

153. False; $e^x = 0$ has no solutions.

155. The error is that both sides of the equation should be divided by 2 before taking the natural log of both sides.

$$2e^x = 10$$

$$e^x = 5$$

$$\ln e^x = \ln 5$$

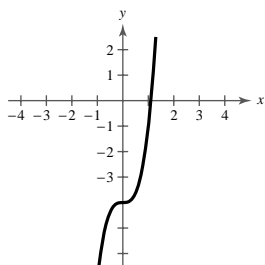
$$x = \ln 5$$

157. Inverse Property. You would take the natural log of both sides, which would give you $x \ln 5 = \ln 34$. So,

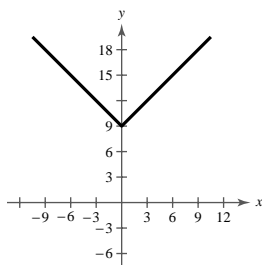
$$x = \frac{\ln 34}{\ln 5}.$$

159. Yes. The investment will double every $\frac{\ln 2}{r}$ years.

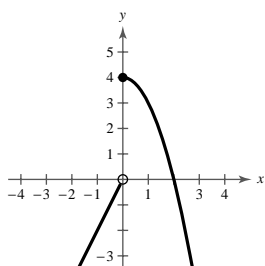
161.



163.



165.



Section 3.5 (page 228)

1. (a) iv (b) i (c) iii (d) vi (e) ii (f) v

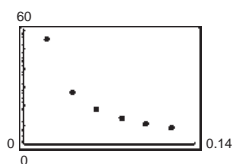
3. sigmoidal 5. Exponential decay

7. c 8. e 9. b 10. a 11. d 12. f

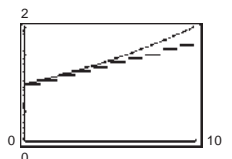
	Initial Investment	Annual % Rate	Time to Double	Amount After 10 Years
13.	\$10,000	3.5%	19.8 yr	\$14,190.68
15.	\$7500	3.30%	21 yr	\$10,432.26
17.	\$5000	1.25%	55.45 yr	\$5665.74
19.	\$63,762.82	4.5%	15.40 yr	\$100,000.00

21.

r	2%	4%	6%	8%	10%	12%
t	54.93	27.47	18.31	13.73	10.99	9.16

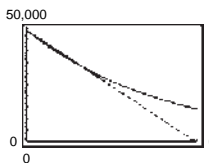


23.



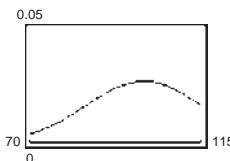
Continuous compounding

25. ^{226}Ra 1599 10 g 6.48 g
 27. ^{14}C 5700 3 g 2.66 g
 29. $y = e^{0.768x}$ 31. $y = 4e^{-0.2773x}$
 33. (a) Decreasing. The negative exponent indicates that the model is decreasing.
 (b) 333,680 people; 317,565 people; 308,272 people
 (c) 2014
 35. (a) 0.0189 (b) About 1,534,104 people
 37. About 15,601 yr ago
 39. (a) $V = -8305t + 49,200$ (b) $V = 49,200e^{-0.2059t}$
 (c)

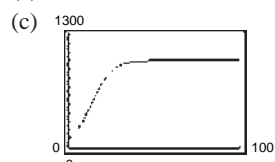


(d) Exponential model (e) $0 < t < 2$; $t \geq 2$

41. (a) 0.05 (b) 100

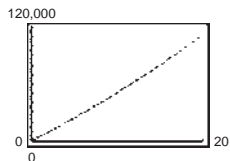


43. (a) About 203 animals (b) About 13 mo



The horizontal asymptotes occur at $p = 1000$ and $p = 0$. The asymptote at $p = 1000$ means there will not be more than 1000 animals in the preserve.

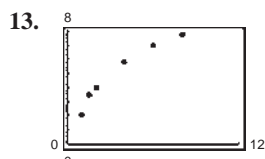
45. (a) 10,000,000 (b) 125,892,541 (c) 1,258,925
 47. (a) 20 dB (b) 70 dB (c) 120 dB
 49. 97.49% 51. 4.64 53. About 31,623 times
 55. (a) 120,000 (b) 21.20 yr; yes



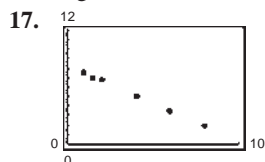
57. 3:00 A.M. 59. False. The domain can be all real numbers.
 61. No. Any x -value in the Gaussian model will give a positive y -value.
 63. Gaussian model 65. Exponential growth model
 67. a; $(0, -3)$, $(\frac{9}{4}, 0)$ 68. b; $(0, 2)$, $(5, 0)$
 69. d; $(0, 25)$, $(\frac{100}{9}, 0)$ 70. c; $(0, 4)$, $(2, 0)$
 71. Falls to the left and rises to the right
 73. Rises to the left, falls to the right
 75. $2x^2 + 3 + \frac{3}{x-4}$ 77. Answers will vary.

Section 3.6 (page 238)

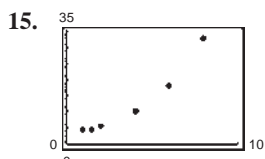
1. $y = ax^b$ 3. Scatter plot 5. Logarithmic model
 7. Quadratic model 9. Exponential model
 11. Quadratic model



Logarithmic model



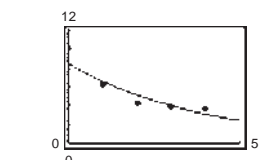
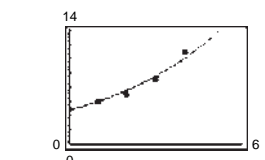
Linear model



Exponential model

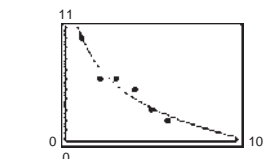
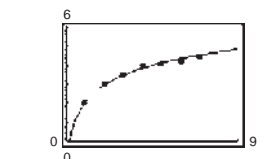
19. $y = 4.752(1.2607)^x$;
0.96773

21. $y = 8.463(0.7775)^x$;
0.86639



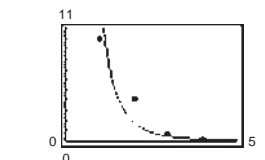
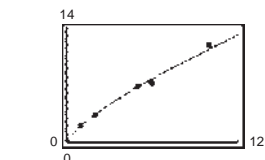
23. $y = 2.083 + 1.257 \ln x$;
0.98672

25. $y = 9.826 - 4.097 \ln x$;
0.93704



27. $y = 1.985x^{0.760}$;
0.99686

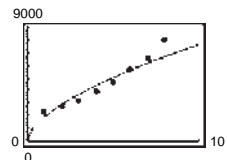
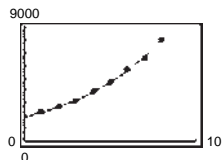
29. $y = 16.103x^{-3.174}$;
0.88161



31. (a) Exponential model: $S = 1876.645(1.1980)^t$
Power model: $S = 1905.844t^{0.6018}$

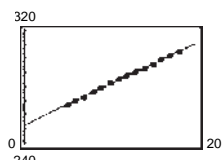
(b) Exponential model:

Power model:

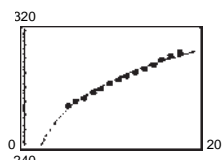


(c) Exponential model

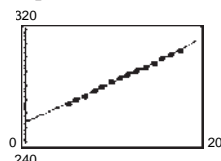
33. (a) Linear model: $P = 2.89t + 252.9$; $r^2 \approx 0.9987$



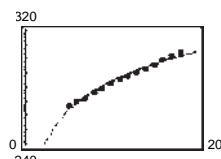
(b) Power model: $P = 222.94t^{0.1048}$; $r^2 \approx 0.9850$



(c) Exponential model: $P = 254.445(1.0102)^t$; $r^2 \approx 0.9972$



(d) Logarithmic model: $P = 29.813 \ln t + 215.36$;
 $r^2 \approx 0.9803$



(e) The linear model is the best fit because its coefficient of determination is closest to 1.

(f) Linear:

Year	2009	2010	2011	2012	2013	2014
Population (in millions)	307.8	310.7	313.6	316.5	319.4	322.3

Power:

Year	2009	2010	2011	2012	2013	2014
Population (in millions)	303.5	305.2	306.7	308.2	309.7	311.1

Exponential:

Year	2009	2010	2011	2012	2013	2014
Population (in millions)	308.6	311.7	314.9	318.1	321.3	324.6

Logarithmic:

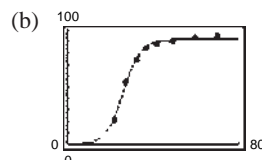
Year	2009	2010	2011	2012	2013	2014
Population (in millions)	303.1	304.7	306.1	307.5	308.8	310.1

(g) and (h) Answers will vary.

35. (a) $y = 1315.584(1.0644)^t$ (b) $y = 1315.584e^{0.0624t}$

(c) About 2307 stores; Answers will vary.

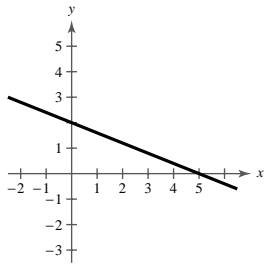
37. (a) $y = \frac{91.3686}{1 + 765.5440e^{-0.2547x}}$



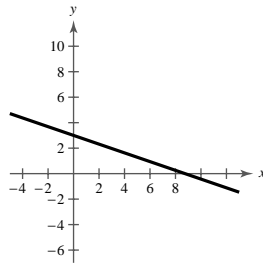
The model fits the data well.

39. True. See page 221. 41. Answers will vary.

43. Slope: $-\frac{2}{5}$
y-intercept: (0, 2)



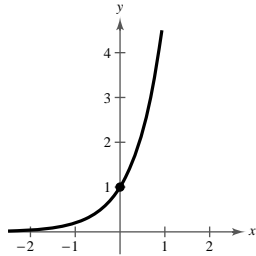
45. Slope: $-\frac{12}{35}$
y-intercept: (0, 3)



47. $y = -(x + 1)^2 + 2$ 49. $y = -2(x - 3)^2 + 2$

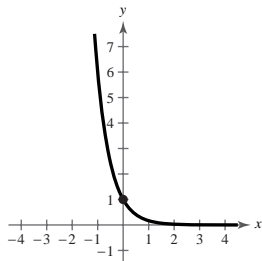
Review Exercises (page 244)

1. 10.3254 3. 0.0001 5. c 6. d 7. b 8. a
9.



Horizontal asymptote: $y = 0$
y-intercept: (0, 1)
Increasing on $(-\infty, \infty)$

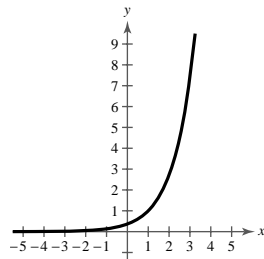
- 11.



Horizontal asymptote: $y = 0$
y-intercept: (0, 1)
Decreasing on $(-\infty, \infty)$

- 13.

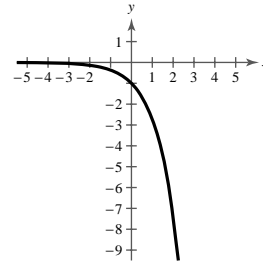
x	0	1	2	3	4
$h(x)$	0.37	1	2.72	7.39	20.09



Horizontal asymptote: $y = 0$

15.

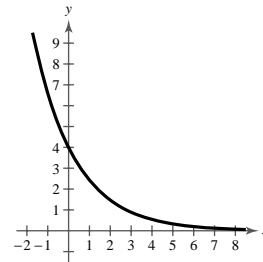
x	-2	-1	0	1	2
$h(x)$	-0.14	-0.37	-1	-2.72	-7.39



Horizontal asymptote: $y = 0$

- 17.

x	-1	0	1	2	3	4
$f(x)$	6.59	4	2.43	1.47	0.89	0.54



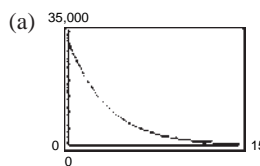
Horizontal asymptote: $y = 0$

- 19.

t	1	10	20
A	\$10,832.87	\$22,255.41	\$49,530.32

t	30	40	50
A	\$110,231.76	\$245,325.30	\$545,981.50

21. (a)

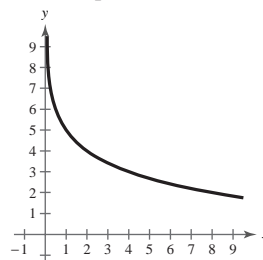


(b) \$18,000

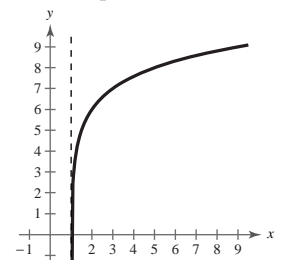
(c) When it is first sold; Yes;
Answers will vary.

23. $5^3 = 125$ 25. $64^{1/6} = 2$ 27. $\log_4 64 = 3$
29. $\log_{125} 25 = \frac{2}{3}$ 31. $\log_{1/2} 8 = -3$ 33. 3 35. -1
37. Domain: $(0, \infty)$ 39. Domain: $(1, \infty)$

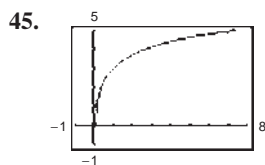
Vertical asymptote: $x = 0$
x-intercept: (32, 0)



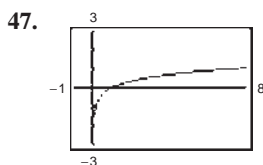
Vertical asymptote: $x = 1$
x-intercept: (1.016, 0)



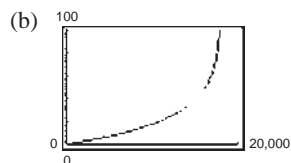
41. 3.068 43. 0.896



Domain: $(0, \infty)$
 Vertical asymptote: $x = 0$
 x -intercept: $(0.05, 0)$



Domain: $(0, \infty)$
 Vertical asymptote: $x = 0$
 x -intercept: $(1, 0)$

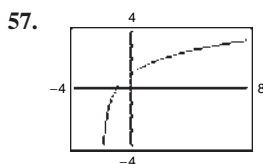
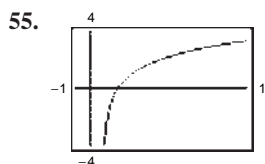
49. (a) $0 \leq h < 18,000$


Asymptote: $h = 18,000$

(c) The time required to increase its altitude further increases.

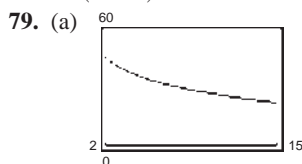
(d) 5.46 min

51. 1.585 53. 2.235


59. 1.13 61. 0.41 63. $\ln 5 - 2$ 65. $2 + \log_{10} 2$

67. $1 + 2 \log_5 x$ 69. $\log_{10} 5 + \frac{1}{2} \log_{10} y - 2 \log_{10} x$

71. $\ln(x+3) - \ln x - \ln y$ 73. $\log_2 9x$

75. $\ln \frac{\sqrt{2x-1}}{(x+1)^2}$ 77. $\ln \frac{3\sqrt[3]{4-x^2}}{x}$


(b)

h	4	6	8	10	12	14
s	38	33	30	27	25	23

(c) The decrease in productivity starts to level off.

81. 4 83. -3 85. -5 87. 4096 89. 9

91. e^4 93. $e^2 + 1$ 95. -0.757 97. 4.459

99. 1.760 101. 3.916 103. 1.609, 0.693

105. 200.615 107. 36.945 109. 53.598

111. No solution 113. 0.9 115. -1 117. 0.368

119. 10.05 yr 121. e 122. b 123. f

124. d 125. a 126. c

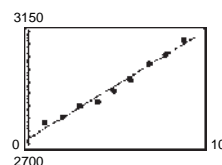
127. $k = 0.0177$; 11,407,330

129. (a) 9.52 weeks (b) 21.20 weeks

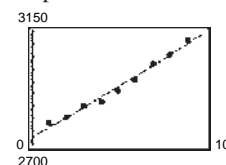
131. Logistic model

133. (a) Linear model: $N = 41.5t + 2722.1$; $r^2 \approx 0.9785$
 Exponential model: $N = 2728(1.0142)^t$; $r^2 \approx 0.9818$
 Power model: $N = 2727.6t^{0.0497}$; $r^2 \approx 0.8398$

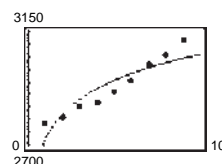
(b) Linear model:



Exponential model:



Power model:



(c) The exponential model is the best fit because its coefficient of determination is closest to 1.

(d) 3,141,090 (e) 2021–2022

135. True. $e^{x-1} = e^x \cdot e^{-1} = \frac{e^x}{e}$

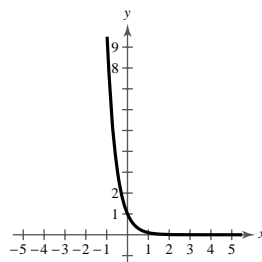
137. False. $x > 0$

139. Because $1 < \sqrt{2} < 2$, then $2^1 < 2^{\sqrt{2}} < 2^2$.

Chapter Test (page 248)

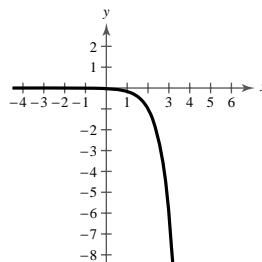
1.

x	-2	-1	0	1	2
$f(x)$	100	10	1	0.1	0.01


Horizontal asymptote: $y = 0$
 y -intercept: $(0, 1)$

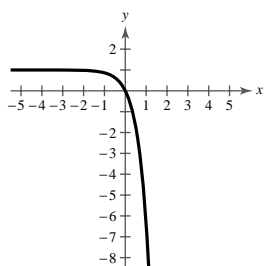
2.

x	0	2	3	4
$f(x)$	-0.03	-1	-6	-36


Horizontal asymptote: $y = 0$
 y -intercept: $(0, -\frac{1}{36})$

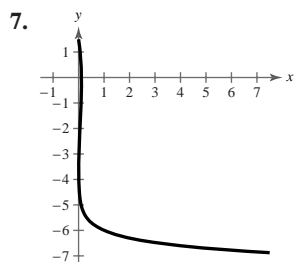
3.

x	-2	-1	0	1	2
$f(x)$	0.9817	0.8647	0	-6.3891	-53.5982

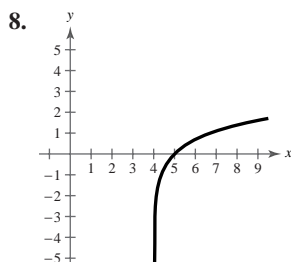


Horizontal asymptote: $y = 1$
Intercept: $(0, 0)$

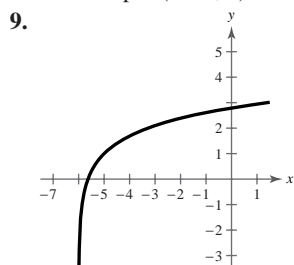
4. -0.89 5. 9.2 6. 2



Domain: $(0, \infty)$
Vertical asymptote: $x = 0$
 x -intercept: $(10^{-6}, 0)$



Domain: $(4, \infty)$
Vertical asymptote: $x = 4$
 x -intercept: $(5, 0)$



Domain: $(-6, \infty)$
Vertical asymptote: $x = -6$
 x -intercept: $(-5.63, 0)$

10. 1.945 11. 0.115 12. 1.674

13. $\log_2 3 + 4 \log_2 a$ 14. $\ln 5 + \frac{1}{2} \ln x - \ln 6$

15. $\ln x + \frac{1}{2} \ln(x+1) - \ln 2 - 4$ 16. $\log_3 13y$

17. $\ln\left(\frac{x^4}{y^4}\right)$ 18. $\ln\left[\frac{x(2x-3)}{x+2}\right]$ 19. 4

20. 2.431 21. 343 22. 100,004 23. 1.321

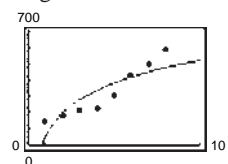
24. 1 25. 1.597 26. 1.649 27. 54.96%

28. (a) Logarithmic model: $R = 200.7 \ln t + 57.835$

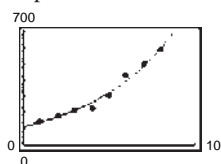
Exponential model: $R = 115.47(1.227)^t$

Power model: $R = 119.22t^{0.6703}$

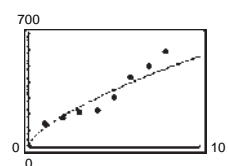
(b) Logarithmic model:



Exponential model:



Power model:



(c) Exponential model; \$2483.9 million

Cumulative Test for Chapters 1–3 (page 249)

1. (a) $y = -x + 3$

(b) Answers will vary.

Sample answer: $(0, 3), (1, 2), (2, 1)$

2. (a) $y = -2x$

(b) Answers will vary.

Sample answer: $(0, 0), (1, -2), (2, -4)$

3. (a) $x = -\frac{3}{7}$

(b) Answers will vary.

Sample answer: $(-\frac{3}{7}, 0), (-\frac{3}{7}, 1), (-\frac{3}{7}, -3)$

4. (a) $\frac{5}{3}$ (b) Undefined (c) $\frac{5+4s}{3+4s}$

5. (a) -32 (b) 4 (c) 20

6. No. It doesn't pass the Vertical Line Test.

7. Decreasing on $(-\infty, 5)$
Increasing on $(5, \infty)$

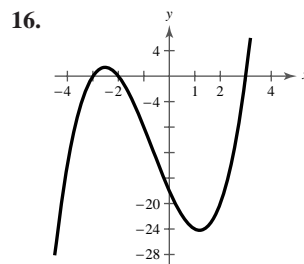
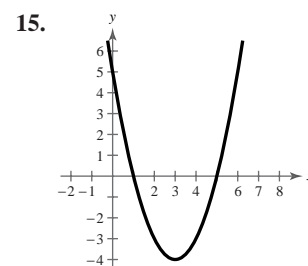
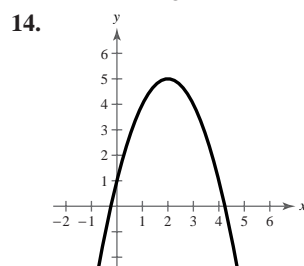
8. (a) Vertical shrink

(b) Vertical shift

(c) Horizontal shift and reflection in the x -axis

9. -53 10. $\frac{197}{16}$ 11. -79 12. 42

13. $h^{-1}(x) = \frac{x+2}{5}$

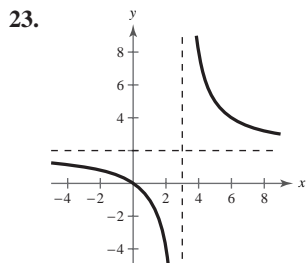


17. $x = -2, \pm 2i$ 18. 1.424 19. $4x + 2 - \frac{15}{x+3}$

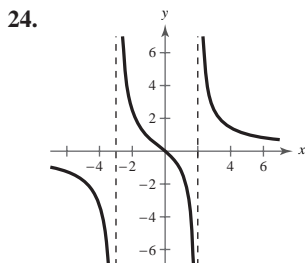
20. $2x^2 + 7x + 48 + \frac{268}{x-6}$ 21. 41

22. Answers will vary.

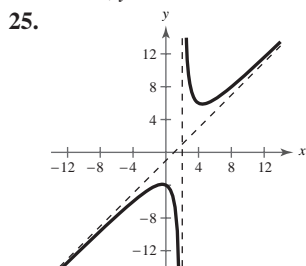
Sample answer: $f(x) = x^4 + x^3 + 18x$



Asymptotes:
 $x = 3, y = 2$

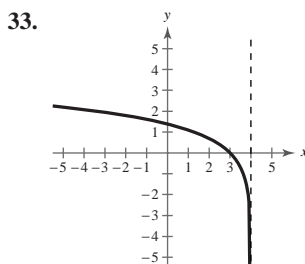
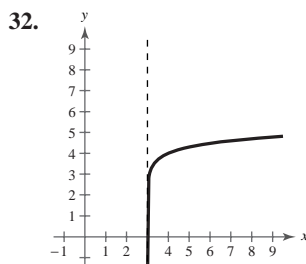
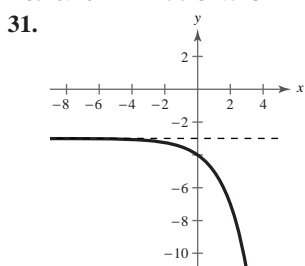
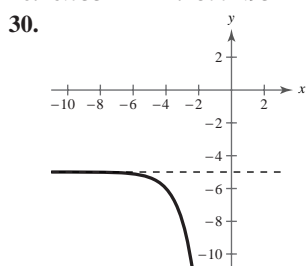


Asymptotes:
 $x = -3, x = 2, y = 0$



Asymptotes: $x = 2, y = x - 1$

26. 6.733 27. 8772.934 28. 0.202 29. 51.743



34. 1.723 35. 0.872 36. 0.585

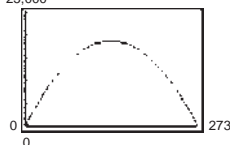
37. $\ln(x+2) + \ln(x-2) - \ln(x^2+1)$

38. $\ln \frac{x^2(x+1)}{x-1}$ 39. 1.242 40. 6.585 41. 12.8

42. 152.018 43. 0, 1 44. No solution

45. (a) $A = x(273 - x)$

(b) $0 < x < 273$



(c) 76.23 ft \times 196.77 ft

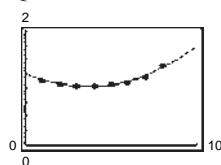
46. (a) Quadratic model:

$$y = 0.0178t^2 - 0.130t + 1.26; r^2 \approx 0.9778$$

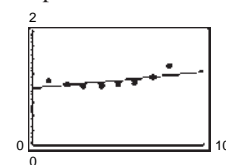
Exponential model: $y = 1.002(1.025)^t; r^2 \approx 0.4009$

Power model: $y = 1.041t^{0.0564}; r^2 \approx 0.1686$

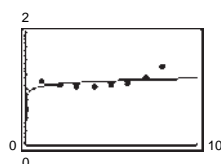
(b) Quadratic model:



Exponential model:



Power model:



(c) The quadratic model is the best fit because its coefficient of determination is closest to 1.

(d) \$1.74; Answers will vary.

Chapter 4

Section 4.1 (page 261)

1. Trigonometry 3. standard position

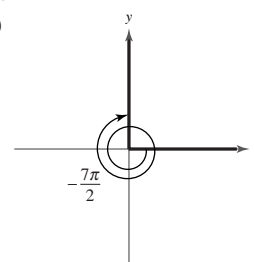
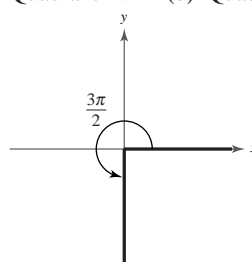
5. radian 7. 180° 9. No 11. 2

13. (a) Quadrant I (b) Quadrant III

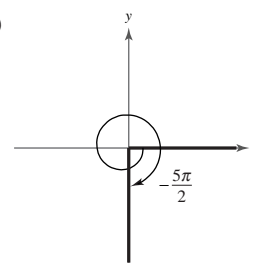
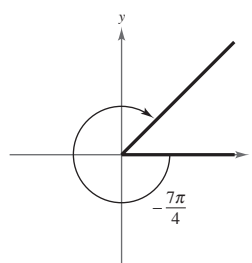
15. (a) Quadrant IV (b) Quadrant II

17. (a) Quadrant IV (b) Quadrant III

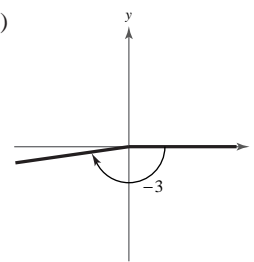
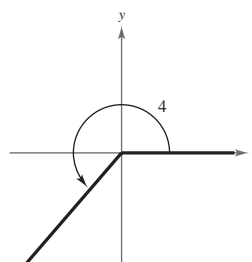
19. (a) (b)



21. (a) (b)



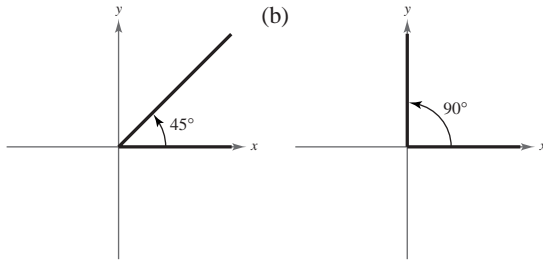
23. (a) (b)



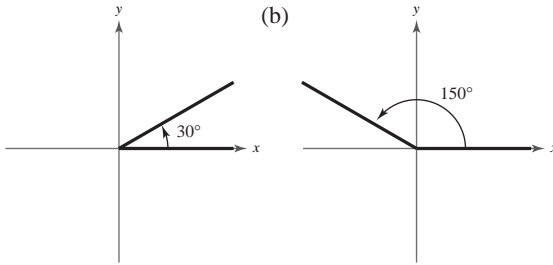
25. (a) $\frac{13\pi}{6}, -\frac{11\pi}{6}$ (b) $\frac{8\pi}{3}, -\frac{4\pi}{3}$

27. (a) $\frac{7\pi}{4}, -\frac{\pi}{4}$ (b) $\frac{28\pi}{15}, -\frac{32\pi}{15}$ 29. 210°

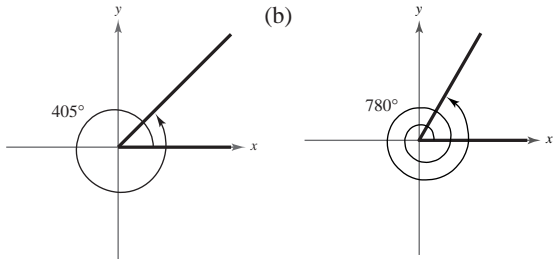
31. (a) Quadrant I (b) Quadrant III
 33. (a) Quadrant II (b) Quadrant IV
 35. (a) Quadrant III (b) Quadrant I
 37. (a)



39. (a)



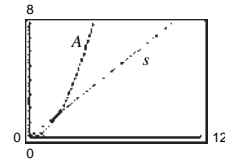
41. (a)



43. (a) 412° , -308° (b) 324° , -396°
 45. (a) 660° , -60° (b) 590° , -130°
 47. (a) $\frac{\pi}{6}$ (b) $\frac{5\pi}{6}$ 49. (a) $-\frac{\pi}{9}$ (b) $-\frac{4\pi}{3}$
 51. (a) 270° (b) -210° 53. (a) 420° (b) -39°
 55. 2.007 57. -3.776 59. -0.014 61. 25.714°
 63. 1170° 65. -114.592° 67. 64.75° 69. 85.308°
 71. -125.01° 73. $280^\circ 36'$ 75. $-345^\circ 7' 12''$
 77. $-20^\circ 20' 24''$ 79. Complement: 66° ; supplement: 156°
 81. Complement: 3° ; supplement: 93°
 83. Complement: $\frac{\pi}{6}$; supplement: $\frac{2\pi}{3}$
 85. Complement: $\frac{\pi}{3}$; supplement: $\frac{5\pi}{6}$ 87. $\frac{6}{5}$ rad
 89. $\frac{8}{15}$ rad 91. $\frac{70}{29}$ rad 93. 14π in. 95. 18π m
 97. 22.92 ft 99. 34.80 mi 101. 591.32 mi
 103. $4^\circ 2' 33''$ 105. 275.02° 107. 436.97 km/min
 109. (a) 80 π rad/sec (b) 25 π ft/sec
 111. (a) 400π rad/min to 1000π rad/min (b) 6000π cm/min
 113. False. A radian is larger: $1 \text{ rad} \approx 57.3^\circ$.
 115. True. The sum of the angles of a triangle must equal
 $180^\circ = \pi$ radians, and $\frac{2\pi}{3} + \frac{\pi}{4} + \frac{\pi}{12} = \pi$.

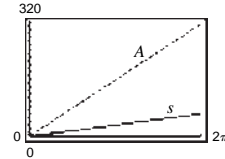
117. $\frac{50\pi}{3} \text{ m}^2$

119. (a) $A = 0.4r^2$, $r > 0$; $s = 0.8r$, $r > 0$



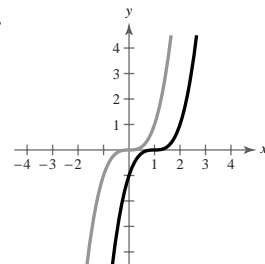
The area function changes more rapidly for $r > 1$ because it is quadratic and the arc length function is linear.

- (b) $A = 50\theta$, $0 < \theta < 2\pi$; $s = 10\theta$, $0 < \theta < 2\pi$



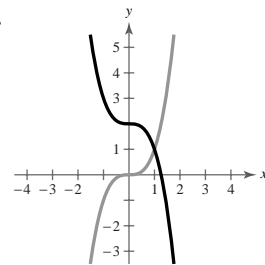
121. Answers will vary.

- 123.



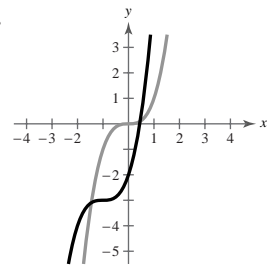
Horizontal shift one unit to the right

- 125.



Reflection in the x -axis, vertical shift two units upward

- 127.



Horizontal shift one unit to the left, vertical shift three units downward

Section 4.2 (page 270)

1. unit circle 3. odd, even

5. Even: cos, sec; Odd: sin, csc, tan, cot 7. 8

9. $\sin \theta = \frac{15}{17}$

$\cos \theta = -\frac{8}{17}$

$\tan \theta = -\frac{15}{8}$

$\csc \theta = \frac{17}{15}$

$\sec \theta = -\frac{17}{8}$

$\cot \theta = -\frac{8}{15}$

11. $\sin \theta = -\frac{5}{13}$

$\cos \theta = \frac{12}{13}$

$\tan \theta = -\frac{5}{12}$

$\csc \theta = -\frac{13}{5}$

$\sec \theta = \frac{13}{12}$

$\cot \theta = -\frac{12}{5}$

13. $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$ 15. $\left(-\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$ 17. $\left(-\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$

19. $(0, -1)$ 21. $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$

23. $\sin \frac{\pi}{4} = \frac{\sqrt{2}}{2}$

$\cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$

$\tan \frac{\pi}{4} = 1$

25. $\sin\left(-\frac{7\pi}{4}\right) = \frac{\sqrt{2}}{2}$

$\cos\left(-\frac{7\pi}{4}\right) = \frac{\sqrt{2}}{2}$

$\tan\left(-\frac{7\pi}{4}\right) = 1$

27. $\sin \frac{2\pi}{3} = \frac{\sqrt{3}}{2}$

$\cos \frac{2\pi}{3} = -\frac{1}{2}$

$\tan \frac{2\pi}{3} = -\sqrt{3}$

31. $\sin\left(-\frac{\pi}{6}\right) = -\frac{1}{2}$

$\cos\left(-\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$

$\tan\left(-\frac{\pi}{6}\right) = -\frac{\sqrt{3}}{3}$

33. $\sin \frac{3\pi}{4} = \frac{\sqrt{2}}{2}$

$\cos \frac{3\pi}{4} = -\frac{\sqrt{2}}{2}$

$\tan \frac{3\pi}{4} = -1$

$\csc \frac{3\pi}{4} = \sqrt{2}$

$\sec \frac{3\pi}{4} = -\sqrt{2}$

$\cot \frac{3\pi}{4} = -1$

37. $\sin\left(-\frac{4\pi}{3}\right) = \frac{\sqrt{3}}{2}$

$\cos\left(-\frac{4\pi}{3}\right) = -\frac{1}{2}$

$\tan\left(-\frac{4\pi}{3}\right) = -\sqrt{3}$

39. 0

41. $-\frac{1}{2}$

43. $\frac{\sqrt{3}}{2}$

45. $-\frac{\sqrt{2}}{2}$

47. (a) $-\frac{1}{3}$ (b) -3

49. (a) $-\frac{1}{5}$ (b) -5

51. (a) $\frac{4}{5}$ (b) $-\frac{4}{5}$

53. 0.4339

55. 0.8090

57. 1.0378

59. -0.1288

61. 1.3940

63. -1.4486

65. -1.3386

67. -1.0025

69. -2.4950

71. (a) -0.9 (b) -0.4

73. (a) 0.25, 2.89 (b) 1.82, 4.46

75. 0.79 amp

77. (a) 0.25 ft

(b) 0.02 ft

(c) -0.25 ft

79. False. $\sin(-t) = -\sin t$ means that the function is odd, not that the sine of a negative angle is a negative number.

81. True. $a - 6\pi$ is coterminal with a .

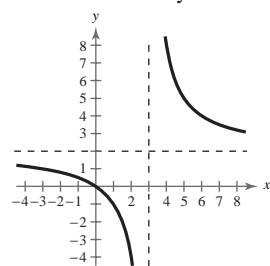
83. True. The values are the same.

85. (a) Origin (b) $\sin(t_1 + \pi) = -\sin t_1$

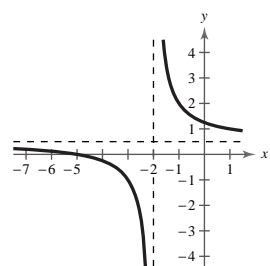
(c) $\cos(t_1 + \pi) = -\cos t_1$

87. Answers will vary. 89. It is an even function.

91.



93.



3. elevation, depression

5. 12

7. $\sin \theta = \frac{9}{41}$

$\cos \theta = \frac{40}{41}$

$\tan \theta = \frac{9}{40}$

$\csc \theta = \frac{41}{9}$

$\sec \theta = \frac{41}{40}$

$\cot \theta = \frac{40}{9}$

11. $\sin \theta = \frac{3}{5}$

$\cos \theta = \frac{4}{5}$

$\tan \theta = \frac{3}{4}$

$\csc \theta = \frac{5}{3}$

$\sec \theta = \frac{5}{4}$

$\cot \theta = \frac{4}{3}$

9. $\sin \theta = \frac{8}{17}$

$\cos \theta = \frac{15}{17}$

$\tan \theta = \frac{8}{15}$

$\csc \theta = \frac{17}{8}$

$\sec \theta = \frac{17}{15}$

$\cot \theta = \frac{15}{8}$

The triangles are similar and corresponding sides are proportional.

13. $\cos \theta = \frac{\sqrt{11}}{6}$

$\tan \theta = \frac{5\sqrt{11}}{11}$

$\csc \theta = \frac{6}{5}$

$\sec \theta = \frac{6\sqrt{11}}{11}$

$\cot \theta = \frac{\sqrt{11}}{5}$

15. $\sin \theta = \frac{\sqrt{15}}{4}$

$\cos \theta = \frac{1}{4}$

$\tan \theta = \sqrt{15}$

$\csc \theta = \frac{4\sqrt{15}}{15}$

$\cot \theta = \frac{\sqrt{15}}{15}$

17. $\sin \theta = \frac{3\sqrt{10}}{10}$

$\cos \theta = \frac{\sqrt{10}}{10}$

$\csc \theta = \frac{\sqrt{10}}{3}$

$\sec \theta = \sqrt{10}$

$\cot \theta = \frac{1}{3}$

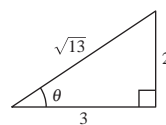
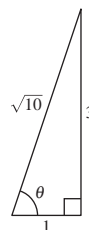
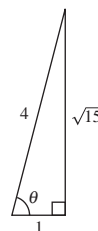
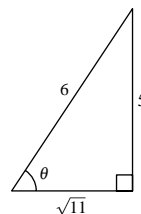
19. $\sin \theta = \frac{2\sqrt{13}}{13}$

$\cos \theta = \frac{3\sqrt{13}}{13}$

$\tan \theta = \frac{2}{3}$

$\sec \theta = \frac{\sqrt{13}}{3}$

$\csc \theta = \frac{\sqrt{13}}{2}$



21. $\frac{\pi}{6}, \frac{1}{2}$

23. $60^\circ, \sqrt{3}$

25. $60^\circ, \frac{\pi}{3}$

27. $30^\circ, \frac{\sqrt{3}}{2}$

29. $45^\circ, \frac{\pi}{4}$

31. (a) 0.1736 (b) 0.1736

33. (a) 1.3499 (b) 1.3432

35. (a) 5.0273

(b) 0.4142

37. $\csc \theta$

39. $\cot \theta$

41. $\cos \theta$

43. $\frac{\sin \theta}{\cos \theta}$

45. 1

Section 4.3 (page 280)

1. (a) iii (b) vi (c) ii (d) v (e) i (f) iv

47. $\cos \theta$ 49. $\cot \theta$ 51. $\csc \theta$

53. (a) $\sqrt{3}$ (b) $\frac{1}{2}$ (c) $\frac{\sqrt{3}}{2}$ (d) $\frac{\sqrt{3}}{3}$

55. (a) $\frac{1}{3}$ (b) $\frac{2\sqrt{2}}{3}$ (c) $\frac{\sqrt{2}}{4}$ (d) 3

57. (a) 3 (b) $\frac{2\sqrt{2}}{3}$ (c) $\frac{\sqrt{2}}{4}$ (d) $\frac{1}{3}$

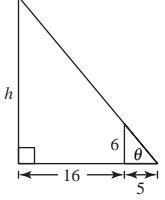
59–65. Answers will vary.

67. (a) $30^\circ = \frac{\pi}{6}$ (b) $30^\circ = \frac{\pi}{6}$

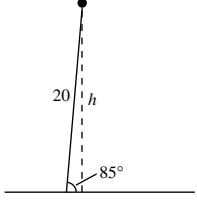
69. (a) $60^\circ = \frac{\pi}{3}$ (b) $45^\circ = \frac{\pi}{4}$

71. (a) $60^\circ = \frac{\pi}{3}$ (b) $45^\circ = \frac{\pi}{4}$

73. $y = 35\sqrt{3}$, $r = 70\sqrt{3}$ 75. $x = 8$, $y = 8\sqrt{3}$

77. (a) 
 (b) $\tan \theta = \frac{h}{21}$
 (c) $h = 25.2$ ft
 79. (a) 45°
 (b) $50\sqrt{2}$ ft
 (c) $\frac{25\sqrt{2}}{3}$ ft/sec; $\frac{25}{3}$ ft/sec

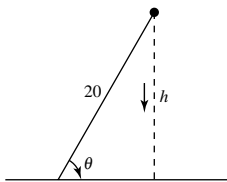
81. 160 ft

83. (a) 
 (b) $\sin 85^\circ = \frac{h}{20}$
 (c) 19.9 m
 (d) The side of the triangle labeled h will become shorter.

(e)

Angle, θ	80°	70°	60°	50°
Height	19.7	18.8	17.3	15.3

Angle, θ	40°	30°	20°	10°
Height	12.9	10.0	6.8	3.5

 (f) As $\theta \rightarrow 0^\circ$, $h \rightarrow 0$.


85. False. $\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \neq 1$

87. Yes, with the Pythagorean Theorem. Answers will vary.

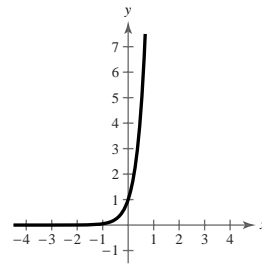
 89. (a)

θ	0°	20°	40°	60°	80°
$\sin \theta$	0	0.3420	0.6428	0.8660	0.9848
$\cos \theta$	1	0.9397	0.7660	0.5	0.1736
$\tan \theta$	0	0.3640	0.8391	1.7321	5.6713

 (b) Sine: increasing; cosine: decreasing; tangent: increasing
 (c) Answers will vary.

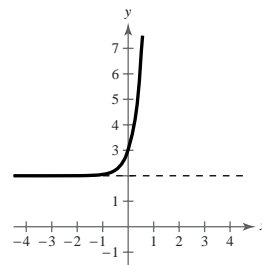
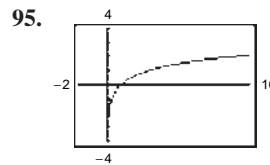
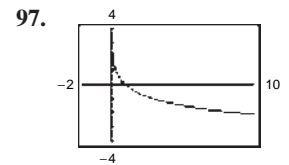
 91.

x	-1	0	1	2
$f(x)$	0.05	1	20.09	403.43


 Asymptote: $y = 0$

 93.

x	-1	0	1	2
$f(x)$	2.05	3	22.09	405.43


 Asymptote: $y = 2$

 Domain: $(0, \infty)$
 Vertical asymptote: $x = 0$
 x-intercept: $(1, 0)$

 Domain: $(0, \infty)$
 Vertical asymptote: $x = 0$
 x-intercept: $(1, 0)$

Section 4.4 (page 289)

1. $\frac{y}{r}$ 3. $\frac{y}{x}$ 5. $\cos \theta$ 7. reference angle 9. $0, \pi$

11. (a) $\sin \theta = \frac{3}{5}$ (b) $\sin \theta = -\frac{15}{17}$
 $\cos \theta = \frac{4}{5}$ $\cos \theta = -\frac{8}{17}$
 $\tan \theta = \frac{3}{4}$ $\tan \theta = \frac{15}{8}$
 $\csc \theta = \frac{5}{3}$ $\csc \theta = -\frac{17}{15}$
 $\sec \theta = \frac{5}{4}$ $\sec \theta = -\frac{17}{8}$
 $\cot \theta = \frac{4}{3}$ $\cot \theta = \frac{8}{15}$

13. (a) $\sin \theta = -\frac{1}{2}$ (b) $\sin \theta = \frac{\sqrt{2}}{2}$
 $\cos \theta = -\frac{\sqrt{3}}{2}$ $\cos \theta = -\frac{\sqrt{2}}{2}$
 $\tan \theta = \frac{\sqrt{3}}{3}$ $\tan \theta = -1$
 $\csc \theta = -2$ $\csc \theta = \sqrt{2}$
 $\sec \theta = -\frac{2\sqrt{3}}{3}$ $\sec \theta = -\sqrt{2}$
 $\cot \theta = \sqrt{3}$ $\cot \theta = -1$

$$\begin{aligned} 15. \sin \theta &= \frac{24}{25} \\ \cos \theta &= \frac{7}{25} \\ \tan \theta &= \frac{24}{7} \\ \csc \theta &= \frac{25}{24} \\ \sec \theta &= \frac{25}{7} \\ \cot \theta &= \frac{7}{24} \end{aligned}$$

$$\begin{aligned} 19. \sin \theta &= \frac{5\sqrt{29}}{29} \\ \cos \theta &= -\frac{2\sqrt{29}}{29} \\ \tan \theta &= -\frac{5}{2} \\ \csc \theta &= \frac{\sqrt{29}}{5} \\ \sec \theta &= -\frac{\sqrt{29}}{2} \\ \cot \theta &= -\frac{2}{5} \end{aligned}$$

23. Quadrant III

$$\begin{aligned} 27. \sin \theta &= \frac{3}{5} \\ \cos \theta &= -\frac{4}{5} \\ \tan \theta &= -\frac{3}{4} \\ \csc \theta &= \frac{5}{3} \\ \sec \theta &= -\frac{5}{4} \\ \cot \theta &= -\frac{4}{3} \end{aligned}$$

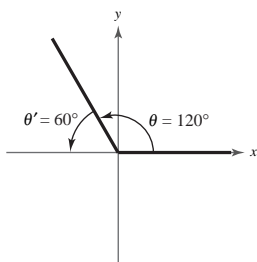
$$\begin{aligned} 31. \sin \theta &= \frac{\sqrt{3}}{2} \\ \cos \theta &= -\frac{1}{2} \\ \tan \theta &= -\sqrt{3} \end{aligned}$$

$$\begin{aligned} 33. \sin \theta &= 0 \\ \cos \theta &= -1 \\ \tan \theta &= 0 \\ \csc \theta &\text{ is undefined.} \\ \sec \theta &= -1 \\ \cot \theta &\text{ is undefined.} \end{aligned}$$

$$\begin{aligned} 37. \sin \theta &= -\frac{2\sqrt{5}}{5} \\ \cos \theta &= -\frac{\sqrt{5}}{5} \\ \tan \theta &= 2 \end{aligned}$$

$$\begin{aligned} 39. -1 \quad 41. 0 \quad 43. 1 \end{aligned}$$

$$47. \theta' = 60^\circ$$



$$\begin{aligned} 17. \sin \theta &= -\frac{12}{13} \\ \cos \theta &= \frac{5}{13} \\ \tan \theta &= -\frac{12}{5} \\ \csc \theta &= -\frac{13}{12} \\ \sec \theta &= \frac{13}{5} \\ \cot \theta &= -\frac{5}{12} \end{aligned}$$

$$\begin{aligned} 21. \sin \theta &= \frac{4\sqrt{41}}{41} \\ \cos \theta &= -\frac{5\sqrt{41}}{41} \\ \tan \theta &= -\frac{4}{5} \\ \csc \theta &= \frac{\sqrt{41}}{4} \\ \sec \theta &= -\frac{\sqrt{41}}{5} \\ \cot \theta &= -\frac{5}{4} \end{aligned}$$

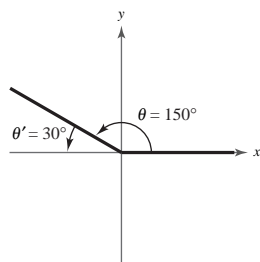
25. Quadrant I

$$\begin{aligned} 29. \sin \theta &= -\frac{15}{17} \\ \cos \theta &= \frac{8}{17} \\ \tan \theta &= -\frac{15}{8} \\ \csc \theta &= -\frac{17}{15} \\ \sec \theta &= \frac{17}{8} \\ \cot \theta &= -\frac{8}{15} \end{aligned}$$

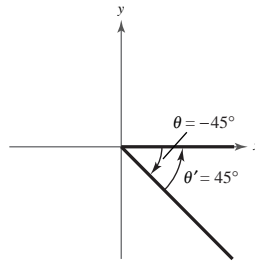
$$\begin{aligned} \csc \theta &= \frac{2\sqrt{3}}{3} \\ \sec \theta &= -2 \\ \cot \theta &= -\frac{\sqrt{3}}{3} \end{aligned}$$

$$\begin{aligned} 35. \sin \theta &= \frac{\sqrt{2}}{2} \\ \cos \theta &= -\frac{\sqrt{2}}{2} \\ \tan \theta &= -1 \\ \csc \theta &= \sqrt{2} \\ \sec \theta &= -\sqrt{2} \\ \cot \theta &= -1 \end{aligned}$$

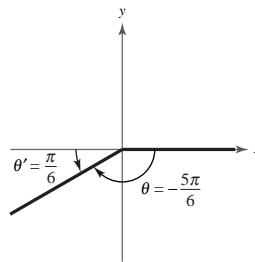
$$\begin{aligned} 45. \text{Undefined} \\ 49. \theta' = 30^\circ \end{aligned}$$



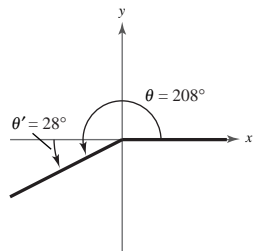
$$51. \theta' = 45^\circ$$



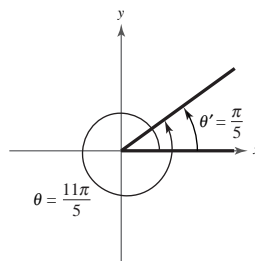
$$55. \theta' = \frac{\pi}{6}$$



$$59. \theta' = 28^\circ$$



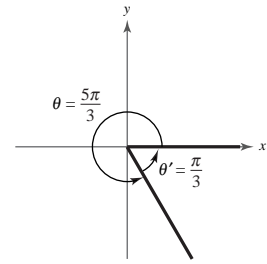
$$63. \theta' = \frac{\pi}{5}$$



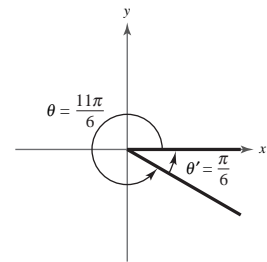
$$\begin{aligned} 67. \sin 225^\circ &= -\frac{\sqrt{2}}{2} \\ \cos 225^\circ &= -\frac{\sqrt{2}}{2} \\ \tan 225^\circ &= 1 \end{aligned}$$

$$\begin{aligned} 71. \sin \frac{5\pi}{3} &= -\frac{\sqrt{3}}{2} \\ \cos \frac{5\pi}{3} &= \frac{1}{2} \\ \tan \frac{5\pi}{3} &= -\sqrt{3} \end{aligned}$$

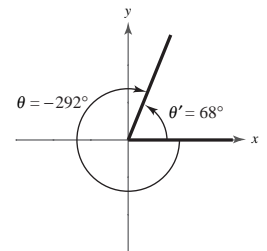
$$53. \theta' = \frac{\pi}{3}$$



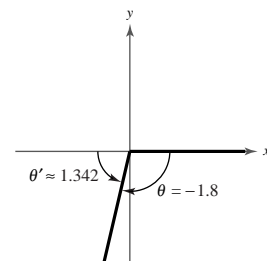
$$57. \theta' = \frac{\pi}{6}$$



$$61. \theta' = 68^\circ$$



$$65. \theta' \approx 1.342$$



$$\begin{aligned} 69. \sin(-750^\circ) &= -\frac{1}{2} \\ \cos(-750^\circ) &= \frac{\sqrt{3}}{2} \\ \tan(-750^\circ) &= -\frac{\sqrt{3}}{3} \end{aligned}$$

$$\begin{aligned} 73. \sin\left(-\frac{\pi}{6}\right) &= -\frac{1}{2} \\ \cos\left(-\frac{\pi}{6}\right) &= \frac{\sqrt{3}}{2} \\ \tan\left(-\frac{\pi}{6}\right) &= -\frac{\sqrt{3}}{3} \end{aligned}$$

$$75. \sin \frac{11\pi}{4} = \frac{\sqrt{2}}{2} \quad 77. \sin\left(-\frac{17\pi}{6}\right) = -\frac{1}{2}$$

$$\cos \frac{11\pi}{4} = -\frac{\sqrt{2}}{2} \quad \cos\left(-\frac{17\pi}{6}\right) = -\frac{\sqrt{3}}{2}$$

$$\tan \frac{11\pi}{4} = -1 \quad \tan\left(-\frac{17\pi}{6}\right) = \frac{\sqrt{3}}{3}$$

$$79. \frac{4}{5} \quad 81. -\sqrt{3} \quad 83. \frac{\sqrt{65}}{4}$$

$$85. \cos \theta = -\frac{\sqrt{21}}{5} \quad 87. \sin \theta = \frac{4\sqrt{17}}{17}$$

$$\tan \theta = -\frac{2\sqrt{21}}{21} \quad \cos \theta = -\frac{\sqrt{17}}{17}$$

$$\csc \theta = \frac{5}{2} \quad \csc \theta = \frac{\sqrt{17}}{4}$$

$$\sec \theta = -\frac{5\sqrt{21}}{21} \quad \sec \theta = -\sqrt{17}$$

$$\cot \theta = -\frac{\sqrt{21}}{2} \quad \cot \theta = -\frac{1}{4}$$

$$89. \sin \theta = -\frac{2}{3} \quad \sec \theta = \frac{3\sqrt{5}}{5}$$

$$\cos \theta = \frac{\sqrt{5}}{3} \quad \cot \theta = -\frac{\sqrt{5}}{2}$$

$$\tan \theta = -\frac{2\sqrt{5}}{5}$$

$$91. 0.1736 \quad 93. 2.1445 \quad 95. -0.3420$$

$$97. 5.7588 \quad 99. 0.8391 \quad 101. -2.9238$$

$$103. (a) 30^\circ = \frac{\pi}{6}, 150^\circ = \frac{5\pi}{6} \quad (b) 210^\circ = \frac{7\pi}{6}, 330^\circ = \frac{11\pi}{6}$$

$$105. (a) 60^\circ = \frac{\pi}{3}, 120^\circ = \frac{2\pi}{3} \quad (b) 135^\circ = \frac{3\pi}{4}, 315^\circ = \frac{7\pi}{4}$$

$$107. (a) 150^\circ = \frac{5\pi}{6}, 210^\circ = \frac{7\pi}{6} \quad (b) 120^\circ = \frac{2\pi}{3}, 240^\circ = \frac{4\pi}{3}$$

$$109. (a) \frac{1+\sqrt{3}}{2} \quad (b) \frac{\sqrt{3}-1}{2} \quad (c) \frac{3}{4}$$

$$(d) \frac{\sqrt{3}}{4} \quad (e) \frac{\sqrt{3}}{2} \quad (f) \frac{\sqrt{3}}{2}$$

$$111. (a) 0 \quad (b) \sqrt{2} \quad (c) \frac{1}{2} \quad (d) -\frac{1}{2} \quad (e) -1 \quad (f) \frac{\sqrt{2}}{2}$$

$$113. (a) \frac{1-\sqrt{3}}{2} \quad (b) -\frac{1+\sqrt{3}}{2} \quad (c) \frac{3}{4}$$

$$(d) -\frac{\sqrt{3}}{4} \quad (e) -\frac{\sqrt{3}}{2} \quad (f) -\frac{\sqrt{3}}{2}$$

$$115. (a) -\frac{1+\sqrt{3}}{2} \quad (b) \frac{1-\sqrt{3}}{2} \quad (c) \frac{3}{4}$$

$$(d) \frac{\sqrt{3}}{4} \quad (e) \frac{\sqrt{3}}{2} \quad (f) -\frac{\sqrt{3}}{2}$$

$$117. (a) -\frac{1+\sqrt{3}}{2} \quad (b) -\frac{1+\sqrt{3}}{2} \quad (c) \frac{1}{4}$$

$$(d) \frac{\sqrt{3}}{4} \quad (e) \frac{\sqrt{3}}{2} \quad (f) -\frac{1}{2}$$

$$119. (a) -1 \quad (b) 1 \quad (c) 0 \quad (d) 0 \quad (e) 0 \quad (f) 0$$

$$121. (a) -1 \quad (b) 1 \quad (c) 0 \quad (d) 0 \quad (e) 0 \quad (f) 0$$

$$123. (a) 60.4^\circ\text{F} \quad (b) 92.3^\circ\text{F} \quad (c) 76.35^\circ\text{F}$$

$$125. (a) 12 \text{ mi} \quad (b) 6 \text{ mi} \quad (c) 6.93 \text{ mi}$$

$$127. \text{True. } 0 < \cos \theta < 1 \text{ in Quadrant I, so}$$

$$\sin \theta < \frac{\sin \theta}{\cos \theta} = \tan \theta.$$

129. False. Sine is positive in Quadrant II.

131. (a)

θ	0°	20°	40°
$\sin \theta$	0	0.3420	0.6428
$\sin(180^\circ - \theta)$	0	0.3420	0.6428

θ	60°	80°
$\sin \theta$	0.8660	0.9848
$\sin(180^\circ - \theta)$	0.8660	0.9848

(b) $\sin \theta = \sin(180^\circ - \theta)$

133. The calculator mode is in degrees instead of radians.

135. 7 137. 3.449, -1.449 139. 4.908, -5.908

Section 4.5 (page 299)

1. amplitude 3. $\frac{2\pi}{b}$ 5. 2π

7. It vertically shifts the graph d units.

9. (a) $x = -2\pi, -\pi, 0, \pi, 2\pi$ (b) $y = 0$

(c) Increasing: $\left(-2\pi, -\frac{3\pi}{2}\right), \left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$

Decreasing: $\left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(\frac{\pi}{2}, -\frac{3\pi}{2}\right)$

(d) Relative maxima: $\left(-\frac{3\pi}{2}, 1\right), \left(\frac{\pi}{2}, 1\right)$

Relative minima: $\left(-\frac{\pi}{2}, -1\right), \left(\frac{3\pi}{2}, -1\right)$

11. Period: π

Amplitude: 3

13. Period: 4π

Amplitude: $\frac{5}{2}$

15. Period: 2

Amplitude: $\frac{2}{3}$

17. Period: 2π

Amplitude: 2

19. Period: 3π

Amplitude: $\frac{1}{4}$

21. g is a shift of f π units to the right.

