

1.3 We have

	Processor	Clock rate	CPI
a	P <sub>1</sub>	3 GHz	1.5
	P <sub>2</sub>	2.5 GHz	1.0
	P <sub>3</sub>	4 GHz	2.2
b	P <sub>1</sub>	2 GHz	1.2
	P <sub>2</sub>	3 GHz	0.8
	P <sub>3</sub>	4 GHz	2.0

1.3.1 Which processor has the highest performance expressed in instructions per second

instructions per second is the units from

$$\text{CPU execution} = \frac{\text{number of instruction} \times \text{CPI}}{\text{clock rate}}$$

$$a P_1 = \frac{n \text{ instr} \times 1.5}{3} = n \text{ instr} \times 0.5$$

$$a P_2 = \frac{n \text{ instr} \times 1.0}{2.5} = n \text{ instr} \times 0.4$$

$$a P_3 = \frac{n \text{ instr} \times 2.2}{4} = n \text{ instr} \times 0.55$$

answ: in instruction a processor P<sub>3</sub> has the highest performance

$$b P_1 = \frac{n \text{ instr} \times 1.2}{2} = n \text{ instr} \times 0.6$$

$$b P_2 = \frac{n \text{ instr} \times 0.8}{3} = n \text{ instr} \times 0.27$$

$$b P_3 = \frac{n \text{ instr} \times 2.0}{4} = n \text{ instr} \times 0.5$$

answ: in instruction b processor P<sub>1</sub> has the highest performance

1.3.2 If the processors each execute a program in 10 seconds, find the number of cycles and the number of instruction from CPU execution time = number of instruction  $\times$  CPI  $\times$  clock cycle number of instruction

$$\text{number of instruction} = \frac{\text{CPU execution time} \times \text{clock rate}}{\text{CPI}}$$

number of cycles

$$\text{number of cycles} = \frac{\text{CPU execution time}}{\text{number of instruction} \times \text{CPI}}$$

N = Number

a

$$P1 \text{ Minstruction} = \frac{10 \times 3 \times 10^9}{1.5} = 20 \times 10^9$$

$$N_{\text{cycle}} = \frac{10}{20 \times 10^9 \times 1.5} = 3 \times 10^{-9}$$

$$P2 \text{ Minstruction} = \frac{10 \times 2.5 \times 10^9}{1.0} = 25 \times 10^9$$

$$N_{\text{cycle}} = \frac{10}{25 \times 10^9 \times 1} = 2.5 \times 10^{-9}$$

$$P3 \text{ Minstruction} = \frac{10 \times 4 \times 10^9}{2.2} = 1.82 \times 10^{10}$$

$$N_{\text{cycle}} = \frac{10}{1.82 \times 10^{10} \times 2.2} = 2.5 \times 10^{-9}$$

b

$$P1 \text{ Minstruction} = \frac{10 \times 2 \times 10^9}{1.2} = 20.83 \times 10^9$$

$$N_{\text{cycle}} = \frac{10}{20.83 \times 10^9 \times 1.2} = 0.4 \times 10^{-9}$$

$$P2 \text{ Minstruction} = \frac{10 \times 3 \times 10^9}{0.8} = 37.5 \times 10^9$$

$$N_{\text{cycle}} = \frac{10}{37.5 \times 10^9 \times 0.8} = 3.33 \times 10^{-9}$$

$$P3 \text{ Minstruction} = \frac{10 \times 4 \times 10^9}{2.0} = 20 \times 10^9$$

$$N_{\text{cycle}} = \frac{10}{20 \times 10^9 \times 2.0} = 0.25 \times 10^{-9}$$

1.3.3 We are trying to reduce the time by 30% but this leads to an increase of 20% in CPI. What clock rate should we have to get this time reduction?

