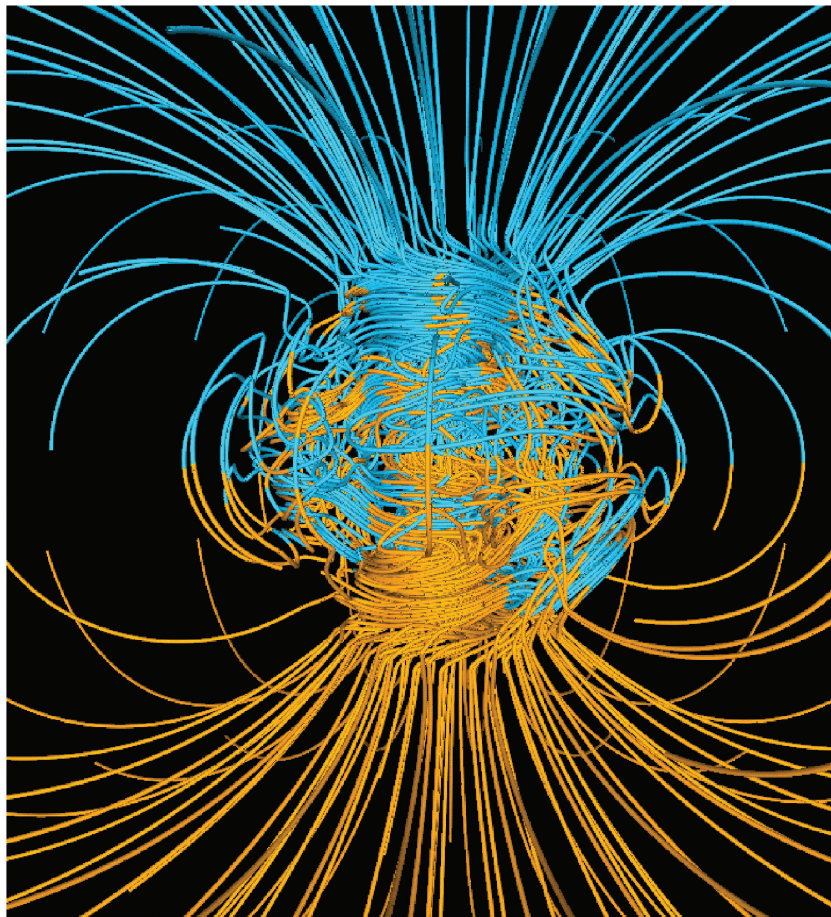


COMPUTATIONAL INFRASTRUCTURE FOR GEODYNAMICS (CIG)

---

# MAG

User Manual  
Version 1.0.1



[www.geodynamics.org](http://www.geodynamics.org)

Peter Olson  
Wei Mi  
Sue Kientz

---



# Contents

<b>I</b>	<b>Preface</b>	<b>7</b>
<b>II</b>	<b>Chapters</b>	<b>11</b>
<b>1</b>	<b>Introduction</b>	<b>13</b>
1.1	About MAG . . . . .	13
1.2	Governing Equations . . . . .	13
<b>2</b>	<b>Installation and Getting Help</b>	<b>15</b>
2.1	Introduction . . . . .	15
2.2	Getting Help . . . . .	15
2.3	System Requirements . . . . .	15
2.4	Downloading and Unpacking Source . . . . .	15
2.5	Installation Procedure . . . . .	16
2.5.1	MAG File Structure . . . . .	16
2.5.2	Prepare MAG for Running . . . . .	16
2.6	Installing from the Software Repository . . . . .	16
2.6.1	Tools You Will Need . . . . .	16
2.6.2	Download Source from Subversion . . . . .	17
<b>3</b>	<b>Running MAG</b>	<b>19</b>
3.1	Using MAG . . . . .	19
3.2	Changing Parameters . . . . .	20
<b>4</b>	<b>Postprocessing and Graphics</b>	<b>21</b>
4.1	Introduction . . . . .	21
4.2	Time Series and Spectra Plot . . . . .	21
4.3	Interactive IDL Procedures . . . . .	23
<b>5</b>	<b>Examples</b>	<b>27</b>
5.1	Benchmark Cases . . . . .	27
5.1.1	Results . . . . .	27
5.1.2	Discussions . . . . .	27
5.2	Reversal Dynamo Case . . . . .	27
5.2.1	Creating MPEGs with IDL . . . . .	27
<b>III</b>	<b>Appendices</b>	<b>35</b>
<b>A</b>	<b>Variables Used in MAG</b>	<b>37</b>
<b>B</b>	<b>MAG Input File Format</b>	<b>49</b>

<b>C MAG Output File Format</b>	<b>53</b>
<b>D License</b>	<b>55</b>

# List of Figures

4.1	Time series plot of energy . . . . .	22
4.2	Spectra plot of a time depentant dynamo . . . . .	23
4.3	IDL figure with Map option . . . . .	24
4.4	Kinetic energy (yellow) and Magnetic energy (blue) plot by the MAGVOL procedure . . . . .	25
5.1	Pole plot 1 . . . . .	29
5.2	Pole plot 2 . . . . .	30
5.3	Pole Plot 3 . . . . .	31
5.4	Pole Plot . . . . .	33
5.5	Field Plot . . . . .	34



# Part I

## Preface





# Preface

## About This Document

This document is organized into three parts. Part I consists of traditional book front matter, including this preface. Part II begins with an introduction to MAG version 1.0 and its capabilities and proceeds to the details of implementation. Part III provides appendices and references.

The style of this publication is based on the Apple Publications Style Guide <http://developer.apple.com/documentation/UserExperience/Conceptual/APStyleGuide/AppleStyleGuide2003.pdf>, as recommended by Python.org <http://www.python.org/>. The documentation was produced using LyX <http://www.lyx.org/> to facilitate the transformation of files from one format to another. LyX is a document processor that encourages an approach to writing based on the structure of your documents, not their appearance. It is released under a Free Software/Open Source license.

Errors and bug fixes in this manual should be directed to CIG Geodynamo Mailing List <[cig-geodyn@geodynamics.org](mailto:cig-geodyn@geodynamics.org)>.

## Who Will Use This Document

This documentation is aimed at scientists who prefer to use prepackaged and specialized analysis tools. Users are likely to be experienced computational Earth scientists and have familiarity with basic scripting, software installation, and programming; but are not likely to be professional programmers. Of those, there are likely to be two classes of users: those who just run models and those who modify the source code.

## Citation

Computational Infrastructure for Geodynamics (CIG) is making this source code available to you in the hope that the software will enhance your research in geophysics. The underlying Fortran code was donated to CIG in July of 2006. A number of individuals have contributed a significant portion of their careers toward the development of MAG. It is essential that you recognize these individuals in the normal scientific practice by citing the appropriate peer reviewed papers and making appropriate acknowledgements.

The MAG development team asks that you cite the following:

- Olson, P., G.A. Glatzmaier (1993), Highly supercritical thermal convection in a rotating spherical shell: centrifugal vs. radial gravity. *Geophys. Astrophys. Fluid Dyn.*, *70*, 113-136.
- Olson, P., G.A. Glatzmaier (1995), Magnetoconvection in a rotating spherical shell: structure of flow in the outer core. *Phys. Earth Planet Int.*, *92*, 109-118.
- Olson, P., G.A. Glatzmaier (1996), Magnetoconvection and Thermal Coupling of the Earth's Core and Mantle. *Phil. Trans. R. Soc. Lond.*, *A354*, 1413-1424.
- Christensen, U.R. and Aubert (2006), J., Scaling properties of convection-driven dynamos in rotating spherical shells and application to planetary magnetic fields. *Geophys J. Int.* *166*, 97-114.
- Olson, P., U. Christensen, G.A. Glatzmaier (1999), Numerical Modeling of the Geodynamo: Mechanisms of Field Generation and Equilibration. *J. Geophys. Res.*, *104*, 10,383-10,404.

- Christensen, U., P. Olson, G.A. Glatzmaier (1999), Numerical modelling of the geodynamo: a systematic parameter study. *Geophys. J. Int.*, 138, 393-409.
- Christensen, et al. (2001), A numerical dynamo benchmark. *Phys. Earth Planet Int.*, 128, 25-34 (benchmark cases).

[Note: there are more recent papers by the same authors.] The developers also request that in your oral presentations and in your paper acknowledgements that you indicate your use of this code, the authors of this code (G. Glatzmaier, U. Christensen, P. Olson), and CIG <http://www.geodynamics.org/>.

## Support

MAG development was funded by grants from NASA HPC and NSF Geophysics. Continued support of MAG is made possible under NSF EAR-0406751.

# Part II

## Chapters



# Chapter 1

## Introduction

Dynamo codes represent a powerful new tool for the quantitative study of a broad range of geophysical processes, ranging from short time-scale phenomena such as magnetic variations, rotational variations, and flow in the core, to long-term phenomena such as magnetic excursions, reversals, superchrons, and the evolution of the core and its thermal and chemical interaction with the mantle. The primary objective of CIG in this area is to provide the Earth Science community with robust, reliable, efficient, flexible, state-of-the-art numerical codes for modeling dynamo processes in the Earth's core and in the interiors of other planets. Another CIG objective is to support graphical- and user-interfaces for these codes that allow Earth scientists to analyze, display, and interpret dynamo code results, and to compare results from the various codes that we support, as well as with geomagnetic, space magnetic, and paleomagnetic data.

### 1.1 About MAG

MAG is a serial version of Gary Glatzmaier's rotating spherical convection/magnetoconvection/dynamo code, modified by Uli Christensen and Peter Olson. The code solves the non-dimensional Boussinesq equations for time-dependent thermal convection in a rotating spherical shell filled with an electrically conducting fluid. The equations of motion are: the Navier-Stokes equation including Coriolis, Lorentz, Buoyancy, pressure, viscous, and inertial terms; the heat equation including advection, diffusion, and uniform-density heat sources; the continuity equation for velocity and Gauss' law for magnetic field, and the induction equation for the magnetic field.

All variables are non-dimensional (see Appendix A); time scale is viscous diffusion, length scale is shell thickness, temperature scale is boundary temperature difference, magnetic field and electric currents use Elsasser number scaling. A variety of boundary and initial conditions are selected as options.

Mag uses toroidal-poloidal decomposition for velocity and magnetic field with explicit timesteps. Linear terms are evaluated spectrally (spherical harmonics plus Chebyshev polynomials in radius) and nonlinear terms are evaluated on a spherical grid.

Additional technical information is found in [1]-[8].

### 1.2 Governing Equations

MAG solves the following non-dimensional Boussinesq magnetohydrodynamics equations for dynamo action due to thermal convection of an electrically conducting fluid in a rotating spherical shell (e.g., Olson et al. 1999)[5].

$$E \left( \frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} - \nabla^2 \mathbf{u} \right) + 2\hat{\mathbf{z}} \times \mathbf{u} + \nabla P = Ra \frac{r}{r_o} T + \frac{1}{Pm} (\nabla \times \mathbf{B}) \times \mathbf{B} \quad (1.1)$$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B}) + \frac{1}{Pm} \nabla^2 \mathbf{B} \quad (1.2)$$

$$\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = \frac{1}{Pr} \nabla^2 T + \epsilon \quad (1.3)$$

$$\nabla \cdot \mathbf{u} = 0, \quad \nabla \cdot \mathbf{B} = 0 \quad (1.4)$$

where  $\mathbf{u}$  is the velocity,  $\mathbf{B}$  is the magnetic field,  $T$  is temperature,  $t$  is time,  $\hat{z}$  is a unit vector in the direction of the rotation axis,  $P$  is pressure, and  $r$  is the position vector in spherical coordinates  $r\theta\phi$ .

Four basic non-dimensional parameters in 1.1 - 1.4 control the dynamo action. The Rayleigh number represents the strength of buoyancy force driving the convection

$$Ra = \frac{\alpha g_0 \Delta T D^3}{\nu \kappa} \quad (1.5)$$

where  $\alpha$  is thermal expansivity,  $g_0$  is gravitational acceleration on the outer boundary at radius  $R$ ,  $\Delta T$  is temperature difference between the inner and outer boundaries,  $D$  is shell thickness,  $\nu$  is kinematic viscosity, and  $\kappa$  is thermal diffusivity. The Ekman number represents the ratio of viscous and Coriolis forces

$$E = \frac{\nu}{\Omega D^2} \quad (1.6)$$

Here  $\Omega$  is rotation rate. The Prandtl number is the ratio of kinematic viscosity to thermal diffusivity

$$Pr = \frac{\nu}{\kappa} \quad (1.7)$$

and the magnetic Prandtl number is the ratio of kinematic viscosity to magnetic diffusivity  $\lambda$

$$P_m = \frac{\nu}{\lambda} \quad (1.8)$$

An additional (optional) control parameter is the non-dimensional volumetric heat source (or heat sink) strength  $\epsilon$ .

## Chapter 2

# Installation and Getting Help

### 2.1 Introduction

To test run MAG, you will download the source package (in the form of a compressed `tar` file) from the Geodynamics Software Packages web page <http://www.geodynamics.org/cig/software/packages/>. After unpacking the source, you will use the `make` utility to build MAG from source, and background execute MAG with the provided benchmark input file.

Advanced users and software developers may be interested in downloading the latest MAG source code directly from the CIG source code repository, instead of using the prepared source package. See the 2.6 section later in this chapter. MAG has been tested on Linux, Mac OS X, and Windows.