23. g is a reflection of f in the x -axis.

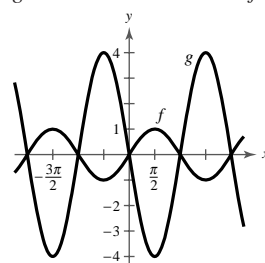
25. g is a reflection of f in the x -axis and has five times the amplitude of f .

27. g is a shift of f three units upward.

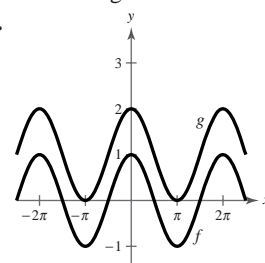
29. g has twice the amplitude of f .

31. g is a horizontal shift of f π units to the right.

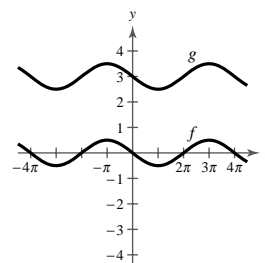
33.

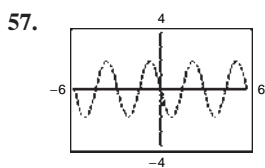
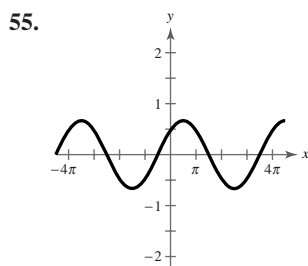
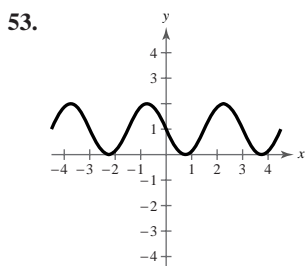
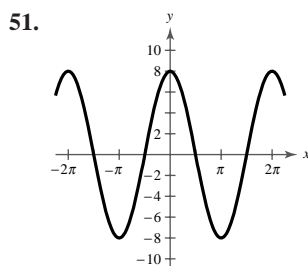
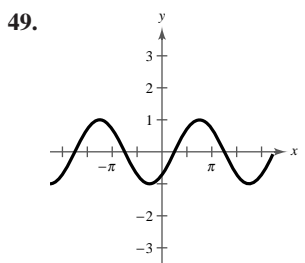
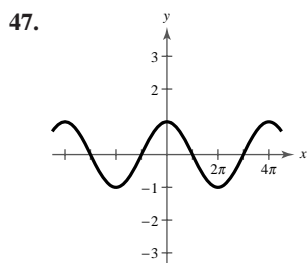
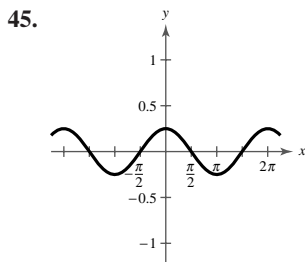
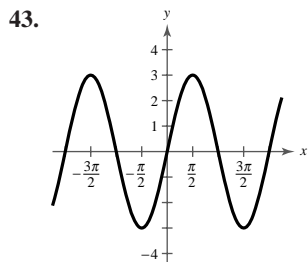
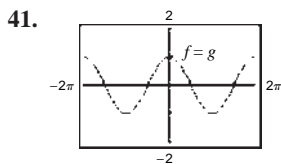
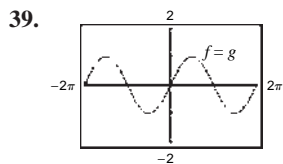


35.

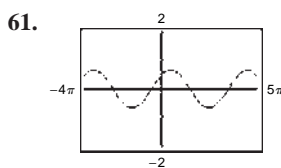
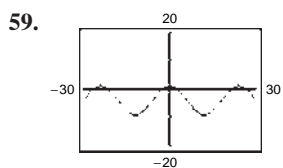


37.

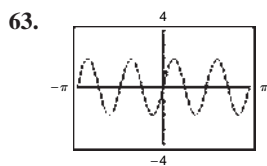




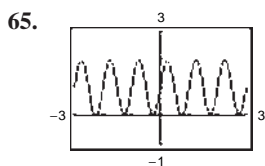
Amplitude: 2
Period: 3



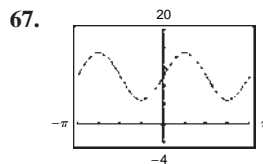
Amplitude: $\frac{2}{3}$
Period: 4π



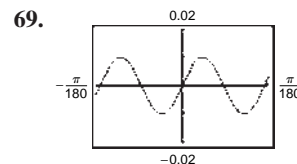
Amplitude: 2
Period: $\frac{\pi}{2}$



Amplitude: 1
Period: 1



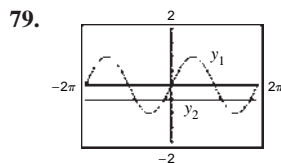
Amplitude: 5
Period: π



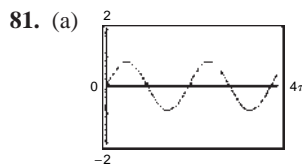
Amplitude: $\frac{1}{100}$
Period: $\frac{1}{60}$

71. $a = -4, d = 4$ 73. $a = -6, d = 1$

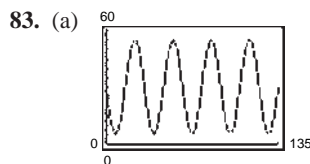
75. $a = -3, b = 2, c = 0$ 77. $a = 1, b = 1, c = \frac{\pi}{4}$



$x = -\frac{\pi}{6}, -\frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$

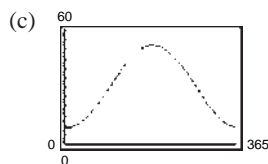


- (b) 6 sec
(c) 10 cycles/min
(d) The period of the model would decrease because the time for a respiratory cycle would decrease.



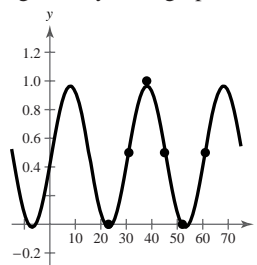
- (b) Minimum height: 5 ft
Maximum height: 55 ft

85. (a) 365 days. The cycle is 1 year.
(b) 30.3 gallons per day. The average is the constant term of the model.



Consumption exceeds 40 gallons per day from the beginning of May through part of September.

87. (a) and (c)



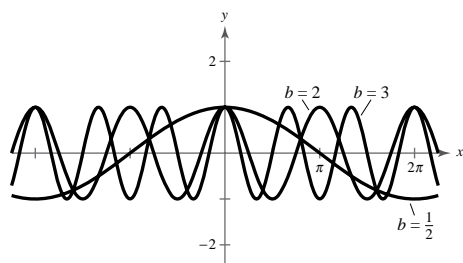
The model fits the data well.

- (b) $y = 0.493 \sin(0.209x - 0.114) + 0.472$
(d) 30 days (e) 12.9%

89. True. The period of $\sin x$ is 2π . Adding 2π moves the graph one period to the right.

91. False. The function $y = \frac{1}{2} \cos 2x$ has an amplitude that is one-half that of the function $y = \cos x$.

93.

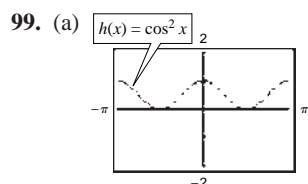

 The value of b affects the period of the graph.

$$b = \frac{1}{2} \rightarrow \frac{1}{2} \text{ cycle}$$

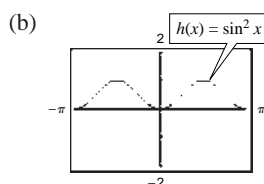
$$b = 2 \rightarrow 2 \text{ cycles}$$

$$b = 3 \rightarrow 3 \text{ cycles}$$

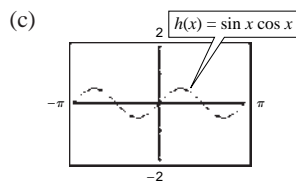
95. e 97. c



Even



Even



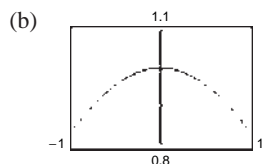
Odd

101. (a)

x	-1	-0.1	-0.01
$\frac{\sin x}{x}$	0.8415	0.9983	1.0000

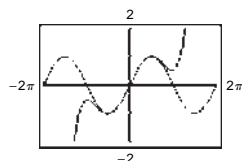
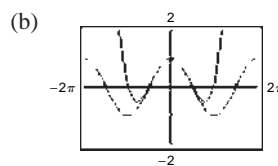
x	-0.001	0	0.001
$\frac{\sin x}{x}$	1.0000	Undefined	1.0000

x	0.01	0.1	1
$\frac{\sin x}{x}$	1.0000	0.9983	0.8415

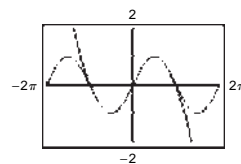

 $f \rightarrow 1$ as $x \rightarrow 0$

 (c) The ratio approaches 1 as x approaches 0.

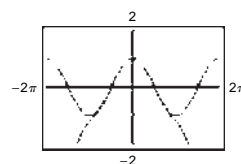
103. (a)


 The polynomial function is a good approximation of the sine function when x is close to 0.

 The polynomial function is a good approximation of the cosine function when x is close to 0.

(c) $\sin x \approx x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!}$

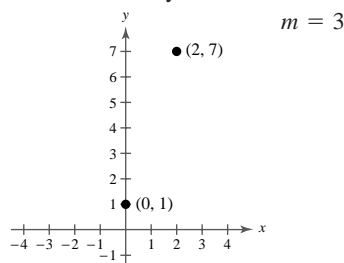


$\cos x \approx 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!}$



The accuracy increased.

105.


 107. 487.014°

109. Answers will vary.

Section 4.6 (page 311)

1. vertical 3. tangent, cotangent

 5. (a) $x = -2\pi, -\pi, 0, \pi, 2\pi$ (b) $y = 0$

(c) Increasing on $\left(-2\pi, -\frac{3\pi}{2}\right), \left(-\frac{3\pi}{2}, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \frac{3\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$

(d) No relative extrema

(e) $x = -\frac{3\pi}{2}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}$

 7. (a) No x -intercepts (b) $y = 1$

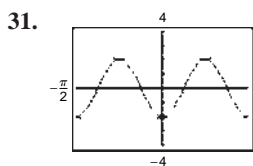
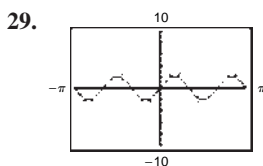
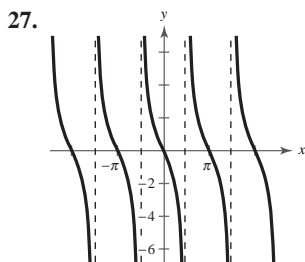
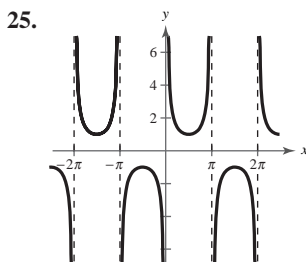
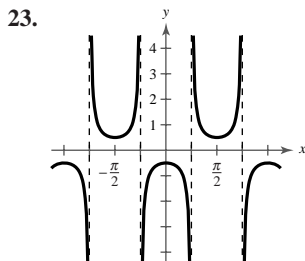
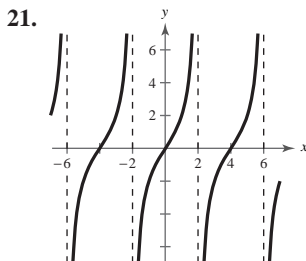
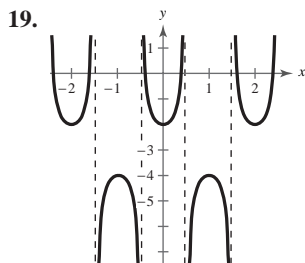
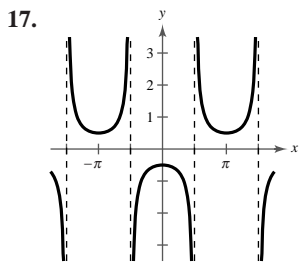
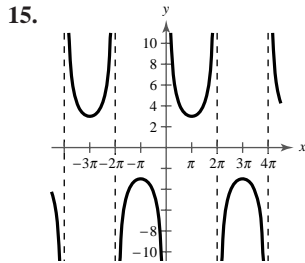
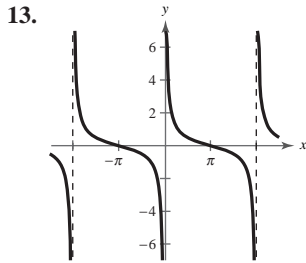
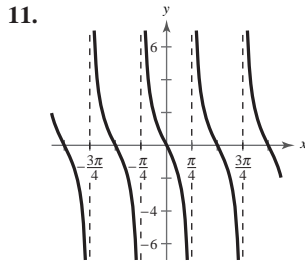
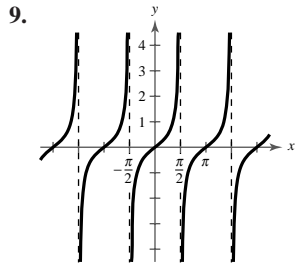
(c) Increasing on $\left(-2\pi, -\frac{3\pi}{2}\right), \left(-\frac{3\pi}{2}, -\pi\right), \left(0, \frac{\pi}{2}\right), \left(\frac{\pi}{2}, \pi\right)$

Decreasing on $\left(-\pi, -\frac{\pi}{2}\right), \left(-\frac{\pi}{2}, 0\right), \left(\pi, \frac{3\pi}{2}\right), \left(\frac{3\pi}{2}, 2\pi\right)$

(d) Relative minima: $(-2\pi, 1), (0, 1), (2\pi, 1)$

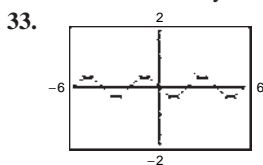
Relative maxima: $(-\pi, -1), (\pi, -1)$

(e) $x = -\frac{3\pi}{2}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}$



Answers will vary.

Answers will vary.



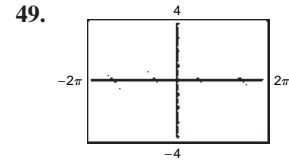
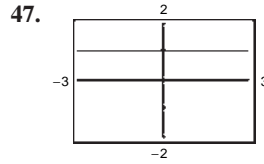
Answers will vary.

35. $-5.498, -2.356, 0.785, 3.927$

37. $-4.189, -2.094, 2.094, 4.189$

39. $-5.236, -2.094, 1.047, 4.189$

41. Even 43. Odd 45. Odd



Not equivalent;

Equivalent

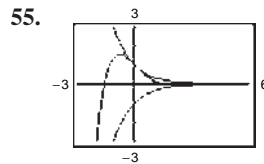
y_1 is undefined at $x = 0$.

51. d; as x approaches 0, $f(x)$ approaches 0.

52. a; as x approaches 0, $f(x)$ approaches 0.

53. b; as x approaches 0, $g(x)$ approaches 0.

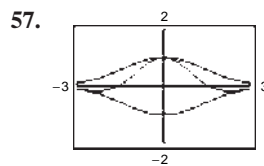
54. c; as x approaches 0, $g(x)$ approaches 0.



$-e^{-x} \leq e^{-x} \cos x \leq e^{-x}$

Touches $y = \pm e^{-x}$ at $x = n\pi$

Intercepts at $x = \frac{\pi}{2} + n\pi$



$-e^{-x^2/4} \leq e^{-x^2/4} \cos x \leq e^{-x^2/4}$

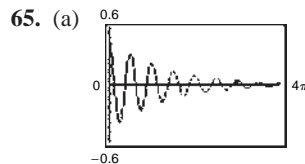
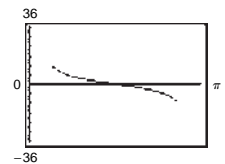
Touches $y = \pm e^{-x}$ at $x = n\pi$

Intercepts at $x = \frac{\pi}{2} + n\pi$

59. (a) $f \rightarrow -\infty$ (b) $f \rightarrow \infty$ (c) $f \rightarrow -\infty$ (d) $f \rightarrow \infty$

61. (a) $f \rightarrow \infty$ (b) $f \rightarrow -\infty$ (c) $f \rightarrow \infty$ (d) $f \rightarrow -\infty$

63. $d = 5 \cot x$



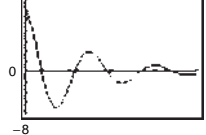
(b) Not periodic and damped; approaches 0 as t increases.

67. (a) Yes. To each t there corresponds one and only one value of y .

(b) 1.3 oscillations/sec (c) $y = 12(0.221)^t \cos(8.2t)$

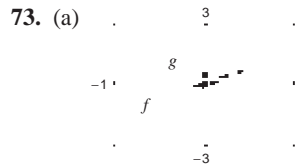
(d) $y = 12e^{-1.5t} \cos(8.2t)$

(e) Answers will vary.



69. True. The sine function is damped.

71. True. $\sec x = \csc\left(x - \frac{\pi}{2}\right) = \frac{1}{\sin\left(x - \frac{\pi}{2}\right)}$



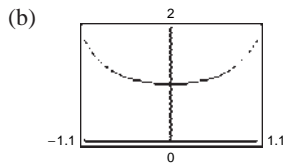
(b) $(-1, \frac{1}{3})$ (c) $(-1, \frac{1}{3})$; The intervals are the same.

75. (a)

x	-1	-0.1	-0.01
$\frac{\tan x}{x}$	1.5574	1.0033	1.0000

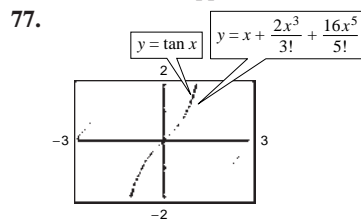
x	-0.001	0	0.001
$\frac{\tan x}{x}$	1.0000	Undefined	1.0000

x	0.01	0.1	1
$\frac{\tan x}{x}$	1.0000	1.0033	1.5574



$f \rightarrow 1$ as $x \rightarrow 0$

(c) The ratio approaches 1 as x approaches 0.



The polynomial function is a good approximation of the tangent function when x is close to 0.

79. Distributive Property 81. Additive Identity Property

83. Not one-to-one 85. One-to-one. $f^{-1}(x) = \frac{x^2 + 14}{3}, x \geq 0$

87. Domain: all real numbers x
Intercepts: $(-4, 0), (1, 0), (0, -4)$
No asymptotes

89. Domain: all real numbers x
Intercept: $(0, 5)$
Asymptote: $y = 2$

Section 4.7 (page 322)

1. $y = \sin^{-1} x, -1 \leq x \leq 1$ 3. $\sin^{-1} x$ or $\arcsin x$

5. (a) $\frac{\pi}{6}$ (b) 0 7. (a) $\frac{\pi}{2}$ (b) 0

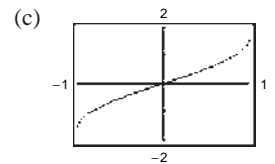
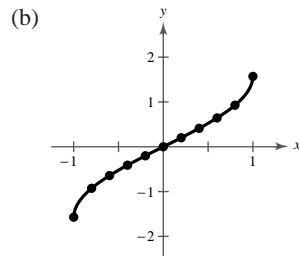
9. (a) $\frac{\pi}{6}$ (b) $-\frac{\pi}{4}$ 11. (a) $-\frac{\pi}{3}$ (b) $\frac{\pi}{3}$

13. (a) $\frac{\pi}{3}$ (b) $-\frac{\pi}{6}$

15. (a)

x	-1	-0.8	-0.6	-0.4	-0.2
y	-1.571	-0.927	-0.644	-0.412	-0.201

x	0	0.2	0.4	0.6	0.8	1
y	0	0.201	0.412	0.644	0.927	1.571



They are the same.

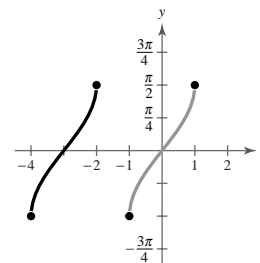
(d) Intercept: $(0, 0)$; symmetric about the origin

17. $(-\sqrt{3}, -\frac{\pi}{3}), (-\frac{\sqrt{3}}{3}, -\frac{\pi}{6}), (1, \frac{\pi}{4})$

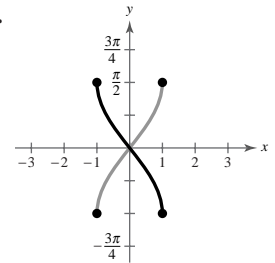
19. 0.47 21. 1.50 23. 0.72 25. -0.85

27. -1.41 29. 0.85 31. 1.29

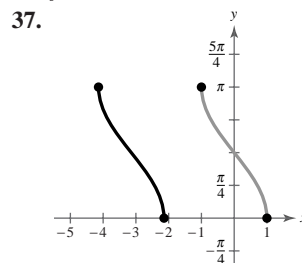
33. 35.



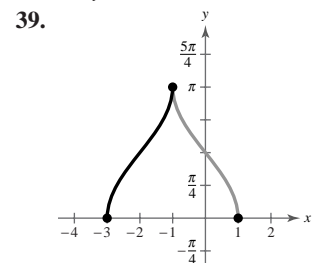
g is a horizontal shift of f three units to the left.



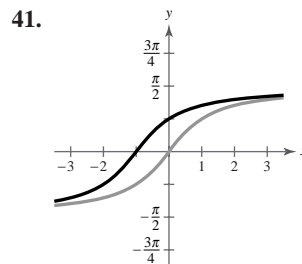
g is a reflection of f in the y -axis.



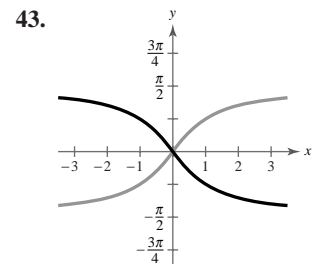
g is a horizontal shift of f π units to the left.



g is a reflection of f in the y -axis and a horizontal shift of f two units to the left.



g is a horizontal shift of f one unit to the left.



g is a reflection of f in the y -axis.

45. $\theta = \arctan \frac{x}{8}$ 47. $\theta = \arcsin \frac{x+2}{5}$

49. $\sqrt{4-x^2}$; $\theta = \arcsin \frac{x}{2}$, $\theta = \arccos \frac{\sqrt{4-x^2}}{2}$,
 $\theta = \arctan \frac{x}{\sqrt{4-x^2}}$

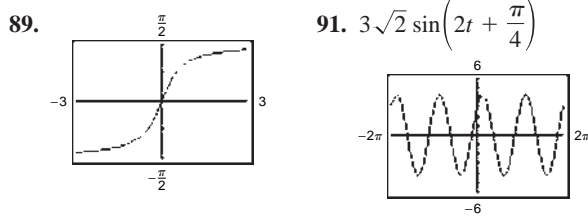
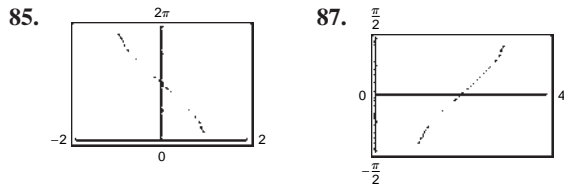
51. $\sqrt{x^2+2x+5}$; $\theta = \arcsin \frac{x+1}{\sqrt{x^2+2x+5}}$,
 $\theta = \arccos \frac{2}{\sqrt{x^2+2x+5}}$, $\theta = \arctan \frac{x+1}{2}$

53. 0.7 55. -0.3 57. 0 59. $-\frac{\pi}{6}$ 61. $\frac{\pi}{2}$

63. $\frac{\pi}{2}$ 65. $\frac{4}{5}$ 67. $\frac{7}{25}$ 69. $\frac{\sqrt{34}}{5}$ 71. $\frac{\sqrt{5}}{3}$

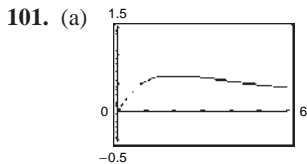
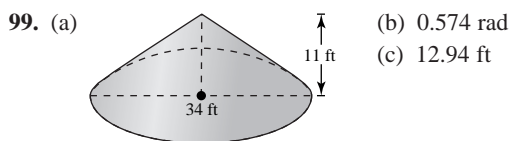
73. $\frac{1}{x}$ 75. $\sqrt{-x^2-4x-3}$ 77. $\frac{\sqrt{25-x^2}}{x}$

79. $\frac{\sqrt{x^2+7}}{x}$ 81. $\frac{14}{\sqrt{x^2+196}}$ 83. $\frac{|x-1|}{\sqrt{x^2-2x+10}}$



The two forms are equivalent.

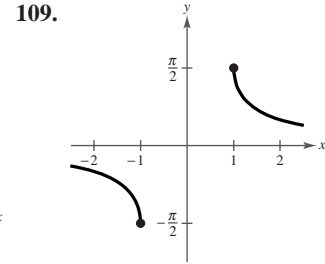
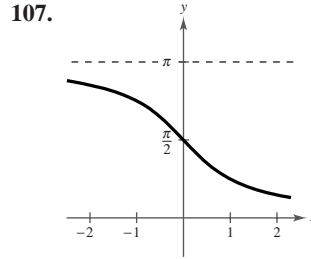
93. $\frac{\pi}{2}$ 95. $\frac{\pi}{2}$ 97. π



- (b) 2 ft
(c) $\beta = 0$; As the camera moves farther from the picture, the angle subtended by the camera approaches zero.

103. (a) $\theta = \arctan \frac{x}{20}$ (b) 0.245 rad, 0.540 rad

105. False. $\arctan 1 = \frac{\pi}{4}$



111. $\frac{\pi}{4}$ 113. $\frac{5\pi}{6}$ 115 and 117. Proofs

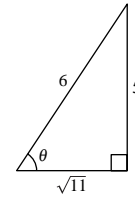
119. $\frac{\sqrt{2}}{2}$ 121. $\frac{\sqrt{3}}{3}$

123. $\cos \theta = \frac{\sqrt{11}}{6}$
 $\tan \theta = \frac{5\sqrt{11}}{11}$

$\csc \theta = \frac{6}{5}$

$\sec \theta = \frac{6\sqrt{11}}{11}$

$\cot \theta = \frac{\sqrt{11}}{5}$



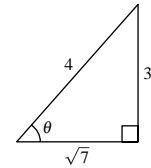
125. $\cos \theta = \frac{\sqrt{7}}{4}$

$\tan \theta = \frac{3\sqrt{7}}{7}$

$\csc \theta = \frac{4}{3}$

$\sec \theta = \frac{4\sqrt{7}}{7}$

$\cot \theta = \frac{\sqrt{7}}{3}$



Section 4.8 (page 332)

1. harmonic motion

3. No

5. $B = 60^\circ$ 7. $A = 19^\circ$

9. $A \approx 26.57^\circ$

$a \approx 5.77$

$a \approx 4.82$

$B \approx 63.43^\circ$

$c \approx 11.55$

$c \approx 14.81$

$c \approx 13.42$

11. $A \approx 72.76^\circ$ 13. $B = 77^\circ 45'$

$B \approx 17.24^\circ$

$a \approx 91.34$

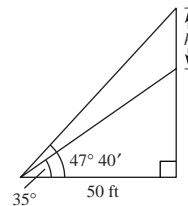
$a \approx 51.58$

$b \approx 420.70$

15. 5.12 in. 17. 8.21 ft 19. 19.70 ft 21. 109.63 ft

23. 2089.99 ft

25. (a) (b) $h = 50(\tan 47^\circ 40' - \tan 35^\circ)$
(c) 19.87 ft



27. (a) $l = \sqrt{h^2 + 28h + 10,196}$ (b) $\theta = \arccos \frac{100}{l}$

(c) $h \approx 56$ ft

29. 70.35°

31. 75.97° 33. 5098.78 ft 35. 0.66 mi
 37. 104.95 nm south, 58.18 nm west
 39. (a) $N 58^\circ E$ (b) 68.82 m 41. $N 56.31^\circ W$
 43. 1933.32 ft 45. 3.23 mi
 47. (a) 61.82° ; 15.64° (b) 31.10 ft
 49. 78.69° 51. 35.26° 53. $y = \sqrt{3}r$

55. $d = 8 \sin \pi t$ 57. $d = 3 \cos \frac{4\pi t}{3}$

59. (a) 4 (b) 4 (c) 4 (d) $\frac{1}{16}$
 61. (a) $\frac{1}{16}$ (b) 70 (c) 0 (d) $\frac{1}{140}$ 63. $\omega = 528\pi$

65. (a)  (b) $\frac{\pi}{8}$ sec (c) $\frac{\pi}{32}$ sec

67. (a)

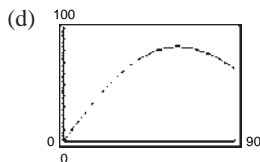
Base 1	Base 2	Altitude	Area
8	$8 + 16 \cos 10^\circ$	$8 \sin 10^\circ$	22.06
8	$8 + 16 \cos 20^\circ$	$8 \sin 20^\circ$	42.46
8	$8 + 16 \cos 30^\circ$	$8 \sin 30^\circ$	59.71
8	$8 + 16 \cos 40^\circ$	$8 \sin 40^\circ$	72.65
8	$8 + 16 \cos 50^\circ$	$8 \sin 50^\circ$	80.54
8	$8 + 16 \cos 60^\circ$	$8 \sin 60^\circ$	83.14
8	$8 + 16 \cos 70^\circ$	$8 \sin 70^\circ$	80.71

(b)

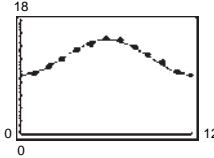
Base 1	Base 2	Altitude	Area
8	$8 + 16 \cos 56^\circ$	$8 \sin 56^\circ$	82.73
8	$8 + 16 \cos 58^\circ$	$8 \sin 58^\circ$	83.04
8	$8 + 16 \cos 59^\circ$	$8 \sin 59^\circ$	83.11
8	$8 + 16 \cos 60^\circ$	$8 \sin 60^\circ$	83.14
8	$8 + 16 \cos 61^\circ$	$8 \sin 61^\circ$	83.11
8	$8 + 16 \cos 62^\circ$	$8 \sin 62^\circ$	83.04

83.14 ft^2

(c) $A = 64(1 + \cos \theta)(\sin \theta)$



83.14 ft^2 ; They are the same.

69. (a)  (b) 12 mo; Yes, there are 12 months in a year.
 (c) 2.77; The maximum change in the number of hours of daylight

71. True. In $a \sin \omega t$ or $a \cos \omega t$, a is a real number.

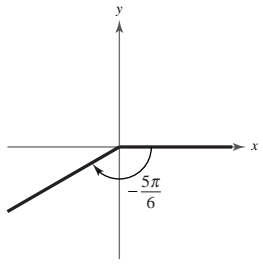
73. False. The amplitude is equal to a .

75. Answers will vary. 77. $4x - y + 6 = 0$
 79. $4x + 5y - 22 = 0$ 81. All real numbers x
 83. All real numbers x

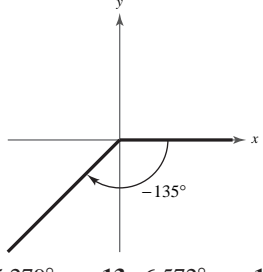
Review Exercises (page 340)

1. 1 rad

3. (a)  (b) Quadrant III
 (c) $\frac{10\pi}{3}, -\frac{2\pi}{3}$

5. (a)  (b) Quadrant III
 (c) $\frac{7\pi}{6}, -\frac{17\pi}{6}$

7. (a)  (b) Quadrant I
 (c) $405^\circ, -315^\circ$

9. (a)  (b) Quadrant III
 (c) $225^\circ, -495^\circ$

11. 135.279° 13. 6.572° 15. $135^\circ 17' 24''$

17. $-85^\circ 21' 36''$ 19. 1.641 21. 7.243

23. 128.571° 25. -200.535°

27. Complement: $\frac{3\pi}{8}$; supplement: $\frac{7\pi}{8}$

29. Complement: $\frac{\pi}{5}$; supplement: $\frac{7\pi}{10}$

31. Complement: 85° ; supplement: 175°

33. Complement: none; supplement: 23°

35. $\frac{25}{12}$ rad 37. $\frac{46\pi}{3}$ m 39. 6000π cm/min

41. $\left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$ 43. $\left(-\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$

45. $\left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ 47. $\left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$

$$49. \sin \frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$\cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$\tan \frac{\pi}{4} = 1$$

$$\csc \frac{\pi}{4} = \sqrt{2}$$

$$\sec \frac{\pi}{4} = \sqrt{2}$$

$$\cot \frac{\pi}{4} = 1$$

$$53. \sin\left(-\frac{11\pi}{6}\right) = \frac{1}{2}$$

$$\cos\left(-\frac{11\pi}{6}\right) = \frac{\sqrt{3}}{2}$$

$$\tan\left(-\frac{11\pi}{6}\right) = \frac{\sqrt{3}}{3}$$

$$\csc\left(-\frac{11\pi}{6}\right) = 2$$

$$\sec\left(-\frac{11\pi}{6}\right) = \frac{2\sqrt{3}}{3}$$

$$\cot\left(-\frac{11\pi}{6}\right) = \sqrt{3}$$

$$57. 1 \quad 59. -\frac{1}{2}$$

$$63. (a) \frac{2}{3} \quad (b) \frac{3}{2}$$

$$69. \sin \theta = \frac{\sqrt{65}}{9}$$

$$\cos \theta = \frac{4}{9}$$

$$\tan \theta = \frac{\sqrt{65}}{4}$$

$$\csc \theta = \frac{9\sqrt{65}}{65}$$

$$\sec \theta = \frac{9}{4}$$

$$\cot \theta = \frac{4\sqrt{65}}{65}$$

$$73. \sin \theta = \frac{7}{24}$$

$$\cos \theta = \frac{\sqrt{527}}{24}$$

$$\tan \theta = \frac{7\sqrt{527}}{527}$$

$$\csc \theta = \frac{24}{7}$$

$$\sec \theta = \frac{24\sqrt{527}}{527}$$

$$\cot \theta = \frac{\sqrt{527}}{7}$$

$$77. (a) 0.1045 \quad (b) 0.1045 \quad 79. (a) 0.7071 \quad (b) 1.4142$$

$$81. \text{Answers will vary.} \quad 83. 235 \text{ ft}$$

$$51. \sin 2\pi = 0$$

$$\cos 2\pi = 1$$

$$\tan 2\pi = 0$$

$$\csc 2\pi \text{ is undefined.}$$

$$\sec 2\pi = 1$$

$$\cot 2\pi \text{ is undefined.}$$

$$55. \sin\left(-\frac{\pi}{2}\right) = -1$$

$$\cos\left(-\frac{\pi}{2}\right) = 0$$

$$\tan\left(-\frac{\pi}{2}\right) \text{ is undefined.}$$

$$\csc\left(-\frac{\pi}{2}\right) = -1$$

$$\sec\left(-\frac{\pi}{2}\right) \text{ is undefined.}$$

$$\cot\left(-\frac{\pi}{2}\right) = 0$$

$$61. (a) -\frac{3}{5} \quad (b) -\frac{5}{3}$$

$$65. -0.8935 \quad 67. 0.5$$

$$71. \sin \theta = \frac{5\sqrt{61}}{61}$$

$$\cos \theta = \frac{6\sqrt{61}}{61}$$

$$\tan \theta = \frac{5}{6}$$

$$\csc \theta = \frac{\sqrt{61}}{5}$$

$$\sec \theta = \frac{\sqrt{61}}{6}$$

$$\cot \theta = \frac{6}{5}$$

$$75. \sin \theta = \frac{\sqrt{17}}{17}$$

$$\cos \theta = \frac{4\sqrt{17}}{17}$$

$$\tan \theta = \frac{1}{4}$$

$$\csc \theta = \sqrt{17}$$

$$\sec \theta = \frac{\sqrt{17}}{4}$$

$$\cot \theta = 4$$

$$85. \sin \theta = \frac{4}{5}$$

$$\cos \theta = \frac{3}{5}$$

$$\tan \theta = \frac{4}{3}$$

$$\csc \theta = \frac{5}{4}$$

$$\sec \theta = \frac{5}{3}$$

$$\cot \theta = \frac{3}{4}$$

$$89. \sin \theta = \frac{15\sqrt{481}}{481}$$

$$\cos \theta = \frac{16\sqrt{481}}{481}$$

$$\tan \theta = \frac{15}{16}$$

$$\csc \theta = \frac{\sqrt{481}}{15}$$

$$\sec \theta = \frac{\sqrt{481}}{16}$$

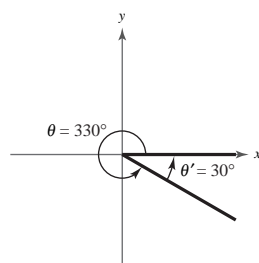
$$\cot \theta = \frac{16}{15}$$

$$93. \cos \theta = -\frac{\sqrt{55}}{8}$$

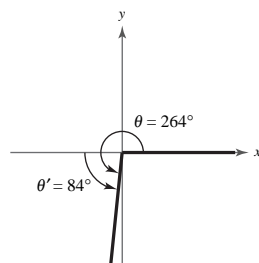
$$\tan \theta = -\frac{3\sqrt{55}}{55}$$

$$\csc \theta = \frac{8}{3}$$

$$95. \theta' = 30^\circ$$



$$99. \theta' = 84^\circ$$



$$103. \sin 240^\circ = -\frac{\sqrt{3}}{2}$$

$$\cos 240^\circ = -\frac{1}{2}$$

$$\tan 240^\circ = \sqrt{3}$$

$$87. \sin \theta = \frac{2\sqrt{53}}{53}$$

$$\cos \theta = -\frac{7\sqrt{53}}{53}$$

$$\tan \theta = -\frac{2}{7}$$

$$\csc \theta = \frac{\sqrt{53}}{2}$$

$$\sec \theta = -\frac{\sqrt{53}}{7}$$

$$\cot \theta = -\frac{7}{2}$$

$$91. \sin \theta = -\frac{\sqrt{11}}{6}$$

$$\cos \theta = \frac{5}{6}$$

$$\tan \theta = -\frac{\sqrt{11}}{5}$$

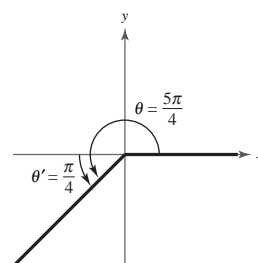
$$\csc \theta = -\frac{6\sqrt{11}}{11}$$

$$\cot \theta = -\frac{5\sqrt{11}}{11}$$

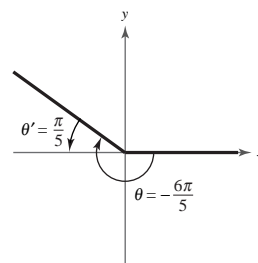
$$\sec \theta = -\frac{8\sqrt{55}}{55}$$

$$\cot \theta = -\frac{\sqrt{55}}{3}$$

$$97. \theta' = \frac{\pi}{4}$$



$$101. \theta' = \frac{\pi}{5}$$



$$105. \sin(-210^\circ) = \frac{1}{2}$$

$$\cos(-210^\circ) = -\frac{\sqrt{3}}{2}$$

$$\tan(-210^\circ) = -\frac{\sqrt{3}}{3}$$

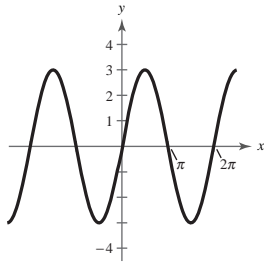
$$107. \sin\left(-\frac{9\pi}{4}\right) = -\frac{\sqrt{2}}{2}$$

$$\cos\left(-\frac{9\pi}{4}\right) = \frac{\sqrt{2}}{2}$$

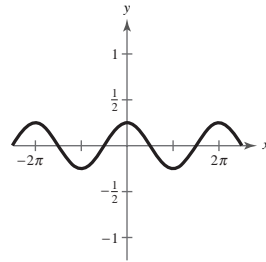
$$\tan\left(-\frac{9\pi}{4}\right) = -1$$

$$111. 0.6494 \quad 113. 3.2361$$

115.



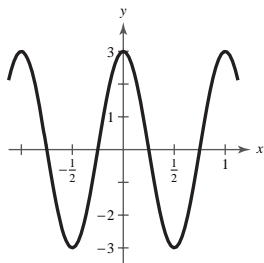
117.



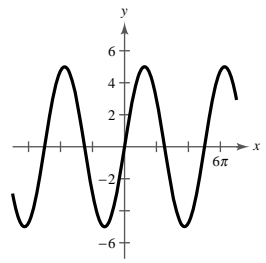
119. Period: 2; amplitude: 5

 121. Period: π ; amplitude: 3.4

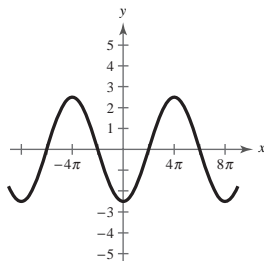
123.



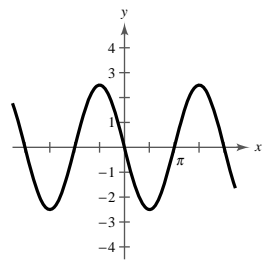
125.



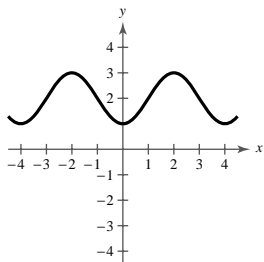
127.



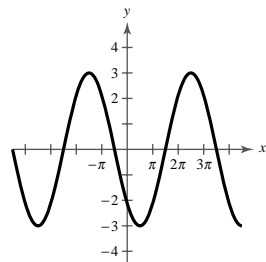
129.



131.



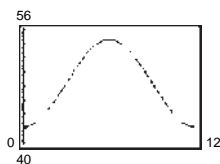
133.



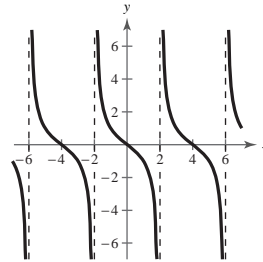
$$135. a = -2, b = 1, c = \frac{\pi}{4}$$

$$137. a = -4, b = 2, c = \frac{\pi}{2}$$

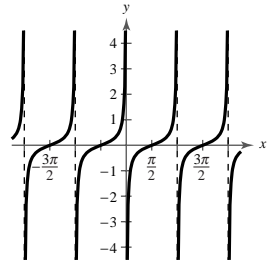
139.


 Maximum sales: June
Minimum sales: December

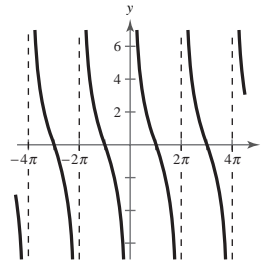
141.



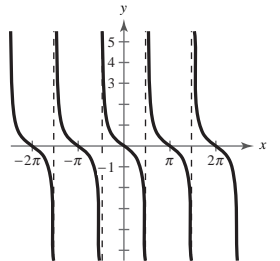
143.



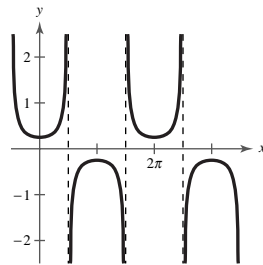
145.



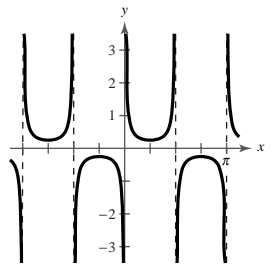
147.



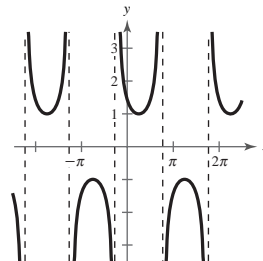
149.



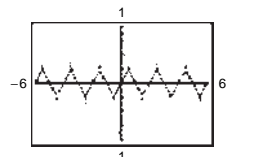
151.



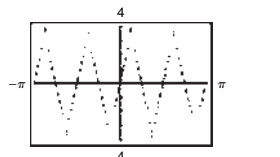
153.



155.



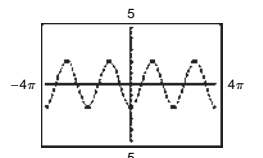
157.



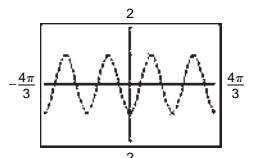
Answers will vary.

Answers will vary.

159.



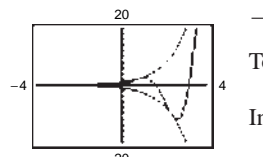
161.



Answers will vary.

Answers will vary.

163.

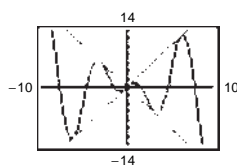


$$-e^x \leq e^x \sin 2x \leq e^x$$

$$\text{Touches } y = \pm e^x \text{ at } x = \frac{\pi}{4} + \frac{n\pi}{2}$$

$$\text{Intercepts at } x = \frac{n\pi}{2}$$

165.



$$-2x \leq 2x \cos x \leq 2x$$

Touches $y = \pm 2x$ at $x = n\pi$

Intercepts at $x = \frac{\pi}{2} + n\pi$

167. (a) $-\frac{\pi}{2}$ (b) 0 169. (a) $\frac{\pi}{4}$ (b) $\frac{5\pi}{6}$

171. 1.14 173. -1.22 175. -1.49 177. 0.68

179. $\theta = \arcsin \frac{x}{16}$ 181. $\frac{1}{\sqrt{2x-x^2}}$ 183. $\frac{2\sqrt{4-2x^2}}{4-x^2}$

185. 0.071 km 187. 9.47 mi 189. $d = 3 \cos \frac{2\pi t}{15}$

191. False. y is a function but is not one-to-one on $30^\circ \leq \theta \leq 150^\circ$.

193. False. Sine or cosine is used to model harmonic motion.

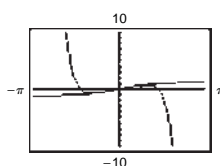
195. (a)

s	10	20	30
θ	0.0224	0.0894	0.1989

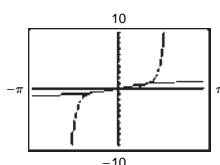
s	40	50	60
θ	0.3441	0.5105	0.6786

(b) θ is not a linear function of s .

197. (a)


The polynomial function is a good approximation for the arctangent function when x is close to 0.

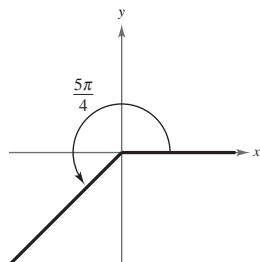
(b) $\arctan x \approx x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \frac{x^9}{9}$



The accuracy of the approximation increases as additional terms are added.

Chapter Test (page 345)

1. (a)



(b) Answers will vary.

Sample answer:

$$\frac{13\pi}{4}, -\frac{3\pi}{4}$$

(c) 225°

2. $44\frac{4}{9} \approx 44.44$ rad/sec

3. $\sin \theta = \frac{4\sqrt{17}}{17}$

$$\cos \theta = -\frac{\sqrt{17}}{17}$$

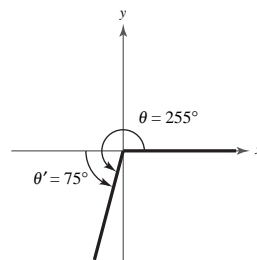
$$\tan \theta = -4$$

$$\csc \theta = \frac{\sqrt{17}}{4}$$

$$\sec \theta = -\sqrt{17}$$

$$\cot \theta = -\frac{1}{4}$$

5. $\theta' = 75^\circ$



7. $135^\circ, 225^\circ$

8. 1.33, 1.81

9. $\sin \theta = \frac{4}{5}$

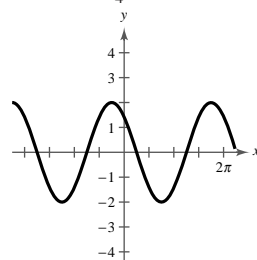
$$\tan \theta = -\frac{4}{3}$$

$$\csc \theta = \frac{5}{4}$$

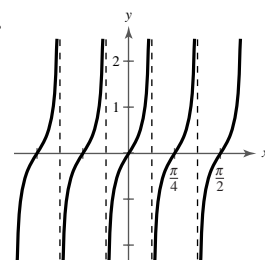
$$\sec \theta = -\frac{5}{3}$$

$$\cot \theta = -\frac{3}{4}$$

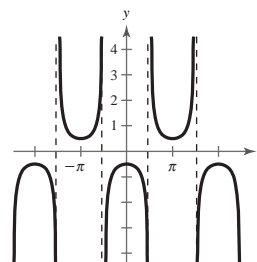
10.



