

# The Life Cycle Dynamics of Wealth Mobility

Richard Audoly  
FRBNY

Rory M<sup>c</sup>Gee  
UWO

Sergio Ocampo  
UWO

Gonzalo Paz-Pardo  
ECB

September, 2023

**Disclaimer:** The views below are those of the authors and do not necessarily reflect the position of the Federal Reserve Bank of New York, the Federal Reserve System, the European Central Bank or the Eurosystem.

## What we learn from measuring wealth mobility:

- Mobility is a key measure for contextualizing inequality (research + public debate)
  - Derive results for whole population + life cycle dynamics

# What we learn from measuring wealth mobility:

- Mobility is a key measure for contextualizing inequality (research + public debate)
  - Derive results for whole population + life cycle dynamics
- How do individuals move through the wealth distribution as they age?
  - Implications of relative changes for wealth levels, asset composition, etc

# What we learn from measuring wealth mobility:

- Mobility is a key measure for contextualizing inequality (research + public debate)
  - Derive results for whole population + life cycle dynamics
- How do individuals move through the wealth distribution as they age?
  - Implications of relative changes for wealth levels, asset composition, etc
- What is behind patterns of wealth mobility? Inter-generational links? Human Capital?
  - Who makes it to the top? the bottom? How long do they stay there?
  - Link *ex-post* histories to differences in background (parents/location) and education

# What we learn from measuring wealth mobility:

- Mobility is a key measure for contextualizing inequality (research + public debate)
  - Derive results for whole population + life cycle dynamics
- How do individuals move through the wealth distribution as they age?
  - Implications of relative changes for wealth levels, asset composition, etc
- What is behind patterns of wealth mobility? Inter-generational links? Human Capital?
  - Who makes it to the top? the bottom? How long do they stay there?
  - Link *ex-post* histories to differences in background (parents/location) and education

**Today:** Document patterns of wealth mobility across life cycle

Made possible by **Norwegian administrative data** on wealth 1993–2017

# Three Main Exercises: Focus on individuals' rank in wealth distribution

1. Document properties of distribution of rank changes
  - Non-linear and non-normal dynamics that change by age

# Three Main Exercises: Focus on individuals' rank in wealth distribution

## 1. Document properties of distribution of rank changes

- Non-linear and non-normal dynamics that change by age

## 2. Focus on “*typical*” trajectories by clustering individuals

- Implications of rank mobility for wealth levels
- Relationship to housing, civil status, portfolio composition, etc.
- **Zoom-in:** *sub-clusters* show heterogeneity in paths for groups starting in different sections of the distribution

# Three Main Exercises: Focus on individuals' rank in wealth distribution

1. Document properties of distribution of rank changes
  - Non-linear and non-normal dynamics that change by age
2. Focus on “*typical*” trajectories by **clustering individuals**
  - Implications of rank mobility for wealth levels
  - Relationship to housing, civil status, portfolio composition, etc.
  - **Zoom-in:** *sub-clusters* show heterogeneity in paths for groups starting in different sections of the distribution
3. Predict trajectories with individual circumstances
  - Determinants of paths through the distribution: prev. generation, education, etc.



# Contributions

1. New evidence on wealth mobility and wealth accumulation: Full life cycle trajectories
  - Add to results for the super wealthy (Ozkan, Hubmer, Salgado, Halvorsen) and the role of individual factors like inheritances (Black, Devereux, Landaud, Salvanes).

# Contributions

1. New evidence on wealth mobility and wealth accumulation: Full life cycle trajectories
  - Add to results for the super wealthy (Ozkan, Hubmer, Salgado, Halvorsen) and the role of individual factors like inheritances (Black, Devereux, Landaud, Salvanes).
2. New facts documenting the distribution of changes in wealth ranks
  - Extensive literature on income (Guvenen, Ozkan, Karahan, Song; Guvenen, Pistaferri, Violante; Arellano, Blundell, Bonhomme; De Nardi, Fella, Paz-Pardo)

# Contributions

1. New evidence on wealth mobility and wealth accumulation: Full life cycle trajectories
  - Add to results for the super wealthy (Ozkan, Hubmer, Salgado, Halvorsen) and the role of individual factors like inheritances (Black, Devereux, Landaud, Salvanes).
2. New facts documenting the distribution of changes in wealth ranks
  - Extensive literature on income (Guvenen, Ozkan, Karahan, Song; Guvenen, Pistaferri, Violante; Arellano, Blundell, Bonhomme; De Nardi, Fella, Paz-Pardo)
3. Intergenerational links to full life cycle wealth dynamics
  - Complements “snapshot” links in income (Solon; Aaronson, Mazumder; Chetty, Hendren, Kline, Saez, Turner; Chetty, Grusky, Hendren, Hell, Manduca, Narang) & **wealth** (Charles, Hurst; Boserup, Kopczuk, Kreiner; Fagereng, Guiso, Malacrino, Pistaferri; Fagereng, Mogstad, Rønning )

# Contributions

1. New evidence on wealth mobility and wealth accumulation: Full life cycle trajectories
  - Add to results for the super wealthy (Ozkan, Hubmer, Salgado, Halvorsen) and the role of individual factors like inheritances (Black, Devereux, Landaud, Salvanes).
2. New facts documenting the distribution of changes in wealth ranks
  - Extensive literature on income (Guvenen, Ozkan, Karahan, Song; Guvenen, Pistaferri, Violante; Arellano, Blundell, Bonhomme; De Nardi, Fella, Paz-Pardo)
3. Intergenerational links to full life cycle wealth dynamics
  - Complements “snapshot” links in income (Solon; Aaronson, Mazumder; Chetty, Hendren, Kline, Saez, Turner; Chetty, Grusky, Hendren, Hell, Manduca, Narang) & **wealth** (Charles, Hurst; Boserup, Kopczuk, Kreiner; Fagereng, Guiso, Malacrino, Pistaferri; Fagereng, Mogstad, Rønning )
4. Dimension reduction methods in economics & applications to labour markets
  - K-Means (Bonhome, Lamadon, Manresa; Gregory, Menzio, Wiczer), Sequence Analysis (Humphries), Hidden Markov (Ahn, Hobijn, Şahin), Finite Mixture

# Norwegian Wealth Data

## Data: Norwegian Tax Registry 1993 – 2017 [▶ Context](#)

- No top-coding + Limited misreporting or measurement error (third-party reporting)
- We link to administrative records (Education, Civil Status, Income)
- We adjust the tax value to reflect market values (Fagereng, Holm, Torstensen, 2023, 2023)
- Focus on wealth with liquidity (e.g., include private pensions but not public pensions)

# Data: Norwegian Tax Registry 1993 – 2017 [▶ Context](#)

- No top-coding + Limited misreporting or measurement error (third-party reporting)
- We link to administrative records (Education, Civil Status, Income)
- We adjust the tax value to reflect market values (Fagereng, Holm, Torstensen, 2023, 2023)
- Focus on wealth with liquidity (e.g., include private pensions but not public pensions)

## **Sample selection:** Norwegian residents 1993–2017, born 1905–1990

- Drop emigrants and immigrants after 25 or 2011
- Focus on birth cohort born between 1960 and 1965 (first observed in early 30s)
  - 292,222 individuals in this sample (217,383 after balancing)

# Ranks and Histories

- Compute within cohort ranks as

$$y_{i,t} = 100 \times F_w(w_{i,t}|t, i \in BC(i))$$

- Computed separately for each year and each cohort (uses unbalanced panel)



# Ranks and Histories

- Compute within cohort ranks as

$$y_{i,t} = 100 \times F_w(w_{i,t}|t, i \in BC(i))$$

- Computed separately for each year and each cohort (uses unbalanced panel)
- Histories of ranks (trajectories)

$$\mathbf{Y}_i = (y_{i,1993}, y_{i,1994}, \dots, y_{i,2016}, y_{i,2017}) \in [0, 100]^{25}$$

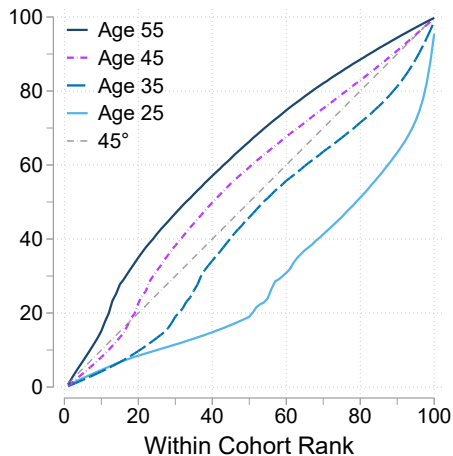
- Vector of rank outcomes (for balanced panel)

We are interested in the distribution of the vectors  $\mathbf{Y}_i$

- Significant changes in wealth levels as the cohort ages
- Significant changes in wealth levels across ranks

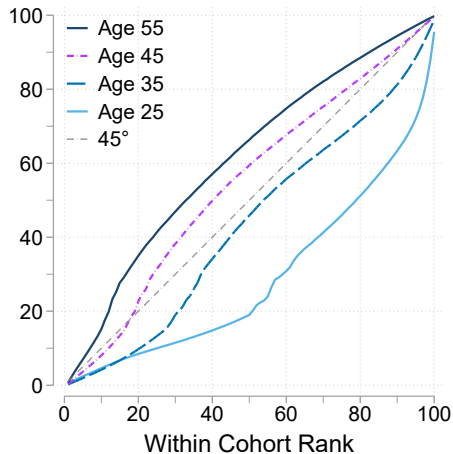
# Birth Cohort Ranks vs Population Ranks vs Wealth Levels

