732A96: AML - Computer Lab 1

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#	Set up general options	
kı	<pre>nitr::opts_chunk\$set(echo = FALSE, warning = FALSE, message = FALSE,</pre>	
1: 0] 1:	<pre>et.seed(12345) ibrary(ggplot2) ptions(kableExtra.latex.load_packages = FALSE) ibrary(kableExtra) ptions(scipen=999)</pre>	
1:	<pre>Prepare packages ibrary("bnlearn") # ls('package:bnlearn') # to show all functions ibrary("gRain") ibrary('RBGL')</pre>	
	Auxilary functions nalyze_cm = function(cm, true){	
	<pre>stopifnot(true %in% colnames(cm)) levels = c(true, colnames(cm)[-which(colnames(cm) == true)]) # ORDER: 1; 0 cm = as.data.frame(cm); colnames(cm)[1:2] = c("True", "Pred") N = sum(cm\$Freq[which(cm\$True == levels[1])])</pre>	

1 Assignment 1: Hill Climbing

Object of change

The purpose of the lab is to put in practice some of the concepts covered in the lectures.

(1) Show that multiple runs of the hill-climbing algorithm can return non-equivalent Bayesian network (BN) structures. Explain why this happens. Use the Asia dataset which is included in the bnlearn package. To load the data, run data("asia").

Hint: Check the function hc in the bnlearn package. Note that you can specify the initial structure, the number of random restarts, the score, and the equivalent sam- ple size (a.k.a imaginary sample size) in the BDeu score. You may want to use these options to answer the question. You may also want to use the functions plot, arcs, vstructs, cpdag and all.equal.

```
# Prepare data
data("asia")
df = data.frame(asia)
rm(asia)
head(df)
##
      Α
          S
              Τ
                          Ε
                              Х
                 L
                      В
                                  D
## 1 no yes
            no no yes
                         no
                             no yes
## 2 no yes
             no no
                     no
                         no
                             no
                                 no
## 3 no no yes no
                     no yes yes yes
## 4 no
        no
             no no yes
                             no yes
                         no
## 5 no no
             no no
                             no yes
                     no
                         no
## 6 no yes
            no no
                             no yes
                     no
                         no
```

- A change in direction of certain arrows (i.e. relations) was the main change that was observed.
- When the score criterion changed, some arrows appeared/disappeared completely.

Reason for changes

According to the documentation, Hill-Climbing (hc) is a a hill climbing greedy search that explores the space of the directed acyclic graphs by single-arc addition, removal and reversals; with random restarts to avoid local optima. The optimized implementation uses score caching, score decomposability and score equivalence to reduce the number of duplicated tests. Hence, the reasons for non-equivalent BN structures are:

- random restarts: If different initial starting points are found, the algorithm may get stuck in (different) local optima. The parameter restart has to be larger than 0 to allow this variation.
- same scores: The example below shows that non-equivalent BNs can have the same score (e.g. BIC score). Hence, the algorithm has no incentive to prioritze the one or the other of these non-equivalent BNs.
- different scores metrics: If different evaluation criteria are used e.g. BIC vs. AIC, the space of the DAGs is explored differently and hence, different results are possible.

Example 1 (random restarts)

In the example below, we set restart=10 and we can see that the arrow points from L to S vs. from S to L in the two diagrams.

```
# Train models
res1 = hc(df, restart=10, score='bic')
res2 = hc(df, restart=10, score='bic')
## [1] "Different arc sets"
## Score BN 1: -11107.29
## Score BN 2: -11107.29
                                          Run 2 (with BIC)
       Run 1 (with BIC)
## true positive (tp) arcs, which appear both in target and in current: 6
## false positive (fp) arcs, which appear in current but not in target: 1
## false negative (fn) arcs, which appear in target but not in current: 1
## Same Skeleton: TRUE
## Hamming distance (zero if same skeleton): 0
## Struct. hamming distance: 0
Example 2 (different scores metrics: aic)
```