### 2.2 Getting Help

For help, send e-mail to the CIG Geodynamo Mailing List <[cig-geodyn@geodynamics.org](mailto:cig-geodyn@geodynamics.org)>. You can subscribe to the Mailing List and view archived discussion at Geodynamics Mail Lists <http://www.geodynamics.org/cig/lists/>.

### 2.3 System Requirements

MAG requires the following:

- A Fortran compiler, g77 or gFortran.
- For Windows you need to install cygwin <http://cygwin.com>.

### 2.4 Downloading and Unpacking Source

Download MAG from the Geodynamics website <http://www.geodynamics.org/>. Click the "software" tab at the top of the page. Then click "Software Packages" and then "Geodynamo." Once you click the MAG link, download the source archive and unpack it using the `tar` command:

```
$ tar xzf MAG-1.0.0.tar.gz
```

If you don't have GNU Tar, try the following command instead:

```
$ gunzip -c MAG-1.0.0.tar.gz | tar xf -
```

## 2.5 Installation Procedure

### 2.5.1 MAG File Structure

After unpacking the source, you will find following directories:

- ~/**src** Contains the set of FORTRAN source code files with suffix ".f". This includes sample grid parameter value files with names like "param32s4.f" for a coarse grid (up to 32 spherical harmonics, 24 radial grid intervals, and 4-fold symmetry in  $\phi$ ). A makefile named "makefile". Sample files with input parameters, par.XXX. The case par.bench0 is for rotating convection at an Ekman number of  $1E-3$ , starting from a conductive temperature perturbation with imposed perturbation with  $l=4$ ,  $m=4$ , and running for a short time. This is the "benchmark0" test case in Christensen et al, 2001[6]. Another input file is par.bench1, the dynamo "benchmark1" case in Christensen et al[6].
- ~/**doc** The directory where you will find this manual and other documentation files.
- ~/**bench-data** Contains output files "ls.benchX", "l.benchX", "g.benchx", and "d.benchx" obtained with short runs of benchmark0 and benchmark1 on a Linux workstation. Explanations of the contents of these files are found in Appendix C. These data files can be used for comparison with the result obtained by your local run of the MAG.
- ~/**idl** This is where the postprocessing IDL (Interactive Data Language) routines reside.

### 2.5.2 Prepare MAG for Running

1. First you need to create a path for execution of **magx** (below is an example; use your path) :

```
printenv PATH $ PATH=$PATH:/your_mag_dir_path $ export PATH
```

2. Compile the program using **make** in the source directory, which by default uses the existing param.f grid and symmetry

```
$ make
```

Note that makefile uses -g77 or other Fortran compiler, and creates executables, either magx(default) or magxYYsZ, where yy=spherical harmonic trunction and Z=longitudinal symmetry.

3. To delete all the object files and executables, simply type:

```
$ make clean
```

## 2.6 Installing from the Software Repository

The MAG source code is available via a Subversion server at the Geodynamics website <http://www.geodynamics.org/>. This allows users to view the revision history of the code, and check out the most recent development version of the software.

**NOTE:** If you are content with the prepared source package, feel free to skip this section.

### 2.6.1 Tools You Will Need

In addition to the usual system requirements, you must have a Subversion client installed in order to work with the source from the CIG software repository. To check whether you have a subversion client installed on your machine, type:

```
$svn help
```

It should return a usage message. For more information on Subversion, visit the Subversion website <http://subversion.tigris.org/>.



### 2.6.2 Download Source from Subversion

To check out the latest version of the software, use the `svn checkout` command:

```
$ svn checkout http://geodynamics.org/svn/cig/geodyn/3D/MAG/trunk MAG
```

where "MAG" is the directory created with the file structure mentioned in 2.5.1



## Chapter 3

# Running MAG

### 3.1 Using MAG

For test-running the code, do the following steps:

1. Uncompress all files, and create a path (see 2.5.2)
2. Link grid parameter file to param.f,<sup>1</sup> which enters into most subroutines through "include" statements. For example, a grid parameter file named "param32f4.f" (32 spherical harmonics truncation degree, longitude symmetry is 4) is linked using.

```
$ ln -sf param32s4.f param.f
```

3. Compile the program with:

```
$ make
$ mv magx magx32s4 (Renaming is optional)
```

4. MAG uses a standard input file. Background execute using par.XXX as the input file and .YYY as the output files extension:

```
$ magx32s4 <par.XXX >p.YYY &
```

For running with the benchmark input files (par.bnch0 or par.bnch1) , the execution statement should be:

```
$ magx32s4 <par.bnch0 >p.bench0 &
```

5. If there is a problem with the input file list, it is often the final three lines; with some systems, a "\$" may be required at the end.
6. MAG produces a series of output files. For example, when using input file par.bnch0 (the example in step 4) MAG generates: 1.bench0, 1s.bench0, g[i].bench0 and d[i].bench0, where i=0,1,2...9. See Appendix C for details on MAG's output files. Compare your output files with the data provided in the directory ~/bench-data/data\_bench0.
7. REMEMBER TO DELETE, MOVE, or RENAME ALL OUTPUT FILES IN THE CURRENT DIRECTORY BEFORE RE-RUNNING WITH THE SAME "output" FILENAME – RETAINING SAME-NAMED OUTPUT FILES IN THE CURRENT DIRECTORY CAUSES MAG TO CRASH!!

---

<sup>1</sup>To change grids or symmetry (in param.f), MAG needs to be recompiled. param.f is what the code looks for and needs to be changed for remaking. param32s6.f and param32s4.f are examples of param.f.

## 3.2 Changing Parameters

Physical and time step parameters can be changed in the par-file namelist without re-compiling MAG. See Appendix B for a list of the input parameter names and definitions. Grid parameters must be changed in param.f and MAG must be then re-compiled. There are some numerical restrictions on the grid parameter combinations, which are given in Appendix A.

## Chapter 4

# Postprocessing and Graphics

### 4.1 Introduction

Once you finish running MAG, you should have a series of output data files. To visualize your results, the MAG software package provides a set of IDL routines found in the directory called `PREFIX/idl`, where `PREFIX` is the directory under which you installed MAG. We should mention here that IDL is a commercial visualization tool by ITT Visual Information Solutions <http://www.itervis.com/idl>. A free IDL compatible program called GDL <http://gnudatalanguage.sourceforge.net> works with MAG's line plot IDL procedure `MAGTS.pro`, but not with the interactive IDL procedures in MAG.

### 4.2 Time Series and Spectra Plot

Procedure `MAGTS.pro` takes data from l-files generated by MAG and creates time series plots and statistics. This version reads an l-file consisting of 17 time series, the first record being dimensionless time. Energies and rms magnetic field and velocity are scaled as in MAG; tilt is dipole vector colatitude; pole longitude is dipole vector longitude. Figures 4.2 and 4.2 show the energy time series plot and spectra plot from a time-dependent dynamo.

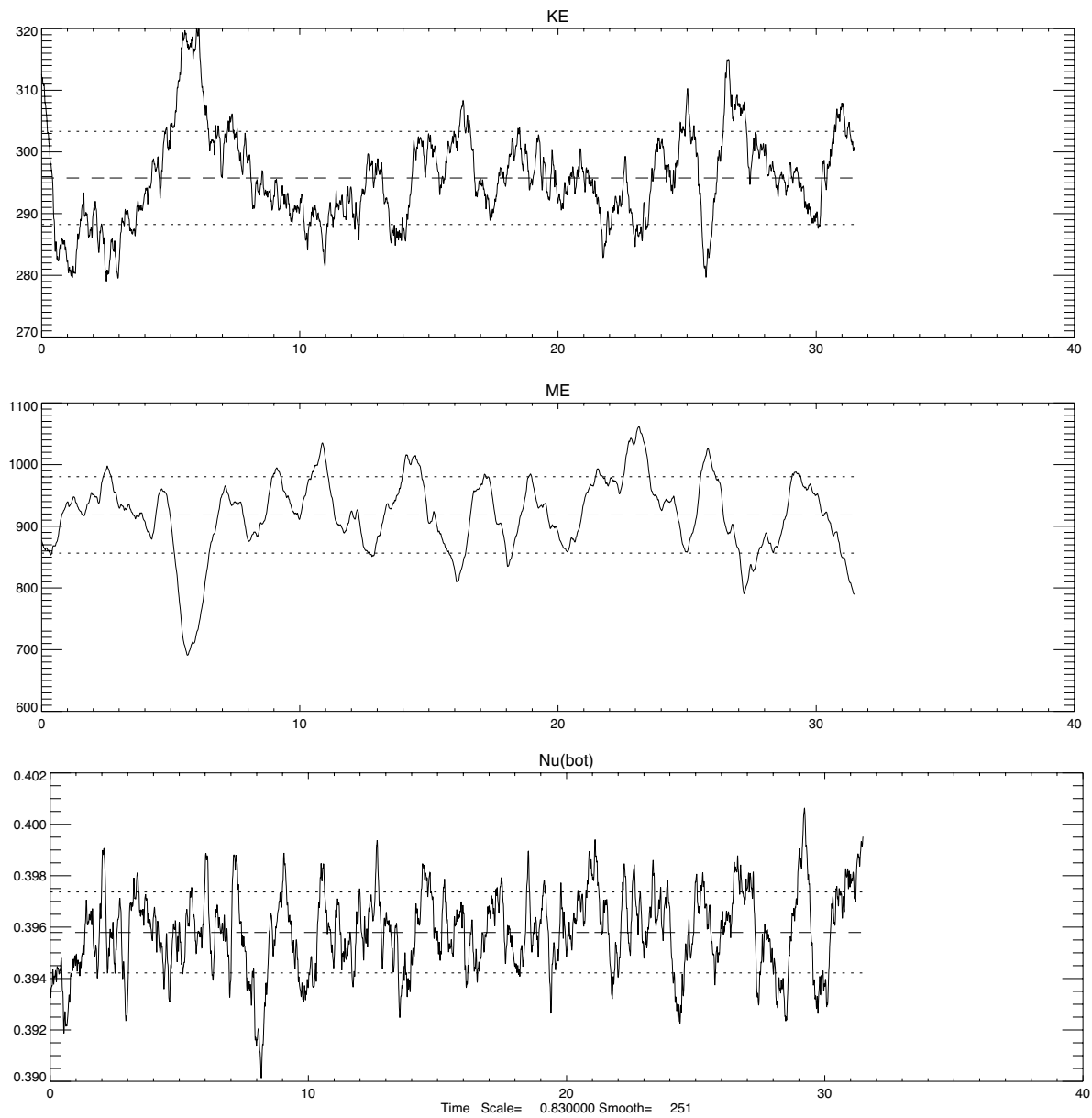


Figure 4.1: Time series plot of energy

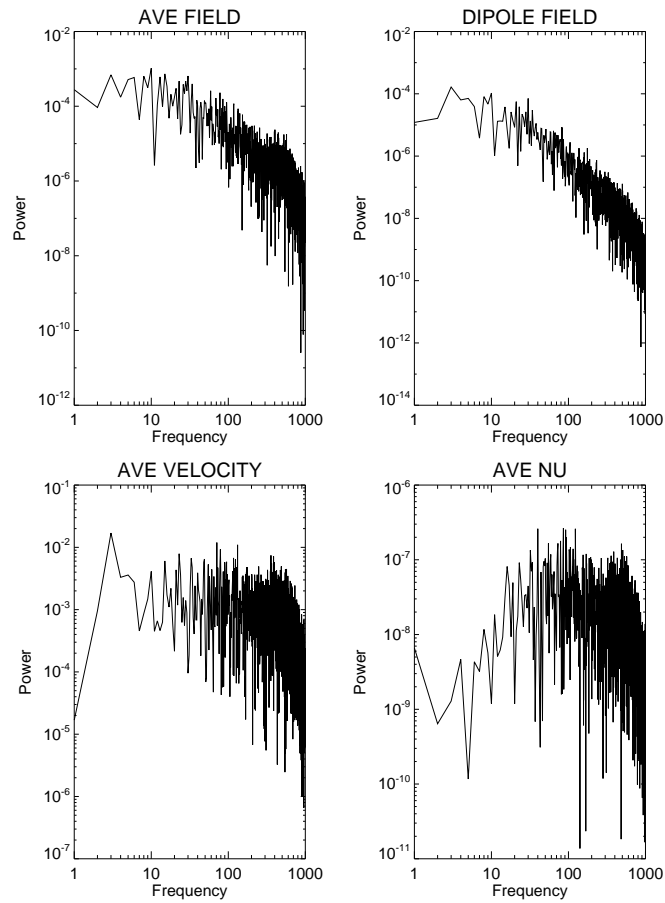


Figure 4.2: Spectra plot of a time dependent dynamo

### 4.3 Interactive IDL Procedures

MAGSYM.pro is an interactive procedure display which results from a g-file produced by MAG. This version uses modified IDL color tables and assumes formatted input. It creates either postscript .ps or .gif files. If other output file formats are required, modification of "LABELOUT" are required. MAGSYM has many plot options: map, closeup, equator, slice... etc. Producing each plot is straightforward by choosing from the option menu. Figure 4.3 is plotted with the map option.

