Scalable Online-Offline Stream Clustering in Apache Spark

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Abstract—Two of the most popular strategies to mine big data are distributed comput- ing and stream mining. The purpose of this thesis is to incorporate both together bringing a competitive stream clustering method into a modern framework for distributed computing, namely, Apache Spark. The method in question is CluS- tream, a stream clustering method which separates the clustering process into two different phases: an online phase which handles the incoming stream, generating statistical summaries of the data and an offline phase which takes those summaries to generate the final clusters. These summaries also contain valuable information which can be used for further analysis. The main goal is to adapt this method in such a framework in order to obtain a scalable stream clustering method which is open source and can be used by the Apache Spark community.

Keywords-big data streams; stream mining; stream clustering; CluStream

I. INTRODUCTION

The analysis of data streams comes along with important questions: what kind of data is it? What important information is contained in it? How does the stream evolve? The key question for this project among those is the latter, i.e. dealing with the evolution of the stream, because prior to the development of the CluStream [8] method there was not an easy to answer that question as it was one of the first to tackle this issue.

Clustering is one of the main tasks in data mining, also often referred as an exploratory subtask of it. As the name implies, the objective is to find clusters, i.e., collections of objects that share common properties. One can also relate this task to unsupervised machine learning, which intends to classify data when it lacks of labels, i.e., when the data instance does not indicate to which category it belongs. The CluStream method was developed in 2003 [8] and its main purpose is to pro- vide more information than previously developed algorithms for data stream clus- tering by that time. It provides a solution for handling streams of data indepen- dently from the one that finds the final clusters. It consists of two phases (passes) instead of one; the first one deals with the incoming data and stores relevant information over time and the second one is in charge of the clustering using the previously generated information.

II. RELATED WORK

CluStream has been implemented in different types of software and libraries, being SAMOA - Scalable Advanced

Massive Online Analysis one of the options. It is also a distributed computing implementation of the algorithm. The difference is that it is not implemented in *Spark*, but rather in a *Distributed Stream Processing Engine* which adapts the *MapReduce* approach to parallel stream processing [17].

Main differences with this adaptation:

- It does not include an offline macro-clustering phase.
- It is developed in Java and not designed to work with Spark.

StreamDM is a collection of algorithms for mining big data streams ¹. One of the included methods for stream clustering is *CluStream*. This collection of algorithms is developed for Spark.

Main differences with this adaptation:

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III. BASIC CONCEPTS

A. CluStream

Clustream is a method developed in the Watson Research Center at IBM and the University of Illinois, UIUC. This method presented a different approach on the matter of clustering streams of data with respect to a modified version of *K-Means* which was adapted to work also with data streams. The main difference relies on the separation of the clustering process into two parts: one which would handle the data stream itself gathering only statistically relevant information (online part) and another which actually process the results of the former to produce the actual clusters wanted (offline part).

Separating the clustering process provides the user several advantages, among others:

- by saving only statistical data, rather than the original content, it is possible to save physical storage space (e.g. hard drive space) and therefore reducing costs and allowing a wider range in time to be clustered.
- The method also allows the analysis of the evolution of the data, as the necessary information for that is contained in the stored statistical information.
- Because the two parts operate independently it allows the user to select a time horizon, or even a time window, to perform the offline clustering part using the stored statistical information.