from formula CPU execution = (Number of Instruction  $\times$  CPI) / clock rate

but from problem we will get CPU execution  $\times 0.7 = (\text{Number of Instruction} \times \text{CPI} \times 1.2) / \text{clock rate}$

$$\text{So clock rate} = \frac{1.2}{0.7} = 1.71$$

a (clock rate  $\times 1.71$ )

$$P1 = 3 \times 1.71 = 5.13 \text{ GHz}$$

$$P2 = 2.5 \times 1.71 = 4.275 \text{ GHz}$$

$$P3 = 4 \times 1.71 = 6.84 \text{ GHz}$$

b (clock rate  $\times 1.71$ )

$$P1 = 2 \times 1.71 = 3.42 \text{ GHz}$$

$$P2 = 3 \times 1.71 = 5.13 \text{ GHz}$$

$$P3 = 4 \times 1.71 = 6.84 \text{ GHz}$$



FOR problems below, use the information in the following table.

	Processor	clock rate	No. Instructions	Tin
a.	P <sub>1</sub>	3 GHz	20 × 10 <sup>9</sup>	7 s
	P <sub>2</sub>	2.5 GHz	30 × 10 <sup>9</sup>	10 s
	P <sub>3</sub>	4 GHz	90 × 10 <sup>9</sup>	9 s
b.	P <sub>1</sub>	2 GHz	20 × 10 <sup>9</sup>	5 s
	P <sub>2</sub>	3 GHz	30 × 10 <sup>9</sup>	8 s
	P <sub>3</sub>	4 GHz	25 × 10 <sup>9</sup>	7 s

1.3.4 Find the IPC (instruction per cycle) for each processor

$$\text{CPU execution} = \frac{\text{No. Instr} \times \text{CPI}}{\text{clock rate}}, \quad \text{IPC} = \frac{1}{\text{CPI}}$$

$$\text{CPI} = \frac{\text{CPU execution} \times \text{clock rate}}{\text{No. Instruction}}$$

$$\text{IPC} = \frac{\text{No. Instruction}}{\text{CPU execution} \times \text{clock rate}}$$

a

$$P_1 = \frac{20}{7 \times 3} = 0.95$$

$$P_2 = \frac{30}{10 \times 2.5} = 1.2$$

$$P_3 = \frac{90}{9 \times 4} = 2.5$$

b

$$P_1 = \frac{20}{5 \times 2} = 2$$

$$P_2 = \frac{30}{8 \times 3} = 1.25$$

$$P_3 = \frac{25}{7 \times 4} = 0.9$$

1.3.5 Find the clock rate for P2 that reduces its execution time to that of P1

$$\text{CPU execute time} = (\text{No. instr} \times \text{CPI}) / \text{Clock rate}$$

But you want to find new clock rate of P2 so it will be

$$\text{CPU execute P2} = (\text{No. instr P2} \times \text{CPI P2}) / \text{clock rate P2}$$

$$\text{CPU execute P1} = (\text{No. instr P1} \times \text{CPI P1}) / \text{clock rate P1}$$

to get clock rate

$$\frac{\text{Clock rate P1}}{\text{Clock rate P2}} = \frac{\text{CPU time P2} \times \text{No. instr P2} \times \text{CPI P2}}{\text{CPU time P1} \times \text{No. instr P2} \times \text{CPI P2}}$$

we will get

$$\text{Clock rate P1} = \frac{\text{CPU time P2}}{\text{CPU time P1}} \times \text{Clock rate P2}$$

$$a \quad \text{Clock rate P1} = \frac{10}{7} \times 2.5 = 3.57$$

$$b \quad \text{Clock rate P1} = \frac{8}{5} \times 3 = 4.8$$

1.3.6 Find the number of instructions for P2 that reduces its execution time to that of P1

$$\text{CPU execute} = (\text{No. instr} \times \text{CPI}) / \text{Clock rate}$$

Compare

$$\text{CPU execute P2} = \frac{(\text{No. Instr P2} \times \text{CPI P2})}{\text{Clock Rate P2}}$$

$$\text{CPU execute P3} = \frac{(\text{No. Instr P3} \times \text{CPI P3})}{\text{Clock Rate P3}}$$