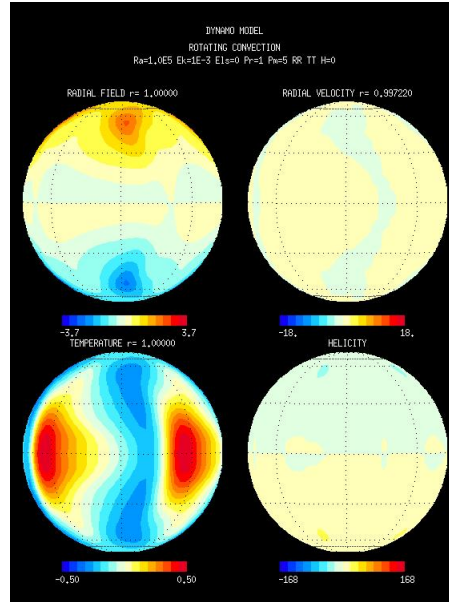


Figure 4.3: IDL figure with Map option

MAGVOL.pro is another interactive IDL procedure to display volume results from rotating convection, magnetoconvection & dynamo calculations (written by P. Olson). It uses G-FILES produced by MAG (some longitudinal symmetry may be assumed in the G-FILE). This version uses modified idl color tables and assumes formatted or unformatted input (it asks for .gif but creates .jpg files); if other output file formats are required, modifications of "labelout" are required. This version assumes x-window screen graphics; for other graphics devices, change the `set_plot,'x'` and `tvrd()` commands accordingly. MAGVOL procedure creates volume-rendered images of temperature, helicity, the z-component of vorticity, kinetic and magnetic energy, joule heating, work by lorentz forces and buoyancy forces. Figure 4.3 shows a plot of kinetic energy and magnetic energy obtained from a numerical dynamo model.



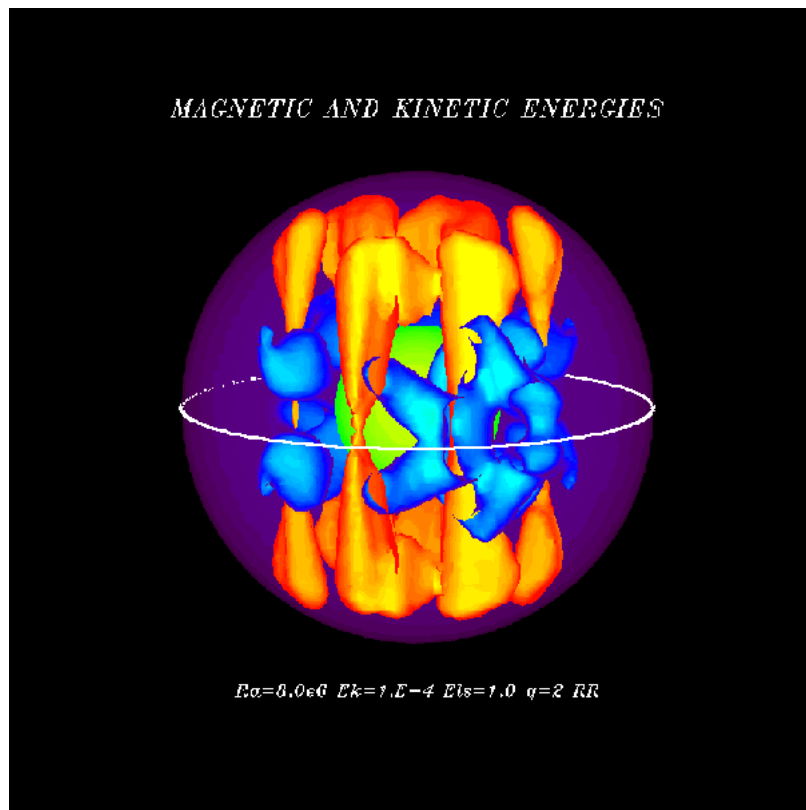


Figure 4.4: Kinetic energy (yellow) and Magnetic energy (blue) plot by the MAGVOL procedure



# Chapter 5

## Examples

Included in this chapter are two benchmark cases and a reversal dynamo case. We will present the cases with their input parameters and typical run of the case with output data analysis.

### 5.1 Benchmark Cases

Historically, these are the cases defined in the benchmark study published in the 2001 paper by Gary Glatzmaier *et al.* [6]. Case 0 is a benchmark of rotating non-magnetic convection. Case 1 is a dynamo with an insulating inner core co-rotating with the outer boundary. The regions outside the fluid shell are electrical insulators and the magnetic field on the boundaries matches with appropriate potential fields in the exterior that imply no external sources of the field.

In both cases the Ekman number is  $E = 10^{-3}$  and the Prandtl number is  $Pr = 1$ . The Rayleigh number is set to  $Ra = 100000$ . Note the definition of Rayleigh number differs from the one in the published cases[6] by a factor of Ekman number  $E$ , ie  $Ra = Ra[6]/E$ . The magnetic Prandtl number is zero in the non-magnetic convection case 0, and is  $Pm = 5$  in case 1. The spherical harmonic expansion is truncated at degree  $lmax = 32$  and a four-fold symmetry is assumed in the longitudinal direction. The input parameter files are `par.bench0` for case 0 and `par.bench1` in case 1, both files resides in `~/src` directory.

#### 5.1.1 Results

The output files of the benchmark cases are stored in the directory `~/bench-data/data_bench0` and `~/bench-data/data-bench1` respectively.

	Case 0 Suggested Value	Mag Case 0	Case 1 Suggested Value	Mag Case 1
$E_{kin}$	$58.348 \pm 0.050$	58.35	$30.733 \pm 0.020$	30.72
$E_{mag}$			$626.41 \pm 0.40$	627.15
$T$	$0.42812 \pm 0.00012$		$0.37338 \pm 0.00040$	
$\mu_\phi$	$-10.1571 \pm 0.0020$	-10.80	$-7.6250 \pm 0.0060$	-7.84
$B_\theta$			$-4.9289 \pm 0.0060$	
$\omega$	$0.1824 \pm 0.0050$		$-3.1017 \pm 0.0040$	

#### 5.1.2 Discussions

### 5.2 Reversal Dynamo Case

#### 5.2.1 Creating MPEGs with IDL

IDL provides an `IDLgrMPEG` class that allows the user to save an array of image frames as an MPEG movie. See the IDL Reference guide.

The MPEG\_PUT procedure stores the specified image array at a specified frame index in an MPEG sequence. The MPEG\_SAVE procedure encodes and saves an open MPEG sequence. The images can be read using the READ\_IMAGE function.

make\_mpg, synopsis

This module, mpg.pro reads a sequence of images (named prefix00001.suffix) and produces an MPEG1 or MPEG2 movie. Supported formats are: BMP, GIF, JPEG, PNG, PPM, SRF, TIFF, DICOM

Parameters

- prefix string(required) A string specifying the prefix of the images to read included the path, for example "/home/data/images/Image"
- suffix string(required) A string specifying the suffix of the images to read, for example "jpg".
- n\_start integer(required) An integer specifying the first image in the sequence.
- n\_end integer(required) An integer specifying the last image in the sequence.
- digits integer(required) An integer specifying the number of digits of the number field in the sequence, for example image00001.jpg would require digits=5.
- dims integer(optional) An integer array specifying the size of the output image. If not specified the size of the first image is used.
- format integer(optional) An integer with values 0 for MPEG1 and 1 for MPEG2. Default is MPEG1.
- frame\_rate integer(optional) An integer with values.

```
1 = 23.976 frames/sec: NTSC encapsulated film rate.
2 = 24 frames/sec: standard film rate.
3 = 25 frames/sec: PAL video frame rate
4 = 29.97 frames/sec: NTSC video frame rate
5 = 30 frames/sec: NTSC drop frame video rate (the default).
6 = 50 frames/sec: double frame rate/progressive PAL
7 = 59.94 frames/sec: double frame rate NTSC
8 = 60 frames/sec: double frame rate NTSC
```

- mpeg\_file string(optional) A string specifying the output MPEG file (default outfile.mpg)
- tmp\_dir string(optional) A string specifying temporary directory to use for the temporary image files.

To run the IDL movie generator type in a shell:

```
%idl
> .compile mpg.pro
> make_mpg, prefix='image', suffix='.bmp', n_start=0, n_end=100, digits=5, dims=[512,512], mpeg_file='mympeg.mp'
```