¹As it is stated by them here: http://huawei-noah.github.io/streamDM/

- 1) The CluStream framework: This method is built over a few ideas that need to be conceptualized, which will answer fundamental questions and set up a basis of terminology useful along this work.
 - Micro-Clusters: that is the given name for the statistical information summaries that is computed during the online component. They are a temporal extension of *cluster feature vectors* [18], which benefit from an additive feature that makes them a natural choice for the data stream problem [8].
 - Pyramidal time frame: micro-clusters are stored periodically following a pyramidal pattern. This allows a nice tradeoff between the ability to store large amounts of information while giving the user the possible to work with different time horizons without loosing too much precision. The statistical summaries stored are used by the offline component to compute finally the macro-clusters which are the actual clusters the user intended to get.
- 2) Maintaining the micro-clusters: Whenever a new point arrives, it is necessary to find its nearest micro-cluster. It is possible to calculate an average radious or RMSD, only to then compare the distance to the point to a factor of it: when the distance between a point and its nearest micro-cluster is smaller or equal to the average radiuos (of the micro-cluster in question) times a user defined factor, then this point is added to the micro-cluster. Adding a point to a micro-cluster means that the properties of the micro-cluster change, such as RMSD and size (number of points).

Whenever a point (outlier) does not fulfill the mentioned condition, then a new micro-cluster has to be created in order to give this point a chance as a potential new cluster. In order to do so, an older micro-cluster has to be deleted or two micro-clusters have to be merged. To determine which solution is appropriate a recency value for each micro-cluster has to be determined² and until all the micro-clusters which have an older recency value than a user specified parameter are deleted, it is possible to start merging the micro-clusters which are closest to one another.

3) Offline macro-clusterig: The macro-clustering part is done by selecting a time window and then performing a modified version of *K-Means* to cluster the center of the current micro-clusters using the size as weights.

B. SPARK

Apache Spark is an open source framework developed in the AMPLab at the University of California. Traditionally, MapReduce and DAG engines are based on an acyclic data flow, which makes them non optimal for these applications listed above. In this flow, data has to be read from a stable storage system, like a distributed file system, and then processed on a series of jobs only to be written back to the stable storage. This process of reading and writing data on each step of the workflow causes a significant rise in computational cost.

The solution proposed offers *resilient distributed datasets* (*RDDs*) to overcome this issue efficiently. RDDs are stored in memory between queries (no need of replication) and they can rebuild themselves in case of failure as they remember how they were originally built from other datasets by transformations such as *map*, *group*, *join*.

C. SPARK streaming



Figure 1: Flow of data in Spark streaming

Figure 1 shows the general idea of Spark streaming [4], a raw stream is linked to this module and it converts it to batches of data at user-defined intervals. These batches of data are then treated as RDDs, thus it gets distributed over the cluster where Spark runs. The abstraction of a data stream in Spark is called *DStream*, which stands for Discretized Stream, and is continuous series of RDDs. In a *DStream*, each RDD contains data from a specific interval of time, as it can be seen in Figure 2.



Figure 2: DStreams are Spark streaming's abstraction of a data stream

IV. CLUSTREAM IN APACHE SPARK

There are some modifications which had to be done in order to adapt *CluStream* in Spark. Working with Spark means worrking distributed computing and, thus, the algorithm has to be able to work in parallel. Both parts (online and offline) were adapted.

A. CluStreamOnline class (online phase)

Two processes were modified: processing the stream and updating the micro-clusters. As this adaptation uses Spark Streaming, the points coming from the stream are processed in batches at user specified time intervals. This contrasts with the original methodology which indicates to process point by point.

²See [8] for more details.

1) Finding nearest micro-cluster: The maintenance of the micro-clusters starts with this operation. After initialization (described in [8]) is performed, finding the nearest micro-clusters for all the points is the very first thing to be done for every new batch of data.

Algorithm 1 Find nearest micro-cluster.

Input: rdd: RDD[breeze.linalg.Vector[Double]], mcInfo: Array[(McI,Int)]— rdd is an RDD containing data points and mcInfo is the collection of the micro-clusters information.