## BC Ranks vs Pop Ranks

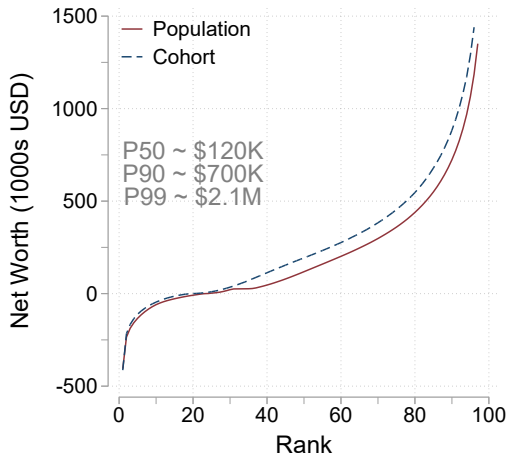


# Birth Cohort Ranks vs Population Ranks vs Wealth Levels

## BC Ranks vs Pop Ranks



## Net Worth CDF (2014)



- US: p90~\$620K, p99~\$3.5M (SZZ, 2022)

# Patterns of Mobility

# How much does people's wealth rank $y_{i,t}$ change over time?

Distribution of future ranks conditional on current rank

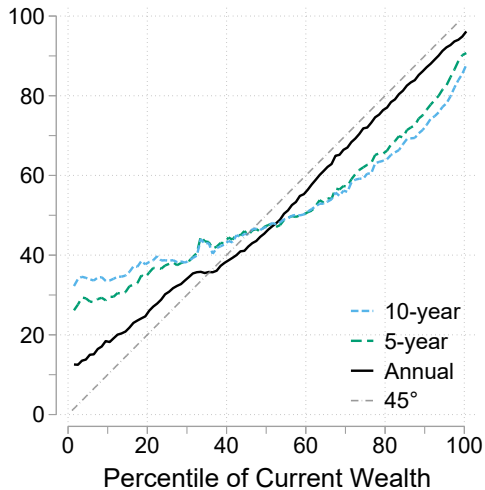
- Conditional mean  $E[y_{i,t+h}|y_{i,t}]$  (also higher order moments)
- Conditional quantiles  $Q_{y_{i,t+h}|y_{i,t}}(\tau)$  for  $\tau \in \{0.1, 0.25, 0.75, 0.9\}$

# How Non-Linear is Wealth Mobility?

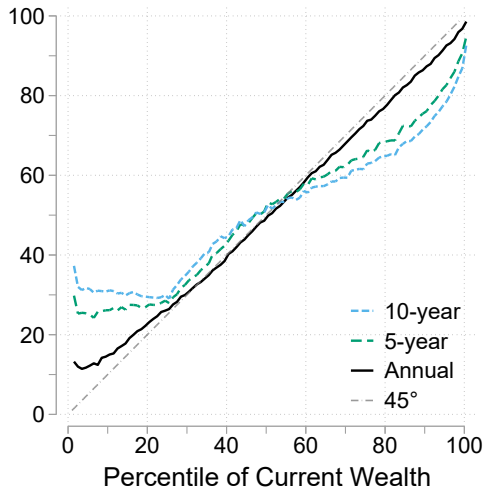
► Age 31

► Income

## Age 35 – Cond. Mean



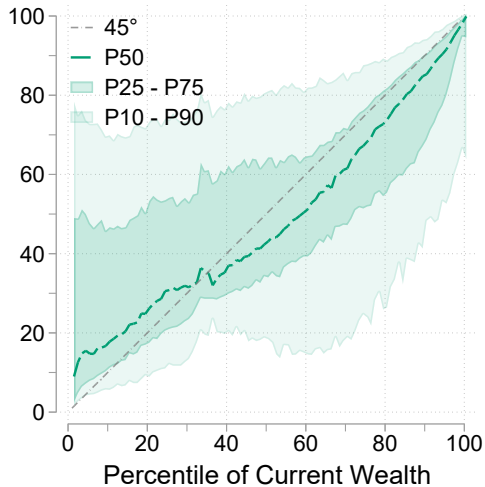
## Age 45 – Cond. Mean



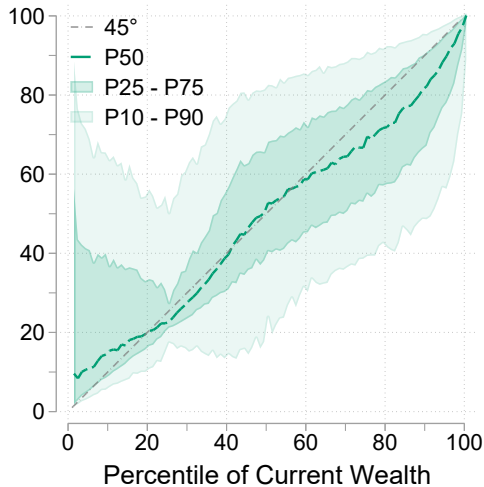
# The Distribution of Rank Changes (5-year)

1y Chg 10y Chg

Age 35



Age 45



At the top few fall, but cushioned Middle class rarely climb, but some fall

# Distribution of rank changes is non-linear and age-dependent!

- Mean reversion in ranks weakens at the top
- Dispersion ↓ with age (consistent w evidence on income) and initial rank
  - Median change is close to no change at all ages(!)

▶ std. dev.

▶ skew.

▶ kurt.



# Distribution of rank changes is non-linear and age-dependent!

- Mean reversion in ranks weakens at the top
- Dispersion ↓ with age (consistent w evidence on income) and initial rank
  - Median change is close to no change at all ages(!) ▶ std. dev. ▶ skew. ▶ kurt.
- Distribution of 5y and 10y changes are similar (despite ↑ in dispersion from 1y to 5y)
  - Variability in 1y changes is misleading about long-run variability
  - 5y, 10y persistence is much higher than implied by 1y persistence!

# Distribution of rank changes is non-linear and age-dependent!

- Mean reversion in ranks weakens at the top
- Dispersion ↓ with age (consistent w evidence on income) and initial rank
  - Median change is close to no change at all ages(!)
- Distribution of 5y and 10y changes are similar (despite ↑ in dispersion from 1y to 5y)
  - Variability in 1y changes is misleading about long-run variability
  - 5y, 10y persistence is much higher than implied by 1y persistence!

▶ std. dev.

▶ skew.

▶ kurt.

Comparing ranks at given ages gives an incomplete view of wealth mobility

**Next Step:** Analyze distribution of complete trajectories through the wealth distribution

# Clustering Wealth Histories

# Grouping Individuals Into Typical Histories

**Goal:** Identify patterns in (ex-post) life cycle paths without restricting to a single statistic

- Uncover rising, falling, and stable trajectories

# Grouping Individuals Into Typical Histories

**Goal:** Identify patterns in (ex-post) life cycle paths without restricting to a single statistic

- Uncover rising, falling, and stable trajectories

**Method:** Agglomerative Hierarchical Clustering to group rank histories

# Grouping Individuals Into Typical Histories

**Goal:** Identify patterns in (ex-post) life cycle paths without restricting to a single statistic

- Uncover rising, falling, and stable trajectories

**Method:** Agglomerative Hierarchical Clustering to group rank histories

- Start with  $G = N$  groups (one for each individual)
- Recursively merge groups by selecting *similar* pairs:  $\operatorname{argmin}_{g, g' \in G, g \neq g'} d(g, g')$ .

# Grouping Individuals Into Typical Histories

**Goal:** Identify patterns in (ex-post) life cycle paths without restricting to a single statistic

- Uncover rising, falling, and stable trajectories

**Method:** Agglomerative Hierarchical Clustering to group rank histories

- Start with  $G = N$  groups (one for each individual)
- Recursively merge groups by selecting *similar* pairs:  $\operatorname{argmin}_{g, g' \in G, g \neq g'} d(g, g')$ .

**Result:** Hierarchy of partitions ranging from  $G = N$  to  $G = 1$ .

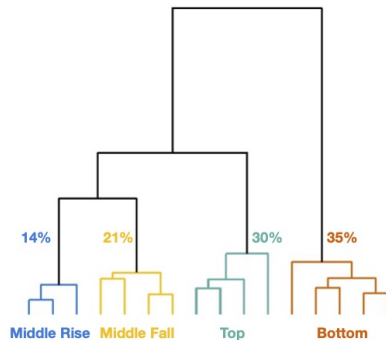
- Similar results for alternative clustering (cum. change, log-assets, “Lorenz” position)

# Two Levels of Clustering

## 1. Focus on 4 major clusters (branches)

- Explain majority of variation in rank histories ( $R^2=0.52$ )

Clustering Tree

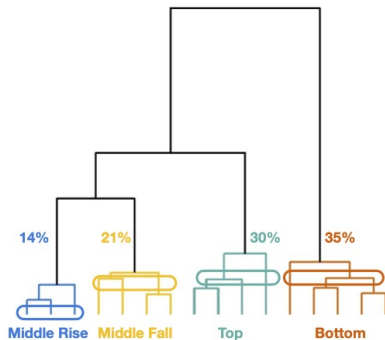




# Two Levels of Clustering

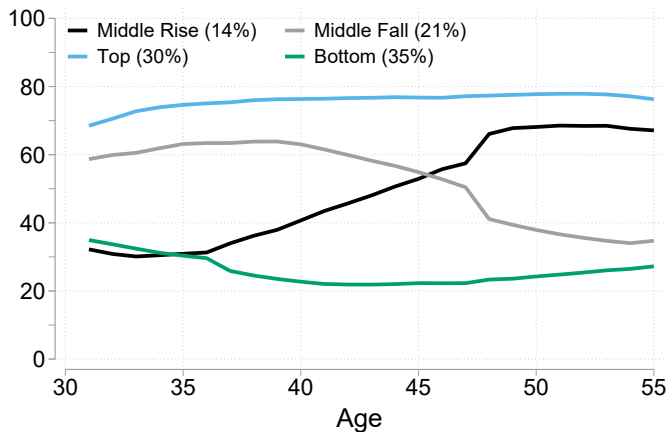
1. Focus on 4 major clusters (branches)
  - Explain majority of variation in rank histories ( $R^2=0.52$ )
2. Zoom into each major cluster
  - Pick 3 main sub-clusters
  - Reveal heterogeneity in major trajectories
  - 12 clusters explain 20% additional variation ( $R^2=0.63$ ; 16 CI,  $R^2=0.66$ )