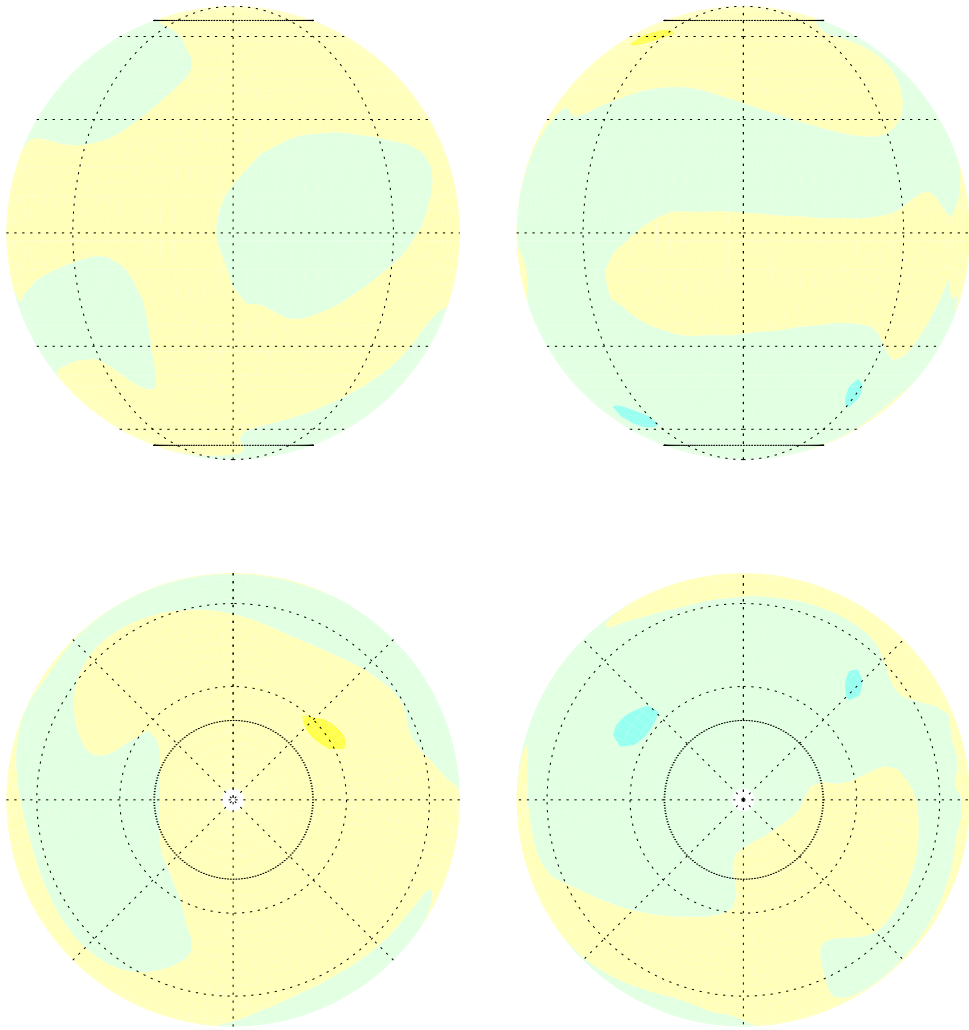


Figure 5.1: Pole plot 1

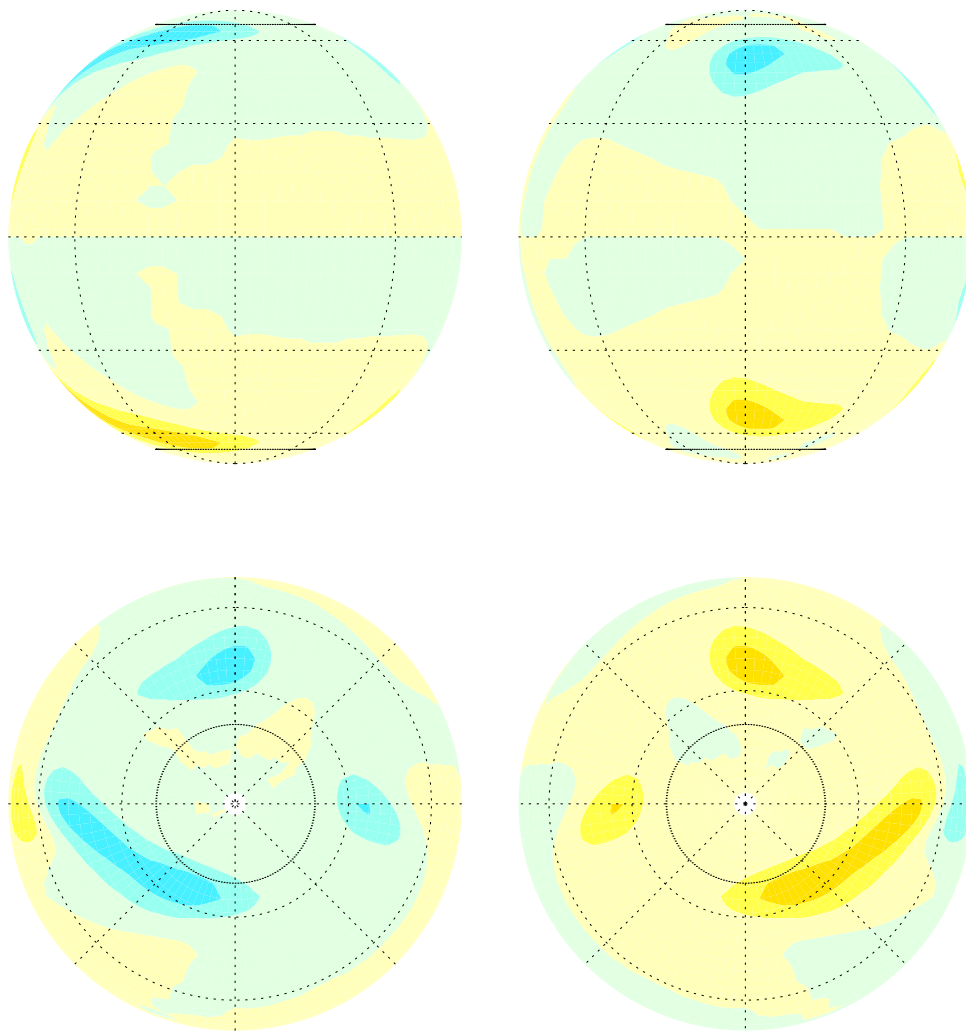


Figure 5.2: Pole plot 2

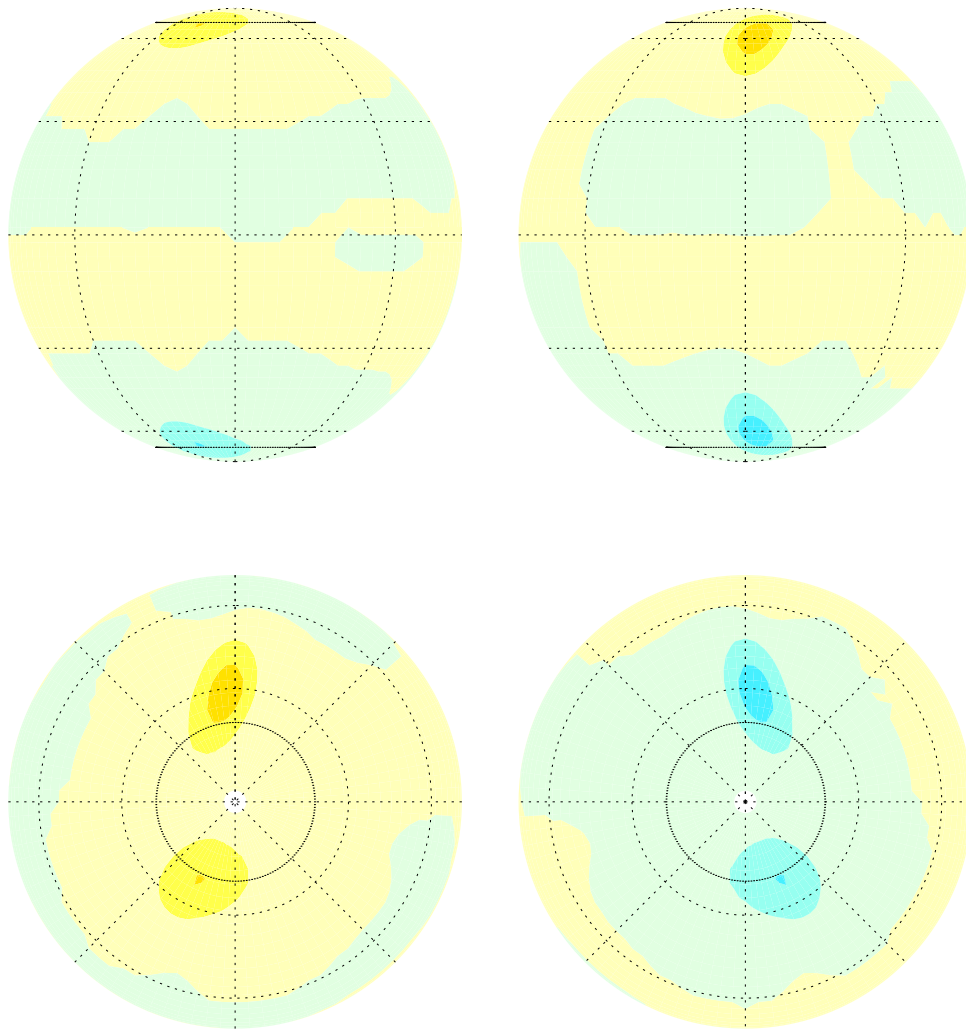
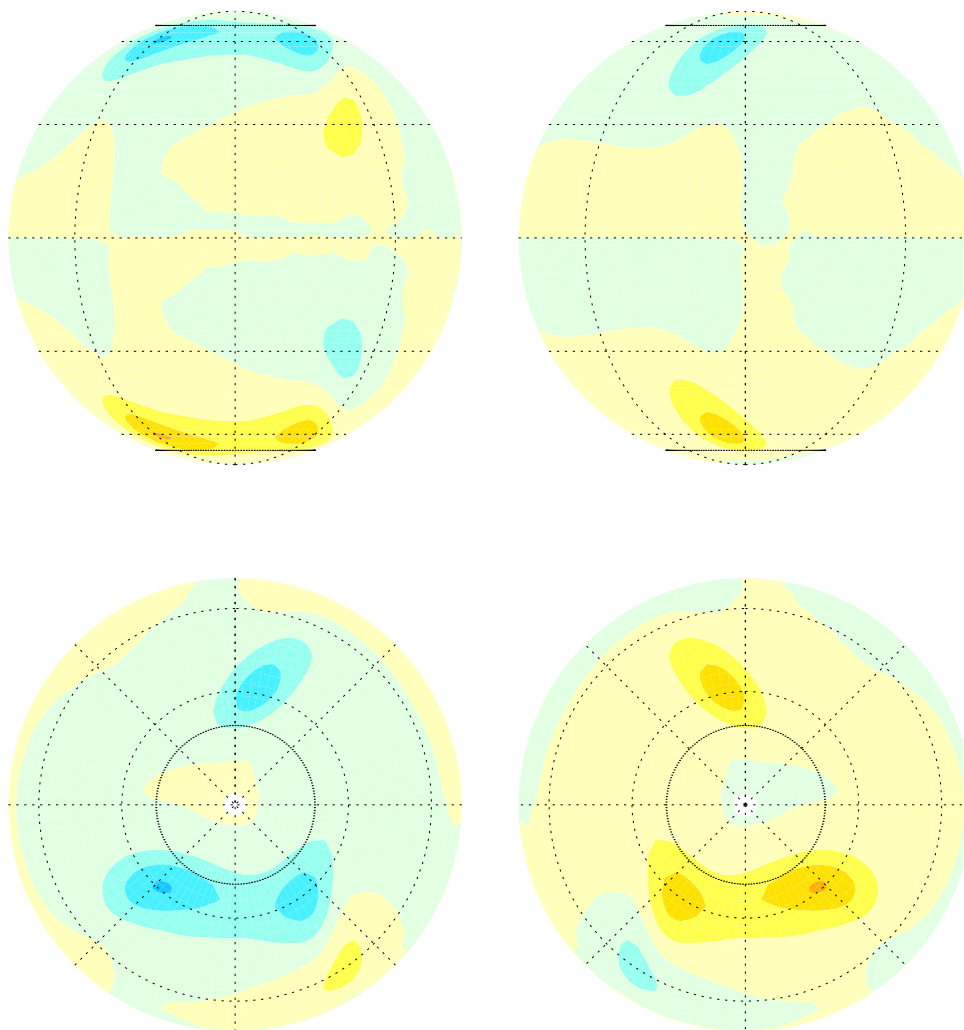


Figure 5.3: Pole Plot 3





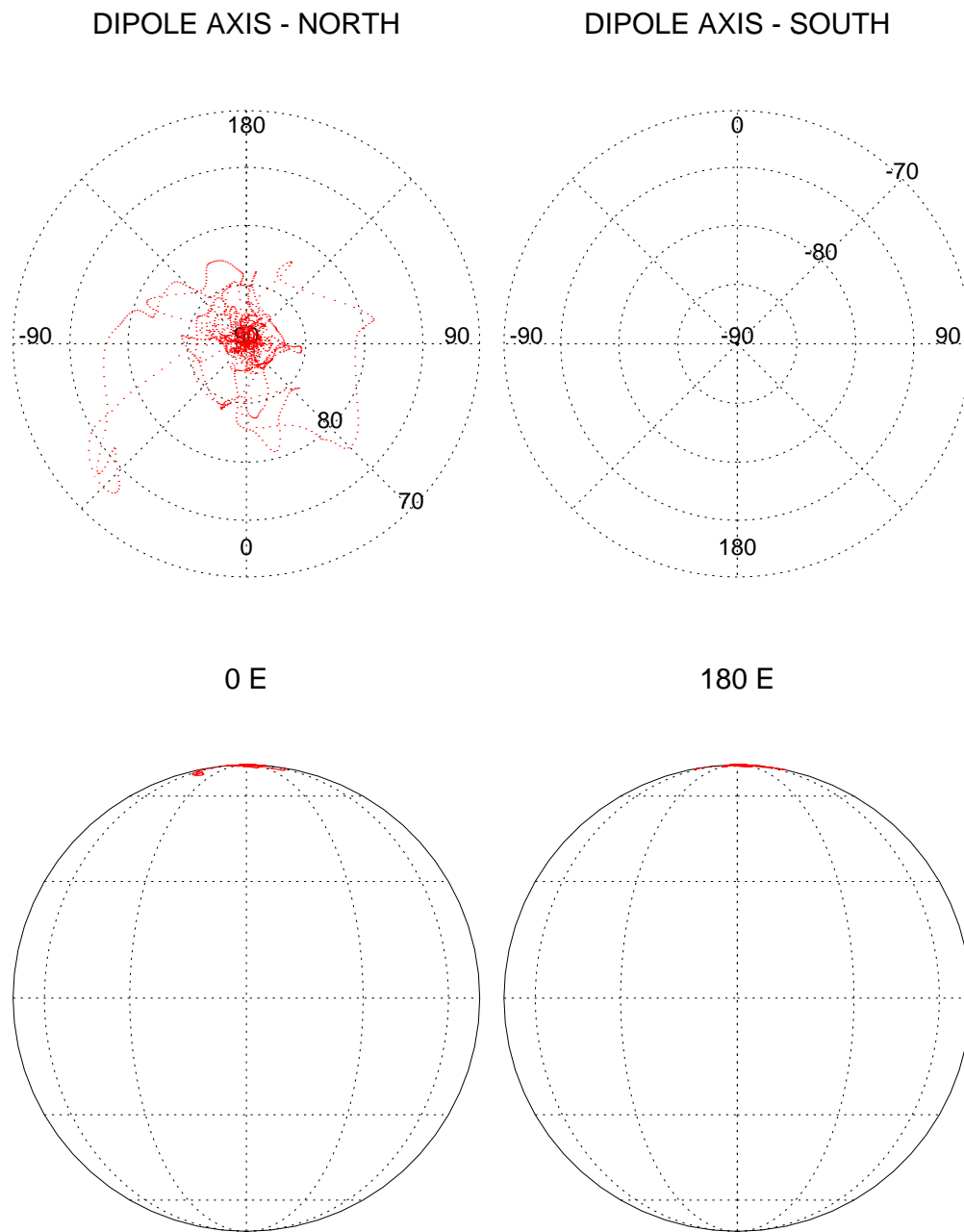


Figure 5.4: Pole Plot

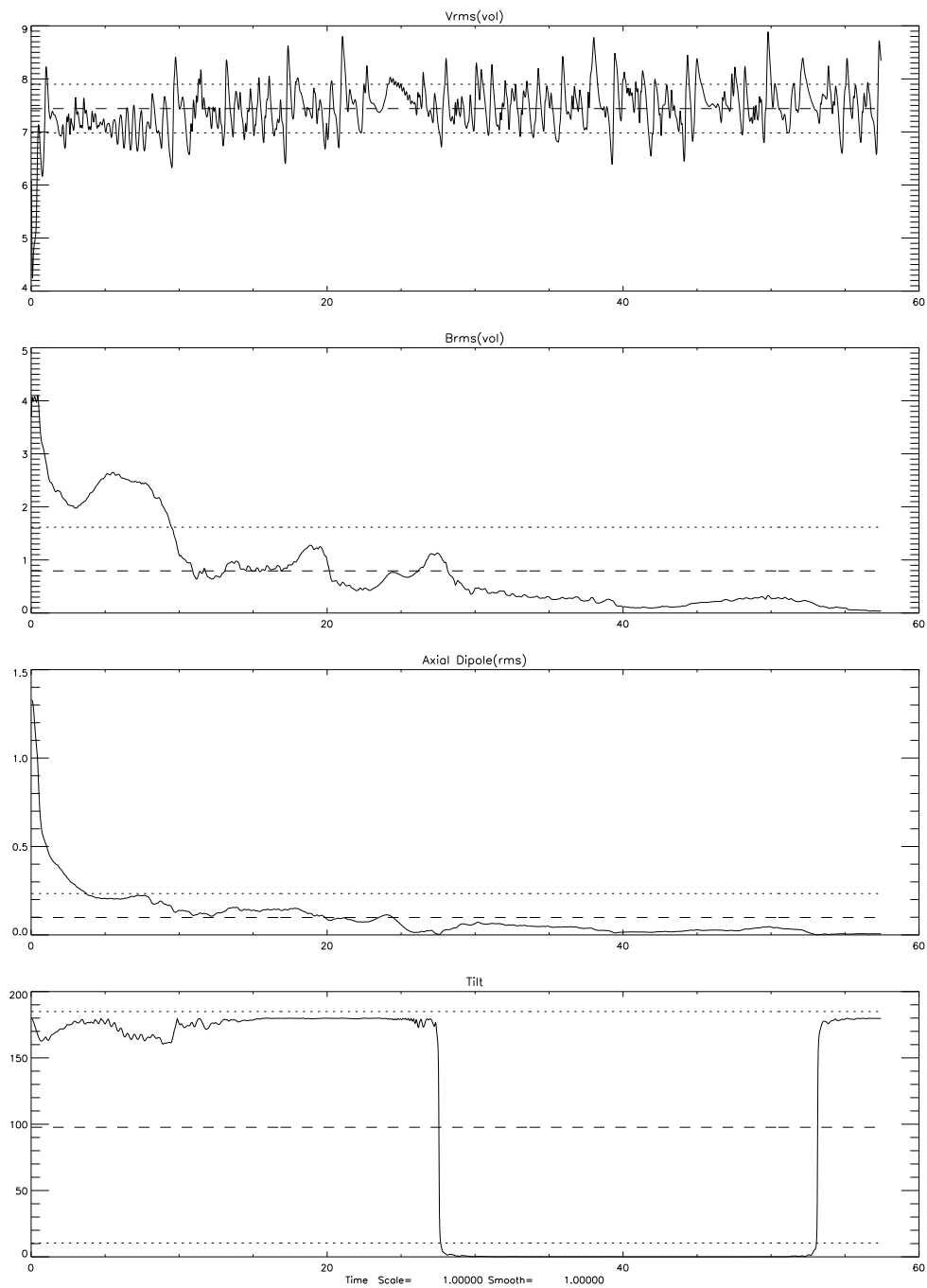


Figure 5.5: Field Plot

## Part III

# Appendices



# Appendix A

## Variables Used in MAG

This is a list of variables and names used in the program set in MAG. The list is in alphabetical order for ease of reference.

