

## Bee Reproduction

1 The solution, pseudocode, instance of the problems, and all possible cases

### 1.1 The problem

There are 3 types of bees,

1. Queen
2. Soldier
3. Worker

Bee will reproduce each year with the following conditions

1. Queen will give one worker bee and still alive
2. Soldier will give one worker bee and die
3. Worker will give one worker bee and one soldier bee and die

Suppose at start we have one Queen and one Worker, find the number of bee in the given year.

### 1.2 The solution

#### 1.2.1 instance of the problems

##### 1.2.1 input and output

- input: the number of the year
- output: the number of the bee

##### 1.2.2 condition

- in this be hive there have a 3 type of bee Q, W and S
- Q will product 1 W
- W product 1 W and 1 S and die
- S product 1 W and die
- repeat this in every year

## 1.2.2 The solution in all possible case

To do this kind of problem we need to find pattern of each year that bee will product thus I will use Y as a year representative like  $Y_0$  mean year 0

Initial year or year 0 has Q and W bee or 2 bees in total

$$Y_0 = 2$$

And Q product 1 W then W product 1 W and 1 S so

W + W + S + Q now in first Y will have 4 bees

$$Y_1 = 4 \text{ (WWSQ)}$$

And process will be repeat like first year

W product 1 W and S then die

S product 1 W then dies

Q product W

So second year will have WSWSWWQ or 7 bee in total

$$Y_2 = 7$$

And third year will be WSWSWSWSWWWQ following by repeat condition

$$Y_3 = 12$$

So, if we make them as an equation will be something like this

$$Y_0 = 2$$

$$Y_1 = 4$$

$$Y_2 = 7 \quad \text{or} \quad Y_2 = Y_1 + Y_0 + 1$$

$$Y_3 = 12 \quad \text{or} \quad Y_3 = Y_2 + Y_1 + 1$$

Thus

$$Y_n = Y_{n-1} + Y_{n-2} + 1$$

And this equation ( $Y_n = Y_{n-1} + Y_{n-2} + 1$ ) can represent all possible case

### 1.3 pseudocode

Define : Read() mean function that receive input from user

Function BeeEachYear (Integer:n) -> Integer :

    If n == 0 Then

        Return 2

    Endif

    If n == 1 Then

        Return 4

    Endif

    Return BeeEachYear(n-2) + BeeEachYear(n-1) + 1

Endfunction

Start

    Let n <- Read()

    Display BeeEachYear(n)

End

### 2 implement a code

implement with python 3.8 on visual studio code with python extension

```
def bee_each_year(n):  
    if n == 0 :  
        return 2  
    if n == 1 :  
        return 4  
    return bee_each_year(n-2) + bee_each_year(n-1) + 1  
  
n = int(input())  
print(bee_each_year(n))
```

```
input:  
8  
output  
143
```