

* Hierarchical Clustering *

- ↳ Unsupervised ML Algo, group unlabelled dataset into a cluster via Hierarchical Cluster Analysis.
- ↳ Develop tree-structured hierarchy of clusters, tree-shaped structure via dendrogram.

↳ Num. of clusters not predefined.

↳ 2 approaches:-

① Agglomerative: Bottom-up approach.

↳ All data points consider individual clusters & iteratively merge until 1 cluster left.

② Divisive: Top-down approach.

- Reverse of Agglomerative.

- Start with consider 1 cluster and iteratively divide till reach individual clusters.

↳ Working of Hierarchical Clustering:-

① start, consider every data point separate individual clusters.

② Identify 2 closest together clusters.

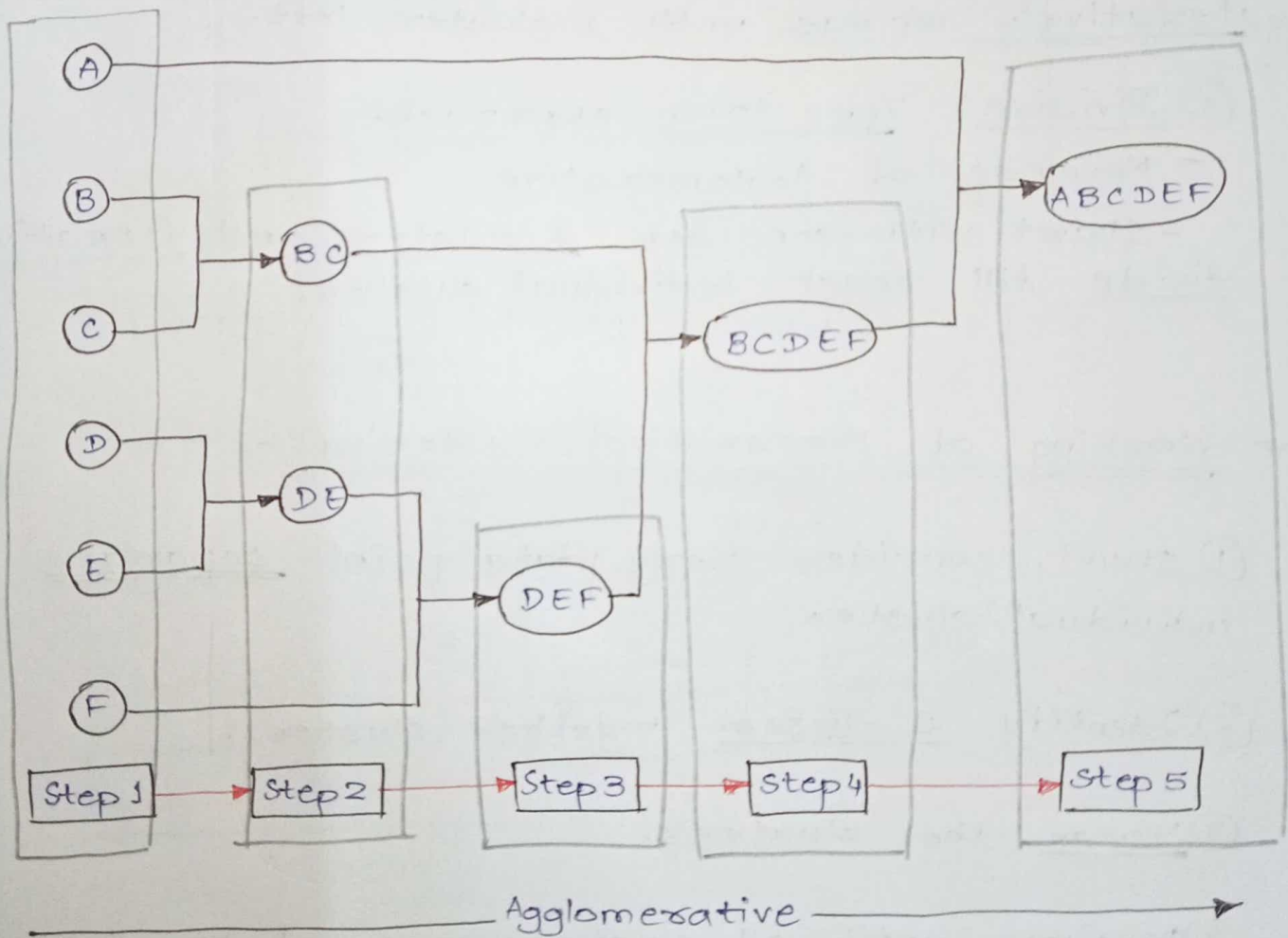
③ Merge the clusters.