**adrke** axisymmetric toroidal kinetic energy (diagnostic)

**ai** imaginary unit =  $\text{complex}(0,1)$

**aj** (**nlma,nn+1**) poloidal magnetic field potential (spectral form); the second index is either the Chebyshev degree (n) or the radial grid point (kc)

**ajmat** (**nn,nn,lmax**) LU-decomposed matrix from Chebyshev collocation of toroidal induction equation. Built in ludc, used in amhd.

**aleg1** (**nlma,ni**) Value of associated Legendre function at grid points

**aleg2** (**nlma,ni**) Value of associated Legendre function, multiplied with Gaussian weight, at grid points

**aleg3** (**nlma,ni**) Value of derivative of associated Legendre function multiplied with  $\sin(\theta)$  at grid points

**alflt** [INPUT] Filter parameter for  $B_r$  in graphics output, see nflt

**alfac** [INPUT] Controls the contribution of the (modified) Alfvén velocity to the Courant time step limit (see under "courfac"). The modified Alfvén velocity is given by  $v_{\text{alfven}}' = (v_a)^2 / \{(v_a)^2 + [\pi * (\eta + \nu) / \Delta x]^2\}$  where  $v_a = B / \sqrt{\mu * \rho}$  and  $\Delta x$  is the Courant length (either  $\Delta x_r$  or  $\Delta x_h$ )

**alpha** [INPUT] =0 linear terms in the equations are treated fully explicit, =1 linear terms are treated fully implicit, =0.5: Crank-N.

**alumn0** Factor for scaling heat flow in output amcke: axisymmetric poloidal kinetic energy

**amhd** [SUBROUTINE] The "workhorse" of the program: advance solution by nstep time steps

**amps** [INPUT] can be used to re-scale entropy

**ampj** [INPUT] can be used to re-scale toroidal magnetic field

**ampb** [INPUT] can be used to re-scale poloidal magnetic field

**ampw** [INPUT] can be used to re-scale poloidal velocity

**ampz** [INPUT] can be used to re-scale toroidal velocity

**anorm** =  $\sqrt{2/[nn+1]}$

**apome** axisymmetric poloidal magnetic field energy

**atome** axisymmetric toroidal magnetic field energy

**b (nlma,nn+1)** poloidal magnetic field potential (spectral form, see aj)

**bleg1 (lmax)** auxiliary array for calculation of aleg1

**bleg2 (lmax)** auxiliary array for calculation of aleg2

**bleg3 (lmax)** auxiliary array for calculation of aleg3

**bmat(nn,nn,lmax)** LU-decomposed matrix from Chebyshev collocation of poloidal induction equation.  
Built in ludc, used in amhd.

**bnlc1 (nja/2,ni)** bnlr1 stored in complex form

**bnlc2 (nja/2,ni)** bnlr2 stored in complex form

**bnlc3 (nja/2,ni)** bnlr3 stored in complex form

**bnlr1 (nja,ni)** nonlinear products for updating b (on grid points)

**bnlr2 (nja,ni)** nonlinear products for updating aj (on grid points)

**bnlr3 (nja,ni)** nonlinear products for updating aj (on grid points)

**bots(0:lmax,0:mmax)** [INPUT] harmonic coefficients of prescribed temperature (entropy) on inner boundary

**br (nja,ni)**  $= r^2 * B_r$  on gridpoints

**brc** br stored as complex array

**bscl**  $= dt * radtop^2$

**bt (nja,ni)**  $= r * \sin(\theta) * b_\theta$

**btrdt (ni)** used in movmout to calculate j\_phi

**bts (ni,3)** used in movmout to calculate j\_phi

**btc** bt stored as complex array

**bp (nja,ni)**  $= r * \sin(\theta) * b_\phi$

**bpc** bp stored as complex array

**bpeak** [INPUT] maximum value of imposed field on boundaries

**bpeakbot** maximum value of imposed field on inner boundary

**bpeaktop** maximum value of imposed field on outer boundary

**cbr (nja,ni)**  $= r^2 * \text{curl}(B) * e_r$

**cbrc** cbr stored as complex array

**cbt (nja,ni)**  $= r * \sin(\theta) * \text{curl}(B) * e_\theta$

**cbtc** ctr stored as complex array

**cbp (nja,ni)**  $= r * \sin(\theta) * \text{curl}(B) * e_\phi$

**cbpc** cbp stored as complex array

**cheb (nn,nn)** cheb(i,j) = value of Chebyshev polynomial i at grid point j

**chebi** [SUBROUTINE] initialize subroutine chebtf

**chebtf** [SUBROUTINE] multiple fast Chebyshev transform

**clm (lmax,mmax)** normalization factors of spherical harmonics

**cmb** [INPUT] integrated conductivity of thin D"-layer

**colat (ni)** vector of colatitudes (Gauss points), local array in subroutine prep

**courfac** [INPUT] factor controlling the time step as fraction of courant advection length. The time step is limited to  $dt < \min( dx/[ courfac * v + alffac * v\_alfven' ] )$

**cvr (nja,ni)**  $=r^2 * \text{curl}(v) * e\_r$

**cvrc** cvr stored as complex array

**db (nlma,nn+1)** radial derivative of poloidal magnetic potential (spectral form, see aj)

**dbdt (nlma,nn,2)** time derivative of poloidal magnetic potential b

**dcheb (nn,nn)** dcheb(i,j) = 1st derivative of Chebyshev polynomial i at grid point j

**d2cheb (nn,nn)** d2cheb(i,j) = 2nd derivative of Chebyshev polynomial i at grid point j

**d3cheb (nn,nn)** d3cheb(i,j) = 3rd derivative of Chebyshev polynomial i at grid point j

**ddb (nlma,nn+1)** 2nd radial derivative of poloidal magnetic potential b

**ddj (nlma,nn+1)** 2nd radial derivative of toroidal magnetic potential aj

**ddw (nlma,nn+1)** 0.25 \* 2nd radial derivative of poloidal velocity potential w

**ddz (nlma,nn+1)** 0.25 \* 2nd radial derivative of toroidal velocity potential z

**djdt (nlma,nn,2)** time derivative of toroidal magnetic potential z

**dpdt (nlma,nn,2)** time derivative of pressure

**dsdt nlma,nn,2)** time derivative of temperature (entropy)

**dw (nlma,nn+1)** 0.50 \* radial derivative of poloidal velocity potential w

**dwdt (nlma,nn,2)** time derivative of poloidal velocity potential w

**dz (nlma,nn+1)** 0.50 \* radial derivative of toroidal velocity potential z

**dzdt (nlma,nn,2)** time derivative of toroidal velocity potential z

**delxh (nn)** horizontal Courant length squared

**delxr (nn)** radial Courant length

**difamp** [INPUT] amplitude of hyperdiffusivity  $D=D*(1 + difamp * [(1+1-ldif)/(lmax+1-ldif)]^{ldifexp})$  when  $l > ldif$

**dipfilt** [INPUT] If nfilt>0 multiply axial dipole component of B\_r on outer surface by dipfilt in graphics file

**dj (nlma,nn+1)** radial derivative of toroidal magnetic potential (spectral form, see aj)

**dt** current time step

**dtchck** [SUBROUTINE] controls time step

**dth** Courant time based on horizontal velocity + Alfven velocity

**dtmax** [INPUT] Upper limit on time step (and initial step)

**dtmin** Lower limit on time step (stop when  $dt < dtmin$ )

**dtold** Time step of previous iterative step

**dtr** Courant time based on radial velocity + Alfven velocity

**dtstart** [INPUT] Initial time step. If =0, dtmax, or when beginning from restart file, the old dt is taken

**dvpdr (nja,ni)** =  $d [r * \sin(\theta) * v_{\phi}] / dr$  on gridpoints

**dvpdrc** dvpdr stored as complex array

**dvpdp (nja,ni)** =  $d [r * \sin(\theta) * v_{\phi}] / d\phi$  on gridpoints

**dvpdpc** dvpdp stored as complex array

**dvrdr (nja,ni)** =  $d [r^2 * v_r] / d\phi$  on gridpoints

**dvrdrpc** dvrdr stored as complex array

**dvrdr (nja,ni)** =  $d [r^2 * v_r] / dr$  on gridpoints

**dvrdrdrc** dvrdr stored as complex array

**dvrdrdt (nja,ni)** =  $\sin(\theta) * d [r^2 * v_r] / d\theta$  on gridpoints

**dvrdrdtc** dvrdrdt stored as complex array

**dvtddp (nja,ni)** =  $d [r * \sin(\theta) * v_{\theta}] / d\phi$  on gridpoints

**dvtddpc** dvtddp stored as complex array

**dvtddr (nja,ni)** =  $d [r * \sin(\theta) * v_{\theta}] / dr$  on gridpoints

**dvtddrc** dvtddr stored as complex array

**dw (nlma,nn+1)** 0.5 \* radial derivative of poloidal velocity potential w

**dz (nlma,nn+1)** 0.5 \* radial derivative of toroidal velocity potential z

**escale** scaling factor for energies in output

**ek** [INPUT] Ekman number

**enb** [OUTPUT] magnetic energy

**ens** [OUTPUT] thermal energy

**enscale** [INPUT] in output listing, energies are multiplied by enscale

**ent** [OUTPUT] total energy

**env** [OUTPUT] kinetic energy

**epsc0** [INPUT] internal heating rate

**flmb1 (nlma+..)** r-component of  $(v \times B)$  term

**flmb2 (nlma+..)** theta-component of  $(v \times B)$  term



**flmb3** (**nlma**+) phi-component of  $(\mathbf{v} \times \mathbf{B})$  term

**flms1** (**nlma**+) r-component of entropy advection term

**flms2** (**nlma**+) theta-component of entropy advection term

**flms3** (**nlma**+) phi-component of entropy advection term

**flmw1** (**nlma**+) r-component of  $\mathbf{v} \cdot \text{grad}(\mathbf{v}) + \text{Lorentz force}$  term

**flmw2** (**nlma**+) theta-component of  $\mathbf{v} \cdot \text{grad}(\mathbf{v}) + \text{Lorentz force}$  term

**flmw3** (**nlma**+) phi-component of  $\mathbf{v} \cdot \text{grad}(\mathbf{v}) + \text{Lorentz force}$  term

**gauss** (**ni**) vector with Gaussian weighting factors, local array in subroutine prep

**gquad** [SUBROUTINE] finds zeros and Gaussian weight of associated Legendre function

**grfile** [CHARACTER] file name for data on spatial grid for graphics with prefix "g."; added to outfile set

**grav** (**nn**) gravity at radial levels

**ib** (**nn,lmax**) pivot array for LU-decomposition of matrix bmat created in sgefa, used in sgesl

**ic** stepping variable commonly used for steps in colatitude

**icour** [INPUT] Courant criterion is checked each ICOUR'th time step

**idiftyp** [INPUT] controls radial variation of diffusivity; =0, no variation

**ifaxc** [13] auxiliary array (factorization) for Chebyshev transform

**ifaxf** [13] auxiliary array (factorization) for Fourier transform

**ifbfrz** [INPUT] logical; if .TRUE., do not update magnetic field

**ifirst** =1 before first call of time-step checking routine, =0 thereafter

**iframes** [INPUT] write altogether iframes frames on the movie files (see description under imovopt)

**ifsfrz** [INPUT] logical; if .TRUE., do not update temperature (entropy)

**ifvfrz** [INPUT] logical; if .TRUE., do not update velocity

**ij** (**nn,lmax**) pivot array for LU-decomposition of matrix ajmat created in sgefa, used in sgesl

**imagcon** [INPUT] <0 imposed poloidal field ( $l=1, m=0$ ) at ICB >=0 imposed toroidal field ( $l=2, m=0$ ) at ICB >=10 additionally imposed field at CMB, field is of same sign and amplitude if imagcon=10 and of opposite sign if imagcon=11

**imovopt** [INPUT] three-digit integer number, controls options for generating movie-files.

**Last digit >0** write  $B_z$ ,  $W_z$  (vortic) and  $T$  in the equatorial plane on file with prefix "me."

**2nd last digit >0** write longitud. averaged  $B_\phi$ ,  $j_\phi$  and  $v_\phi$  on file with prefix "ma."

**3rd last digit >0** write  $B_r$  at outer surface and  $v_p$  and  $v_t$  at level given by this digit on file with prefix "mm."

