

# The Life Cycle Dynamics of Wealth Mobility

Richard Audoly  
FRBNY

Rory M<sup>c</sup>Gee  
UWO

Sergio Ocampo  
UWO

Gonzalo Paz-Pardo  
ECB

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**Today:** Document patterns of wealth mobility across life cycle

Made possible by **Norwegian administrative data** on wealth 1993–2017

# Three Main Exercises: Focus on individuals' rank in wealth distribution

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  - **Zoom-in:** *sub-clusters* show heterogeneity in paths for groups moving through different sections of the distribution
3. Predict trajectories with individual circumstances
  - Determinants of paths through the distribution: prev. generation, education, etc.



# Contributions

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4. Dimension reduction methods in economics & applications to labour markets
  - K-Means (Bonhome, Lamadon, Manresa; Gregory, Menzio, Wiczer), Sequence Analysis (Humphries), Hidden Markov (Ahn, Hobijn, Şahin), Finite Mixture

# Norwegian Wealth Data

# Data: Norwegian Tax Registry 1993 – 2017 [▶ Context](#)

- No top-coding + Limited misreporting or measurement error (third-party reporting)
- We link to administrative records (Education, Civil Status, Income)
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## **Sample selection:** Norwegian residents 1993–2017, born 1905–1990

- Drop emigrants and immigrants after 25 or 2011
- Focus on birth cohort born between 1960 and 1965 (first observed in early 30s)
  - 292,222 individuals in this sample (217,383 after balancing)

# Ranks and Histories

- Compute within cohort ranks as

$$y_{i,t} = 100 \times F_w(w_{i,t}|t, i \in BC(i))$$

- Computed separately for each year and each cohort (uses unbalanced panel)



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- Computed separately for each year and each cohort (uses unbalanced panel)
- Histories of ranks (trajectories)

$$\mathbf{Y}_i = (y_{i,1993}, y_{i,1994}, \dots, y_{i,2016}, y_{i,2017}) \in [0, 100]^{25}$$

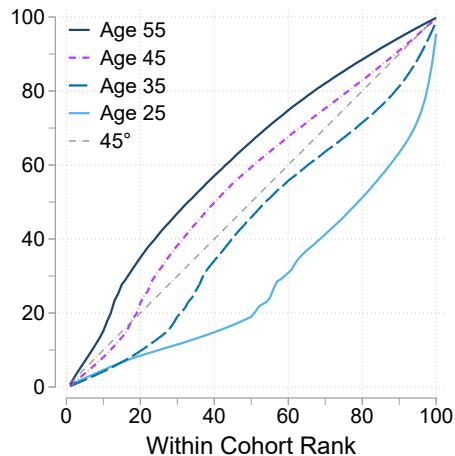
- Vector of rank outcomes (for balanced panel)

We are interested in the distribution of the vectors  $\mathbf{Y}_i$

- Significant changes in wealth levels as the cohort ages
- Significant changes in wealth levels across ranks

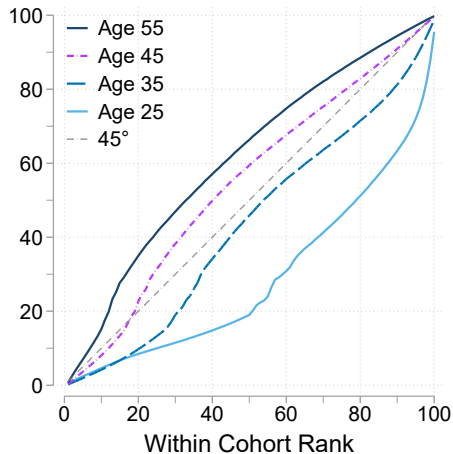
# Birth Cohort Ranks vs Population Ranks vs Wealth Levels

## BC Ranks vs Pop Ranks

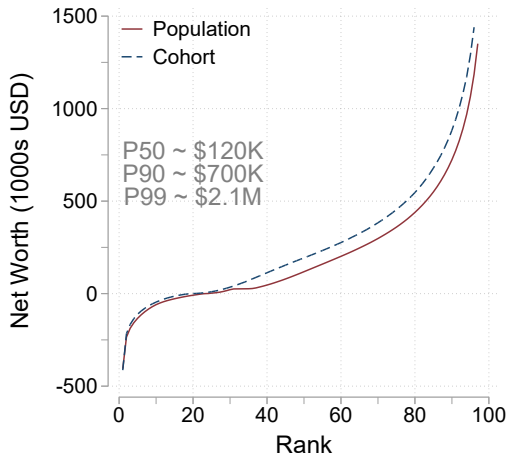


# Birth Cohort Ranks vs Population Ranks vs Wealth Levels

## BC Ranks vs Pop Ranks



## Net Worth CDF (2014)



- US: p90~\$620K, p99~\$3.5M (SZZ, 2022)

