

DLS Lab Seminar

Octavio A. Villarreal Magaña

Istituto Italiano di Tecnologia, Genova, Italy

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Outline

- ① Control structure
- ② Numeric simulations
- ③ Further work

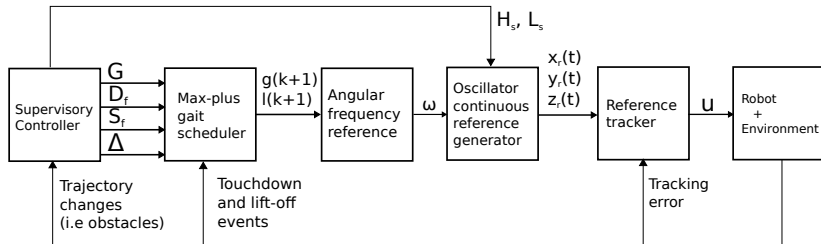
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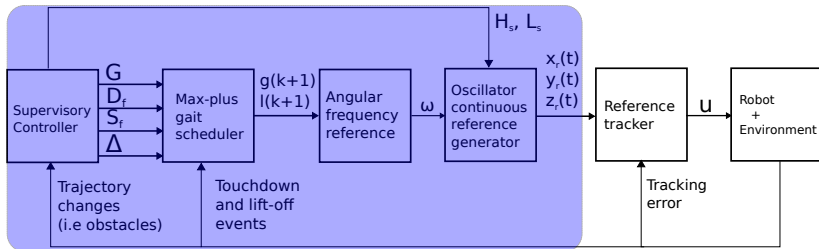
Motivation

- Provide versatility to the types of gaits that the robot can perform
- Have a unified and systematic way to generate motions of the legs according to the scenario
- Can be applied to other legged systems

General picture



General picture



Supervisory controller

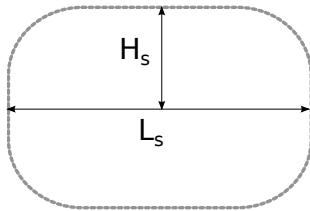
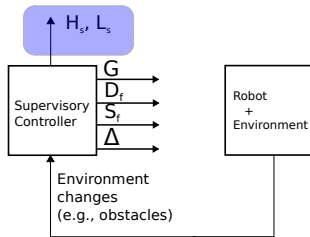
Main goal

Provide **geometrical** and **time** gait parameters, based on sensory data, to overcome the scenario that the robot is facing.

Supervisory controller (continue)

Geometrical parameters:

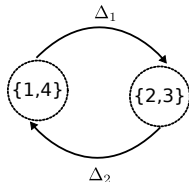
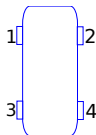
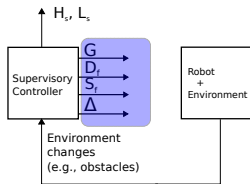
- Step height H_s
- Step length L_s
- Oscillator "primitive" shape changes



Supervisory controller (continue)

Time parameters:

- Duty factor D_f
- Step frequency S_f
- Gait parameterization G
(e.g.,
 $G_{trot} = \{1, 4\} \prec \{2, 3\}$)
- Time difference vector Δ

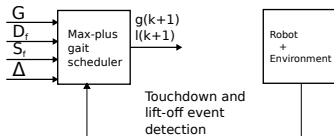


Max-plus gait scheduler

Main goal

Using the **time**-related gait parameters provided by the supervisory controller, generate the list of time-instants when each leg has to leave and touch the ground, so that a desired coordination is achieved.

Max-plus gait scheduler (continue)

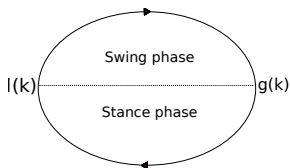


$$G_{trot} = \{1, 4\} \prec \{2, 3\}$$

$$D_f = 0.58$$

$$S_f = 0.42$$

$$\Delta = [0.2, 0.2]$$



| k | $g_1(k)$ | $g_2(k)$ | $g_3(k)$ | $g_4(k)$ | $l_1(k)$ | $l_2(k)$ | $l_3(k)$ | $l_4(k)$ |
|-----|----------|----------|----------|----------|----------|----------|----------|----------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 2.4 | 3.6 | 3.6 | 2.4 | 1.4 | 2.6 | 2.6 | 1.4 |
| 2 | 4.8 | 6 | 6 | 4.8 | 3.8 | 5 | 5 | 3.8 |
| 3 | 7.2 | 8.4 | 8.4 | 7.2 | 6.2 | 7.4 | 7.4 | 6.2 |
| 4 | 9.6 | 10.8 | 10.8 | 9.6 | 8.6 | 9.8 | 9.8 | 8.6 |
| 5 | 12 | 13.2 | 13.2 | 12 | 11 | 12.2 | 12.2 | 11 |

