2.11	6.77 (3.11)	-12.1 (-11.6)	5.46	8.21	1.91
CAM-B3LYP/6-311+G(d,p)	11.7 (8.01)	-13.2 (-12.6)	5.27	4.95	2.22	$8.80 (3.61)^b$	-11.7(-11.0)	4.88	$5.47^{b}$	2.24
						7.51 (3.47) <sup>c</sup>			$7.46^{c}$	
LC- $BLYP/6$ - $311$ + $G(d,p)$	11.7 (8.13)	-10.9(-10.2)	4.44	4.75	2.33	8.26 (3.08)	-9.51 (-8.73)	4.04	5.07	2.45
M06-2X/6-311+G(d,p)	9.89 (6.53)	-13.7(-13.1)	5.73	5.10	2.59	5.61 (1.71)	-12.2 (-11.1)	5.12	5.49	3.06
WB97XD/6-311+ $G(d,p)$	12.6 (9.16)	-13.4 (-12.8)	5.60	5.11	2.59	$9.77 (4.85)^b$	-11.8 (-10.9)	5.10	$5.73^{b}$	2.35
						8.46 (4.38) <sup>c</sup>			$7.74^{c}$	
The numbers in parentheses include zero point energies. Energies are in kcal/mol. bTS1 cTS2										

 $<sup>^</sup>a$ The numbers in parentheses include zero-point energies. Energies are in kcal/mol.  $^b$  TS1.  $^c$  TS2.

distance between atoms A and B. The negative or positive  $q_1$ value corresponds to early or late TS, respectively, and the small or large  $q_2$  value corresponds to tight or loose TS, respectively. In addition, the two  $q_1$  values at the TS of double proton transfer should be very similar and different in the synchronous and asynchronous mechanisms, respectively. Bond distance depends on bond energy and bond order. In the A $-H\cdots$ B complexes, the  $r_{AH}$  and  $r_{BH}$  distances depend on each other, leading to allowed  $r_{AH}$  and  $r_{BH}$  values based on the Pauling equations under the assumption that the sum of the two bond orders is conserved. This type of correlation, i.e., the bond energy bond order method, has been used for many years to study hydrogen atom transfer. <sup>58,59</sup> When H is transferred from A to B in the  $A-H\cdots B$ complex,  $q_1$  increases from a negative to positive value, and  $q_2$  goes through a minimum at  $q_1$  = 0. Limbach et al. <sup>55–57</sup> suggested that both proton transfer and hydrogen-bonding coordinates could be combined into the same correlation.

The correlation between  $q_1$  and  $q_2$  at the TS of 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> in methanol are illustrated in Figures 4 and 5. Interestingly, all correlation points of TS were at or near the solid lines that satisfy the Pauling equations, although their geometric parameters highly depend on the theoretical level. The parameters for the Pauling equations were taken from the literature. <sup>56</sup> At the TS of 7AI-CH<sub>3</sub>OH, the correlation of  $q_1$  with  $q_2$  was dependent on the solvent effect, which greatly enhanced the asynchronicity of the double proton transfer; the differences in  $q_1$  values between  $H_{10}$  and  $H_{17}$  increased significantly. At the TDDFT levels, the positive and negative  $q_1$  values of  $H_{10}$  and H<sub>17</sub>, respectively, suggested asynchronous double proton transfer, where the  $H_{10}$  atom moved first, followed by the  $H_{17}$  atom. The TDDFT level generated the same mechanism (but with significantly smaller asynchronicity) as the CASSCF. For the TS of  $7AI-(CH_3OH)_2$  at the CASSCF level, as described above, two TS structures represent two different ESTPT mechanisms. At TS1, the  $H_{10}$  and  $H_{23}$  correlation points appeared in the right and left side of Figure 5, respectively, which showed large asynchronicity of TS1, i.e., the TS positions in terms of the  $H_{10}$  and  $H_{23}$ transfers became very late (product-like) and early (reactant-like), respectively. At TS2, however, the H<sub>10</sub> and H<sub>23</sub> correlation points appeared in the opposite manner. At the TDDFT levels, two TSs (TS1 and TS2) were obtained only at the CAM-B3LYP/6-311+G(d,p) and WB97XD/6-311+G(d,p) levels. As shown in Figure 5, the correlation points of TS1 for  $H_{10}$  transfer and  $H_{23}$  transfer at these two levels are not separated as much as those at the CASSCF level, which implies that the asynchronicity of TS1 is much less than that at the CASSCF level so are the correlation points and the asynchronicity of TS2. The TS of B3LYP resembled TS2, whereas those of M06-2X and LC-BLYP resembled TS1 that has a lower barrier at the MRPT2 level.

Tautomerization energies, barrier heights, and dipole moments for 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> calculated at the TDDFT levels are listed in Table 6. The TDDFT levels predicted  $\Delta E_{\rm T}$  values in better agreement with the MRPT2 values than with the CASSCF without the dynamic electron correlation. However, the  $\Delta V^{\dagger}$  values highly depend on the size of the basis sets. For 7AI-CH<sub>3</sub>OH, the ZPE-corrected  $\Delta V^{\dagger}$  values at most TDDFT levels with the 6-31G(d,p) basis set agreed well with the MRPT2 values using the same basis sets. Using the larger basis set, however, increased these values in opposition to the MRPT2 results. The bond lengths listed in Table 4 revealed that the asynchronicity of TS was increased by using larger basis sets, which produced better agreement with the CASSCF structures. However, the calculated  $\Delta V^{\dagger}$  values with larger basis sets were actually worse.