# Patterns of Mobility

# How much does people's wealth rank $y_{i,t}$ change over time?

Distribution of future ranks conditional on current rank

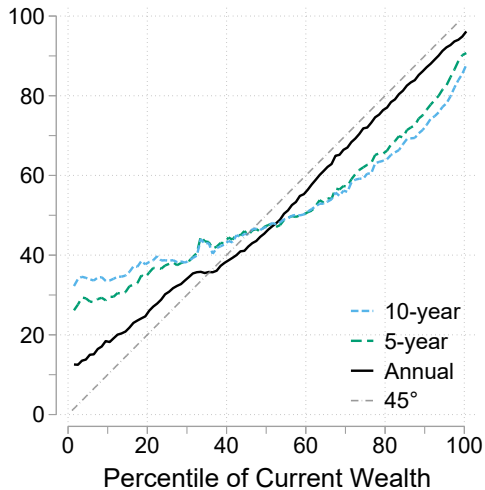
- Conditional mean  $E[y_{i,t+h}|y_{i,t}]$  (also higher order moments)
- Conditional quantiles  $Q_{y_{i,t+h}|y_{i,t}}(\tau)$  for  $\tau \in \{0.1, 0.25, 0.75, 0.9\}$

# How Non-Linear is Wealth Mobility?

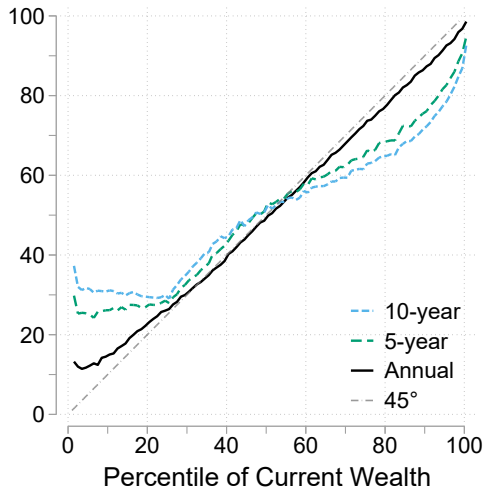
► Age 31

► Income

## Age 35 – Cond. Mean



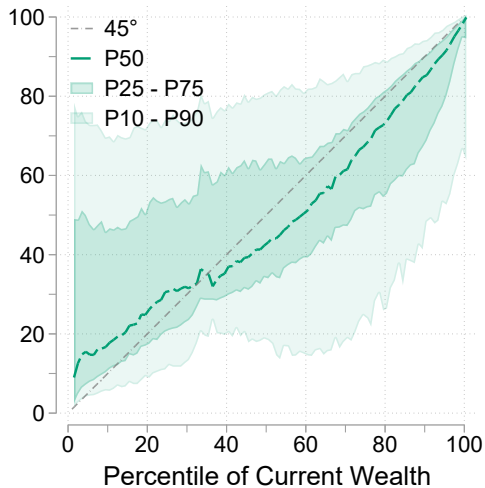
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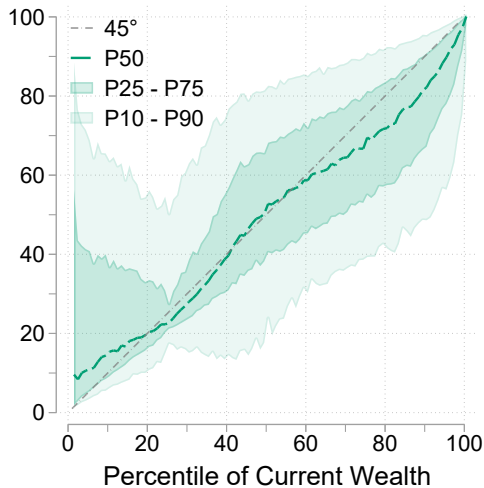
# The Distribution of Rank Changes (5-year)

1y Chg 10y Chg

Age 35



Age 45



At the top few fall, but cushioned Middle class rarely climb, but some fall

# Distribution of rank changes is non-linear and age-dependent!

- Mean reversion in ranks weakens at the top
- Dispersion ↓ with age (consistent w evidence on income) and initial rank
  - Median change is close to no change at all ages(!)