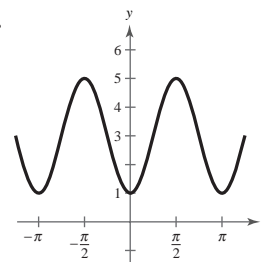
11.



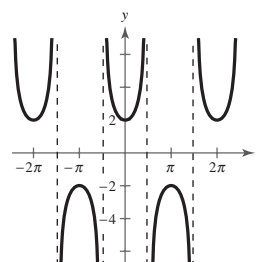
12.



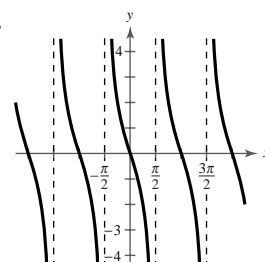
13.

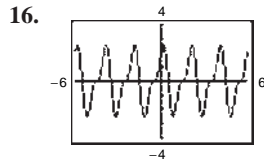


14.



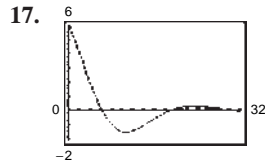
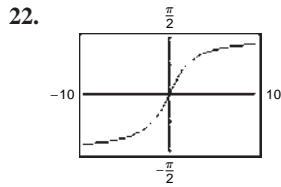
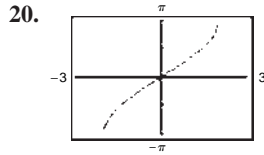
15.



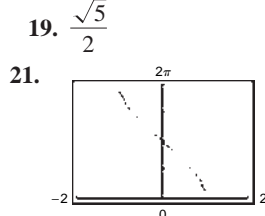


Period: 2

18. $a = -2$, $b = \frac{1}{2}$, $c = -\frac{\pi}{4}$



Not periodic

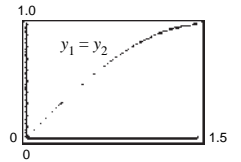


23. 231.34°

71.

x	0.2	0.4	0.6	0.8
y_1	0.1987	0.3894	0.5646	0.7174
y_2	0.1987	0.3894	0.5646	0.7174

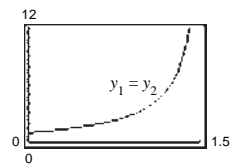
x	1.0	1.2	1.4
y_1	0.8415	0.9320	0.9854
y_2	0.8415	0.9320	0.9854



73.

x	0.2	0.4	0.6	0.8
y_1	1.2230	1.5085	1.8958	2.4650
y_2	1.2230	1.5085	1.8958	2.4650

x	1.0	1.2	1.4
y_1	3.4082	5.3319	11.6814
y_2	3.4082	5.3319	11.6814



Chapter 5

Section 5.1 (page 354)

1. (a) iii (b) i (c) ii 3. $\sin u$ 5. $\cos u$
7. $\tan x = \frac{\sqrt{3}}{3}$ 9. $\cos \theta = \frac{\sqrt{2}}{2}$
 $\csc x = 2$ $\tan \theta = -1$
 $\sec x = \frac{2\sqrt{3}}{3}$ $\csc \theta = -\sqrt{2}$
 $\cot x = \sqrt{3}$ $\cot \theta = -1$
11. $\sin x = -\frac{7}{25}$ 13. $\cos \phi = -\frac{15}{17}$
 $\cos x = -\frac{24}{25}$ $\tan \phi = -\frac{8}{15}$
 $\csc x = -\frac{25}{7}$ $\csc \phi = \frac{17}{8}$
 $\cot x = \frac{24}{7}$ $\cot \phi = -\frac{15}{8}$
15. $\sin x = \frac{2}{3}$ 17. $\sin \theta = -\frac{2\sqrt{5}}{5}$
 $\cos x = -\frac{\sqrt{5}}{3}$ $\cos \theta = -\frac{\sqrt{5}}{5}$
 $\csc x = \frac{3}{2}$ $\csc \theta = -\frac{\sqrt{5}}{2}$
 $\sec x = -\frac{3\sqrt{5}}{5}$ $\sec \theta = -\sqrt{5}$
 $\cot x = -\frac{\sqrt{5}}{2}$ $\cot \theta = \frac{1}{2}$
19. $\sin \theta = 0$ $\sec \theta = -1$
 $\cos \theta = -1$ $\cot \theta$ is undefined.
 $\tan \theta = 0$
21. d 22. a 23. b 24. f 25. e 26. c
 27. b 28. c 29. f 30. a 31. e 32. d
 33. $\cos x$ 35. $\cos^2 \phi$ 37. $\sec x$ 39. 1
 41. $\cot x$ 43. $1 + \sin y$ 45. $\cos^2 x$ 47. $\cos x + 2$
 49. $\sec^4 x$ 51. $\sin^2 x - \cos^2 x$ 53. $(\csc x - 1) \cot^2 x$
 55. $1 + 2 \sin x \cos x$ 57. $\cot^2 x$ 59. $2 \csc^2 x$
 61. $-\cot x$ 63. $\sec x$ 65. $1 + \cos y$ 67. $\cos x$
 69. $3(\sec x + \tan x)$

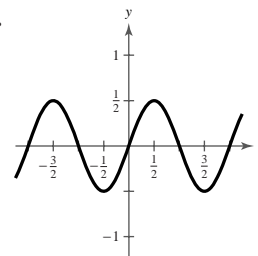
75. $\csc x$ 77. $\tan x$ 79. $5 \cos \theta$ 81. $3 \tan \theta$
 83. $3 \cos \theta$ 85. $3 \sec \theta$ 87. $3 \tan \theta$ 89. $\sqrt{2} \cos \theta$
 91. $0 \leq \theta \leq \pi$ 93. $0 \leq \theta < \frac{\pi}{2}$, $\frac{3\pi}{2} < \theta < 2\pi$
 95. $\ln|\cot \theta|$ 97. $\ln|(\cos x)(1 + \sin x)|$ 99. $\ln|\tan x|$
 101. The identity is not true when $\theta = \frac{7\pi}{6}$.
 103. The identity is not true when $\theta = \frac{5\pi}{3}$.
 105. The identity is not true when $\theta = \frac{7\pi}{4}$.
 107. (a) and (b) Answers will vary.
 109. (a) and (b) Answers will vary.
 111. $\mu = \tan \theta$ 113. Answers will vary.
 115. False. $\cos 0 \cdot \sec \frac{\pi}{4} \neq 1$ 117. 1, 1 119. $\infty, 0$

121. $\cos \theta = \pm \sqrt{1 - \sin^2 \theta}$ $\sec \theta = \pm \frac{1}{\sqrt{1 - \sin^2 \theta}}$
 $\tan \theta = \pm \frac{\sin \theta}{\sqrt{1 - \sin^2 \theta}}$ $\cot \theta = \pm \frac{\sqrt{1 - \sin^2 \theta}}{\sin \theta}$
 $\csc \theta = \frac{1}{\sin \theta}$

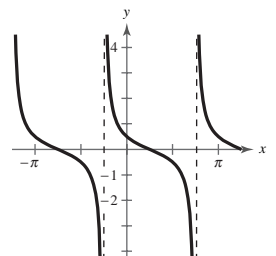
 The sign depends on the choice of θ .

123. $\frac{x^2 + 6x - 8}{(x + 5)(x - 8)}$ 125. $\frac{-5x^2 + 8x + 28}{(x^2 - 4)(x + 4)}$

127.



129.



Section 5.2 (page 362)

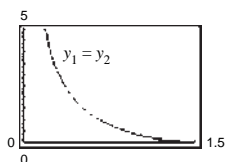
1. $\cot u$ 3. $\tan u$ 5. $\cos^2 u$ 7. $-\sin u$ 9. No

11–19. Answers will vary.

21.

x	0.2	0.4	0.6	0.8
y_1	4.8348	2.1785	1.2064	0.6767
y_2	4.8348	2.1785	1.2064	0.6767

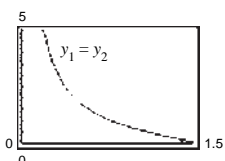
x	1.0	1.2	1.4
y_1	0.3469	0.1409	0.0293
y_2	0.3469	0.1409	0.0293



23.

x	0.2	0.4	0.6	0.8
y_1	4.8348	2.1785	1.2064	0.6767
y_2	4.8348	2.1785	1.2064	0.6767

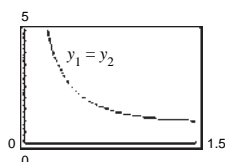
x	1.0	1.2	1.4
y_1	0.3469	0.1409	0.0293
y_2	0.3469	0.1409	0.0293



25.

x	0.2	0.4	0.6	0.8
y_1	5.0335	2.5679	1.7710	1.3940
y_2	5.0335	2.5679	1.7710	1.3940

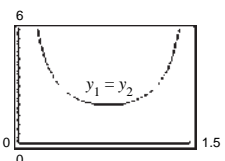
x	1.0	1.2	1.4
y_1	1.1884	1.0729	1.0148
y_2	1.1884	1.0729	1.0148



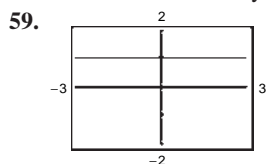
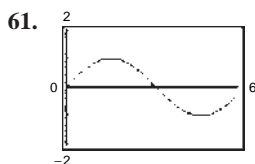
27.

x	0.2	0.4	0.6	0.8
y_1	5.1359	2.7880	2.1458	2.0009
y_2	5.1359	2.7880	2.1458	2.0009

x	1.0	1.2	1.4
y_1	2.1995	2.9609	5.9704
y_2	2.1995	2.9609	5.9704

29. $\cot(-x) = -\cot(x)$ 31. $(\tan^2 x)^2$

33–57. Answers will vary.

 $y = 1$  $y = \sin x$

63. Answers will vary. 65. 1 67. 2

69–75. Answers will vary.

77. (a) Answers will vary.

(b)

θ	15°	30°	45°	60°	75°	90°
s	18.66	8.66	5	2.88	1.34	0

(c) Maximum: 15° (d) Noon

Minimum: 90°

79. True. For instance, $(\sec^2 \theta - 1)/\sec^2 \theta = \sin^2 \theta$ was verified two different ways on page 358.81. False. $\sin^2\left(\frac{\pi}{4}\right) + \cos^2\left(\frac{\pi}{4}\right) \neq 1 + \tan^2\left(\frac{\pi}{4}\right)$

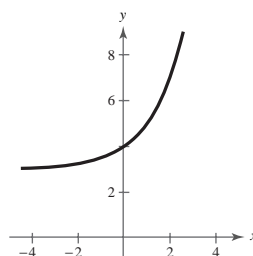
83. (a) Answers will vary. (b) No. Division by zero.

85. $a \cos \theta$ 87. $a \sec \theta$ 89. $\sqrt{\tan^2 x} = |\tan x|$; $\frac{3\pi}{4}$ 91. $|\tan \theta| = \sqrt{\sec^2 \theta - 1}$; $\frac{3\pi}{4}$

93. Answers will vary.

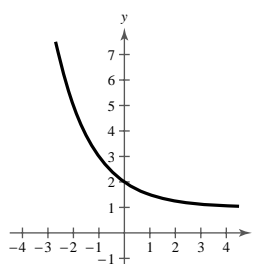
95.

x	-4	-2	0	2	3
y	3.0625	3.25	4	7	11

Horizontal asymptote at $y = 3$

97.

x	-3	-2	0	2	4
y	9	5	2	1.25	1.0625

Horizontal asymptote at $y = 1$

Section 5.3 (page 373)

1. general 3. No 5–9. Answers will vary.

11. 30°, 150° 13. 120°, 240° 15. 45°, 225°

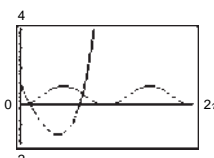
17. $\frac{5\pi}{6}, \frac{7\pi}{6}$ 19. $\frac{3\pi}{4}, \frac{7\pi}{4}$ 21. $\frac{5\pi}{6}, \frac{11\pi}{6}$ 23. $\frac{7\pi}{6}, \frac{11\pi}{6}$ 25. $\frac{\pi}{6}, \frac{7\pi}{6}$ 27. $\frac{3\pi}{4}, \frac{7\pi}{4}$ 29. $\frac{7\pi}{6} + 2n\pi, \frac{11\pi}{6} + 2n\pi$ 31. $\frac{\pi}{6} + 2n\pi, \frac{11\pi}{6} + 2n\pi$ 33. $\frac{\pi}{6} + n\pi, \frac{5\pi}{6} + n\pi$ 35. $\frac{\pi}{3} + n\pi, \frac{2\pi}{3} + n\pi$ 37. $\frac{2\pi}{3}, \frac{5\pi}{3}$ 39. $\frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$ 41. 0, $\frac{\pi}{2}, \pi, \frac{3\pi}{2}$

43. $\frac{\pi}{3}, \pi, \frac{5\pi}{3}$ 45. No solution 47. $\frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$

49. 3.6652, 4.7124, 5.7596 51. 0.8614, 5.4218

53. 1.5708 55. 0.5236, 2.6180

57. (a)  (b) $\sin 2x = x^2 - 2x$
 (c) (0, 0), (1.7757, -0.3984)

59. (a)  (b) $\sin^2 x = e^x - 4x$
 (c) (0.3194, -0.0986), (2.2680, 0.5878)

61. $2\pi + 4n\pi$ 63. $\frac{\pi}{8} + \frac{n\pi}{2}$ 65. $\frac{2\pi}{3} + n\pi, \frac{5\pi}{6} + n\pi$

67. $\frac{\pi}{2} + 4n\pi, \frac{7\pi}{2} + 4n\pi$ 69. $x = -1, 3$ 71. $x = \pm 2$

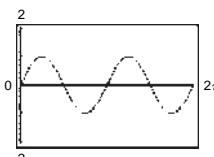
73. 1.1071, 4.2487 75. 0.8603, 3.4256

77. 0, 2.6779, 3.1416, 5.8195

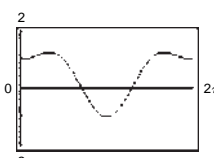
79. 0.3398, 0.8481, 2.2935, 2.8018

81. $\frac{\pi}{4}, \frac{5\pi}{4}, \arctan 5, \arctan 5 + \pi$

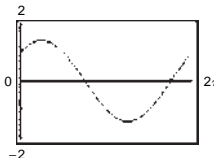
83. -1.154, 0.534 85. 1.110

87. (a) 
 Maxima: (0.7854, 1), (3.9270, 1)
 Minima: (2.3562, -1), (5.4978, -1)

(b) $\frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$

89. (a) 
 Maxima: (1.0472, 1.25), (5.2360, 1.25)
 Minima: (0, 1), (3.1416, -1), (6.2832, 1)

(b) $0, \frac{\pi}{3}, \pi, \frac{5\pi}{3}, 2\pi$

91. (a) 
 Maximum: (0.7854, 1.4142)
 Minimum: (3.9270, -1.4142)

(b) $\frac{\pi}{4}, \frac{5\pi}{4}$

93. 1 95. May, June, July

97. (a) All real numbers x except $x = 0$
 (b) y -axis symmetry; horizontal asymptote: $y = 1$
 (c) Oscillates
 (d) Infinite number of solutions
 (e) Yes. 0.6366

99. 0.04 sec, 0.43 sec, 0.83 sec 101. $36.87^\circ, 53.13^\circ$

103. (a)  (b) $0.6100 < x < 1.0980$

$x \approx 0.86, A \approx 1.12$

105. 1 107. False. $\sin x - x = 0$ has one solution, $x = 0$.

109. False. The range of the sine function does not include 3.4.

111. Answers will vary. 113. 2.164 rad

115. -0.007 rad 117. Answers will vary.

Section 5.4 (page 381)

1. $\sin u \cos v - \cos u \sin v$ 3. $\frac{\tan u + \tan v}{1 - \tan u \tan v}$

5. $\cos u \cos v + \sin u \sin v$

7. Sample answer: $\sin(45^\circ + 60^\circ)$

9. (a) $-\frac{1}{2}$ (b) $-\frac{3}{2}$ 11. (a) $\frac{\sqrt{2} - \sqrt{6}}{4}$ (b) $\frac{1 + \sqrt{2}}{2}$

13. (a) $\frac{\sqrt{2} + \sqrt{6}}{4}$ (b) $\frac{\sqrt{2} - 1}{2}$

15. $\sin 105^\circ = \frac{\sqrt{2} + \sqrt{6}}{4}$ 17. $\sin 195^\circ = \frac{\sqrt{2} - \sqrt{6}}{4}$

$\cos 105^\circ = \frac{\sqrt{2} - \sqrt{6}}{4}$ $\cos 195^\circ = -\frac{\sqrt{2} + \sqrt{6}}{4}$

$\tan 105^\circ = -2 - \sqrt{3}$ $\tan 195^\circ = 2 - \sqrt{3}$

19. $\sin \frac{11\pi}{12} = \frac{\sqrt{6} - \sqrt{2}}{4}$ 21. $\sin\left(-\frac{\pi}{12}\right) = \frac{\sqrt{2} - \sqrt{6}}{4}$

$\cos \frac{11\pi}{12} = -\frac{\sqrt{2} + \sqrt{6}}{4}$ $\cos\left(-\frac{\pi}{12}\right) = \frac{\sqrt{2} + \sqrt{6}}{4}$

$\tan \frac{11\pi}{12} = -2 + \sqrt{3}$ $\tan\left(-\frac{\pi}{12}\right) = \sqrt{3} - 2$

23. $\sin 75^\circ = \frac{\sqrt{2} + \sqrt{6}}{4}$ 25. $\sin(-285^\circ) = \frac{\sqrt{6} + \sqrt{2}}{4}$

$\cos 75^\circ = \frac{\sqrt{6} - \sqrt{2}}{4}$ $\cos(-285^\circ) = \frac{\sqrt{6} - \sqrt{2}}{4}$

$\tan 75^\circ = 2 + \sqrt{3}$ $\tan(-285^\circ) = \sqrt{3} + 2$

27. $\sin \frac{13\pi}{12} = \frac{\sqrt{2} - \sqrt{6}}{4}$ 29. $\sin\left(-\frac{7\pi}{12}\right) = -\frac{\sqrt{2} + \sqrt{6}}{4}$

$\cos \frac{13\pi}{12} = -\frac{\sqrt{2} + \sqrt{6}}{4}$ $\cos\left(-\frac{7\pi}{12}\right) = \frac{\sqrt{2} - \sqrt{6}}{4}$

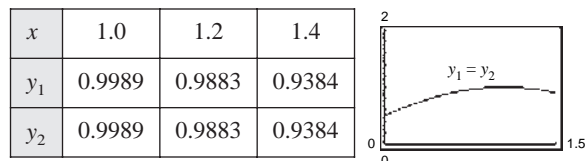
$\tan \frac{13\pi}{12} = 2 - \sqrt{3}$ $\tan\left(-\frac{7\pi}{12}\right) = 2 + \sqrt{3}$

31. $\cos 70^\circ$ 33. $\tan 209^\circ$ 35. $\sin 2.3$

37. $\cos \frac{16\pi}{63}$ 39. $\frac{\sqrt{3}}{2}$ 41. $\frac{\sqrt{3}}{2}$ 43. $-\sqrt{3}$

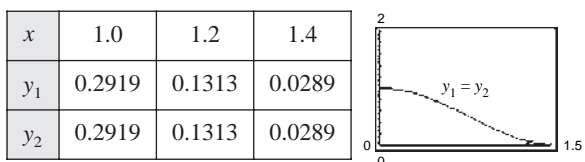
45.

x	0.2	0.4	0.6	0.8
y_1	0.6621	0.7978	0.9017	0.9696
y_2	0.6621	0.7978	0.9017	0.9696



47.

x	0.2	0.4	0.6	0.8
y_1	0.9605	0.8484	0.6812	0.4854
y_2	0.9605	0.8484	0.6812	0.4854



49. $-\frac{56}{65}$ 51. $-\frac{56}{33}$ 53. $\frac{13}{85}$ 55. $\frac{36}{85}$ 57. 1
59. $\frac{2x^2 - \sqrt{1-x^2}}{\sqrt{4x^2+1}}$ 61. 0 63. 0 65. 1
67. -1 69. $\frac{33}{65}$ 71. $\frac{24}{25}$ 73-79. Answers will vary.
81. $\frac{\pi}{2}$ 83. 0, $\frac{\pi}{3}$, π , $\frac{5\pi}{3}$ 85. 0.7854, 5.4978
87. $\frac{\pi}{2}$, π , $\frac{3\pi}{2}$ 89. Answers will vary.
91. False. $\cos(u \pm v) = \cos u \cos v \mp \sin u \sin v$
- 93 and 95. Answers will vary.
97. (a) $\sqrt{2} \sin\left(\theta + \frac{\pi}{4}\right)$ (b) $\sqrt{2} \cos\left(\theta - \frac{\pi}{4}\right)$
99. (a) $13 \sin(3\theta + 0.3948)$ (b) $13 \cos(3\theta - 1.1760)$
101. $2 \cos \theta$ 103. Answers will vary.
105. $u + v = w$. Answers will vary.
107. $\cos(u + v + w) = \cos u \cos v \cos w - \sin u \sin v \cos w - \sin u \cos v \sin w - \cos u \sin v \sin w$
109. (0, 19), (38, 0) 111. (0, 4), (2, 0), (7, 0)

Section 5.5 (page 390)

1. $\frac{1 + \cos 2u}{2}$ 3. $-2 \sin\left(\frac{u+v}{2}\right) \sin\left(\frac{u-v}{2}\right)$
5. $\tan \frac{u}{2}$ 7. (a) ii (b) i (c) iii
9. (a) $\frac{3}{5}$ (b) $\frac{4}{5}$ (c) $\frac{3}{4}$ (d) $\frac{24}{25}$
(e) $\frac{7}{25}$ (f) $\frac{25}{7}$ (g) $\frac{24}{24}$ (h) $\frac{7}{24}$
11. 0, 1.0472, 3.1416, 5.2360; 0, $\frac{\pi}{3}$, π , $\frac{5\pi}{3}$
13. 0.2618, 1.3090, 3.4034, 4.4506; $\frac{\pi}{12}$, $\frac{5\pi}{12}$, $\frac{13\pi}{12}$, $\frac{17\pi}{12}$
15. 0, 2.0944, 4.1888; 0, $\frac{2\pi}{3}$, $\frac{4\pi}{3}$
17. 0, 1.5708, 3.1416, 4.7124; 0, $\frac{\pi}{2}$, π , $\frac{3\pi}{2}$

19. 1.5708, 3.6652, 5.7596; $\frac{\pi}{2}$, $\frac{7\pi}{6}$, $\frac{11\pi}{6}$

21. $\sin 2u = \frac{24}{25}$ 23. $\sin 2u = \frac{4}{5}$
 $\cos 2u = \frac{7}{25}$ $\cos 2u = \frac{3}{5}$
 $\tan 2u = \frac{24}{7}$ $\tan 2u = \frac{4}{3}$

25. $\sin 2u = -\frac{\sqrt{3}}{2}$
 $\cos 2u = -\frac{1}{2}$
 $\tan 2u = \sqrt{3}$

27. $4 \sin 2x$ 29. $4 \cos 2x$ 31. $\frac{1}{8}(3 + 4 \cos 2x + \cos 4x)$

33. $\frac{1}{8}(1 - \cos 4x)$ 35. $\frac{1}{32}(2 + \cos 2x - 2 \cos 4x - \cos 6x)$

37. $\frac{1}{2}(1 - \cos 4x)$ 39. $\frac{1}{2}(1 + \cos x)$

41. $\frac{1 - \cos 4x}{1 + \cos 4x}$ 43. $\frac{1}{8}(3 - 4 \cos x + \cos 2x)$

45. (a) $\frac{4\sqrt{17}}{17}$ (b) $\frac{\sqrt{17}}{17}$ (c) $\frac{1}{4}$ (d) $\frac{\sqrt{17}}{4}$

(e) $\sqrt{17}$ (f) 4 (g) $\frac{8}{17}$ (h) $\frac{2\sqrt{17}}{17}$

47. $\sin 75^\circ = \frac{\sqrt{2 + \sqrt{3}}}{2}$

49. $\sin 67^\circ 30' = \frac{\sqrt{2 + \sqrt{2}}}{2}$

$\cos 75^\circ = \frac{\sqrt{2 - \sqrt{3}}}{2}$

$\cos 67^\circ 30' = \frac{\sqrt{2 - \sqrt{2}}}{2}$

$\tan 75^\circ = \frac{\sqrt{3 + 2}}{2}$

$\tan 67^\circ 30' = 1 + \sqrt{2}$

51. $\sin \frac{\pi}{8} = \frac{\sqrt{2 - \sqrt{2}}}{2}$

53. $\sin \frac{3\pi}{8} = \frac{\sqrt{2 + \sqrt{2}}}{2}$

$\cos \frac{\pi}{8} = \frac{\sqrt{2 + \sqrt{2}}}{2}$

$\cos \frac{3\pi}{8} = \frac{\sqrt{2 - \sqrt{2}}}{2}$

$\tan \frac{\pi}{8} = \sqrt{2} - 1$

$\tan \frac{3\pi}{8} = \sqrt{2} + 1$

55. $\sin \frac{u}{2} = \frac{5\sqrt{26}}{26}$

57. $\sin \frac{u}{2} = \sqrt{\frac{89 - 5\sqrt{89}}{178}}$

$\cos \frac{u}{2} = \frac{\sqrt{26}}{26}$

$\cos \frac{u}{2} = -\sqrt{\frac{89 + 5\sqrt{89}}{178}}$

$\tan \frac{u}{2} = 5$

$\tan \frac{u}{2} = \frac{5 - \sqrt{89}}{8}$

59. $\sin \frac{u}{2} = \frac{3\sqrt{10}}{10}$

$\cos \frac{u}{2} = -\frac{\sqrt{10}}{10}$

$\tan \frac{u}{2} = -3$

61. $|\sin 3x|$ 63. $-\tan 4x$ 65. π

67. $\frac{\pi}{3}$, π , $\frac{5\pi}{3}$ 69. $3\left(\sin \frac{2\pi}{3} + \sin 0\right)$

71. $\frac{1}{2}(\sin 8\theta + \sin 2\theta)$ 73. $5(\cos 60^\circ + \cos 90^\circ)$

75. $\frac{1}{2}(\cos 2y - \cos 2x)$ 77. $2 \cos 3\theta \sin 2\theta$

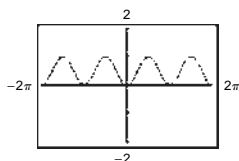
79. $2 \cos 4x \cos 2x$ 81. $2 \cos \alpha \sin \beta$

83. $-2 \sin \theta \sin \frac{\pi}{2}$ 85. $\frac{\sqrt{2}}{2}$ 87. $\frac{\sqrt{6}}{2}$

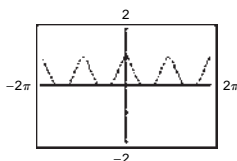
89. 0, $\frac{\pi}{4}$, $\frac{\pi}{2}$, $\frac{3\pi}{4}$, π , $\frac{5\pi}{4}$, $\frac{3\pi}{2}$, $\frac{7\pi}{4}$ 91. $\frac{\pi}{6}$, $\frac{5\pi}{6}$

93. $\frac{25}{169}$ 95. $\frac{4}{13}$ 97-109. Answers will vary.

111. $\frac{1 - \cos 2x}{2}$



113. $\frac{3 + 4 \cos 2x + \cos 4x}{8}$



115. $2x\sqrt{1-x^2}$ 117. $1 - 2x^2$ 119. $\frac{1-x^2}{1+x^2}$

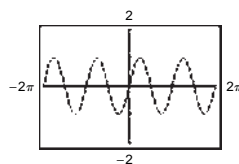
121. (a) $x = 0, \frac{\pi}{3}, \pi, \frac{5\pi}{3}, 2\pi$

(b) $x = \arccos \frac{1 \pm \sqrt{33}}{8}, 2\pi - \arccos \frac{1 \pm \sqrt{33}}{8}$

123. 23.85° 125. $x = 2r(1 - \cos \theta)$

127. False. $\sin \frac{x}{2} = -\sqrt{\frac{1 - \cos x}{2}}$ for $\pi \leq \frac{x}{2} \leq 2\pi$.

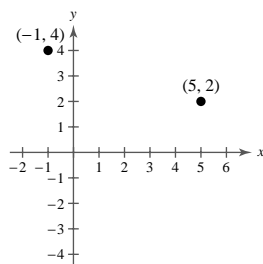
129. (a)



(b) $y = \sin 2x$

(c) Answers will vary.

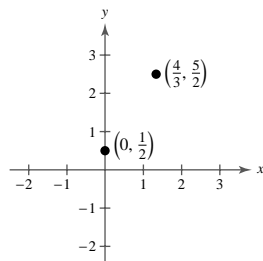
131. (a)



(b) $2\sqrt{10}$

(c) $(2, 3)$

133. (a)



(b) $\frac{2\sqrt{13}}{3}$ (c) $(\frac{2}{3}, \frac{3}{2})$

135. (a) Complement: 35° ; supplement: 125°

(b) Complement: none; supplement: 18°

137. (a) Complement: $\frac{4\pi}{9}$; supplement: $\frac{17\pi}{18}$

(b) Complement: $\frac{\pi}{20}$; supplement: $\frac{11\pi}{20}$

139. 0.4667 rad

Review Exercises (page 396)

1. $\sec x$ 3. $\cos x$ 5. $|\sin x|$

7. $\sec x$ 9. $\sec x$

11. $\tan x = \frac{4}{3}$

$\csc x = \frac{5}{4}$

$\sec x = \frac{5}{3}$

$\cot x = \frac{3}{4}$

13. $\cos x = \frac{\sqrt{2}}{2}$

$\tan x = -1$

$\csc x = -\sqrt{2}$

$\sec x = \sqrt{2}$

$\cot x = -1$

15. $\cos^2 x$ 17. $\csc \theta$ 19. 1 21. $\csc x$

23. $1 + \cot \alpha$ 25–37. Answers will vary.

39. $\frac{\pi}{6} + 2n\pi, \frac{5\pi}{6} + 2n\pi$ 41. $\frac{\pi}{3} + 2n\pi, \frac{2\pi}{3} + 2n\pi$

43. $\frac{\pi}{6} + n\pi$ 45. $\frac{\pi}{3} + n\pi, \frac{2\pi}{3} + n\pi$

47. $\frac{\pi}{6} + n\pi, \frac{5\pi}{6} + n\pi$ 49. $n\pi$ 51. $0, \frac{2\pi}{3}, \frac{4\pi}{3}$

53. $0, \frac{\pi}{2}, \pi$ 55. $\frac{\pi}{8}, \frac{3\pi}{8}, \frac{9\pi}{8}, \frac{11\pi}{8}$

57. $0, \frac{\pi}{8}, \frac{3\pi}{8}, \frac{5\pi}{8}, \frac{7\pi}{8}, \frac{9\pi}{8}, \frac{11\pi}{8}, \frac{13\pi}{8}, \frac{15\pi}{8}$

59. $\frac{\pi}{12} + n\pi, \frac{5\pi}{12} + n\pi$ 61. $\frac{\pi}{12} + \frac{n\pi}{6}$ 63. $0, \pi$

65. $\arctan(-4) + \pi, \arctan 3, \arctan(-4) + 2\pi, \arctan 3 + \pi$

67. $\sin 285^\circ = -\frac{\sqrt{2} + \sqrt{6}}{4}$ 69. $\sin \frac{31\pi}{12} = \frac{\sqrt{2} + \sqrt{6}}{4}$

$\cos 285^\circ = \frac{\sqrt{6} - \sqrt{2}}{4}$ $\cos \frac{31\pi}{12} = \frac{\sqrt{2} - \sqrt{6}}{4}$

$\tan 285^\circ = -2 - \sqrt{3}$ $\tan \frac{31\pi}{12} = -2 - \sqrt{3}$

71. $\sin 180^\circ$ 73. $\tan 75^\circ$ 75. $-\frac{4}{5}$ 77. $\frac{44}{117}$

79. $-\frac{3}{5}$ 81–85. Answers will vary. 87. $\frac{\pi}{4}, \frac{7\pi}{4}$

89. $\sin 2u = \frac{20\sqrt{6}}{49}$

91. $\sin 2u = -\frac{36}{85}$

$\cos 2u = -\frac{1}{49}$

$\cos 2u = \frac{77}{85}$

$\tan 2u = -20\sqrt{6}$

$\tan 2u = -\frac{36}{77}$

93 and 95. Answers will vary. 97. $15^\circ, 75^\circ$

99. $\frac{1}{32}(10 - 15 \cos 2x + 6 \cos 4x - \cos 6x)$

101. $\frac{1}{8}(3 + 4 \cos 4x + \cos 8x)$ 103. $\frac{1 - \cos 8x}{1 + \cos 8x}$

105. $\sin 15^\circ = \frac{\sqrt{2} - \sqrt{3}}{2}$

107. $\sin \frac{7\pi}{8} = \frac{\sqrt{2} - \sqrt{2}}{2}$

$\cos 15^\circ = \frac{\sqrt{2} + \sqrt{3}}{2}$

$\cos \frac{7\pi}{8} = -\frac{\sqrt{2} + \sqrt{2}}{2}$

$\tan 15^\circ = 2 - \sqrt{3}$

$\tan \frac{7\pi}{8} = 1 - \sqrt{2}$

109. $\sin \frac{u}{2} = \frac{\sqrt{10}}{10}$

111. $\sin \frac{u}{2} = \frac{3\sqrt{14}}{14}$

$\cos \frac{u}{2} = \frac{3\sqrt{10}}{10}$

$\cos \frac{u}{2} = \frac{\sqrt{70}}{14}$

$\tan \frac{u}{2} = \frac{1}{3}$

$\tan \frac{u}{2} = \frac{3\sqrt{5}}{5}$

113. $-|\cos 4x|$ 115. $\tan 5x$ 117. $V = \sin \frac{\theta}{2} \cos \frac{\theta}{2} \text{ m}^3$

119. $3\left(\sin \frac{\pi}{2} + \sin 0\right)$ 121. $\frac{1}{2}(\cos \alpha - \cos 9\alpha)$

123. $2 \cos\left(\frac{9\theta}{2}\right) \cos\left(\frac{\theta}{2}\right)$ 125. $2 \cos x \sin \frac{\pi}{4}$

127. $y = \frac{1}{2}\sqrt{10} \sin(8t - \arctan \frac{1}{3})$

129. $\frac{\sqrt{10}}{2}$ ft 131. False. $\cos \frac{\theta}{2} > 0$

133. True. Answers will vary. 135. Answers will vary.

137. No. $\sin \theta = \frac{1}{2}$ has an infinite number of solutions but is not an identity.

139. $y_3 = y_2 + 1$

Chapter Test (page 399)

1. $\sin \theta = \frac{-3\sqrt{13}}{13}$ 2. 1 3. 1

$$\cos \theta = \frac{-2\sqrt{13}}{13}$$

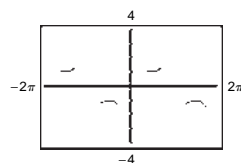
$$\csc \theta = \frac{-\sqrt{13}}{3}$$

$$\sec \theta = \frac{-\sqrt{13}}{2}$$

$$\cot \theta = \frac{2}{3}$$

4. $\csc \theta \sec \theta$ 5. $0, \frac{\pi}{2} < \theta \leq \pi, \frac{3\pi}{2} < \theta < 2\pi$

6. $y_1 = y_2$


7–12. Answers will vary. 13. $\sqrt{3} + 2$

14. $\frac{1}{16} \left(\frac{10 - 15 \cos 2x + 6 \cos 4x - \cos 6x}{1 + \cos 2x} \right)$

15. $\tan 2\theta$ 16. $2(\sin 6\theta + \sin 2\theta)$

17. $-2 \cos \frac{7\theta}{2} \sin \frac{\theta}{2}$ 18. $0, \frac{3\pi}{4}, \pi, \frac{7\pi}{4}$

19. $\frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{3\pi}{2}$ 20. $\frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$

21. $\frac{\pi}{6}, \frac{5\pi}{6}, \frac{3\pi}{2}$ 22. $-2.938, -2.663, 1.170$

23. $\sin 2u = \frac{4}{5}$
 $\cos 2u = -\frac{3}{5}$
 $\tan 2u = -\frac{4}{3}$ 24. 76.52°

Chapter 6

Section 6.1 (page 410)

1. oblique 3. $\frac{1}{2}bc \sin A; \frac{1}{2}ab \sin C; \frac{1}{2}ac \sin B$

5. AAS (or ASA) and SSA

7. $C = 95^\circ, b \approx 24.59$ in., $c \approx 28.29$ in.

9. $A = 40^\circ, a \approx 15.69$ cm, $b \approx 6.32$ cm

11. $C = 74^\circ 15', a \approx 6.41$ km, $c \approx 6.26$ km

13. $B \approx 21.55^\circ, C \approx 122.45^\circ, c \approx 11.49$

15. $B = 60.9^\circ, b \approx 19.32, c \approx 6.36$

17. $B \approx 18^\circ 13', C \approx 51^\circ 32', c \approx 40.05$

19. $B \approx 48.74^\circ, C \approx 21.26^\circ, c \approx 48.23$

21. $A = 48^\circ, b \approx 2.29, c \approx 4.73$

23. $A = 35^\circ, a \approx 36.50, b \approx 11.05$

25. $A \approx 44^\circ 14', B \approx 50^\circ 26', b \approx 38.67$ 27. No solution

29. Two solutions

$B \approx 72.21^\circ, C \approx 49.79^\circ, c \approx 10.27$

$B \approx 107.79^\circ, C \approx 14.21^\circ, c \approx 3.30$

31. Given: $A = 36^\circ, a = 5$

(a) One solution if $b \leq 5$ or $b = \frac{5}{\sin 36^\circ}$.

(b) Two solutions if $5 < b < \frac{5}{\sin 36^\circ}$.

(c) No solution if $b > \frac{5}{\sin 36^\circ}$.

33. Given: $A = 10^\circ, a = 10.8$

(a) One solution if $b \leq 10.8$ or $b = \frac{10.8}{\sin 10^\circ}$.

(b) Two solutions if $10.8 < b < \frac{10.8}{\sin 10^\circ}$.

(c) No solution if $b > \frac{10.8}{\sin 10^\circ}$.

35. 28.19 square units

37. 1782.32 square units

39. 2888.57 square units

41. (a) (b) $\frac{16}{\sin 70^\circ} = \frac{h}{\sin 34^\circ}$
(c) 9.52 m

43. 240.03°

45. 15.53 km from Colt Station; 42.43 km from Pine Knob

47. $\theta \approx 16.08^\circ$

49. (a) $\alpha \approx 5.36^\circ$

(b) $\beta = \arcsin\left(\frac{d \sin \theta}{58.36}\right)$ (c) $d = \sin(84.64 - \theta) \left[\frac{58.36}{\sin \theta} \right]$

(d)

θ	10°	20°	30°	40°	50°	60°
d	324.08	154.19	95.19	63.80	43.30	28.10

51. False. The triangle cannot be solved if only three angles are known.

53. False. AAS and ASA cases have unique solutions.

55. (a) Answers will vary; Sample answer: $b = 4$

(b) Answers will vary; Sample answer: $b = 7$

(c) Answers will vary; Sample answer: $b = 10$

57. $\tan \theta = -\frac{12}{5}, \csc \theta = -\frac{13}{12}, \sec \theta = \frac{13}{5}, \cot \theta = -\frac{5}{12}$

59. $3(\sin 11\theta + \sin 5\theta)$ 61. $\frac{3}{2} \left(\sin \frac{11\pi}{6} + \sin \frac{3\pi}{2} \right)$

Section 6.2 (page 417)

1. $c^2 = a^2 + b^2 - 2ab \cos C$ 3. No 5. Yes

7. $A \approx 40.80^\circ, B \approx 60.61^\circ, C \approx 78.59^\circ$

9. $A \approx 49.51^\circ, B \approx 55.40^\circ, C \approx 75.09^\circ$

11. $A \approx 31.40^\circ, C \approx 128.60^\circ, b \approx 6.56$ mm

13. $A \approx 26.38^\circ, B \approx 36.34^\circ, C \approx 117.28^\circ$

15. $B \approx 29.44^\circ, C \approx 100.56^\circ, a \approx 23.38$

17. $A \approx 36.87^\circ, B \approx 53.13^\circ, C = 90^\circ$

19. $A \approx 103.52^\circ, B \approx 38.24^\circ, C \approx 38.24^\circ$

21. $A \approx 154^\circ 14', C \approx 17^\circ 31', b \approx 8.58$

23. $A \approx 37^\circ 6' 7'', C \approx 67^\circ 33' 53'', b \approx 9.94$

	a	b	c	d	θ	ϕ
25.	4	8	11.64	4.96	30°	150°
27.	10	14	20	13.86	68.20°	111.80°
29.	15	16.96	25	20	77.22°	102.78°

31. Law of Cosines; $A \approx 102.44^\circ, C \approx 37.56^\circ, b \approx 5.26$

33. Law of Sines; no solution

35. Law of Sines; $C = 103^\circ, a \approx 0.82, b \approx 0.71$ 37. 104.57

39. 19.81 41. 0.27 ft^2 43. 15.52 45. 35.19

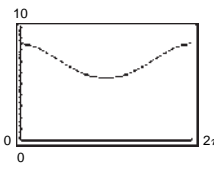
47. 483.40 m 49. (a) $N 59.7^\circ E$ (b) $N 72.8^\circ E$

51. 72.28° 53. $PQ \approx 9.43, QS = 5, RS \approx 12.81$

55. $18,617.66 \text{ ft}^2$

57. (a) $49 = 2.25 + x^2 - 3x \cos \theta$

(b) $x = \frac{1}{2}(3 \cos \theta + \sqrt{9 \cos^2 \theta + 187})$

(c)  (d) 6 in.

59. True 61. Proof

63. To solve the triangle using the Law of Cosines, substitute values into $a^2 = b^2 + c^2 - 2bc \cos A$.

Simplify the equation so that you have a quadratic equation in terms of c . Then, find the two values of c , and find the two triangles that model the given information.

Using the Law of Sines will give the same result as using the Law of Cosines.

Sample answer: An advantage of using the Law of Cosines is that it is easier to choose the correct value to avoid the ambiguous case, but its disadvantage is that there are more computations. The opposite is true for the Law of Sines.

65. Proof 67. $-\frac{\pi}{2}$ 69. $\frac{\pi}{3}$

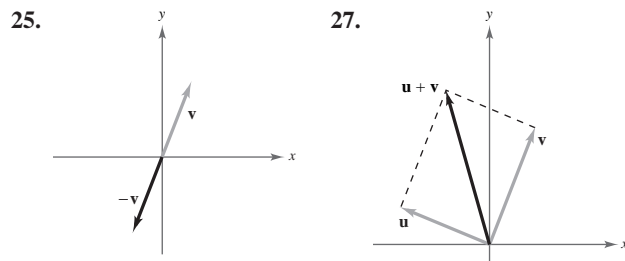
Section 6.3 (page 429)

1. directed line segment 3. magnitude
5. standard position 7. resultant
9. magnitude and direction 11. Answers will vary.

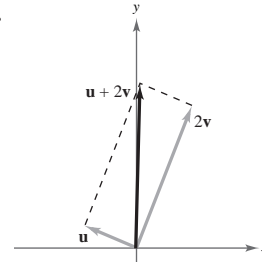
13. $\langle 1, 3 \rangle, \|\mathbf{v}\| = \sqrt{10}$ 15. $\langle -3, 2 \rangle, \|\mathbf{v}\| = \sqrt{13}$

17. $\langle 0, 5 \rangle, \|\mathbf{v}\| = 5$ 19. $\langle 8, 6 \rangle, \|\mathbf{v}\| = 10$

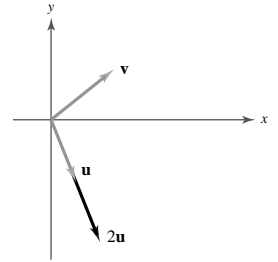
21. $\langle \frac{3}{5}, -\frac{3}{5} \rangle, \|\mathbf{v}\| = \frac{3\sqrt{2}}{5}$ 23. $\langle \frac{7}{6}, \frac{9}{5} \rangle, \|\mathbf{v}\| = \frac{\sqrt{4141}}{30}$



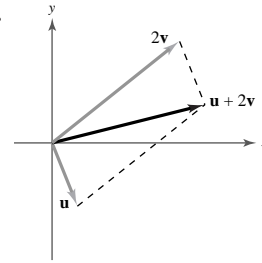
29.



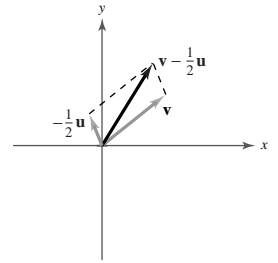
31.



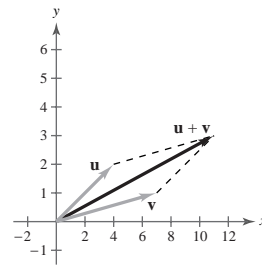
33.



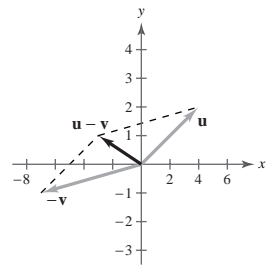
35.



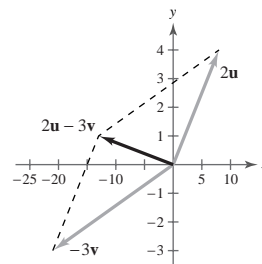
37. (a) $\langle 11, 3 \rangle$



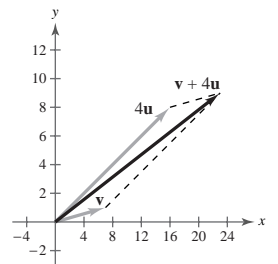
(b) $\langle -3, 1 \rangle$



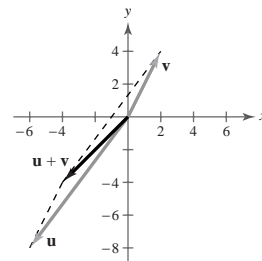
(c) $\langle -13, 1 \rangle$



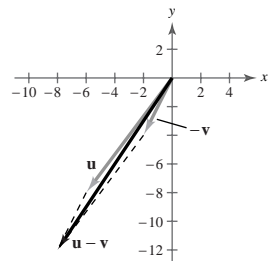
(d) $\langle 23, 9 \rangle$



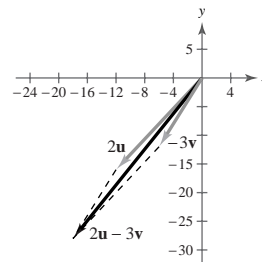
39. (a) $\langle -4, -4 \rangle$



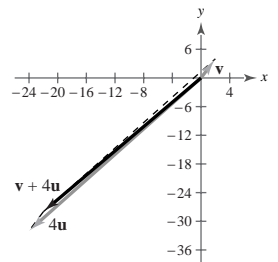
(b) $\langle -8, -12 \rangle$



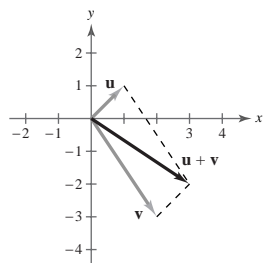
(c) $\langle -18, -28 \rangle$



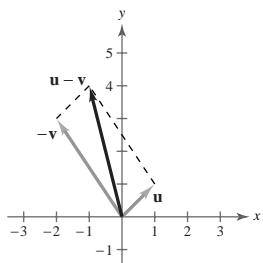
(d) $\langle -22, -28 \rangle$



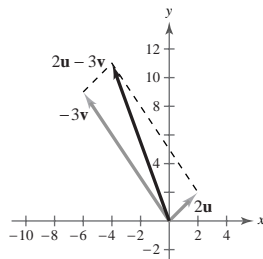
41. (a) $3\mathbf{i} - 2\mathbf{j}$



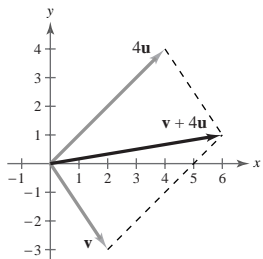
(b) $-\mathbf{i} + 4\mathbf{j}$



(c) $-4\mathbf{i} + 11\mathbf{j}$



(d) $6\mathbf{i} + \mathbf{j}$



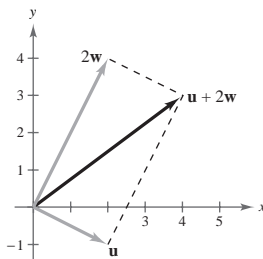
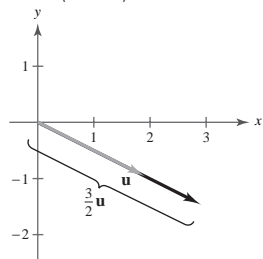
43. $\mathbf{u} + \mathbf{v}$ 45. $\mathbf{w} - \mathbf{v}$ 47. $\langle 1, 0 \rangle$

49. $\left\langle -\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} \right\rangle$ 51. $\left\langle -\frac{24}{25}, -\frac{7}{25} \right\rangle$ 53. $\frac{4}{5}\mathbf{i} - \frac{3}{5}\mathbf{j}$

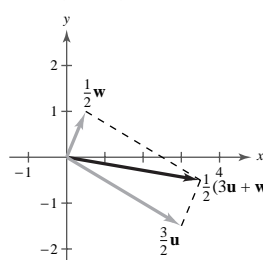
55. \mathbf{j} 57. $\frac{40\sqrt{61}}{61}\mathbf{i} + \frac{48\sqrt{61}}{61}\mathbf{j}$ 59. $\frac{21}{5}\mathbf{i} + \frac{28}{5}\mathbf{j}$

61. $-8\mathbf{i}$ 63. $7\mathbf{i} + 4\mathbf{j}$ 65. $3\mathbf{i} + 8\mathbf{j}$

67. $\mathbf{v} = \langle 3, -\frac{3}{2} \rangle$ 69. $\mathbf{v} = \langle 4, 3 \rangle$



71. $\mathbf{v} = \left\langle \frac{7}{2}, -\frac{1}{2} \right\rangle$

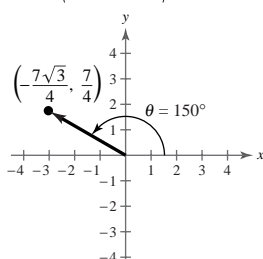
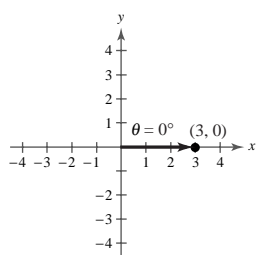


73. $\|\mathbf{v}\| = 5, \theta = 30^\circ$

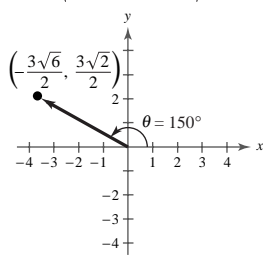


75. $\|\mathbf{v}\| = 6\sqrt{2}, \theta = 315^\circ$ 77. $\|\mathbf{v}\| = \sqrt{29}, \theta \approx 111.80^\circ$

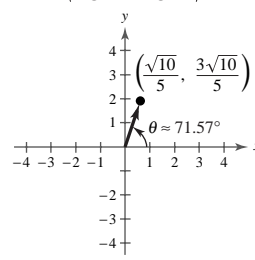
79. $\mathbf{v} = \langle 3, 0 \rangle$ 81. $\mathbf{v} = \left\langle -\frac{7\sqrt{3}}{4}, \frac{7}{4} \right\rangle$



83. $\mathbf{v} = \left\langle -\frac{3\sqrt{6}}{2}, \frac{3\sqrt{2}}{2} \right\rangle$



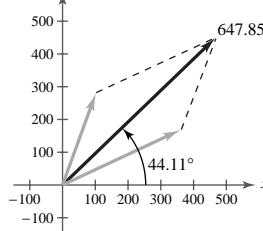
85. $\mathbf{v} = \left\langle \frac{\sqrt{10}}{5}, \frac{3\sqrt{10}}{5} \right\rangle$



87. $\left\langle \frac{5}{2}, \frac{10 + 5\sqrt{3}}{2} \right\rangle$

89. $\langle 10\sqrt{2} - 25\sqrt{3}, 25 + 10\sqrt{2} \rangle$ 91. 90°

93. 95. 62.72°



$\|\mathbf{v}\| \approx 647.85, \theta \approx 44.11^\circ$

97. Horizontal component: about 53.62 ft/sec

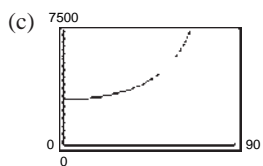
Vertical component: about 45.00 ft/sec

99. $T_{AC} \approx 3611.1$ lb, $T_{BC} \approx 2169.5$ lb

101. (a) $T = 3000 \sec \theta$; Domain: $0^\circ \leq \theta < 90^\circ$

θ	10°	20°	30°
T	3046.28	3192.53	3464.10

θ	40°	50°	60°
T	3916.22	4667.17	6000



(d) The component in the direction of the motion of the barge decreases.