Output: *rdd: RDD[(Int, breeze.linalg.Vector[Double])]* — returns a tuple of the point itself and the unique ID of the nearest micro-cluster.

```
1: for all p \in rdd do
        minDistance \leftarrow Double.PositiveInfinity
 2:
 3:
        minIndex \leftarrow Int.MaxValue
        for all mc \in mcInfo do
 4:
           distance \leftarrow squaredDistance(p, mc_1.centroid)
 5:
           if distance < minDistance then
 6.
               minDistance \leftarrow distance
 7:
               minIndex \leftarrow mc_2
 8:
           end if
 9:
        end for
10:
        p = (minIndex, p)
11:
12: end forreturn rdd
```

Finding the nearest micro-clusters is an operation of complexity O(n*q*d), where n is the number of points, q the number of micro-clusters and d the dimension of the points; q and d remain constant during runtime but n might vary. Algorithm 1 describes a simple search for the minimum distance for every point in the RDD to the micro-clusters. This is also a good opportunity to show how this works using Spark and Scala:

```
def assignToMicroCluster(rdd: RDD[Vector[Double]],
1
         mcInfo: Array [(MicroClusterInfo, Int)]): RDD
        [(Int, Vector[Double])] = {
        rdd.map { a =>
          var minDist = Double. PositiveInfinity
3
4
          var minIndex = Int.MaxValue
5
          for (mc <- mcInfo) {
            val dist = squaredDistance(a, mc._1.
6
                centroid)
7
            if (dist < minDist) {
8
              minDist = dist
              minIndex = mc._2
10
11
          (minIndex, a)
12
        }}
```

Spark uses this map operation to serialize the function passed so that all nodes in the cluster get the same instruction, this is exactly how computations are parallelized within this framework. At this point, every node performs

this operation to find the nearest micro-cluster for all the points they locally have.

- 2) Processing points: The points are separated in two: points within micro-clusters and outliers, it is possible to compute the necessary information from them to update the micro-clusters. It is important to perform this step before handling the outliers because this adaptation process the points for batches of data and not points individually as they arrive, and the reasons are:
 - Every point in a batch is treated equally in terms of temporal properties as this batch gets distributed among the cluster with the same time stamp and there is no constant communication among nodes.
 - The process of handling outliers involves deleting and merging micro-clusters for every outlier, modifying the micro-clusters' structure. A sequential implementation was preferred to reduce communication costs.

These two points are some of the key differences between the original CluStream method and this adaptation. For the original, it is possible to handle point by point as each have different clear time stamps.

- 3) Handling outliers: First the micro-clusters which are safe to delete are determined, then the outliers can be handled. In general, there are three possible scenarios for outliers:
 - If the point lies within the restriction regarding the RMSD for its nearest micro-cluster in the array newMicroClusters, the point is added to it. This stores all newly created micro-clusters.
 - If the point does not lie within any of the new microclusters, then it replaces a micro-cluster from the safeDelete array, while there are safe-to-delete microclusters.
 - If none of the previous scenarios are viable, then the two micro-clusters that are closest to each other get merged, freeing one spot to create the new micro-cluster. This is the the most computationally expensive scenario. The function getTwoClosestMicroClusters() has a complexity of $O(p_md \cdot \frac{q!}{2!(q-2)!})$, where p_m is the number of outliers that require a merge, d the dimension of the points, and q the number of micro-clusters.

It is important in the procedure described in Algorithm 2 to locally update the mcInfo every time a point is added to a micro-cluster, two micro clusters are merged and when a new micro-cluster is created. There could be a lot of change, depending on the outliers, and this loop requires up-to-date information for each iteration, otherwise merges and the RMSD check would be inaccurate.

B. CluStream class (offline phase)

Using a *weighted K-Means* approach, as described in [8] was not directly possible, and for that reason, a new adaptation had to be done in order to achive similar results.