▶ std. dev.

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Comparing ranks at given ages gives an incomplete view of wealth mobility

**Next Step:** Analyze distribution of complete trajectories through the wealth distribution

# Clustering Wealth Histories

# Grouping Individuals Into Typical Histories

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- Recursively merge groups by selecting *similar* pairs:  $\operatorname{argmin}_{g, g' \in G, g \neq g'} d(g, g')$ .

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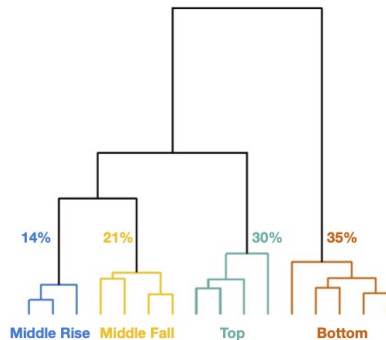
**Result:** Hierarchy of partitions ranging from  $G = N$  to  $G = 1$ .

- Similar results for alternative clustering (cum. change, log-assets, “Lorenz” position)

# Two Levels of Clustering

1. Focus on 4 major clusters (branches)
  - Explain majority of variation in rank histories ( $R^2=0.52$ )

Clustering Tree

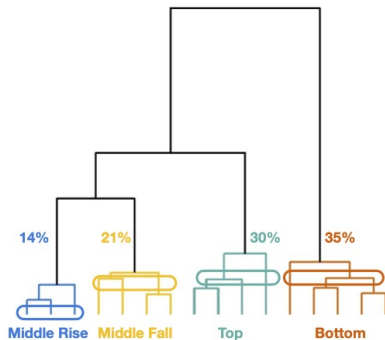




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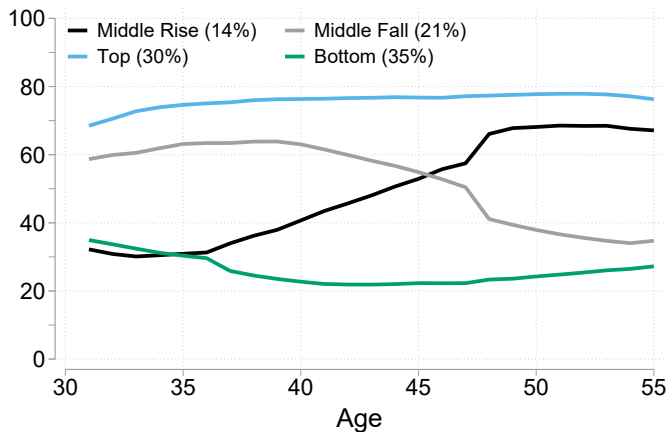
1. Focus on 4 major clusters (branches)
  - Explain majority of variation in rank histories ( $R^2=0.52$ )
2. Zoom into each major cluster
  - Pick 3 main sub-clusters
  - Reveal heterogeneity in major trajectories
  - 12 clusters explain 20% additional variation ( $R^2=0.63$ ; 16 CI,  $R^2=0.66$ )

Clustering Tree



# Typical Rank Histories: Segmented Mobility

## Cohort Ranks



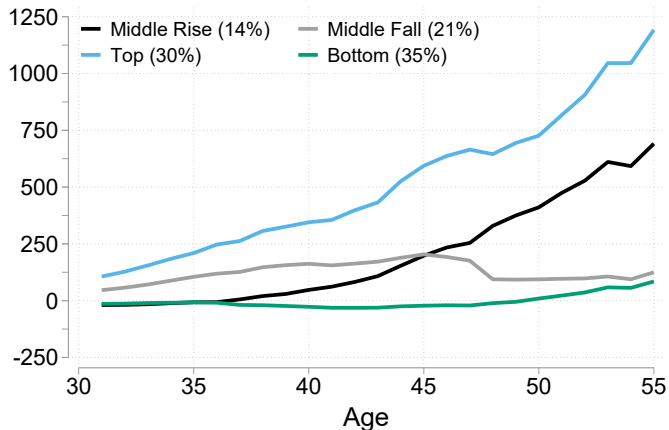
4 Main clusters show patterns of **segmented mobility**

- Individuals move within segments of the distribution
- The mean trajectory of a group hides rank swaps within
- Segments overlap:  
Top 40% // Bottom 40% //  
Middle 80%

**Next:** Levels + Heterogeneity

# Wealth Histories Across Segments of the Distribution

## Net Worth (\$1000s)



Differences in ranks imply significant wealth differences:

- **Risers:** start with no wealth + grow like top group
- **Fallers:** ahead in 30s + low growth + great recession
- **Top:** Maintaining rank means rapid growth
- **Bottom:** Close to no wealth + growth in 50s (housing)

# What Else Happens Along These Paths?

- **Housing:** Increasing trends except for *fallers*
  - Fallers home-ownership: 40%→70%→65%
  - Risers home-ownership: 20%→85% (as high as top group)
- **Civil Status:** Similar marriage/cohabitation rates by cluster
  - Bottom group have lowest marriage rates, top group the highest
- **Portfolio Composition + Income:** Soon!