We find P3 but use P2

$$\frac{\text{No. Instr P3}}{\text{No. Instr P2}} = \frac{(\text{CPU exe P3}) \times \text{CPI P2} / \text{Clock Rate P2}}{(\text{CPU exe P2}) \times \text{CPI P2} / \text{Clock Rate P2}}$$

$$\text{No. Instr P2} = \frac{(\text{CPU exe P3}) \times \text{CPI P2} / \text{Clock Rate P2}}{(\text{CPU exe P2}) \times \text{CPI P2} / \text{Clock Rate P2}}$$

we will get

$$\text{No. Instr P3} = \frac{\text{CPU exe P3}}{\text{CPU exe P2}} \times \text{No. Instr P2}$$

$$a \quad \text{No. Instr P3} = \frac{9}{10} \times 30 \times 10^9 = 27 \times 10^9$$

$$b \quad \text{No. Instr P3} = \frac{7}{8} \times 30 \times 10^9 = 26.25 \times 10^9$$



1.4. Consider two different implementations of the same instruction set architecture. There are 4 classes of instruction, A, B, C, D. Clock rate and CPI are given in following table

		clock rate	CPI A	CPI B	CPI C	CPI D
a	P1	2.5 GHz	1	2	3	3
	P2	3 GHz	2	2	2	2
b	P1	2.5 GHz	2	1.5	2	1
	P2	3 GHz	1	2	1	1

1.4.1 Given a program with  $10^6$  instructions divided into class

A  $\times 1.1$ , B  $\times 1.2$ , C  $\times 1.5$ , D  $\times 1.2$

$$\text{CPU execution time} = \frac{\sum (\text{number of instructions} \times \text{CPI})}{\text{clock rate}}$$

if it is the same instruction but implement it so it will be

$$\text{Class A } 10\% \text{ of } 10^6 = 1 \times 10^5$$

$$\text{Class B } 20\% \text{ of } 10^6 = 2 \times 10^5$$

$$\text{Class C } 50\% \text{ of } 10^6 = 5 \times 10^5$$

$$\text{Class D } 20\% \text{ of } 10^6 = 2 \times 10^5$$

$$a \quad P1 = \frac{(1 \times 10^5) + (2 \times 2 \times 10^5) + (3 \times 5 \times 10^5) + (3 \times 2 \times 10^5)}{2.5 \times 10^9} = 10.4 \times 10^{-4} \text{ s}$$

$$P2 = \frac{(2 \times 10^5) + (2 \times 2 \times 10^5) + (2 \times 5 \times 10^5) + (2 \times 2 \times 10^5)}{3 \times 10^9} = 6.66 \times 10^{-4} \text{ s}$$

Ans in set a P2 is faster than P1

$$b \quad P1 = \frac{(2 \times 10^5) + (1.5 \times 2 \times 10^5) + (2 \times 2 \times 10^5) + (1 \times 2 \times 10^5)}{2.5 \times 10^9} = 4.4 \times 10^{-4} \text{ s}$$

$$P2 = \frac{(1 \times 10^5) + (2 \times 2 \times 10^5) + (1 \times 5 \times 10^5) + (1 \times 2 \times 10^5)}{3 \times 10^9} = 4 \times 10^{-4} \text{ s}$$

Ans in set b P2 is faster than P1

1.4.2 What is the global CPI for each implementation

$$\text{CPU execution} = \frac{\text{No. Instruction} \times \text{CPI}}{\text{Clock rate}}$$

$$\text{CPI} = \frac{\text{CPU execution} \times \text{Clock rate}}{\text{No. Instruction}}$$