**4th last digit >0** write spherical harmonic coeffs for poloidal field at outer boundary and for velocity potentials at radial level given by this digit on file with prefix "cc.". (This option is not working in current release of MAG).

**imovct** counter variable for movie frames

**infile** [CHARACT INPUT] name of input file for initial values (restart)

**init** [INPUT] =0 start from dat-file, =1: random initial cond., =-1: hydro. condition from dat-file, magnetic random >=100: initial temperature perturbation in a single mode l,m. Here m is given by the last two digits of init and l by the preceding digits.

**ip0 (nn)** pivot array for LU-decomposition of matrix p0mat created in sgefa, used in sgesl

**iprnt** counting blocks in time iteration sequence with printed output created at completion of block

**is (nn,lmax)** pivot array for LU-decomposition of matrix smat created in sgefa, used in sgesl

**is0 (nn)** pivot array for LU-decomposition of matrix s0mat created in sgefa, used in sgesl

**iscale** [INPUT] determines which diffusivity is used for scaling of time, velocity, energy. 1=viscous, 2=thermal, 3=magnetic

**istep** time step counter (routine amh)

**istor** counting superblocks in time iteration sequence, upon completion of superblock disk file with data saved

**ivfilt** [INPUT] Apply filter to v\_r at radial level ivfilt and right into first radial position in graphics file; see nfilt

**iwp (nn,lmax)** pivot array for LU-decomposition of matrix wpmat created in sgefa, used in sgesl

**iz (nn,lmax)** pivot array for LU-decomposition of matrix zmat created in sgefa, used in sgesl

**k2k (nn1)** auxiliary array for Chebyshev transform

**kc** stepping variable commonly used for steps in radius

**kcour** auxiliary variable for time step checking procedure

**kbotb** [INPUT] magnetic bottom condition; =1 insulating, =2 perfect condition

**kbotv** [INPUT] mechanical bottom condition; =1 free, =2 rigid

**kbots** [INPUT] thermal bottom condition; =1 fixed entropy, =2 flux

**kei** [SUBROUTINE] calculates kinetic energy

**kstep** global time step counter

**ktops** [INPUT] thermal top condition; =1 fixed entropy, =2 flux

**ktopb** [INPUT] magnetic top condition; =1 insulating, =2 perfect condition

**ktopv** [INPUT] mechanical top condition; =1 free, =2 rigid

**ldif** [INPUT] control parameter for hyperdiffusivity, see difamp

**ldifexp** [INPUT] control parameter for hyperdiffusivity, see difamp

**lm** stepping variable used to cover all l and m  $lm = m*(lmax+1)/minc - m*(m-minc)/(2*minc) + l-m+1$

**lmax** maximum harmonic degree, calculated as  $(nj-1)/3$

**logfile** [CHARACT] file name for continuous log of energies and other data prefix "l."; added to outfile set

**lot** [PARAM] = 2 \* nlma (twice the number of harmonic modes)

**lpfile** [CHARACT] file name for continuous log of specified values with prefix "lp."; added to outfile set

**lsfile:** [CHARACTER] file name for power spectra of magnetic and kinetic as function of  $l$  and  $m$  with prefix "ls."; added to outfile set

**ludc:** [SUBROUTINE] Chebyshev collocation

**mclm (nlma)** used to unscramble harmonic order  $m$  from variable  $lm$

**mclma (nlma)** =  $m/\text{minc}+1$  for given  $lm$  (storage order of  $m$ )

**kei** [SUBROUTINE] calculates magnetic energy

**minc** [PARAM] if  $>1$ , minc-fold symmetry in longitude assumed

**mmax** maximum harmonic order, is the largest integer  $\leq l_{\text{max}}$  divisible by minc

**movafile** [CHARACTER] file name for movie data (longitudinal averages) with prefix "ma."; added to outfile set

**movefile** [CHARACTER] file name for movie data in equatorial plane with prefix "me." ; added to outfile set

**movmfile** [CHARACTER] file name for movie data in map views with prefix "mm." ; added to outfile set

**n, nc** stepping variables commonly used for steps over Chebyshev polynomial

**nep** [PARAM] =  $n_{\text{ja}}/2$  used for storage of points in  $\phi$  in complex array

**nfilt** [INPUT] Apply filter  $F(l)=\exp(-|l|/l_{\text{filt}})^{n_{\text{filt}}}$  to  $B_r$  on outer surface in graphics output file (if  $n_{\text{filt}}>0$  and  $al_{\text{filt}}>0$ ) When  $n_{\text{filt}}>0$ ,  $al_{\text{filt}}<0$ , apply cos-tapered filtered with cutoff at  $n_{\text{filt}}$  and taper width  $|al_{\text{filt}}|$

**ngcolat** [INPUT] graphics output on each  $ng_{\text{colat}}$ 'th point in latitude

**ngform** [INPUT] if .ne. 0, graphics output is written each time a restart file is (finally) written.  $ng_{\text{form}}=1$  or -1: formatted graphics file,  $ng_{\text{form}}=2$ : unformatted for  $ng_{\text{form}}=-1$  additional comment lines are inserted (this is to look at the file, not for graphics)

**nglon** [INPUT] graphics output for each  $ng_{\text{lon}}$ 'th point in longitude

**ngrad** [INPUT] graphics output on each  $n_{\text{grad}}$ 'th radial level

**ni** [PARAM] # of grid points in colatide; must be even

**nip1** [PARAM] =  $ni+1$

**nj** [PARAM] # of grid points in longitude;  $n_{\text{j}}/\text{minc}$  must be multiple of four

**nja** =  $n_{\text{j}}/\text{minc}$ , # of actually needed grid points in  $\phi$

**njp1** [PARAM] =  $n_{\text{j}}+1$

**nlaf** [PARAM] =  $l_{\text{max}}+1$

**nlafp1** [PARAM] =  $l_{\text{max}}+2$

**nlm** [PARAM] =  $(m_{\text{max}}+1)*(m_{\text{max}}+2)/2$

**nlma** [PARAM] # of angular modes employed  $nl_{\text{ma}} = m_{\text{max}}*(l_{\text{max}}+1)/\text{minc} - m_{\text{max}}*(m_{\text{max}}-\text{minc})/(2*\text{minc}) + l_{\text{max}}-m_{\text{max}}+1$ .

**nlmpa** [PARAM] =  $nl_{\text{ma}} + m_{\text{max}}/\text{minc} + 1$

**nlogstep** [INPUT] write data on logfile (prefix l.) after each  $n_{\text{logstep}}$  steps.

**nmaf** [PARAM] =  $m_{\text{max}}+1$

**nmafa** [PARAM] = mmax/minc+1

**nn** [PARAM] # of radial grid points, nn-1 must be multiple of 4, and contain no prime factors larger than 5

**nn1** [PARAM] = nn-1

**nn2** [PARAM] = nn-2

**nn3** [PARAM] = nn-3

**nnp1** [PARAM] = nn+1

**nnp2** [PARAM] = nn+2

**nnaf** [PARAM] # of radial Chebyshev modes, must be  $\leq$  nn

**nnx2** [PARAM] = 2\*nn

**nplog** [INPUT] if  $>0$  write velocity values at specific points of the grid on separate logfile (prefix "lp.") after every nplog steps (for arrays, see vrpoint, vppoint, vtpoint in subroutine amhd for details)

**nprnt** [INPUT] # of printed output blocks created until next data storage for restart

**nps2** [PARAM] = (nn+1)/2

**nrp** [PARAM] = nja+2 (# of points in phi +2)

**ns2** [PARAM] = (nn-1)/2

**nstep** [INPUT] # of time steps done until next printed output (total # of time steps is nstep\*nprnt\*nstor)

**nstor** [INPUT] # of data storages before program termination

**ntf** [PARAM] = 3\*nja/2+1, used for Fourier transform array trigsf

**ocorevol** volume of spherical shell (outer core)

**oek** = 1. / Ekman number

**oekpm** = 1. / (Ekman number \* Magnetic Prandtl number)

**oodt** = 1. / dt (inverse time step)

**oosscl** = 1. / dt

**opr** = 1. / Prandtl number

**outfile** [CHARACT INPUT] Name of output files (pre-fixes d.,l.,ls.,g.,me.,ma.,mm., lp. added)

**p0mat** (**nn,nn**) LU-decomposed matrix from Chebyshev collocation of pol. equation of motion, l=0-term for pressure. Constructed in ludc, used in amhd

**pbar** [SUBROUTINE] Calculates value of associated Legendre function

**pscale** scaling pressure in output

**pr** [INPUT] Prandtl number

**prmag** [INPUT] Magnetic Prandtl number

**prnt** [SUBROUTINE] print diagnostic data

**pscl** = radtop<sup>2</sup>

**qi (ni,5)** array with various coefficients depending on colatitude (look in subroutine prep, loop "do 32 " for details)

**qk (nn,16)** array with various coefficients depending on radius (look in subroutine prep for details)

**ql (nlma,10)** various expressions depending on l and m (look in subroutine prep, loop "do 35" for details)

**qn (nn,6)** Chebyshev integrals

**r (nn)** vector with radial levels,  $r(1)=\text{radtop}$ ,  $r(\text{nn})=\text{radbot}$

**ra** [INPUT] Rayleigh number

**rapr** = Rayleigh number / Prandtl number

**radbot** radius of inner boundary

**radratio** [INPUT] ratio of inner radius to outer radius

**radtop** radius of outer boundary

**rderiv** [SUBROUTINE] radial derivative

**rffti** [SUBROUTINE] subroutine called in chebi

**rstfile** [CHARACT] file name for data in spectral form ('restart data') with prefix "d." or "d0.", "d1." ...; added to outfile set

**runid** [CHAR\*64] text identifying the run

**rva (nn)** auxiliary array used in prep

**rvap (nn)** auxiliary array used in kei, mei

**rvat (nn)** auxiliary array used in kei, mei

**rvb (nn)** auxiliary array used in prep, kei, mei

**rvc (nn)** auxiliary array used in kei, mei

**p (nlma,nn+1)** pressure (spectral form)

**p00co** =  $4/\sqrt{3}$

**prep** [SUBROUTINE] parameter input, set up auxiliary arrays, set initial conditions, etc.

**s (nlma,nn+1)** entropy perturbation (spectral form)

**sc (ncp,ni)** sr stored in complex form

**snlc1 (ncp,ni)** slnr1 stored in complex form

**snlc2 (ncp,ni)** slnr2 stored in complex form

**snlc3 (ncp,ni)** slnr3 stored in complex form

**snlr1 (nrp,ni)** nonlinear term (radial advection) for updating temperature

**snlr2 (nrp,ni)** nonlinear term (theta advection) for updating temperature

**snlr3 (nrp,ni)** nonlinear term (phi advection) for updating temperature

**sr (nrp,ni)** temperature (entropy) on grid points

**s0mat (nn,nn)** LU-decomposed matrix from Chebyshev collocation of temperature equation,  $l=0$ -term.  
Constructed in ludc, used in amhd

**samp** [INPUT] amplitude of initial entropy perturbation

**smat (nn,nn,lmax)** LU-decomposed matrix from Chebyshev collocation of temperature equation. Built  
in ludc, used in amhd

**sr (nja,ni)** entropy on gridpoints

**src** sr stored as complex array

**sscl** = dt

**stor** [SUBROUTINE] store data in restart file

**tei** [SUBROUTINE] calculates thermal energy

**time** time

**timediff** time

**tipdipole** [INPUT] rotate poloidal dipole term when beginning from restart file

**tmovnext** auxiliary variable (next output time) for movie file generation

**tmovstart** [INPUT] time at which to start writing movie-frames on m.\*-file

**tmovstep** [INPUT] time increments for writing movie-frames on m.\*-file

**tops (0:lmax,0:mmax)** [INPUT] harmonic coefficients of prescribed temperature (entropy) on outer bound-  
ary

**treset** [INPUT; LOGICAL] if true reset time and step counter to zero when starting from a stored dataset

**trigsc (nn)** auxiliary array for Chebyshev transform routine created in chebi, used in chebtf

**trigsf (ntf)** auxiliary array for Fourier transform routine created in fft trig, used in fourtf

**tscale** scaling of time in output

**up (nja,3)** phi-component of velocity in equatorial plane for three consecutive radial levels; used in moveout  
to calculate vorticity

**urdp (nja)** derivative  $dv_r/d\phi$  in equatorial plane; used in moveout to calculate vorticity

**vr (nja,ni)** =  $r^2 * v_r$  on grid points

**vrc** vr stored as complex array

**vp (nja,ni)** =  $c * \sin(\theta) * v_\phi$  on grid points

**vpc** vp stored as complex array

**vscale** scaling of velocity in output

**vt (nja,ni)** =  $r * \sin(\theta) * v_\theta$  on grid points

**vtc** vt stored as complex array

**w (nlma,nn+1)** poloidal velocity potential (spectral form)

**wpmat (nn,nn,lmax)** LU-decomposed matrix from Chebyshev collocation of poloidal equation of motion;  
built in ludc, used in amhd

**wnlc1** (**nja/2,ni**) wnlr1 stored in complex form  
**wnlc2** (**nja/2,ni**) wnlr2 stored in complex form  
**wnlc3** (**nja/2,ni**) wnlr3 stored in complex form  
**wnlr1** (**nja,ni**) nonlinear products for updating w (on grid points)  
**wnlr2** (**nja,ni**) nonlinear products for updating z (on grid points)  
**wnlr3** (**nja,ni**) nonlinear products for updating z (on grid points)  
**work** (**lot,nnp2**) work array used in Fourier and Chebyshev transforms  
**wsave** (**nn**) auxiliary array used for Chebyshev transform  
**wscl** =  $dt * radtop^2$   
**y00** =  $1/\sqrt{4*\pi}$   
**z** (**nlma,nn+1**) toroidal velocity potential (spectral form)  
**zscl** =  $dt * radtop^2$   
**zmat** (**nn,nn,lmax**) LU-decomposed matrix from Chebyshev collocation of toroidal equation of motion;  
built in ludc, used in amhd





## Appendix B

# MAG Input File Format

### Introduction

This is an overview of the components of the code, input parameters, structure of output files, etc. MAG expects Unix-styled ASCII files (i.e., no carriage-return character following new line character) for all input files. This can be a nuisance in DOS/Windows systems. You may want to find a text editor that can write Unix-style ASCII files. All parameters are in non-dimensional units unless specified.

