

problem 3

$$4t^3 - 3t + \sin(t)$$

$$f(t) = 4t^3 - 3t + \sin(t)$$

$$f(t) = \sum_{n=0}^{\infty} c_n h_n(t)$$

$$c_n = \langle h_n, f(t) \rangle$$

$$\int_0^1 h_0(t) f(t) dt = \int_0^1 (4t^3 - 3t + \sin(t)) dt = -0.04030$$

$$\int_0^1 h_1(t) f(t) dt = \int_0^{\frac{1}{2}} (4t^3 - 3t + \sin(t)) dt + \int_{\frac{1}{2}}^1 (-4t^3 + 3t - \sin(t)) dt$$

$$= -0.19008 - 0.14978 = -0.33986$$

$$\int_0^1 h_2(t) f(t) dt = \int_0^{\frac{1}{4}} f(t) dt + \int_{\frac{1}{4}}^{\frac{1}{2}} -f(t) dt = -0.05876 + 0.13133$$

$$\int_0^1 h_3(t) f(t) dt = \int_{\frac{1}{2}}^{\frac{3}{4}} f(t) dt + \int_{\frac{3}{4}}^1 -f(t) dt = -0.06791 + (-0.21873)$$

$$\int_0^1 h_4(t) f(t) dt = \int_0^{\frac{1}{8}} f(t) dt + \int_{\frac{1}{8}}^{\frac{3}{8}} -f(t) dt = -0.015391 + 0.04327$$

$$h_5 \quad \int_{\frac{3}{8}}^{\frac{5}{8}} + \int_{\frac{5}{8}}^{\frac{7}{8}} = -0.06291 + 0.06841$$

$$h_6 \quad \int_{\frac{1}{6}}^{\frac{5}{6}} + \int_{\frac{5}{6}}^1 = -0.05423 + 0.01472$$

$$h_7 \quad \int_{\frac{7}{8}}^1 + \int_{\frac{1}{8}}^{\frac{3}{8}} = 0.0558 + (-0.10291)$$

$$c_n = \begin{matrix} -0.04030 & -0.33986 & 0.07257 & -0.28768 \\ 0.027979 & 0.0055 & -0.03951 & -0.10715 \end{matrix}$$

clear