from previous problem we know CPU execution P1 is 10.4 and P2 is 6.66

$$\text{a } P1 = \frac{10.4 \times 10^{-9} \times 2.5 \times 10^9}{10^6} = 2.6$$

$$P2 = \frac{6.66 \times 10^{-9} \times 3 \times 10^9}{10^6} = 2.0$$

from previous problem we know CPU execution P1 is 4.4 and P2 is 4.0

$$\text{b } P1 = \frac{4.4 \times 10^{-9} \times 2.5 \times 10^9}{10^6} = 1.1$$

$$P2 = \frac{4 \times 10^{-9} \times 3 \times 10^9}{10^6} = 1.2$$

1.4.3 Find the clock cycles required in both case

$$\text{from CPU execution} = \text{No. instr} \times \text{CPI} \times \text{clock cycle}$$

$$\text{so clock cycles} = \frac{\text{CPU execution}}{\text{No. instr} \times \text{CPI}}$$

from previous we know CPU exe P1 is 10.4 and CPI P1 is 2.6, P2 is 2.0 CPI 1.2

$$\text{a } P1 \text{ clock cycle} = \frac{10.4 \times 10^{-9}}{10^6 \times 2.6} = 4 \times 10^2$$

$$P2 \text{ clock cycle} = \frac{6.66 \times 10^{-9}}{10^6 \times 2.0} = 3.33 \times 10^2$$

from previous we know CPU exe P1 is 4.4 CPI P1 is 1.1 CPU exe P2 is 4.0 CPI 1.2

$$\text{b } P1 \text{ clock cycle} = \frac{4.4 \times 10^{-9}}{10^6 \times 1.1} = 4 \times 10^2$$

$$P2 \text{ clock cycle} = \frac{4.0 \times 10^{-9}}{10^6 \times 1.1} = 3.6 \times 10^2$$



The following table shows the number of instructions for a program

	arith	store	load	Branch	Total
a	650	100	600	50	1400
b	750	200	500	500	2000

1.4.4 Assuming that arith instns take 1 cycle and store 5 cycles branches 2 cycle what is the execution time in 2 GHz processor

$$\text{CPU execution} = \frac{\text{CPU clock cycle}}{\text{clock rate}}$$

$$a = \frac{(650 \times 1) + (5 \times 100) + (5 \times 600) + (2 \times 50)}{2 \times 10^9} = 2,125 \times 10^3$$

$$b = \frac{(750 \times 1) + (5 \times 200) + (5 \times 500) + (2 \times 500)}{2 \times 10^9} = 2,750 \times 10^3$$

1.4.2 Find the CPI for the program

$$CPI = \text{CPU clock cycle} / \text{Instructions}$$

$$a \text{ CPI} = 4250 / 1400 = 3.04$$

$$b \text{ CPI} = 5500 / 2000 = 2.75$$

1.46 If number of load instructions can be reduced by one half find speed up and CPI

$$a \text{ new instruction} = 650 + 100 + (600/2) + 50 = 1100$$

$$\text{new clock cycle} = (650 \times 1) + (5 \times 100) + (5 \times 300) + (2 \times 50) = 2750$$

$$\therefore CPI = \frac{2750}{1100} = 2.5$$

$$\text{CPU execution} = \frac{1100 \times 2.5}{2 \times 10^{-9}} = 1375 \times 10^{-9}$$

$$\text{Speed up} = \frac{\text{CPU exe old}}{\text{CPU exe new}} = \frac{2125 \times 10^{-9}}{1375 \times 10^{-9}} = 1.5$$

$$b \text{ new instruction} = 750 + 250 + (500/2) + 500 = 1750$$

$$\text{new clock cycle} = (750 \times 1) + (250 \times 5) + (250 \times 5) + (500 \times 2) = 4250$$

$$CPI = \frac{4250}{1750} = 2.4$$

$$\text{CPU execution} = \frac{1750 \times 2.4}{2 \times 10^{-9}} = 2100 \times 10^{-9}$$

$$\text{Speed up} = \frac{\text{CPU exe old}}{\text{CPU exe now}} = \frac{2750 \times 10^{-9}}{2100 \times 10^{-9}} = 1.3$$