④ continue until all clusters merged together.

1) Agglomerative clustering :- Bottom-up method.

- ① Consider every data point individual clusters.
- ② Calculate proximity matrix (similarity of clusters with all other clusters).
- ③ Merge highly similar / closest clusters.
- ④ Recalculate proximity matrix of each clusters.
- ⑤ Repeat steps 3 & 4, until only 1 cluster remain.

• Example:



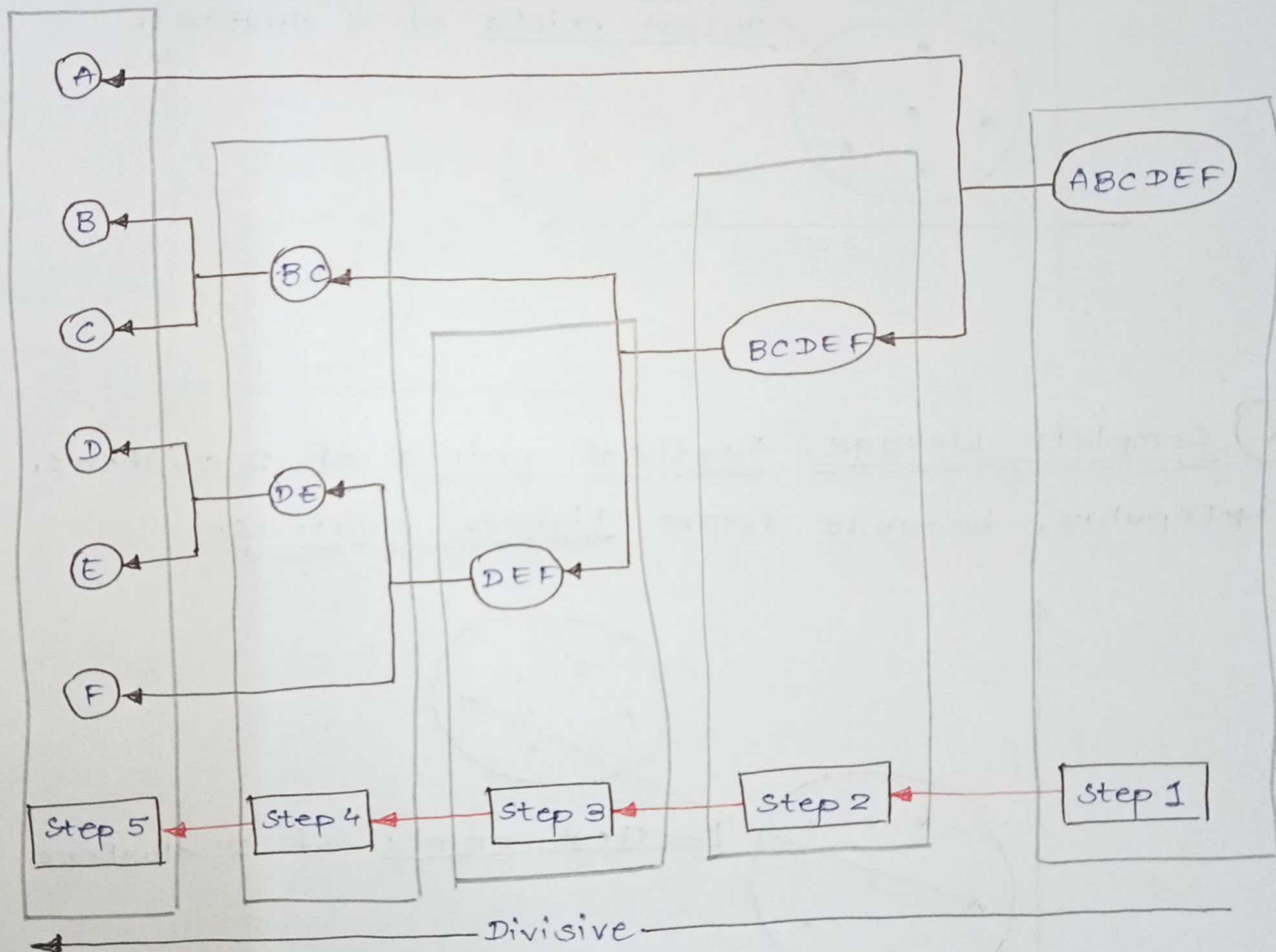
2) Divisive Clustering! - Top-down method.