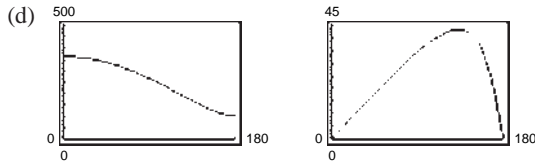
103. (a) $12.10^\circ, 357.85$ N

(b) $M = 10\sqrt{660 \cos \theta + 709}$

$$\alpha = \arctan \frac{15 \sin \theta}{15 \cos \theta + 22}$$

θ	0°	30°	60°	90°
M	370	357.85	322.34	266.27
α	0°	12.10°	23.77°	34.29°

θ	120°	150°	180°
M	194.68	117.23	70
α	41.86°	39.78°	0°



(e) For increasing θ , the two vectors tend to work against each other, resulting in a decrease in the magnitude of the resultant.

105. N 26.67° E, 130.35 km/h 107. True by definition

109. True. $a = b = 0$

111. True. The magnitudes are equal and the directions are opposite.

113. True. $\mathbf{a} - \mathbf{b} = \mathbf{c}$ and $\mathbf{u} = -\mathbf{b}$

115. True. $\mathbf{a} = -\mathbf{d}$, $\mathbf{w} = -\mathbf{d}$

117. False. $\mathbf{u} - \mathbf{v} = -(\mathbf{b} + \mathbf{t})$

119. (a) 0°

(b) 180°

(c) No. The magnitude is equal to the sum when the angle between the vectors is 0°.

121. Proof 123. Answers will vary.

125. $\langle 1, 3 \rangle$ or $\langle -1, -3 \rangle$ 127. $12x^3y^7$, $x \neq 0$, $y \neq 0$

129. $48xy^2$, $x \neq 0$ 131. 7.14×10^5

133. $\frac{\pi}{2} + n\pi$, $\pi + 2n\pi$ 135. $\frac{\pi}{3} + 2n\pi$, $\frac{5\pi}{3} + 2n\pi$

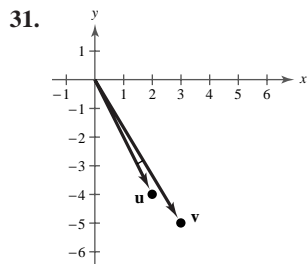
Section 6.4 (page 440)

1. Yes 3. scalar 5. $\left(\frac{\mathbf{u} \cdot \mathbf{v}}{\|\mathbf{v}\|^2}\right)\mathbf{v}$ 7. 0 9. 14

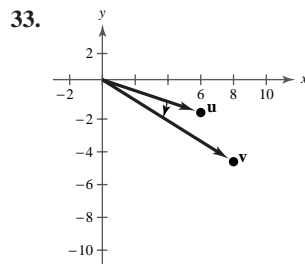
11. 8, scalar 13. 4, scalar 15. $\langle -114, -114 \rangle$, vector

17. 13 19. $5\sqrt{41}$ 21. 4 23. 90° 25. 70.56°

27. 90° 29. $\frac{5\pi}{12}$



$\theta \approx 4.40^\circ$



$\theta \approx 13.57^\circ$

35. 26.57°, 63.43°, 90° 37. 41.63°, 53.13°, 85.24°

39. $-162\sqrt{2}$ 41. -20 43. Orthogonal

45. Not orthogonal 47. Neither 49. Parallel

51. 3 53. 10 55. 0

57. $\frac{16}{17}\langle 4, 1 \rangle$, $\mathbf{u} = \left\langle \frac{64}{17}, \frac{16}{17} \right\rangle + \left\langle -\frac{13}{17}, \frac{52}{17} \right\rangle$

59. $\frac{45}{229}\langle 2, 15 \rangle$, $\mathbf{u} = \left\langle \frac{90}{229}, \frac{675}{229} \right\rangle + \left\langle -\frac{90}{229}, \frac{12}{229} \right\rangle$ 61. \mathbf{u} 63. 0

65. $\langle 3, -1 \rangle$, $\langle -3, 1 \rangle$ 67. $-\frac{3}{4}\mathbf{i} - \frac{1}{2}\mathbf{j}$, $\frac{3}{4}\mathbf{i} + \frac{1}{2}\mathbf{j}$ 69. 32

71. (a) 35,727.50; It is the total dollar amount paid to the employees.

(b) Multiply \mathbf{v} by 1.02.

73. (a) Force = 30,000 sin d

d	0°	1°	2°	3°	4°
Force	0	523.57	1046.98	1570.08	2092.69

d	5°	6°	7°	8°
Force	2614.67	3135.85	3656.08	4175.19

d	9°	10°
Force	4693.03	5209.45

(c) 29,885.84 lb

75. (a) Work = 125 $\sqrt{3}d$

d	25	50	100
Work	5412.66	10,825.32	21,650.64

77. 10,282,651.78 N-m

79. True. The zero vector is orthogonal to every vector.

81. Orthogonal. $\mathbf{u} \cdot \mathbf{v} = 0$

83. 1. The angle between \mathbf{u} and itself is 0. Then, using the equation

$$\cos \theta = \frac{\mathbf{u} \cdot \mathbf{u}}{\|\mathbf{u}\| \|\mathbf{u}\|}$$

and substituting 0 for θ , you see that $\cos 0 = 1$.

85. (a) \mathbf{u} and \mathbf{v} are parallel. (b) \mathbf{u} and \mathbf{v} are orthogonal.

87 and 89. Proofs

91. g is a horizontal shift of f four units to the right.

93. g is a vertical shift of f six units upward.

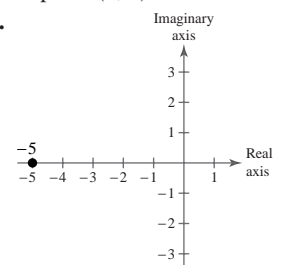
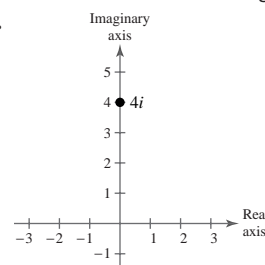
95. $15 + 12i$ 97. 10 99. $\frac{47}{26} - \frac{27}{26}i$

Section 6.5 (page 452)

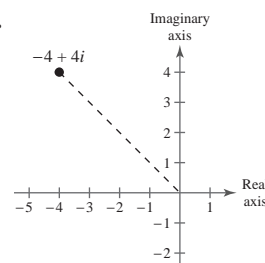
1. absolute value 3. n th root

5. The distance from the origin to the point (a, b)

7. 9.

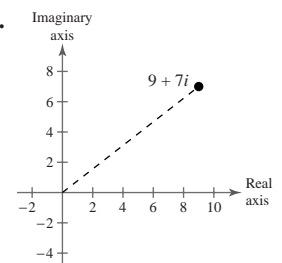


4 11.



$4\sqrt{2}$

5 13.



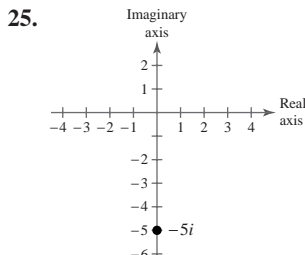
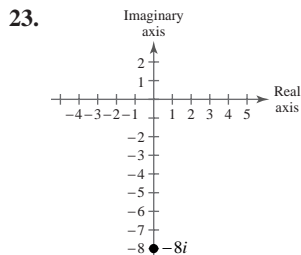
$\sqrt{130}$

15. $2\left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2}\right)$

17. $4(\cos \pi + i \sin \pi)$

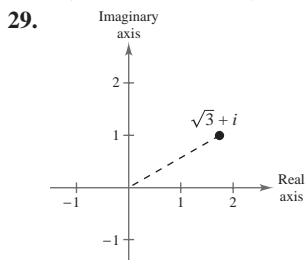
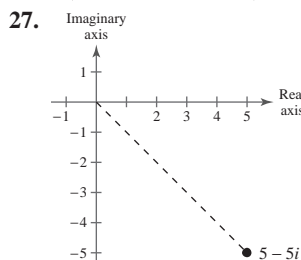
19. $3\sqrt{2}\left(\cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4}\right)$

21. $2\left(\cos \frac{11\pi}{6} + i \sin \frac{11\pi}{6}\right)$



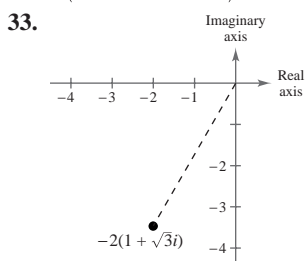
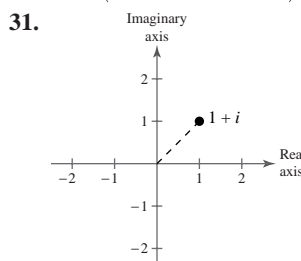
27. $8\left(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2}\right)$

29. $5\left(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2}\right)$



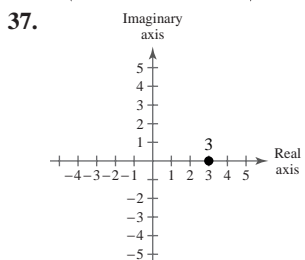
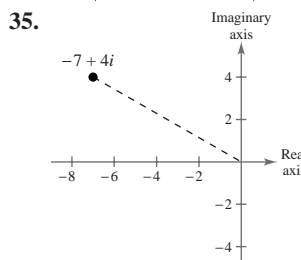
31. $5\sqrt{2}\left(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4}\right)$

33. $2\left(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6}\right)$



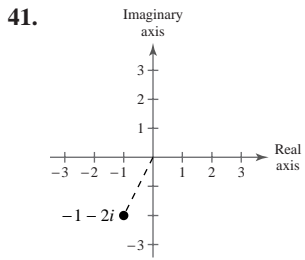
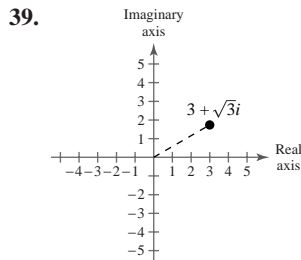
35. $\sqrt{2}\left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$

37. $4\left(\cos \frac{4\pi}{3} + i \sin \frac{4\pi}{3}\right)$



39. $\sqrt{65}(\cos 2.622 + i \sin 2.622)$

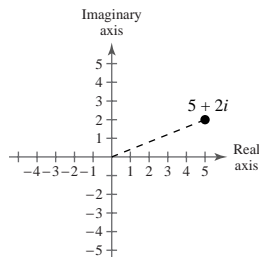
41. $3(\cos 0 + i \sin 0)$



$2\sqrt{3}\left(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6}\right)$

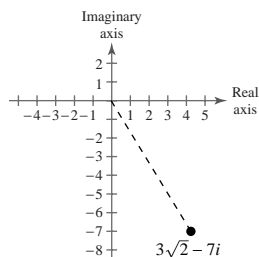
$\sqrt{5}(\cos 4.249 + i \sin 4.249)$

43.



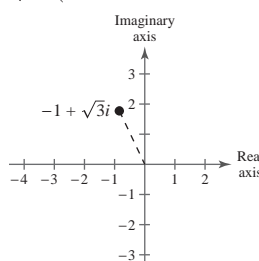
$\sqrt{29}(\cos 0.381 + i \sin 0.381)$

45.

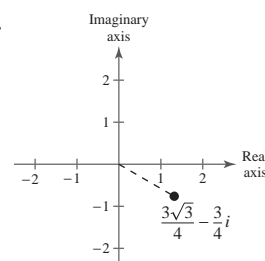


$\sqrt{67}(\cos 5.257 + i \sin 5.257)$

47.

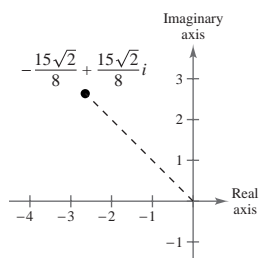


49.

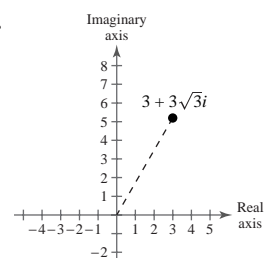


$-1 + \sqrt{3}i$

51.

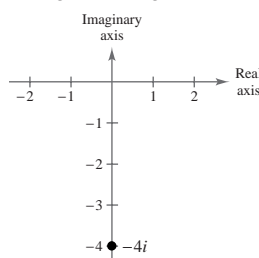


53.

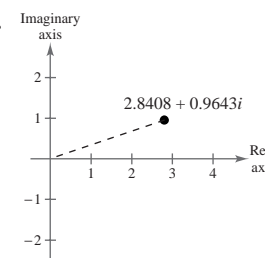


$-\frac{15\sqrt{2}}{8} + \frac{15\sqrt{2}}{8}i$

55.



57.

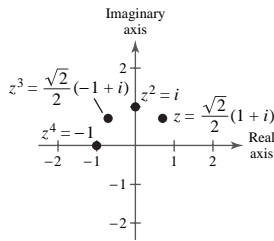


$-4i$

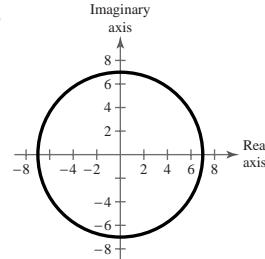
59. $4.6985 + 1.7101i$

61. $4.7693 + 7.6324i$

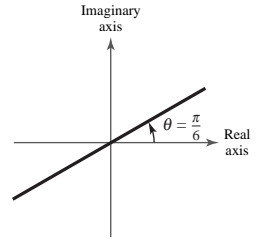
63.


 65. $10(\cos 0 + i \sin 0)$

99.



101.



The absolute value of each is 1.

 67. $6(\cos \pi + i \sin \pi)$ 69. $\frac{10}{9}(\cos 200^\circ + i \sin 200^\circ)$

 71. $\frac{11}{50}(\cos 130^\circ + i \sin 130^\circ)$ 73. $\cos 30^\circ + i \sin 30^\circ$

 75. $\frac{1}{2}(\cos 80^\circ + i \sin 80^\circ)$ 77. $6(\cos 312^\circ + i \sin 312^\circ)$

 79. (a) $2\sqrt{2}(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4})$ (b) and (c) 4

$$\sqrt{2}(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4})$$

 81. (a) $2\sqrt{2}(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4})$ (b) and (c) 4

$$\sqrt{2}(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4})$$

 83. (a) $2(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2})$ (b) and (c) $2 - 2i$

$$\sqrt{2}(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4})$$

 85. (a) $2(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2})$ (b) and (c) $-2 - 2\sqrt{3}i$

$$2(\cos \frac{11\pi}{6} + i \sin \frac{11\pi}{6})$$

 87. (a) $2(\cos 0 + i \sin 0)$ (b) and (c) $2 - 2i$

$$\sqrt{2}(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4})$$

 89. (a) $5(\cos 0.93 + i \sin 0.93)$

$$2(\cos \frac{5\pi}{3} + i \sin \frac{5\pi}{3})$$

$$(b) \text{ and } (c) \left(\frac{3}{4} - \sqrt{3}\right) + \left(\frac{3\sqrt{3}}{4} + 1\right)i$$

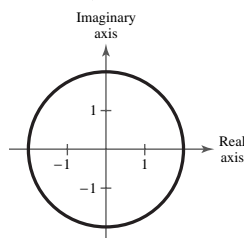
 91. (a) $5(\cos 0 + i \sin 0)$ (b) and (c) $\frac{5}{4} - \frac{5}{4}i$

$$2\sqrt{2}(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4})$$

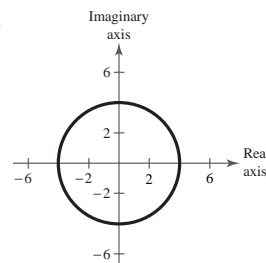
 93. (a) $4(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2})$ (b) and (c) $2 - 2i$

$$\sqrt{2}(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4})$$

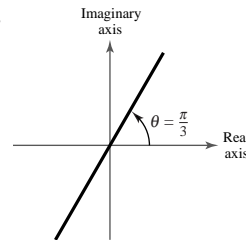
95.



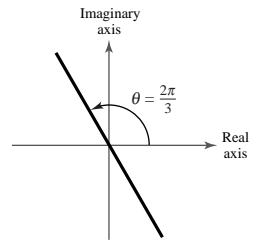
97.



103.



105.


 107. $-2 + 2i$ 109. $8i$ 111. $-32\sqrt{3} + 32i$

 113. $\frac{125}{2} + \frac{125\sqrt{3}}{2}i$ 115. i 117. $4.5386 - 15.3428i$

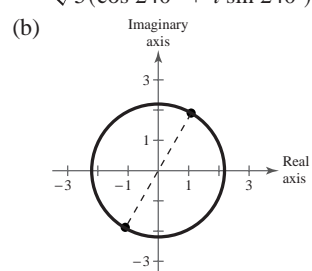
 119. 256 121. $-597 - 122i$ 123. $2048 + 2048\sqrt{3}i$

 125. $\frac{9\sqrt{2}}{2} + \frac{9\sqrt{2}}{2}i$ 127. Answers will vary.

 129. $1 + i, -1 - i$ 131. $-\frac{\sqrt{6}}{2} + \frac{\sqrt{6}}{2}i, \frac{\sqrt{6}}{2} - \frac{\sqrt{6}}{2}i$

 133. $-1.5538 + 0.6436i, 1.5538 - 0.6436i$

 135. $\frac{\sqrt{6}}{2} + \frac{\sqrt{2}}{2}i, -\frac{\sqrt{6}}{2} - \frac{\sqrt{2}}{2}i$

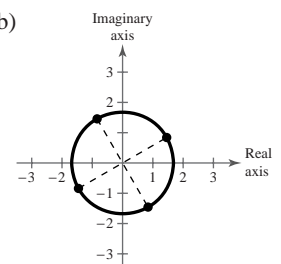
 137. (a) $\sqrt{5}(\cos 60^\circ + i \sin 60^\circ)$
 $\sqrt{5}(\cos 240^\circ + i \sin 240^\circ)$

 (c) $\frac{\sqrt{5}}{2} + \frac{\sqrt{15}}{2}i, -\frac{\sqrt{5}}{2} - \frac{\sqrt{15}}{2}i$

 139. (a) $\sqrt[4]{8}(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6})$ (b)

$$\sqrt[4]{8}(\cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3})$$

$$\sqrt[4]{8}(\cos \frac{7\pi}{6} + i \sin \frac{7\pi}{6})$$

$$\sqrt[4]{8}(\cos \frac{5\pi}{3} + i \sin \frac{5\pi}{3})$$

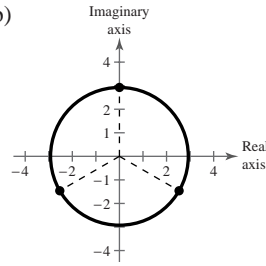
 (c) $1.4565 + 0.8409i$
 $-0.8409 + 1.4565i$
 $-1.4565 - 0.8409i$
 $0.8409 - 1.4565i$


141. (a) $\sqrt[3]{25}\left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2}\right)$ (b)

$$\sqrt[3]{25}\left(\cos \frac{7\pi}{6} + i \sin \frac{7\pi}{6}\right)$$

$$\sqrt[3]{25}\left(\cos \frac{11\pi}{6} + i \sin \frac{11\pi}{6}\right)$$

(c) $2.9240i$
 $-2.5323 - 1.4620i$
 $2.5323 - 1.4620i$

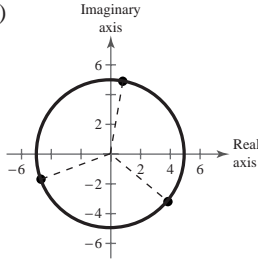


143. (a) $5\left(\cos \frac{4\pi}{9} + i \sin \frac{4\pi}{9}\right)$ (b)

$$5\left(\cos \frac{10\pi}{9} + i \sin \frac{10\pi}{9}\right)$$

$$5\left(\cos \frac{16\pi}{9} + i \sin \frac{16\pi}{9}\right)$$

(c) $0.8682 + 4.9240i$,
 $-4.6985 - 1.7101i$,
 $3.8302 - 3.2139i$

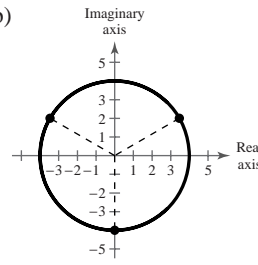


145. (a) $4\left(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6}\right)$ (b)

$$4\left(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6}\right)$$

$$4\left(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2}\right)$$

(c) $2\sqrt{3} + 2i$,
 $-2\sqrt{3} + 2i$, $-4i$



147. (a) $\cos 0 + i \sin 0$ (b)

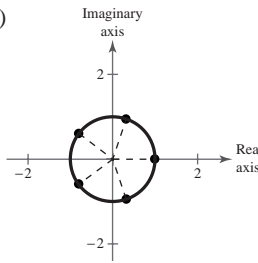
$$\cos \frac{2\pi}{5} + i \sin \frac{2\pi}{5}$$

$$\cos \frac{4\pi}{5} + i \sin \frac{4\pi}{5}$$

$$\cos \frac{6\pi}{5} + i \sin \frac{6\pi}{5}$$

$$\cos \frac{8\pi}{5} + i \sin \frac{8\pi}{5}$$

(c) $1, 0.3090 + 0.9511i, -0.8090 + 0.5878i$,
 $-0.8090 - 0.5878i, 0.3090 - 0.9511i$

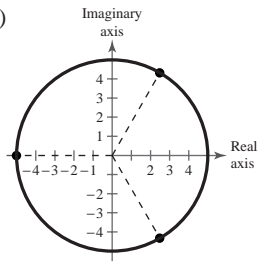


149. (a) $5\left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}\right)$ (b)

$$5(\cos \pi + i \sin \pi)$$

$$5\left(\cos \frac{5\pi}{3} + i \sin \frac{5\pi}{3}\right)$$

(c) $\frac{5}{2} + \frac{5\sqrt{3}}{2}i, -5$,
 $\frac{5}{2} - \frac{5\sqrt{3}}{2}i$



151. (a) $2\sqrt{2}\left(\cos \frac{3\pi}{20} + i \sin \frac{3\pi}{20}\right)$

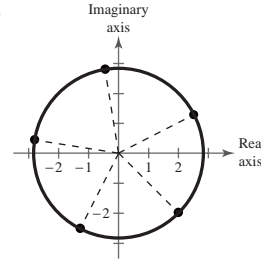
$$2\sqrt{2}\left(\cos \frac{11\pi}{20} + i \sin \frac{11\pi}{20}\right)$$

$$2\sqrt{2}\left(\cos \frac{19\pi}{20} + i \sin \frac{19\pi}{20}\right)$$

$$2\sqrt{2}\left(\cos \frac{27\pi}{20} + i \sin \frac{27\pi}{20}\right)$$

$$2\sqrt{2}\left(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4}\right)$$

(b)



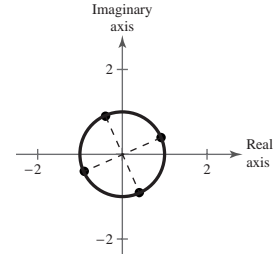
(c) $2.5201 + 1.2841i$,
 $-0.4425 + 2.7936i$,
 $-2.7936 + 0.4425i$,
 $-1.2841 - 2.5201i$,
 $2 - 2i$

153. $\cos \frac{\pi}{8} + i \sin \frac{\pi}{8}$

$$\cos \frac{5\pi}{8} + i \sin \frac{5\pi}{8}$$

$$\cos \frac{9\pi}{8} + i \sin \frac{9\pi}{8}$$

$$\cos \frac{13\pi}{8} + i \sin \frac{13\pi}{8}$$



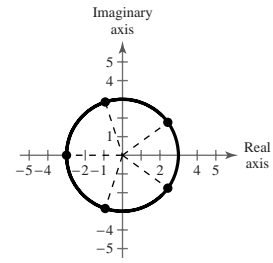
155. $3\left(\cos \frac{\pi}{5} + i \sin \frac{\pi}{5}\right)$

$$3\left(\cos \frac{3\pi}{5} + i \sin \frac{3\pi}{5}\right)$$

$$3(\cos \pi + i \sin \pi)$$

$$3\left(\cos \frac{7\pi}{5} + i \sin \frac{7\pi}{5}\right)$$

$$3\left(\cos \frac{9\pi}{5} + i \sin \frac{9\pi}{5}\right)$$

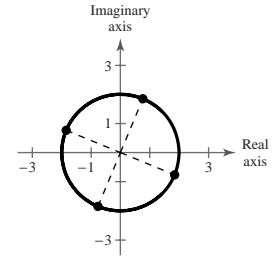


157. $2\left(\cos \frac{3\pi}{8} + i \sin \frac{3\pi}{8}\right)$

$$2\left(\cos \frac{7\pi}{8} + i \sin \frac{7\pi}{8}\right)$$

$$2\left(\cos \frac{11\pi}{8} + i \sin \frac{11\pi}{8}\right)$$

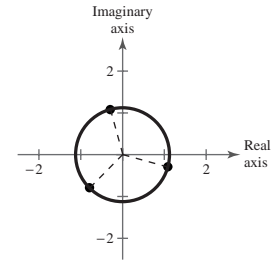
$$2\left(\cos \frac{15\pi}{8} + i \sin \frac{15\pi}{8}\right)$$



159. $\sqrt[6]{2}\left(\cos \frac{7\pi}{12} + i \sin \frac{7\pi}{12}\right)$

$$\sqrt[6]{2}\left(\cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4}\right)$$

$$\sqrt[6]{2}\left(\cos \frac{23\pi}{12} + i \sin \frac{23\pi}{12}\right)$$



161. $E = 34 + 38i$

163. $Z = \frac{3}{2} - \frac{1}{2}i$

165. $I = \frac{39}{34} + \frac{3}{34}i$

167. True. $\left[\frac{1}{2}(1 - \sqrt{3}i)\right]^9 = -1$

169. True. $z_1 z_2 = r_1 r_2 [\cos(\theta_1 + \theta_2) + i \sin(\theta_1 + \theta_2)] = 0$ if and only if $r_1 = 0$ and/or $r_2 = 0$.

171. Answers will vary.

173. (a) r^2

(b) $\cos 2\theta + i \sin 2\theta$

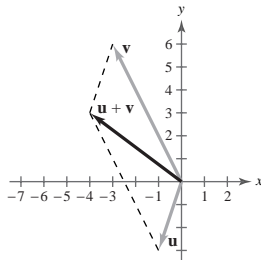
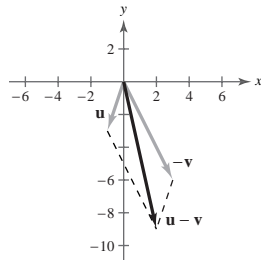
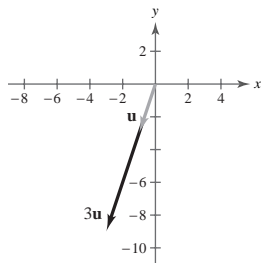
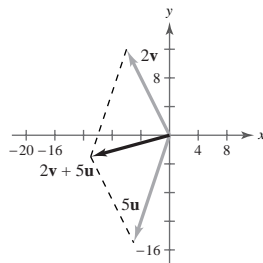
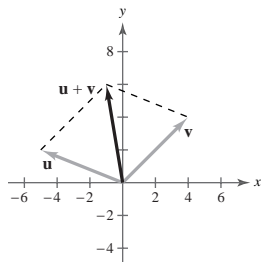
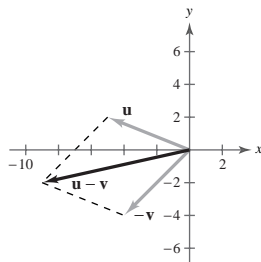
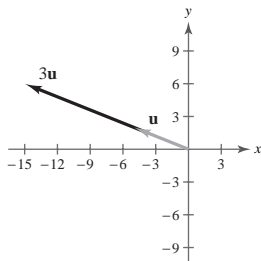
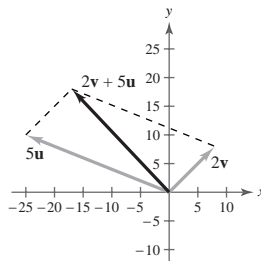
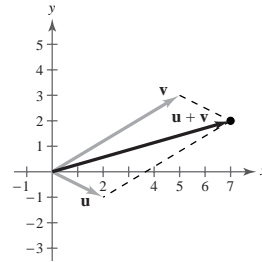
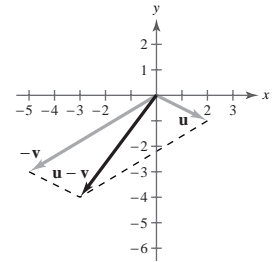
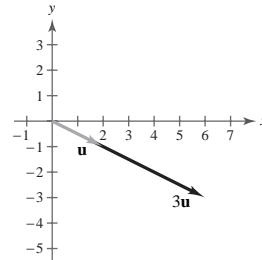
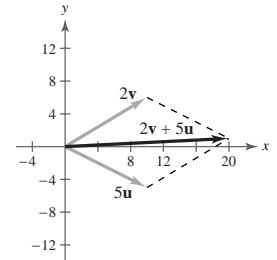
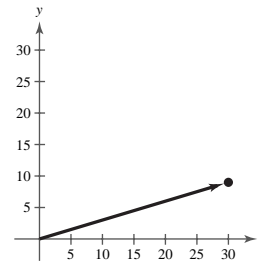
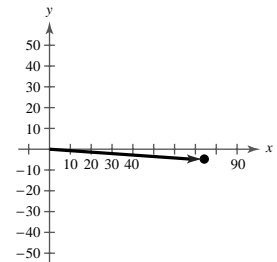
175. Answers will vary.

177. Maximum displacement: 16; $t = 2$

179. Maximum displacement: $\frac{1}{8}$; $t = \frac{1}{24}$

Review Exercises (page 458)

1. $C = 98^\circ$, $b \approx 23.13$, $c \approx 29.90$
3. $A = 50^\circ$, $a \approx 19.83$, $b \approx 10.94$
5. $C = 74^\circ 15'$, $a \approx 5.84$, $c \approx 6.48$
7. No solution
9. $A \approx 34.23^\circ$, $C \approx 30.77^\circ$, $c \approx 8.18$
11. 19.06
13. 221.34
15. 31.01 ft
17. $A \approx 27.81^\circ$, $B \approx 54.75^\circ$, $C \approx 97.44^\circ$
19. $A \approx 15.29^\circ$, $B \approx 20.59^\circ$, $C \approx 144.11^\circ$
21. $A \approx 13.19^\circ$, $B \approx 20.98^\circ$, $C \approx 145.83^\circ$
23. $A \approx 86.38^\circ$, $B \approx 28.62^\circ$, $c \approx 22.70$
25. 4.29 ft, 12.63 ft
27. 7.64 square units
29. 511.71 square units
31. $\langle 7, -5 \rangle$, $\|\mathbf{v}\| = \sqrt{74}$
33. $\langle 7, -7 \rangle$, $\|\mathbf{v}\| = 7\sqrt{2}$
35. (a) $\langle -4, 3 \rangle$


 (b) $\langle 2, -9 \rangle$

 (c) $\langle -3, -9 \rangle$

 (d) $\langle -11, -3 \rangle$

 37. (a) $\langle -1, 6 \rangle$

 (b) $\langle -9, -2 \rangle$

 (c) $\langle -15, 6 \rangle$

 (d) $\langle -17, 18 \rangle$

 39. (a) $7\mathbf{i} + 2\mathbf{j}$

 (b) $-3\mathbf{i} - 4\mathbf{j}$

 (c) $6\mathbf{i} - 3\mathbf{j}$

 (d) $20\mathbf{i} + \mathbf{j}$

 41. $\langle 30, 9 \rangle$

 43. $\langle 74, -5 \rangle$

 45. $\langle 0, -1 \rangle$

 47. $\frac{\sqrt{29}}{29} \langle 5, -2 \rangle$

 49. $9\mathbf{i} - 8\mathbf{j}$

 51. $\|\mathbf{v}\| = 7$; $\theta = 60^\circ$

 53. $\|\mathbf{v}\| = \sqrt{41}$; $\theta = 38.7^\circ$

 55. $\|\mathbf{v}\| = 3\sqrt{2}$; $\theta = 225^\circ$

 57. 133.92 lb, 5.55° from the 85-lb force

59. 115.47 lb

61. -20

63. 7

65. 25

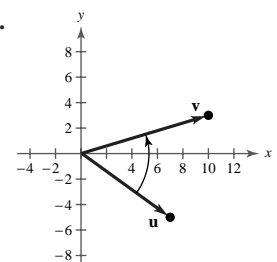
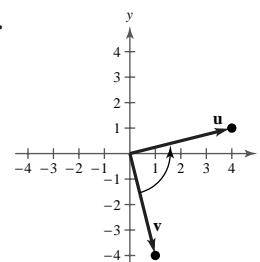
67. -40

69. 2.802

 71. $\frac{11\pi}{12}$

73.

75.



90°

52.2°

77. Parallel

79. Neither

 81. $\frac{1}{2}$

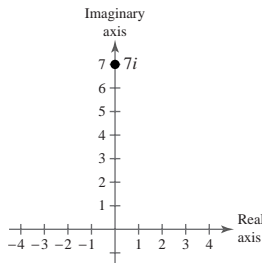
83. -1

 85. $\frac{13}{17} \langle -4, -1 \rangle$, $\langle -\frac{52}{17}, -\frac{13}{17} \rangle + \langle -\frac{16}{17}, \frac{64}{17} \rangle$

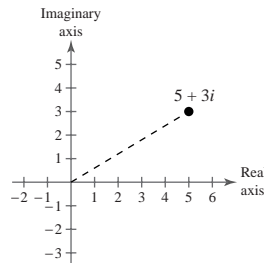
 87. $\frac{5}{2} \langle -1, 1 \rangle$, $\langle -\frac{5}{2}, \frac{5}{2} \rangle + \langle \frac{9}{2}, \frac{9}{2} \rangle$

89. 72,000 ft-lb

91.



93.



7

 $\sqrt{34}$

95. $2\sqrt{2}\left(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4}\right)$

97. $2\left(\cos \frac{7\pi}{6} + i \sin \frac{7\pi}{6}\right)$

99. $10\left(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}\right)$

101. $4(\cos 240^\circ + i \sin 240^\circ)$

103. (a) $2\sqrt{2}\left(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4}\right)$ (b) and (c) 12

$3\sqrt{2}\left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$

105. (a) $3\sqrt{2}\left(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4}\right)$ (b) and (c) $-\frac{3}{2}i$

$2\sqrt{2}\left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$

107. $\frac{625}{2} + \frac{625\sqrt{3}}{2}i$

109. $2035 - 828i$

111. $\pm(0.3660 + 1.3660i)$

113. $-1 + i, 1 - i$

115. (a) $3\left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$ (b)

$3\left(\cos \frac{7\pi}{12} + i \sin \frac{7\pi}{12}\right)$

$3\left(\cos \frac{11\pi}{12} + i \sin \frac{11\pi}{12}\right)$

$3\left(\cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4}\right)$

$3\left(\cos \frac{19\pi}{12} + i \sin \frac{19\pi}{12}\right)$

$3\left(\cos \frac{23\pi}{12} + i \sin \frac{23\pi}{12}\right)$

(c) $2.1213 + 2.1213i, -0.7765 + 2.8978i,$
 $-2.8978 + 0.7765i, -2.1213 - 2.1213i,$
 $0.7765 - 2.8978i, 2.8978 - 0.7765i$

117. (a) $2(\cos 0 + i \sin 0)$ (b)

$2\left(\cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3}\right)$

$2\left(\cos \frac{4\pi}{3} + i \sin \frac{4\pi}{3}\right)$

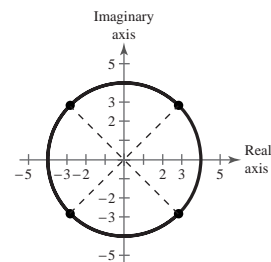
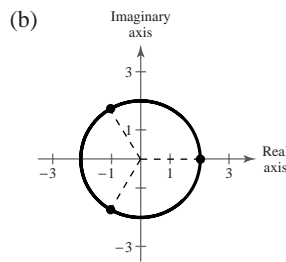
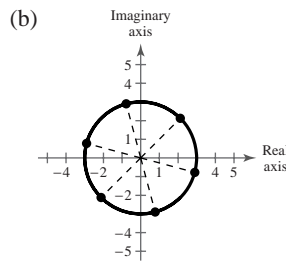
(c) $2, -1 + \sqrt{3}i,$
 $-1 - \sqrt{3}i$

119. $4\left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right)$

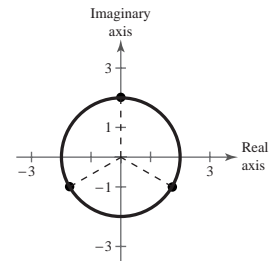
$4\left(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}\right)$

$4\left(\cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4}\right)$

$4\left(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4}\right)$



121. $2\left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2}\right)$
 $2\left(\cos \frac{7\pi}{6} + i \sin \frac{7\pi}{6}\right)$
 $2\left(\cos \frac{11\pi}{6} + i \sin \frac{11\pi}{6}\right)$


123. True. $\sin 90^\circ$ is defined in the Law of Sines.

Chapter Test (page 461)

1. $C = 46^\circ, a \approx 13.07, b \approx 22.03$

2. $A \approx 22.33^\circ, B \approx 49.46^\circ, C \approx 108.21^\circ$

3. $B \approx 40.11^\circ, C \approx 104.89^\circ, a \approx 7.12$

4. Two solutions

$B \approx 41.10^\circ, C \approx 113.90^\circ, c \approx 38.94$

$B \approx 138.90^\circ, C \approx 16.10^\circ, c \approx 11.81$

5. No solution 6. $B \approx 14.79^\circ, C \approx 15.21^\circ, c \approx 4.93$

7. 675 ft 8. 2337 m² 9. $\mathbf{w} = \langle 12, 13 \rangle, \|\mathbf{w}\| \approx \sqrt{313}$

10. (a) $\langle 8, 8 \rangle$ (b) $\langle -12, -22 \rangle$ (c) $\langle -4, -26 \rangle$

11. (a) $\langle -7, -18 \rangle$ (b) $\langle -2, 32 \rangle$ (c) $\langle -24, 20 \rangle$

12. (a) $13\mathbf{i} + 17\mathbf{j}$ (b) $-17\mathbf{i} - 28\mathbf{j}$ (c) $-\mathbf{i} - 14\mathbf{j}$

13. (a) $-\mathbf{j}$ (b) $5\mathbf{i} + 9\mathbf{j}$ (c) $11\mathbf{i} + 17\mathbf{j}$

14. $\left\langle \frac{3\sqrt{13}}{13}, -\frac{2\sqrt{13}}{13} \right\rangle$ 15. $\left\langle \frac{18\sqrt{34}}{17}, -\frac{30\sqrt{34}}{17} \right\rangle$

16. $\theta \approx 14.87^\circ, 250.15 \text{ lb}$ 17. -1 18. 105.95°

19. Yes. $\mathbf{u} \cdot \mathbf{v} = 0$ 20. $\left\langle \frac{185}{26}, \frac{37}{26} \right\rangle, \mathbf{u} = \left\langle \frac{185}{26}, \frac{37}{26} \right\rangle + \left\langle -\frac{29}{26}, \frac{145}{26} \right\rangle$

21. $z = 6\sqrt{2}\left(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4}\right)$ 22. $-50 - 50\sqrt{3}i$

23. $-\frac{6561}{2} + \frac{6561\sqrt{3}}{2}i$ 24. $5832i$

25. $4\left(\cos \frac{\pi}{12} + i \sin \frac{\pi}{12}\right)$

$4\left(\cos \frac{7\pi}{12} + i \sin \frac{7\pi}{12}\right)$

$4\left(\cos \frac{13\pi}{12} + i \sin \frac{13\pi}{12}\right)$

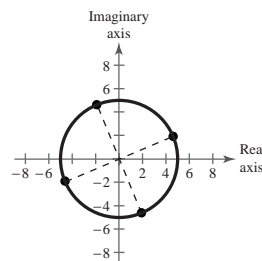
$4\left(\cos \frac{19\pi}{12} + i \sin \frac{19\pi}{12}\right)$

26. $5\left(\cos \frac{\pi}{8} + i \sin \frac{\pi}{8}\right)$

$5\left(\cos \frac{5\pi}{8} + i \sin \frac{5\pi}{8}\right)$

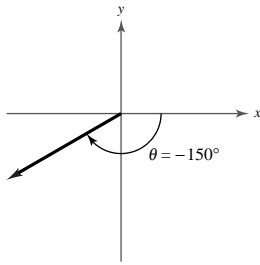
$5\left(\cos \frac{9\pi}{8} + i \sin \frac{9\pi}{8}\right)$

$5\left(\cos \frac{13\pi}{8} + i \sin \frac{13\pi}{8}\right)$



Cumulative Test for Chapters 4–6
(page 462)

1. (a)

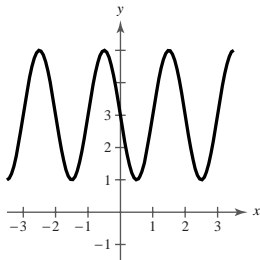


- (b) 210°
(c) $-\frac{5\pi}{6}$
(d) 30°

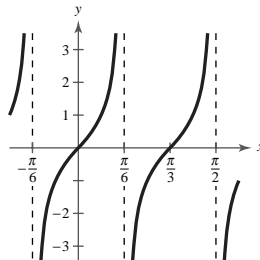
(e) $\sin(-150^\circ) = -\frac{1}{2}$
 $\cos(-150^\circ) = -\frac{\sqrt{3}}{2}$
 $\tan(-150^\circ) = \frac{\sqrt{3}}{3}$
 $\csc(-150^\circ) = -2$
 $\sec(-150^\circ) = -\frac{2\sqrt{3}}{3}$
 $\cot(-150^\circ) = \sqrt{3}$

2. 146.1° 3. $\cos \theta = -\frac{5}{13}$

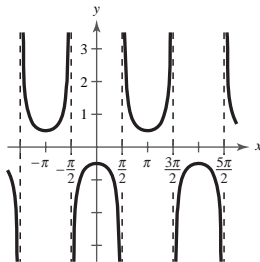
4.



5.



6.



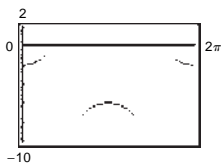
7. $a = 3, b = \pi, c = \pi$

8. $\frac{3}{5}$ 9. $-\frac{\sqrt{3}}{3}$ 10. $\frac{2x}{\sqrt{4x^2+1}}$ 11. $2 \tan \theta$

12–14. Answers will vary. 15. $\frac{3\pi}{2} + 2n\pi$

16. $\frac{\pi}{6} + n\pi, \frac{5\pi}{6} + n\pi$ 17. 1.7646, 4.5186

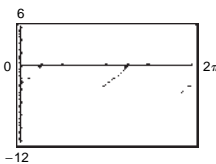
18.



$\frac{\pi}{3}, \frac{5\pi}{3}$

20. $\frac{16}{63}$ 21. $\frac{4}{3}$ 22. $\frac{2\sqrt{5}}{5}$

19.



$\frac{\pi}{4}, \frac{5\pi}{4}$

23. $2 \cos 6x \cos 2x$ 24–27. Answers will vary.

28. $B \approx 14.89^\circ$ 29. $B \approx 52.82^\circ$

$C \approx 119.11^\circ$ $C \approx 95.18^\circ$

$c \approx 17.00$ $a \approx 5.32$

30. $B = 55^\circ$ 31. $A \approx 26.07^\circ$

$b \approx 20.14$ $B \approx 33.33^\circ$

$c \approx 24.13$ $C \approx 120.60^\circ$

32. 131.71 in.^2 33. 94.10 in.^2 34. $3i + 5j$

35. $\frac{\sqrt{5}}{5}i - \frac{2\sqrt{5}}{5}j$ 36. -5 37. 1

38. $\langle -\frac{1}{13}, -\frac{5}{13} \rangle; \mathbf{u} = \langle \frac{105}{13}, -\frac{21}{13} \rangle + \langle -\frac{1}{13}, -\frac{5}{13} \rangle$

39. $3\sqrt{2}(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4})$ 40. $-9 + 3\sqrt{3}i$

41. $-12\sqrt{3} + 12i$

42. $1.4553 + 0.3436i, -1.4553 - 0.3436i$

43. $1, -\frac{1}{2} + \frac{\sqrt{3}}{2}i, -\frac{1}{2} - \frac{\sqrt{3}}{2}i$

44. $5(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4})$ 45. 5 ft

$5(\cos \frac{3\pi}{4} + i \sin \frac{3\pi}{4})$

$5(\cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4})$

$5(\cos \frac{7\pi}{4} + i \sin \frac{7\pi}{4})$

46. $d = 7 \sin \frac{\pi}{4}t$ 47. $54.34^\circ; 489.45 \text{ km/h}$ 48. 80.28°

Chapter 7

Section 7.1 (page 476)

1. system, equations 3. substitution

5. Break-even point

7. (a) No (b) No (c) No (d) Yes

9. (a) No (b) Yes (c) No (d) No

11. $(2, 2)$ 13. $(2, 6), (-1, 3)$

15. $(0, 2), (\sqrt{3}, 2 - 3\sqrt{3}), (-\sqrt{3}, 2 + 3\sqrt{3})$ 17. $(4, 4)$

19. $(5, 5)$ 21. $(\frac{1}{2}, 3)$ 23. $(1, 1)$ 25. $(\frac{20}{3}, \frac{40}{3})$

27. No solution 29. \$4000 at 4%, \$14,000 at 6%

31. \$3500 at 7.6%, \$14,500 at 8.8% 33. $(-2, 0), (3, 5)$

35. No real solution 37. $(0, 0), (1, 1), (-1, -1)$

39. $(4, 3)$ 41. $(\frac{5}{2}, \frac{3}{2})$ 43. No real solution

45. $(3, 6), (-3, 0)$ 47. $(4, -0.5)$ 49. $(8, 3), (3, -2)$

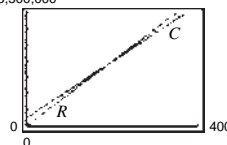
51. $(\pm 1.540, 2.372)$ 53. $(0, 1)$ 55. $(2.318, 2.841)$

57. $(2.25, 5.5)$ 59. $(0, -13), (\pm 12, 5)$ 61. $(1, 2)$

63. $(-2, 0), (\frac{29}{10}, \frac{21}{10})$ 65. No real solution 67. $(0.25, 1.5)$

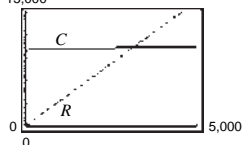
69. $(0.287, 1.751)$ 71. $(0, 1), (1, 0)$ 73. $(-4, -\frac{1}{4}), (\frac{1}{2}, 2)$

75. 3,500,000



192 units; \$1,910,400

77. 15,000



3133 units; \$10,308

79. $6 \text{ m} \times 9 \text{ m}$

81. (a)

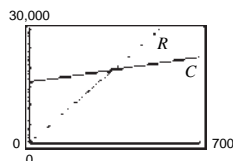
Week	Animated	Horror
1	336	42
2	312	60
3	288	78
4	264	96
5	240	114
6	216	132
7	192	150
8	168	168
9	144	186
10	120	204
11	96	222
12	72	240

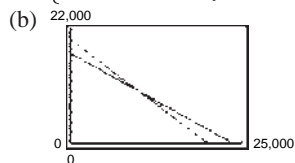
(b) and (c) $x = 8$ (d) The answers are the same.

(e) During week 8 the same number of animated and horror films were rented.

83. (a) $C = 9.45x + 16,000$
 $R = 55.95x$

(b) 344 units


85. 8 mi \times 12 mi

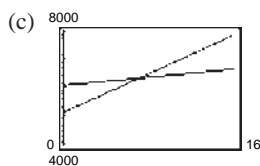
87. (a)
$$\begin{cases} x + y = 20,000 \\ 0.055x + 0.075y = 1300 \end{cases}$$


(c) \$10,000. The solution is (10,000, 10,000).

89. (a)

t	Year	Arizona	Indiana
0	2000	5118	6080
1	2001	5289.9	6115.7
2	2002	5461.8	6151.4
3	2003	5633.7	6187.1
4	2004	5805.6	6222.8
5	2005	5977.5	6258.5
6	2006	6149.4	6294.2
7	2007	6321.3	6329.9
8	2008	6493.2	6365.6

(b) 2008



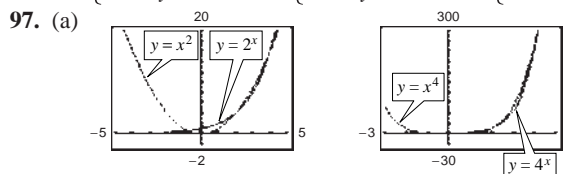
(7.06, 6332.15)

(d) (7.06, 6332.15)

(e) At one point in 2007, the populations of Arizona and Indiana were equal.

91. False. You can solve for either variable before back-substituting.

93. For a linear system, the result will be a contradictory equation such as $0 = N$, where N is a nonzero real number. For a nonlinear system, there may be an equation with imaginary roots.

95. (a) $\begin{cases} 3x + y = 3 \\ 3x + y = 5 \end{cases}$ (b) $\begin{cases} 3x + y = 4 \\ 2x + y = 2 \end{cases}$ (c) $\begin{cases} 6x + 3y = 9 \\ 2x + y = 3 \end{cases}$

(b) There are three points of intersection when b is even.

99. $y = -\frac{2}{7}x + \frac{45}{7}$ 101. $y = 3$ 103. $y = \frac{30}{17}x - \frac{18}{17}$

105. Domain: All real numbers x except $x = 6$

Asymptotes: $y = 0$, $x = 6$

107. Domain: All real numbers x except $x = \pm 4$

Asymptotes: $y = 1$, $x = \pm 4$

109. Domain: All real numbers x

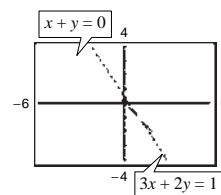
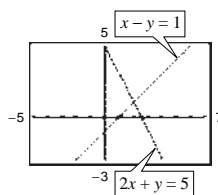
Asymptote: $y = 0$

Section 7.2 (page 485)

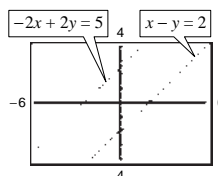
1. method, elimination 3. Inconsistent 5. Yes

7. (2, 1)

9. (1, -1)



11. Inconsistent


13. $(2, \frac{1}{2})$ 15. (3, 4) 17. (4, -1) 19. $(\frac{12}{7}, \frac{18}{7})$

21. Inconsistent 23. b; One solution, consistent

24. a; Infinitely many solutions, consistent

25. c; One solution, consistent

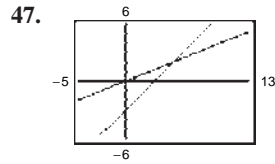
26. d; No solutions, inconsistent 27. $(\frac{3}{2}, -\frac{1}{2})$

29. Inconsistent 31. All points on $6x + 8y - 1 = 0$

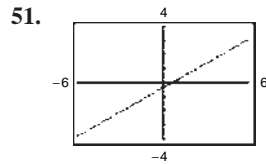
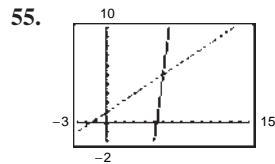
33. (5, -2) 35. All points on $-5x + 6y = -3$

37. All points on $5x - 6y - 3 = 0$ 39. (101, 96)

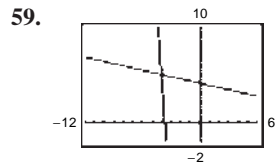
41. $(\frac{90}{31}, -\frac{67}{31})$ 43. (-1, 1) 45. $(1, \frac{1}{2})$



Consistent; (5, 2)


 Consistent; all points on $8x - 14y = 5$


(6, 5)



(-4, 5)

61. (4, 1) 63. (2, -1) 65. (6, -3) 67. $(\frac{49}{4}, \frac{33}{4})$

69. $\begin{cases} 3x + \frac{1}{2}y = 4 \\ x + 3y = 24 \end{cases}$ 71. $\begin{cases} 2x + 2y = 11 \\ x - 4y = -7 \end{cases}$

73. (240, 404) 75. (2,000,000, 100)

77. Plane: 550 mi/hr; wind: 50 mi/hr

79. (a) $\begin{cases} 5.00A + 3.50C = 5087.50 \\ A + C = 1175 \end{cases}$
 (b) $A = 650, C = 525$; Answers will vary.
 (c) $A = 650, C = 525$

81. 9 oranges, 7 grapefruit 83. 185 movies, 125 video games

85. $y = 0.97x + 2.1$ 87. $y = -2.5x + 5.54$

89. (a) and (b) $y = 14x + 19$
 (c) (d) 41.4 bushels per acre

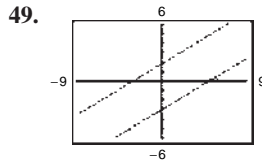
91. True. A linear system can have only one solution, no solution, or infinitely many solutions.

93. False. Sometimes you will be able to get only a close approximation.

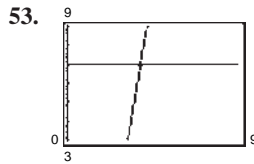
95. (a) $\begin{cases} x + y = 10 \\ x + y = 20 \end{cases}$ (b) $\begin{cases} x + y = 4 \\ 3x + 3y = 12 \end{cases}$

97. $u = 1; v = -\tan x$

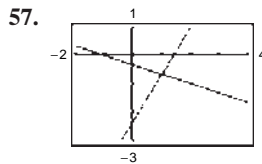
99. $x \leq -\frac{22}{3}$ 101. $-2 < x < 18$



Inconsistent

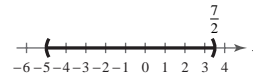


(3.833, 7)



(1, -0.667)

103. $-5 < x < \frac{7}{2}$



105. $\ln 6x$

107. $\log_9 \frac{12}{x}$ 109. $\ln \frac{x^2}{x+2}$

111. Answers will vary.

Section 7.3 (page 499)

1. row-echelon 3. Gaussian 5. three-dimensional

7. Independent 9. (a) No (b) Yes (c) No (d) No

11. (a) No (b) No (c) Yes (d) No

13. (2, -2, 2) 15. (3, 10, 2) 17. $(\frac{11}{4}, 7, 11)$

19. $\begin{cases} x - 2y + 3z = 5 \\ y - 2z = 9 \\ 2x - 3z = 0 \end{cases}$

It removed the x -term from Equation 2.