Clustering Tree



# Typical Rank Histories: Segmented Mobility

## Cohort Ranks



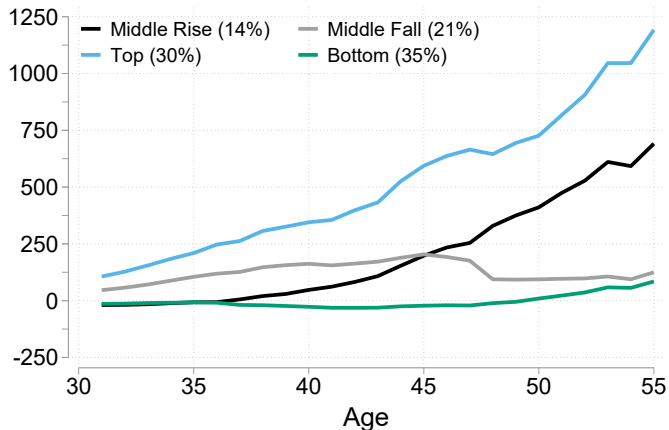
4 Main clusters show patterns of **segmented mobility**

- Individuals move within segments of the distribution
- The mean trajectory of a group hides rank swaps within
- Segments overlap:  
Top 40% // Bottom 40% //  
Middle 80%

**Next:** Levels + Heterogeneity

# Wealth Histories Across Segments of the Distribution

## Net Worth (\$1000s)



Differences in ranks imply significant wealth differences:

- **Risers:** start with no wealth + grow like top group
- **Fallers:** ahead in 30s + low growth + great recession
- **Top:** Maintaining rank means rapid growth
- **Bottom:** Close to no wealth + growth in 50s (housing)

# What Else Happens Along These Paths?

- **Housing:** Increasing trends except for *fallers*
  - Fallers home-ownership: 40%→70%→65%
  - Risers home-ownership: 20%→85% (as high as top group)
- **Civil Status:** Similar marriage/cohabitation rates by cluster
  - Bottom group have lowest marriage rates, top group the highest
- **Portfolio Composition + Income:** Soon!

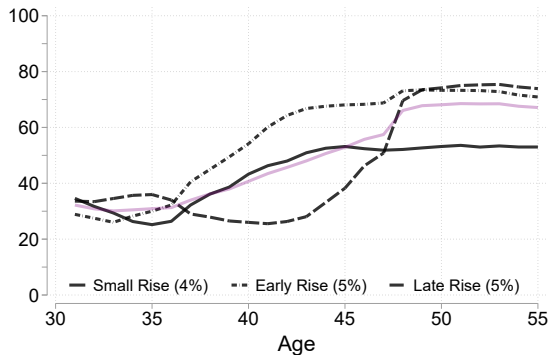
[▶ details](#)[▶ details](#)

**Next Step:** Zoom into heterogeneity within group

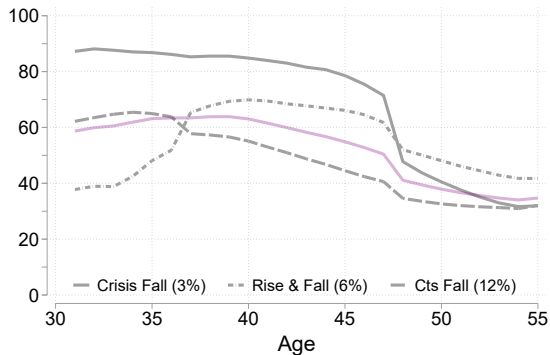
# Heterogeneity in Trajectories: Levels vs Timing

► Wealth Levels

## Middle Risers



## Middle Fallers

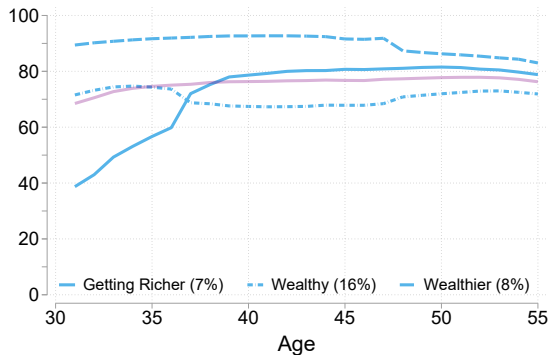


- Risers differ mainly in timing of changes (Rise from rank 20 to 70, similar initial conditions)
- Fallers differ in initial conditions and timing of changes

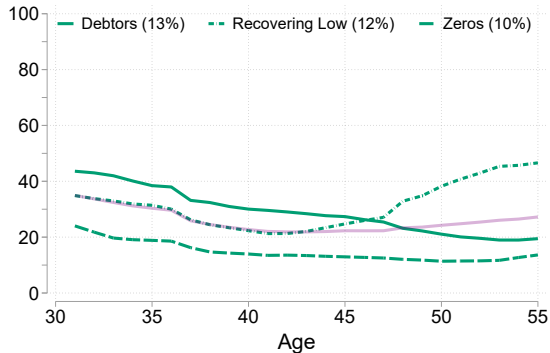
# Heterogeneity in Trajectories: Levels vs Timing

► Wealth Levels

## Top of the Distribution



## Bottom of the Distribution

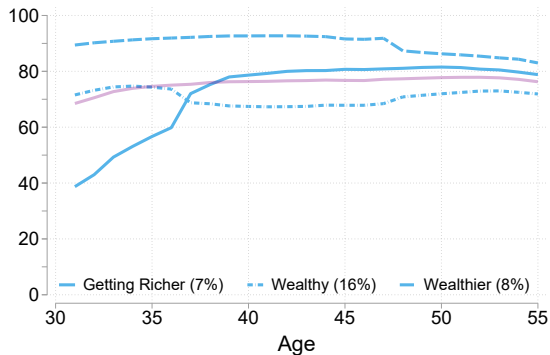


- Risers differ mainly in timing of changes (Rise from rank 20 to 70, similar initial conditions)
- Fallers differ in initial conditions and timing of changes
- Top and bottom groups differ mainly in ave. levels (with a rising sub-group in each)

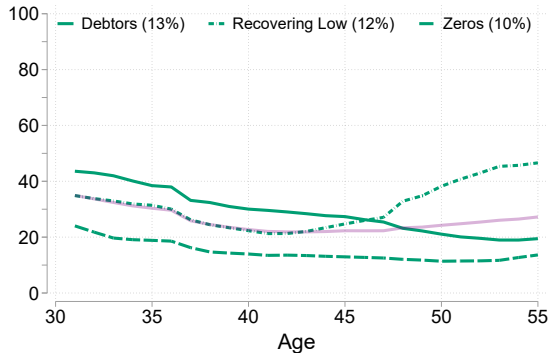
# Heterogeneity in Trajectories: Levels vs Timing

► Wealth Levels

## Top of the Distribution



## Bottom of the Distribution



- Risers differ mainly in timing of changes (Rise from rank 20 to 70, similar initial conditions)
- Fallers differ in initial conditions and timing of changes
- Top and bottom groups differ mainly in ave. levels (with a rising sub-group in each)

# Towards Determinants of Trajectories



# Hereditary Advantage vs Human Capital

**Goal:** Understand role of different circumstances/characteristics in determining trajectories

# Hereditary Advantage vs Human Capital

**Goal:** Understand role of different circumstances/characteristics in determining trajectories

$$Pr(g = j) = F\left(\beta_0^j + \alpha_{q(i)}^j + \delta_{educ(i)}^j + \gamma_{subj(i)}^j + \mu_{male(i)}^j + \lambda_{bcounty(i)}^j\right)$$

- $\alpha_{q(i)}^j$ : Fixed effect for 1993 parental wealth (cohort rank by ventile)

# Hereditary Advantage vs Human Capital

**Goal:** Understand role of different circumstances/characteristics in determining trajectories

$$Pr(g = j) = F\left(\beta_0^j + \alpha_{q(i)}^j + \delta_{educ(i)}^j + \gamma_{subj(i)}^j + \mu_{male(i)}^j + \lambda_{bcounty(i)}^j\right)$$

- $\alpha_{q(i)}^j$ : Fixed effect for 1993 parental wealth (cohort rank by ventile)
- $\delta_{educ(i)}^j, \gamma_{subj(i)}^j$ : Fixed effect for education level and subject (only for higher ed.)

# Hereditary Advantage vs Human Capital

**Goal:** Understand role of different circumstances/characteristics in determining trajectories

$$Pr(g = j) = F\left(\beta_0^j + \alpha_{q(i)}^j + \delta_{educ(i)}^j + \gamma_{subj(i)}^j + \mu_{male(i)}^j + \lambda_{bcounty(i)}^j\right)$$

- $\alpha_{q(i)}^j$ : Fixed effect for 1993 parental wealth (cohort rank by ventile)
- $\delta_{educ(i)}^j, \gamma_{subj(i)}^j$ : Fixed effect for education level and subject (only for higher ed.)
- $\mu_{male(i)}^j$ : Fixed effect for sex
- $\lambda_{bcounty(i)}^j$ : Fixed effect for birth location

► Sex APE

► Location APE

# Hereditary Advantage vs Human Capital

**Goal:** Understand role of different circumstances/characteristics in determining trajectories

$$Pr(g = j) = F\left(\beta_0^j + \alpha_{q(i)}^j + \delta_{educ(i)}^j + \gamma_{subj(i)}^j + \mu_{male(i)}^j + \lambda_{bcounty(i)}^j\right)$$

- $\alpha_{q(i)}^j$ : Fixed effect for 1993 parental wealth (cohort rank by ventile)
- $\delta_{educ(i)}^j, \gamma_{subj(i)}^j$ : Fixed effect for education level and subject (only for higher ed.)
- $\mu_{male(i)}^j$ : Fixed effect for sex ► Sex APE
- $\lambda_{bcounty(i)}^j$ : Fixed effect for birth location ► Location APE

