#### PANEL DATA METHODS

### Ozan Bakış<sup>1</sup>

<sup>1</sup>Bahcesehir University, Department of Economics and BETAM

## Outline

1 Panel data methods

#### Definitions I

- A panel (longitudinal) data set consists of observations of one or several variables over time. We can think it as many time series data set One ofr each cross-sectional unit).
- The best way to store panel data is to stack the time periods for each *i* on top of each other. In particular, the time periods for each unit should be adjacent, and stored in chronological order (from earliest period to the most recent). This is sometimes called the "long" storage format. It is by far the most common.
- We can use both plm and fixest packages to estimate panel data methods. The first thing to do is to convert the usual data (data.frame in R language) into panel data (pdata.frame)

```
library("plm")
pdat = pdata.frame(my_data, index=c("id_var","time_var"))
library("fixest")
feols( ..., panel.id =c("id_var","time_var"))
```

### **Definitions II**

where  ${\tt id\_var}$  and  ${\tt time\_var}$  are, respectively, unit and time identifiers.

#### Unobserved effects model I

 An unobserved effects model (or a fixed effects model) can be written as:

$$y_{it} = \beta_0 + \lambda_t + \beta_1 x_{1it} + \beta_2 x_{2it} + \dots + \underbrace{a_i + u_{it}}_{v_{it}}$$

where  $\lambda_t$  is a shorthand for all year dummies:  $\delta_0 year_2 + \delta_1 year_3 \dots$ 

- $v_{it}$  is the composite error term consisting of a time-constant  $(a_i)$  and a time-variable component  $(u_{it})$ . Usually, the last one is known as the "idiosyncratic shock".
- the *unobserved effect*  $(a_i)$  is the main reason of *unobserved heterogeneity*. It represents all factors that are constant but unobservable to the econometrician.

### Two-period panel data analyis I

- Consider the following example where we have unemployment and crime rates data for two years (1982, 1987) for 46 cities in USA (crime2.rds).
- We want to know whether an increase in unemployment rate in a city causes an increase in crime rates. The unemployment rate is in percent and crime rate is measured as the number of crimes per 1000 people.

```
url = "https://github.com/obakis/econ_data/raw/master/crime2.rds"
download.file(url, "crime.rds", mode = "wb")
crime = readRDS("crime.rds")
```

A basic model that can be used is

$$crmrte_{it} = \beta_0 + \delta_0 d87_t + \beta_1 unem_{it} + v_{it}, \quad t = 1, 2.$$

### Two-period panel data analyis II

• The above model is called a pooled OLS (POLS) model. The variable  $d87_t$  is a constructed time dummy for the second time period:  $d87_t = 1$  if year = 1987 and  $d87_t = 0$  if year = 1982. This model does not use the "panel data" characteristics.

• The coefficient on unemployment is positive but not significant. When we have multiple years, we need to use year dummies to allow changing intercepts (control for common macro shocks) to get a good estimate of a causal effect

# Two-period panel data analyis III

- It is likely that  $\hat{\beta}_1$  is still biased because of unobserved city characteristics that are correlated with unemployment (such as migration, temperature etc.) so that  $Cov(unem_{it}, v_{it}) \neq 0$ .
- If there are unobserved factors making  $Cov(unem_{it}, v_{it}) \neq 0$ , then we have omitted variables problem, and OLS estimates are biased!
- Let  $a_i$  be a city specific unobserved factor that is time constant. And assume that it is correlated both with unemployment and crime rates. Given that in the above regression, naturally  $a_i$  is part of the error term, we expect  $Cov(x_{it}, v_{it}) \neq 0$ .

### Two-period panel data analyis IV

• So, it would be better to decompose the *composite error* into two components  $v_{it} = a_i + u_{it}$  ( $a_i$ : unobserved fixed effect;  $u_{it}$ : idiosyncratic error) and specify an **unobserved** (or fixed) effects model:

$$crmrte_{it} = \beta_0 + \delta_0 d87_t + \beta_1 unem_{it} + \underbrace{a_i + u_{it}}_{v_{it}}$$

The estimate in the POLS model is likely to be biased because for unbiasedness we need  $Cov(x_{it}, v_{it}) = 0$  which requires

$$Cov(x_{it}, a_i) = 0$$
, and  $Cov(x_{it}, u_{it}) = 0$ 

 Even if the second one is respected, it is usually unreasonable to assume the first one. Because, usually we have city fixed unobserved effects that affect crime rates and are correlated with unemployment rate. In such situations, we say that POLS suffers from heterogeneity bias.

