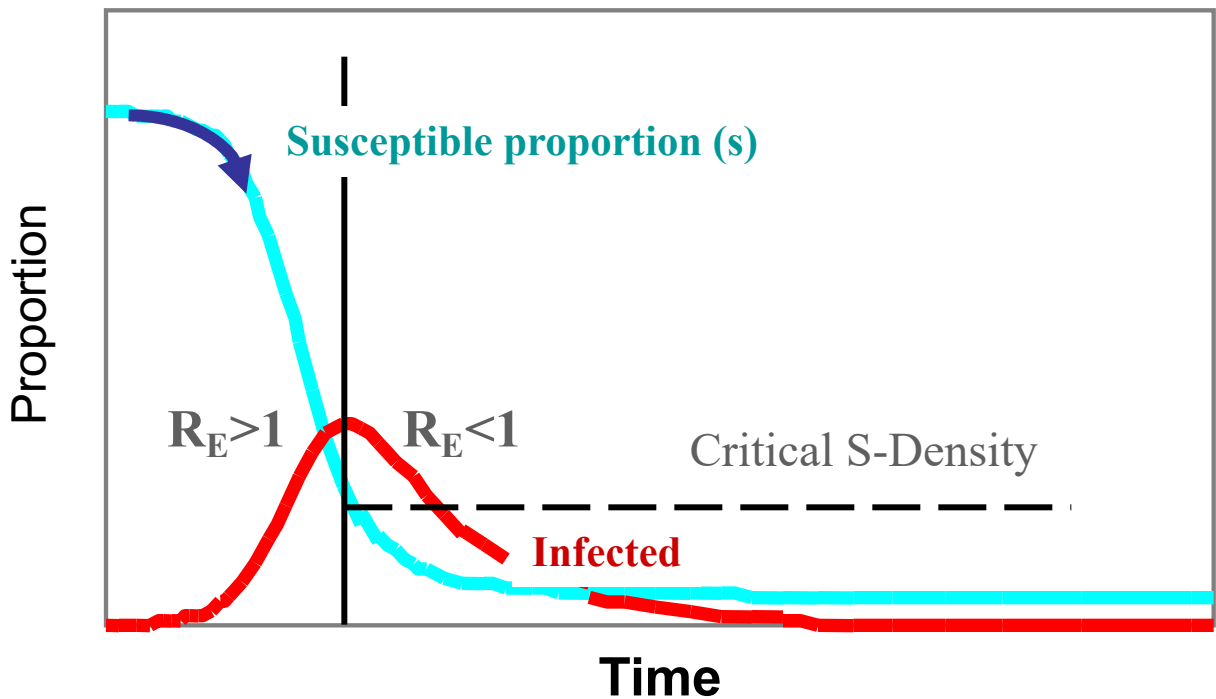


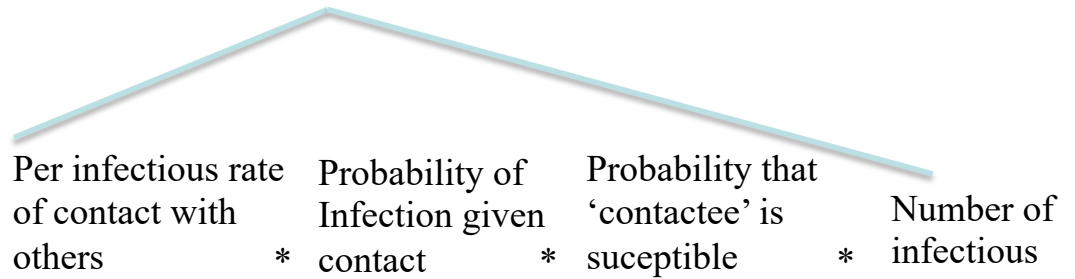
The anatomy of the simple epidemic



- Initial exponential growth with rate R_0
- Infection depletes the pool of susceptibles
- *effective reproductive ratio* R_E decreases
- R_E drops with susceptibles proportion: $R_E = R_0 s$.
(eg $R_0=18$, $s=0.5$ makes $R=9$ secondary cases)
- $R_E < 1$: Cases fall and epidemic dies out