Predictors explain at most 6.4% of cross-group variation (same as rank-rank inter-gen reg)

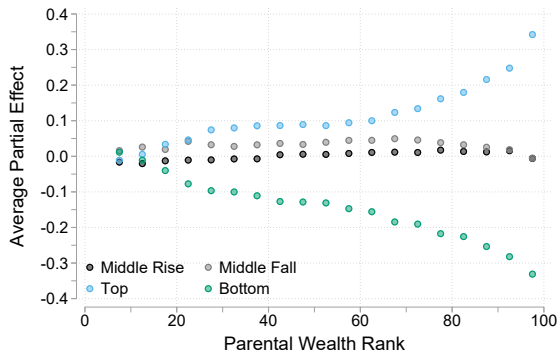
► Results

# The Non-Linear Effect of Parental Wealth and Education

▸ PW CIs

▸ ED CIs

## Parental Wealth

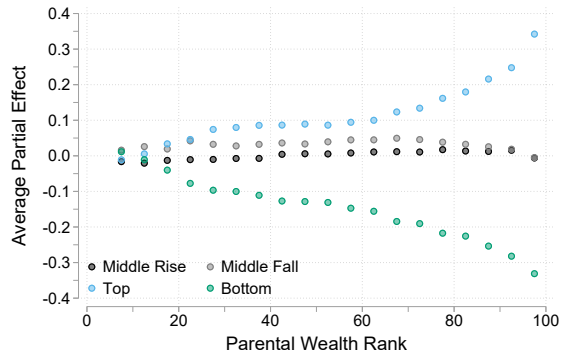


- Parental wealth's explanatory power: High for top/bottom, limited for middle groups

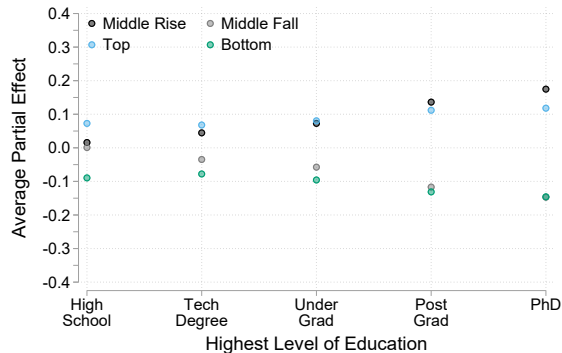
# The Non-Linear Effect of Parental Wealth and Education

► PW CIs ► ED CIs

## Parental Wealth



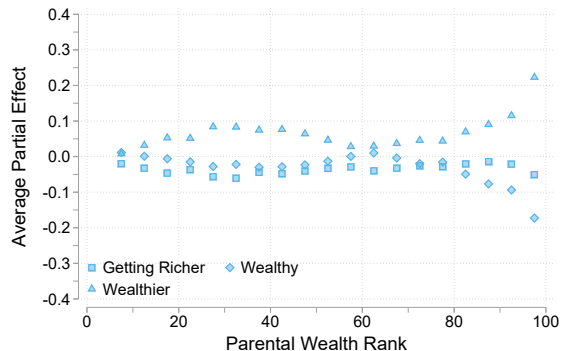
## Education



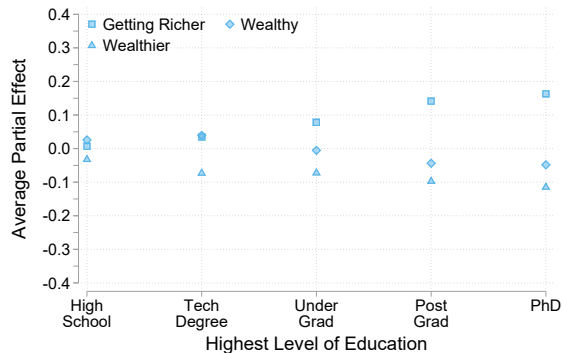
- Parental wealth's explanatory power: High for top/bottom, limited for middle groups
- Education tells risers/fallers apart: Equalizing effect but doesn't overcome initial cond.

# What about heterogeneity within clusters? Top Group ▶ Other CI ▶ PW ▶ ED

## Parental Wealth



## Education



- Even within the top group, movers are hard to predict with parental wealth
- Education does not matter for those born rich but helps those getting to the top



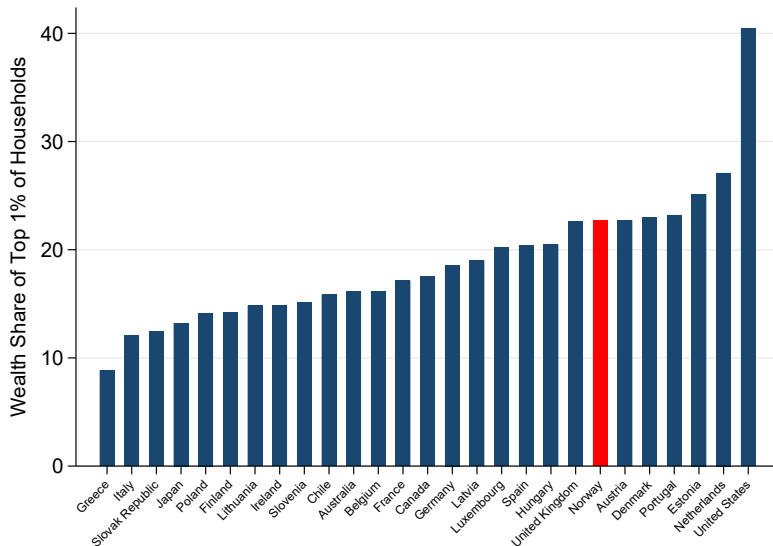
# Conclusions

# Conclusions

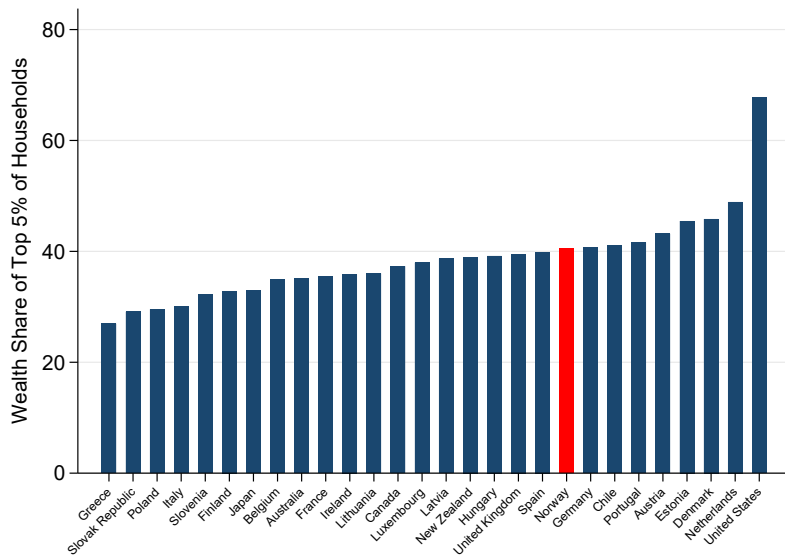
- Document persistence of wealth over the life cycle
- Characterise non-linear persistence and mobility
  - Top of the distribution cushioned against falls
- Uncover typical trajectories of individuals through the wealth distribution
- Intergenerational background an important predictor of **whole** history
  - But limited explanatory power
- Education is key for movements through the wealth distribution

Extra

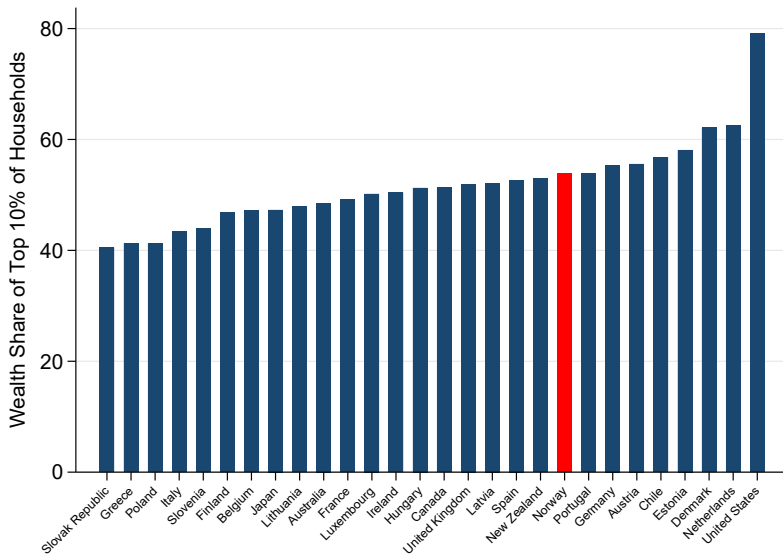
# Norway in Context

[◀ Back](#)