### Two-period panel data analyis V

• A first option to eliminate heterogeneity bias is estimate  $a_i$  along with other parameters. This is the same thing as estimating an intercept for each i, and is called **the dummy variable regression**:

$$crmrte_{it} = \underbrace{\theta_i}_{\beta_0 + a_i} + \delta_0 d87_t + \beta_1 unem_{it} + u_{it}$$

In practice, for *n* cross-sectional units we need to use n-1 dummy variables to estimate  $\theta_i$ .

• **Important:** Since  $a_i$  is modeled as a covariate we need only  $Cov(x_{it}, u_{it}) = 0$  to get unbiased estimates.  $Cov(x_{it}, a_i) \neq 0$  is allowed in this model!

```
crime$id = rep(1:46, each=2) # create panel id which is missing
dvr = lm(crmrte ~ factor(id) + d87 + unem, data=crime)
summary(dvr)$coef[c(1:3,45:48),]
```

### Two-period panel data analyis VI

```
##
              Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                51.49
                         12.346 4.171 0.00014
## factor(id)2 17.29 14.195 1.218 0.22967
## factor(id)3 4.69 14.239 0.329 0.74351
## factor(id)45
               -17.75 14.178 -1.252 0.21713
## factor(id)46
               -3.28 14.517 -0.226 0.82244
## d87
                15.40 4.702 3.276 0.00206
## unem
                 2.22
                          0.878 2.527 0.01519
librarv("fixest")
dvr2 = feols(crmrte ~ unem + i(year) | id,
           panel.id = c("id", "year"),
           data=crime. vcov="iid")
summary(dvr2)
```

### Two-period panel data analyis VII

```
## OLS estimation, Dep. Var.: crmrte
## Observations: 92
## Fixed-effects: id: 46
## Standard-errors: IID
           Estimate Std. Error t value Pr(>|t|)
##
## unem
        2.22 0.878 2.53 0.0151893 *
## year::87 15.40 4.702 3.28 0.0020605 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 9.80504 Adj. R2: 0.774292
                 Within R2: 0.196062
##
dvr3 = feols(crmrte ~ unem | id+vear.
            panel.id = c("id", "year"),
            data=crime. vcov="cluster")
summarv(dvr3)
```

### Two-period panel data analyis VIII

• If the explanatory variable changes over time, instead of estimating  $a_i$  directly using the model,  $y_{it} = \beta_0 + a_i + \delta_0 d2_t + \beta_1 x_{it} + u_{it}$ , a second option is to eliminate it:

$$y_{i2} = (\beta_0 + \delta_0) + \beta_1 x_{i2} + a_i + u_{i2}$$

$$y_{i1} = \beta_0 + \beta_1 x_{i1} + a_i + u_{i1}$$

$$\Rightarrow y_{i2} - y_{i1} = \delta_0 + \beta_1 (x_{i2} - x_{i1}) + (u_{i2} - u_{i1})$$

### Two-period panel data analyis IX

Or in first differenced form, also called estimating equation:

$$\Delta y_i = \delta_0 + \beta_1 \Delta x_i + \Delta u_i$$

where  $\Delta = change$  (or difference). Estimating the above yields the first-difference (FD) estimator. Differencing away  $a_i$ , is a powerful way of isolating causal effects. The key assumption for unbiasedness is  $Cov(\Delta u, \Delta x) = 0$  (strict exogeneity). Again  $Cov(x_{it}, a_i) \neq 0$  is allowed

**1** We can estimate the "estimating equation" directly by using lm function (by manually creating  $ccrmrte = \Delta crmrte, cunem = \Delta unem)$ 

Or alternatively using plm or fixest packages:

#### Two-period panel data analyis X

```
# librarv("plm")
# pdat = pdata.frame(crime, index=c("id","vear"))
# reg4 = plm(crmrte ~ d87 + unem, data=pdat, model="fd")
# summarv(reg4)$coef
reg5 = feols(d(crmrte) ~ d(unem) | year,
            panel.id = c("id","vear").
            data=crime. vcov="iid")
## NOTE: unitary time step taken: 5.
## NOTE: 46 observations removed because of NA values (LHS: 46. RHS:
46).
summarv(reg5)
## OLS estimation, Dep. Var.: d(crmrte, 1)
## Observations: 46
## Fixed-effects: year: 1
## Standard-errors: IID
           Estimate Std. Error t value Pr(>|t|)
##
## d(unem. 1) 2.22 0.878 2.53 0.015189 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 19.6 Adj. R2: 0.106852
```