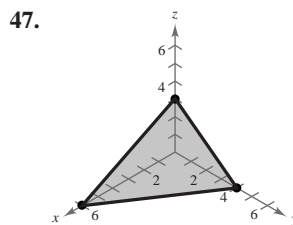
21. (1, 2, 3) 23. (-4, 8, 5) 25. (2, -3, -2)

27. Inconsistent 29. $(1, -\frac{3}{2}, \frac{1}{2})$ 31. $(-a + 3, a + 1, a)$

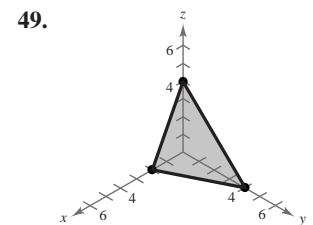
33. Inconsistent 35. Inconsistent 37. (-1, 1, 0)

39. $(2a, 21a - 1, 8a)$ 41. $(-\frac{3}{2}a + \frac{1}{2}, -\frac{2}{3}a + 1, a)$

43. $\begin{cases} x + y + z = 1 \\ 2x + y + z = 4 \\ x + y - 3z = -7 \end{cases}$ 45. $\begin{cases} x + y + 2z = -10 \\ -x + 12y + 8z = -14 \\ x + 14y - 4z = -6 \end{cases}$



(6, 0, 0), (0, 4, 0),
(0, 0, 3), (4, 0, 1)



(2, 0, 0), (0, 4, 0),
(0, 0, 4), (0, 2, 2)

51. $\frac{A}{x} + \frac{B}{x-14}$ 53. $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{x-10}$

55. $\frac{A}{x-5} + \frac{B}{(x-5)^2} + \frac{C}{(x-5)^3}$ 57. $\frac{1}{2}(\frac{1}{x-1} - \frac{1}{x+1})$

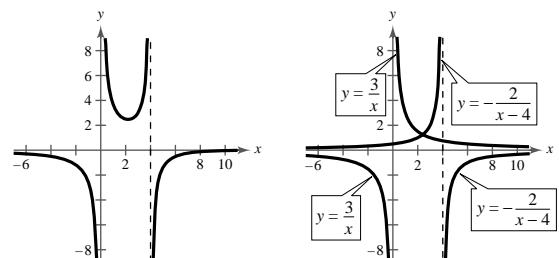
59. $\frac{1}{x} - \frac{1}{x+1}$ 61. $\frac{3}{2x-1} - \frac{2}{x+1}$

63. $-\frac{3}{x} - \frac{1}{x+2} + \frac{5}{x-2}$ 65. $\frac{3}{x} - \frac{1}{x^2} + \frac{1}{x+1}$

67. $2x - 7 + \frac{17}{x+2} + \frac{1}{x+1}$

69. $x + 3 + \frac{6}{x-1} + \frac{4}{(x-1)^2} + \frac{1}{(x-1)^3}$

71. $\frac{3}{x} - \frac{2}{x-4}$



The vertical asymptotes are the same.

73. $s = -16t^2 + 144$ 75. $s = -16t^2 - 32t + 400$
77. $y = \frac{1}{2}x^2 - 2x$ 79. $y = x^2 - 6x + 8$
81. $x^2 + y^2 - 10x = 0$ 83. $x^2 + y^2 + 6x - 8y = 0$
85. \$300,000 at 8%, \$400,000 at 9%, and \$75,000 at 10%
87. 187,500 + s in certificates of deposit
187,500 - s in municipal bonds
125,000 - s in blue-chip stocks
 s in growth stocks

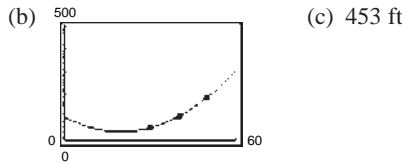
89. 13 two-point baskets, 6 three-point baskets, 9 free throws

91. $I_1 = 1, I_2 = 2, I_3 = 1$

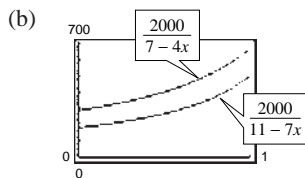
93. $y = -\frac{5}{24}x^2 - \frac{3}{10}x + \frac{41}{6}$ 95. $y = x^2 - x$

97. (a)
$$\begin{cases} 900a + 30b + c = 55 \\ 1600a + 40b + c = 105 \\ 2500a + 50b + c = 188 \end{cases}$$

 $y = 0.165x^2 - 6.55x + 103$



99. (a) $\frac{2000}{7-4x} - \frac{2000}{11-7x}, 0 \leq x \leq 1$



101. False. The leading coefficients are not all 1.

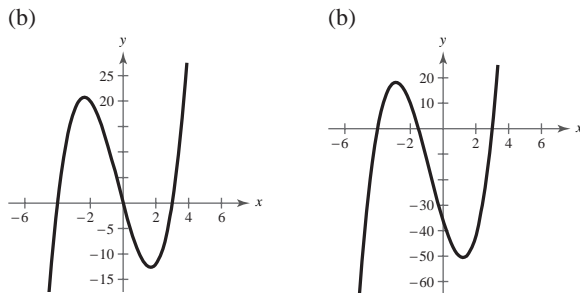
103. The student did not work the problem correctly. Because $\frac{x^2 + 1}{x(x-1)}$ is an improper fraction, the student should have divided before decomposing.

105. No. There are two arithmetic errors. The constant in the second equation should be -11 and the coefficient of z in the third equation should be 2.

107. $x = 5, y = 5, \lambda = -5$

109. (a) -4, 0, 3

111. (a) -4, $-\frac{3}{2}, 3$



113. $\frac{\pi}{6} + n\pi$ 115. Answers will vary.

Section 7.4 (page 513)

1. matrix 3. Gauss-Jordan elimination 5. No

7. 1×2 9. 3×1 11. 2×2

13.
$$\begin{bmatrix} 4 & -3 & \vdots & -5 \\ -1 & 3 & \vdots & 12 \end{bmatrix} 2 \times 3$$

15.
$$\begin{bmatrix} 1 & 10 & -2 & \vdots & 2 \\ 5 & -3 & 4 & \vdots & 0 \\ 2 & 1 & 0 & \vdots & 6 \end{bmatrix} 3 \times 4$$

17.
$$\begin{bmatrix} 7 & -5 & 1 & \vdots & 13 \\ 19 & 0 & -8 & \vdots & 10 \end{bmatrix} 2 \times 4$$

19.
$$\begin{cases} 3x + 4y = 9 \\ x - y = -3 \end{cases} 21. \begin{cases} 9x + 12y + 3z = 0 \\ -2x + 18y + 5z = 10 \\ x + 7y - 8z = -4 \end{cases}$$

23. Add -3 times R_2 to R_1 . 25. Interchange R_1 and R_2 .

27.
$$\begin{bmatrix} 1 & 4 & 3 \\ 0 & 2 & -1 \end{bmatrix}$$

29.
$$\begin{bmatrix} 1 & 1 & 4 & -1 \\ 0 & 5 & -2 & 6 \\ 0 & 3 & 20 & 4 \end{bmatrix}, \begin{bmatrix} 1 & 1 & 4 & -1 \\ 0 & 1 & -\frac{2}{5} & \frac{6}{5} \\ 0 & 3 & 20 & 4 \end{bmatrix}$$

31. (a) i)
$$\begin{bmatrix} 3 & 0 & \vdots & -6 \\ 6 & -4 & \vdots & -28 \end{bmatrix}$$
 ii)
$$\begin{bmatrix} 3 & 0 & \vdots & -6 \\ 0 & -4 & \vdots & -16 \end{bmatrix}$$

iii)
$$\begin{bmatrix} 3 & 0 & \vdots & -6 \\ 0 & 1 & \vdots & 4 \end{bmatrix}$$
 iv)
$$\begin{bmatrix} 1 & 0 & \vdots & -2 \\ 0 & 1 & \vdots & 4 \end{bmatrix}$$

(b) $x = -2, y = 4$ (c) Answers will vary.

33. i)
$$\begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$
 ii)
$$\begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$

iii)
$$\begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$
 iv)
$$\begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$

35. Reduced row-echelon form

37. Not in row-echelon form

39. Not in row-echelon form

41.
$$\begin{bmatrix} 1 & 3 & \frac{3}{2} & 5 \\ 0 & 1 & \frac{3}{14} & 0 \\ 0 & 0 & 1 & -\frac{35}{12} \end{bmatrix}$$
 43.
$$\begin{bmatrix} 1 & -1 & -1 & 1 \\ 0 & 1 & 6 & 3 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

45.
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
 47.
$$\begin{bmatrix} 1 & 0 & -\frac{3}{7} & -\frac{8}{7} \\ 0 & 1 & -\frac{12}{7} & \frac{10}{7} \end{bmatrix}$$

49.
$$\begin{cases} x - 2y = 4 \\ y = -3 \end{cases} (-2, -3)$$
 51.
$$\begin{cases} x - y + 2z = 4 \\ y - z = 2 \\ z = -2 \end{cases} (8, 0, -2)$$

53. (7, -5) 55. (-4, -8, 2) 57. (3, 2)

59. Inconsistent 61. (3, -2, 5, 0) 63. (4, -3, 2)

65. $(2a + 1, 3a + 2, a)$ 67. (7, -3, 4)

69. $(0, 2 - 4a, a)$ 71. $(-5a, a, 3)$

73. Yes; (-1, 1, -3) 75. No 77. $y = x^2 + 2x + 5$

79. $y = 2x^2 - x + 1$ 81. $f(x) = -9x^2 - 5x + 11$

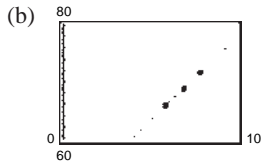
83. $f(x) = x^3 - 2x^2 - 4x + 1$ 85. $I_1 = \frac{13}{10}, I_2 = \frac{11}{5}, I_3 = \frac{9}{10}$

87.
$$\begin{cases} x + 5y + 10z + 20w = 95 \\ x + y + z + w = 26 \\ y - 4z = 0 \\ x - 2y = -1 \end{cases}$$

15 \$1 bills, 8 \$5 bills, 2 \$10 bills, 1 \$20 bill

$$89. \frac{8x^2}{(x-1)^2(x+1)} = \frac{2}{x+1} + \frac{6}{x-1} + \frac{4}{(x-1)^2}$$

$$91. (a) y = -0.01t^2 + 3.08t + 47.7$$



- (b) 2010: \$77.50,
2015: \$91.65,
2020: \$105.30
(d) Answers will vary.

$$93. (a) x_1 = s, x_2 = t, x_3 = 600 - s,$$

$$x_4 = s - t, x_5 = 500 - t, x_6 = s, x_7 = t$$

$$(b) x_1 = 0, x_2 = 0, x_3 = 600, x_4 = 0, x_5 = 500,$$

$$x_6 = 0, x_7 = 0$$

$$(c) x_1 = 500, x_2 = 100, x_3 = 100, x_4 = 400,$$

$$x_5 = 400, x_6 = 500, x_7 = 100$$

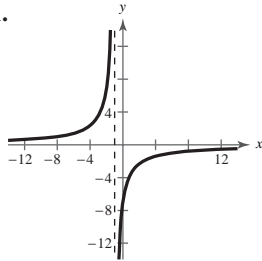
95. True. See Example 7.

$$97. \begin{cases} x + y + 7z = -1 \\ x + 2y + 11z = 0 \\ 2x + y + 10z = -3 \end{cases}$$

(Answer is not unique.)

99. No; Answers will vary.

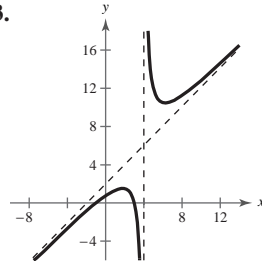
101.



Asymptotes:

$$x = -1, y = 0$$

103.



Asymptotes:

$$x = 4, y = x + 2$$

Section 7.5 (page 527)

1. equal 3. zero, 0

5. (a) iii (b) i (c) iv (d) v (e) ii

7. No, not in general. 9. $x = 5, y = -8$

11. $x = -1, y = 4, z = 6$

$$13. (a) \begin{bmatrix} 8 & -1 \\ 1 & 7 \end{bmatrix} \quad (b) \begin{bmatrix} 2 & -3 \\ 5 & -5 \end{bmatrix}$$

$$(c) \begin{bmatrix} 15 & -6 \\ 9 & 3 \end{bmatrix} \quad (d) \begin{bmatrix} 9 & -8 \\ 13 & -9 \end{bmatrix}$$

$$15. (a) \begin{bmatrix} 9 & 5 \\ 1 & -2 \\ -3 & 15 \end{bmatrix} \quad (b) \begin{bmatrix} 7 & -7 \\ 3 & 8 \\ -5 & -5 \end{bmatrix}$$

$$(c) \begin{bmatrix} 24 & -3 \\ 6 & 9 \\ -12 & 15 \end{bmatrix} \quad (d) \begin{bmatrix} 22 & -15 \\ 8 & 19 \\ -14 & -5 \end{bmatrix}$$

$$17. (a) \begin{bmatrix} 5 & 5 & -2 & 4 & 4 \\ -5 & 10 & 0 & -4 & -7 \end{bmatrix}$$

$$(b) \begin{bmatrix} 3 & 5 & 0 & 2 & 4 \\ 7 & -6 & -4 & 2 & 7 \end{bmatrix}$$

$$(c) \begin{bmatrix} 12 & 15 & -3 & 9 & 12 \\ 3 & 6 & -6 & -3 & 0 \end{bmatrix}$$

$$(d) \begin{bmatrix} 10 & 15 & -1 & 7 & 12 \\ 15 & -10 & -10 & 3 & 14 \end{bmatrix}$$

19. (a) Not possible (b) Not possible

$$(c) \begin{bmatrix} 18 & 0 & 9 \\ -3 & -12 & 0 \end{bmatrix} \quad (d) \text{Not possible}$$

$$21. \begin{bmatrix} -8 & -7 \\ 15 & -1 \end{bmatrix} \quad 23. \begin{bmatrix} -24 & -4 & 12 \\ -12 & 32 & 12 \end{bmatrix}$$

$$25. \begin{bmatrix} -17.143 & 2.143 \\ 11.571 & 10.286 \end{bmatrix} \quad 27. \begin{bmatrix} -4.841 & -3.739 \\ -4.252 & -13.249 \\ 9.713 & -0.362 \end{bmatrix}$$

$$29. \begin{bmatrix} -6 & -9 \\ -1 & 0 \\ 17 & -10 \end{bmatrix} \quad 31. \begin{bmatrix} 3 & 3 \\ -\frac{1}{2} & 0 \\ -\frac{13}{2} & \frac{11}{2} \end{bmatrix} \quad 33. \text{Not possible}$$

$$35. \begin{bmatrix} -2 & 51 \\ -8 & 33 \\ 0 & 27 \end{bmatrix} \quad 37. \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & \frac{7}{2} \end{bmatrix}$$

$$39. \begin{bmatrix} -15 & -5 & -25 & -45 \\ -18 & -6 & -30 & -54 \end{bmatrix}$$

$$41. (a) \begin{bmatrix} 0 & 15 \\ 6 & 12 \end{bmatrix} \quad (b) \begin{bmatrix} -2 & 2 \\ 31 & 14 \end{bmatrix} \quad (c) \begin{bmatrix} 9 & 6 \\ 12 & 12 \end{bmatrix}$$

$$43. (a) \begin{bmatrix} 0 & -10 \\ 10 & 0 \end{bmatrix} \quad (b) \begin{bmatrix} 0 & -10 \\ 10 & 0 \end{bmatrix} \quad (c) \begin{bmatrix} 8 & -6 \\ 6 & 8 \end{bmatrix}$$

$$45. (a) \begin{bmatrix} 7 & 7 & 14 \\ 8 & 8 & 16 \\ -1 & -1 & -2 \end{bmatrix} \quad (b) [13] \quad (c) \text{Not possible}$$

$$47. \begin{bmatrix} 70 & -17 & 73 \\ 32 & 11 & 6 \\ 16 & -38 & 70 \end{bmatrix} \quad 49. \begin{bmatrix} 151 & 25 & 48 \\ 516 & 279 & 387 \\ 47 & -20 & 87 \end{bmatrix}$$

$$51. \begin{bmatrix} 5 & 8 \\ -4 & -16 \end{bmatrix} \quad 53. \begin{bmatrix} -4 & 10 \\ 3 & 14 \end{bmatrix}$$

55. (a) No (b) Yes (c) No (d) No

57. (a) No (b) Yes (c) No (d) No

$$59. (a) \begin{bmatrix} -1 & 1 \\ -2 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 4 \\ 0 \end{bmatrix} \quad (b) \begin{bmatrix} 4 \\ 8 \end{bmatrix}$$

$$61. (a) \begin{bmatrix} -2 & -3 \\ 6 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -4 \\ -36 \end{bmatrix} \quad (b) \begin{bmatrix} -7 \\ 6 \end{bmatrix}$$

$$63. (a) \begin{bmatrix} 1 & -2 & 3 \\ -1 & 3 & -1 \\ 2 & -5 & 5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 9 \\ -6 \\ 17 \end{bmatrix} \quad (b) \begin{bmatrix} 1 \\ -1 \\ 2 \end{bmatrix}$$

$$65. (a) \begin{bmatrix} 1 & -5 & 2 \\ -3 & 1 & -1 \\ 0 & -2 & 5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -20 \\ 8 \\ -16 \end{bmatrix} \quad (b) \begin{bmatrix} -1 \\ 3 \\ -2 \end{bmatrix}$$

$$67. (a) \begin{bmatrix} 7 & -2 & 5 \\ -6 & 13 & -8 \\ 16 & 11 & -3 \end{bmatrix} \quad (b) \begin{bmatrix} 7 & -2 & 5 \\ -6 & 13 & -8 \\ 16 & 11 & -3 \end{bmatrix}$$

The answers are the same.

$$69. (a) \begin{bmatrix} 26 & 11 & 0 \\ 11 & 20 & -3 \\ 11 & 14 & 0 \end{bmatrix} \quad (b) \begin{bmatrix} 26 & 11 & 0 \\ 11 & 20 & -3 \\ 11 & 14 & 0 \end{bmatrix}$$

The answers are the same.

$$71. (a) \begin{bmatrix} 25 & -34 & 28 \\ -53 & 34 & -7 \\ -76 & 30 & 21 \end{bmatrix} \quad (b) \begin{bmatrix} 25 & -34 & 28 \\ -53 & 34 & -7 \\ -76 & 30 & 21 \end{bmatrix}$$

The answers are the same.

73. (a) and (b) $\begin{bmatrix} 3 & -6 & 0 \\ 3 & 3 & 0 \end{bmatrix}$ 75. Not possible, undefined

77. Not possible, undefined

79. (a) and (b) $\begin{bmatrix} 6 & 12 & -12 \\ -6 & 6 & 0 \end{bmatrix}$ 81. $\begin{bmatrix} -4 & 0 \\ 8 & 2 \end{bmatrix}$

83. $\begin{bmatrix} 84 & 60 & 30 \\ 42 & 120 & 84 \end{bmatrix}$ 85. $\begin{bmatrix} 90 & 108 & 54 & 36 \\ 126 & 144 & 180 & 72 \end{bmatrix}$

87. [\$1037.50 \$1400.00 \$1012.50]

The entries represent the total profits made at the three outlets.

89. $\begin{bmatrix} \$23.20 & \$20.50 \\ \$38.20 & \$33.80 \\ \$76.90 & \$68.50 \end{bmatrix}$ The entries represent labor costs at the two plants for the three boat sizes.

91. $\begin{bmatrix} 0.40 & 0.15 & 0.15 \\ 0.28 & 0.53 & 0.17 \\ 0.32 & 0.32 & 0.68 \end{bmatrix}$ P^2 represents the proportion of changes in party affiliations after two elections.

93. True. To add two matrices, you add corresponding entries.

95. Not possible 97. Not possible 99. 2×2

101. 2×3 103 and 105. Answers will vary.

107. $AC = BC = \begin{bmatrix} 2 & 3 \\ 2 & 3 \end{bmatrix}, A \neq B$

109. (a) $A^2 = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}, A^3 = \begin{bmatrix} -i & 0 \\ 0 & -i \end{bmatrix}, A^4 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

The entries on the main diagonal are i^2 in A^2 , i^3 in A^3 , and i^4 in A^4 .

(b) $B^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

B^2 is the identity matrix.

111. (a) $A = \begin{bmatrix} 0 & 2 \\ 0 & 0 \end{bmatrix}, B = \begin{bmatrix} 0 & 2 & 3 \\ 0 & 0 & 4 \\ 0 & 0 & 0 \end{bmatrix}$

(Answers are not unique.)

(b) A^2 and B^3 are zero matrices.

(c) $A = \begin{bmatrix} 0 & 2 & 3 & 4 \\ 0 & 0 & 5 & 6 \\ 0 & 0 & 0 & 7 \\ 0 & 0 & 0 & 0 \end{bmatrix}$

A^4 is the zero matrix.

(d) A^n is the zero matrix.

113. $\ln \frac{64}{\sqrt[3]{x^2 + 3}}$

Section 7.6 (page 538)

1. inverse 3. No 5–9. Answers will vary.

11. $\begin{bmatrix} \frac{1}{2} & 0 \\ 0 & \frac{1}{3} \end{bmatrix}$ 13. $\begin{bmatrix} -3 & 2 \\ -2 & 1 \end{bmatrix}$ 15. Does not exist

17. $\begin{bmatrix} 1 & 1 & -1 \\ -3 & 2 & -1 \\ 3 & -3 & 2 \end{bmatrix}$ 19. $\begin{bmatrix} 1 & 0 & 0 \\ -\frac{3}{4} & \frac{1}{4} & 0 \\ \frac{7}{20} & -\frac{1}{4} & \frac{1}{5} \end{bmatrix}$

21. $\begin{bmatrix} -\frac{3}{2} & \frac{3}{2} & 1 \\ \frac{9}{2} & -\frac{7}{2} & -3 \\ -1 & 1 & 1 \end{bmatrix}$ 23. $\begin{bmatrix} -12 & -5 & -9 \\ -4 & -2 & -4 \\ -8 & -4 & -6 \end{bmatrix}$

25. $\frac{5}{11} \begin{bmatrix} 0 & -4 & 2 \\ -22 & 11 & 11 \\ 22 & -6 & -8 \end{bmatrix}$ 27. $\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 2 & 0 & 1 & 0 \\ 0 & 1 & 0 & 2 \end{bmatrix}$

29. $\begin{bmatrix} \frac{1}{4} & \frac{1}{8} \\ -\frac{1}{4} & -\frac{5}{8} \end{bmatrix}$ 31. $\frac{1}{59} \begin{bmatrix} 16 & 15 \\ -4 & 70 \end{bmatrix}$ 33. $\begin{bmatrix} \frac{5}{13} & -\frac{3}{13} \\ \frac{1}{13} & \frac{2}{13} \end{bmatrix}$

35. $k = 0$ 37. (5, 0) 39. (-8, -6) 41. (3, 8, -11)

43. (2, 1, 0, 0) 45. (2, -2)

47. Not possible, because A is not invertible. 49. (-4, -8)

51. (-1, 3, 2) 53. $(0.3125t + 0.8125, 1.1875t + 0.6875, t)$

55. (5, 0, -2, 3)

57. \$7000 in AAA-rated bonds, \$1000 in A-rated bonds, and \$2000 in B-rated bonds

59. \$9000 in AAA-rated bonds, \$1000 in A-rated bonds, and \$2000 in B-rated bonds

61. $I_1 = \frac{1}{2}$ ampere, $I_2 = 3$ amperes, $I_3 = 3.5$ amperes

63. 100 bags for seedlings, 100 bags for general potting, 100 bags for hardwood plants

65. (a) $\begin{cases} 2.5r + 4l + 2i = 300 \\ -r + 2l + 2i = 0 \\ r + l + i = 120 \end{cases}$

(b) $\begin{bmatrix} 2.5 & 4 & 2 \\ -1 & 2 & 2 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} r \\ l \\ i \end{bmatrix} = \begin{bmatrix} 300 \\ 0 \\ 120 \end{bmatrix}$

(c) 80 roses, 10 lilies, 30 irises

67. True, $AA^{-1} = I = A^{-1}A$. 69. Answers will vary.

71. (a) Answers will vary.

(b) $A^{-1} = \begin{bmatrix} \frac{1}{a_{11}} & 0 & 0 & 0 & \dots & 0 \\ 0 & \frac{1}{a_{22}} & 0 & 0 & \dots & 0 \\ 0 & 0 & \frac{1}{a_{33}} & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \dots & \vdots \\ 0 & 0 & 0 & 0 & \dots & \frac{1}{a_{nn}} \end{bmatrix}$

73. $\ln 3 \approx 1.099$ 75. $\frac{e^{12/7}}{3} \approx 1.851$

77. Answers will vary.

Section 7.7 (page 545)

1. determinant 3. -5 5. 4 7. 16

9. 28 11. -24 13. -0.002

15. (a) $M_{11} = -5, M_{12} = 2, M_{21} = 4, M_{22} = 3$

(b) $C_{11} = -5, C_{12} = -2, C_{21} = -4, C_{22} = 3$

17. (a) $M_{11} = 10, M_{12} = -43, M_{13} = 2, M_{21} = -30, M_{22} = 17, M_{23} = -6, M_{31} = 54, M_{32} = -53, M_{33} = -34$

(b) $C_{11} = 10, C_{12} = 43, C_{13} = 2, C_{21} = 30, C_{22} = 17, C_{23} = 6, C_{31} = 54, C_{32} = 53, C_{33} = -34$

19. (a) -75 (b) -75 21. (a) 170 (b) 170

23. -58 25. 0 27. -9 29. -168

31. 412 33. -336 35. 410

37. (a) -3 (b) -2

(c) $\begin{bmatrix} -2 & 0 \\ 0 & -3 \end{bmatrix}$ (d) $6; |AB| = |A| \cdot |B|$

39. (a) 2 (b) -6

$$(c) \begin{bmatrix} 1 & 4 & 3 \\ -1 & 0 & 3 \\ 0 & 2 & 0 \end{bmatrix} \quad (d) -12; |AB| = |A| \cdot |B|$$

41. (a) -25 (b) -220

$$(c) \begin{bmatrix} -7 & -16 & -1 & -28 \\ -4 & -14 & -11 & 8 \\ 13 & 4 & 4 & -4 \\ -2 & 3 & 2 & 2 \end{bmatrix} \quad (d) 5500; |AB| = |A| \cdot |B|$$

43–47. Answers will vary. 49. $x = \pm 2$ 51. $x = \pm \frac{3}{2}$

53. $x = 1 \pm \sqrt{2}$ 55. $x = -4, -1$ 57. $x = 1, \frac{1}{2}$

59. $x = 3$ 61. $8uv - 1$ 63. e^{5x} 65. $1 - \ln x$

67. True. Expansion by cofactors on a row of zeros is zero.

69. Answers will vary. Sample answer:

$$A = \begin{bmatrix} 1 & 0 & -3 \\ 6 & -2 & 7 \\ 9 & 5 & -1 \end{bmatrix}, \quad B = \begin{bmatrix} 3 & 1 & 5 \\ -8 & 1 & 0 \\ -7 & 6 & -2 \end{bmatrix}$$

$$|A + B| = -328, |A| + |B| = -404$$

71. (a) 6 (b) $\begin{bmatrix} \frac{1}{3} & -\frac{1}{3} \\ \frac{1}{3} & \frac{1}{6} \end{bmatrix}$ (c) $\frac{1}{6}$ (d) They are reciprocals.

73. (a) 2 (b) $\begin{bmatrix} -4 & -5 & 1.5 \\ -1 & -1 & 0.5 \\ -1 & -1 & 0 \end{bmatrix}$

(c) $\frac{1}{2}$ (d) They are reciprocals.

75. (a) Columns 2 and 3 are interchanged.

(b) Rows 1 and 3 are interchanged.

77. (a) 3 is factored from the second row.

(b) 2 and 4 are factored from the first and second columns, respectively.

79. (a) 15 (b) -75 (c) -120

The determinant of a triangular matrix is the product of the numbers along the main diagonal.

81. Answers will vary. 83. $(x - 2)(x - 1)$

85. $(2y - 3)^2$ 87. $(2, -4)$

Section 7.8 (page 556)

1. Cramer's Rule 3. $-\frac{1}{2}$ 5. $\frac{5}{2}$ 7. $\frac{33}{8}$ 9. 24

11. $x = 0, -\frac{16}{5}$ 13. Collinear 15. Not collinear

17. $x = 3$ 19. $(-3, -2)$ 21. Not possible

23. $(-1, 3, 2)$ 25. (a) and (b) $(0, -\frac{1}{2}, \frac{1}{2})$

27. (a) $y = -1.086t^2 + 15.949t + 25.326$

(b)  The model fits the data well.

29. (a) $\begin{bmatrix} 20 & 5 & 24 \\ 20 & 0 & 13 \\ 20 & 0 & 23 \end{bmatrix}, \begin{bmatrix} 20 & 0 & 13 \\ 15 & 18 & 11 \end{bmatrix}$

(b) $-119 \ 28 \ 67 \ -58 \ 6 \ 39 \ -1 \ -3 \ 3$
 $-118 \ 26 \ 69 \ -33 \ 7 \ 15$

31. 1 -43 -108 49 91 91 1 -29 -73 33 42 15 7 14 14

33. HAPPY NEW YEAR

35. IF YOU CANT BE KIND BE VAGUE

37. True. Cramer's Rule divides by the determinant.

39. Answers will vary. 41. $x + 4y - 19 = 0$

43. $2x - 7y - 27 = 0$

Review Exercises (page 560)

1. (1, 1) 3. $(\frac{3}{2}, 5)$ 5. (0.25, 0.625) 7. (5, 4)

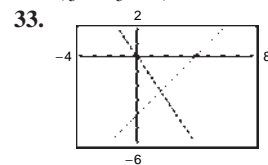
9. (0, 0), (2, 8), (-2, 8) 11. (2, -0.5)

13. (0, 0), (4, -4) 15. (-1, 2), (0.67, 2.56) 17. (4, 4)

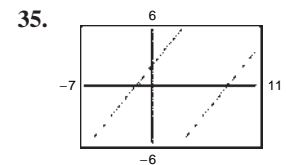
19. 800 plants 21. 96 m \times 144 m 23. $(\frac{5}{2}, 3)$

25. (-0.5, 0.8) 27. $(-\frac{1}{2}, \frac{4}{5})$ 29. (0, 0)

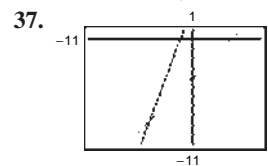
31. $(\frac{14}{5} + \frac{8}{5}a, a)$



Consistent; (1.6, -2.4)



Inconsistent



Consistent; (-4.6, -8.6)

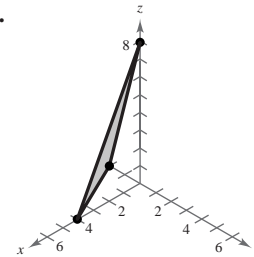
39. $(\frac{500,000}{7}, \frac{159}{7})$ 41. 218.75 mi/h; 193.75 mi/h

43. (2, -4, -5) 45. $(\frac{38}{17}, \frac{40}{17}, -\frac{63}{17})$

47. $(3a + 4, 2a + 5, a)$ 49. $(-\frac{19}{6}, \frac{17}{12}, \frac{1}{3})$

51. $(a - 4, a - 3, a)$

53.



Sample answer: (0, 0, 8), (0, -2, 0), (4, 0, 0), (1, -1, 2)

55. $\frac{3}{x+2} - \frac{4}{x+4}$ 57. $\frac{1}{2}(\frac{3}{x-1} - \frac{x-3}{x^2+1})$

59. $\frac{2x-1}{x^2+1} + \frac{-1}{x+2}$ 61. $y = 2x^2 + x - 5$

63. 4 par-3 holes, 10 par-4 holes, 4 par-5 holes

65. 3×1 67. 1×1

69. $\begin{bmatrix} 6 & -7 & \vdots & 11 \\ -2 & 5 & \vdots & -1 \end{bmatrix}$ 71. $\begin{bmatrix} 8 & -7 & 4 & \vdots & 12 \\ 3 & -5 & 2 & \vdots & 20 \\ 5 & 3 & -3 & \vdots & 26 \end{bmatrix}$

73. $\begin{cases} 5x + y + 7z = -9 \\ 4x + 2y = 10 \\ 9x + 4y + 2z = 3 \end{cases}$ 75. $\begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$

77. $\begin{bmatrix} 1 & 0 & 3 & -2 \\ 0 & 1 & 4 & -3 \end{bmatrix}$ 79. $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

81. (10, -12) 83. (-0.2, 0.7) 85. $(\frac{1}{2}, -\frac{1}{3}, 1)$

87. $(3a + 1, -a, a)$ 89. (2, -3, 3) 91. $(1, 2, \frac{1}{2})$

93. (1, 2, 2) 95. (3, 0, -4) 97. (2, 6, -10, -3)

99. $x = 12, y = -7$ 101. $x = 1, y = 11$

103. (a) $\begin{bmatrix} 17 & -17 \\ 13 & 2 \end{bmatrix}$ (b) $\begin{bmatrix} -3 & 23 \\ -15 & 8 \end{bmatrix}$

(c) $\begin{bmatrix} 14 & 6 \\ -2 & 10 \end{bmatrix}$ (d) $\begin{bmatrix} 37 & -57 \\ 41 & -4 \end{bmatrix}$

105. (a) $\begin{bmatrix} 6 & 5 & 8 \\ 1 & 7 & 8 \\ 5 & 1 & 4 \end{bmatrix}$ (b) $\begin{bmatrix} 6 & -5 & 6 \\ 9 & -9 & -4 \\ 1 & 3 & 2 \end{bmatrix}$

(c) $\begin{bmatrix} 12 & 0 & 14 \\ 10 & -2 & 4 \\ 6 & 4 & 6 \end{bmatrix}$ (d) $\begin{bmatrix} 6 & 15 & 10 \\ -7 & 23 & 20 \\ 9 & -1 & 6 \end{bmatrix}$

107. $\begin{bmatrix} -13 & -8 & 18 \\ 0 & 11 & -19 \end{bmatrix}$ 109. $\begin{bmatrix} 9 & -7 \\ -9 & 4 \end{bmatrix}$

111. $\begin{bmatrix} 48 & -18 & -3 \\ 15 & 51 & 33 \end{bmatrix}$ 113. $\begin{bmatrix} -8 & -4 \\ 7 & -17 \\ -17 & -2 \end{bmatrix}$

115. $\frac{1}{3} \begin{bmatrix} 6 & 2 \\ -4 & 11 \\ 10 & 0 \end{bmatrix}$ 117. $\begin{bmatrix} 14 & -2 & 8 \\ 14 & -10 & 40 \\ 36 & -12 & 48 \end{bmatrix}$

119. [30] 121. $\begin{bmatrix} 14 & -22 & 22 \\ 19 & -41 & 80 \\ 42 & -66 & 66 \end{bmatrix}$ 123. $\begin{bmatrix} 1 & 17 \\ 12 & 36 \end{bmatrix}$

125. (a) $\begin{bmatrix} 525.88 & 47.40 \\ 734.94 & 66.20 \\ 861.76 & 77.20 \end{bmatrix}$

The entries represent the dairy mart's sales and profits on milk for Friday, Saturday, and Sunday.

(b) \$190.80

127. Answers will vary. 129. $\begin{bmatrix} 4 & -5 \\ 5 & -6 \end{bmatrix}$

131. $\begin{bmatrix} \frac{1}{2} & -1 & -\frac{1}{2} \\ \frac{1}{2} & -\frac{2}{3} & -\frac{5}{6} \\ 0 & \frac{2}{3} & \frac{1}{3} \end{bmatrix}$ 133. $\begin{bmatrix} \frac{1}{5} & \frac{1}{5} \\ \frac{1}{10} & -\frac{1}{15} \end{bmatrix}$

135. $\begin{bmatrix} 1 & 0 & 2 \\ 0 & 0 & -1 \\ 1 & 1 & 3 \end{bmatrix}$ 137. $\begin{bmatrix} 1 & -1 \\ 4 & -\frac{7}{2} \end{bmatrix}$ 139. $\begin{bmatrix} -\frac{1}{2} & \frac{1}{4} \\ \frac{1}{20} & \frac{1}{40} \end{bmatrix}$

141. (36, 11) 143. (2, -1, -2) 145. (1, -2, 1, 0)

147. (-3, 1) 149. (1, 1, -2) 151. -42 153. 550

155. (a) $M_{11} = 4, M_{12} = 7, M_{21} = -1, M_{22} = 2$

(b) $C_{11} = 4, C_{12} = -7, C_{21} = 1, C_{22} = 2$

157. (a) $M_{11} = 30, M_{12} = -12, M_{13} = -21, M_{21} = 20,$

$M_{22} = 19, M_{23} = 22, M_{31} = 5, M_{32} = -2,$

$M_{33} = 19$

(b) $C_{11} = 30, C_{12} = 12, C_{13} = -21, C_{21} = -20,$

$C_{22} = 19, C_{23} = -22, C_{31} = 5, C_{32} = 2, C_{33} = 19$

159. 130 161. 6 163. -3 165. 279 167. 16

169. 1.75 171. $\frac{13}{2}$ 173. 48 175. Collinear

177. (1, 2) 179. (4, 7) 181. (-1, 4, 5)

183. (0, -2.4, -2.6) 185. (a) and (b) $(\frac{53}{33}, -\frac{17}{33}, \frac{61}{66})$

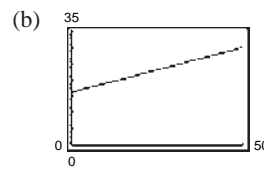
187. (a) $[12 \ 15 \ 15], [11 \ 0 \ 15], [21 \ 20 \ 0],$
 $[2 \ 5 \ 12], [15 \ 23 \ 0]$

(b) -21 6 0 -68 8 45 102 -42 -60 -53

20 21 99 -30 -69

189. I WILL BE BACK 191. THAT IS MY FINAL ANSWER

193. (a) $y = 0.275t + 16.2$



(c) and (d) $t \approx 13.8$ or 2013

195. True. This is the correct sum of the two determinants.

197. An $n \times n$ matrix A has an inverse A^{-1} if $\det(A) \neq 0$.

Chapter Test (page 566)

1. (4, -2) 2. (0, -1), (1, 0), (2, 1)

3. (8, 5), (2, -1) 4. $(\frac{28}{9}, -\frac{31}{9})$ 5. $(-\frac{2}{3}, -\frac{1}{2}, 1)$

6. (1, 0, -2) 7. $y = -\frac{1}{2}x^2 + x + 6$

8. $\frac{5}{x-1} + \frac{3}{(x-1)^2}$ 9. $\frac{1}{x} + \frac{2}{x^2} - \frac{1}{x^2+1}$

10. $(-2a + 1.5, 2a + 1, a)$ 11. (5, 2, -6)

12. (a) $\begin{bmatrix} 1 & 0 & 4 \\ -7 & -6 & -1 \\ 0 & 4 & 0 \end{bmatrix}$ (b) $\begin{bmatrix} 15 & 12 & 12 \\ -12 & -12 & 0 \\ 3 & 6 & 0 \end{bmatrix}$

(c) $\begin{bmatrix} 7 & 6 & 12 \\ -18 & -16 & -2 \\ 1 & 10 & 0 \end{bmatrix}$ (d) $\begin{bmatrix} 36 & 20 & 4 \\ -28 & -24 & -4 \\ 10 & 8 & 2 \end{bmatrix}$

13. $\begin{bmatrix} -\frac{4}{3} & -\frac{5}{3} & 1 \\ -\frac{4}{3} & -\frac{8}{3} & 1 \\ \frac{1}{3} & \frac{2}{3} & 0 \end{bmatrix}, (-2, 3, -1)$ 14. 67 15. -2

16. 30 17. $(1, -\frac{1}{2})$

18. $x_1 = 700 - s - t, x_2 = 300 - s - t,$

$x_3 = s, x_4 = 100 - t, x_5 = t$

Chapter 8

Section 8.1 (page 577)

1. terms 3. index, upper limit, lower limit

5. (a) Finite sequence (b) Infinite sequence

7. 7, 9, 11, 13, 15 9. 3, 9, 27, 81, 243

11. $-\frac{1}{2}, \frac{1}{4}, -\frac{1}{8}, \frac{1}{16}, -\frac{1}{32}$ 13. $2, \frac{3}{2}, \frac{4}{3}, \frac{5}{4}, \frac{6}{5}$ 15. $\frac{1}{2}, \frac{2}{5}, \frac{3}{10}, \frac{4}{17}, \frac{5}{26}$

17. (a) 0, 1, 0, 0.5, 0 (b) 0, 1, 0, $\frac{1}{2}, 0$

19. (a) 0.5, 0.75, 0.875, 0.938, 0.969 (b) $\frac{1}{2}, \frac{3}{4}, \frac{7}{8}, \frac{15}{16}, \frac{31}{32}$

21. (a) 1, 0.354, 0.192, 0.125, 0.089 (b) $1, \frac{1}{2^{3/2}}, \frac{1}{3^{3/2}}, \frac{1}{8}, \frac{1}{5^{3/2}}$

23. (a) -1, 0.25, -0.111, 0.063, -0.04

(b) $-1, \frac{1}{4}, -\frac{1}{9}, \frac{1}{16}, -\frac{1}{25}$

25. (a) and (b) 3, 15, 35, 63, 99

27. 9, 15, 21, 27, 33, 39, 45, 51, 57, 63

29. $3, \frac{5}{2}, \frac{7}{3}, \frac{9}{4}, \frac{11}{5}, \frac{13}{6}, \frac{15}{7}, \frac{17}{8}, \frac{19}{9}, \frac{21}{10}$

31. 0, 2, 0, 2, 0, 2, 0, 2, 0, 2 33. $\frac{100}{101}$ 35. -73

37. $\frac{64}{65}$ 39. $a_n = 3n - 2$ 41. $a_n = n^2 - 1$

43. $a_n = \frac{n+1}{n+2}$ 45. $a_n = \frac{(-1)^{n+1}}{2^n}$ 47. $a_n = 1 + \frac{1}{n}$

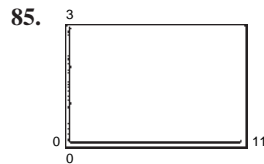
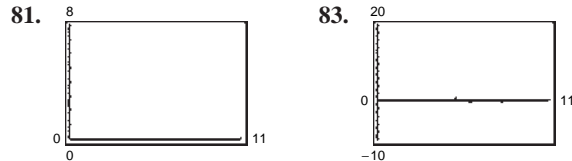
49. $a_n = \frac{1}{n!}$ 51. $a_n = (-1)^n + 2(1)^n = (-1)^n + 2$

53. 28, 24, 20, 16, 12 55. 3, 4, 6, 10, 18
 57. 1, 3, 4, 7, 11 59. 6, 8, 10, 12, 14; $a_n = 2n + 4$

61. 81, 27, 9, 3, 1; $a_n = \frac{243}{3^n}$
 63. (a) 1, 1, 0.5, 0.167, 0.042 (b) $1, 1, \frac{1}{2}, \frac{1}{6}, \frac{1}{24}$
 65. (a) 1, 0.333, 0.4, 0.857, 2.667 (b) $1, \frac{1}{3}, \frac{2}{5}, \frac{6}{7}, \frac{8}{3}$
 67. (a) 1, 0.5, 0.042, 0.001, 2.480×10^{-5}
 (b) $1, \frac{1}{2}, \frac{1}{24}, \frac{1}{720}, \frac{1}{40,320}$

69. $\frac{1}{12}$ 71. 495 73. $n + 1$ 75. $\frac{1}{2n(2n+1)}$

77. c 78. b 79. d 80. a



87. 35 89. 40 91. 30 93. $\frac{9}{5}$ 95. 238

97. 30 99. 81 101. $\frac{47}{60}$

103. $\sum_{i=1}^9 \frac{1}{3i} \approx 0.94299$ 105. $\sum_{i=1}^8 \left[2\left(\frac{i}{8}\right) + 3 \right] = 33$

107. $\sum_{i=1}^6 (-1)^{i+1} 3^i = -546$ 109. $\sum_{i=1}^{20} \frac{(-1)^{i+1}}{i^2} \approx 0.821$

111. $\sum_{i=1}^5 \frac{2^i - 1}{2^{i+1}} \approx 2.0156$ 113. $\frac{75}{16}$ 115. $-\frac{3}{2}$

117. (a) $\frac{3333}{5000}$ (b) $\frac{2}{3}$ 119. (a) $\frac{1111}{10,000}$ (b) $\frac{1}{9}$

121. (a) $A_1 = \$5037.50$, $A_2 = \$5075.28$,
 $A_3 = \$5113.35$, $A_4 = \$5151.70$,
 $A_5 = \$5190.33$, $A_6 = \$5229.26$,
 $A_7 = \$5268.48$, $A_8 = \$5307.99$
 (b) \$6741.74

123. \$72,443 million 125. True by the Properties of Sums

127. 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144;
 $1, 2, \frac{3}{2}, \frac{5}{3}, \frac{8}{5}, \frac{13}{8}, \frac{21}{13}, \frac{34}{21}, \frac{55}{34}, \frac{89}{55}$

129. 1, 1, 2, 3, 5

131. $a_{n+1} = \frac{1}{2}a_n + \frac{(1 + \sqrt{5})^n + (1 - \sqrt{5})^n}{2^{n+1}}$
 $a_{n+2} = \frac{3}{2}a_n + \frac{(1 + \sqrt{5})^n + (1 - \sqrt{5})^n}{2^{n+1}}$

133. $x, \frac{x^2}{2}, \frac{x^3}{6}, \frac{x^4}{24}, \frac{x^5}{120}$ 135. $-\frac{x^3}{3}, \frac{x^5}{5}, -\frac{x^7}{7}, \frac{x^9}{9}, -\frac{x^{11}}{11}$

137. $-\frac{x^2}{2}, \frac{x^4}{24}, -\frac{x^6}{720}, \frac{x^8}{40,320}, -\frac{x^{10}}{3,628,800}$

139. $-x, \frac{x^2}{2}, -\frac{x^3}{6}, \frac{x^4}{24}, -\frac{x^5}{120}$

141. $x + 1, -\frac{(x+1)^2}{2}, \frac{(x+1)^3}{6}, -\frac{(x+1)^4}{24}, \frac{(x+1)^5}{120}$

143. $\frac{1}{4}, \frac{1}{12}, \frac{1}{24}, \frac{1}{40}, \frac{1}{60}, \frac{1}{2} - \frac{1}{2n+2}$

145. $\frac{1}{6}, \frac{1}{12}, \frac{1}{20}, \frac{1}{30}, \frac{1}{42}, \frac{1}{2} - \frac{1}{n+2}$

147. Yes, if there is a finite number of integer terms, you can always find a sum.

149. (a) $\begin{bmatrix} 8 & 1 \\ -3 & 7 \end{bmatrix}$ (b) $\begin{bmatrix} -22 & -7 \\ 3 & -18 \end{bmatrix}$

- (c) $\begin{bmatrix} 18 & 9 \\ 18 & 0 \end{bmatrix}$ (d) $\begin{bmatrix} 0 & 6 \\ 27 & 18 \end{bmatrix}$

151. (a) $\begin{bmatrix} -3 & -7 & 4 \\ 4 & 4 & 1 \\ 1 & 4 & 3 \end{bmatrix}$ (b) $\begin{bmatrix} 8 & 17 & -14 \\ -12 & -13 & -9 \\ -3 & -15 & -10 \end{bmatrix}$

- (c) $\begin{bmatrix} -2 & 7 & -16 \\ 4 & 42 & 45 \\ 1 & 23 & 48 \end{bmatrix}$ (d) $\begin{bmatrix} 16 & 31 & 42 \\ 10 & 47 & 31 \\ 13 & 22 & 25 \end{bmatrix}$

Section 8.2 (page 586)

1. $a_n = a_1 + (n-1)d$

3. A sequence is arithmetic when the differences between consecutive terms are the same.

5. Arithmetic sequence, $d = -2$

7. Arithmetic sequence, $d = -\frac{1}{2}$

9. Arithmetic sequence, $d = 0.6$

11. 21, 34, 47, 60, 73

- Arithmetic sequence, $d = 13$

13. $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \frac{1}{5}, \frac{1}{6}$

- Not an arithmetic sequence

15. 143, 136, 129, 122, 115

- Arithmetic sequence, $d = -7$

17. 1, 5, 1, 5, 1

- Not an arithmetic sequence

19. -1, 1, -1, 1, -1

- Not an arithmetic sequence

21. $a_n = -2 + 3n$ 23. $a_n = 108 - 8n$

25. $a_n = \frac{13}{2} - \frac{5}{2}n$ 27. $a_n = \frac{10}{3}n + \frac{5}{3}$

29. $a_n = 103 - 3n$ 31. 5, 11, 17, 23, 29

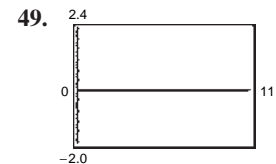
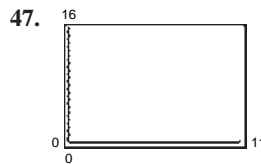
33. -10, -22, -34, -46, -58 35. -2, 2, 6, 10, 14

37. 22.45, 20.725, 19, 17.275, 15.55

39. 15, 19, 23, 27, 31; $d = 4$; $a_n = 11 + 4n$

41. $\frac{3}{5}, \frac{1}{2}, \frac{2}{5}, \frac{3}{10}, \frac{1}{5}$; $d = -\frac{1}{10}$; $a_n = -\frac{1}{10}n + \frac{7}{10}$

43. 59 45. 18.6



51. -1, 3, 7, 11, 15, 19, 23, 27, 31, 35

53. 19.25, 18.5, 17.75, 17, 16.25, 15.5, 14.75, 14, 13.25, 12.5

55. 1.55, 1.6, 1.65, 1.7, 1.75, 1.8, 1.85, 1.9, 1.95, 2

57. 110 59. -25 61. 5050 63. -4585

65. 620 67. 41 69. 4000 71. 1275

73. 355 75. 129,250 77. 440 79. 2575

81. 14,268 83. 405 bricks 85. \$200,000

87. (a) $a_n = 0.84n + 14.9$

(b)	Year	2001	2002	2003	2004
	Sales (in billions of dollars)	15.7	16.6	17.4	18.3

Year	2005	2006	2007	2008
Sales (in billions of dollars)	19.1	19.9	20.8	21.6

The model fits the data well.

(c) \$149.5 billion (d) \$203.2 billion; Answers will vary.

89. True. Use the recursion formula, $a_{n+1} = a_n + d$.

91. $x, 3x, 5x, 7x, 9x, 11x, 13x, 15x, 17x, 19x$

93. 4 95. $S_n + 5n$

97. Answers will vary. Sample answer: Gauss saw that the sum of the first and last numbers was 101, the sum of the second and second-last numbers was 101, and so on. Seeing that there were 50 such pairs of numbers, Gauss simply multiplied 50 by 101 to get the summation 5050.

$a_n = (n+1)\left(\frac{n}{2}\right)$, where n is the total number of natural numbers.

99. 20,100 101. 2601

103. (1, 5, -1) 105. Answers will vary.

Section 8.3 (page 595)

1. geometric, common 3. geometric series 5. $|r| < 1$

7. Geometric sequence, $r = 3$ 9. Not a geometric sequence

11. Geometric sequence, $r = -\frac{1}{2}$

13. Geometric sequence, $r = 2$

15. Not a geometric sequence 17. 6, 18, 54, 162, 486

19. $1, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}$ 21. $5, -\frac{1}{2}, \frac{1}{20}, -\frac{1}{200}, \frac{1}{2000}$

23. $1, e, e^2, e^3, e^4$ 25. 64, 32, 16, 8, 4; $r = \frac{1}{2}$; $a_n = 64\left(\frac{1}{2}\right)^{n-1}$

27. 9, 18, 36, 72, 144; $r = 2$; $a_n = 9(2)^{n-1}$

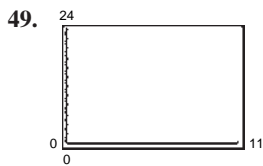
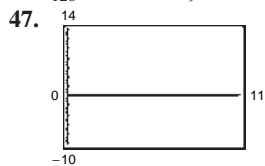
29. 6, -9, $\frac{27}{2}, -\frac{81}{4}, \frac{243}{8}$; $r = -\frac{3}{2}$; $a_n = 6\left(-\frac{3}{2}\right)^{n-1}$

31. (a) 0.000034 (b) $\frac{2}{59,049}$ 33. (a) 44.949 (b) $\frac{32,768}{729}$

35. (a) and (b) -243 37. (a) and (b) -646.803

39. $a_n = 7(3)^{n-1}$; 45,927 41. $a_n = 5(6)^{n-1}$; 50,388,480

43. $\frac{1}{128}$ 45. $-\frac{2}{9}$



51. 8, 4, 6, 5, $\frac{11}{2}$

n	S_n
1	16
2	24
3	28
4	30
5	31
6	31.5
7	31.75
8	31.875
9	31.9375
10	31.96875

53.