## Norway in Context: Top 5% Share [◀ Back](#)

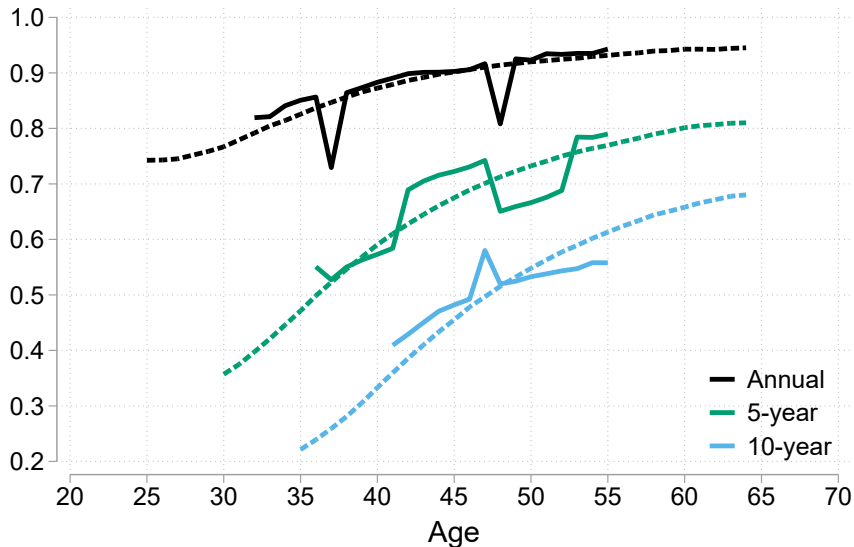


## Norway in Context: Top 10% Share [◀ Back](#)



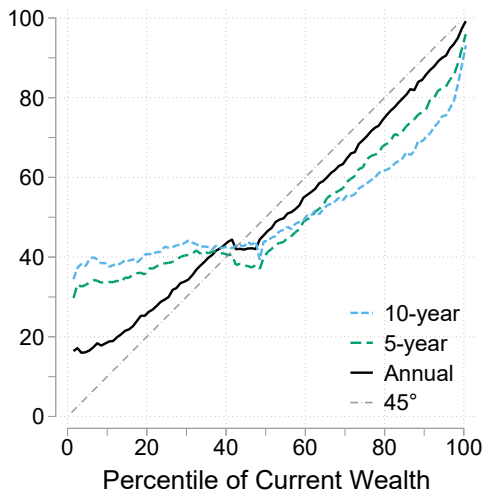
# Persistence in Wealth Rank: Within Cohort ◀

All Cohorts vs 1960-1964 Birth Cohort



# How Non-Linear is Wealth Mobility? [◀ back](#)

Age 31

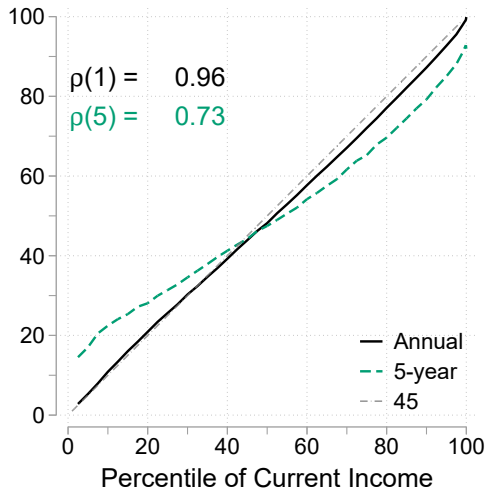




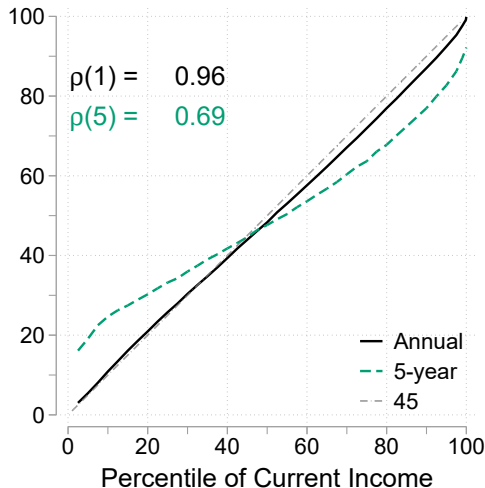
# How Non-Linear is Income Mobility in Norway?

[◀ back](#)[▶ USA](#)

## Age 35-44



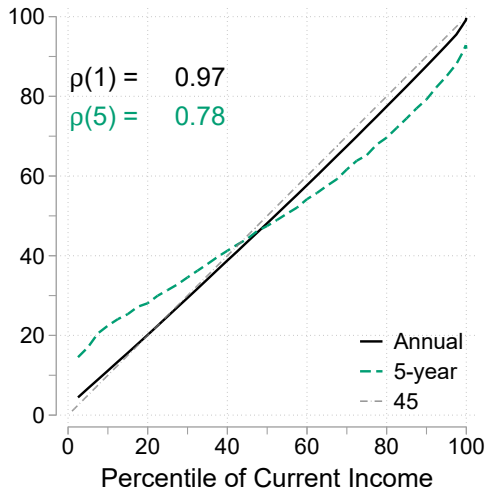
## All



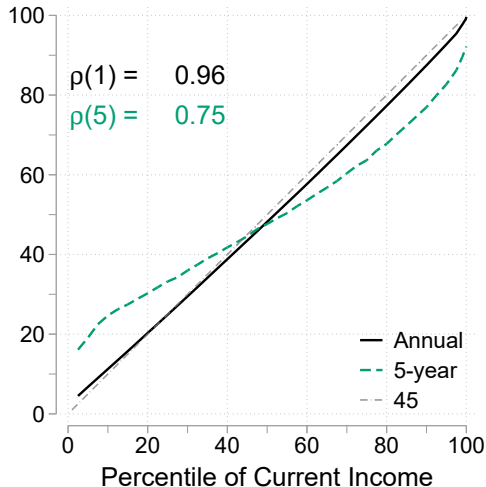
Source: GRID database for 2005

# How Non-Linear is Income Mobility in the U.S.? [◀ back](#)

Age 35-44



All

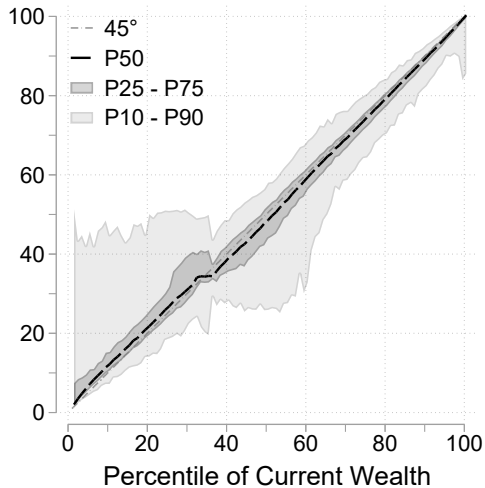


Source: GRID database for 2005

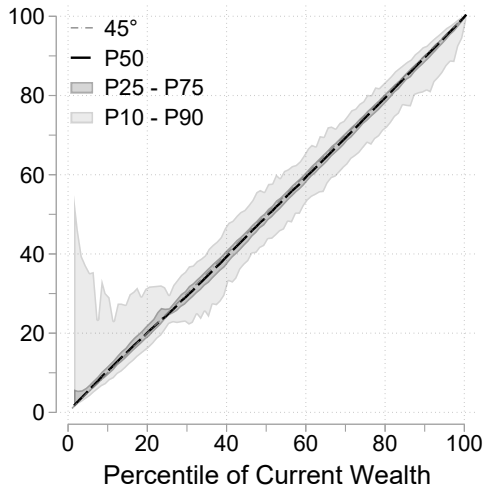
# The Distribution of Rank Changes (1-year)

[◀ back](#)[▶ 10y Chg](#)

## Age 35 – Cond. pct



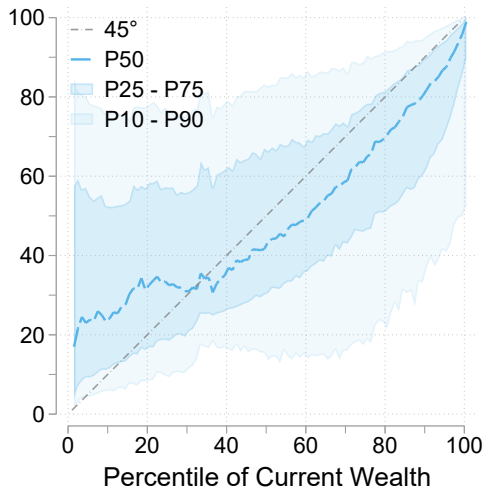
## Age 45 – Cond. pct



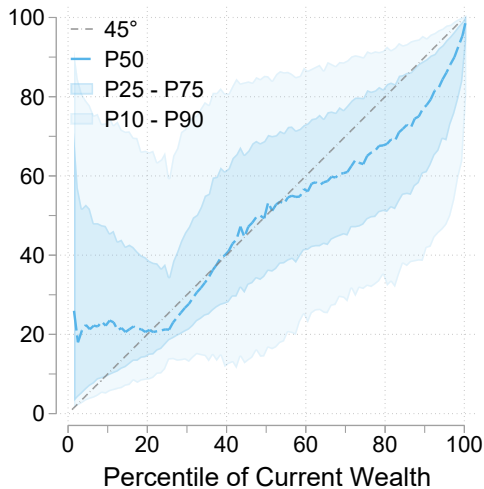
# The Distribution of Rank Changes (10-year)

[◀ back](#)

## Age 35

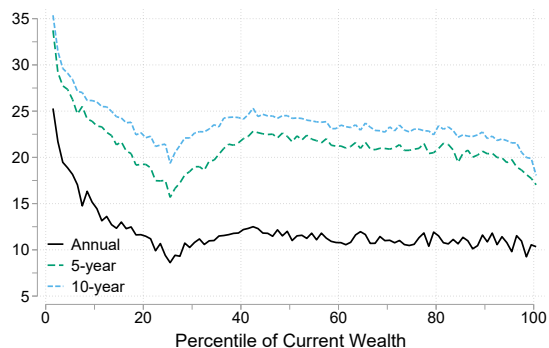
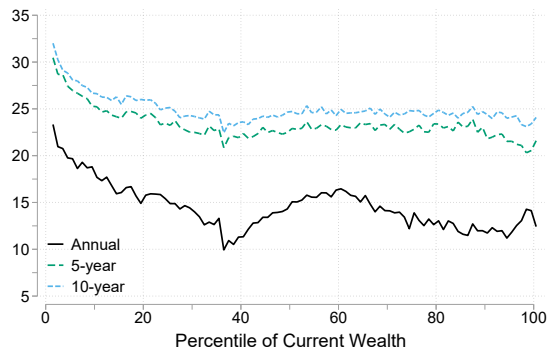