# Two-period panel data analyis XI

## Within R2: 0.1267

- Now, we have a positive and statistically significant relationship between the crime and unemployment rates. Thus, differencing to eliminate time-constant effects makes a big difference in this example.
- When unemployment rate goes up by 1 percentage point, the number of crimes per 1000 people increases by 2.2.

# Returns to union membership and marriage I

- wagepan.rds: Working men from 1980 to 1987, so eight years. N=545. Use lwage as the dependent variable and standard panel data methods.  $lwage_{it} = \beta_0 + \beta_1 educ_{it} + \beta_2 exper_{it} + \beta_3 married_{it} + \beta_4 union_{it} + \delta_t + a_i + u_{it}$   $\delta_t$  refers to **set of year dummies**. Union status and marital status change over time. Education does not. Experience does, but if we know the experience in 1980 we know it in any other year (increases by one each year).
- While experience, union status and marital status change over time, race and education stay constant.

# Returns to union membership and marriage II

• We are likely to have two problems. First, unobserved effects are probably endogenous:  $Cov(\mathbf{X}_{it}, a_i) \neq 0$ . This implies that people that are married and have union membeship are likely to differ from others. Second, strict exogeneity is likely to fail:  $Cov(\mathbf{X}_{it}, u_{it}) \neq 0$ . Why are union status and marital status changing over time? Do shocks to wages contribute?

```
url = "https://github.com/obakis/econ_data/raw/master/wagepan.rds"
download.file(url, "wagepan.rds", mode = "wb")
wagepan = readRDS("wagepan.rds")
wagepan$f_year = factor(wagepan$year)
library("plm")
pdat = pdata.frame(wagepan, index=c("nr","year"))
library("fixest")
```

 One can use POLS for computing returns to marraige and union membership.

# Returns to union membership and marriage III

```
# reg_po = plm(lwage ~ educ + exper + black + union + married + f_year,
#
              data=pdat.
#
              model="pooling")
# summarv(reg po)$coef
reg po = feols(lwage ~ educ + exper + black + union + married | year.
              data=wagepan.
              panel.id = c("nr"."vear"), vcov="iid")
summarv(reg po)
## OLS estimation, Dep. Var.: lwage
## Observations: 4,360
## Fixed-effects: year: 8
## Standard-errors: TID
##
        Estimate Std. Error t value Pr(>|t|)
## educ 0.0923 0.00515 17.94 < 2.2e-16 ***
## exper 0.0304 0.00549 5.53 3.2982e-08 ***
## black -0.1400 0.02324 -6.02 1.8504e-09 ***
## union 0.1869 0.01710 10.93 < 2.2e-16 ***
## married 0.1109 0.01567 7.07 1.7557e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

# Returns to union membership and marriage IV

```
## RMSE: 0.480008 Adj. R2: 0.185341
## Within R2: 0.121537
```

But the estimate is likely to be biased. What about FD or FE?

# Returns to union membership and marriage V

```
## OLS estimation, Dep. Var.: d(lwage, 1)
## Observations: 3.815
## Fixed-effects: year: 7
## Standard-errors: Clustered (nr)
##
           Estimate Std. Error t value Pr(>|t|)
## d(union, 1) 0.0419 0.0219 1.91 0.056375 .
## d(married, 1) 0.0403 0.0242 1.67 0.096484 .
## ... 1 variable was removed because of collinearity (d(exper. 1))
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## RMSE: 0.442721 Adi. R2: 0.002494
                   Within Ro: 0.002004
##
# reg fe = plm(lwage ~ educ + exper + black + union + married + f vear.
              data=pdat.
#
              model="within")
# summary(reg fe)$coef
# reg fe2 = feols(lwage ~ educ+exper+black+union+married+f year|nr, data=wagepan,
                 panel.id = c("nr", "vear"))
#
# summary(reg_fe2)
```

# Returns to union membership and marriage VI