Algorithm 2 handle outliers.

```
1: i \leftarrow 0
2: for all p \in dataOut do
       distance, mcID \leftarrow
   qetMinDistanceFromIDs(newMicroClusters, p_2)
       if distance < t * mcInfo[mcID]_1.rmsd then
4:
           addPointToMicroCluster(mcID, p_2)
5:
       else
6:
7:
          if safeDelete[j].isDefined then
              replaceMicroCluster(safeDelete[j], p_2)
8:
              newMicroClusters.append(i)
9:
              j \leftarrow j + 1
10:
11:
          else
              index1, index2 \leftarrow
12:
   getTwoClosestMicroClusters(keepOrMerge)
              mergeMicroClusters(index1, index2)
13:
              replaceMicroClusters(index 2, p_2)
14:
15:
              newMicroClusters.append(j)
              j \leftarrow j + 1
16:
          end if
17:
       end if
18:
19: end for
```

The fakeKMeans solution:

The original *CluStream* method suggests to use a slightly modified version of K-Means, a version for which one can initialize the seeds (initial clusters) by sampling from the micro-clusters' centroids taking into account the number of points each micro-cluster has and for which one can use these centroids as weighted input points. These weights, again, are related to the number of points they absorbed. Spark's (current) implementation of K-Means does allow to initialize the seeds but unfortunately it is not possible to predefine the weights for the input points.

In order to solve this issue, a new version of K-Means needs to be implemented. This version uses, in fact, Spark's own version, but to overcome the problem of not being able to define the weights at the beginning, this new version uses as input many points sampled from the micro-clusters' centroids.

V. EXPERIMENTS

A. Experiments setting

For the experiments we used the Network Intrusion dataset³, which consists of 494,021 instances. For the analysis, we used only the numerical attributes (#34 out of #43 attributes). We vary the speed of the stream and the horizon and we derive two different stream configurations. The first one, denoted as DS1, has a speed v=2,0000 points per timestamp, which implies that it lasts for $\frac{494,021}{2.000} \approx 247$

time units, and a horizon H=1. The second one, denoted as DS2, has a speed of v=200 points per timestamp, thus lasting for a period of $\frac{494021}{200}\approx 2470$ time points, and a horizon H=256. To evaluate the clustering quality, we report in Section V-B on the sum of square distances (SSQ) from the points to their nearest micro-cluster, using Euclidean distance as the distance function, within a horizon H. Efficiency and scalability is discussed in Section V-C.

B. Clustering quality

We first compare *CluStream-Spark* to the original *CluStream* (Section V-B1) and then against other stream clustering approaches in Spark (Section V-B2).

1) Quality of Spark — CluStream vs original CluStream:

Results for DS1: The SSQ for DS1 is shown in Figure 9 for the original CluStream and our Spark-CluStream. We used the same parameters as in [8], i.e., $\alpha=2, l=10, InitNumber=2000, \delta=512, t=2$. The parameter m, for m last points, was the only one not provided, we set it to m=20. m is used to determine the approximate recency value as if the time of arrival of the last m points was averaged. For DS1, both m and δ are irrelevant and the reason is that the threshold is never reached (247 time units vs. 512). The number of microclusters was set to q=50, 10 times the number of final clusters (5).

In Table I we show the SSQ scores for our *CluStream-Spark* and the results from *CluStream* as reported in [8] - these are approximate results "extracted" from the original paper. Although we don't know the exact values for *CluStream*, we can see that the magnitudes of the average SSQ are comparable.

Results for DS2: Parameters were set as for DS1. The exact scores of CluStream-Spark and the approximate values from CluStream are reported in Table II. Again the quality scores are comparable, i.e., our CluStream-Spark achieves similar quality clusterings to the original CluStream.

2) Spark-CluStream vs other clustering approaches in SPARK: We compare our CluStream-Spark against available solutions for stream clustering in Spark and in particular againstStreaming K-Means ⁴ andStreamDM-CluStream ⁵. We report here on their clustering quality, the efficiency issue is discussed in Section V-C.

We roughly overview these methods hereafter.