## Age 45



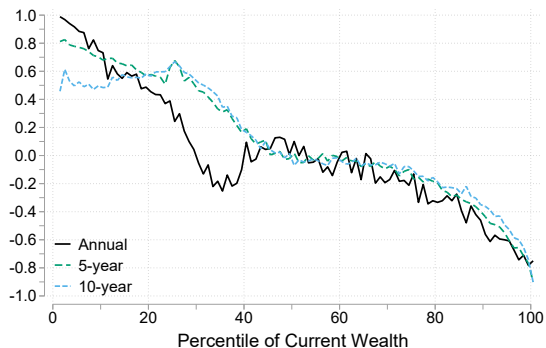
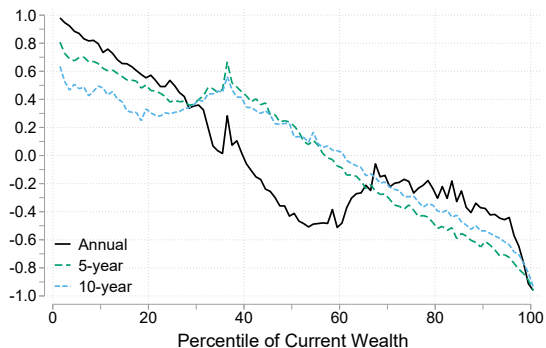
Over longer horizons more evenly spread and dispersion growing

# Rank Changes: Standard Deviation [◀ back](#)



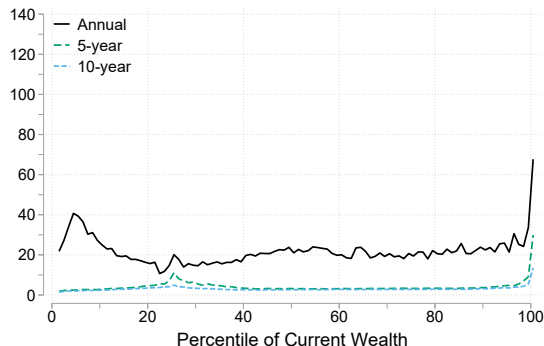
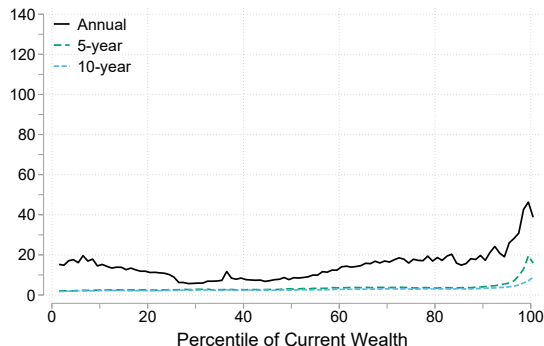
- Dispersion grows slowly with time horizon
- Dispersion level depends (asymmetrically) on rank: Lower dispersion at the top!

## Rank Changes: Skewness

[◀ back](#)

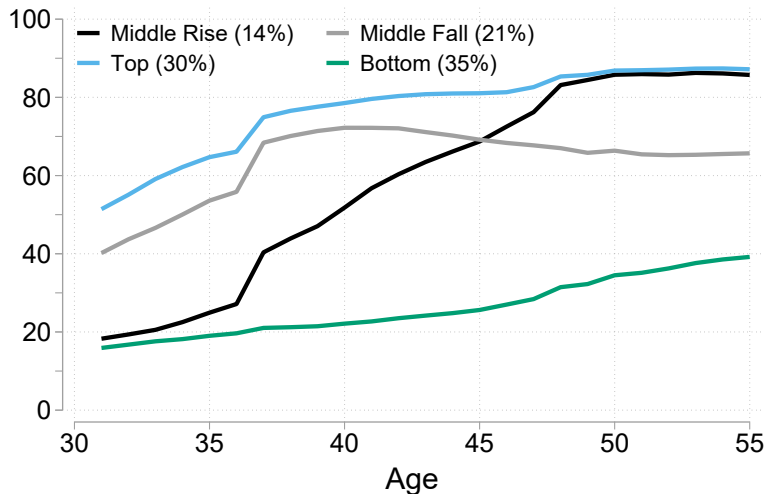
- Skewness decreases by construction
- Changes in ranks: No way to go but up/down for low/high ranks

## Rank Changes: Kurtosis [◀ back](#)



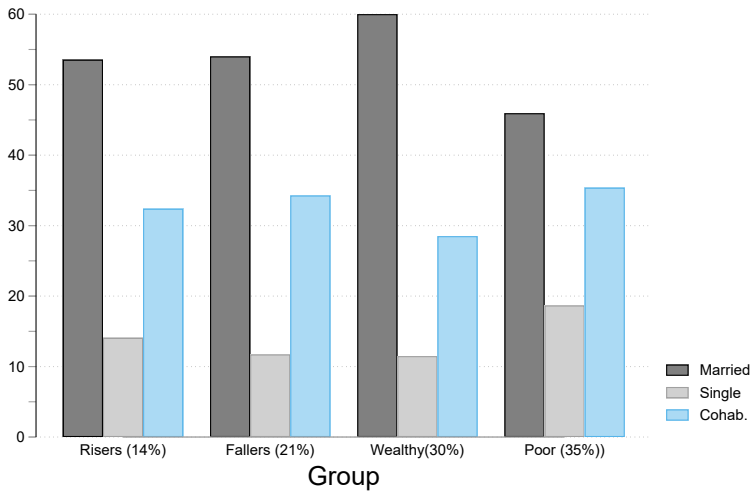
- Distribution of rank changes is *leptokurtic*
- Most individuals experience small changes with some individuals having large changes
- Holds across ranks but is particularly so at short horizon (1y) and upper tail

# Home-ownership Rates by Cluster

[◀ Back](#)



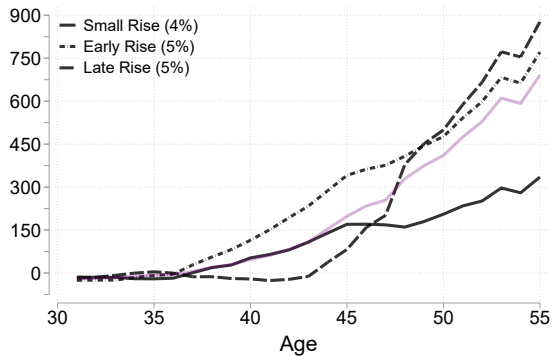
## Civil Status at Age 55 by Cluster

[◀ Back](#)

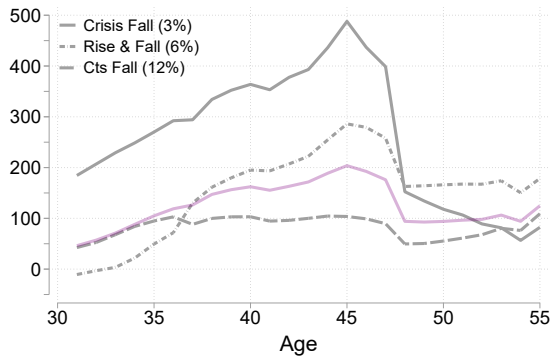
# Sub-Clusters - Wealth Level

[◀ back](#)

## Risers



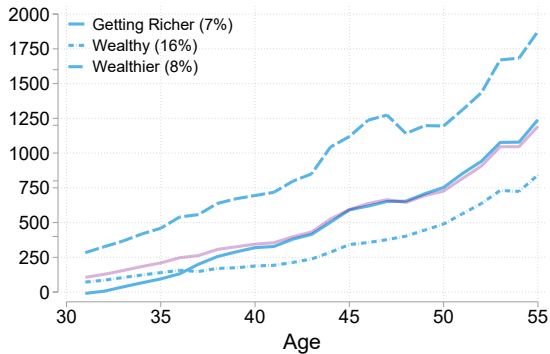
## Fallers



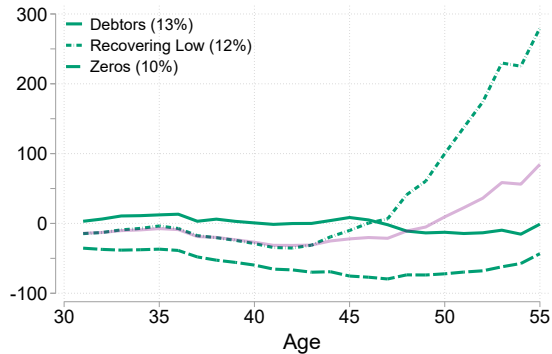
# Sub-Clusters - Wealth Level

[◀ back](#)