```
reg_fe = feols(lwage ~ educ + exper + black + union + married | nr + year,
              data=wagepan. panel.id = c("nr"."vear").
              vcov="cluster")
## The variables 'educ', 'exper' and 'black' have been removed because of
collinearity (see $collin.var).
summary(reg_fe)
## OLS estimation, Dep. Var.: lwage
## Observations: 4.360
## Fixed-effects: nr: 545, year: 8
## Standard-errors: Clustered (nr)
         Estimate Std. Error t value Pr(>|t|)
##
## union 0.0834 0.0231 3.62 0.0003279 ***
## married 0.0583 0.0213 2.73 0.0064602 **
## ... 3 variables were removed because of collinearity (educ. exper and black)
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 0.330217 Adj. R2: 0.559649
##
                   Within R2: 0.007635
```

# Returns to union membership and marriage VII

- Observable time-constant variables's coefficients are dropped (education and black). So we can not compute the level of the returns to education.
- exper is dropped for another reason. The reason is we can not separately identify / estimate the effect of exper and years in estimating equation of FD or FE. Both increases by one for every year in the sample. The starting points for exper are different across people but this is not distinguishable from the fixed effect, a<sub>i</sub>.

### Random effects estimator (RE) I

- What to do when  $x_{it}$  is constant such as education or race dummies?  $\Rightarrow$  If  $x_{it} = \bar{x}$  for each individual i and time t, we cannot estimate its coefficient using any of estimators we know: POLS, FD, FE. Actually, "no perfect collinearity" assumption (one of Gauss-Markov assumptions) rules out this.
  - $\Rightarrow$  If  $x_{it} = x_i$  for each time t this means that x differs across people but does not change over time for the same individual. Ex. gender or years of schooling for people who have completed their schooling. We will be limited in what we can learn in that case. In such cases we can not separate the effect of  $a_i$  on  $y_{it}$  from the effect of time-constant factors  $(x_i)$  and as a result we can not rely on FE or FD estimation.
- Any solution?
  - ⇒ No perfect solution: an improved version of pooled OLS: random effects estimator

### Random effects estimator (RE) II

- We already know that when  $Cov(x_{it}, a_i) = 0$ , we can use pooled OLS estimator. But, because of the presence of  $a_i$  in the composite error term  $v_{it} = a_i + u_{it}$ , we need to deal with serial correlation in the error term.
- To deal with the serial correlation described above, one solution is using generalized least squares (GLS). This is known as "random effects" (RE) estimation.
- Even if RE allows time constant covariates, it is crucial to keep in mind that RE rely on not only strict exogeneity with respect to u<sub>it</sub>:
   Cov(X<sub>is</sub>, u<sub>it</sub>) = 0 for s ≠ t but also exogeneity of fixed effects a<sub>i</sub>,
   Cov(X<sub>it</sub>, a<sub>i</sub>) = 0. This is likely to be wrong!
- For policy analysis, RE is typically less convincing than FD or FE: we want to allow  $X_{it}$  to be correlated with the time-constant factors in  $a_i$ .

### Random effects estimator (RE) III

- However, with good time-constant controls, RE may be convincing. This is because more is taken out of  $a_i$  as we add time-constant variables.
- The serial correlation in  $\{v_{it}\}$  ( $\rho$ ) is also known as intraclass correlation. It is the proportion of total variance in dependent variable that is due to  $a_i$ s.

$$Corr(v_{it}, v_{is}) = \frac{\sigma_a^2}{\sigma_a^2 + \sigma_u^2} \equiv \rho$$

• A useful characterization of RE is in terms of a "partially-time-demeaned" equation. It can be shown that for a given  $\theta(T,\rho)$ , that is between zero and one and increases with both  $\rho$  and T, Then RE estimate is obtained by regressing

$$y_{it} - \hat{\theta}\bar{y}_i$$
 on  $\mathbf{X}_{it} - \hat{\theta}\bar{\mathbf{X}}_i$ 

### Random effects estimator (RE) IV

 $y_{it} - \hat{\theta}\bar{y}_i$  and  $\mathbf{X}_{it} - \hat{\theta}\bar{\mathbf{X}}_i$  are "partially-time-demeaned" variables.

• We have the following

$$\hat{\theta} \rightarrow 0 \Rightarrow \hat{\beta}_{RE} \approx \hat{\beta}_{POLS}$$
 $\hat{\theta} \rightarrow 1 \Rightarrow \hat{\beta}_{RE} \approx \hat{\beta}_{FE}$ 

When  $\theta$  approaches 1, and RE converges to FE!

- Actually,  $\hat{\theta}$  is a measure for how much of the unobserved effect  $a_i$  we are extracting from the error term, during the estimation. If  $\theta$  goes to zero we are leaving a large part in the error term and as a result the bias of the RE estimator will be larger.
- While POLS leaves  $a_i$  entirely in the error term; FE (or FD) remove it completely and RE leaves it partially in the error term.

### Random effects estimator (RE) V