After using aic, we see that the resulting networks looks very different than the above networks (comparison to the 2nd network from above). This time, also the score differs since a different score metric was used for training.

```
res3 = hc(df, restart=10, score='aic')
```

Score BN 3: -11129.57
Run 2 (with BIC)

Run 3 (with AIC)

S

S

B

E

X

Alternatives

We can also randomly initialize a graph and run hc. If we do this several times, we may also notice different structures due to to different random starting points. They may cause the heuristic algorithm to get stuck in different local optima. If we were to then increase the restart parameter from e.g. 1 to 1000, we still get the same result because hc (likely) manages to find the global optimum.

```
rand = random.graph(colnames(df))
res4 = hc(asia, start = rand)
```

References

- http://www.bnlearn.com/examples/compare-dags/
- http://bnlearn.com/examples/score/

2 Assignment 2: Structure/Parameter Learning and Inference

Learn a BN from 80 % of the Asia dataset. The dataset is included in the bnlearn package. To load the data, run data("asia"). Learn both the structure and the parameters. Use any learning algorithm and settings that you consider appropriate. Use the BN learned to classify the remaining 20 % of the Asia dataset in two classes: S = yes and S = no. In other words, compute the posterior probability distribution of S for each case and classify it in the most likely class. To do so, you have to use exact or approximate inference with the help of the bnlearn and gRain packages, i.e. you are not allowed to use functions such as predict. Report the confusion matrix, i.e. true/false positives/negatives. Compare your results with those of the true Asia BN, which can be obtained by running dag = model2network("[A][S][T|A][L|S][B|S][D|B:E][E|T:L][X|E]").

Hint: You already know the Lauritzen-Spiegelhalter algorithm for inference in BNs, which is an exact algorithm. There are also approximate algorithms for when the exact ones are too demanding computationally. For exact inference, you may need the functions bn.fit and as.grain from the bnlearn package, and the functions compile, setFinding and querygrain from the package gRain. For approximate inference, you may need the functions prop.table, table and cpdist from the bnlearn package. When you try to load the package gRain, you will get an error as the pack- age RBGL cannot be found. You have to install this package by running the following two commands (answer no to any offer to update packages):

```
source("https://bioconductor.org/biocLite.R")
biocLite("RBGL")
```

Prepare data

```
# Prepare data
data("asia")
df = asia
#df = data.frame(apply(asia, 2, as.character), stringsAsFactors = F)
rm(asia)

# Split data randomly
set.seed(12345)
N = nrow(df)
idx = sample(1:N, round(N * 0.8))
df_tr = df[idx, ]
df_te = df[-idx, ]
```

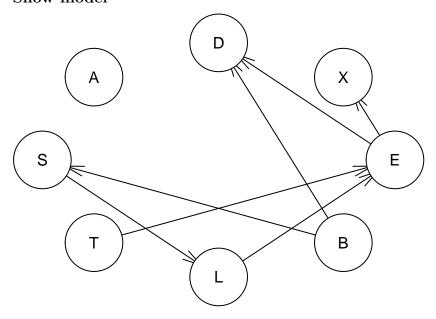
Fit model on training data

First, we have to learn the network structure and second we have to learn the parameters. To learn the stucture, we could choose one out of many different algorithms: constraint-based, score based, local search. Here, the (BIC) score-based algorithm Hill-Climbing is used. For learning the parameters, the method mle was used (for Bayesian parameter estimation).

```
# Fit the structure (given data set)
dag = hc(df_tr, restart=100, score='bic')
# dag = iamb(df_tr)

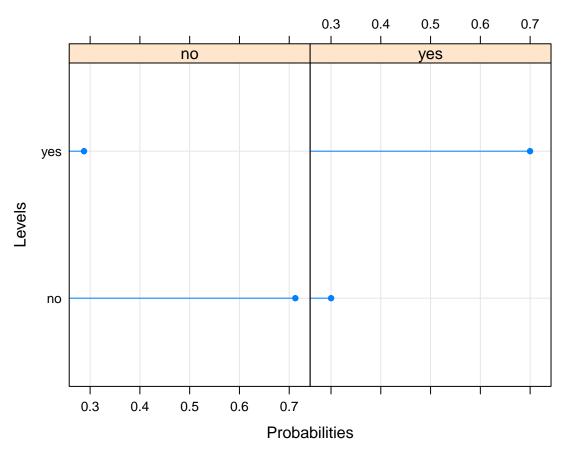
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(dag, df_tr, method='mle')
```