### Input Parameters

Parameters have pre-defined (default) values. They are read through a namelist in the subroutine "prep."

#### INPUT, OUTPUT, STEPPING CONTROL, INITIALIZATION OF THE RUN

**outfile** Name of output files (prefixes **d.**, **g.**, **l.**, **ls.**, **me.**, **ma.**, **mm.**, are added)

**infile** Complete name of file from which initial values are read (restart file)

**runid** Arbitrary text of up to 64 characters to describe the model

**init** Set 1 to start from scratch (random noise initial condition); set 0 to start from a previous result obtained on the same grid which has been written into a file named `d[0-9].<name>` set to a value  $\geq 100$  to start from an initial temperature perturbation of one given mode `l,m`. Here, `m` is given by the two last digits of `init` and `l` by the preceding digits; for example `init=606` means that a temperature perturbation of `l=6` and `m=6` is imposed.

**samp** Amplitude of initial perturbation (whether random or single mode)

**nstep** Do one block of `nstep` time step before producing a summary printout of some diagnostics standard output; `nstep` should be even

**nprnt** Do one 'superblock' consisting of `nprnt` blocks of `nstep` time steps each, before saving all data in file `'d[0-9].name'`. If `nstor=1`, there is no number added after the `'d'`; if `nstor>1` the number is incremented by one for each new superblock, starting with zero.

**nstor** Do `nstor` 'superblocks' consisting of `nstep*nprnt` time steps before terminating the process. The total number of time steps is `nstep*nprnt*nstor`; `nstor` must be  $\leq 10$ .

**ngform** Write data at grid points for graphics processing and other post-processing (programs `column.f` `diagnos.f`) into file `'g[0-9].<name>'` each time a superblock is written.

**ngform=2** unformatted file

**ngform=1** formatted file  
**ngform=0** nothing written  
**ngform=-1** comment lines are included into file for easier reading (cannot be used for graphics processing in this form)

**ngrad** Output on graphics file for each ngrad'th radial point

**ngcolat** Output on graphics file every ngcolat'th point in colatitude

**nlon** Output on graphics file every nlon'th point in longitude

**nfilt** If >0 apply filter of type  $F(l) = \exp[-(l/\text{alfilt})^{\text{nfil}}]$  to the radial component of the magnetic field on the outer radius ( $kc=1$ ) before writing data into graphics file (for  $\text{alfilt} > 0$ ). When  $\text{alfilt} < 0$  then apply filter  $F(l) = (1 + \sin(\pi * (l - \text{nfil}) / \text{alfilt}))$  as long as  $|l - \text{nfil}| < 0.5 * \text{alfilt}$ , and  $F=1$  and  $F=0$  respectively for small/large  $l$ .

**alfilt** See under **nfil**

**ivfilt** If >0 apply the same filter as above to the radial velocity at radial level **ivfilt** and write the result into graphics file at the first radial location ( $kc=1$ )

**dipfilt** If **nfil**>0 multiply axial dipole component of  $B_r$  on outer surface by **dipfilt** in graphics output

**nlogstep** Writes data on logfile (prefix **l**.) after each **nlogstep** step

**nplog** If >0, writes velocity values at specific points of the grid on separate logfile (prefix "**lp**." ) after every **nplog** step (for arrays, see **vrpoint**, **vpptpoint**, **vtpoint** in subroutine **amhd** for details)

**iscale** Determines which diffusivity is used for scaling of time, velocity and energy. 1=viscous, 2=thermal, 3=magnetic

**enscale** In output listings, energies are multiplied by **enscale**

**treset** [LOGICAL] If true, reset time and step counter to zero when starting from a stored dataset

**tipdipole** When starting calculation without imposed symmetry (**minc**=1) from a data file with symmetry (**minc**>1), add an equatorial dipole component with **tipdipole** times the magnitude of the polar dipole

**amps** Option for rescaling temperature perturbation (from restart file) by factor **amps** (if not equal to 1)

**ampw** Same for poloidal velocity

**ampz** Same for toroidal velocity

**ampb** Same for poloidal magnetic field

**ampj** Same for toroidal magnetic field

**ifvfrz** [LOGICAL] If true, do not update velocity during iteration

**ifbfrz** [LOGICAL] If true, do not update magnetic field during iteration

**ifsfrz** [LOGICAL] If true, do not update temperature during iteration

## TIME STEP CONTROL

**dtmin** Minimum time step (in seconds). If the dynamically determined time step becomes less, the program terminates.

**dtmax** Maximum (and usually initial) time step. This must be less than  $0.25 \cdot \text{ek}$ . Between dtmax and dtmin the actual time step is controlled by a Courant criterion (see below).

**dtstart** Initial time step. If dtmax=0, dtmax is used for the initial time step when init>0 and the last time step used in the previous run (stored in the restart file) is used when init=0.

**courfac** Controls the contribution of the fluid velocity to the Courant time step limit (a larger value leads to smaller dt)

**alfac** Controls the contribution of the (modified) Alfven velocity to the Courant time step limit (a larger value leads to smaller dt)

**icour** Check Courant criterion after each icour time step (even numbers)

## PHYSICAL CONTROL PARAMETERS

**ra** Rayleigh number (defined with gravity on outer boundary)

**ek** Ekman number

**pr** Prandtl number

**prmag** Magnetic Prandtl number

**radratio** Ratio of inner to outer radius

**bpeak** Peak value of magnetic field imposed by boundary conditions at ICB (also when imagcon=0, bpeak controls the initial magnetic field: toroidal when bpeak>0, poloidal dipole when bpeak<0!)

**epsc0** Volumetric rate of internal heating

## BOUNDARY CONDITIONS AT INNER AND OUTER RADII

**ktops** thermal boundary condition at CMB. 1-fixed temp, 2-fixed radial heat flow. (ktops=2 not tested!).

**kbots** thermal boundary condition at ICB. As above.

**ktopv** velocity condition at CMB. 1-free, 2-rigid.

**kbotv** velocity condition at ICB. As above.

**kbotb** =1 for insulating inner core =2: ideally conducting inner core

**ktopb** =1 for insulating mantle =2: not implemented! imagcon: <0 imposed poloidal field (l=1,m=0) at ICB >=0 imposed toroidal field (l=2,m=0) at ICB >=10 imposed toroidal field (l=2,m=0) at both CMB and ICB (same amplitude and same sign if =10, opposite sign if =11)

**cmb** If >0, thin conducting layer at bottom of mantle (not tested!)

## HYPERDIFFUSIVITIES

**difamp** Amplitude of hyperdiffusivities

**ldif** Hyperdiffusivities applied for harmonic degrees  $l \geq \text{ldif}$

**ldifexp** Exponent for increase of hyperdiffusivities with  $l$  (analytical details see definition of ql(lm,11) in prep.f)

**PARAMETERS FOR GENERATING MOVIE FILES**

**imovopt** Three-digit integer number, options for generating movie files

**Last digit > 0** Write  $B_z$ ,  $W_z$  (vorticity) and  $T$  in the equatorial plane on file with prefix "me."

**2nd last digit > 0** Write longitudinally averaged  $B_\phi$ ,  $j_\phi$  and  $v_\phi$  on file with prefix "ma."

**3rd last digit > 0** Write  $B_r$  at outer surface and  $B_r$  and  $v_r$  at mid- depth on file with prefix "mm."

**4th last digit > 0** Write spherical harmonic coefficients for poloidal field at outer boundary and for velocity potentials at radial level given by this digit on file with prefix "cc." (This option is not working for this release).

**iframes** Write altogether iframes frames on the movie files

**tmovstart** Time at which to start writing movie-frames

**tmovstep** Time increments for writing movie-frames

# Appendix C

## MAG Output File Format

MAG produces a set of output files for further processing. All outputs are in non-dimensional units unless specified.

**l.[outfile]** Lists a set of diagnostic values each nlogstep time-steps

**ls.[outfile]** Spectra of kinetic energy and magnetic field every nprint timesteps, sorted for modes with equal l, and additionally sorted for modes with equal m.

**g.[outfile] or g[i].[outfile]** where i=0,1,2,..9 (optional, written when ngstep>0) – Contains temperature, velocity and magnetic field components for graphics processing (idl-program magts)

**d.[outfile] or d[i].outfile** Restart files with the complete set of variables (stored as spectral values l,m in the angular coordinates for radial grid-levels)

**lp.[outfile]** Written when nplog>0. Velocity at specific points written every nplog'th time step.

**me.[outfile]** Written when last digit of imovopt>0. Values in the equatorial plane for producing movie (idl-program movie2; not provided in this release)

**mm.[outfile]** Written when first digit of imovopt>0. Values on spherical surfaces for producing movie (idl-program )

**ma.[outfile]** Written when second digit of imovopt>0. Longitudinal averages for producing movie (movie program does not yet exist).

**Note:** If one of the abovefiles already exists, the program will not run.

The standard output file contains summaries of grid paramaters and all process control and physical parameters that occur in the namelist statements. It lists the values of non-dimensional parameters and of the various diffusive time-scales. Then, at the end of each block, it lists a number of diagnostic values:

Parameters	Definitions
dt	actual time step
dtrmin	Courant time calculated with radial velocities
dthmin	Courant time calculated with horizontal velocities
cour	maximum inverse Courant time based on radial fluid velocity
couh	maximum inverse Courant time based on horizontal fluid velocity
alfr	maximum inverse Courant time based on radial modified Alfven velocity
alfh	maximum inverse Courant time based on horizontal modified Alfven velocity (in addition, the radial level at which the maximum is reached is indicated)
ent	total energy
env	kinetic energy
enb	magnetic energy

The meaning of other quantities is obvious.

For the primary variables, the modes for which they assume their absolute maximum and the maximum are printed. Maxima are determined for the toroidal potential multiplied by  $1/r$ , and for poloidal potentials multiplied by  $l(l+1)/r^2$ , in order to find the modes which exhibit the maximum longitudinal toroidal velocity (field strength) and the maximum radial velocity (field strength), respectively.

**l.[outfile]** printed every nlogstep time step, one record is printed that contains 17 output fields:

- 1) time
- 2) mean kinetic energy density
- 3) mean poloidal kinetic energy density
- 4) mean magnetic energy density
- 5) mean poloidal magnetic energy density
- 6) mean axisymmetric toroidal kinetic energy density
- 7) mean axisymmetric poloidal kinetic energy density
- 8) mean axisymmetric poloidal magnetic energy density
- 9) mean axisymmetric toroidal magnetic energy density
- 10) mean top heatflow (nusselt number)
- 11) mean bottom heatflow (nusselt number)
- 12) mean magnetic field strength
- 13) rms dipole, outer boundary
- 14) rms axial dipole, outer boundary
- 15) dipole tilt, outer boundary
- 16) dipole longitude, outer boundary
- 17) mean velocity

**ls.[outfile]** Printed each nprint time step are four records with time being the first variable followed by the spectral power of kinetic and magnetic energy, respectively, as a function of harmonic degree  $l$ , from  $l=0$  to  $l_{\max}$  (first two records in a block), and spectral power as a function of harmonic order  $m$  in the last two records of a block.

# Appendix D

## License

**GNU GENERAL PUBLIC LICENSE Version 2, June 1991. Copyright (C) 1989, 1991 Free Software Foundation, Inc. 59 Temple Place, Suite 330, Boston, MA 02111-1307 USA**

Everyone is permitted to copy and distribute verbatim copies of this license document, but changing it is not allowed.

### Preamble

The licenses for most software are designed to take away your freedom to share and change it. By contrast, the GNU General Public License is intended to guarantee your freedom to share and change free software – to make sure the software is free for all its users. This General Public License applies to most of the Free Software Foundation’s software and to any other program whose authors commit to using it. (Some other Free Software Foundation software is covered by the GNU Library General Public License instead.) You can apply it to your programs, too.

When we speak of free software, we are referring to freedom, not price. Our General Public Licenses are designed to make sure that you have the freedom to distribute copies of free software (and charge for this service if you wish), that you receive source code or can get it if you want it, that you can change the software or use pieces of it in new free programs; and that you know you can do these things.

To protect your rights, we need to make restrictions that forbid anyone to deny you these rights or to ask you to surrender the rights. These restrictions translate to certain responsibilities for you if you distribute copies of the software, or if you modify it.

For example, if you distribute copies of such a program, whether gratis or for a fee, you must give the recipients all the rights that you have. You must make sure that they, too, receive or can get the source code. And you must show them these terms so they know their rights.

