

Haigh Beck & graphical cost-effectiveness tool

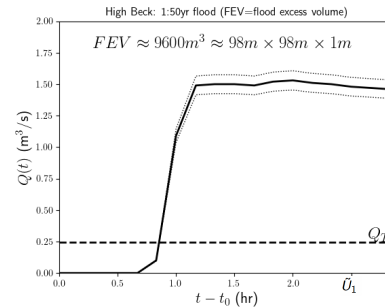
Goal & outcome: value unvalued (NBS)co-benefits! *Case study:* Urban **Haigh Beck** runs 2000m from spring to River Aire with 100m drop, flows into/under canal, culverted last 200m. **Surface flooding** occurs in neighborhoods near river & canal at ~1:15yrs AEP. New flood defense walls near river cover 1:200yrs AEP but trap beck: limited pump action $Q_T=0.245\text{m}^3/\text{s}$. Canal segment for large (extra) flood storage between two locks is $7.5\text{km} \times 10\text{m} \times 1.5\text{m}$ with several overflows. **CSO** pollutes beck.

Flooding, polluted, 06-05-2024 of 6 Bradford apartments (~1:15yrs AEP):



Haigh Beck-canal-Dyehouse Mill
<https://www.youtube.com/shorts/T9mH2MOKA3s>

canal-apartments of Mill
<https://www.youtube.com/shorts/JIE3CoXOVFe>



Flood—Excess Volume (FEV) is volume that causes damage [1];
~numerical modelling (LCC/BDMC) 1:50yrs Haigh Beck flood:
 $FEV = \int_{t_0}^{t_0+T} Q(t) - Q_T dt = 9600\text{m}^3 = 98 \times 98 \times 1\text{m}^3$ sense of size!

Measure	Base cost q_i (k£)	Probability p_i (/50yrs)	Damage q_{pi} (k£)	Total (k£)
C1	500(900)	1	70	570(970)
B2	385	0.25	200	435
FP3	400	0.05	200	410
B2+FP3	-	-	-	845

Base costs, probabilities & damage costs:

To obtain estimate for q_{p1} , start from £ 1.7M repair costs of a culvert breach, emptying 60km of the Leeds-Liverpool canal (2021-2022 CRT). Since the canal stretch involved in C1 is 7km, 1/8 of those costs are involved so ~£ 210k, of which £ 140k are standard costs occurring even in the absence of flood storage in the canal, so £ 70k extra investment. Base costs: C1 $q_1 =$ £ 500k, plus extra costs for (optional) 200m pipeline to separate CSO from beck £ 400k (clean-up). **Real figures impossible to obtain in real cases** (~10xFOIs!), $q_2+q_3=785\text{k}$ given; rest estimated, e.g., $q_{p2}=q_{p3}=$ £ 200k, see Table above.

Utility functions U_1 and U_2 :

$U_1 = \sum_{j=1}^2 w_j C_j$ without co-benefits, weights $w_j=0,1$. **B2+FP3** best.
 $U_2 = \sum_{j=1}^2 w_j C_j - \sum_{k=1}^N a_{jk} B_{jk}$ with co-benefits B_{jk} , $B_{2k}=0$, $N_2=5$.
Take $B_{11} = -q_{1CSO} =$ £ 400k (no pollution beck/canal).

But value benefits unknown: $B_{12} = q_{1cc}$ (extra climate-change canal storage); $B_{13} = q_{1D}$ (drought benefits beck flow into canal); $B_{14} = q_{1E}$ (ecological value beck water in canal); $B_{15} = q_{1clean}$ (clean beck & canal). Difference $D =$ £ 125k costs C1 (w. CSO) - (B2+FP3). When we are **willing to assign** combined benefits $\sum_{k=2}^5 B_{1k} > D$ over 50yrs, scenario **C1** becomes best: **break-even** 2.5k p/a.

Info-gap theory values NBS co-benefits!

Info-gap decision theory (Ben-Haim [5]) consists of three components:

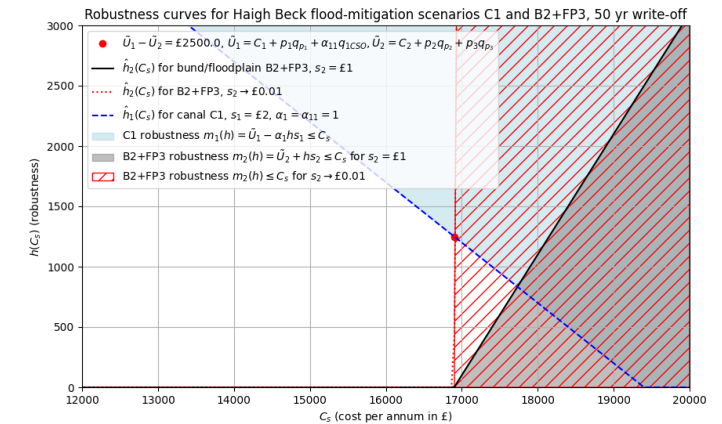
- (i) Costs $\tilde{U}_1 = C_1 + p_1 q_{p1} + \alpha_{11} q_{1CSO}$, $\tilde{U}_2 = C_2 + p_2 q_{p2} + p_3 q_{p3}$ benefits combined into B_1 , $\alpha_{11}=1$; $\alpha_1=1$, i.e., system's model for scenarios C1 and B2+FP3.
(ii) Performance requirements $m_i(h) < C_s$, costs & uncertainty models $l_1(h)$, $l_2(h)$ for C1, B2+FP3: $m_1(h) = \tilde{U}_1 - \alpha_1 h s_1 \leq C_s$, $\tilde{U}_1 = C_1 + p_1 q_{p1} + \alpha_{11} q_{1CSO}$