Show model



```
##
## Parameters of node S (multinomial distribution)
##
## Conditional probability table:
##
## B
## S no yes
## no 0.7122665 0.3001486
## yes 0.2877335 0.6998514
```

Conditional Probabilities for Node S



Evaluate model on test data

Here, we use the BN learned to classify the remaining 20 % of the Asia dataset in two classes: S = yes and S = no. We compute the posterior probability distribution of S for each case and classify it in the most likely class. For that, we use the packages **bnlearn** (for approximate inference with Monte Carlo) or gRain (for exact inference).

Exact inference

```
N = nrow(df_te)
  Y true = df te[[y name]]
  Y pred = numeric(length = N)
  Y_space = as.character(unique(Y_true))
  for (i in 1:N){
    # With all RVs
    x = df_te[i, colnames(df_te) != y_name]
    if (markov == FALSE){
      var_names = names(x)
      var_values = vapply(x, as.character, character(1))
    } else {
      var_names = mb(dag_fitted, y_name)
      var_values = vapply(x, as.character, character(1))[var_names]
    }
    evidence = setEvidence(junction, nodes = var_names, states = var_values)
    Y_prob = querygrain(evidence, nodes = y_name)[[1]]
    Y pred[i] = Y space[which.max(Y prob)]
  }
  return(list(Y pred = Y pred, Y true = Y true))
}
# Make predictions
res = predict_exact(dag_fitted, df_te, "S")
Y true = res$Y true
Y pred = res$Y pred
## Confusion matrix (absolute):
##
        Predicted
## True
         no yes
##
    no 322 146
##
    yes 120 412
##
## Confusion matrix (relative):
##
        Predicted
## True
             no
                   yes
##
    no 0.0644 0.0292
##
     yes 0.0240 0.0824
```

Performance statistics:

MCR	Accuracy	Recall	Precision	FPR	TNR
0.266	0.734	0.7744361	0.7383513	0.3119658	0.6880342

Approximate inference

Note: cpquery was used here instead of cdist. Unfortunately, we had to hardcode various values for that. Also, there was an issue with using cpquery in a function: It could only find \mathbf{x} if it is in the main working environment.

```
# -----
# Input:
# - dag_fitted: dag with learned structure and parameters
# - df_te: data frame with all features and the Y (all factors)
# MAKE SURE TO ADJUST THE EVIDENCE AND EVENT!
N = nrow(df te)
Y_{true} = df_{te}[['S']]
Y pred = numeric(length = N)
Y space = as.character(unique(Y true))
Y_prob = numeric(length = length(Y_space))
junction = compile(as.grain(dag fitted))
for (i in 1:N){
 # With all RVs
 x = vapply(df_te[i, colnames(df_te) != 'S'], as.character, character(1))
 for (j in 1:length(Y_space)){
   Y_prob[j] = cpquery(dag_fitted, event = (S == Y_space[j]),
                         evidence = ((A == x['A']) & (T == x['T'])
                                     & (L == x['L']) & (B == x['B'])
                                     & (E == x['E']) & (X == x['X'])
                                     & (D == x['E'])
                       )
 }
 Y pred[i] = Y space[which.max(Y prob)]
}
## Confusion matrix (absolute):
##
       Predicted
## True
        no yes
##
    no 322 146
    yes 122 410
##
```

```
##
## Confusion matrix (relative):
## Predicted
## True no yes
## no 0.322 0.146
## yes 0.122 0.410
##
## Performance statistics:
```