↳ Consider all data points a single cluster.

↳ In each iteration, separate data points from clusters which aren't comparable.

↳ At the end get N-clusters.

• Example -

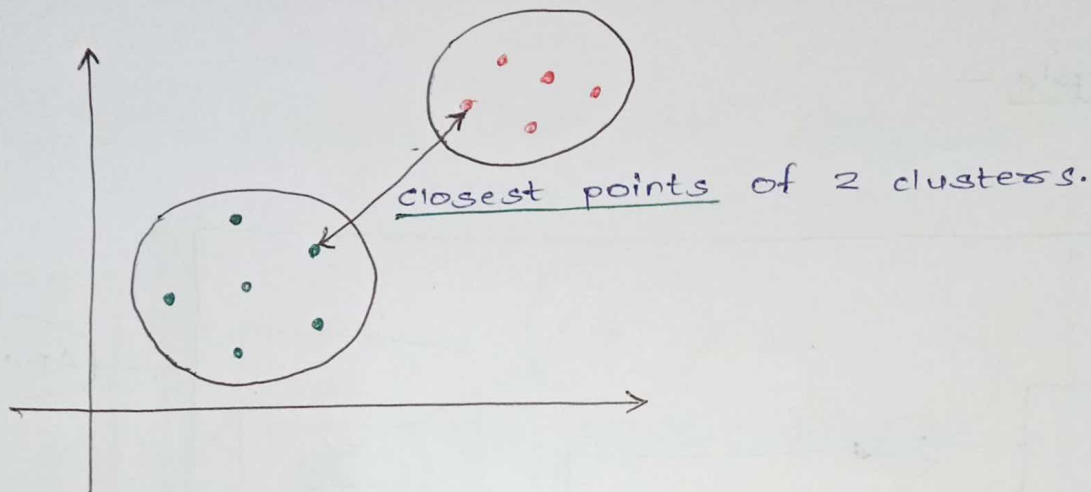


• Measure Dist. betⁿ 2 clusters:-

↳ Find closest distance betⁿ 2 clusters.