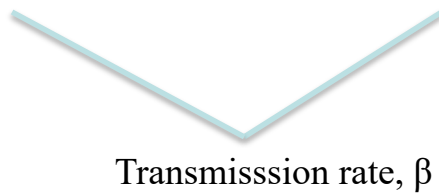
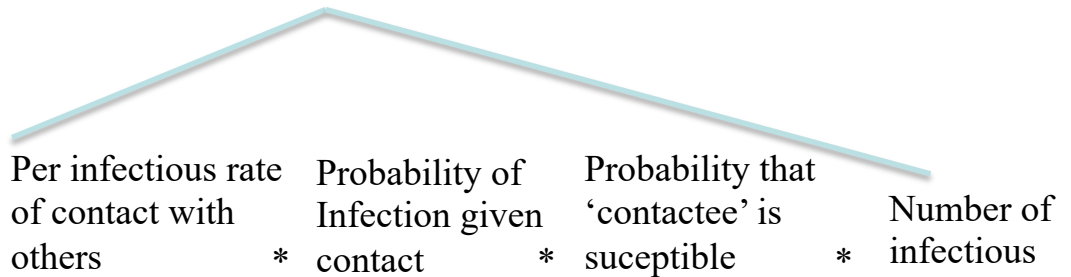
The S-I-R model

Change in S = + new births – new infections - deaths



The simple S-I-R model

Change in S = + new births – new infections - deaths



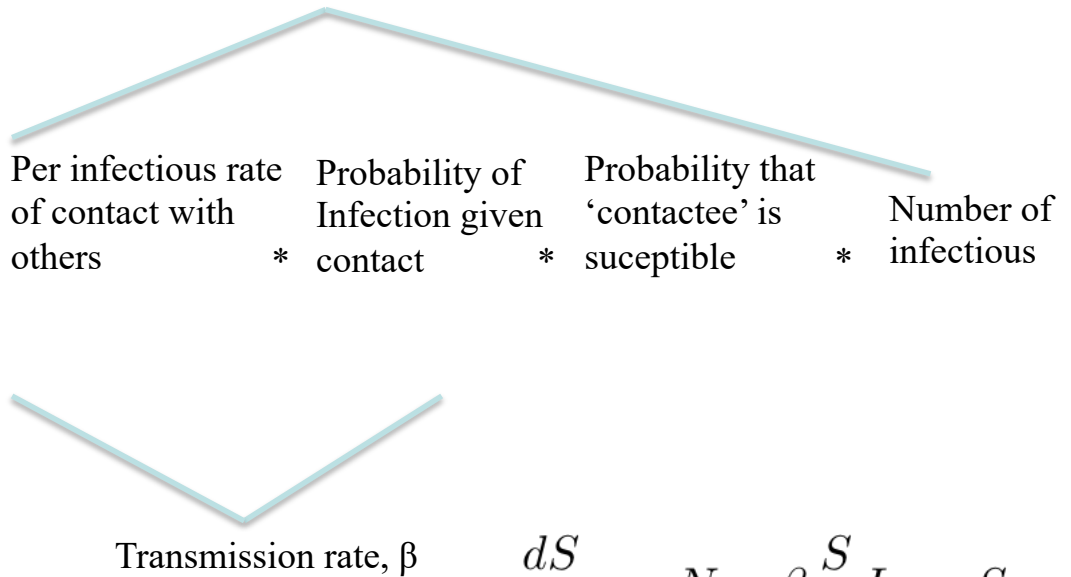
$$\frac{dS}{dt} = \nu N - \beta \frac{S}{N} I - \mu S$$

