

Math 116: Worksheet 3

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1. (a)

| | y_1 | y_2 |
|----|-------|-------|
| 88 | 1 | 0 |
| 63 | 0 | 1 |
| 25 | 1 | -1 |
| 13 | -2 | 3 |
| 12 | 3 | -4 |
| 1 | -5 | 7 |

$$88(-5) + 63(7) = 1$$
 - (b) $x = 65 \cdot 63 \cdot 7 + 52 \cdot 88 \cdot (-5) + 88 \cdot 63k = 5785 \equiv 241 \pmod{88 \cdot 63}$.
 $x \equiv 241 \pmod{5544}$.
 - (c) $x = 23 \cdot 63 \cdot 7 + 42 \cdot 88 \cdot (-5) + 88 \cdot 63k = -8337 \equiv 2751 \pmod{5544}$.
 $x \equiv 2751 \pmod{5544}$.
2. $x \equiv 162869022118 \pmod{542909251286}$
3. $x \equiv 569 \pmod{133980}$. They must all be pairwise coprime.
4. (a) $\gcd(18, 60) = 6$. Because 18 and 60 are not co-prime, the CRT does not guarantee a solution.
- (b)