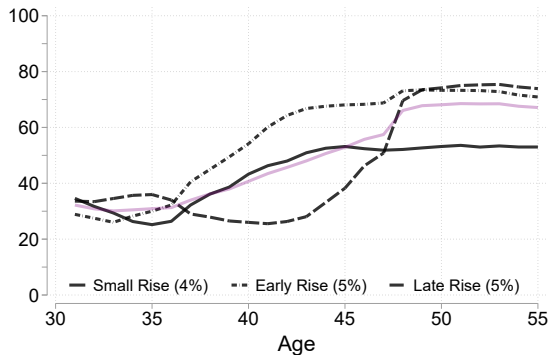
[▶ details](#)[▶ details](#)

**Next Step:** Zoom into heterogeneity within group

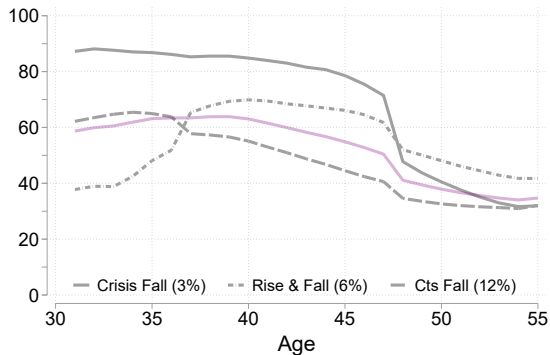
# Heterogeneity in Trajectories: Levels vs Timing

► Wealth Levels

## Middle Risers



## Middle Fallers

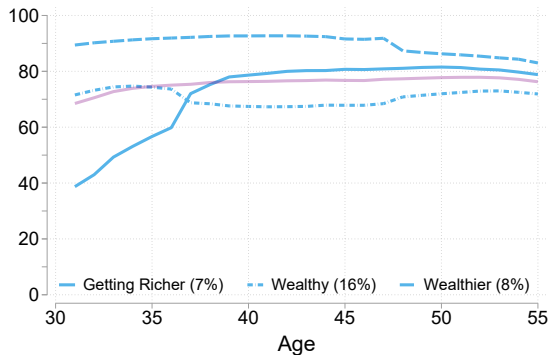


- Risers differ mainly in timing of changes (similar initial conditions)
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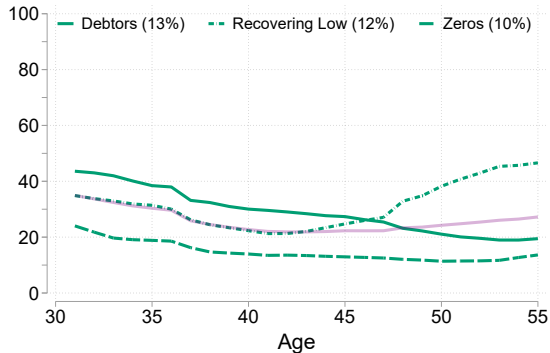
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## Bottom of the Distribution

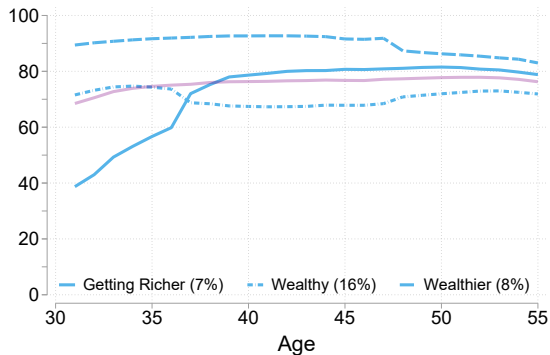


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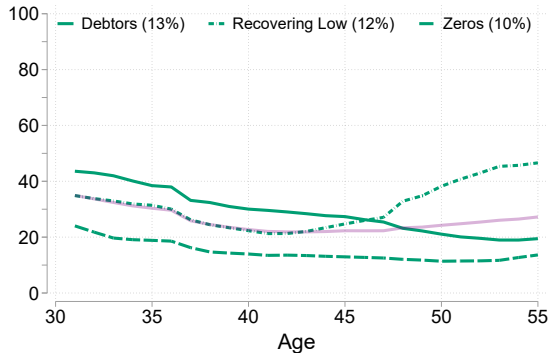
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# Towards Determinants of Trajectories