Max-plus gait scheduler (continue)

- Systematic gait generation
- No coupling matrix \mathbb{C}_{ij}
- Total cycle time analysis (max-plus eigenvalues of A matrix in $x(k+1) = A \otimes x(k)$)
- Coupling time analysis ("settling time")
- Not computationally expensive
- Possibility to provide "optimal" gait switching

Angular frequency reference generator

Main goal

Making use of the **touchdown** and **lift-off** times of the max-plus gait scheduler, provide a function for the evolution of the angular frequency of the oscillator-based reference generator.

Angular frequency reference generator (continue)

Stance and swing period:

$$Ti_{st} = l_i(k+1) - g_i(k)$$

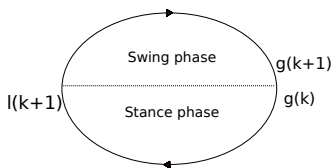
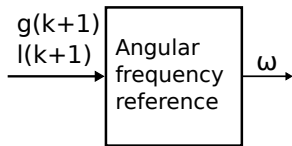
$$Ti_{sw} = g_i(k+1) - l_i(k+1),$$

Average angular frequency:

$$\bar{\omega} = \begin{cases} \frac{\pi}{Ti_{st}} & \text{for } t \in [g_i(k), l_i(k+1)] \\ \frac{\pi}{Ti_{sw}} & \text{for } t \in (l_i(k+1), g_i(k+1)] \end{cases}$$

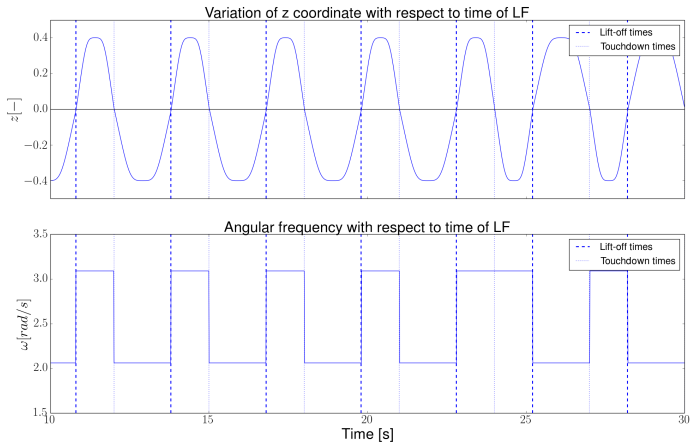
Condition for the angular frequency function:

$$\frac{1}{Ti_p} \int^{Ti_p} \omega dt = \bar{\omega} \text{ for } p = st, sw.$$



Angular frequency reference generator (continue)

$$\omega = \bar{\omega}$$



Oscillator continuous time reference generator

Main goal

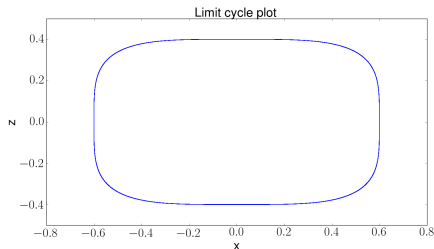
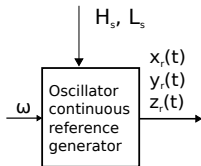
Generate reference trajectories for each of the legs of the robot in such a way that the desired gait is achieved, according to the angular frequency obtained from the angular frequency reference generator.

Oscillator continuous time reference generator (continue)

Oscillator equations:

$$\dot{x} = \alpha \left(1 - \frac{16x^4}{L_s^4} - \frac{z^4}{H_s^4} \right) x + \frac{1.18\omega L_s}{2H_s^3} z^3$$

$$\dot{z} = \beta \left(1 - \frac{16x^4}{L_s^4} - \frac{z^4}{H_s^4} \right) z - \frac{9.44\omega H_s}{L_s^3} x^3$$