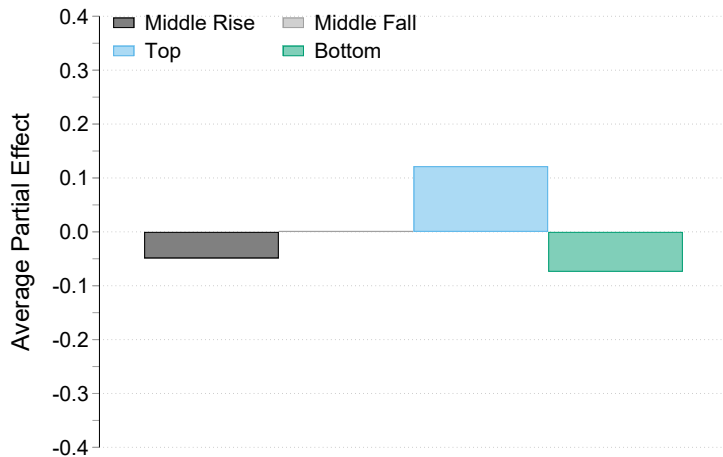
## Wealthy



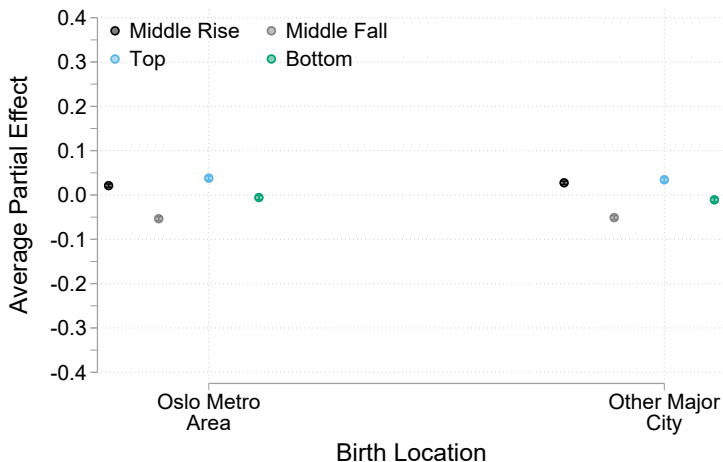
## Poor



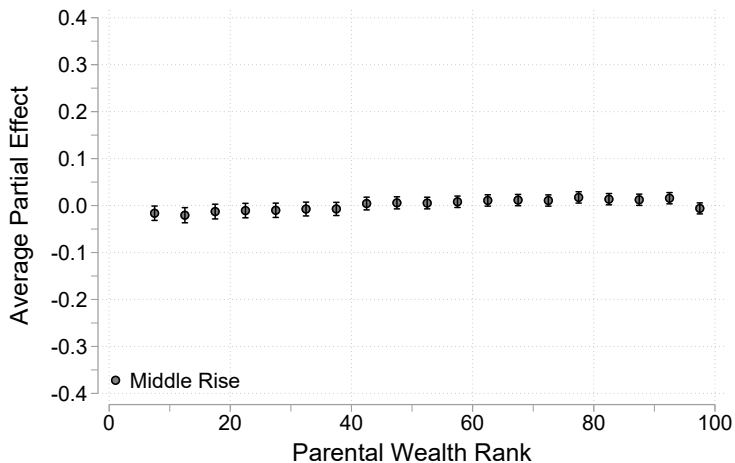
# Sex Average Partial Effect [◀ back](#)



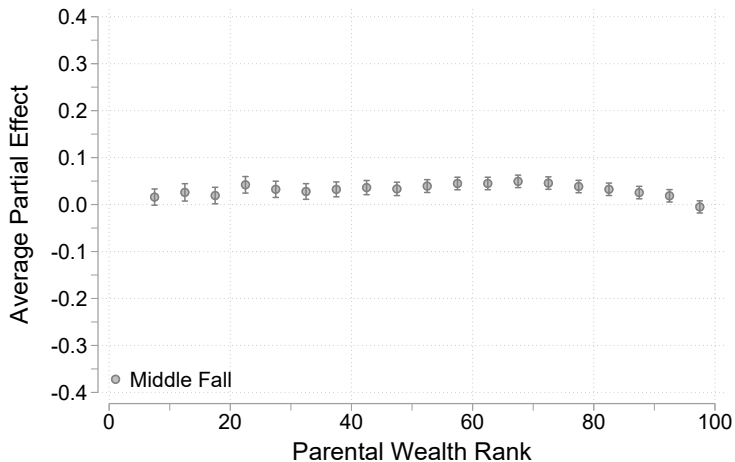
# Where Is The Land of Opportunity? Norway

[◀ back](#)

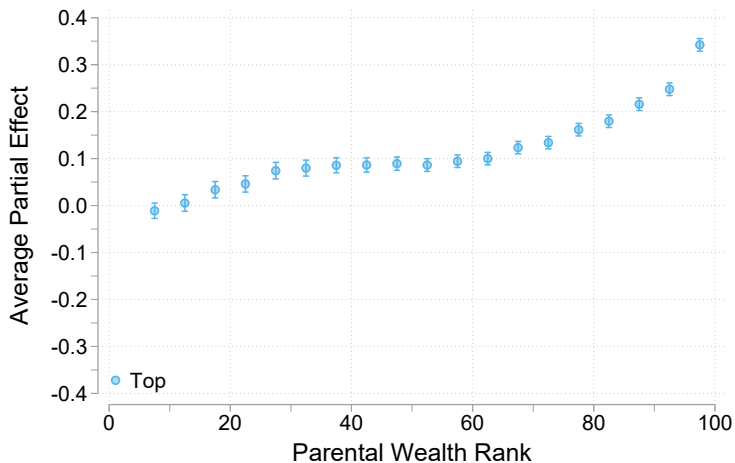
# The Non-Linear Effect of Parental Wealth: CI

[◀ back](#)

# The Non-Linear Effect of Parental Wealth: CI

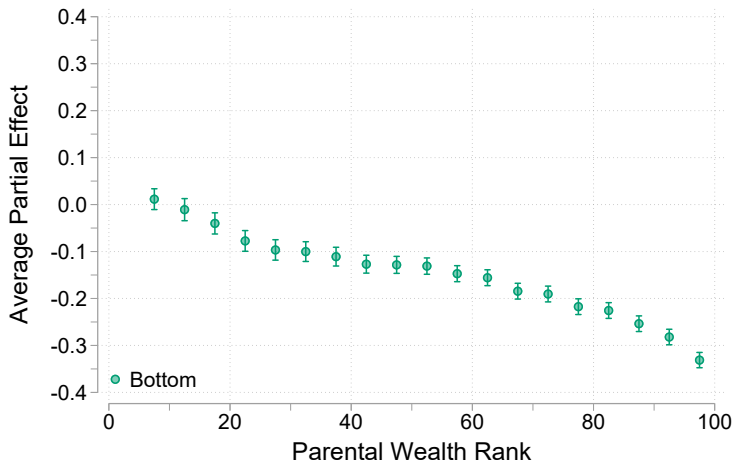
[◀ back](#)

# The Non-Linear Effect of Parental Wealth: CI

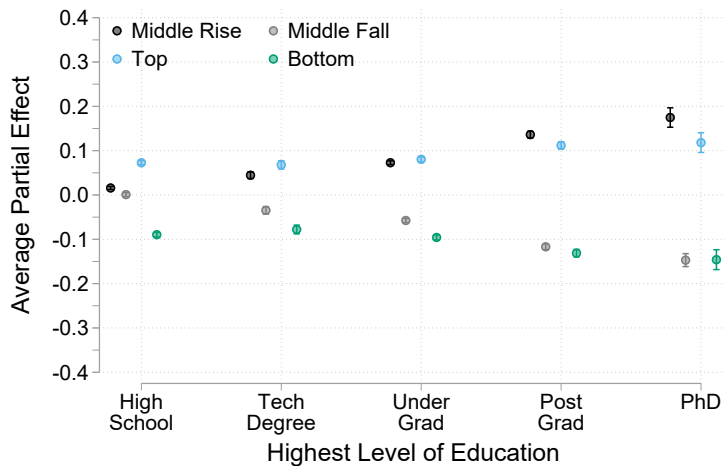
[◀ back](#)



# The Non-Linear Effect of Parental Wealth: CI

[◀ back](#)

# Learn & Rise?: CI

[◀ back](#)

## How Important Are Ex-Ante Explanations? [◀ back](#)

Share of Cross-Group Variation Explained by Variable

Group	Full Model	Partial Contribution			
		Parent	Sex	Education	Birth Place
1	2.12	0.15	0.55	1.35	0.06
2	1.23	0.17	0.02	0.65	0.4
3	9.15	4.89	1.61	2.54	0.12
4	7.70	4.37	0.92	2.33	0.08
<b>All</b>	6.44	3.34	0.95	1.99	0.15

## How Important Are Ex-Ante Explanations? [◀ back](#)

### Share of Individuals Correctly Classified

Group	Full Model	Total Contribution*	Partial Contribution			
			Parent	Sex	Birth Place	Education
1	14.33	1.99	0.13	0.46	0.08	1.32
2	21.16	1.29	0.17	0.02	0.37	0.74
3	30.46	4.99	2.59	1.02	0.10	1.28
4	34.05	3.65	2.11	0.34	0.02	1.18
<b>All</b>	<b>27.44</b>	<b>3.28</b>	<b>1.52</b>	<b>0.49</b>	<b>0.13</b>	<b>1.14</b>

\* Contribution relative to random classification using population shares.

# How Important Are Ex-Ante Explanations? [◀ Back](#)

## Two measures:

1. Distance Weighted Classification Rate  $\in [0, 1]$

$$1 - \frac{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) D(g(i), k)}{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k) D(g(i), k)} \quad \left( \text{in spirit of } \frac{ESS}{TSS} \right)$$

# How Important Are Ex-Ante Explanations? [◀ Back](#)

## Two measures:

1. Distance Weighted Classification Rate  $\in [0, 1]$

$$1 - \frac{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) D(g(i), k)}{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k) D(g(i), k)} \quad \left( \text{in spirit of } \frac{ESS}{TSS} \right)$$

2. Correct Classification Rate  $\in [0, 1]$

$$\frac{1}{N} \sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) \mathbb{1}[g(i) = k]$$

# How Important Are Ex-Ante Explanations? [◀ Back](#)

## Two measures:

1. Distance Weighted Classification Rate  $\in [0, 1]$

$$1 - \frac{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) D(g(i), k)}{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k) D(g(i), k)} \quad \left( \text{in spirit of } \frac{ESS}{TSS} \right)$$

2. Correct Classification Rate  $\in [0, 1]$

$$\frac{1}{N} \sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) \mathbb{1}[g(i) = k]$$

- Report Shapley-Owen decomposition of covariates
  - Order invariant & sums to statistic + Single value per covariate category

# How Important Are Ex-Ante Explanations? [◀ Back](#)

Total Contribution *	Partial Contribution			
	Parent	Sex	Education	Birth Place
Share of Distance Variation Explained by Variable (pp)				
6.44	2.32	3.38	0.65	0.08

\* Contribution relative to random classification using population shares.