MCR	Accuracy	Recall	Precision	FPR	TNR
0.268	0.732	0.7706767	0.7374101	0.3119658	0.6880342

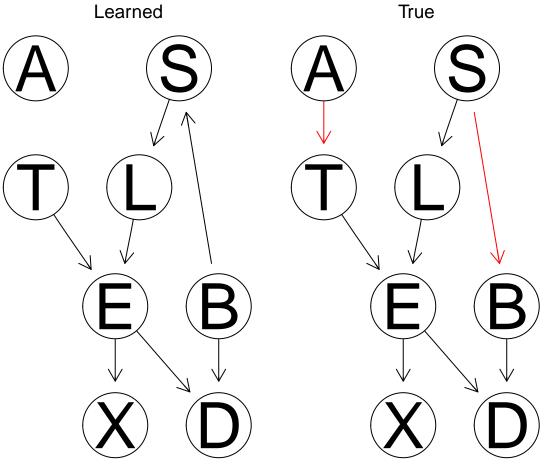
Comparison with true DAG (only exact inference)

```
# Prepare the structure

# Option 1:
dag_true = model2network("[A][S][T|A][L|S][B|S][D|B:E][E|T:L][X|E]")

# #Option 2
# dag_true = empty.graph(names(df))
# modelstring(dag_true) = "[A][S][T|A][L|S][B|S][D|B:E][E|T:L][X|E]"

# Visual comparison only:
par(mfrow = c(1, 2))
graphviz.compare(dag, dag_true, main = c("Learned", "True"))
```



```
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(dag_true, df_tr, method='mle')
# Make predictions
res = predict_exact(dag_fitted, df_te, "S")
Y_true = res$Y_true
Y_pred = res$Y_pred
## Confusion matrix (absolute):
##
        Predicted
## True
          no yes
##
        322 146
    no
##
     yes 120 412
##
## Confusion matrix (relative):
##
        Predicted
## True
            no
                 yes
##
     no 0.322 0.146
##
    yes 0.120 0.412
##
```

Performance statistics:

MCR	Accuracy	Recall	Precision	FPR	TNR
0.266	0.734	0.7744361	0.7383513	0.3119658	0.6880342

References

- http://bnlearn.com/examples/whitelist/
- http://bnlearn.com/documentation/man/structure.learning.html
- http://bnlearn.com/examples/fit/

3 Assignment 3: Structure/Parameter Learning and Inference (Markov Blanket)

In the previous exercise, you classified the variable S given observations for all the rest of the variables. Now, you are asked to classify S given observations only for the so-called Markov blanket of S, i.e. its parents plus its children plus the parents of its children minus S itself. Report again the confusion matrix.

Hint: You may want to use the function mb from the bnlearn package.

Exact inference

Note: This time we only use *Exact inference*.

The confusion matrix looks exactly the same as before. This seems expected since variables that are not in the Markov blanket of S only have a rather small relationship with S and hence don't help with the classification.

```
# Fit the structure (given data set)
dag = hc(df tr, restart=10, score='bic')
# Fit the parameters (given structure and data set)
dag fitted = bn.fit(dag, df tr, method='mle')
# Make predictions
res = predict_exact(dag fitted, df te, "S", markov = TRUE)
Y true = res$Y true
Y pred = res$Y pred
## Confusion matrix (absolute):
##
        Predicted
## True
         no yes
##
        322 146
     yes 120 412
##
```

Confusion matrix (relative):

```
## Predicted
## True no yes
## no 0.322 0.146
## yes 0.120 0.412
```

##

Performance statistics:

MCR	Accuracy	Recall	Precision	FPR	TNR
0.266	0.734	0.7744361	0.7383513	0.3119658	0.6880342

4 Assignment 4: Naive Bayes

Repeat the exercise (2) using a naive Bayes classifier, i.e. the predictive variables are independent given the class variable. See p. 380 in Bishop's book or Wikipedia for more information on the naive Bayes classifier. Model the naive Bayes classifier as a BN. You have to create the BN by hand, i.e. you are not allowed to use the function naive.bayes from the bnlearn package.