We protect your rights with two steps:

1. Copyright the software, and
2. Offer you this license which gives you legal permission to copy, distribute and/or modify the software.

Also, for each author’s protection and ours, we want to make certain that everyone understands that there is no warranty for this free software. If the software is modified by someone else and passed on, we want its recipients to know that what they have is not the original, so that any problems introduced by others will not reflect on the original authors’ reputations.

Finally, any free program is threatened constantly by software patents. We wish to avoid the danger that redistributors of a free program will individually obtain patent licenses, in effect making the program proprietary. To prevent this, we have made it clear that any patent must be licensed for everyone’s free use or not licensed at all.

The precise terms and conditions for copying, distribution and modification follow.

## GNU GENERAL PUBLIC LICENSE TERMS AND CONDITIONS FOR COPYING, DISTRIBUTION AND MODIFICATION

This License applies to any program or other work which contains a notice placed by the copyright holder saying it may be distributed under the terms of this General Public License. The "Program," below, refers to any such program or work, and a "work based on the Program" means either the Program or any derivative work under copyright law: that is to say, a work containing the Program or a portion of it, either verbatim or with modifications and/or translated into another language. (Hereinafter, translation is included without limitation in the term "modification.") Each licensee is addressed as "you."

Activities other than copying, distribution and modification are not covered by this License; they are outside its scope. The act of running the Program is not restricted, and the output from the Program is covered only if its contents constitute a work based on the Program (independent of having been made by running the Program). Whether that is true depends on what the Program does.

1. You may copy and distribute verbatim copies of the Program's source code as you receive it, in any medium, provided that you conspicuously and appropriately publish on each copy an appropriate copyright notice and disclaimer of warranty; keep intact all the notices that refer to this License and to the absence of any warranty; and give any other recipients of the Program a copy of this License along with the Program.

You may charge a fee for the physical act of transferring a copy, and you may at your option offer warranty protection in exchange for a fee.

2. You may modify your copy or copies of the Program or any portion of it, thus forming a work based on the Program, and copy and distribute such modifications or work under the terms of Section 1 above, provided that you also meet all of these conditions:
  - (a) You must cause the modified files to carry prominent notices stating that you changed the files and the date of any change.
  - (b) You must cause any work that you distribute or publish, that in whole or in part contains or is derived from the Program or any part thereof, to be licensed as a whole at no charge to all third parties under the terms of this License.
  - (c) If the modified program normally reads commands interactively when run, you must cause it, when started running for such interactive use in the most ordinary way, to print or display an announcement including an appropriate copyright notice and a notice that there is no warranty (or else, saying that you provide a warranty) and that users may redistribute the program under these conditions, and telling the user how to view a copy of this License. (Exception: if the Program itself is interactive but does not normally print such an announcement, your work based on the Program is not required to print an announcement.)

These requirements apply to the modified work as a whole. If identifiable sections of that work are not derived from the Program, and can be reasonably considered independent and separate works in themselves, then this License, and its terms, do not apply to those sections when you distribute them as separate works. But when you distribute the same sections as part of a whole which is a work based on the Program, the distribution of the whole must be on the terms of this License, whose permissions for other licensees extend to the entire whole, and thus to each and every part regardless of who wrote it.

Thus, it is not the intent of this section to claim rights or contest your rights to work written entirely by you; rather, the intent is to exercise the right to control the distribution of derivative or collective works based on the Program.

In addition, mere aggregation of another work not based on the Program with the Program (or with a work based on the Program) on a volume of a storage or distribution medium does not bring the other work under the scope of this License.



3. You may copy and distribute the Program (or a work based on it, under Section 2) in object code or executable form under the terms of Sections 1 and 2 above provided that you also do one of the following:
  - (a) Accompany it with the complete corresponding machine-readable source code, which must be distributed under the terms of Sections 1 and 2 above on a medium customarily used for software interchange; or,
  - (b) Accompany it with a written offer, valid for at least three years, to give any third party, for a charge no more than your cost of physically performing source distribution, a complete machine-readable copy of the corresponding source code, to be distributed under the terms of Sections 1 and 2 above on a medium customarily used for software interchange; or,
  - (c) Accompany it with the information you received as to the offer to distribute corresponding source code. (This alternative is allowed only for noncommercial distribution and only if you received the program in object code or executable form with such an offer, in accord with Subsection b above.)

The source code for a work means the preferred form of the work for making modifications to it. For an executable work, complete source code means all the source code for all modules it contains, plus any associated interface definition files, plus the scripts used to control compilation and installation of the executable. However, as a special exception, the source code distributed need not include anything that is normally distributed (in either source or binary form) with the major components (compiler, kernel, and so on) of the operating system on which the executable runs, unless that component itself accompanies the executable.

If distribution of executable or object code is made by offering access to copy from a designated place, then offering equivalent access to copy the source code from the same place counts as distribution of the source code, even though third parties are not compelled to copy the source along with the object code.

4. You may not copy, modify, sublicense, or distribute the Program except as expressly provided under this License. Any attempt otherwise to copy, modify, sublicense or distribute the Program is void, and will automatically terminate your rights under this License. However, parties who have received copies, or rights, from you under this License will not have their licenses terminated so long as such parties remain in full compliance.
5. You are not required to accept this License, since you have not signed it. However, nothing else grants you permission to modify or distribute the Program or its derivative works. These actions are prohibited by law if you do not accept this License. Therefore, by modifying or distributing the Program (or any work based on the Program), you indicate your acceptance of this License to do so, and all its terms and conditions for copying, distributing or modifying the Program or works based on it.
6. Each time you redistribute the Program (or any work based on the Program), the recipient automatically receives a license from the original licensor to copy, distribute or modify the Program subject to these terms and conditions. You may not impose any further restrictions on the recipients' exercise of the rights granted herein. You are not responsible for enforcing compliance by third parties to this License.
7. If, as a consequence of a court judgment or allegation of patent infringement or for any other reason (not limited to patent issues), conditions are imposed on you (whether by court order, agreement or otherwise) that contradict the conditions of this License, they do not excuse you from the conditions of this License. If you cannot distribute so as to satisfy simultaneously your obligations under this License and any other pertinent obligations, then as a consequence you may not distribute the Program at all. For example, if a patent license would not permit royalty-free redistribution of the Program by all those who receive copies directly or indirectly through you, then the only way you could satisfy

both it and this License would be to refrain entirely from distribution of the Program.

If any portion of this section is held invalid or unenforceable under any particular circumstance, the balance of the section is intended to apply and the section as a whole is intended to apply in other circumstances.

It is not the purpose of this section to induce you to infringe any patents or other property right claims or to contest validity of any such claims; this section has the sole purpose of protecting the integrity of the free software distribution system, which is implemented by public license practices. Many people have made generous contributions to the wide range of software distributed through that system in reliance on consistent application of that system; it is up to the author/donor to decide if he or she is willing to distribute software through any other system and a licensee cannot impose that choice.

This section is intended to make thoroughly clear what is believed to be a consequence of the rest of this License.

8. If the distribution and/or use of the Program is restricted in certain countries either by patents or by copyrighted interfaces, the original copyright holder who places the Program under this License may add an explicit geographical distribution limitation excluding those countries, so that distribution is permitted only in or among countries not thus excluded. In such case, this License incorporates the limitation as if written in the body of this License.
9. The Free Software Foundation may publish revised and/or new versions of the General Public License from time to time. Such new versions will be similar in spirit to the present version, but may differ in detail to address new problems or concerns.

Each version is given a distinguishing version number. If the Program specifies a version number of this License which applies to it and "any later version," you have the option of following the terms and conditions either of that version or of any later version published by the Free Software Foundation. If the Program does not specify a version number of this License, you may choose any version ever published by the Free Software Foundation.

10. If you wish to incorporate parts of the Program into other free programs whose distribution conditions are different, write to the author to ask for permission. For software which is copyrighted by the Free Software Foundation, write to the Free Software Foundation; we sometimes make exceptions for this. Our decision will be guided by the two goals of preserving the free status of all derivatives of our free software and of promoting the sharing and reuse of software generally.

## NO WARRANTY

11. BECAUSE THE PROGRAM IS LICENSED FREE OF CHARGE, THERE IS NO WARRANTY FOR THE PROGRAM, TO THE EXTENT PERMITTED BY APPLICABLE LAW. EXCEPT WHEN OTHERWISE STATED IN WRITING THE COPYRIGHT HOLDERS AND/OR OTHER PARTIES PROVIDE THE PROGRAM "AS IS" WITHOUT WARRANTY OF ANY KIND, EITHER EXPRESSED OR IMPLIED, INCLUDING, BUT NOT LIMITED TO, THE IMPLIED WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR PURPOSE. THE ENTIRE RISK AS TO THE QUALITY AND PERFORMANCE OF THE PROGRAM IS WITH YOU. SHOULD THE PROGRAM PROVE DEFECTIVE, YOU ASSUME THE COST OF ALL NECESSARY SERVICING, REPAIR OR CORRECTION.
12. IN NO EVENT UNLESS REQUIRED BY APPLICABLE LAW OR AGREED TO IN WRITING WILL ANY COPYRIGHT HOLDER, OR ANY OTHER PARTY WHO MAY MODIFY AND/OR REDISTRIBUTE THE PROGRAM AS PERMITTED ABOVE, BE LIABLE TO YOU FOR DAMAGES, INCLUDING ANY GENERAL, SPECIAL, INCIDENTAL OR CONSEQUENTIAL DAMAGES ARISING OUT OF THE USE OR INABILITY TO USE THE PROGRAM (INCLUDING

BUT NOT LIMITED TO LOSS OF DATA OR DATA BEING RENDERED INACCURATE OR LOSSES SUSTAINED BY YOU OR THIRD PARTIES OR A FAILURE OF THE PROGRAM TO OPERATE WITH ANY OTHER PROGRAMS), EVEN IF SUCH HOLDER OR OTHER PARTY HAS BEEN ADVISED OF THE POSSIBILITY OF SUCH DAMAGES.

## END OF TERMS AND CONDITIONS

### How to Apply These Terms to Your New Programs

If you develop a new program, and you want it to be of the greatest possible use to the public, the best way to achieve this is to make it free software which everyone can redistribute and change under these terms.

To do so, attach the following notices to the program. It is safest to attach them to the start of each source file to most effectively convey the exclusion of warranty; and each file should have at least the "copyright" line and a pointer to where the full notice is found. For example:

One line to give the program's name and a brief idea of what it does. Copyright (C) (year) (name of author)

This program is free software; you can redistribute it and/or modify it under the terms of the GNU General Public License as published by the Free Software Foundation; either version 2 of the License, or (at your option) any later version.

This program is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License for more details.

You should have received a copy of the GNU General Public License along with this program; if not, write to the Free Software Foundation, Inc., 59 Temple Place, Suite 330, Boston, MA 02111-1307 USA

Also add information on how to contact you by electronic and paper mail.

If the program is interactive, make it output a short notice like this when it starts in an interactive mode:

Gnomovision version 69, Copyright (C) year name of author Gnomovision comes with ABSOLUTELY NO WARRANTY; for details type 'show w'. This is free software, and you are welcome to redistribute it under certain conditions; type 'show c' for details.

The hypothetical commands 'show w' and 'show c' should show the appropriate parts of the General Public License. Of course, the commands you use may be called something other than 'show w' and 'show c'; they could even be mouse-clicks or menu items – whatever suits your program.

You should also get your employer (if you work as a programmer) or your school, if any, to sign a "copyright disclaimer" for the program, if necessary. Here is a sample; alter the names:

Yoyodyne, Inc., hereby disclaims all copyright interest in the program 'Gnomovision' (which makes passes at compilers) written by James Hacker.

(signature of Ty Coon)

1 April 2006

Ty Coon, President of Vice

This General Public License does not permit incorporating your program into proprietary programs. If your program is a subroutine library, you may consider it more useful to permit linking proprietary applications with the library. If this is what you want to do, use the GNU Library General Public License instead of this License.



# Bibliography

- [1] Olson, P., G.A. Glatzmaier (1995), Highly supercritical thermal convection in a rotating spherical shell: centrifugal vs. radial gravity. *Geophys. Astrophys. Fluid Dyn.*, *70*, 113-136
- [2] Olson, P., G.A. Glatzmaier (1995), Magnetoconvection in a rotating spherical shell: structure of flow in the outer core. *Phys. Earth Planet Int.*, *92*, 109-118
- [3] Olson, P., G.A. Glatzmaier (1996), Magnetoconvection and Thermal Coupling of the Earth's Core and Mantle. *Phil. Trans. R. Soc. Lond.*, *A354*, 1413-1424
- [4] Olson, P., U. Christensen, G.A. Glatzmaier (1999), Numerical Modeling of the Geodynamo: Mechanisms of Field Generation and Equilibration. *J. Geophys. Res.*, *104*, 10,383-10,404
- [5] Christensen, U., Olson, P., G.A. Glatzmaier (1999), Numerical modelling of the geodynamo: a systematic parameter study. *Geophys. J. Int.*, *138*, 393-409
- [6] Christensen, et al. (2001), A numerical dynamo benchmark. *Phys. Earth Planet Int.*, *128*, 25-34 (benchmark cases)
- [7] Olson, P., G.A. Glatzmaier (2005), Probing the geodynamo. *Scientific American* *15*:2, 29-35
- [8] Christensen, U.R. and Aubert, J. (2006), Scaling properties of convection-driven dynamos in rotating spherical shells and application to planetary magnetic fields. *Geophys J. Int.* *166*, 97-114.