55. 511 57. 43 59. 29,921.31 61. 6.4

63. 2092.60 65. $\sum_{n=1}^7 5(3)^{n-1}$ 67. $\sum_{n=1}^7 2\left(-\frac{1}{4}\right)^{n-1}$

69. 50 71. $\frac{10}{3}$

73. Series does not have a finite sum because $\left|\frac{7}{3}\right| > 1$.

75. $\frac{1000}{89}$ 77. $-\frac{30}{19}$ 79. 27 81. $\frac{9}{4}$ 83. $\frac{4}{11}$ 85. $\frac{113}{90}$

87. Geometric; $r = 2$; 262,136 89. Geometric; $r = \frac{1}{3}$; 135

91. Arithmetic; $d = 6$; 720 93. Geometric; $r = 0.8$; 28,944

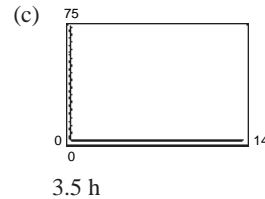
95. (a) \$1343.92 (b) \$1346.86 (c) \$1348.35

(d) \$1349.35 (e) \$1349.84

97. Answers will vary. 99. (a) \$26,198.27 (b) \$26,263.88

101. (a) \$153,237.86 (b) \$153,657.02 103. 126 in.²

105. (a) $T_n = 70(0.8)^n$ (b) 18.4°F; 4.8°F



107. (a) $a_n = 1269.10(1.006)^n$

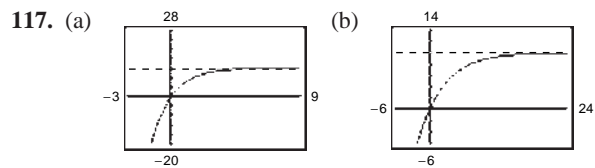
(b) The population is growing at a rate of 0.6% per year.

(c) 1388.2 million. This value is close to the prediction.

(d) 2010

109. 42 ft 111. True. The terms all equal a_1 .

113. $3, \frac{3x}{2}, \frac{3x^2}{4}, \frac{3x^3}{8}, \frac{3x^4}{16}$ 115. $100e^{8x}$



Horizontal asymptote:
 $y = 12$

Corresponds to the sum
of the series

Horizontal asymptote:
 $y = 10$

Corresponds to the sum of
the series.

119. Divide the second term by the first to obtain the common ratio. The n th term is the first term times the common ratio raised to the $(n-1)$ th power.

121. 45.65 mi/h 123. -102 125. Answers will vary.

Section 8.4 (page 604)

1. ${}_nC_r$ or $\binom{n}{r}$ 3. Binomial Theorem, Pascal's Triangle

5. 21 7. 15,504 9. 14 11. 1 13. 210

15. 4950 17. 749,398 19. 1225 21. 31,125

23. $x^4 + 8x^3 + 24x^2 + 32x + 16$

25. $a^3 + 9a^2 + 27a + 27$ 27. $y^3 - 12y^2 + 48y - 64$

29. $x^5 + 5x^4y + 10x^3y^2 + 10x^2y^3 + 5xy^4 + y^5$

31. $r^6 + 18r^5s + 135r^4s^2 + 540r^3s^3 + 1215r^2s^4$
 $+ 1458rs^5 + 729s^6$

33. $x^5 - 5x^4y + 10x^3y^2 - 10x^2y^3 + 5xy^4 - y^5$

35. $1 - 12x + 48x^2 - 64x^3$

37. $x^8 + 8x^6 + 24x^4 + 32x^2 + 16$

39. $x^{10} - 25x^8 + 250x^6 - 1250x^4 + 3125x^2 - 3125$

41. $x^8 + 4x^6y^2 + 6x^4y^4 + 4x^2y^6 + y^8$

43. $x^{18} - 6x^{15}y + 15x^{12}y^2 - 20x^9y^3 + 15x^6y^4 - 6x^3y^5 + y^6$

45. $\frac{1}{x^5} + \frac{5y}{x^4} + \frac{10y^2}{x^3} + \frac{10y^3}{x^2} + \frac{5y^4}{x} + y^5$

47. $\frac{16}{x^4} - \frac{32y}{x^3} + \frac{24y^2}{x^2} - \frac{8y^3}{x} + y^4$

49. $-512x^4 + 576x^3 - 240x^2 + 44x - 3$

51. $2x^4 - 24x^3 + 113x^2 - 246x + 207$

53. $-4x^6 - 24x^5 - 60x^4 - 83x^3 - 42x^2 - 60x + 20$

55. $61,440x^7$ 57. $360x^3y^2$ 59. $1,259,712x^2y^7$

61. $-4,330,260,000x^3y^9$ 63. $1,737,104$ 65. 180

67. $-489,888$ 69. 210 71. 35 73. 6

75. $81t^4 - 216t^3v + 216t^2v^2 - 96tv^3 + 16v^4$

77. $32x^5 - 240x^4y + 720x^3y^2 - 1080x^2y^3 + 810xy^4 - 243y^5$

79. $x^5 + 10x^4y + 40x^3y^2 + 80x^2y^3 + 80xy^4 + 32y^5$

81. $x^{3/2} + 15x + 75\sqrt{x} + 125$

83. $x^2 - 3x^{4/3}y^{1/3} + 3x^{2/3}y^{2/3} - y$

85. $3x^2 + 3xh + h^2, h \neq 0$

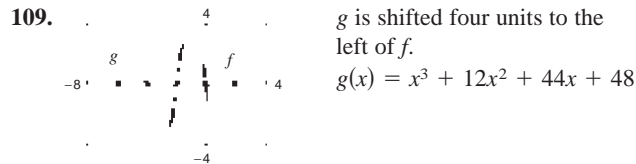
87. $6x^5 + 15x^4h + 20x^3h^2 + 15x^2h^3 + 6xh^4 + h^5, h \neq 0$

89. $\frac{\sqrt{x+h} - \sqrt{x}}{h} = \frac{1}{\sqrt{x+h} + \sqrt{x}}, h \neq 0$

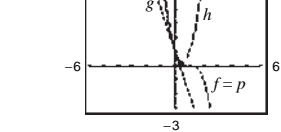
91. -4 93. $161 + 240i$ 95. $2035 + 828i$

97. $-115 + 236i$ 99. $-23 + 208\sqrt{3}i$ 101. 1

103. $-\frac{1}{8}$ 105. 1.172 107. $510,568.785$

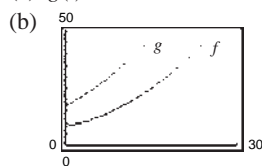


111. $p(x)$ is the expansion of $f(x)$.



113. 0.273 115. 0.171

117. (a) $g(t) = 0.044t^2 + 1.32t + 17.1$



119. True. Pascal's Triangle is made up of binomial coefficients.

121. False. The correct term is $126,720x^4y^8$. 123. $n + 1$ terms

125. (a) $5(2x)^4(-3y)^1 = -240x^4y$

(b) ${}_6C_3(\frac{1}{2}x)^3(7y)^3 = 857.5x^3y^3$

127 and 129. Answers will vary. 131. $\begin{bmatrix} 1 & 2 \\ -0.5 & -0.5 \end{bmatrix}$

Section 8.5 (page 613)

1. Fundamental Counting Principle 3. Permutation

5. 8 7. 6 9. 11 11. 10 13. 120

15. 1024 17. (a) 900 (b) 648 (c) 180

19. 16,000,000 21. (a) 35,152 (b) 3902

23. (a) 100,000 (b) 20,000 25. (a) 720 (b) 48

27. 24 29. 336 31. 120 33. 27,907,200

35. 197,149,680 37. 120 39. 362,880 41. 11,880

43. 50,653

45. ABCD, ABDC, ACBD, ACDB, ADBC, ADCB, BACD, BADC, CABD, CADB, DABC, DACB, BCAD, BDAC, CBAD, CDAB, DBAC, DCAB, BCDA, BDCA, CBDA, CDBA, DBCA, DCBA

47. 420 49. 2520 51. 10 53. 4 55. 1

57. 15,504 59. 850,668

61. AB, AC, AD, AE, AF, BC, BD, BE, BF, CD, CE, CF, DE, DF, EF

63. 2.53×10^{17} 65. 195,249,054

67. (a) 17,550 (b) 1053 (c) 27,378 69. 24

71. 462,000 73. 5 75. 20 77. $n = 5$ or $n = 6$

79. $n = 10$ 81. $n = 3$ 83. $n = 2$

85. False. 87. For some calculators the answer is too large.

89. ${}_nP_r$ represents the number of ways to choose and order r elements out of a collection of n elements.

91 and 93. Answers will vary. 95. 35 97. $(-2, -8)$

Section 8.6 (page 622)

1. sample space 3. mutually exclusive

5. $0 \leq P(E) \leq 1$ 7. $P(E) = 1$

9. $\{(H, 1), (H, 2), (H, 3), (H, 4), (H, 5), (H, 6), (T, 1), (T, 2), (T, 3), (T, 4), (T, 5), (T, 6)\}$

11. $\{ABC, ACB, BAC, BCA, CAB, CBA\}$ 13. $\frac{3}{8}$ 15. $\frac{7}{8}$

17. $\frac{3}{13}$ 19. $\frac{3}{52}$ 21. $\frac{5}{36}$ 23. $\frac{11}{12}$ 25. $\frac{3}{100}$ 27. $\frac{9}{25}$

29. $\frac{1}{5}$ 31. $\frac{2}{5}$ 33. 0.25 35. $\frac{1}{3}$ 37. 0.88 39. $\frac{7}{20}$

41. $\frac{4}{13}$ 43. $\frac{4}{13}$ 45. $\frac{9}{16}$ 47. $\frac{3}{32}$ 49. $\frac{1}{8}$ 51. $\frac{2}{125}$

53. $P(\{\text{Taylor wins}\}) = \frac{1}{2}$

$P(\{\text{Moore wins}\}) = P(\{\text{Perez wins}\}) = \frac{1}{4}$

55. (a) 20.22 million (b) 0.294 (c) 0.866

57. (a) $\frac{1}{120}$ (b) $\frac{1}{24}$ 59. (a) $\frac{14}{55}$ (b) $\frac{12}{55}$ (c) $\frac{54}{55}$

61. 0.1024 63. (a) $\frac{1}{15,625}$ (b) $\frac{4096}{15,625}$ (c) $\frac{11,529}{15,625}$

65. (a) $\frac{\pi}{4}$ (b) Answers will vary.

67. True. The sum of the probabilities of all outcomes must be 1.

69. (a) As you consider successive people with distinct birthdays, the probabilities must decrease to take into account the birth dates already used. Because the birth dates of people are independent events, multiply the respective probabilities of distinct birthdays.

(b) $\frac{365}{365} \cdot \frac{364}{365} \cdot \frac{363}{365} \cdot \frac{362}{365}$

(c) Answers will vary.

(d) Q_n is the probability that the birthdays are *not* distinct, which is equivalent to at least two people having the same birthday.

n	10	15	20	23	30	40	50
P_n	0.88	0.75	0.59	0.49	0.29	0.11	0.03
Q_n	0.12	0.25	0.41	0.51	0.71	0.89	0.97

(f) 23

71. (a) No. $P(A) + P(B) = 0.76 + 0.58 = 1.34 > 1$. The sum of the probabilities is greater than 1, so A and B cannot be mutually exclusive.

(b) Yes. $A' = 0.24$, $B' = 0.42$, and $A' + B' = 0.66 < 1$, so A' and B' can be mutually exclusive.

(c) $0.76 \leq P(A \cup B) \leq 1$

73. 15 75. 165

Review Exercises (page 628)

1. $\frac{2}{3}, \frac{4}{5}, \frac{8}{9}, \frac{16}{17}, \frac{32}{33}$
3. $a_n = 5n$
5. $a_n = \frac{2}{2n-1}$
7. 9, 5, 1, -3, -7
9. $\frac{1}{380}$
11. $(n+1)(n)$
13. 30
15. $\frac{205}{24}$
17. $\sum_{k=1}^{20} \frac{1}{2k} \approx 1.799$
19. $\sum_{k=1}^9 \frac{k}{k+1} \approx 7.071$
21. (a) $\frac{1111}{2000}$ (b) $\frac{5}{9}$
23. (a) $\frac{15}{8}$ (b) 2
25. (a) 3015.00, 3030.08, 3045.23, 3060.45, 3075.75, 3091.13, 3106.59, 3122.12
(b) \$3662.38
27. Arithmetic sequence, $d = -2$
29. Arithmetic sequence, $d = \frac{1}{2}$
31. 3, 7, 11, 15, 19
33. 1, 4, 7, 10, 13
35. 35, 32, 29, 26, 23; $d = -3$; $a_n = 38 - 3n$
37. $a_n = 103 - 3n$; 1600
39. 80
41. 6375
43. (a) \$45,000 (b) \$202,500
45. Geometric sequence, $r = 2$
47. Geometric sequence, $r = -\frac{1}{3}$
49. 4, -1, $\frac{1}{4}$, $-\frac{1}{16}$, $\frac{1}{64}$
51. 9, 6, 4, $\frac{8}{3}$, $\frac{16}{9}$ or 9, -6, 4, $-\frac{8}{3}$, $\frac{16}{9}$
53. 120, 40, $\frac{40}{3}$, $\frac{40}{9}$, $\frac{40}{27}$; $r = \frac{1}{3}$; $a_n = 120(\frac{1}{3})^{n-1}$
55. (a) $-\frac{1}{2}$ (b) -0.5
57. 127
59. 3277
61. 32
63. 12
65. (a) $a_t = 130,000(0.7)^t$ (b) \$21,849.10
67. 45
69. 126
71. $x^4 + 20x^3 + 150x^2 + 500x + 625$
73. $a^5 - 20a^4b + 160a^3b^2 - 640a^2b^3 + 1280ab^4 - 1024b^5$
75. 20
77. 70
79. 10
81. (a) 216 (b) 108 (c) 36
83. 239,500,800
85. 5040
87. $n = 3$
89. 28
91. 479,001,600
93. $\frac{1}{9}$
95. (a) 0.416 (b) 0.8 (c) 0.074
97. True. $\frac{(n+2)!}{n!} = \frac{(n+2)(n+1)n!}{n!} = (n+2)(n+1)$
99. (a) Each term is obtained by adding the same constant (common difference) to the preceding term.
(b) Each term is obtained by multiplying the same constant (common ratio) by the preceding term.

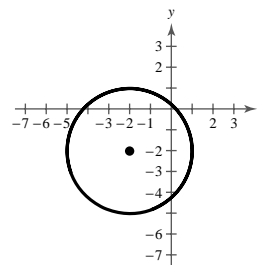
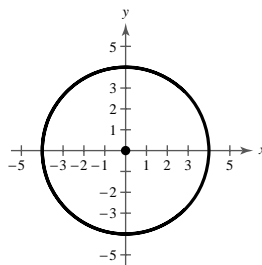
Chapter Test (page 631)

1. $1, -\frac{2}{3}, \frac{4}{9}, -\frac{8}{27}, \frac{16}{81}$
2. 12, 16, 20, 24, 28
3. $-x, \frac{x^2}{2}, -\frac{x^3}{3}, \frac{x^4}{4}, -\frac{x^5}{5}$
4. $-\frac{x^3}{6}, -\frac{x^5}{120}, -\frac{x^7}{5040}, -\frac{x^9}{362,880}, -\frac{x^{11}}{39,916,800}$
5. 7920
6. $\frac{1}{n+1}$
7. $2n$
8. $a_n = n^2 + 1$
9. $a_n = 5100 - 100n$
10. $a_n = 4(\frac{1}{2})^{n-1}$
11. $\sum_{n=1}^{12} \frac{2}{3n+1}$
12. $\sum_{n=1}^{\infty} 2(\frac{1}{4})^{n-1}$
13. 189
14. 28.80
15. $\frac{25}{7}$
16. $16a^4 - 160a^3b + 600a^2b^2 - 1000ab^3 + 625b^4$
17. 84
18. 1140
19. 72
20. 328,440
21. $n = 3$
22. 26,000
23. 12,650
24. $\frac{3}{26}$
25. $\frac{1}{462}$
26. (a) $\frac{1}{4}$ (b) $\frac{121}{3600}$ (c) $\frac{1}{60}$
27. 0.25

Chapter 9

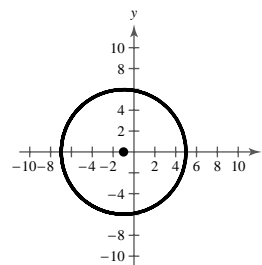
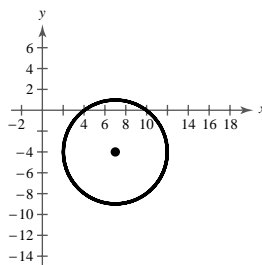
Section 9.1 (page 643)

1. conic section
3. circle, center
5. The standard form of the equation of a circle; (h, k) represents the center of the circle, r represents the radius of the circle.
7. $x^2 + y^2 = 16$
9. $(x-3)^2 + (y-7)^2 = 53$
11. $(x+3)^2 + (y+1)^2 = 7$
13. Center: (0, 0)
Radius: 7
15. Center: (-2, 7)
Radius: 4
17. Center: (1, 0)
Radius: $\sqrt{15}$
19. $x^2 + y^2 = 4$
Center: (0, 0)
Radius: 2
21. $x^2 + y^2 = \frac{3}{4}$
Center: (0, 0)
Radius: $\frac{\sqrt{3}}{2}$
23. $(x-1)^2 + (y+3)^2 = 1$
Center: (1, -3)
Radius: 1
25. $(x+\frac{3}{2})^2 + (y-3)^2 = 1$
Center: $(-\frac{3}{2}, 3)$
Radius: 1
27. Center: (0, 0)
Radius: 4
29. Center: (-2, -2)
Radius: 3



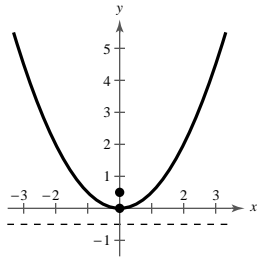
31. Center: (7, -4)
Radius: 5

33. Center: (-1, 0)
Radius: 6

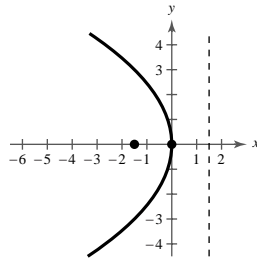


35. x-intercept: (2, 0)
y-intercepts: $(0, -3 \pm \sqrt{5})$
37. x-intercepts: $(1 \pm 2\sqrt{7}, 0)$
y-intercepts: (0, 9), (0, -3)
39. x-intercepts: $(6 \pm \sqrt{7}, 0)$
y-intercept: none
41. (a) $x^2 + y^2 = 2704$ (b) Yes (c) 2 mi
43. e
44. b
45. d
46. f
47. a
48. c
49. $x^2 = \frac{3}{2}y$
51. $x^2 = -6y$
53. $y^2 = -8x$
55. $x^2 = -4y$
57. $y^2 = -8x$
59. $y^2 = 9x$

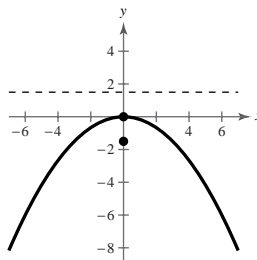
61. Vertex: $(0, 0)$
Focus: $(0, \frac{1}{2})$
Directrix: $y = -\frac{1}{2}$



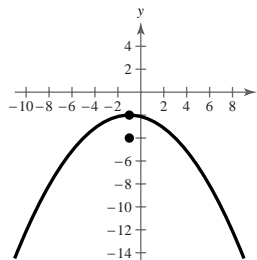
63. Vertex: $(0, 0)$
Focus: $(-\frac{3}{2}, 0)$
Directrix: $x = \frac{3}{2}$



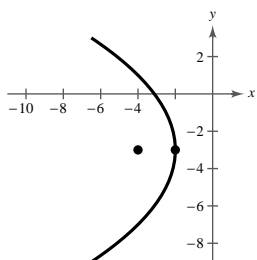
65. Vertex: $(0, 0)$
Focus: $(0, -\frac{3}{2})$
Directrix: $y = \frac{3}{2}$



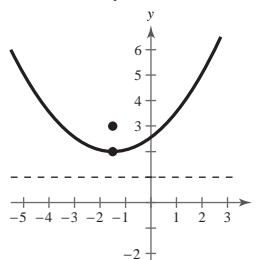
67. Vertex: $(-1, -2)$
Focus: $(-1, -4)$
Directrix: $y = 0$



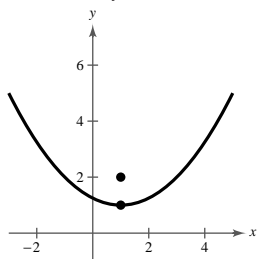
69. Vertex: $(-2, -3)$
Focus: $(-4, -3)$
Directrix: $x = 0$



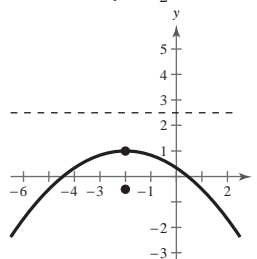
71. Vertex: $(-\frac{3}{2}, 2)$
Focus: $(-\frac{3}{2}, 3)$
Directrix: $y = 1$



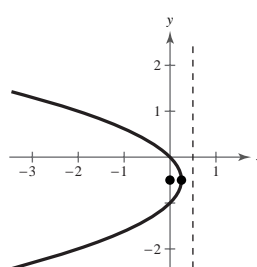
73. Vertex: $(1, 1)$
Focus: $(1, 2)$
Directrix: $y = 0$



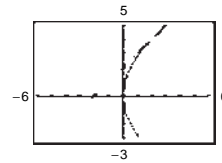
75. Vertex: $(-2, 1)$
Focus: $(-2, -\frac{1}{2})$
Directrix: $y = \frac{5}{2}$



77. Vertex: $(\frac{1}{4}, -\frac{1}{2})$
Focus: $(0, -\frac{1}{2})$
Directrix: $x = \frac{1}{2}$



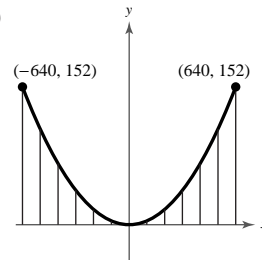
79. $(x - 3)^2 = -(y - 1)$ 81. $y^2 = 4(x + 4)$
83. $y^2 = 2(x + 2)$ 85. $(y - 2)^2 = -8(x - 5)$
87. $x^2 = 8(y - 4)$ 89. $(y - 2)^2 = 8x$
91.



$(2, 4)$

93. $4x - y - 8 = 0$; $(2, 0)$ 95. $4x - y + 2 = 0$; $(-\frac{1}{2}, 0)$
97. (a) $x^2 = 12,288y$ (in feet) (b) 22.6 ft
99. (a) $y^2 = 6x$ (b) 2.67 in.

101. (a) (b) $x^2 = \frac{51,200}{19}y$



(c)

x	0	200	400	500	600
y	0	14.844	59.375	92.773	133.59

103. $y^2 = 640x$ 105. (a) $x^2 = -49(y - 100)$ (b) 70 ft

107. $y = \frac{3}{4}x - \frac{25}{4}$ 109. $y = \frac{\sqrt{2}}{2}x - 3\sqrt{2}$

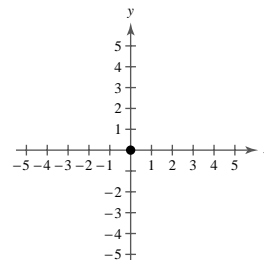
111. False. $x^2 + (y + 5)^2 = 25$ represents a circle with its center at $(0, -5)$ and a radius of 5.

113. False. A circle is a conic section.

115. True. The vertex is the closest point to the directrix or focus.

117. True. If the axis is horizontal, then the directrix must be vertical.

- 119.



The intersection results in a point.

121. $y = -\sqrt{2(x - 2)} - 1$

123. Minimum: $(-0.75, -1.13)$

125. Minimum: $(0.88, -3.11)$; maximum: $(-0.88, 1.11)$

Section 9.2 (page 653)

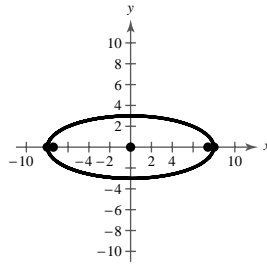
1. ellipse, foci 3. minor axis 5. Vertical 7. 4
9. b 10. c 11. a 12. d

13. Center: (0, 0)

Vertices: $(\pm 8, 0)$

Foci: $(\pm \sqrt{55}, 0)$

Eccentricity: $\frac{\sqrt{55}}{8}$

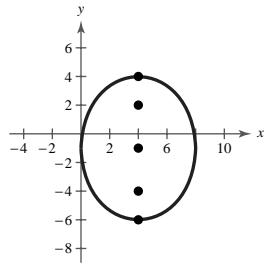


15. Center: (4, -1)

Vertices: (4, 4), (4, -6)

Foci: (4, 2), (4, -4)

Eccentricity: $\frac{3}{5}$

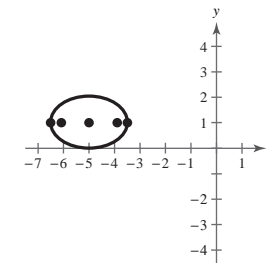


17. Center: (-5, 1)

Vertices: $(-\frac{7}{2}, 1)$, $(-\frac{13}{2}, 1)$

Foci: $(-5 \pm \frac{\sqrt{5}}{2}, 1)$

Eccentricity: $\frac{\sqrt{5}}{3}$



19. $\frac{x^2}{4} + \frac{y^2}{16} = 1$ 21. $\frac{x^2}{9} + \frac{y^2}{5} = 1$ 23. $\frac{x^2}{49} + \frac{y^2}{24} = 1$

25. $\frac{x^2}{400/21} + \frac{y^2}{25} = 1$ 27. $\frac{(x-2)^2}{1} + \frac{(y-3)^2}{9} = 1$

29. $\frac{(x-4)^2}{16} + \frac{(y-2)^2}{1} = 1$ 31. $\frac{x^2}{308} + \frac{(y-4)^2}{324} = 1$

33. $\frac{(x-3)^2}{9} + \frac{(y-5)^2}{16} = 1$ 35. $\frac{x^2}{16} + \frac{(y-4)^2}{12} = 1$

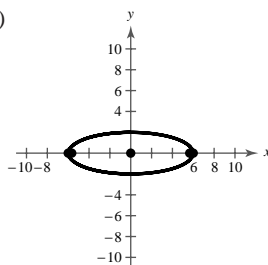
37. (a) $\frac{x^2}{36} + \frac{y^2}{4} = 1$ (c)

(b) Center: (0, 0)

Vertices: $(\pm 6, 0)$

Foci: $(\pm 4\sqrt{2}, 0)$

Eccentricity: $\frac{2\sqrt{2}}{3}$



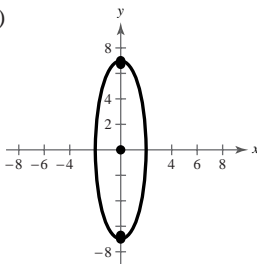
39. (a) $\frac{x^2}{4} + \frac{y^2}{49} = 1$ (c)

(b) Center: (0, 0)

Vertices: $(0, \pm 7)$

Foci: $(0, \pm 3\sqrt{5})$

Eccentricity: $\frac{3\sqrt{5}}{7}$



41. (a) $\frac{(x+2)^2}{4} + \frac{(y-3)^2}{9} = 1$

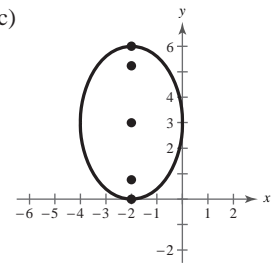
(b) Center: (-2, 3) (c)

Vertices:

$(-2, 6), (-2, 0)$

Foci: $(-2, 3 \pm \sqrt{5})$

Eccentricity: $\frac{\sqrt{5}}{3}$



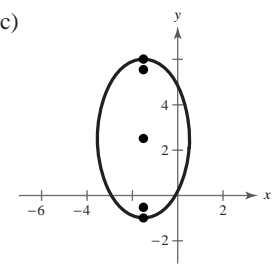
43. (a) $\frac{(x+\frac{3}{2})^2}{4} + \frac{(y-\frac{5}{2})^2}{12} = 1$ (c)

(b) Center: $(-\frac{3}{2}, \frac{5}{2})$

Vertices: $(-\frac{3}{2}, \frac{5 \pm 4\sqrt{3}}{2})$

Foci: $(-\frac{3}{2}, \frac{5}{2} \pm 2\sqrt{2})$

Eccentricity: $\frac{\sqrt{6}}{3}$



45. (a) $\frac{(x-1)^2}{25/16} + (y+1)^2 = 1$ (c)

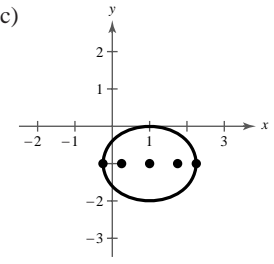
(b) Center: (1, -1)

Vertices:

$(\frac{9}{4}, -1), (-\frac{1}{4}, -1)$

Foci: $(\frac{7}{4}, -1), (\frac{1}{4}, -1)$

Eccentricity: $\frac{3}{5}$



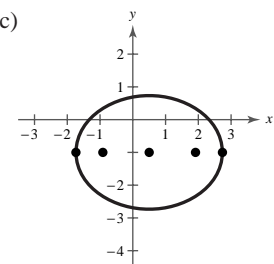
47. (a) $\frac{(x-\frac{1}{2})^2}{5} + \frac{(y+1)^2}{3} = 1$ (c)

(b) Center: $(\frac{1}{2}, -1)$

Vertices: $(\frac{1}{2} \pm \sqrt{5}, -1)$

Foci: $(\frac{1}{2} \pm \sqrt{2}, -1)$

Eccentricity: $\frac{\sqrt{10}}{5}$

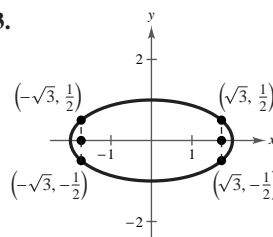


49. $\frac{\sqrt{5}}{3}$ 51. $\frac{2\sqrt{2}}{3}$ 53. $\frac{x^2}{25} + \frac{y^2}{16} = 1$

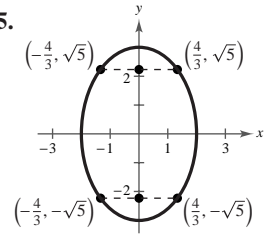
55. $\frac{x^2}{225/16} + \frac{y^2}{81/16} = 1$ 57. $(\pm \sqrt{5}, 0)$; 6 ft

59. $\frac{x^2}{321.84} + \frac{y^2}{19.02} = 1$ 61. $e = \frac{c}{a} \approx 0.052$

63.

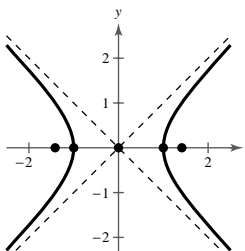
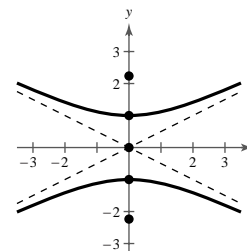
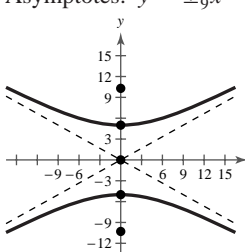
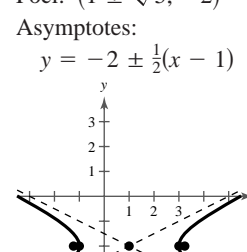
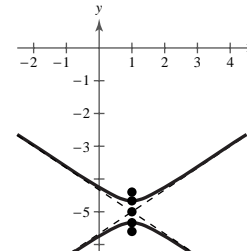


65.

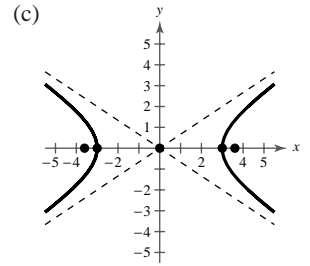


67. True. The ellipse is more elongated when e is close to 1.
 69. Nearly circular because its eccentricity is about 0.055, which is close to zero.
 71. (a) $2a$
 (b) The sum of the distances from the two fixed points is constant.
 73. $\frac{(x-6)^2}{324} + \frac{(y-2)^2}{308} = 1$ 75. Arithmetic
 77. Geometric 79. 1093

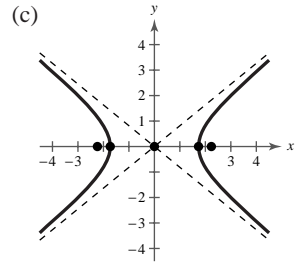
Section 9.3 (page 665)

1. hyperbola
 3. $Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$
 5. Horizontal: a, d ; vertical: b, c
 7. b 8. c 9. a 10. d
 11. Center: $(0, 0)$
 Vertices: $(\pm 1, 0)$
 Foci: $(\pm \sqrt{2}, 0)$
 Asymptotes: $y = \pm x$

 13. Center: $(0, 0)$
 Vertices: $(0, \pm 1)$
 Foci: $(0, \pm \sqrt{5})$
 Asymptotes: $y = \pm \frac{1}{2}x$

 15. Center: $(0, 0)$
 Vertices: $(0, \pm 5)$
 Foci: $(0, \pm \sqrt{106})$
 Asymptotes: $y = \pm \frac{5}{3}x$

 17. Center: $(1, -2)$
 Vertices: $(3, -2), (-1, -2)$
 Foci: $(1 \pm \sqrt{5}, -2)$
 Asymptotes: $y = -2 \pm \frac{1}{2}(x - 1)$

 19. Center: $(1, -5)$
 Vertices: $(1, -5 \pm \frac{1}{3})$
 Foci: $(1, -5 \pm \frac{\sqrt{13}}{6})$
 Asymptotes: $y = -5 \pm \frac{2}{3}(x - 1)$


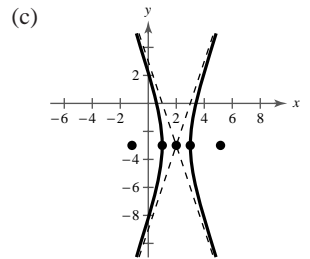
21. (a) $\frac{x^2}{9} - \frac{y^2}{4} = 1$
 (b) Center: $(0, 0)$
 Vertices: $(\pm 3, 0)$
 Foci: $(\pm \sqrt{13}, 0)$
 Asymptotes: $y = \pm \frac{2}{3}x$



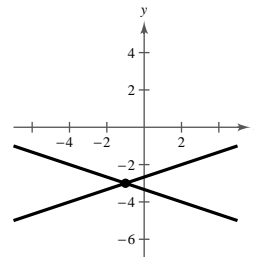
23. (a) $\frac{x^2}{3} - \frac{y^2}{2} = 1$
 (b) Center: $(0, 0)$
 Vertices: $(\pm \sqrt{3}, 0)$
 Foci: $(\pm \sqrt{5}, 0)$
 Asymptotes: $y = \pm \frac{\sqrt{6}}{3}x$



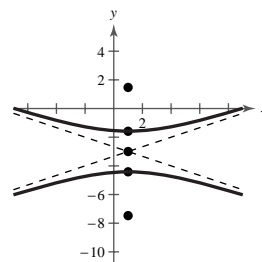
25. (a) $(x-2)^2 - \frac{(y+3)^2}{9} = 1$
 (b) Center: $(2, -3)$
 Vertices: $(3, -3), (1, -3)$
 Foci: $(2 \pm \sqrt{10}, -3)$
 Asymptotes: $y = -3 \pm 3(x - 2)$



27. (a) $(x+1)^2 - 9(y+3)^2 = 0$
 (b) It is a degenerate conic. The graph of this equation is two lines intersecting at $(-1, -3)$.
 (c)



29. (a) $\frac{(y+3)^2}{2} - \frac{(x-1)^2}{18} = 1$
 (b) Center: $(1, -3)$
 Vertices: $(1, -3 \pm \sqrt{2})$
 Foci: $(1, -3 \pm 2\sqrt{5})$
 Asymptotes: $y = -3 \pm \frac{1}{3}(x - 1)$
 (c)



31. $\frac{y^2}{4} - \frac{x^2}{12} = 1$ 33. $\frac{x^2}{1} - \frac{y^2}{25} = 1$
 35. $\frac{17y^2}{1024} - \frac{17x^2}{64} = 1$ 37. $\frac{(x-4)^2}{4} - \frac{y^2}{12} = 1$
 39. $\frac{(y-5)^2}{16} - \frac{(x-4)^2}{9} = 1$ 41. $\frac{y^2}{9} - \frac{4(x-2)^2}{9} = 1$
 43. $\frac{(y-2)^2}{4} - \frac{x^2}{4} = 1$ 45. $\frac{(x-2)^2}{1} - \frac{(y-2)^2}{1} = 1$
 47. $\frac{(x-3)^2}{9} - \frac{(y-2)^2}{4} = 1$
 49. $\frac{x^2}{98,010,000} - \frac{y^2}{13,503,600} = 1$

51. (a) $x^2 - \frac{y^2}{27} = 1$ (b) 1.89 ft = 22.68 in.

53. $(12\sqrt{5} - 12, 0) \approx (14.83, 0)$

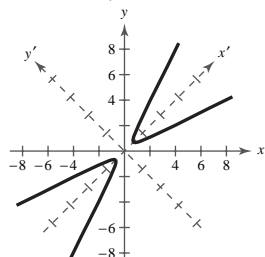
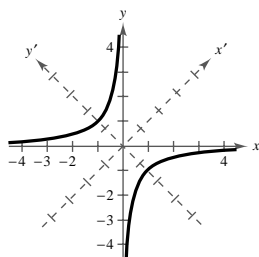
55. Ellipse 57. Hyperbola 59. Parabola

61. Circle 63. Parabola

65. e 66. b 67. f 68. a 69. d 70. c

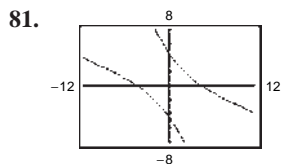
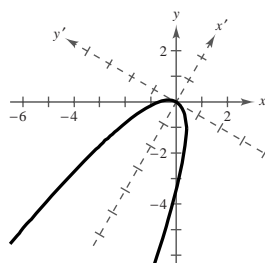
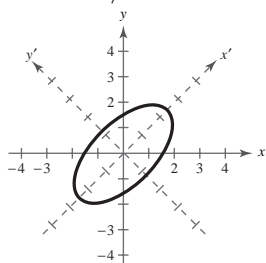
71. (3, 0)

73. $\frac{(y')^2}{2} - \frac{(x')^2}{2} = 1$ 75. $(x')^2 - \frac{(y')^2}{1/3} = 1$

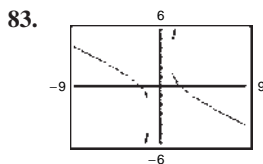


77. $\frac{(x')^2}{6} + \frac{(y')^2}{3/2} = 1$

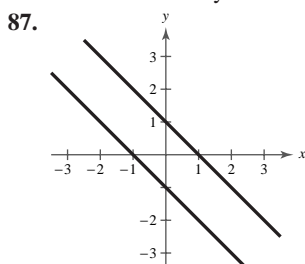
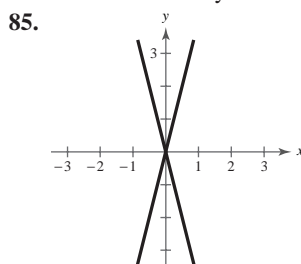
79. $x' = -(y')^2$



$\theta = 45^\circ$;
 Answers will vary.



$\theta \approx 26.57^\circ$;
 Answers will vary.



89. True. For a hyperbola, $c^2 = a^2 + b^2$. The larger the ratio of b to a , the larger the eccentricity of the hyperbola, $e = c/a$.

91. False. If $D = E$ or $D = -E$, the graph is two intersecting lines. For example, the graph of $x^2 - y^2 - 2x + 2y = 0$ is two intersecting lines.

93. False. The constant term F remains the same.

95. The asymptotes pass through the corners of the rectangle.

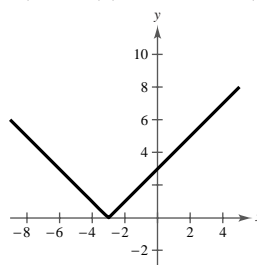
97. $\frac{(x-6)^2}{9} - \frac{(y-2)^2}{7} = 1$ 99. Proof

101. $x^3 + x^2 + 2x - 6$ 103. $x^2 - 2x + 1 + \frac{2}{x+2}$

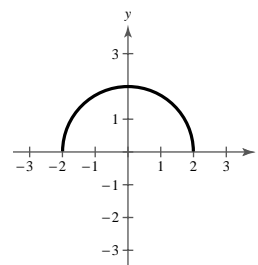
105. $x(x+4)(x-4)$ 107. $2x(x-6)^2$

109. $2(2x+3)(4x^2-6x+9)$

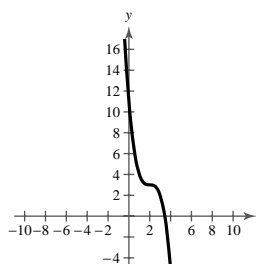
111.



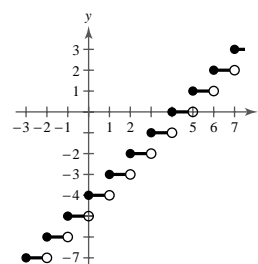
113.



115.



117.



Section 9.4 (page 674)

1. plane curve, parametric equations, parameter

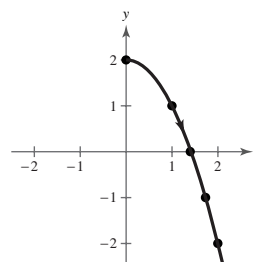
3. Eliminate the parameter.

5. c 6. d 7. b 8. a

9. (a)

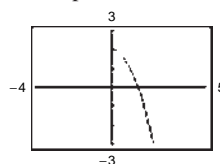
t	0	1	2	3	4
x	0	1	$\sqrt{2}$	$\sqrt{3}$	2
y	2	1	0	-1	-2

(b)

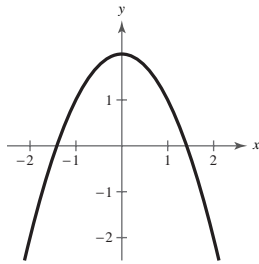


The curve starts at (0, 2) and moves along the right half of the parabola.

(c)



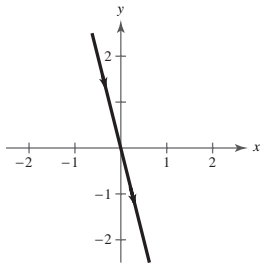
(d) $y = 2 - x^2$



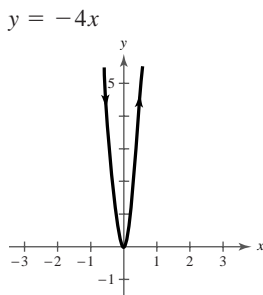
The graph is an entire parabola rather than just the right half.

11. b

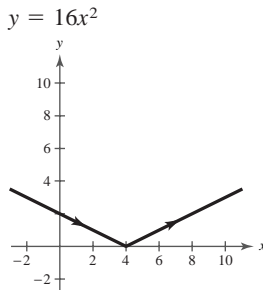
13.



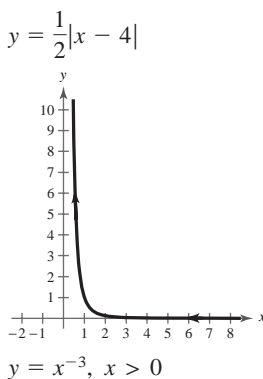
17.



21.

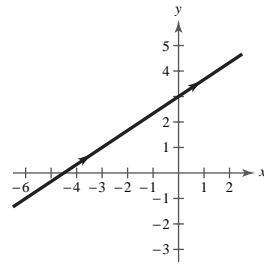


25.

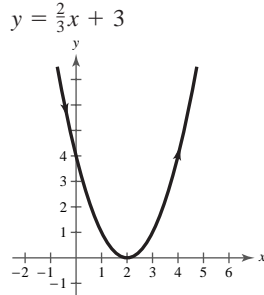


$$y = x^{-3}, x > 0$$

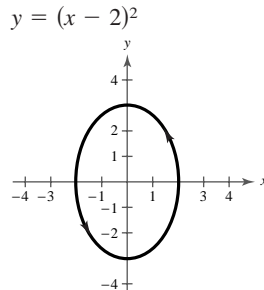
15.



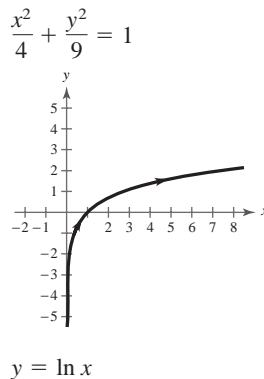
19.



23.

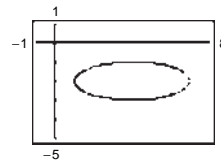


27.

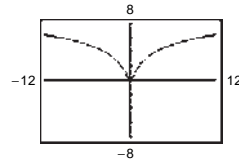


$$y = \ln x$$

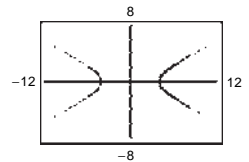
29.



33.



31.


 35. Each curve represents a portion of the line $y = 2x + 1$.

Domain

Orientation

 (a) $(-\infty, \infty)$

Left to right

 (b) $[-1, 1]$

 Depends on θ

 (c) $(0, \infty)$

Right to left

 (d) $(0, \infty)$

Left to right

$$37. y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1) \quad 39. \frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$$

$$41. x = 3 - 5t, y = 1 + 5t \quad 43. x = 5 \cos \theta, y = 4 \sin \theta$$

$$45. (a) x = t, y = 5t - 3 \quad (b) x = 2 - t, y = -5t + 7$$

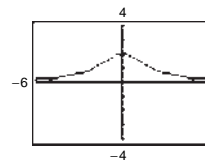
$$47. (a) x = t, y = \frac{1}{t} \quad (b) x = 2 - t, y = \frac{1}{2 - t}$$

$$49. (a) x = t, y = 6t^2 - 5$$

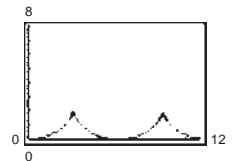
$$(b) x = 2 - t, y = 6t^2 - 24t + 19$$

$$51. (a) x = t, y = e^t \quad (b) x = 2 - t, y = e^{2-t}$$

53.



55.



57. b

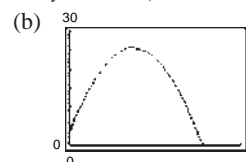
58. c

59. d

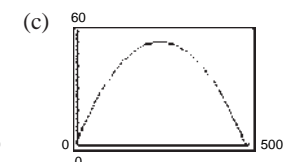
60. a

$$61. (a) x = (146.67 \cos \theta)t$$

$$y = 3 + (146.67 \sin \theta)t - 16t^2$$



No



Yes

 (d) About 19.4°

 63. True. Both sets of parametric equations correspond to $y = x^2 + 1$.

 65. False. The set $x = t^2, y = t$ does not correspond to y as a function of x .

67. Yes, the orientation would be reversed.

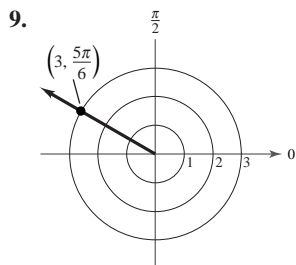
69. Even 71. Neither

Section 9.5 (page 681)

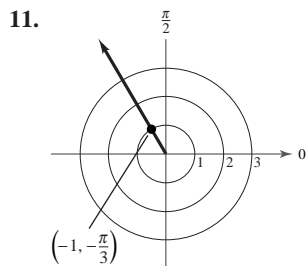
1. pole

$$3. x = r \cos \theta, y = r \sin \theta \text{ and } \tan \theta = \frac{y}{x}, r^2 = x^2 + y^2$$

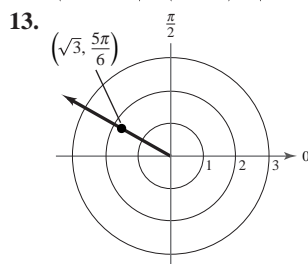
$$5. (0, 4) \quad 7. \left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} \right)$$



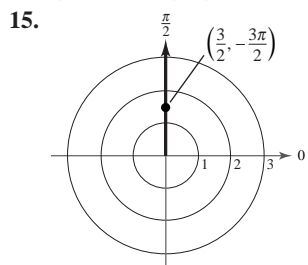
$$\left(3, -\frac{7\pi}{6}\right), \left(-3, \frac{11\pi}{6}\right), \left(-3, -\frac{\pi}{6}\right)$$



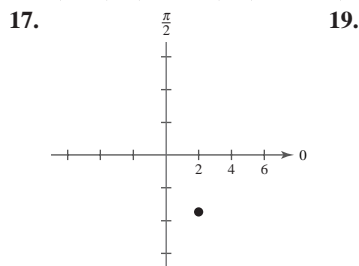
$$\left(-1, \frac{5\pi}{3}\right), \left(1, \frac{2\pi}{3}\right), \left(1, -\frac{4\pi}{3}\right)$$



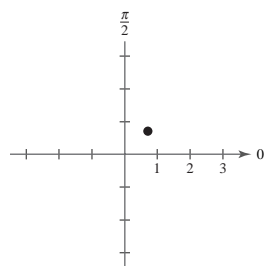
$$\left(-\sqrt{3}, \frac{11\pi}{6}\right), \left(\sqrt{3}, -\frac{7\pi}{6}\right), \left(-\sqrt{3}, -\frac{\pi}{6}\right)$$



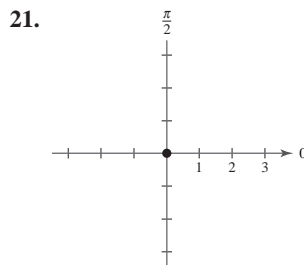
$$\left(\frac{3}{2}, \frac{\pi}{2}\right), \left(-\frac{3}{2}, \frac{3\pi}{2}\right), \left(-\frac{3}{2}, -\frac{\pi}{2}\right)$$



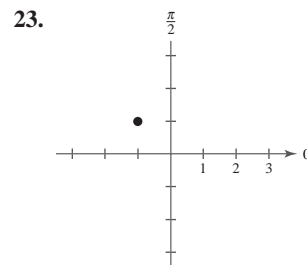
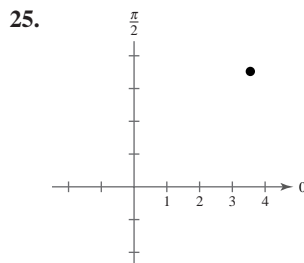
$$(2, -2\sqrt{3})$$



$$\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$$



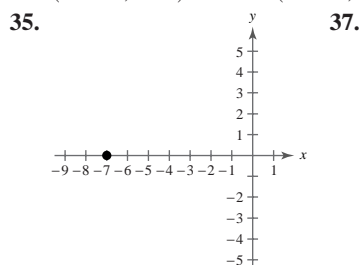
$$(0, 0)$$



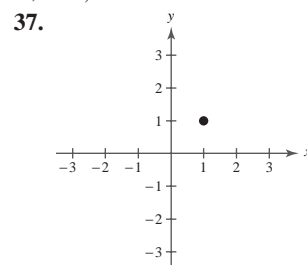
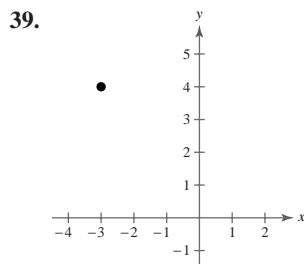
$$(-1.004, 0.996)$$

27. (1.53, 1.29) 29. (-1.20, -4.34)

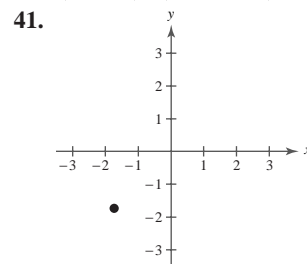
31. (-0.02, 2.50) 33. (-3.60, 1.97)



$$(7, \pi), (-7, 0)$$

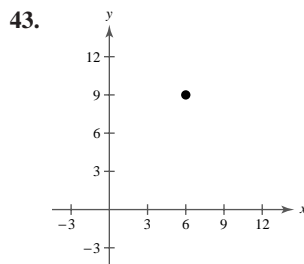


$$\left(\sqrt{2}, \frac{\pi}{4}\right), \left(-\sqrt{2}, \frac{5\pi}{4}\right)$$



$$(5, 2.214), (-5, 5.356)$$

$$\left(\sqrt{6}, \frac{5\pi}{4}\right), \left(-\sqrt{6}, \frac{\pi}{4}\right)$$



$$(10.82, 0.98), (-10.82, 4.12)$$

45. (3.61, -0.59) 47. (2.65, 0.86) 49. (2.83, 0.49)

51. $r = 3$ 53. $r = 4 \csc \theta$ 55. $r = 8 \sec \theta$

57. $r = -\frac{2}{3 \cos \theta - \sin \theta}$ 59. $r^2 = 8 \csc 2\theta$

61. $r^2 = 9 \cos 2\theta$ 63. $r = 6 \cos \theta$ 65. $r = 2a \cos \theta$

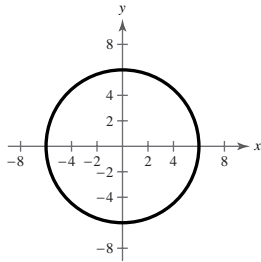
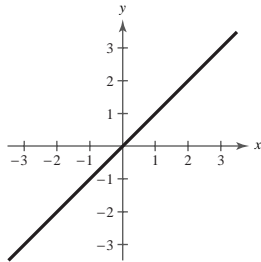
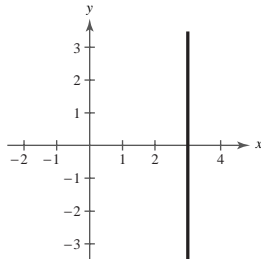
67. $r = \tan^2 \theta \sec \theta$ 69. $x^2 + y^2 - 4y = 0$

71. $y = -\sqrt{3}x$ 73. $y = -\frac{\sqrt{3}}{3}x$ 75. $x = 0$

77. $x^2 + y^2 = 16$ 79. $y = -3$ 81. $(x^2 + y^2)^3 = x^2$

83. $(x^2 + y^2)^2 = 6x^2y - 2y^3$ 85. $y^2 = 2x + 1$

87. $4x^2 - 5y^2 = 36y + 36$

 89. The graph is a circle centered at the origin with a radius of 6; $x^2 + y^2 = 36$.

 91. The graph consists of all points on the line that makes an angle of $\pi/4$ with the positive x -axis; $x - y = 0$.

 93. The graph is a vertical line through (3, 0); $x - 3 = 0$.

 95. True. Because r is a directed distance, (r, θ) can be represented by $(-r, \theta \pm (2n + 1)\pi)$, so $|r| = |-r|$.