Hint: Check http://www.bnlearn.com/examples/dag/ to see how to create a BN by hand.

Review Naive Bayes

Conditional probability is defined as:

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$
$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

Solving both equations for $P(A \cap B)$ and setting them equal, we get:

$$P(A|B)P(B) = P(B|A)P(A)$$
$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

Replace A with S and B with X (all other variables):

$$P(S|X) = \frac{P(X|S)P(S)}{P(X)} \propto P(X|S)P(S)$$

Since we have several Xs and since they are assumed to be independent (recall that independence implies that P(A, B) = P(A)P(B)):

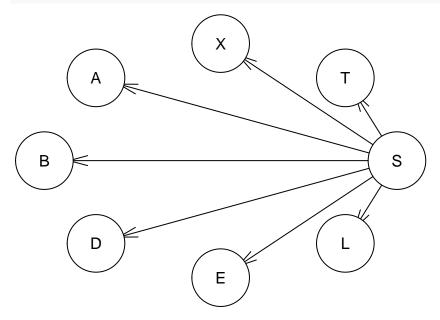
$$P(S|X) \propto P(X_1, X_2, ..., X_n|S)P(S) = P(X_1|S)P(X_2|S)...P(X_D|S)P(S) = P(S)\prod_{d=1}^{D} P(X_d|S)$$

The above tells us that S has to point to all X. Finally, classifications in naive bayes for observation i are done by:

$$\operatorname{argmax}_{S_i} P(S_i) \prod_{d=1}^{D} P(X_{i,d}|S_i)$$

Creating network structure

```
# S pointing to all variables
IVs = paste0("[", colnames(df_tr)[-which(colnames(df_tr)=='S')], "|S]", collapse = "")
naive_bayes = model2network(paste0("[S]", IVs))
plot(naive_bayes)
```



Exact inference

Note: This time we only use *Exact inference*.

The confusion matrix looks exactly the same as before. This seems expected since variables that are not in the Markov blanket of S only have a rather small relationship with S and hence don't help with the classification.

```
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(naive_bayes, df_tr, method = 'mle')

# Make predictions
res = predict_exact(dag_fitted, df_te, "S", markov = TRUE)
Y_true = res$Y_true
Y_pred = res$Y_pred
```

```
## Confusion matrix (absolute):
##
        Predicted
## True
           no yes
##
     no
         349 119
##
     yes 188 344
##
  Confusion matrix (relative):
##
##
        Predicted
## True
             no
                  yes
##
         0.349 0.119
     no
##
     yes 0.188 0.344
##
## Performance statistics:
                                             FPR
                                                        TNR
 MCR
                      Recall
                              Precision
        Accuracy
                                                    0.7457265
 0.307
           0.693
                  0.6466165
                             0.7429806
                                         0.2542735
```

5 Assignment 5: Explanation

Explain why you obtain the same or different results in the exercises (2-4).

Overall, we can see that the differences are very small for asg. 2-3. It seems like the nodes that are not in the markov blanket don't provide incremental value in the classification. This is because all variables outside the markov blanket are conditionally independent of S when conditioned on MB(S), the markov blanket of S (https://en.wikipedia.org/wiki/Markov blanket).