- Streaming K-Means ⁶:
 - In order to have comparable results, the time horizon H must be interpreted differently. There are two strategies: the first option is to use the

³Source: http://kdd.ics.uci.edu/databases/kddcup99/kddcup99.html

⁴More information: https://databricks.com/blog/2015/01/28/introducing-streaming-k-means-in-spark-1-2.html

⁵More information: http://huawei-noah.github.io/streamDM/

 $^{^6\}mathrm{More}$ information: https://databricks.com/blog/2015/01/28/introducing-streaming-k-means-in-spark-1-2.html

DS1 - avg SSQ	10k	40k	160k	320k
CluStream	$10^5 - 10^6$	$10^{12} - 10^{13}$	$\approx 10^6$	$10^2 - 10^3$
Spark-CluStream	3.099×10^{5}	6.676×10^{12}	7.833×10^{5}	4.191×10^{2}

Table I: DS1 - Average SSQ values

DS2 - avg SSQ	150k	250k	350k	450k
CluStream	$10^{13} - 10^{14}$	$\approx 10^5$	$10^{12} - 10^{13}$	$\approx 10^8$
Spark-CluStream	5.402×10^{13}	5.143×10^4	1.892×10^{13}	9.646×10^{7}

Table II: DS2 - Average SSQ values

parameter halfLife, which can be configured to let the algorithm to completely adjust the clusters after HL points or batches.

The alternative would be to set the decayFactor, which sets the weight for the clusters of the "old" data (only the current batch is considered "new" data). This is a number between 0 and 1, such that if it is 0 then only the clusters for "new" data determine the final clusters, if it is set to 1, then the clusters of past data will have the same influence on the final clusters. As it also considers the number of points, after some time "old" data will be considerably larger than new batches.

• StreamDM-CluStream 7:

– This adaptation of *CluStream* does not include the offline part as a separate module, meaning that it does not save snapshots and therefore it has to perform the macro-clustering process for every batch. This brings some limitations, the horizon H no longer has the same meaning: the δ parameter is used instead as an equivalent, relying on the micro-clustering part only and its ability to delete and create new micro-clusters.

Results on DS1: For the DS1 stream the results are shown in Figure 3. For Streaming K-Means, the horizon H=1 is transformed to halfLife=1,000 points, as the stream speed is 2,000 points. The decayFactor is set to 0, i.e., only the last 2,000 points will influence on the clusters. StreamDM-CluStream is set up with its default parameters, only changing the horizon to 1 and the number of microclusters to 50 to match those of CluStream-Spark. As we can see, our *CluStream-Spark* delivers results which are very close to those of Streaming K-Means, whereas Streaming K-Means with the decayFactor (DF) is the best. The surprising results come from StreamDM-CluStream, which is the worse among the tested methods, especially for the last two points, i.e., at 160k and 320k. To further investigate this, we conduct another experiment where we compare CluStream-Spark without snapshots against StreamDM-CluStream. The results are shown in Figure 4.

As we can see, CluStream-Spark outperforms StreamDM-

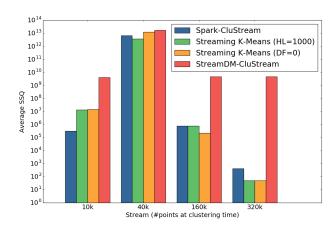


Figure 3: Average SSQ for different stream clustering methods in SPARK. DS1 (Stream speed v = 2,000, H=1)

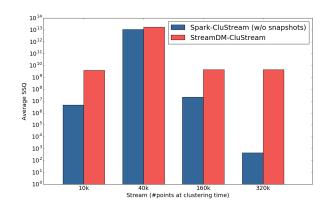


Figure 4: CluStream-Spark without snapshots vs StreamDM-CluStream. DS1 (Stream speed $v=2,000,\,H=1,\,m=100$).

CluStream even if we remove the snapshot part, but the quality is lower comparing to the snapshot version.