```
reg po = feols(lwage ~ educ + exper + black + union + married | year,
              data=wagepan,
              panel.id = c("nr"."vear"). vcov="iid")
summarv(reg po)
## OLS estimation, Dep. Var.: lwage
## Observations: 4.360
## Fixed-effects: vear: 8
## Standard-errors: IID
       Estimate Std. Error t value Pr(>|t|)
##
## educ 0.0923 0.00515 17.94 < 2.2e-16 ***
## exper 0.0304 0.00549 5.53 3.2982e-08 ***
## black -0.1400 0.02324 -6.02 1.8504e-09 ***
## union 0.1869 0.01710 10.93 < 2.2e-16 ***
## married 0.1109 0.01567 7.07 1.7557e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 0.480008 Adj. R2: 0.185341
##
                  Within R2: 0.121537
```

### Random effects estimator (RE) VI

```
# reg_p = plm(lwage ~ educ+exper+married+union+f_year, data=pdat, model="pooling")
# summary(reg_p)$coef
```

- With POLS everything is statistically significant. Returns to union wage premium is about 17.5%. Marriage premium is about 12.5%. Is this causal, or is their a matching story?
- When  $a_i$  is in the error term (case of POLS) the marriage and union premiums are relatively higher. If married or unionized workers are also more able, then, our results will be biased.
- When we eliminate a<sub>i</sub> from the error term (FD or FE), then they go
  down significantly which suggests that POLS estimates are biased.
  Otherwise, the estimate for marriage and union premiums would not
  change significantly.

```
summary(reg_fe2)
```

### Random effects estimator (RE) VII

```
## Error in h(simpleError(msg, call)): error in evaluating the argument
'object' in selecting a method for function 'summary': object 'reg_fe2' not
found
```

 RE estimates of union membership and marriage premiums are much smaller compared POLS.

```
reg re = plm(lwage \sim educ + exper + black + union + married + f year.
             data=pdat.
             model="random")
summarv(reg re)
## Oneway (individual) effect Random Effect Model
      (Swamy-Arora's transformation)
##
## Call:
## plm(formula = lwage ~ educ + exper + black + union + married +
       f vear. data = pdat. model = "random")
##
## Balanced Panel: n = 545, T = 8, N = 4360
##
```

### Random effects estimator (RE) VIII

```
## Fffects:
##
                var std.dev share
  idiosyncratic 0.125 0.353 0.54
## individual 0.105
                     0.324 0.46
## theta: 0.641
##
## Residuals:
##
     Min. 1st Ou. Median 3rd Ou.
                              Max.
## -4.5657 -0.1441 0.0268 0.1916 1.5422
##
## Coefficients:
##
             Estimate Std. Error z-value Pr(>|z|)
## (Intercept) 0.1608
                        0.1469 1.09 0.2738
## educ
              0.0940 0.0105 8.95 < 2e-16 ***
                        0.0111 2.99 0.0028 **
## exper
             0.0333
## black
              -0.1376
                        0.0470 -2.93 0.0034 **
## union
              0.1108
                        0.0179 6.18 6.4e-10 ***
## married
                        0.0168
                                 4.36
                                       1.3e-05 ***
           0.0733
## f vear1981 0.0787
                        0.0242
                                 3.26 0.0011 **
## f_year1982 0.0983
                        0.0309
                                 3.18 0.0015 **
## f vear1983 0.1071
                        0.0396
                                 2.70
                                       0.0069 **
```

### Random effects estimator (RE) IX