The result with naive bayes asg. 4 sticks out. This is because it assumes independence between all the features which is a strong assumption that does not seem to be fulfilled. This is reflected in the fact that the structures learned in asg. 2-3 look very different. Therefore, the results are slightly worse for naive bayes.

```
[1] "asg2 exact"
##
        Predicted
## True
          no yes
##
         322 146
     no
##
     yes 120 412
   [1] "asg2_approx"
##
        Predicted
## True
          no yes
         322 146
##
##
     yes 122 410
## [1] "asg2 true"
```

```
##
        Predicted
## True
          no yes
     no 322 146
##
##
     yes 120 412
## [1] "asg3_markov"
##
        Predicted
## True
          no yes
##
     no 322 146
##
     yes 120 412
## [1] "asg4_naivebayes"
##
        Predicted
## True
          no yes
##
         349 119
     no
     yes 188 344
##
```

	MCR	Accuracy	Recall	Precision	FPR	TNR
asg2_exact	0.266	0.734	0.7744	0.7384	0.3120	0.6880
asg2_approx	0.268	0.732	0.7707	0.7374	0.3120	0.6880
asg2_true	0.266	0.734	0.7744	0.7384	0.3120	0.6880
asg3_markov	0.266	0.734	0.7744	0.7384	0.3120	0.6880
asg4_naivebayes	0.307	0.693	0.6466	0.7430	0.2543	0.7457