ν = natality rate

μ = mortality rate

The simple S-I-R model

Change in S = + new births – new infections - deaths



$$\frac{dS}{dt} = \nu N - \beta \frac{S}{N} I - \mu S$$

ν = natality rate

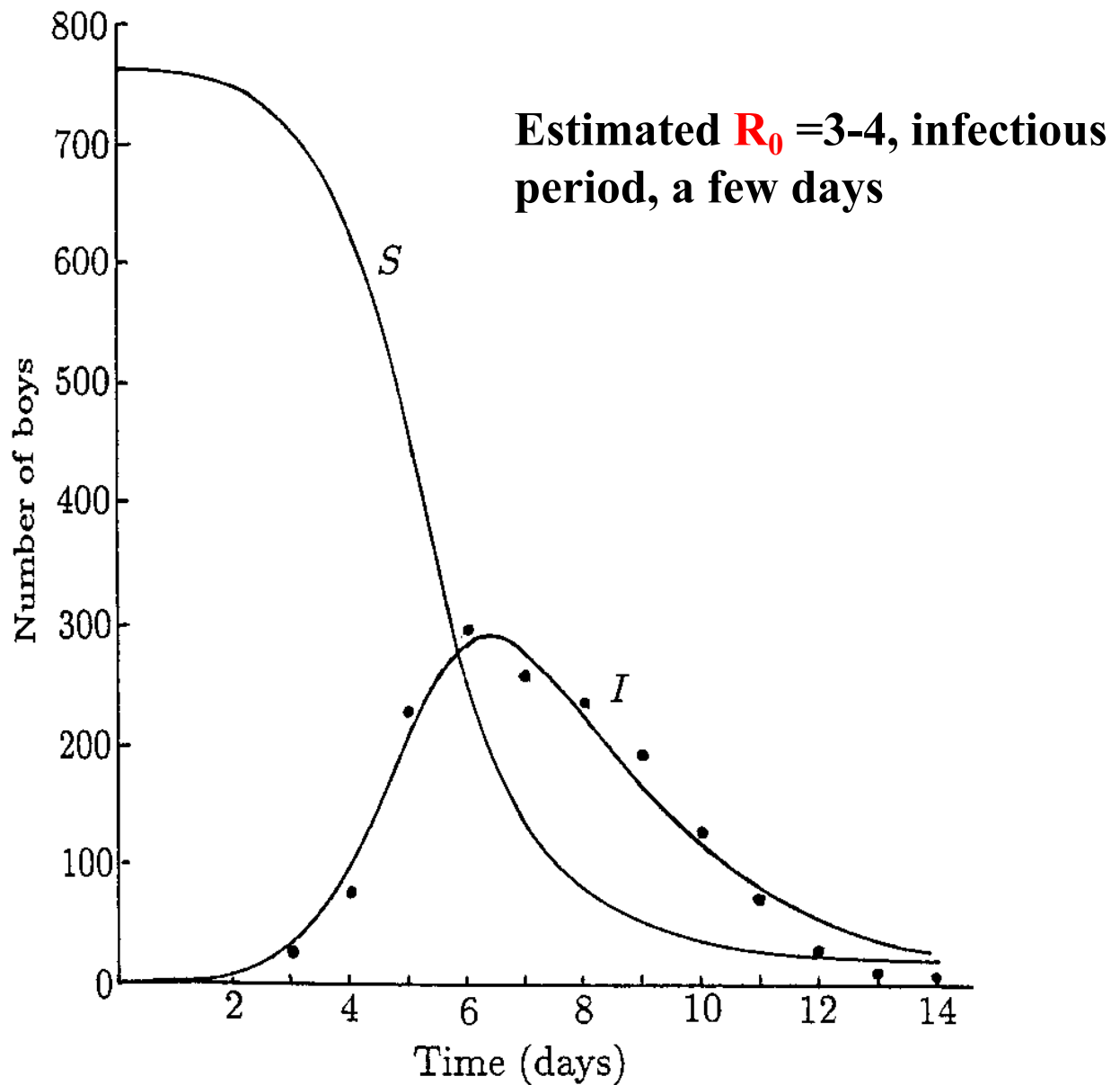
μ = mortality rate

Change in I = + new infections – new recovered - deaths

$$\frac{dI}{dt} = \beta \frac{S}{N} I - \gamma I - \mu I$$

$$\gamma = \frac{1}{\text{latent} + \text{infectious period}}$$

Ex. Outbreak of flu in a British boarding school



In-host immunology \rightarrow population flows

In-host dynamics \rightarrow population flows