```
## f_year1984 0.1403 0.0493 2.84 0.0045 **
## f_year1985 0.1562 0.0595 2.62 0.0087 **
## f year1986 0.1820 0.0700 2.60 0.0093 **
## f_year1987 0.2069 0.0806 2.57 0.0103 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares: 658
## Residual Sum of Squares: 545
## R-Squared: 0.172
## Adj. R-Squared: 0.169
## Chisq: 901.556 on 12 DF, p-value: <2e-16
# library("lme4") # for random effects estimator
# reg re = lmer(lwage ~ educ + exper + black + union + married + f vear + (1/nr).
            data = pdat)
#
# summary(reg re)$coef
```

• The partial-time-demeaning parameter,  $\hat{\theta} = 0.64$ , so not close to zero and pretty far from one. But, we expect them to be closer to the FE estimates than to the POLS estimates.

# Random effects estimator (RE) X

- The remaining positive returns to marriage or union can be interpreted in two ways and unfortunately we cannot distinguish between these alternative hypothesis.
  - ⇒ marriage or union really makes men (reminder: we have only data on men) more productive
  - ⇒ firms judge married and unionized men as more stable or reliable and pay them higher wages.

# Application I

Effect of Direct Sale Points ("tanzim satış") on inflation rate in Turkey

- On 11 February 2019, the government introduced Direct Sale Points (DSP). DSP are municipality-led vegetable stalls which sell products at discounted prices (called "tanzim satış" in Turkish).
- Only 9 products have been sold at these DSP (tomatoes, potatoes, onions, green peppers and other vegetables). The data
  ("tanzim\_pooled.rds") contains monthly inflation rate in February for these 9 products in all regions of Turkey in 2018 (before DSP) and in 2019 (after DSP).

# Application II

• In February 2019 DSP were operated only in Istanbul and Ankara (called "tanzim regions"), later they were operated in other cities as well. Since there were only 65 DSP in Tanzim regions (50 in Istanbul and 15 in Ankara) but a large population (15 million in Istanbul and almost 6 million in Ankara) it is not obvious that there is an effect on inflation rates.

```
furl = "https://github.com/obakis/econ_data/raw/master/tanzim_panel.rds"
download.file(furl, destfile = "tanzim_panel.rds", mode="wb")
tanzim = readRDS("tanzim panel.rds")
```

• To calculate the effect of DSP we can use simple averages

```
reg_po1 = lm(inf ~ dsp+ y19 + nuts2, data=tanzim)
summary(reg po1)
```

# Application III

```
##
## Call:
## lm(formula = inf ~ dsp + v19 + nuts2, data = tanzim)
##
## Residuals:
##
    Min
        10 Median
                    30 Max
  -22.20 -9.59 -1.85 8.30 38.62
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.4434
                       3.4979 1.56 0.12
## dsp
           -6.4570
                      4.2039 -1.54 0.13
                      1.1660 -4.84 1.8e-06 ***
## V19
      -5.6480
## nuts2TR21 -2.3831
                      4.5532 -0.52 0.60
## nuts2TR22
          3.1321
                      4.5532 0.69
                                    0.49
## nuts2TR31 0.4946
                      4.5532 0.11 0.91
## nuts2TR32 1.4981
                      4.5532 0.33
                                      0.74
## nuts2TR33 2.2672
                       4.5532 0.50
                                      0.62
## nuts2TR41 -0.9140
                       4.5532
                              -0.20
                                      0.84
## nuts2TR42 -1.3841
                       4.5532
                              -0.30 0.76
## nuts2TR51 0.4576
                       4.0390 0.11
                                      0.91
```

### Application IV

```
## nuts2TR52
                0.1799
                           4.5532
                                     0.04
                                              0.97
## nuts2TR61
               -0.0512
                           4.5532
                                    -0.01
                                              0.99
## nuts2TR62
                2.5462
                           4.5532
                                     0.56
                                              0.58
## nuts2TR63
                2.5034
                           4.5532
                                     0.55
                                              0.58
## nuts2TR71
                                              0.86
                0.8141
                           4.5532
                                     0.18
## nuts2TR72
                1.2443
                           4.5532
                                     0.27
                                              0.78
## nuts2TR81
                                     0.27
                                              0.78
                1.2519
                           4.5532
## nutsaTR82
                2.1824
                           4.5532
                                     0.48
                                              0.63
## nuts2TR83
                0.3363
                           4.5532
                                     0.07
                                              0.94
## nuts2TR90
                4.8643
                           4.5532
                                     1.07
                                              0.29
## nutsoTRA1
                2.9662
                           4.5532
                                     0.65
                                              0.52
## nuts2TRA2
                0.2680
                                     0.06
                           4.5532
                                              0.95
## nutsoTRB1
                2,5411
                           4.5532
                                     0.56
                                              0.58
## nuts2TRB2
                                     1.10
                5.0159
                           4.5532
                                              0.27
## nuts2TRC1
               1.2519
                           4.5532
                                     0.27
                                              0.78
## nuts2TRC2
               -0.9974
                           4.5532
                                    -0.22
                                              0.83
## nuts2TRC3
               -2.0754
                           4.5532
                                    -0.46
                                              0.65
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.1 on 440 degrees of freedom
```

# Application V