97. (a) Answers will vary.

(b) The points lie on a line passing through the pole.

$$d = \sqrt{r_1^2 + r_2^2 - 2r_1r_2} = |r_1 - r_2|$$

 (c) $d = \sqrt{r_1^2 + r_2^2}$ (Pythagorean Theorem)

Answers will vary.

(d) Answers will vary. The Distance Formula should give the same result in both cases.

 99. $\left(x - \frac{1}{2}\right)^2 + \left(y - \frac{3}{2}\right)^2 = \frac{5}{2}$; A circle centered at $\left(\frac{1}{2}, \frac{3}{2}\right)$ with a radius of $\frac{\sqrt{10}}{2}$.

101. $A \approx 30.68^\circ$

$B \approx 48.23^\circ$

$C \approx 101.09^\circ$

103. $a \approx 16.16$

$b \approx 19.44$

$B \approx 86^\circ$

Section 9.6 (page 689)

1. convex limaçon 3. lemniscate

 5. When (r, θ) can be replaced with $(r, \pi - \theta)$ or $(-r, -\theta)$ and yield an equivalent equation

7. Rose curve

9. Lemniscate

11. Rose curve

13. a

15. c

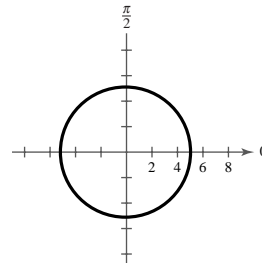
17. Polar axis

19. $\theta = \frac{\pi}{2}$

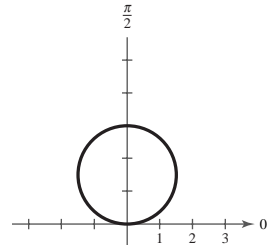
21. $\theta = \frac{\pi}{2}$

23. Pole

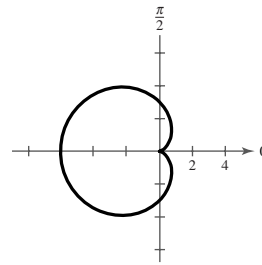
25.



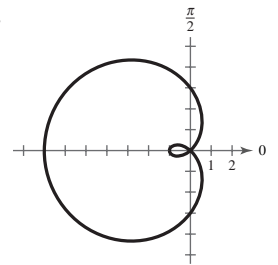
27.



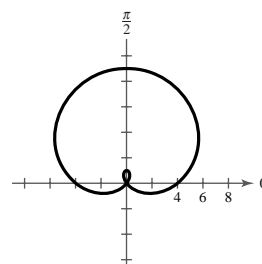
29.



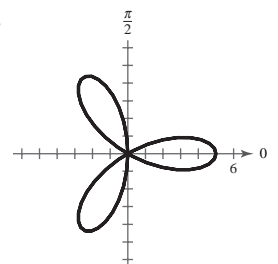
31.



33.



35.



Symmetry: polar axis

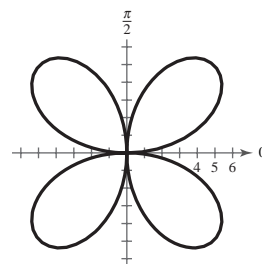
Zeros: $\frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}$

Symmetry:

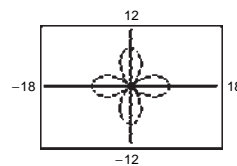
$\theta = \frac{\pi}{2}, \text{ polar axis, pole}$

Zeros: $0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}, 2\pi$

37.

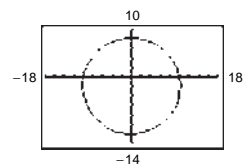


39.



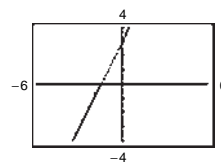
Answers will vary.

41.



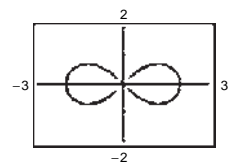
Answers will vary.

43.

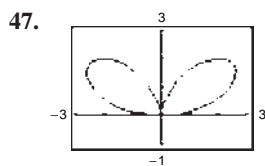


Answers will vary.

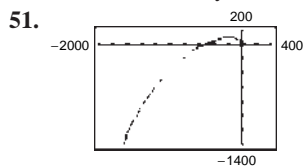
45.



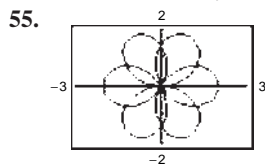
Answers will vary.



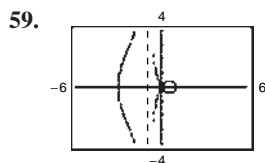
Answers will vary.



Answers will vary.

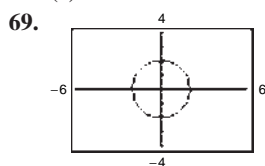


$$0 \leq \theta < 4\pi$$

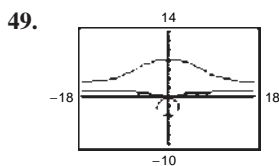


63. True. $n = 5$ 65. Answers will vary.

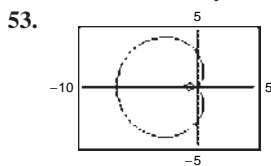
67. (a) $r = 2 - \sin\left(\theta - \frac{\pi}{4}\right)$ (b) $r = 2 + \cos \theta$
(c) $r = 2 + \sin \theta$ (d) $r = 2 - \cos \theta$



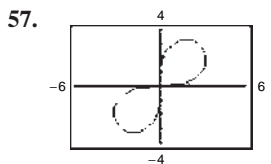
$k = 0$; circle



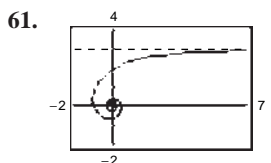
Answers will vary.



$$0 \leq \theta < 2\pi$$

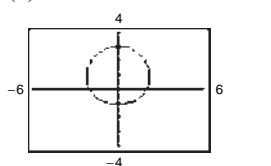


$$0 \leq \theta < \frac{\pi}{2}$$

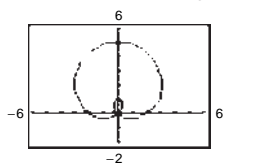


Answers will vary.

(a) $r = 2 - \sin\left(\theta - \frac{\pi}{4}\right)$ (b) $r = 2 + \cos \theta$
(c) $r = 2 + \sin \theta$ (d) $r = 2 - \cos \theta$



$k = 1$; convex limaçon



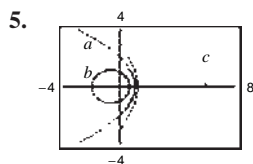
$k = 2$; cardioid

$k = 3$; limaçon with inner loop

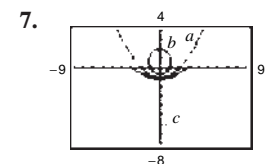
71. $x = -3, 3$ 73. $x = \frac{13}{5}$

Section 9.7 (page 695)

1. conic 3. vertical



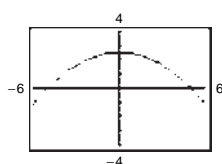
(a) Parabola
(b) Ellipse
(c) Hyperbola



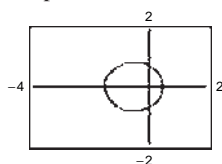
(a) Parabola
(b) Ellipse
(c) Hyperbola

9. b 10. c 11. f 12. e 13. d 14. a

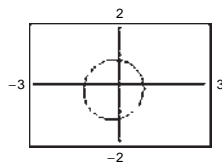
15. Parabola 17. Ellipse 19. Ellipse
21. Ellipse 23. Hyperbola
25. Parabola 27. Hyperbola



29. Ellipse



33.



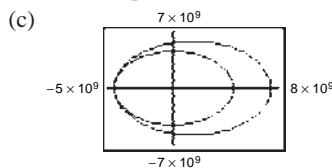
37. $r = \frac{1}{1 - \cos \theta}$ 39. $r = \frac{1}{2 + \sin \theta}$
41. $r = \frac{2}{1 + 2 \cos \theta}$ 43. $r = \frac{2}{1 - \sin \theta}$
45. $r = \frac{10}{1 - \cos \theta}$ 47. $r = \frac{10}{3 + 2 \cos \theta}$
49. $r = \frac{20}{3 - 2 \cos \theta}$ 51. $r = \frac{16}{3 + 5 \cos \theta}$

53. Answers will vary.

55. $r = \frac{9.2930 \times 10^7}{1 - 0.0167 \cos \theta}$ 57. $r = \frac{6.7280 \times 10^7}{1 - 0.0068 \cos \theta}$
Perihelion: 9.1404 $\times 10^7$ mi Perihelion: 6.6781 $\times 10^7$ mi
Aphelion: 9.4508 $\times 10^7$ mi Aphelion: 6.7695 $\times 10^7$ mi

59. (a) $r_{\text{Neptune}} = \frac{4.4977 \times 10^9}{1 - 0.0086 \cos \theta}$
 $r_{\text{Pluto}} = \frac{5.5404 \times 10^9}{1 - 0.2488 \cos \theta}$

(b) Neptune: Perihelion: 4.4593 $\times 10^9$ km
Aphelion: 4.5367 $\times 10^9$ km
Pluto: Perihelion: 4.4366 $\times 10^9$ km
Aphelion: 7.3754 $\times 10^9$ km



(d) Yes; because on average, Pluto is farther from the sun than Neptune.
(e) Using a graphing utility, it would appear that the orbits intersect. No, Pluto and Neptune will never collide because the orbits do not intersect in three-dimensional space.

61. False. The equation can be rewritten as $r = \frac{-4/3}{1 + \sin \theta}$.
 Because ep is negative, p must be negative, and because p represents the distance between the pole and the directrix, the directrix has to be below the pole.

63. True. The graphs represent the same hyperbola.

65. Answers will vary.

67. $r^2 = \frac{24,336}{169 - 25 \cos^2 \theta}$ 69. $r^2 = \frac{400}{25 - 9 \cos^2 \theta}$

71. $r^2 = \frac{144}{25 \sin^2 \theta - 16}$

73. (a) Ellipse

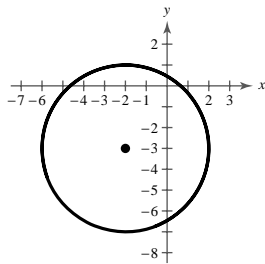
(b) $r = \frac{4}{1 + 0.4 \cos \theta}$ is reflected about the line $\theta = \frac{\pi}{2}$.

$r = \frac{4}{1 - 0.4 \sin \theta}$ is rotated 90° counterclockwise.

75. Circle 77. $\frac{\sqrt{2}}{10}$ 79. $\frac{\sqrt{2}}{10}$

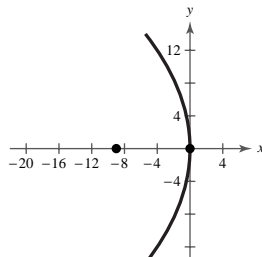
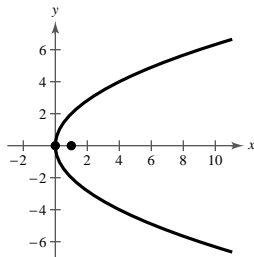
Review Exercises (page 700)

1. Hyperbola 3. $x^2 + y^2 = 25$
 5. $(x - 2)^2 + (y - 4)^2 = 13$
 7. $x^2 + y^2 = 36$ 9. $(x - \frac{1}{2})^2 + (y + \frac{3}{4})^2 = 1$
 Center: (0, 0) Center: $(\frac{1}{2}, -\frac{3}{4})$
 Radius: 6 Radius: 1
 11. 13. $(3 \pm \sqrt{6}, 0)$



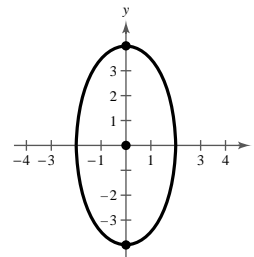
Center: (-2, -3)
 Radius: 4

15. Vertex: (0, 0) 17. Vertex: (0, 0)
 Focus: (1, 0) Focus: (-9, 0)
 Directrix: $x = -1$ Directrix: $x = 9$

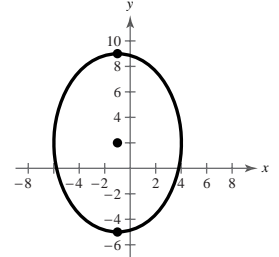


19. $y^2 = 16x$ 21. $(x + 6)^2 = -9(y - 4)$
 23. $2x + y - 2 = 0; (1, 0)$ 25. $8\sqrt{6} \text{ m}$

27. Center: (0, 0)
 Vertices: (0, ± 4)
 Foci: (0, $\pm 2\sqrt{3}$)
 Eccentricity: $\frac{\sqrt{3}}{2}$

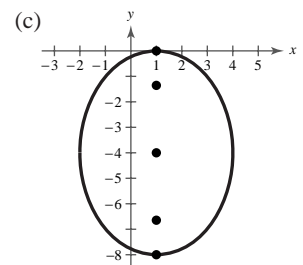


29. Center: (-1, 2)
 Vertices: (-1, 9), (-1, -5)
 Foci: $(-1, 2 \pm 2\sqrt{6})$
 Eccentricity: $\frac{2\sqrt{6}}{7}$



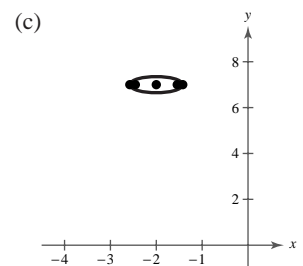
31. (a) $\frac{(x - 1)^2}{9} + \frac{(y + 4)^2}{16} = 1$

- (b) Center: (1, -4)
 Vertices: (1, 0), (1, -8)
 Foci: $(1, -4 \pm \sqrt{7})$
 Eccentricity: $\frac{\sqrt{7}}{4}$



33. (a) $\frac{(x + 2)^2}{1/3} + \frac{(y - 7)^2}{1/8} = 1$

- (b) Center: (-2, 7)
 Vertices: $(-2 \pm \frac{\sqrt{3}}{3}, 7)$
 Foci: $(-2 \pm \frac{\sqrt{30}}{12}, 7)$
 Eccentricity: $\frac{\sqrt{10}}{4}$



35. $\frac{x^2}{25} + \frac{y^2}{9} = 1$ 37. $\frac{(x - 2)^2}{25} + \frac{y^2}{21} = 1$

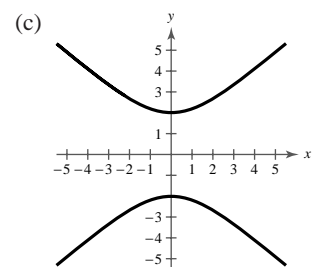
39. The foci should be placed 3 feet on either side of the center at the same height as the pillars.

41. $e \approx 0.0543$ 43. $\frac{x^2}{16} - \frac{y^2}{20} = 1$

45. $\frac{(x - 4)^2}{16/5} - \frac{y^2}{64/5} = 1$

47. (a) $\frac{y^2}{4} - \frac{x^2}{5} = 1$

- (b) Center: (0, 0)
 Vertices: (0, ± 2)
 Foci: (0, ± 3)
 Eccentricity: $\frac{3}{2}$



49. (a) $\frac{(x-1)^2}{16} - \frac{(y+1)^2}{9} = 1$

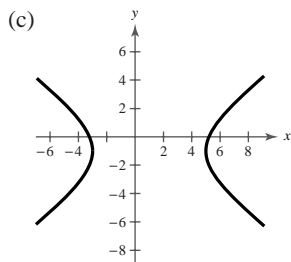
(b) Center: $(1, -1)$

Vertices:

$(5, -1), (-3, -1)$

Foci: $(6, -1), (-4, -1)$

Eccentricity: $\frac{5}{4}$



51. (a) $\frac{(x+6)^2}{101/2} - \frac{(y-1)^2}{202} = 1$

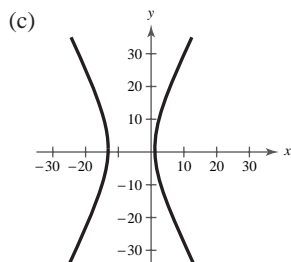
(b) Center: $(-6, 1)$

Vertices:

$\left(-6 \pm \frac{\sqrt{202}}{2}, 1\right)$

Foci: $\left(-6 \pm \frac{\sqrt{1010}}{2}, 1\right)$

Eccentricity: $\sqrt{5}$



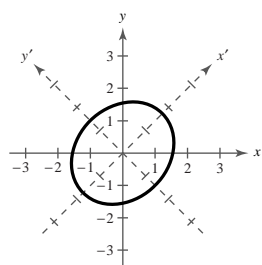
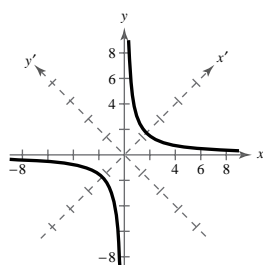
53. About 72 mi

55. Ellipse

57. Hyperbola

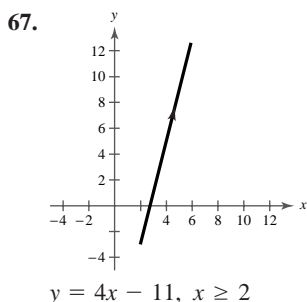
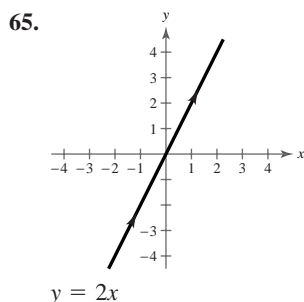
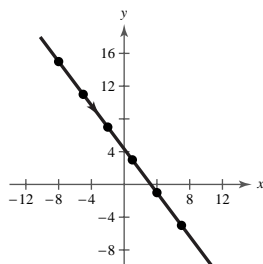
59. $\frac{(x')^2}{6} - \frac{(y')^2}{6} = 1$

61. $\frac{(x')^2}{3} + \frac{(y')^2}{2} = 1$

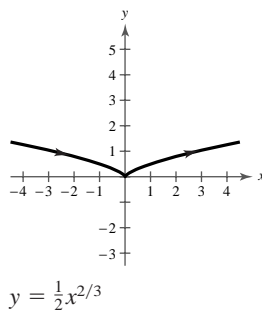


63.

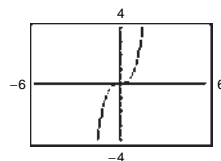
t	-2	-1	0	1	2	3
x	-8	-5	-2	1	4	7
y	15	11	7	3	-1	-5



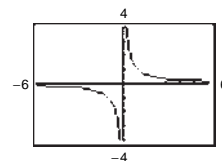
69.



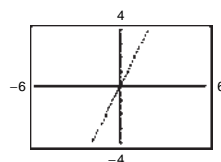
71.



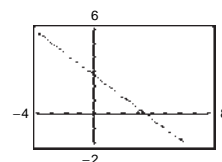
73.



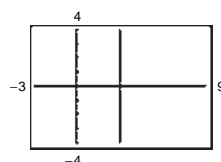
75.



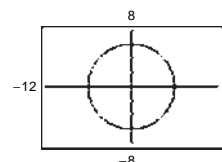
77.



79.



81.



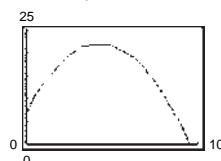
83. (a) $x = t, y = 6t + 2$ (b) $x = 1 - t, y = 8 - 6t$

85. (a) $x = t, y = t^2 + 2$ (b) $x = 1 - t, y = t^2 - 2t + 3$

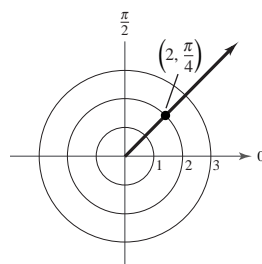
87. $x = t, y = 5$ 89. $x = -1 + 11t, y = 6 - 6t$

91. 54.22 ft/sec

93. 21.93 ft

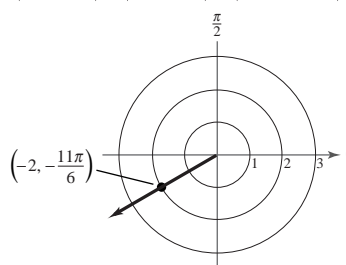


95.



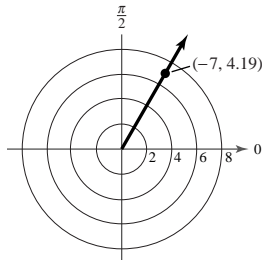
$\left(2 - \frac{7\pi}{4}, \left(-2, \frac{5\pi}{4}\right), \left(-2, -\frac{3\pi}{4}\right)\right)$

97.

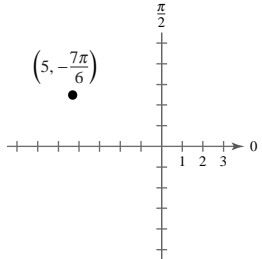


$\left(-2, \frac{\pi}{6}\right), \left(2, \frac{7\pi}{6}\right), \left(2, -\frac{5\pi}{6}\right)$

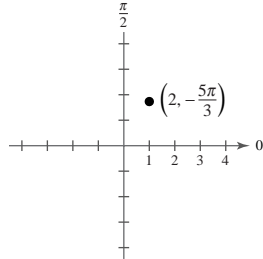
99.


 $(-7, -2.09), (7, -5.23), (7, 1.05)$

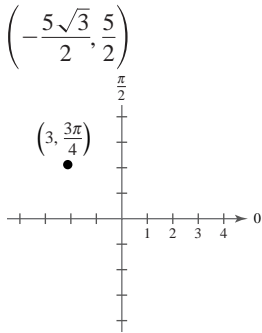
101.



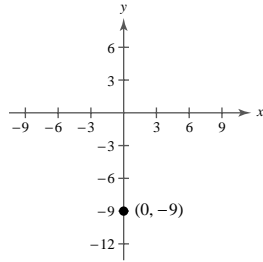
103.



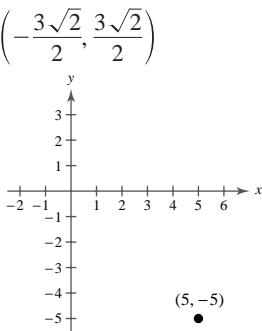
105.



107.



109.


 $(-5\sqrt{2}, \frac{3\pi}{4}), (5\sqrt{2}, \frac{7\pi}{4})$

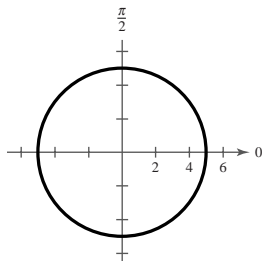
 111. $r = 9$ 113. $r = 4 \cos \theta$ 115. $r^2 = 5 \sec \theta \csc \theta$

 117. $r^2 = \frac{1}{1 + 3 \cos^2 \theta}$ 119. $x^2 + y^2 = 25$

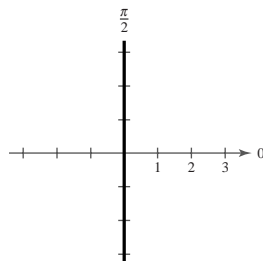
 121. $x^2 + y^2 = 3x$ 123. $(x^2 + y^2)^2 - x^2 + y^2 = 0$

 125. $y = -\frac{\sqrt{3}}{3}x$

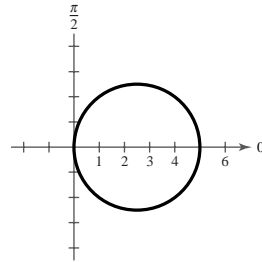
127.



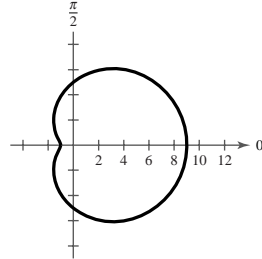
129.



131.



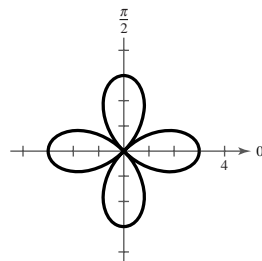
133. Dimpled limaçon



Symmetry: Polar axis

 Zeros of r : None

137. Rose curve

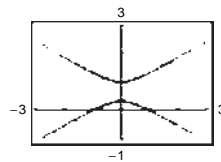


Symmetry:

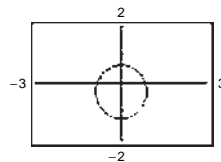
 Pole, polar axis, $\theta = \frac{\pi}{2}$

 Zeros of r : $\theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$

141. Hyperbola



145. Ellipse


 147. $r = \frac{4}{1 - \cos \theta}$ 149. $r = \frac{5}{3 - 2 \cos \theta}$

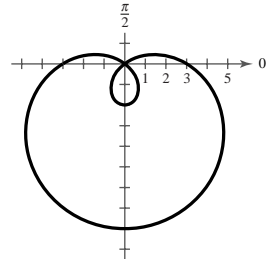
 151. $r = \frac{1.512}{1 - 0.093 \cos \theta}$

Perihelion: 1.383 astronomical units

Aphelion: 1.667 astronomical units

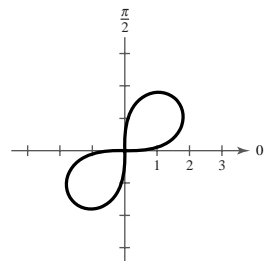
153. False. The equation of a hyperbola is a second-degree equation.

135. Limaçon with inner loop


 Symmetry: $\theta = \frac{\pi}{2}$

 Zeros of r : $\theta \approx 0.64, 2.50$

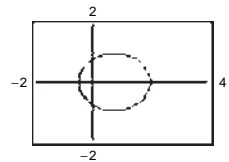
139. Lemniscate



Symmetry: Pole

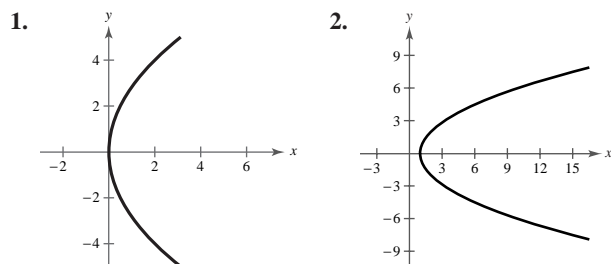
 Zeros of r : $\theta = 0, \frac{\pi}{2}$

143. Ellipse



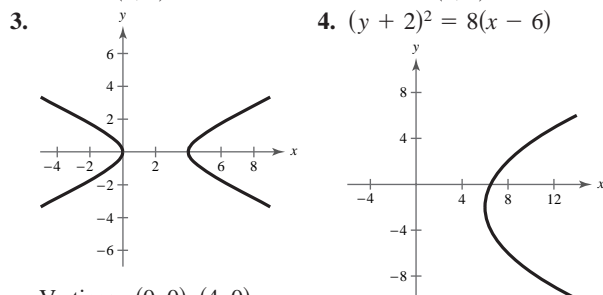
155. (a) Vertical translation (b) Horizontal translation
(c) Reflection in the y-axis (d) Vertical shrink
157. The orientation would be reversed.

Chapter Test (page 704)



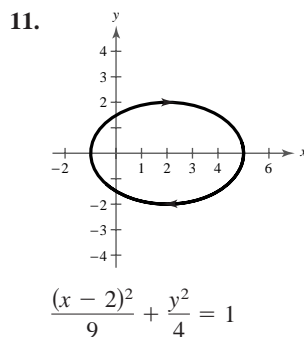
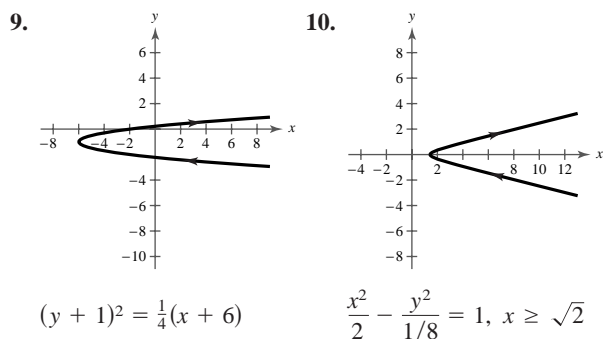
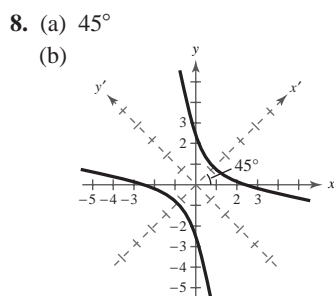
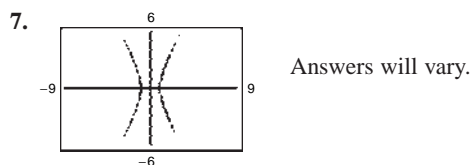
Vertex: (0, 0)
Focus: (2, 0)

Vertex: (1, 0)
Focus: (2, 0)

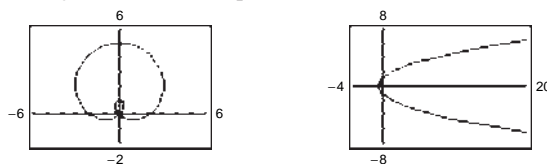


Vertices: (0, 0), (4, 0)
Foci: $(2 \pm \sqrt{5}, 0)$

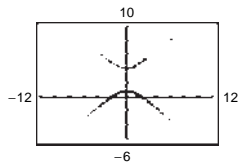
5. $\frac{(x+6)^2}{16} + \frac{(y-3)^2}{49} = 1$ 6. $\frac{y^2}{9} - \frac{x^2}{4} = 1$



12. (a) $x = t, y = 7 - 4t$ (b) $x = 2 - t, y = 4t - 1$
13. (a) $x = t, y = \frac{3}{t}$ (b) $x = 2 - t, y = \frac{3}{2-t}$
14. (a) $x = t, y = t^2 + 10$ (b) $x = t - 2, y = t^2 - 4t + 14$
15. $(\sqrt{3}, -1)$
16. Sample answer: $(2\sqrt{2}, \frac{7\pi}{4}); (2\sqrt{2}, -\frac{\pi}{4}), (-2\sqrt{2}, \frac{3\pi}{4})$
17. $r = 3 \cos \theta$ 18. $x^2 + (y-1)^2 = 1$
19. Limaçon with inner loop 20. Parabola



21. Hyperbola



22. $r = \frac{4}{4 + \sin \theta}$ 23. $r = \frac{10}{4 + 5 \sin \theta}$

24. Maximum: $|r| = 8$

Zeros of r : $\theta = \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}$

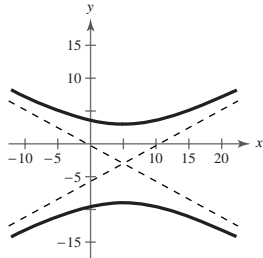
Cumulative Test for Chapters 7–9 (page 705)

1. (4, -3) 2. (8, 4), (2, -2)
3. $(\frac{3}{5}, -4, -\frac{1}{5})$ 4. (1, -4, -4)
5. $\begin{bmatrix} -7 & -10 & -16 \\ -6 & 18 & 9 \\ -12 & 16 & 7 \end{bmatrix}$ 6. $\begin{bmatrix} -18 & 15 & -14 \\ 28 & 11 & 34 \\ -20 & 52 & -1 \end{bmatrix}$
7. $\begin{bmatrix} 3 & -31 & 2 \\ 22 & 18 & 6 \\ 52 & -40 & 14 \end{bmatrix}$ 8. $\begin{bmatrix} 5 & 36 & 31 \\ -36 & 12 & -36 \\ 16 & 0 & 18 \end{bmatrix}$
9. (a) $\begin{bmatrix} -175 & 37 & -13 \\ 95 & -20 & 7 \\ 14 & -3 & 1 \end{bmatrix}$ (b) 1
10. 22 11. (a) $\frac{1}{5}, -\frac{1}{7}, \frac{1}{9}, -\frac{1}{11}, \frac{1}{13}$ (b) 3, 6, 12, 24, 48
12. 135 13. $\frac{47}{52}$ 14. 34.48 15. 66.67 16. $\frac{15}{8}$
17. $-\frac{5}{51}$ 18. $\frac{8}{3}$ 19. (a) 190 (b) 190
20. $x^4 + 12x^3 + 54x^2 + 108x + 81$

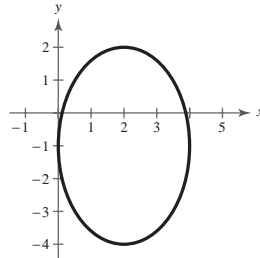
21. $32x^5 + 80x^4y^2 + 80x^3y^4 + 40x^2y^6 + 10xy^8 + y^{10}$
 22. $x^6 - 12x^5y + 60x^4y^2 - 160x^3y^3 + 240x^2y^4 - 192xy^5 + 64y^6$
 23. $6561a^8 - 69,984a^7b + 326,592a^6b^2 - 870,912a^5b^3$
 $+ 1,451,520a^4b^4 - 1,548,288a^3b^5 + 1,032,192a^2b^6$
 $- 393,216ab^7 + 65,536b^8$

24. 120 25. 420 26. 302,400 27. 15,120

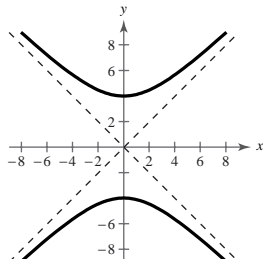
28. Hyperbola



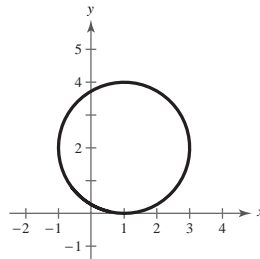
29. Ellipse



30. Hyperbola



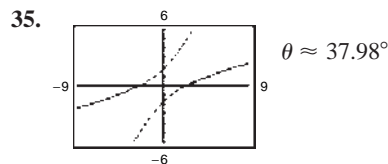
31. Circle



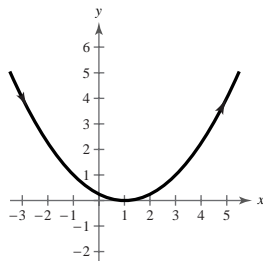
32. $(x - 2)^2 = -\frac{4}{3}(y - 3)$

33. $\frac{(x - 1)^2}{25} + \frac{(y - 4)^2}{4} = 1$

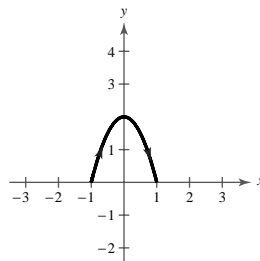
34. $\frac{(y + 4)^2}{4} - \frac{x^2}{16/3} = 1$



36. (a) and (b)



37. (a) and (b)

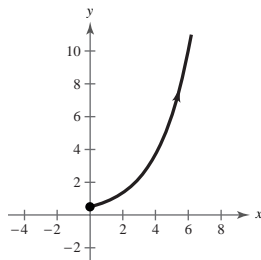


(c) $y = \frac{x^2 - 2x + 1}{4}$

(c) $y = 2 - 2x^2$,
 $-1 \leq x \leq 1$

38. (a) and (b)

(c) $y = 0.5e^{0.5x}$, $x \geq 0$



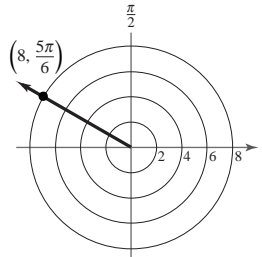
39. (a) $x = t$, $y = 3t - 2$ (b) $x = 2t$, $y = 6t - 2$

40. (a) $x = t$, $y = t^2 - 16$ (b) $x = 2t$, $y = 4t^2 - 16$

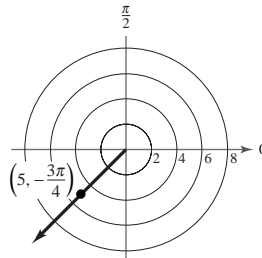
41. (a) $x = t$, $y = \frac{2}{t}$ (b) $x = 2t$, $y = \frac{1}{t}$

42. (a) $x = t$, $y = \frac{e^{2t}}{e^{2t} + 1}$ (b) $x = 2t$, $y = \frac{e^{4t}}{e^{4t} + 1}$

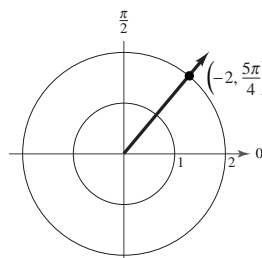
43. $(8, \frac{5\pi}{6})$, $(8, -\frac{7\pi}{6})$, $(-8, -\frac{\pi}{6})$, $(-8, \frac{11\pi}{6})$



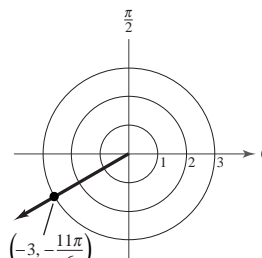
44. $(5, \frac{5\pi}{4})$, $(-5, -\frac{7\pi}{4})$, $(-5, \frac{\pi}{4})$



45. $(-2, \frac{5\pi}{4})$, $(2, -\frac{7\pi}{4})$, $(2, \frac{\pi}{4})$



46. $(-3, \frac{\pi}{6})$, $(3, -\frac{5\pi}{6})$, $(3, \frac{7\pi}{6})$

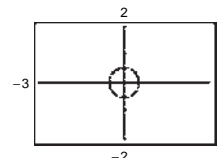


47. $r = -\frac{1}{4 \sin \theta + 4 \cos \theta}$

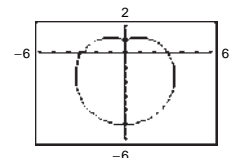
48. $(x - 2)^2 + y^2 = 4$

49. $\frac{(x + \frac{10}{9})^2}{\frac{64}{81}} - \frac{y^2}{\frac{4}{9}} = 1$

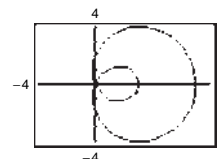
50. Circle



51. Dimpled limaçon



52. Limaçon with inner loop



53. \$701,303.32

54. $\frac{1}{4}$

55. $24\sqrt{2}$ m

Chapter 10

Section 10.1 (page 716)

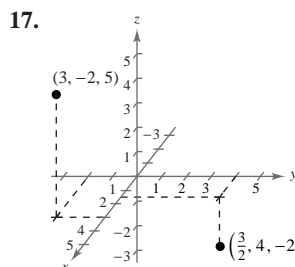
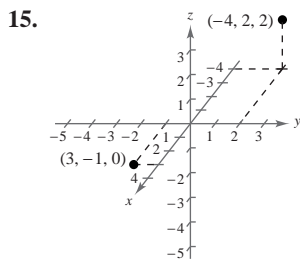
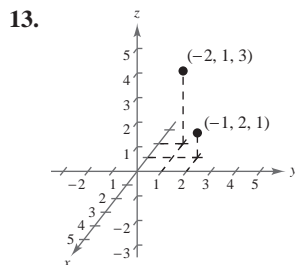
1. three-dimensional 3. Distance Formula

5. surface, space

7. A sphere with center (h, k, j) and radius r

9. $A(-1, 4, 3)$, $B(1, 3, -2)$, $C(-3, 0, -2)$

11. $A(-2, -1, 4)$, $B(3, -2, 0)$, $C(-2, 2, -3)$



19. $(-3, 3, 5)$ 21. $(11, 0, 0)$ 23. Octant V

25. Octants I, II, III, and IV 27. Octants II, IV, VI, and VIII

29. $3\sqrt{21}$ units 31. $\sqrt{65}$ units

33. $\sqrt{114}$ units 35. $\sqrt{105}$ units 37. $2\sqrt{5}$, 3, $\sqrt{29}$

39. 3, 6, $3\sqrt{5}$ 41. 6, 6, $2\sqrt{10}$; isosceles triangle

43. 6, 6, $2\sqrt{10}$; isosceles triangle

45. $(0, -1, 7)$ 47. $(1, 0, 6)$ 49. $(\frac{5}{2}, 2, 6)$

51. $(x - 3)^2 + (y - 2)^2 + (z - 4)^2 = 16$

53. $(x + 1)^2 + (y - 2)^2 + z^2 = 3$

55. $x^2 + (y - 4)^2 + (z - 3)^2 = 16$

57. $(x + 3)^2 + (y - 7)^2 + (z - 5)^2 = 25$

59. $(x - \frac{3}{2})^2 + y^2 + (z - 3)^2 = \frac{45}{4}$

61. Center: $(3, 0, 0)$; radius: 3

63. Center: $(2, -1, 0)$; radius: $\sqrt{5}$

65. Center: $(2, -1, 3)$; radius: 2

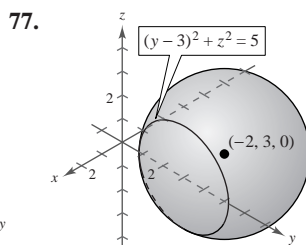
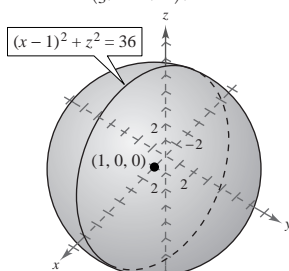
67. Center: $(-2, 0, 4)$; radius: 1

69. Center: $(1, \frac{1}{3}, 4)$; radius: 3

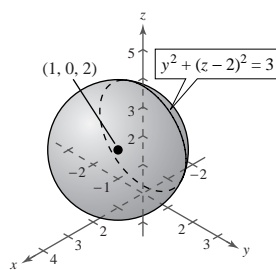
71. Center: $(1, -2, 0)$; radius: $\frac{\sqrt{21}}{2}$

73. Center: $(\frac{1}{3}, -1, 0)$; radius: 1

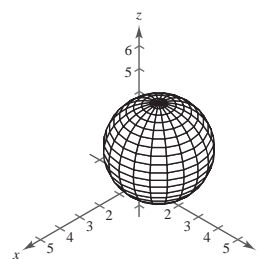
75.



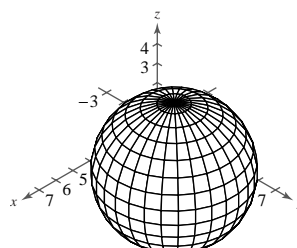
79.



81.



83.



85. $(3, 3, 3)$ 87. $x^2 + y^2 + z^2 = \frac{205^2}{4}$

89. False. z is the directed distance from the xy -plane to P .

91. 0; 0; 0 93. $(x_2, y_2, z_2) = (2x_m - x_1, 2y_m - y_1, 2z_m - z_1)$

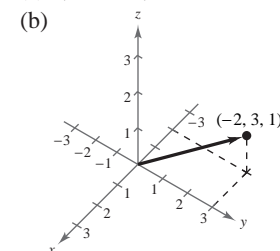
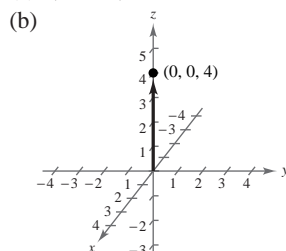
95. $v = -\frac{3 \pm \sqrt{17}}{2}$ 97. $x = \frac{5 \pm \sqrt{5}}{2}$ 99. $y = -\frac{1 \pm \sqrt{10}}{2}$

Section 10.2 (page 724)

1. zero 3. parallel 5. $\|\mathbf{v}\| = \sqrt{v_1^2 + v_2^2 + v_3^2}$

7. (a) $\langle 0, 0, 4 \rangle$

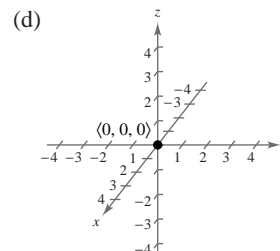
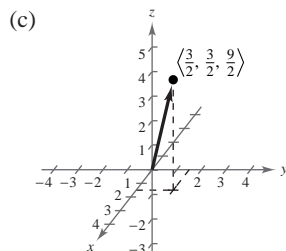
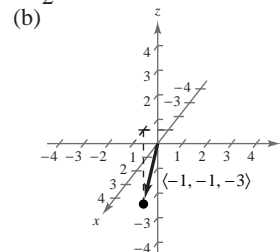
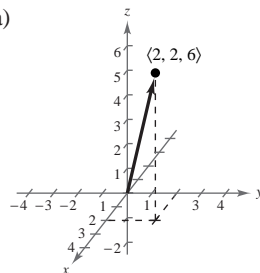
9. (a) $\langle -2, 3, 1 \rangle$



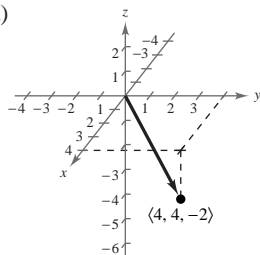
11. (a) $\langle 7, -5, 5 \rangle$ (b) $3\sqrt{11}$ (c) $\frac{\sqrt{11}}{33} \langle 7, -5, 5 \rangle$

13. (a) $\langle 2, 2, 0 \rangle$ (b) $2\sqrt{2}$ (c) $\frac{\sqrt{2}}{2} \langle 1, 1, 0 \rangle$

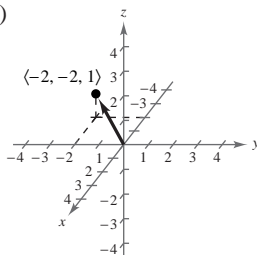
15. (a)



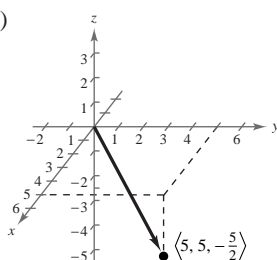
17. (a)



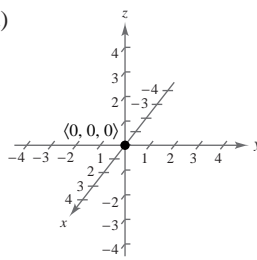
(b)



(c)



(d)



19. $\mathbf{z} = \langle -3, 7, 6 \rangle$ 21. $\mathbf{z} = \langle \frac{1}{2}, 6, \frac{3}{2} \rangle$
 23. $\mathbf{z} = \langle -\frac{5}{2}, 12, \frac{15}{2} \rangle$ 25. $9\sqrt{2}$ 27. $\sqrt{21}$
 29. $\sqrt{21}$ 31. $\sqrt{34}$
 33. (a) $\frac{1}{13}(5\mathbf{i} - 12\mathbf{k})$ (b) $-\frac{1}{13}(5\mathbf{i} - 12\mathbf{k})$
 35. (a) $\frac{\sqrt{74}}{74}(8\mathbf{i} + 3\mathbf{j} - \mathbf{k})$ (b) $-\frac{\sqrt{74}}{74}(8\mathbf{i} + 3\mathbf{j} - \mathbf{k})$
 37. $\langle -26, 0, 48 \rangle$ 39. 8.73 41. -4 43. 0
 45. 124.45° 47. 109.92° 49. Parallel 51. Neither
 53. Orthogonal 55. Not collinear 57. Collinear
 59. Right triangle. Answers will vary.
 61. Acute triangle. Answers will vary.
 63. $(3, 1, 7)$ 65. $(6, \frac{5}{2}, -\frac{7}{4})$ 67. $\pm \frac{3\sqrt{14}}{14}$
 69. $\langle 0, 2\sqrt{2}, 2\sqrt{2} \rangle$ or $\langle 0, 2\sqrt{2}, -2\sqrt{2} \rangle$
 71. 3.64 lb 73. True. $\cos^{-1} 0 = 90^\circ$
 75. Sphere of radius 4 centered at (x_1, y_1, z_1)

Section 10.3 (page 731)

1. cross product 3. $\|\mathbf{u}\| \|\mathbf{v}\| \sin \theta$ 5. $\langle -1, 0, 2 \rangle$
 7. $\langle 1, 1, 1 \rangle$ 9. $\langle 3, -3, -3 \rangle$ 11. $\langle 0, 42, 0 \rangle$
 13. $-7\mathbf{i} + 13\mathbf{j} + 16\mathbf{k}$ 15. $-17\mathbf{i} + \mathbf{j} + 10\mathbf{k}$
 17. $-\frac{7}{6}\mathbf{i} - \frac{7}{8}\mathbf{j}$ 19. $-18\mathbf{i} - 6\mathbf{j}$ 21. $-\mathbf{i} - 2\mathbf{j} - \mathbf{k}$
 23. $\langle 10, -2, -4 \rangle$ 25. $-6\mathbf{i} - 15\mathbf{j} - 6\mathbf{k}$
 27. $-\frac{1}{4}\mathbf{i} - \frac{7}{10}\mathbf{j} - 2\mathbf{k}$ 29. $\frac{1}{3}\mathbf{i} - \frac{2}{3}\mathbf{j} - \frac{2}{3}\mathbf{k}$
 31. $\frac{\sqrt{19}}{19}(\mathbf{i} - 3\mathbf{j} + 3\mathbf{k})$ 33. $\frac{\sqrt{7602}}{7602}(-71\mathbf{i} - 44\mathbf{j} + 25\mathbf{k})$
 35. $\frac{\sqrt{2}}{2}(\mathbf{i} - \mathbf{j})$ 37. 1 39. $\sqrt{806}$ 41. 56
 43. (a) Answers will vary. (b) $6\sqrt{10}$
 (c) The parallelogram is not a rectangle.
 45. $\frac{3\sqrt{13}}{2}$ 47. $\frac{1}{2}\sqrt{4290}$ 49. -16
 51. 2 53. 2 55. 12 57. 84
 59. (a) $T(p) = \frac{p}{2} \cos 40^\circ$

(b)	p	15	20	25	30	35	40	45
	T	5.75	7.66	9.58	11.49	13.41	15.32	17.24

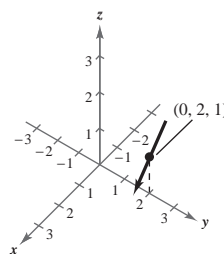
61. True. The cross product is defined only for three-dimensional vectors.

63. Proof 65. Proof 67. $-\frac{1}{2}$

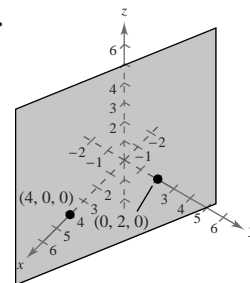
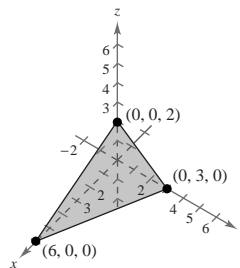
Section 10.4 (page 740)

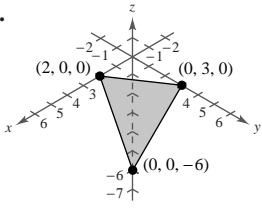
1. direction 3. perpendicular 5. yz -plane
 7. (a) $x = t, y = 2t, z = 3t$ (b) $x = \frac{y}{2} = \frac{z}{3}$
 9. (a) $x = -4 + 3t, y = 1 + 8t, z = -6t$
 (b) $\frac{x+4}{3} = \frac{y-1}{8} = \frac{z}{-6}$
 11. (a) $x = 2 + 2t, y = -3 - 3t, z = 5 + t$
 (b) $\frac{x-2}{2} = \frac{y+3}{-3} = \frac{z-5}{1}$
 13. (a) $x = 2 - t, y = 4t, z = 2 - 5t$
 (b) $\frac{x-2}{-1} = \frac{y}{4} = \frac{z-2}{-5}$
 15. (a) $x = -3 + 4t, y = 8 - 10t, z = 15 + t$
 (b) $\frac{x+3}{4} = \frac{y-8}{-10} = \frac{z-15}{1}$
 17. (a) $x = 3 - 4t, y = 1, z = 2 + 3t$ (b) Not possible
 19. (a) $x = -\frac{1}{2} + 3t, y = 2 - 5t, z = \frac{1}{2} - t$
 (b) $\frac{x+\frac{1}{2}}{3} = \frac{y-2}{-5} = \frac{z-\frac{1}{2}}{-1}$

21.



23. $x - 2 = 0$ 25. $-2x + y - 2z + 10 = 0$
 27. $-x - 2y + z + 2 = 0$ 29. $-3x - 9y + 7z = 0$
 31. $6x - 2y - z - 8 = 0$ 33. $y - 5 = 0$
 35. $y - z + 2 = 0$ 37. $7x + y - 11z - 5 = 0$
 39. $x = 2, y = 3, z = 4 + t$
 41. $x = 2 + 3t, y = 3 + 2t, z = 4 - t$
 43. $x = 5 + 2t, y = -3 - t, z = -4 + 3t$
 45. $x = 2 - t, y = 1 + t, z = 2 + t$
 47. Orthogonal 49. Orthogonal
 51. (a) 60.67° (b) $x = 2 - t, y = 8t, z = 7t$
 53. (a) 77.83° (b) $x = 1 + 6t, y = t, z = 1 + 7t$
 55. 57.



59.  61. $\frac{8}{9}$ 63. $\frac{2\sqrt{6}}{3}$ 65. 88.45°

67. False. Lines that do not intersect and are not in the same plane may not be parallel.

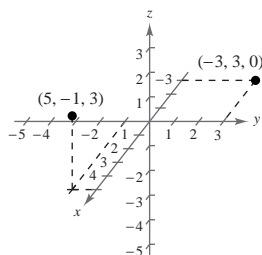
69. The point and the vector are reversed. The correct answer should be:

$$\frac{x-1}{3} = \frac{y-2}{5} = \frac{z-6}{4}$$

71. Parallel. $\langle 10, -18, 20 \rangle$ is a scalar multiple of $\langle -15, 27, -30 \rangle$.

Review Exercises (page 744)

1.