6 Appendix

```
# Auxilary functions
analyze_cm = function(cm, true){
  stopifnot(true %in% colnames(cm))
  levels = c(true, colnames(cm)[-which(colnames(cm) == true)]) # ORDER: 1; 0
  cm = as.data.frame(cm); colnames(cm)[1:2] = c("True", "Pred")
  N = sum(cm\$Freq)
  Npos = sum(cm$Freq[which(cm$True == levels[1])])
  Nneg = sum(cm$Freq[which(cm$True == levels[2])])
  TP = sum(cm$Freq[which(cm$True == levels[1] & cm$Pred == levels[1])])
  TN = sum(cm$Freq[which(cm$True == levels[2] & cm$Pred == levels[2])])
  FP = sum(cm$Freq[which(cm$True == levels[2] & cm$Pred == levels[1])])
  FN = sum(cm$Freq[which(cm$True == levels[1] & cm$Pred == levels[2])])
  return(data.frame(MCR = (FP+FN)/N, Accuracy = (TP + TN)/N,
                    Recall = TP/Npos, # recall = TPR = sensitivity,
                    Precision = TP/(TP + FP),
                    FPR = FP/Nneg, TNR = TN/Nneg)) # TNR = specificity
}
# cm = table(Y true, Y pred, dnn = c("True", "Predicted"))
# knitr::kable(analyze_cm(cm, true = "yes"))
# Assignment 1
# Prepare data
data("asia")
df = data.frame(asia)
rm(asia)
head(df)
# Train models
res1 = hc(df, restart=10, score='bic')
res2 = hc(df, restart=10, score='bic')
# Overview and scores
all.equal(res1, res2)
cat("Score BN 1: ", bnlearn::score(res1, df)) # smaller BIC is better
cat("Score BN 2: ", bnlearn::score(res2, df))
```

```
# Visual Comparison of arcs
par(mfrow = c(1, 2))
graphviz.compare(res1, res2, main = c("Run 1 (with BIC)", "Run 2 (with BIC)"))
# Printed comparison of arcs
comp = compare(res1, res2)
cat("true positive (tp) arcs, which appear both in target and in current:", comp$tp)
cat("false positive (fp) arcs, which appear in current but not in target:", comp$fp)
cat("false negative (fn) arcs, which appear in target but not in current:", comp$fn)
# Hamming
cat('Same Skeleton:', all.equal(skeleton(res1), skeleton(res2)))
cat("Hamming distance (zero if same skeleton):", hamming(res1, res2))
cat("Struct. hamming distance:", shd(res1, res2))
# Other -----
# # Create individual plots for each dag
# plot(res1)
# plot(res2)
# # Print the arcs (from, to) for each dag
# arcs(res1)
# arcs(res12
# vstructs(res1)
# vstructs(res2)
# cpdaq(res1)
# cpdag(res2)
res3 = hc(df, restart=10, score='aic')
cat("Score BN 3: ", bnlearn::score(res3, df)) # smaller AIC is better
par(mfrow = c(1, 2))
graphviz.compare(res2, res3, main = c("Run 2 (with BIC)", "Run 3 (with AIC)"))
rand = random.graph(colnames(df))
res4 = hc(asia, start = rand)
```

```
# Assignment 2
# Prepare data
data("asia")
df = asia
#df = data.frame(apply(asia, 2, as.character), stringsAsFactors = F)
rm(asia)
# Split data randomly
set.seed(12345)
N = nrow(df)
idx = sample(1:N, round(N * 0.8))
df tr = df[idx, ]
df te = df[-idx,]
# Fit the structure (given data set)
dag = hc(df_tr, restart=100, score='bic')
\# dag = iamb(df_tr)
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(dag, df_tr, method='mle')
# Show model
plot(dag)
# Show conditional probabilities for S
dag fitted$S
bn.fit.dotplot(dag_fitted$S) # bn.fit.barchart(dag_fitted$S)
predict exact = function(dag fitted, df te, y name, markov = FALSE){
  # -----
  # Input:
  # - dag_fitted: dag with learned structure and parameters
  # - df_te: data frame with all features and the Y (all factors)
  # - y_name: string with the name of the Y variable
  # Output:
  # - list with factor vectors: Y_true and Y_pred
```

```
junction = compile(as.grain(dag_fitted))
  N = nrow(df te)
  Y_true = df_te[[y_name]]
  Y pred = numeric(length = N)
  Y space = as.character(unique(Y true))
  for (i in 1:N){
    # With all RVs
    x = df_te[i, colnames(df_te) != y_name]
    if (markov == FALSE){
      var names = names(x)
     var_values = vapply(x, as.character, character(1))
      var_names = mb(dag_fitted, y_name)
      var_values = vapply(x, as.character, character(1))[var_names]
    evidence = setEvidence(junction, nodes = var_names, states = var_values)
    Y prob = querygrain(evidence, nodes = y name)[[1]]
   Y_pred[i] = Y_space[which.max(Y_prob)]
  }
  return(list(Y_pred = Y_pred, Y_true = Y_true))
}
# Make predictions
res = predict_exact(dag_fitted, df_te, "S")
Y_true = res$Y_true
Y pred = res$Y pred
# Evaluate predictions
cat("Confusion matrix (absolute):\n")
cm = table(Y true, Y pred, dnn = c("True", "Predicted"))