Results on DS2: For the DS2 stream the results are shown in Figure 5. All parameters remained the same for all methods, except for the halfLife parameter for Streaming K-Means, which is set to $halfLife = 25,600 (200 \cdot 256 = 51,200)$. We calculate the decayFactor as follows: At

⁷More information: http://huawei-noah.github.io/streamDM/

150,000 points, the ratio of the points to cluster to the total number of points at that particular time is $\frac{51,200}{150,000} \approx 0.3413$. At 250,000 points, this equals to $\frac{51,200}{250,000} \approx 0.2048$. At 350,000 points, this equals to $\frac{51,200}{350,000} \approx 0.1462$. At 450,000 points, this equals to $\frac{51,200}{450,000} \approx 0.1137$. Averaging those ratios leads to a *decayFactor* = 0.2015. As we can

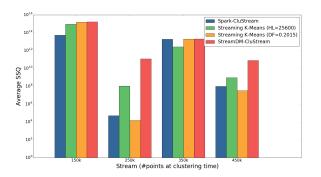


Figure 5: Average SSQ for different stream clustering methods in SPARK. DS2 (Stream speed v = 200, H=256)

see, CluStream-Spark performs consistently well and better than StreamDM-CluStream. As expected Streaming K-Means with the decayFactor achieves the best performance.

We repeat the without-snapshot experiment, the results are shown in Figure 6. As we can see, *CluStream-Spark* delivers

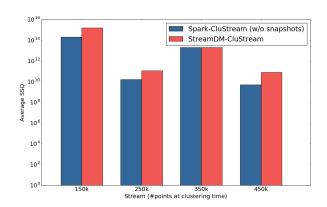


Figure 6: CluStream-Spark without snapshots vs StreamDM-CluStream. DS2 (Stream speed $v=200,\ H=256,\ m=100$).

better results than StreamDM-CluStream but the difference is reduced significantly comparing to DS1. These results might indicate that StreamDM-CluStream benefits from larger horizons.

C. Scalability

We test the scalability with respect to data dimensionality and number of microclusters, using data generated by a Random Radial Basis Function generator. The scalability tests are performed in two different scenarios: one being an analysis of how it scales for different number of attributes (dimensions of the data points) using only 20 micro-clusters and the other one using 200 micro-clusters as the number of attributes and the number of final clusters for a specific purpose are two key factors which determine the complexity of *Spark-CluStream*. The speed of the stream is controlled for 10000 points for every batch of data because it is easier to test the scalability when many computations have to be done. An application using Spark streaming assigns one core exclusively to handle the stream, therefore the number of processors mentioned in here is the total, but the real number of processors used for the computations is that number minus one.

Figure 7 shows that using only 20 micro-clusters and 2 dimensions has poor scalability, not even being able to perform twice as fast as for a single processor (2 in total). Even for this high speed streaming, one processor is enough to process the batches of data before a new batch is processed, meaning that the setup is stable.

Increasing the dimensionality of the points increases the computational effort needed to process the points in every batch of data and here is where *Spark-CluStream* shows its scalability, which is almost linear⁸ for up to 16-17 processors, as it can be seen in Figure 8. From the average processing time per batch, it can be seen that from 32 to 40 processors it does not improve much anymore and the speedup does not increase quasi-linearly anymore. Here a total of 9 processors were required to stabilize *Spark-CluStream*.

Interestingly, increasing the number of micro-clusters by a factor of 10 for 2 attributes resulted in good scalability, similarly to the scenario with 20 micro-clusters and 100 attributes. Here a total of 8 processors were enough for a stable run, as shown in Figure 9.

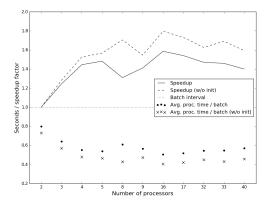
Finally, when the number of clusters and the number of attributes are both increased significantly, Figure 10 shows for *Spark-CluStream* quasi-linear scalability but this time only up to about 8-9 processors. After that point, the speedup slows down showing almost no improvement after 16 processors. This test never reached a stable configuration.