[▶ Breakdown D](#)[▶ Breakdown C](#)



## How Important Are Ex-Ante Explanations? [◀ Back](#)

Total Contribution *	Partial Contribution			
	Parent	Sex	Education	Birth Place
<b>Share of Distance Variation Explained by Variable (pp)</b>				
6.44	3.34	0.95	1.99	0.158
<b>Share of Individuals Correctly Classified (pp)</b>				
3.28	1.52	0.49	0.13	1.14

\* Contribution relative to random classification using population shares.

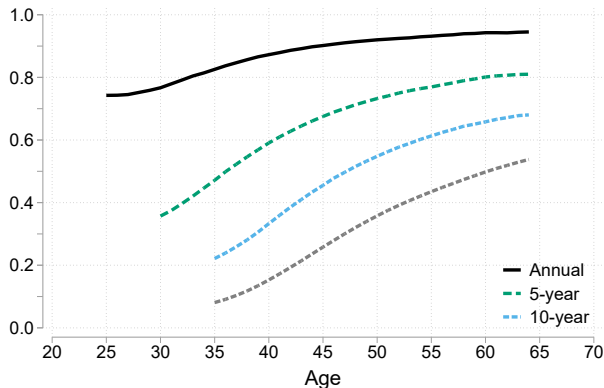
Share of individuals correctly classified by random classification 17.63% vs 21.02% with full model.

[▶ Breakdown D](#)

[▶ Breakdown C](#)

# Persistence in Wealth Rank: Higher at long-run [◀ back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$

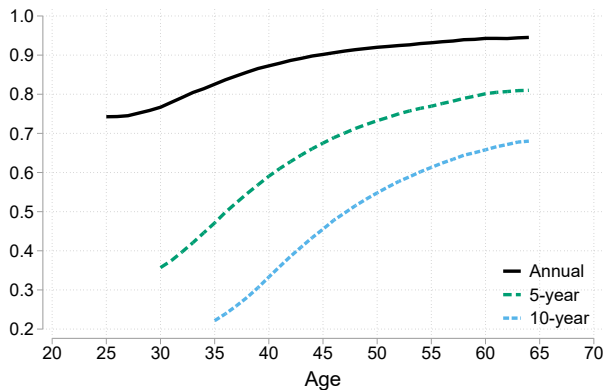


- **10y Iteration bias:** Dramatic bias! Actual  $\rho(10)$  is 50-250% implied persistence

# Persistence in Wealth Rank: Higher at long-run

[▶ 1960bc](#)[▶ 10yr](#)[◀ Back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h) y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$

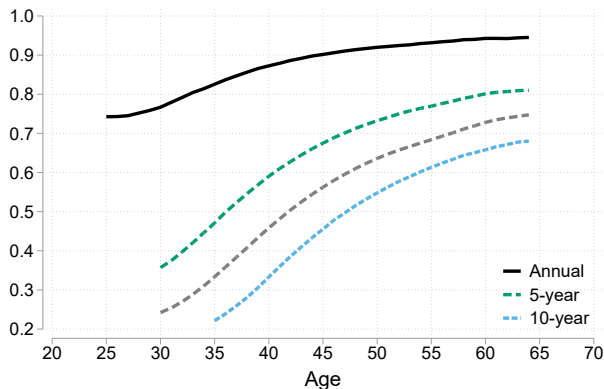


- Annual persistence is slow to stabilize, but eventually high ( $\rho_t(1) \approx 0.95$ )

# Persistence in Wealth Rank: Higher at long-run

[▶ 1960bc](#)[▶ 10yr](#)[◀ Back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$

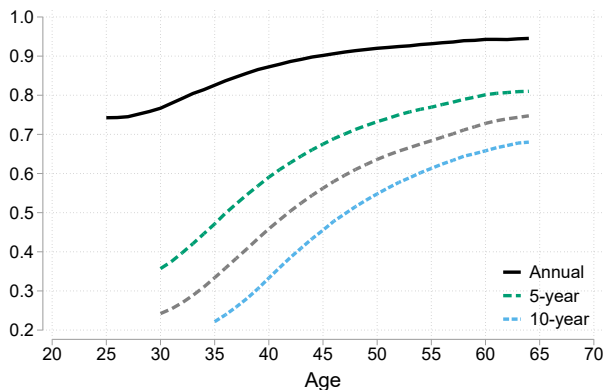


- **5y Iteration bias:** 5y Persistence higher than implied by annual  $\rho$

# Persistence in Wealth Rank: Higher at long-run

[▶ 1960bc](#)[▶ 10yr](#)[◀ Back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$



- **5y Iteration bias:** 5y Persistence higher than implied by annual  $\rho$
- Life cycle snapshots can be misleading! Short-run mobility  $\gg$  Long-run mobility

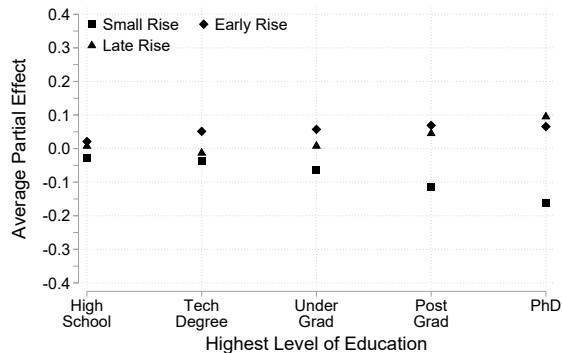
# What about heterogeneity within clusters? Middle Risers

[◀ Back](#)

## Parental Wealth



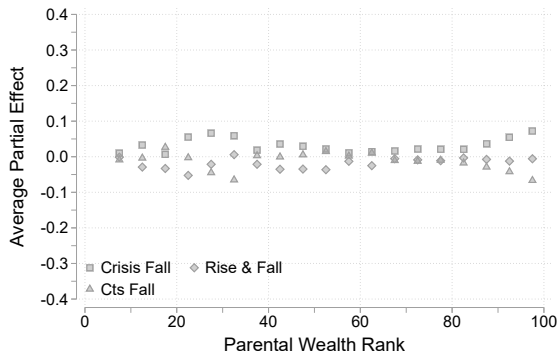
## Education



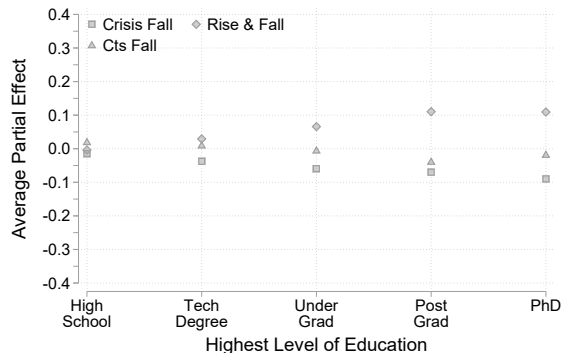
- Within Risers, movers not predicted by parental wealth
- Education predicts timing

## What about heterogeneity within clusters? Middle Fallers [◀ Back](#)

Parental Wealth



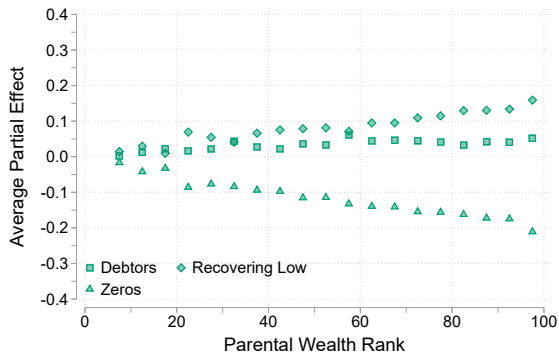
Education



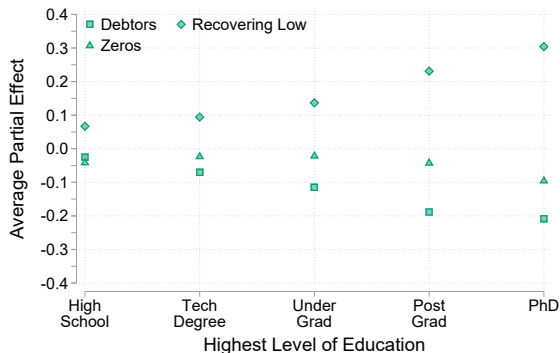
- Similar to Risers, little role for parental wealth
- But Education predicts dynamics

## What about heterogeneity within clusters? Bottom Group [◀ Back](#)

### Parental Wealth



### Education



- Among poor, parental wealth does not predict movements
- Education predicts recovery



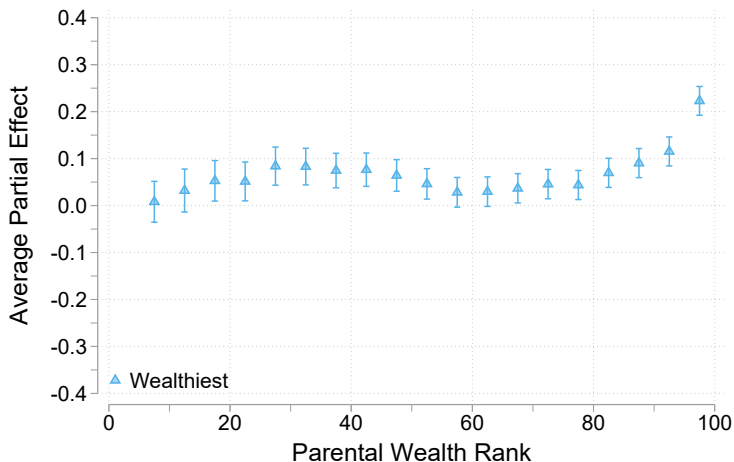
# The Non-Linear Effect of Parental Wealth for Wealthy: CI

[← back](#)

# The Non-Linear Effect of Parental Wealth for Wealthy: CI

[◀ back](#)

# The Non-Linear Effect of Parental Wealth for Wealthy: CI

[◀ back](#)

# Learn & Rise for Wealthy: CI

[◀ back](#)