$$m_2(2) = \tilde{U}_2 + h s_2 \leq C_s, \quad \tilde{U}_2 = C_2 + p_2 q_{p2} + p_3 q_{p3}$$

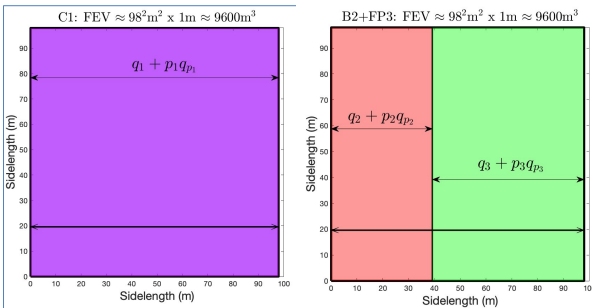
$$l_1(h) = \frac{|B_1|}{s_1} \leq h, \quad l_2(h) = \frac{|U_2 - \tilde{U}_2|}{s_2} \leq h$$

$$\text{Hence: } h = \frac{(\tilde{U}_1 - C_s)}{\alpha_1 s_1} \geq 0, \quad h = \frac{(C_s - \tilde{U}_2)}{s_2} \geq 0 \quad (\text{see graph below}).$$

- (iii) Performance aspiration or opportuneness [5,6] $\tilde{U}_2 - \beta s_2 \leq C_w$, $\tilde{U}_1 + \alpha_1 \beta s_1 \leq C_w$.



Discussion: C1 has factually **unvalued** co-benefits but base costs > B2+FP3 (starting point of lines at $h=0$). For well-known costs of B2+FP3 such that $s_2 \rightarrow 0$, red dot at cross-over sets value of 2500p/a, **quantifying co-benefits**. C1 can be more robust than B2+FP3. Decision-makers decide whether worth money for extra co-benefits. **Critique:** Info-gap vs. Bayesian analysis? **Outcome: unvalued NBS benefits can be valued robustly!**



Flood-mitigation scenarios shown in square-lake graphs [1,2,3,4]:

C1 canal: beck diverted into canal, automated gate to divide water into canal/culvert, coverage of $\alpha_1 \times FEV$ with $\alpha_1 > 1$, **costs** $q_1 + p_1 q_{p1}$, excess FEV coverage. Benefits **Nature-Based Solutions:** anti-drought, clean canal, extra storage for climate change; split CSO spills split from beck to limit/cut Combined Sewer Overflows; extra **costs** $-B_{11} = q_{1CSO}$.

B2+FP3 bund & flood-plain storage: $1.0 \times FEV$. **B2 upstream bund:** in flatter areas, partial prevention $\alpha_2 \times FEV$ with $\alpha_2 = 0.4$, **costs** $q_2 + p_2 q_{p2}$. **FP3 culvert** from canal to river opened at playing fields (protective flood plains), pumping needed, partial prevention $\alpha_3 \times FEV$ with $\alpha_3 = 0.6$, **costs** $q_3 + p_3 q_{p3}$.

References

- [1] Bokhove, Kent, Kelmanson, Piton, Tacnet 2020: *Water* 12. <https://doi.org/10.3390/w12030552>
- [2] Bokhove, Kelmanson, Kent, Hicks 2021: REF2021 Impact Case Study. <https://results2021.ref.ac.uk/impact/0ad7c1be-8e91-4aac-ab57-6c1e873c83f1?page=1>
- [3] Bokhove 2024: LMS recorded talk (ourtool catches errors!): <https://www.youtube.com/watch?v=2KVoV3y5lmE>
- [4] Knotters, Bokhove, Lamb, Poortvliet 2024: *Cambridge Prisms: Water* 2:e6. <https://doi.org/10.1017/wat.2024.4>
- [5] Ben-Haim 2019: Info-Gap Decision Theory (IG). In: Decision making under deep uncertainty. <https://doi.org/10.1017/wat.2024.4>
- [6] Bokhove 2025: Info-gap assessment. Slides: <https://bokhove.github.io/EGU2025BokhoveVienna2025.pdf>