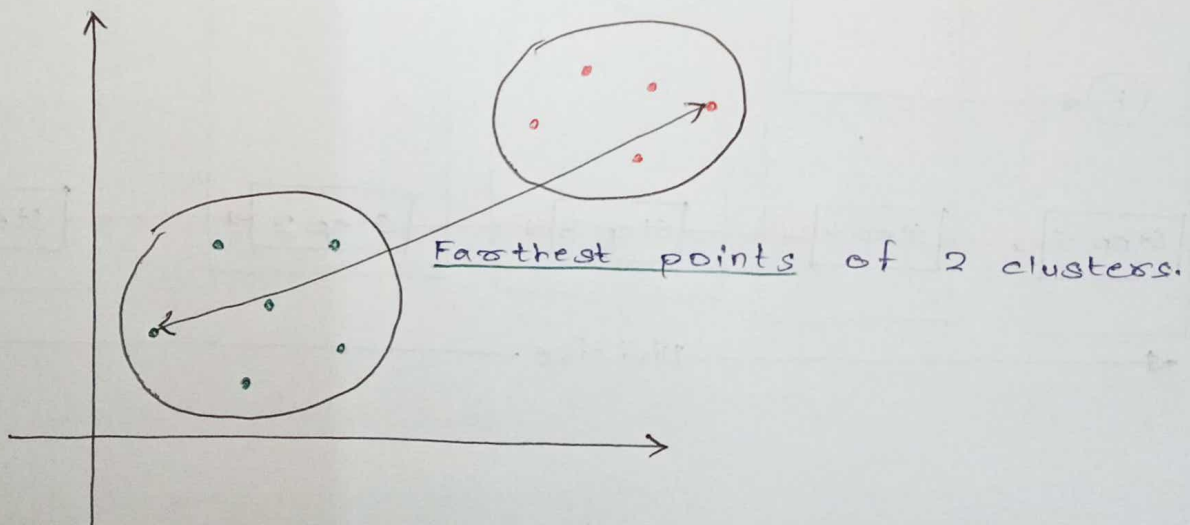
↳ Different methods ca Linkage Methods.

① Single Linkage: shortest distance between the closest points.



② Complete Linkage: Farthest points of 2 clusters.

↳ Popular, because form tighter clusters.

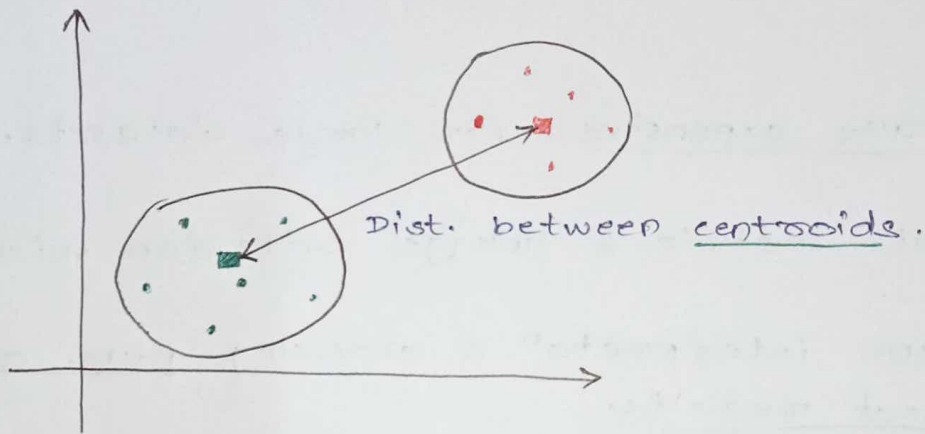


③ Average Linkage: - calculate average distances.

↳ Add up dist. betⁿ each pairs of datasets & then divide by total num. of data points.

$$\left(\begin{array}{c} \text{Average} \\ \text{Dist} \end{array} \right) = \frac{\sum \text{dist. bet}^n \text{ each data pairs}}{\text{Num. of data points}}$$

④ Centroid Linkage: Dist. betⁿ centroids.



• Advantages:

↳ Not required to predefine num. of clusters.

↳ Hierarchical cluster representation useful for multiple level data points.

↳ Work well for different dist. metrics & linkage criterion.

• Limitations:

↳ Computationally expensive for large datasets.

↳ choose dist. metric & linkage criterion wisely.

↳ Dendrogram interpretation & choosing num. of clusters affect results.