```
## Multiple R-squared: 0.0965, Adjusted R-squared: 0.041
## F-statistic: 1.74 on 27 and 440 DF, p-value: 0.0131
# librarv(plm)
# pdat = pdata.frame(tanzim, index = c("id", "vear"))
#reg fd = plm(inf \sim v19 + nuts2 + dsp. model = "fd". data = pdat)
#reg re = plm(inf ~ v19 + nuts2 + dsp. model="random", data=pdat)
#summary(reg re)
#summarv(reg fd)
# reg po = plm(inf ~ v19 + nuts2 + dsp. model="pooling", data=pdat)
# reg fe = plm(inf ~ y19 + nuts2 + dsp, model="within", data=pdat)
reg po = feols(inf ~ dsp + nuts2 | y19,
                data=tanzim.
                panel.id = c("id", "year"), vcov="iid")
summary(reg po)
```

# Application VI

```
## OLS estimation. Dep. Var.: inf
## Observations: 468
## Fixed-effects: y19: 2
## Standard-errors: IID
##
             Estimate Std. Error t value Pr(>|t|)
## dsp
              -6.4570
                            4.20 -1.5360 0.12527
## nuts2TR21
              -2.3831
                            4.55 -0.5234
                                         0.60097
## nuts2TR22
               3.1321
                            4.55 0.6879 0.49188
## nuts2TR31
              0.4946
                            4.55 0.1086
                                         0.91355
## nuts2TR32
              1.4981
                            4.55 0.3290
                                          0.74231
## nuts2TR33
              2,2672
                            4.55 0.4979
                                         0.61878
## nuts2TR41
              -0.9140
                            4.55 -0.2007
                                          0.84100
## nuts2TR42
              -1.3841
                            4.55 -0.3040
                                          0.76128
## nuts2TR51
              0.4576
                            4.04
                                          0.90984
                                  0.1133
## nuts2TR52
              0.1799
                            4.55
                                  0.0395
                                          0.96851
## nuts2TR61
              -0.0512
                            4.55 -0.0112
                                          0.99103
## nuts2TR62
               2.5462
                            4.55
                                  0.5592
                                          0.57631
## nuts2TR63
               2.5034
                            4.55
                                  0.5498
                                          0.58273
## nuts2TR71
               0.8141
                            4.55
                                  0.1788
                                         0.85819
## nuts2TR72
               1.2443
                            4.55
                                  0.2733 0.78477
## nuts2TR81
               1.2519
                            4.55 0.2749 0.78349
```

### Application VII

```
## nutsaTR82
             2.1824
                         4.55 0.4793 0.63196
## nuts2TR83
             0.3363
                         4.55 0.0739 0.94116
## nuts2TR90 4.8643
                         4.55 1.0683 0.28597
## nuts2TRA1
             2.9662
                         4.55 0.6514 0.51510
## nuts2TRA2
             0.2680
                         4.55 0.0588 0.95310
## nuts2TRB1 2.5411
                         4.55 0.5581 0.57707
## nuts2TRB2 5.0159
                         4.55 1.1016 0.27123
## nuts2TRC1 1.2519
                         4.55 0.2749 0.78349
## nuts2TRC2 -0.9974
                         4.55 -0.2191 0.82671
## nuts2TRC3 -2.0753
                         4.55 -0.4558 0.64876
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## RMSE: 11.7 Adj. R2: 0.041033
##
              Within R2: 0.036976
reg fe = feols(inf ~ dsp + nuts2 | id + year,
              data=tanzim.
              panel.id = \mathbf{c}("id"."vear").
              cluster = "nuts2") # vcov = "cluster" is not automatically implied !
```

## The variables 'nuts2TR21', 'nuts2TR22' and twenty-three others have been

removed because of collinearity (see \$collin.var).

# **Application VIII**