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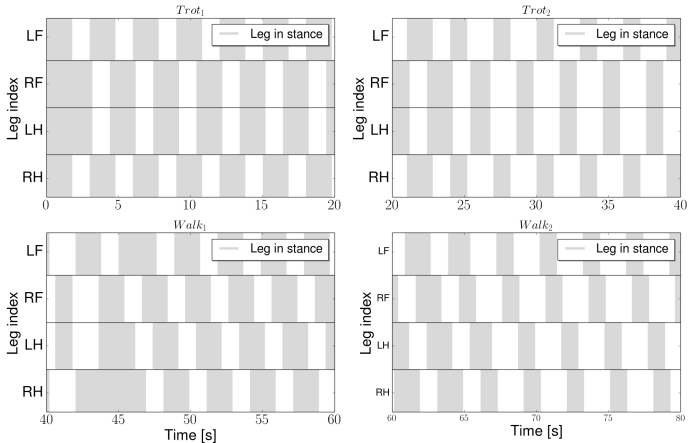
Parameters used

Switch between four different sets of gait parameters:

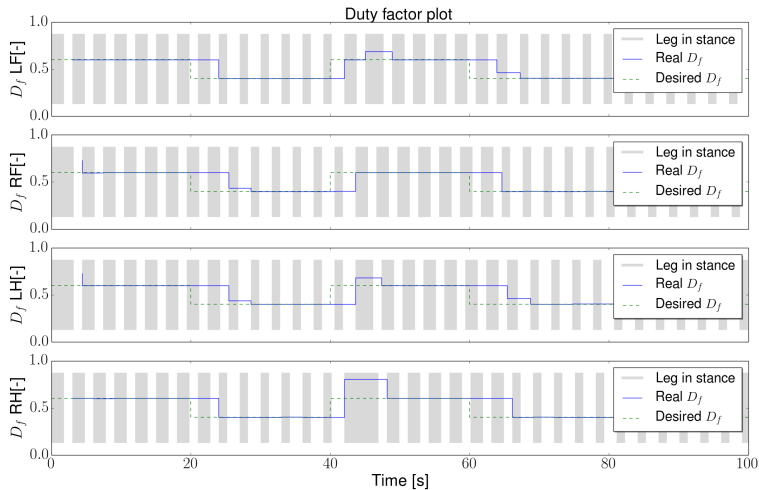
| | G | D_f | $S_f[\frac{1}{s}]$ | $\Delta[s]$ |
|-------|---------------------------------------------|-------|--------------------|--------------------------------|
| T_1 | $\{1, 4\} \prec \{2, 3\}$ | 0.6 | 1/3 | $[0.2, 0.4]$ |
| T_2 | $\{1, 4\} \prec \{2, 3\}$ | 0.4 | 1/3 | $[-0.2, -0.4]$ |
| W_1 | $\{1\} \prec \{2\} \prec \{3\} \prec \{4\}$ | 0.6 | 1/3 | $[-0.45, -0.45, -0.45, -0.45]$ |
| W_2 | $\{1\} \prec \{2\} \prec \{3\} \prec \{4\}$ | 0.4 | 1/3 | $[-1.4, -0.7, -1.4, -0.7]$ |

Generated motion references

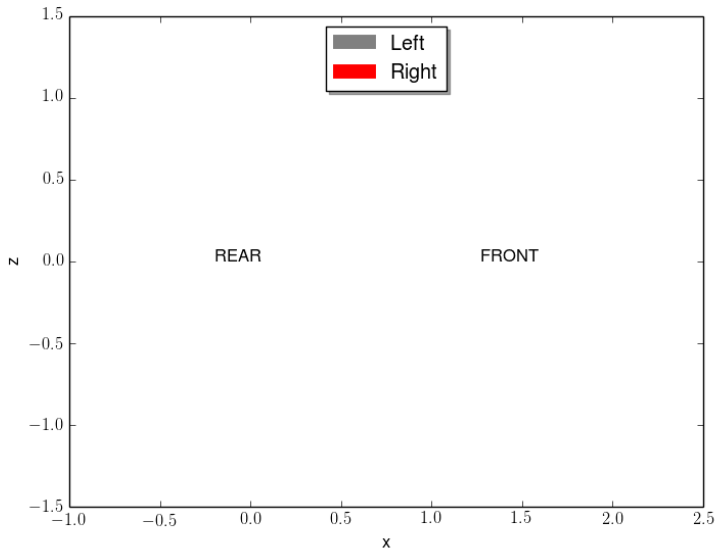
Plots for gaits with different parameters



Duty factor



Animation



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Further work

- Use the proposed strategy in the current framework
- Design angular frequency generator
- Account for disturbances in the max-plus algebra gait scheduler
- Design of supervisory parameters according to sensory information
- Design transition between one set of parameters to another

Thank you. Questions or comments?