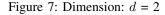
D. Performance

In this section, the scalability of Spark-CluStream is compared to that of StreamDM-CluStream and Spark's Streaming K-Means using the Spark cluster setup for q=20 and d=100, for the CluStream method. Also, a test on a single machine is performed.

When it comes to higher dimensions, Spark-CluStream shows a significant improvement over StreamDM-CluStream, which never got to the point were it was

 $^{^8\}mathrm{By}$ linear scalability does not mean it scales with a 1 to 1 ratio, but rather linearly proportional.





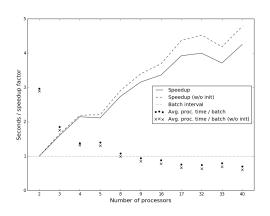


Figure 8: Dimension: d = 100

Scalability-dimensionality comparison for Stream speed = 10000 and q = 20

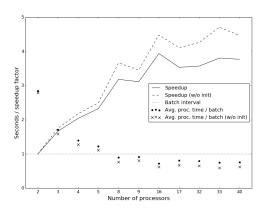


Figure 9: Dimension: d = 2

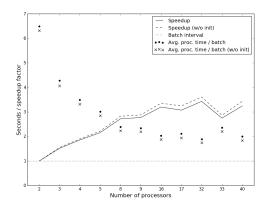


Figure 10: Dimension: d = 100

Scalability-dimensionality comparison for Stream speed = 10000 and q = 200

stable (below the 1 second mark), as shown in 11, it seems to scale as fast as *Spark-CluStream* but it was not enough even with 40 processors.

Another interesting comparison, is the processing time per batch of data for a single machine, using a real dataset such as the *Network Intrusion*. Here, communication is less of an issue as all the partitions lie in the same share memory space, and still there are 4 virtual cores in disposition for the algorithms to run.

The test was performed using a stream speed of 2000 points per batch and with a horizon H=1, to match one of the validation tests.

The results shown in Figure 12 are quite remarkable. As *StreamDM-CluStream* shows a very significant disadvantage when using greater numbers of micro-clusters and higher dimensions.

For this single machine test, *Spark-CluStream* was about 18 times faster on average than *StreamDM-CluStream* and

about two times slower than *Streaming K-Means* on average.

Another consideration to be made, is that *Spark-CluStream* saves a snapshot for every batch of data, having to write to disk, while the other two algorithms never access the disk for this matter.

VI. CONCLUSIONS

We proposed a variation of *CluStream* tailored to Apache Spark, *CluStream-Spark*. Our experiments show that *CluStream-Spark* achieves similar quality to the original approach [8], while it is far more efficient. Comparing to other stream clustering approaches in Spark, our results show that *Streaming K-Means* is the fastest algorithm among the three tested (highly optimized for Spark), but it does not offer the flexibility of the online-offline clustering approaches like *CluStream* that better fit evolving data streams. Comparing *CluStream-Spark* to *StreamDM-CluStream*, *CluStream-Spark* delivers more consistent and accurate re-

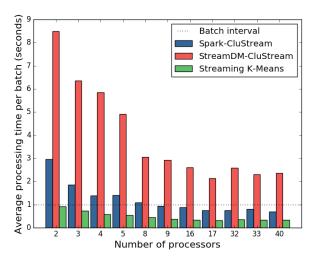


Figure 11: Processing time comparison: q = 20, d = 100

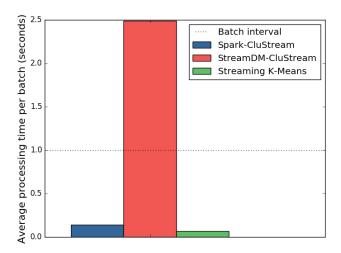


Figure 12: Processing time comparison for a single machine: q = 50, d = 34

sults, and outperforms *StreamDM-CluStream* in most cases, including one up to around 18 times faster.

As part of our future work, we will focus on minimizing the communication cost between the different nodes to further improve the efficiency and also on dealing with outliers to improve quality.

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