print(cm)
asg2 exact = cm
cat("\nConfusion matrix (relative):\n")
table(Y true, Y pred, dnn = c("True", "Predicted"))/N
```

```
cat("\nPerformance statistics:\n")
knitr::kable(analyze_cm(cm, true = "yes"))
# Alternative: The below code could be used if we only wanted to use node "B"
# for prediction
# # With only B as RV
# val = as.character(df_te[i, 'B'])
# evidence = setEvidence(junction, nodes = "B", states = val)
# Input:
# - dag_fitted: dag with learned structure and parameters
# - df_te: data frame with all features and the Y (all factors)
# MAKE SURE TO ADJUST THE EVIDENCE AND EVENT!
N = nrow(df te)
Y true = df te[['S']]
Y pred = numeric(length = N)
Y space = as.character(unique(Y true))
Y prob = numeric(length = length(Y space))
junction = compile(as.grain(dag_fitted))
for (i in 1:N){
  # With all RVs
  x = vapply(df_te[i, colnames(df_te) != 'S'], as.character, character(1))
  for (j in 1:length(Y space)){
   Y_prob[j] = cpquery(dag_fitted, event = (S == Y_space[j]),
                          evidence = ((A == x['A']) & (T == x['T'])
                                      & (L == x['L']) & (B == x['B'])
                                      & (E == x['E']) & (X == x['X'])
                                      & (D == x['E'])
                        )
  }
  Y_pred[i] = Y_space[which.max(Y_prob)]
```

```
# Evaluate predictions
cat("Confusion matrix (absolute):\n")
cm = table(Y true, Y pred, dnn = c("True", "Predicted"))
print(cm)
asg2\_approx = cm
cat("\nConfusion matrix (relative):\n")
table(Y_true, Y_pred, dnn = c("True", "Predicted"))/N
cat("\nPerformance statistics:\n")
knitr::kable(analyze_cm(cm, true = "yes"))
# Prepare the structure
# Option 1:
dag_true = model2network("[A][S][T|A][L|S][B|S][D|B:E][E|T:L][X|E]")
# #Option 2
# dag true = empty.graph(names(df))
\# modelstring(dag_true) = "[A][S][T/A][L/S][B/S][D/B:E][E/T:L][X/E]"
# Visual comparison only:
par(mfrow = c(1, 2))
graphviz.compare(dag, dag true, main = c("Learned", "True"))
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(dag_true, df_tr, method='mle')
# Make predictions
res = predict_exact(dag_fitted, df_te, "S")
Y true = res$Y true
Y pred = res$Y pred
# Evaluate predictions
cat("Confusion matrix (absolute):\n")
cm = table(Y_true, Y_pred, dnn = c("True", "Predicted"))
print(cm)
asg2 true = cm
cat("\nConfusion matrix (relative):\n")
table(Y true, Y pred, dnn = c("True", "Predicted"))/N
```

```
cat("\nPerformance statistics:\n")
knitr::kable(analyze_cm(cm, true = "yes"))
# Assignment 3
# Fit the structure (given data set)
dag = hc(df_tr, restart=10, score='bic')
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(dag, df_tr, method='mle')
# Make predictions
res = predict_exact(dag fitted, df te, "S", markov = TRUE)
Y_true = res$Y_true
Y_pred = res$Y_pred
# Evaluate predictions
cat("Confusion matrix (absolute):\n")
cm = table(Y_true, Y_pred, dnn = c("True", "Predicted"))
print(cm)
asg3 markov = cm
cat("\nConfusion matrix (relative):\n")
table(Y true, Y pred, dnn = c("True", "Predicted"))/N
cat("\nPerformance statistics:\n")
knitr::kable(analyze_cm(cm, true = "yes"))
# Assignment 4
# S pointing to all variables
IVs = paste0("[", colnames(df tr)[-which(colnames(df tr)=='S')], "|S]", collapse = "")
naive bayes = model2network(paste0("[S]", IVs))
plot(naive_bayes)
```

```
# # All variables pointing to S (wrong)
# cond = pasteO(colnames(df tr)[-which(colnames(df tr)=='S')], ":", collapse = "")
\# cond = substr(cond, 1, nchar(cond)-1)
# IVs = pasteO("[", colnames(df_tr)[-which(colnames(df_tr)=='S')], "]", collapse = "")
# naive_bayes = model2network(paste0("[S/", cond, "]", IVs))
# plot(naive bayes)
# Fit the parameters (given structure and data set)
dag_fitted = bn.fit(naive_bayes, df_tr, method = 'mle')
# Make predictions
res = predict_exact(dag_fitted, df_te, "S", markov = TRUE)
Y_true = res$Y_true
Y pred = res$Y pred
# Evaluate predictions
cat("Confusion matrix (absolute):\n")
cm = table(Y true, Y pred, dnn = c("True", "Predicted"))
print(cm)
asg4_naivebayes = cm
cat("\nConfusion matrix (relative):\n")
table(Y true, Y pred, dnn = c("True", "Predicted"))/N
cat("\nPerformance statistics:\n")
knitr::kable(analyze_cm(cm, true = "yes"))
# Assignment 5
print("asg2_exact")
asg2_exact
print("asg2 approx")
asg2_approx
print("asg2 true")
asg2_true
```