For 7AI-(CH<sub>3</sub>OH)<sub>2</sub>, we were unable to find two TSs at the TDDFT levels using the 6-31G(d,p) basis set. Interestingly, the ZPE-corrected  $\Delta V^{\dagger}$  values were near zero using the 6-31G(d,p) basis set and increased by using larger basis sets, in opposition to the MRPT2 results. Only two DFT methods, namely, CAM-B3LYP/6-311+G(d,p) and WB97XD/6-311+G(d,p), predicted two TSs (TS1 and TS2), whose ZPE-corrected  $\Delta V^{\dagger}$  values were nearly the same. The CAM-B3LYP level generated about 1 kcal/mol lower energy barriers than that of the WB97XD level. Although the M06-2X/6-311+G(d,p) level failed to locate two TSs, it produced a better ZPE-corrected  $\Delta V^{\dagger}$  value than the above two methods, compared with the corresponding MRPT2 value of TS1, which is probably due to the TS structure being similar to TS1, as described above.

The ZPE-corrected barrier heights of 7AI-CH<sub>3</sub>OH and  $7AI-(CH_3OH)_2$  at the TDDFT/6-311+G(d,p) levels were 3.68-5.53 kcal/mol and -0.76-1.42 kcal/mol, respectively, in the gas phase. However, solvation increased the barriers by about 2-3 kcal/mol, whereas the barriers at the MRPT2 levels were reduced upon solvation. Such opposite solvent effects on the barrier heights can be explained by the dipole moments listed in Tables 3 and 6. The larger dipole moments originated from the geometric change upon solvation to increase the ionic character of the reactant and transition states in a polar solvent. Consequently, species with larger dipole moments are likely to be more stabilized in a polar solvent. At the CASSCF level, the dipole moments of TSs are greater than those of the reactants for both 7AI-CH<sub>3</sub>OH and 7AI-(CH<sub>3</sub>OH)<sub>2</sub> (Table 3), which lowers the barrier heights in solution. However, at the TDDFT levels for 7AI-CH<sub>3</sub>OH, the dipole moments of TS were smaller than those of the reactant (Table 6), which led to larger barrier heights. Such problematic prediction of dipole moments at the TDDFT levels may originate from the incorrect estimation of the excited-state charge densities, particularly at the TS. The TDDFT barriers for  $7AI-(CH_3OH)_2$  in solution became larger than those in the gas phase, although the dipole moments of TS were slightly larger than those of reactant, which may require further study.

#### 4. CONCLUSIONS

In the present work, systematic studies of the excited-state proton transfer reactions in methanol were performed on 7AI-(CH<sub>3</sub>OH) $_n$  (n=1,2) complexes using TDDFT and CASSCF methods. The energetics of the excited-state tautomerization depend on the dynamic electron correlation and the size of the basis sets. For the 7AI-(CH<sub>3</sub>OH) $_2$  complex, CASSCF levels predicted two concerted but asynchronous paths of ESTPT; one where the proton moved first from the pyrole ring of 7AI to methanol and the other where the methanol proton moved first to the pyridine ring. No obvious difference was found between the barrier heights of the two paths when not considering the dynamic electron correlation. However, the MRPT2 correction clearly showed that the former path was much preferable to the latter.

The MRPT2 barrier of ESDPT in 7AI-CH $_3$ OH was 2.8 kcal/mol, which is consistent with the experimental results that the excited-state tautomerization was not observed in the gas phase but only in solution. Additionally, the 7AI-(CH $_3$ OH) $_2$  MRPT2 barrier was smaller than the activation energy of solvent reorganization, so the ESTPT is not rate-limiting. Because the amount of ground-state 7AI-(CH $_3$ OH) $_2$  is very small in methanol, the tautomerization by the ESTPT in 7AI-(CH $_3$ OH) $_2$  might not be important.

The MRPT2 barrier of deuterium transfer in 7AI-CH<sub>3</sub>OH is 3.81 kcal/mol (1.03 kcal/mol larger than the proton transfer), which leads to the predicted H/D KIE of 5.87. The  $\Delta V^{\dagger}$  value of deuterium transfer is larger than the activation energy of solvent reorganization; therefore, the intrinsic deuterium transfer is ratelimiting, but the proton transfer must compete with solvent reorganization. In the 7AI-(CH<sub>3</sub>OH)<sub>2</sub> complex, the  $\Delta V^{\dagger}$  value of deuterium transfer is still smaller than the activation energy of methanol viscosity.

All TDDFT methods slightly underestimated tautomerization energies compared with the MRPT2 values. No significant benefits, in terms of either structural or energetic prediction, were found using the DFT methods with long-range correction

or empirical dispersion. At all TDDFT levels used in this study, the TS structures and barrier heights greatly depend on the basis set and the solvent effect. Only two methods, WB97XD and CAM-B3LYP, predicted two TSs for two asynchronous paths in the 7AI-(CH $_3$ OH) $_2$  complex, although their barrier heights had nearly the same energies, unlike the MRPT2 results. The solvation increased the TDDFT barrier heights, which is attributed to the unreasonable dipole moments in the excited-state.

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