3. $(-5, 3, 0)$ 5. $\sqrt{30}$ 7. $\sqrt{29}, \sqrt{38}, \sqrt{67}$

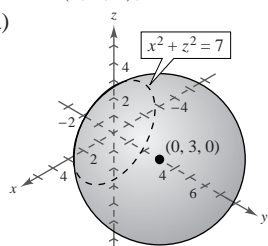
9. $(0, -1, -1)$ 11. $(1, 1, -9)$

13. $(x-2)^2 + (y-3)^2 + (z-5)^2 = 1$

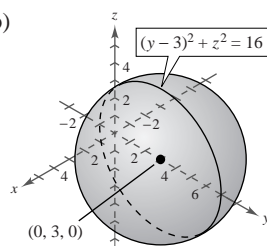
15. $(x-1)^2 + (y-5)^2 + (z-2)^2 = 36$

17. Center: $(2, 3, 0)$; radius: 3

19. (a)



(b)



21. (a) $\langle 1, 4, -3 \rangle$ (b) $\sqrt{26}$ (c) $\frac{\sqrt{26}}{26} \langle 1, 4, -3 \rangle$

23. (a) $\langle -10, 6, 7 \rangle$ (b) $\sqrt{185}$ (c) $\frac{\sqrt{185}}{185} \langle -10, 6, 7 \rangle$

25. -9 27. 1 29. 90° 31. 90° 33. Orthogonal

35. Orthogonal 37. Not collinear 39. Collinear

41. A: 159.10 lb of tension

B: 115.58 lb of tension

C: 115.58 lb of tension

43. $\langle -10, 0, -10 \rangle$

45. $\frac{\sqrt{7602}}{7602} (-71\mathbf{i} - 44\mathbf{j} + 25\mathbf{k})$

47. (a) Answers will vary. (b) $2\sqrt{43}$
(c) The parallelogram is not a rectangle.

49. 75

51. (a) $x = 3 + 6t, y = 11t, z = 2 + 4t$

(b) $\frac{x-3}{6} = \frac{y}{11} = \frac{z-2}{4}$

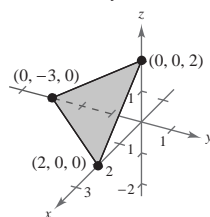
53. (a) $x = -1 + 4t, y = 3 + 3t, z = 5 - 6t$

(b) $\frac{x+1}{4} = \frac{y-3}{3} = \frac{z-5}{-6}$

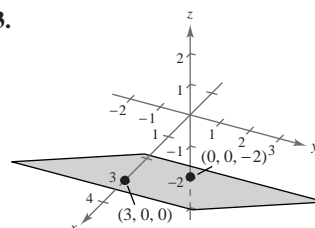
55. (a) $x = -2t, y = \frac{5}{2}t, z = t$ (b) $\frac{x}{-2} = \frac{y}{5/2} = z$

57. $-2x - 12y + 5z = 0$ 59. $z - 2 = 0$

61.



63.



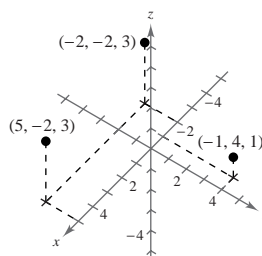
65. $\frac{\sqrt{110}}{110}$ 67. $\frac{\sqrt{110}}{55}$

69. False. $\mathbf{u} \times \mathbf{v} = -(\mathbf{v} \times \mathbf{u})$ 71 and 73. Answers will vary.

75. $\mathbf{u} \times \mathbf{v} = (u_2v_3 - u_3v_2)\mathbf{i} - (u_1v_3 - u_3v_1)\mathbf{j} + (u_1v_2 - u_2v_1)\mathbf{k}$

Chapter Test (page 746)

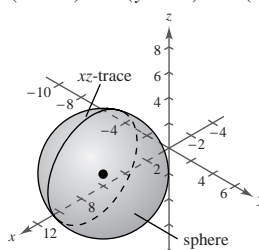
1.



2. No. Answers will vary.

3. $(7, 1, 2)$

4. $(x-7)^2 + (y-1)^2 + (z-2)^2 = 19$



5. $\langle 2, 5, -10 \rangle; \sqrt{129}$ 6. $\langle -3, -5, 8 \rangle; 7\sqrt{2}$

7. $\mathbf{u} = \langle -2, 6, -6 \rangle, \mathbf{v} = \langle -12, 5, -5 \rangle$

8. (a) $\sqrt{194}$ (b) 84 (c) $\langle 0, 62, 62 \rangle$ 9. 46.23°

10. Answers will vary. Sample answer:

(a) $x = 8 - 2t, y = -2 + 6t, z = 5 - 6t$

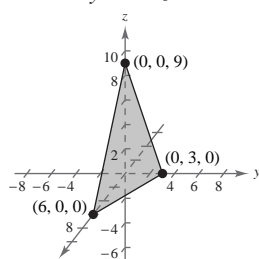
(b) $\frac{x-8}{-2} = \frac{y+2}{6} = \frac{z-5}{-6}$

11. Neither 12. Orthogonal

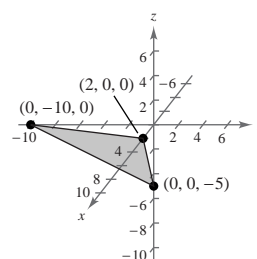
13. Answers will vary; $2\sqrt{230}$

14. $27x + 4y + 32z + 33 = 0$ 15. 200

16.



17.



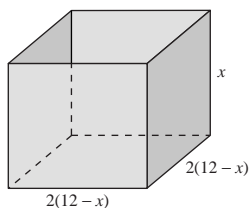
18. $\frac{4\sqrt{14}}{7}$

Chapter 11

Section 11.1 (page 757)

1. limit 3. 3

5. (a)



(b) Answers will vary.

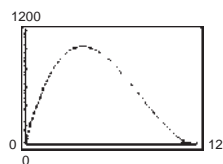
(c)

x	3	3.5	3.9	4
V	972	1011.5	1023.5	1024

x	4.1	4.5	5
V	1023.5	1012.5	980

$$\lim_{x \rightarrow 4} V = 1024$$

(d)



7.

x	1.9	1.99	1.999	2
$f(x)$	13.5	13.95	13.995	14

x	2.001	2.01	2.1
$f(x)$	14.005	14.05	14.5

14; Yes

9.

x	-1.1	-1.01	-1.001	-1
$f(x)$	-0.3226	-0.3322	-0.3332	Error

x	-0.999	-0.99	-0.9
$f(x)$	-0.3334	-0.3344	-0.3448

-0.3333; No

11.

x	-0.1	-0.01	-0.001	0
$f(x)$	0.5017	0.50002	0.5000002	Error

x	0.001	0.01	0.1
$f(x)$	0.5000002	0.50002	0.5017

0.5; No

13.

x	-1.1	-1.01	-1.001	-1
$f(x)$	-2.1	-2.01	-2.001	Error

x	-0.999	-0.99	-0.9
$f(x)$	-1.999	-1.99	-1.9

-2

15.

x	0.9	0.99	0.999	1
$f(x)$	0.2564	0.2506	0.2501	Error

x	1.001	1.01	1.1
$f(x)$	0.2499	0.2494	0.2439

0.25

17.

x	-0.1	-0.01	-0.001	0
$f(x)$	0.2247	0.2237	0.2236	Error

x	0.001	0.01	0.1
$f(x)$	0.2236	0.2235	0.2225

0.2236

19.

x	-4.1	-4.01	-4.001	-4
$f(x)$	0.4762	0.4975	0.4998	Error

x	-3.999	-3.99	-3.9
$f(x)$	0.5003	0.5025	0.5263

0.5

21.

x	-0.1	-0.01	-0.001	0
$f(x)$	0.9983	0.99998	0.9999998	Error

x	0.001	0.01	0.1
$f(x)$	0.9999998	0.99998	0.9983

1

23.

x	-0.1	-0.01	-0.001	0
$f(x)$	-0.0997	-0.0100	-0.0010	Error

x	0.001	0.01	0.1
$f(x)$	0.0010	0.0100	0.0997

0

25.

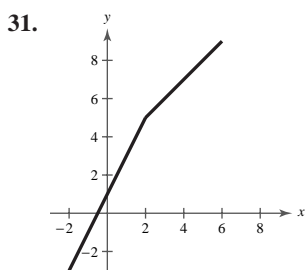
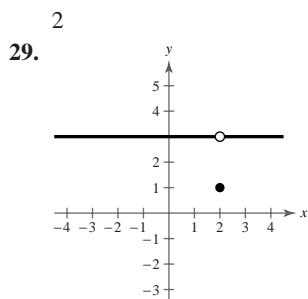
x	-0.1	-0.01	-0.001	0
$f(x)$	0.9063	0.9901	0.9990	Error

x	0.001	0.01	0.1
$f(x)$	1.0010	1.0101	1.1070

27.

x	1.9	1.99	1.999	2
$f(x)$	2.2314	2.0203	2.002	Error

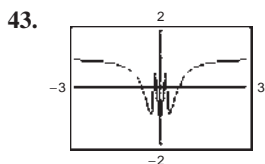
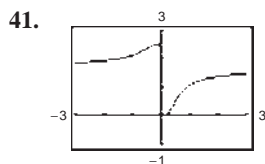
x	2.001	2.01	2.1
$f(x)$	1.998	1.9803	1.8232



$$\lim_{x \rightarrow 2} f(x) = 3$$

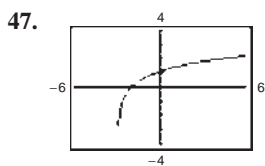
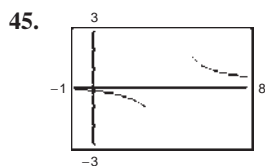
$$\lim_{x \rightarrow 2} f(x) = 5$$

33. 2
 35. Limit does not exist; One-sided limits do not agree.
 37. Limit does not exist; One-sided limits do not agree.
 39. Limit does not exist; Function oscillates between -2 and 2.



No

No



No

Yes

49. (a) -16 (b) 12 (c) $\frac{1}{2}$ (d) 2
 51. (a) 8 (b) $\frac{3}{8}$ (c) 3 (d) $-\frac{61}{8}$
 53. -15 55. 7 57. $-\frac{9}{10}$ 59. $\frac{7}{13}$ 61. 1
 63. e^3 65. 0 67. $\frac{\pi}{6}$

69. True. See Condition 1 on page 754.
 71. (a) and (b) Answers will vary.
 73. (a) No. The function may approach different values from the right and left of 4.
 (b) No. The function may approach 4 as x approaches 2, but the function could be undefined at $x = 2$.
 75. $-\frac{1}{3}$, $x \neq 5$

77. $\frac{5x+4}{5x+2}$, $x \neq \frac{1}{3}$ 79. $\frac{x^2-3x+9}{x-2}$, $x \neq -3$

Section 11.2 (page 767)

1. dividing out technique 3. Rationalizing technique
 5. (a) 1 (b) 3 (c) 5
 $g_2(x) = -2x + 1$
 7. (a) 2 (b) 0 (c) 0
 $g_2(x) = x(x+1)$
 9. $\frac{1}{12}$ 11. 3 13. 4 15. 12 17. 80 19. $\frac{7}{2}$
 21. $\frac{1}{3}$ 23. $\frac{\sqrt{5}}{10}$ 25. $\frac{1}{4}$ 27. -1 29. $-\frac{1}{16}$
 31. 0 33. 0 35. 0

37.

x	-0.1	-0.01	-0.001	0
$f(x)$	1.813	1.980	1.998	Error

x	0.001	0.01	0.1
$f(x)$	2.002	2.020	2.214

2.000

39.

x	-0.1	-0.01	-0.001	0
$f(x)$	1.056	1.005	1.001	Error

x	0.001	0.01	0.1
$f(x)$	0.9995	0.995	0.954

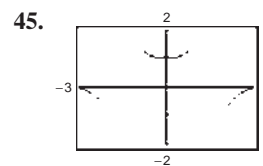
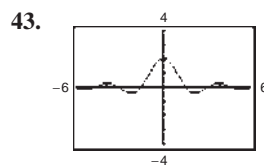
1.000

41.

x	-0.1	-0.01	-0.001	0
$f(x)$	0.149	0.137	0.135	Error

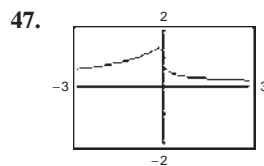
x	0.001	0.01	0.1
$f(x)$	0.135	0.134	0.122

0.135



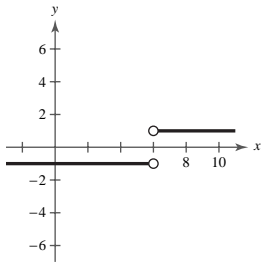
2.000

1.000



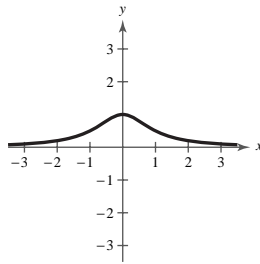
0.333

49.



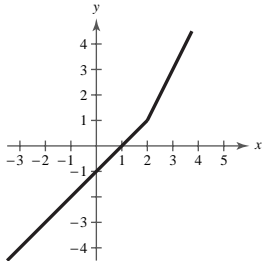
Limit does not exist.

51.



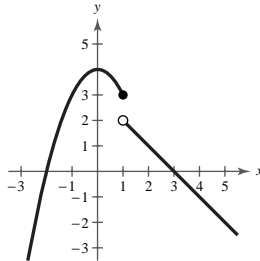
$$\lim_{x \rightarrow 1} f(x) = \frac{1}{2}$$

53.



$$\lim_{x \rightarrow 2} f(x) = 1$$

55.

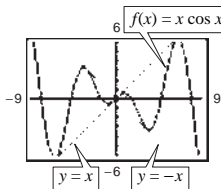


Limit does not exist.

 57. (a) and (b) 0.50 (c) $\frac{1}{2}$

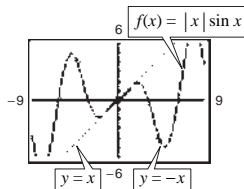
 59. (a) and (b) -0.13 (c) $-\frac{1}{8}$

61.



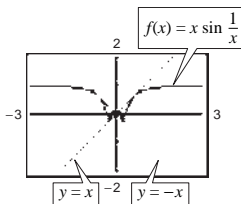
$$\lim_{x \rightarrow 0} f(x) = 0$$

63.



$$\lim_{x \rightarrow 0} f(x) = 0$$

65.

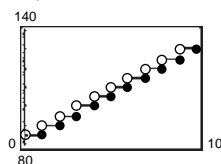


$$\lim_{x \rightarrow 0} f(x) = 0$$

67. (a) Direct substitution; 0 (b) 1

69. -32 ft/sec 71. Answers will vary.

73. (a)



x	5	5.3	5.4	5.5	5.6	5.7	6
$C(x)$	105	110	110	110	110	110	110

$$\lim_{x \rightarrow 5.5} C(x) = 110$$

x	4	4.5	4.9	5	5.1	5.5	6
$C(x)$	100	105	105	105	110	110	110

The limit does not exist.

75. 3 77. $\frac{1}{2\sqrt{x}}$ 79. $2x - 3$ 81. $-\frac{1}{(x+2)^2}$

83. True. See page 761. 85-87. Answers will vary.

89. Parabola 91. Hyperbola

93. Orthogonal 95. Neither

Section 11.3 (page 777)

1. Calculus 3. secant line

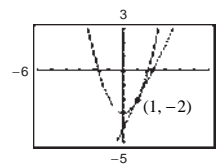
 5. 2 7. 0 9. $\frac{1}{2}$ 11. 2 13. -2

 15. -1 17. $\frac{1}{6}$ 19. $m = -2x$; (a) 0 (b) 4

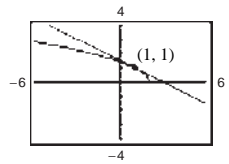
 21. $m = -\frac{1}{(x+4)^2}$; (a) $-\frac{1}{16}$ (b) $-\frac{1}{4}$

 23. $m = \frac{1}{2\sqrt{x-1}}$; (a) $\frac{1}{2}$ (b) $\frac{1}{6}$

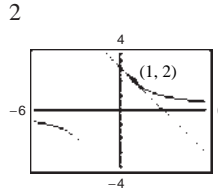
25.



27.



29.


 31. -6x 33. 0 35. $-\frac{1}{3}$

 37. $-\frac{2}{x^3}$ 39. $\frac{1}{2\sqrt{x-4}}$

 41. $-\frac{1}{2(x-9)^{3/2}}$

43. (a) 4

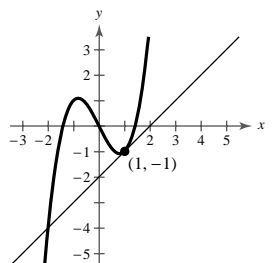
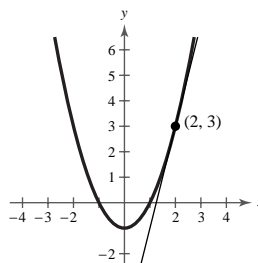
 (b) $y = 4x - 5$

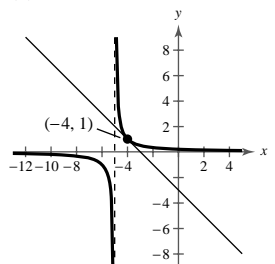
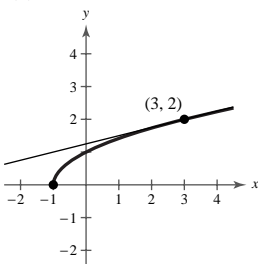
(c)

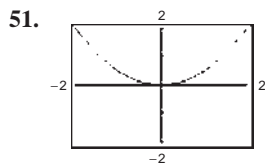
45. (a) 1

 (b) $y = x - 2$

(c)


 47. (a) $\frac{1}{4}$
 (b) $y = \frac{1}{4}x + \frac{5}{4}$
 (c)

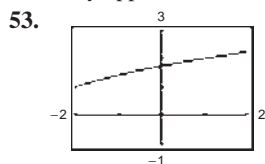
 49. (a) -1
 (b) $y = -x - 3$
 (c)




x	-2	-1.5	-1	-0.5	0
$f(x)$	2	1.125	0.5	0.125	0
$f'(x)$	-2	-1.5	-1	-0.5	0

x	0.5	1	1.5	2
$f(x)$	0.125	0.5	1.125	2
$f'(x)$	0.5	1	1.5	2

They appear to be the same.



x	-2	-1.5	-1	-0.5	0
$f(x)$	1	1.225	1.414	1.581	1.732
$f'(x)$	0.5	0.408	0.354	0.316	0.289

x	0.5	1	1.5	2
$f(x)$	1.871	2	2.121	2.236
$f'(x)$	0.267	0.25	0.236	0.224

They appear to be the same.

55. $f'(x) = 2x - 4$; $(2, -1)$

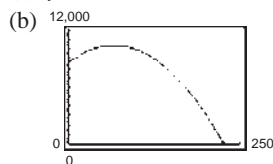
57. $f'(x) = 9x^2 - 9$; $(-1, 6)$, $(1, -6)$

59. $(-1, -1)$, $(0, 0)$, $(1, -1)$

61. $\left(\frac{\pi}{6}, \sqrt{3} + \frac{\pi}{6}\right)$, $\left(\frac{5\pi}{6}, \frac{5\pi}{6} - \sqrt{3}\right)$

63. $(0, 0)$, $(-2, 4e^{-2})$ 65. $(e^{-1}, -e^{-1})$

67. (a) $y = -0.41t^2 + 54.7t + 8529$



38; The population is increasing by approximately 38,000 people per year in 2020.

(c) $y' = -0.82t + 54.7$; 38.3

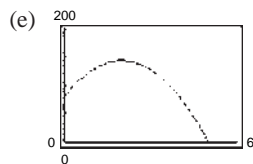
(d) Answers will vary.

69. (a) $V'(r) = 4\pi r^2$ (b) About 201.06

(c) Cubic inches per inch; The derivative is a formula for rate of change.

71. (a) $s'(t) = -32t + 64$ (b) 16 ft/sec

(c) $t = 2$ sec; Answers will vary. (d) -96 ft/sec

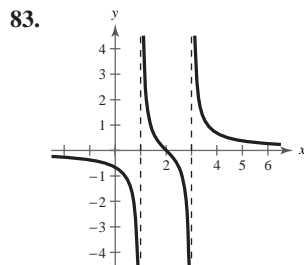


73. True. The graph of the derivative is a line, which is a one-to-one function.

75. b 76. a 77. d 78. c

79. Answers will vary. Sample answer: A sketch of any linear function with positive slope

81. Answers will vary. Sample answer: A sketch of any quadratic function of the form $y = a(x - 1)^2 + k$, where $a > 0$



Section 11.4 (page 786)

1. 5 3. converge 5. c 6. a 7. d 8. b

9. f 10. g 11. h 12. e 13. 0 15. -1

17. $\frac{5}{6}$ 19. -4 21. Limit does not exist. 23. $\frac{4}{3}$

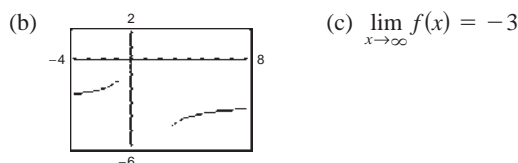
25. 2 27. -1 29. -4 31. -5

33. (a)

x	10^0	10^1	10^2	10^3
$f(x)$	Error	-3.33	-3.03	-3.003

x	10^4	10^5	10^6
$f(x)$	-3.0003	-3.00003	-3.000003

-3



(c) $\lim_{x \rightarrow \infty} f(x) = -3$

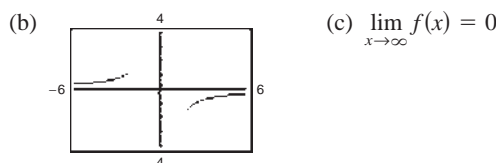
-3

35. (a)

x	10^0	10^1	10^2	10^3
$f(x)$	Error	-0.202	-0.0200	-0.002

x	10^4	10^5	10^6
$f(x)$	-0.0002	-0.00002	-0.000002

0



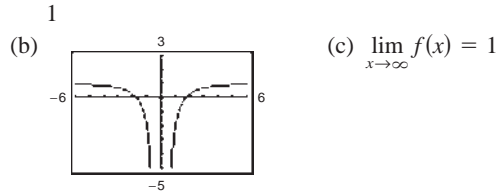
(c) $\lim_{x \rightarrow \infty} f(x) = 0$

0

37. (a)

x	10^0	10^1	10^2	10^3
$f(x)$	-2	0.97	0.9997	0.999997

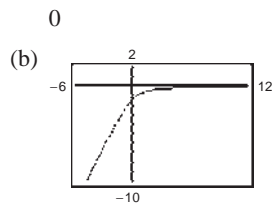
x	10^4	10^5	10^6
$f(x)$	0.99999997	0.999999997	1



39. (a)

x	10^0	10^1	10^2	10^3
$f(x)$	-0.7321	-0.0995	-0.0100	-0.0010

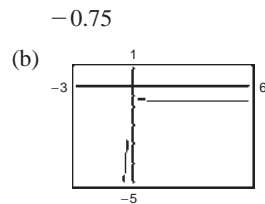
x	10^4	10^5	10^6
$f(x)$	-1.0×10^{-4}	-1.0×10^{-5}	-1.0×10^{-6}



41. (a)

x	10^0	10^1	10^2	10^3
$f(x)$	-0.7082	-0.7454	-0.7495	-0.74995

x	10^4	10^5	10^6
$f(x)$	-0.749995	-0.7499995	-0.7500



43. $1, \frac{3}{5}, \frac{2}{5}, \frac{5}{17}, \frac{3}{13}$
Limit: 0

47. $\frac{1}{5}, \frac{1}{2}, \frac{9}{11}, \frac{8}{7}, \frac{25}{17}$
Limit does not exist.

51. $-1, \frac{1}{2}, -\frac{1}{3}, \frac{1}{4}, -\frac{1}{5}$
Limit: 0

45. $\frac{1}{3}, \frac{2}{5}, \frac{3}{7}, \frac{4}{9}, \frac{5}{11}$
Limit: $\frac{1}{2}$

49. 2, 3, 4, 5, 6
Limit does not exist.

53.

n	10^0	10^1	10^2	10^3
a_n	2	1.55	1.505	1.5005

1.5
 $\lim_{n \rightarrow \infty} a_n = \frac{3}{2}$

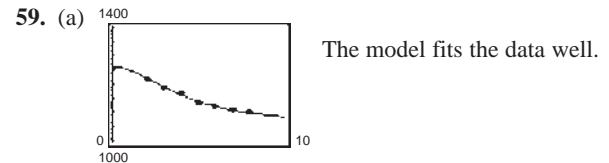
55.

n	10^0	10^1	10^2	10^3
a_n	13.33	5.683	5.06683	5.0066683

5
 $\lim_{n \rightarrow \infty} a_n = 5$

57. (a) $\bar{C} = \frac{13.50x + 45,750}{x}$ (b) \$471; \$59.25

(c) \$13.50; As the number of PDAs produced gets very large, the average cost approaches \$13.50.



(b) 2009: 1,092,000
2010: 1,086,000

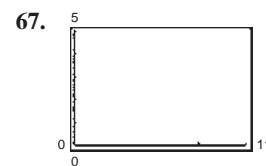
(c) 1,056,000; As time passes, the number of United States military reserve personnel approaches 1,056,000.

(d) Answers will vary.

61. False. $y = \frac{x^2}{x+1}$ does not have a horizontal asymptote.

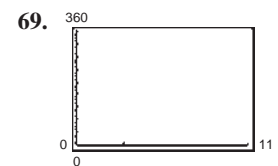
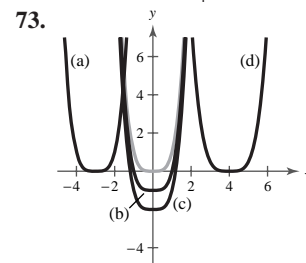
63. True. See page 784.

65. Answers will vary. Sample answer: Let $f(x) = x^2$ and $g(x) = x^2$. Then $\lim_{x \rightarrow \infty} x^2 = \infty$ and $\lim_{x \rightarrow \infty} [f(x) - g(x)] = 0$.



Converges to 0

71. The limit is $-\frac{1}{4}$.



Diverges

75. 60 77. 150

Section 11.5 (page 794)

1. $\frac{n(n+1)}{2}$ 3. 100 rectangles 5. 420 7. 44,100
9. 44,140 11. 5850

13. (a) $S(n) = \frac{n^2 + 2n + 1}{4n^2}$

n	10^0	10^1	10^2	10^3	10^4
$S(n)$	1	0.3025	0.2550	0.2505	0.2501

(c) $\lim_{n \rightarrow \infty} S(n) = \frac{1}{4}$

15. (a) $S(n) = \frac{2n^2 + 3n + 7}{2n^2}$

n	10^0	10^1	10^2	10^3	10^4
$S(n)$	6	1.185	1.0154	1.0015	1.0002

(c) $\lim_{n \rightarrow \infty} S(n) = 1$

17. (a) $S(n) = \frac{14n^2 + 3n + 1}{6n^3}$

n	10^0	10^1	10^2	10^3	10^4
$S(n)$	3	0.2385	0.0234	0.0023	0.0002

(c) $\lim_{n \rightarrow \infty} S(n) = 0$

19. 14.25 21. 1.27

n	4	8	20	50
Approximate area	18	21	22.8	23.52

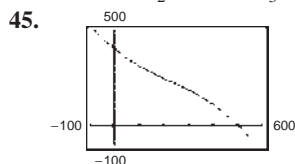
n	4	8	20	50
Approximate area	3.5156	2.8477	2.4806	2.3409

n	4	8	20	50	100	∞
Area	40	38	36.8	36.32	36.16	36

n	4	8	20	50	100	∞
Area	14.25	14.81	15.13	15.25	15.29	$\frac{46}{3}$

n	4	8	20	50	100	∞
Area	19	18.5	18.2	18.08	18.04	18

33. 3 35. $\frac{15}{2}$ 37. $\frac{128}{3}$ 39. $\frac{3}{4}$ 41. $\frac{3}{4}$ 43. 144



105,208.33 ft²

47. True. See Formula 2 on page 789. 49. c

Review Exercises (page 798)

x	2.9	2.99	2.999	3
$f(x)$	16.4	16.94	16.994	17

x	3.001	3.01	3.1
$f(x)$	17.006	17.06	17.6

17; Yes

x	-0.1	-0.01	-0.001	0
$f(x)$	1.0517	1.0050	1.0005	Error

x	0.001	0.01	0.1
$f(x)$	0.9995	0.9950	0.9516

1; No

5. 2 7. Limit does not exist.

9. (a) 8 (b) 1 (c) 10 (d) $\frac{2}{5}$

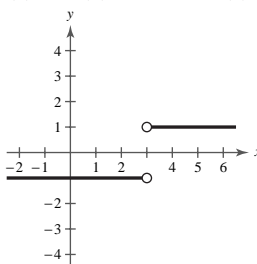
11. 5 13. $\frac{10}{3}$ 15. -2 17. 0 19. e

21. $-\frac{\pi}{6}$ 23. $-\frac{1}{4}$ 25. $\frac{1}{15}$ 27. -9 29. -1

31. $\frac{1}{4}$ 33. (a) and (b) 0.17 35. Limit does not exist.

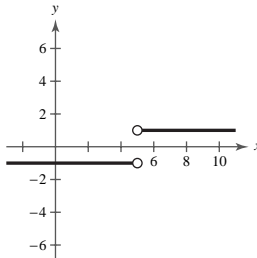
37. (a) and (b) 2 39. (a) and (b) 0.577

41.



Limit does not exist.

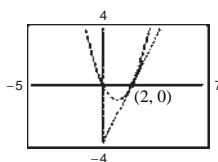
45.



Limit does not exist.

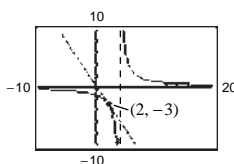
49. $3 - 2x$ 51. 2

53.



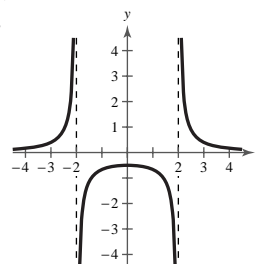
2

57.



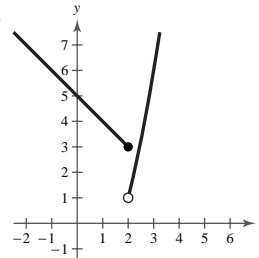
$-\frac{3}{2}$

43.



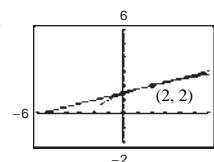
Limit does not exist.

47.



Limit does not exist.

55.



$\frac{1}{4}$

59. $m = 2x - 4$; (a) -4 (b) 6

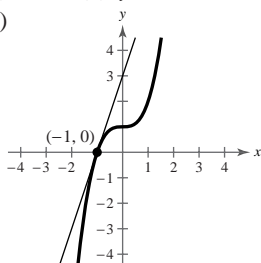
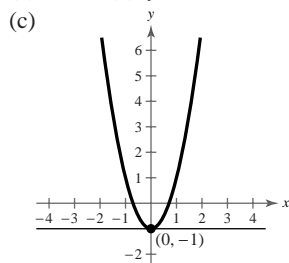
61. $m = -\frac{4}{(x-6)^2}$; (a) -4 (b) -1

63. $f'(x) = 0$ 65. $h'(x) = -\frac{1}{2}$ 67. $g'(x) = 4x$

69. $f'(t) = \frac{1}{2\sqrt{t+5}}$ 71. $g'(s) = -\frac{4}{(s+5)^2}$

73. $g'(x) = -\frac{1}{2(x+4)^{3/2}}$

75. (a) 0 (b) $y = -1$ 77. (a) 3 (b) $y = 3x + 3$



79. 2 81. 0 83. Limit does not exist. 85. 3

87. $-\frac{1}{9}, \frac{1}{14}, \frac{3}{19}, \frac{5}{24}, \frac{7}{29}$ 89. $-1, \frac{1}{8}, -\frac{1}{27}, \frac{1}{64}, -\frac{1}{125}$

Limit: $\frac{2}{5}$

Limit: 0

91. $-\frac{1}{2}, -\frac{9}{8}, -\frac{7}{6}, -\frac{37}{32}, -\frac{57}{50}$

Limit: -1

93. (a) $S(n) = \frac{5n^2 + 9n + 4}{6n^2}$

n	10^0	10^1	10^2	10^3	10^4
$S(n)$	3	0.99	0.8484	0.8348	0.8335

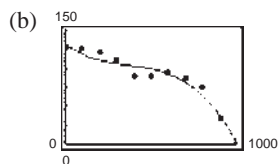
(c) $\frac{5}{6}$

95. 6.75

n	4	8	20	50
Approximate area	7.5	6.375	5.74	5.4944

99. 50 101. 21 103. 68

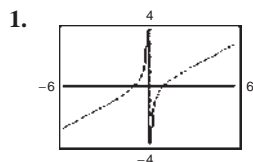
105. (a) $y = (-3.376 \times 10^{-7})x^3 + (3.753 \times 10^{-4})x^2 - 0.168x + 132$



(c) $88,700 \text{ ft}^2$

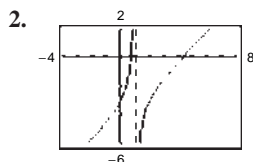
107. True. See page 775.

Chapter Test (page 801)

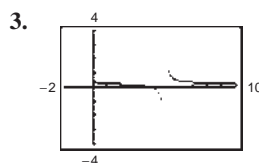


-0.75

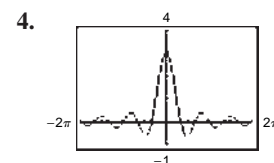
$\lim_{x \rightarrow -2} f(x) = -\frac{3}{4}$



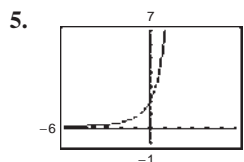
Limit does not exist.



Limit does not exist.



3.0000



2.0000

6. (a) $m = 6x - 5$; 7 (b) $m = 6x^2 + 6$; 12

7. $f'(x) = -\frac{2}{5}$ 8. $f'(x) = 4x + 4$

9. $f'(x) = -\frac{1}{(x+1)^2}$ 10. 0 11. -3

12. Limit does not exist.

13. $0, \frac{3}{4}, \frac{14}{19}, \frac{12}{17}, \frac{36}{53}$

14. $0, 1, 0, \frac{1}{2}, 0$

Limit: $\frac{1}{2}$

Limit: 0

15. 12.5 16. 8 17. $\frac{34}{3}$

18. (a) $y = 8.79x^2 - 6.2x - 0.4$ (b) 81.7 ft/sec

Cumulative Test for Chapters 10 and 11 (page 802)

1. $(-6, 1, 2)$ 2. $(0, -5, 0)$ 3. $\sqrt{149}$

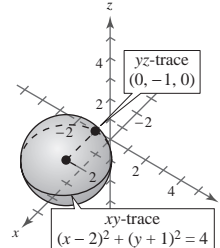
4. $3, 4, 5$ 5. $(-1, 2, \frac{1}{2})$

6. $(x-2)^2 + (y-2)^2 + (z-4)^2 = 24$

7.

8. $\mathbf{u} \cdot \mathbf{v} = -38$

$\mathbf{u} \times \mathbf{v} = \langle -18, -6, -14 \rangle$



9. Neither 10. Orthogonal 11. Parallel 12. 12

13. (a) $x = -2 + 7t, y = 3 + 5t, z = 25t$

(b) $\frac{x+2}{7} = \frac{y-3}{5} = \frac{z}{25}$

14. $x = -1 + 2t, y = 2 - 4t, z = t$ 15. $75x + 50y - 31z = 0$

16. $\frac{\sqrt{30}}{2}$ 17. 84.26°

19. 4 20. $-\frac{1}{3}$ 21. $\frac{1}{14}$

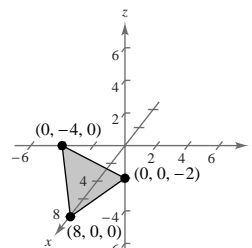
22. $\frac{1}{4}$ 23. -1

24. Limit does not exist.

25. $-\frac{1}{9}$ 26. $\frac{1}{8}$ 27. $\frac{1}{4}$

28. $m = -2x; 4$

29. $m = \frac{1}{2}(x+3)^{-1/2}; \frac{1}{2}$



30. $m = -(x+3)^{-2}; -\frac{1}{16}$ 31. $m = 2x - 1; 1$

32. Limit does not exist. 33. -7 34. 3 35. 0

36. 0 37. Limit does not exist. 38. $-42,875$

39. 8190 40. $672,880$ 41. 10.5 42. 8.13

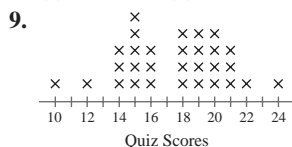
43. 2.69 44. 1.57 45. $\frac{5}{2}$ 46. $\frac{76}{3}$ 47. $\frac{16}{3}$ 48. $\frac{3}{4}$

Appendices

Appendix B.1 (page A31)

1. Line plots 3. frequency distribution 5. scatter plot

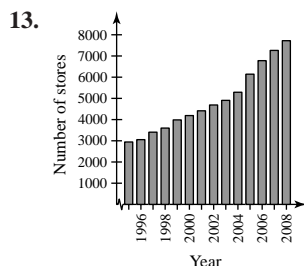
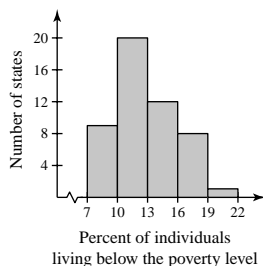
7. (a) 2.979 (b) 0.19



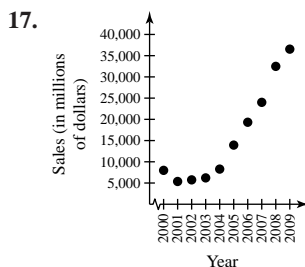
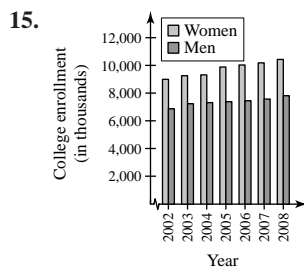
15

11. Sample answer:

Interval	Tally
[7, 10)	
[10, 13)	
[13, 16)	
[16, 19)	
[19, 22)	

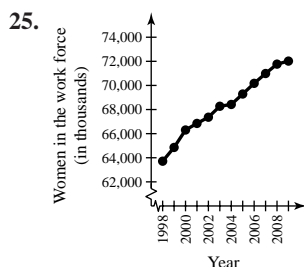


Answers will vary.
Sample answer: As time progresses from 1995 to 2008, the number of Wal-Mart stores increases at a fairly constant rate.



19. The price decreased slightly from 2000 to 2002.

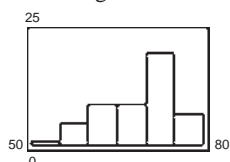
21. From 2001 to 2002 23. About 40%



Answers will vary.
Sample answer: As time progresses from 1998 to 2009, the number of women in the work force increases at a fairly constant rate.

27. 65 29. Yes

31. Answers will vary. Sample answer: A histogram is best because the data are percents within a year that do not relate to increasing or decreasing behavior.



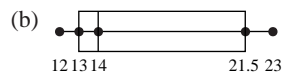
33. A bar graph is similar to a histogram, except that the bars can be either horizontal or vertical and the labels of the bars are not necessarily numbers. Another difference between a bar graph and a histogram is that the bars in a bar graph are usually separated by spaces.

35. Line plots are useful for ordering small sets.
Histograms or bar graphs can be used to organize larger sets.
Line graphs are used to show trends over periods of time.

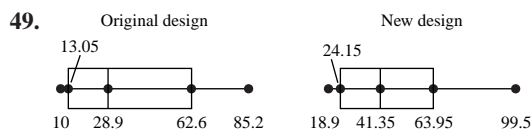
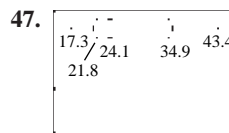
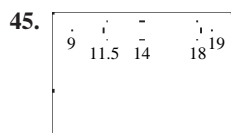
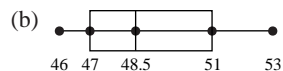
Appendix B.2 (page A41)

1. measure, central tendency
3. variance, standard deviation
5. Mean: About 8.86; median: 8; mode: 7
7. Mean: About 10.29; median: 8; mode: 7
9. Mean: 9; median: 8; mode: 7
11. (a) The mean; Answers will vary.
(b) Mean: About 14.86; median: 14; mode: 13
Each is increased by 6.
(c) Each will increase by k .
13. Mean: 320; median: 320; mode: 320
15. (a) Jay: 199.67; Hank: 199.67; Buck: 229.33
(b) 209.56 (c) 202
17. Answers will vary. Sample answer: {4, 4, 10}
19. The median
21. (a) $\bar{x} = 12$; $\sigma \approx 2.83$ (b) $\bar{x} = 20$; $\sigma \approx 2.83$
(c) $\bar{x} = 12$; $\sigma \approx 1.41$ (d) $\bar{x} = 9$; $\sigma \approx 1.41$
23. $\bar{x} = 6$, $v = 10$, $\sigma \approx 3.16$
25. $\bar{x} = 2$, $v = \frac{4}{3}$, $\sigma \approx 1.15$ 27. $\bar{x} = 4$, $v = 4$, $\sigma = 2$
29. $\bar{x} = 47$, $v = 226$, $\sigma \approx 15.03$
31. 3.42 33. 1.65
35. $\bar{x} = 12$ and $|x_i - 12| = 8$ for all x_i .
37. The mean will increase by 5, but the standard deviation will not change.
39. [179, 291]; [151, 319]
[203, 267]; [187, 283]

41. (a) Upper quartile: 21.5
Lower quartile: 13



43. (a) Upper quartile: 51
Lower quartile: 47



From the plots, you can see that the lifetimes of the sample units made by the new design are greater than the lifetimes of the sample units made by the original design. (The median lifetime increased by more than 12 months.)

Appendix B.3 (page A45)

1. $y = 1.6x + 7.5$ 3. $y = 0.262x + 1.93$

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Go to this textbook's *Companion Website* for a complete list of applications.

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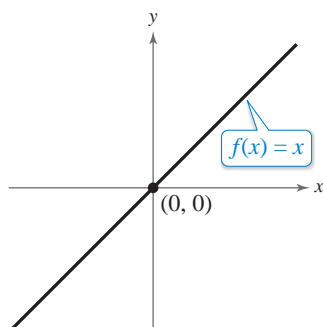
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Library of Parent Functions Summary

Linear Function (p. 6)

$$f(x) = x$$



Domain: $(-\infty, \infty)$

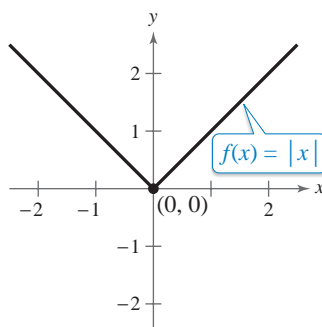
Range: $(-\infty, \infty)$

Intercept: $(0, 0)$

Increasing

Absolute Value Function (p. 19)

$$f(x) = |x| = \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$$



Domain: $(-\infty, \infty)$

Range: $[0, \infty)$

Intercept: $(0, 0)$

Decreasing on $(-\infty, 0)$

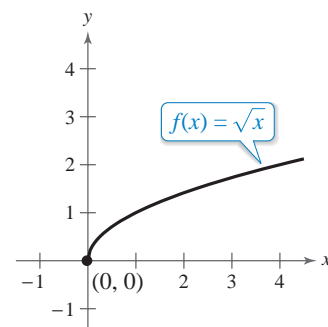
Increasing on $(0, \infty)$

Even function

y-axis symmetry

Square Root Function (p. 20)

$$f(x) = \sqrt{x}$$



Domain: $[0, \infty)$

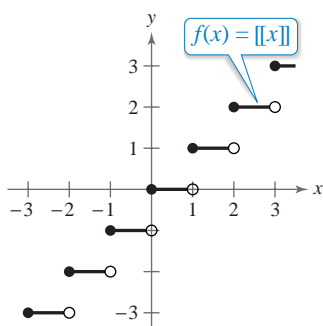
Range: $[0, \infty)$

Intercept: $(0, 0)$

Increasing on $(0, \infty)$

Greatest Integer Function (p. 34)

$$f(x) = \llbracket x \rrbracket$$



Domain: $(-\infty, \infty)$

Range: the set of integers

x-intercepts: in the interval $[0, 1)$

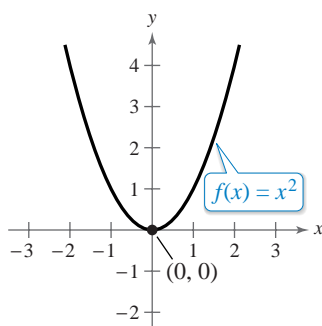
y-intercept: $(0, 0)$

Constant between each pair of consecutive integers

Jumps vertically one unit at each integer value

Quadratic Function (p. 92)

$$f(x) = ax^2$$



Domain: $(-\infty, \infty)$

Range: $[0, \infty)$

Intercept: $(0, 0)$

Decreasing on $(-\infty, 0)$

Increasing on $(0, \infty)$

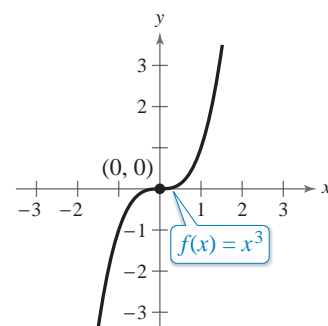
Even function

Axis of symmetry: $x = 0$

Relative minimum or vertex: $(0, 0)$

Cubic Function (p. 101)

$$f(x) = x^3$$



Domain: $(-\infty, \infty)$

Range: $(-\infty, \infty)$

Intercept: $(0, 0)$

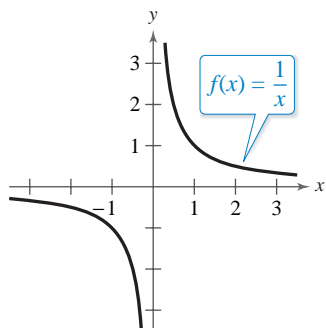
Increasing on $(-\infty, \infty)$

Odd function

Origin symmetry

Rational Function (p. 152)

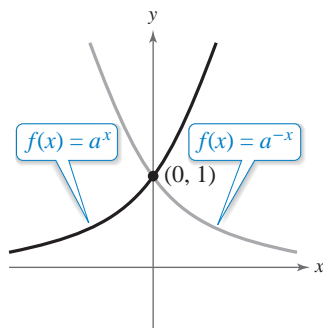
$$f(x) = \frac{1}{x}$$



Domain: $(-\infty, 0) \cup (0, \infty)$
 Range: $(-\infty, 0) \cup (0, \infty)$
 No intercepts
 Decreasing on $(-\infty, 0)$ and $(0, \infty)$
 Odd function
 Origin symmetry
 Vertical asymptote: y -axis
 Horizontal asymptote: x -axis

Exponential Function (p. 182)

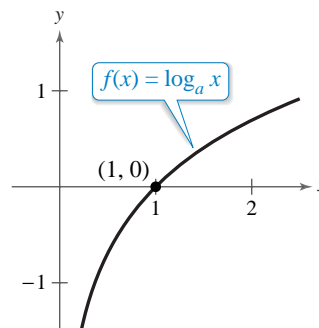
$$f(x) = a^x, \quad a > 0, \quad a \neq 1$$



Domain: $(-\infty, \infty)$
 Range: $(0, \infty)$
 Intercept: $(0, 1)$
 Increasing on $(-\infty, \infty)$
 for $f(x) = a^x$
 Decreasing on $(-\infty, \infty)$
 for $f(x) = a^{-x}$
 x -axis is a horizontal asymptote
 Continuous

Logarithmic Function (p. 195)

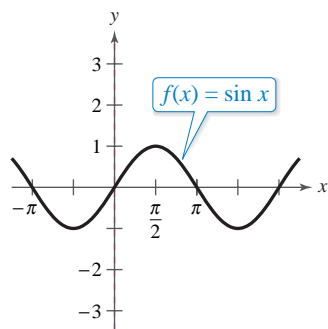
$$f(x) = \log_a x, \quad a > 0, \quad a \neq 1$$



Domain: $(0, \infty)$
 Range: $(-\infty, \infty)$
 Intercept: $(1, 0)$
 Increasing on $(0, \infty)$
 y -axis is a vertical asymptote
 Continuous
 Reflection of graph of $f(x) = a^x$
 in the line $y = x$

Sine Function (p. 293)

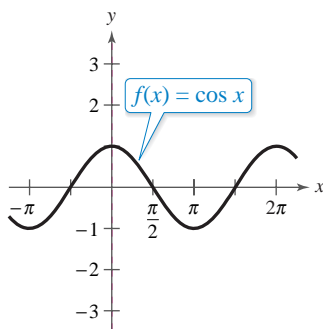
$$f(x) = \sin x$$



Domain: $(-\infty, \infty)$
 Range: $[-1, 1]$
 Period: 2π
 x -intercepts: $(n\pi, 0)$
 y -intercept: $(0, 0)$
 Odd function
 Origin symmetry

Cosine Function (p. 293)

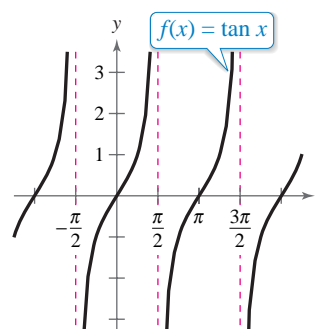
$$f(x) = \cos x$$



Domain: $(-\infty, \infty)$
 Range: $[-1, 1]$
 Period: 2π
 x -intercepts: $\left(\frac{\pi}{2} + n\pi, 0\right)$
 y -intercept: $(0, 1)$
 Even function
 y -axis symmetry

Tangent Function (p. 304)

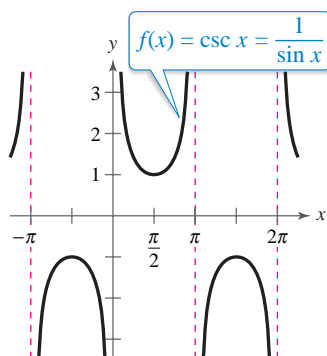
$$f(x) = \tan x$$



Domain: $x \neq \frac{\pi}{2} + n\pi$
 Range: $(-\infty, \infty)$
 Period: π
 x -intercepts: $(n\pi, 0)$
 y -intercept: $(0, 0)$
 Vertical asymptotes: $x = \frac{\pi}{2} + n\pi$
 Odd function
 Origin symmetry

Cosecant Function (p. 307)

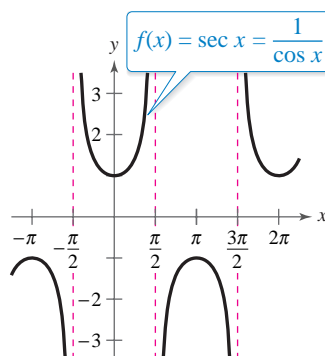
$$f(x) = \csc x$$



Domain: $x \neq n\pi$
 Range: $(-\infty, -1] \cup [1, \infty)$
 Period: 2π
 No intercepts
 Vertical asymptotes: $x = n\pi$
 Odd function
 Origin symmetry

Secant Function (p. 307)

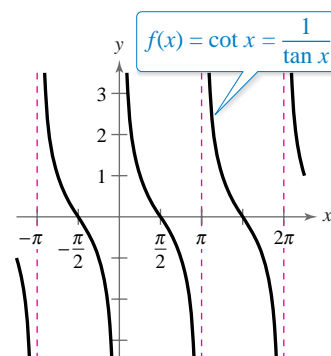
$$f(x) = \sec x$$



Domain: $x \neq \frac{\pi}{2} + n\pi$
 Range: $(-\infty, -1] \cup [1, \infty)$
 Period: 2π
 y-intercept: $(0, 1)$
 Vertical asymptotes:
 $x = \frac{\pi}{2} + n\pi$
 Even function
 y-axis symmetry

Cotangent Function (p. 306)

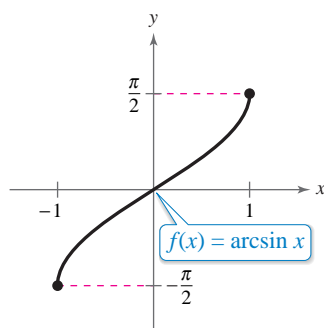
$$f(x) = \cot x$$



Domain: $x \neq n\pi$
 Range: $(-\infty, \infty)$
 Period: π
 x-intercepts: $\left(\frac{\pi}{2} + n\pi, 0\right)$
 Vertical asymptotes: $x = n\pi$
 Odd function
 Origin symmetry

Inverse Sine Function (p. 319)

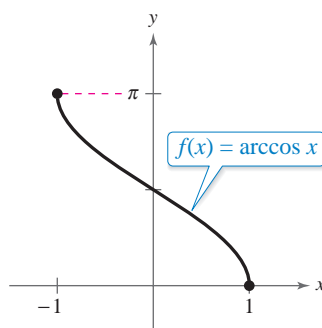
$$f(x) = \arcsin x$$



Domain: $[-1, 1]$
 Range: $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$
 Intercept: $(0, 0)$
 Odd function
 Origin symmetry

Inverse Cosine Function (p. 319)

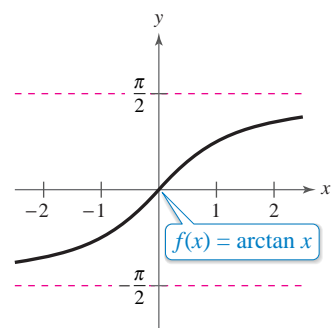
$$f(x) = \arccos x$$



Domain: $[-1, 1]$
 Range: $[0, \pi]$
 y-intercept: $\left(0, \frac{\pi}{2}\right)$

Inverse Tangent Function (p. 319)

$$f(x) = \arctan x$$



Domain: $(-\infty, \infty)$
 Range: $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$
 Intercept: $(0, 0)$
 Horizontal asymptotes: $y = \pm\frac{\pi}{2}$
 Odd function
 Origin symmetry