# Hereditary Advantage vs Human Capital

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► Sex APE

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Predictors explain at most 6.4% of cross-group variation (same as rank-rank inter-gen reg)

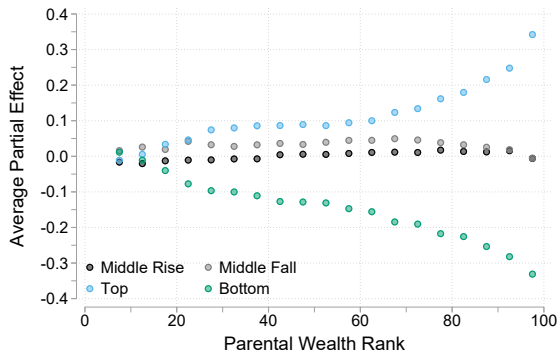
► Results

# The Non-Linear Effect of Parental Wealth and Education

▸ PW CIs

▸ ED CIs

## Parental Wealth

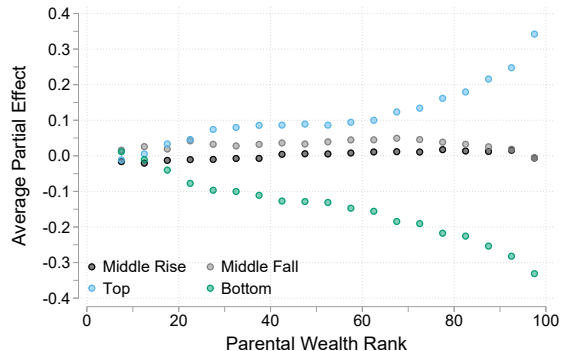


- Parental wealth's explanatory power: High for top/bottom, limited for middle groups

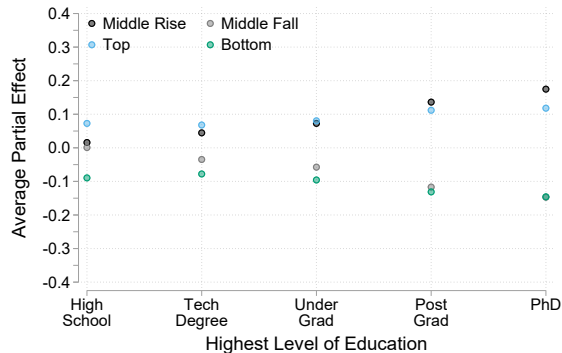
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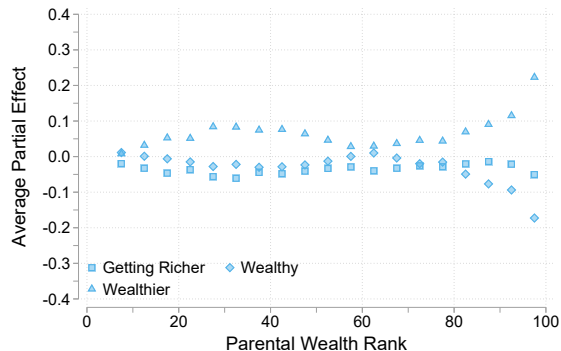


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- Education tells risers/fallers apart: Equalizing effect but doesn't overcome initial cond.

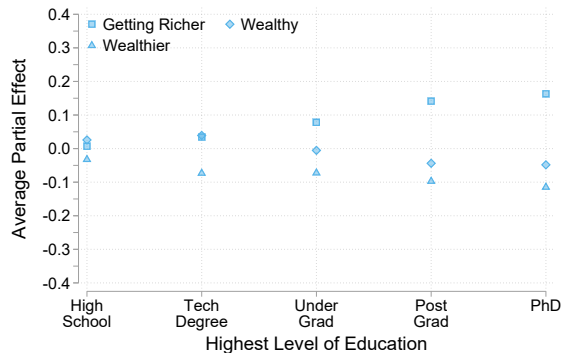
# What about heterogeneity within clusters? Top Group

Other CI PW ED

## Parental Wealth



## Education



- Even within the groups, movers are hard to predict with parental wealth
- Education predicts dynamics within groups (e.g., getting richer vs already wealthy)



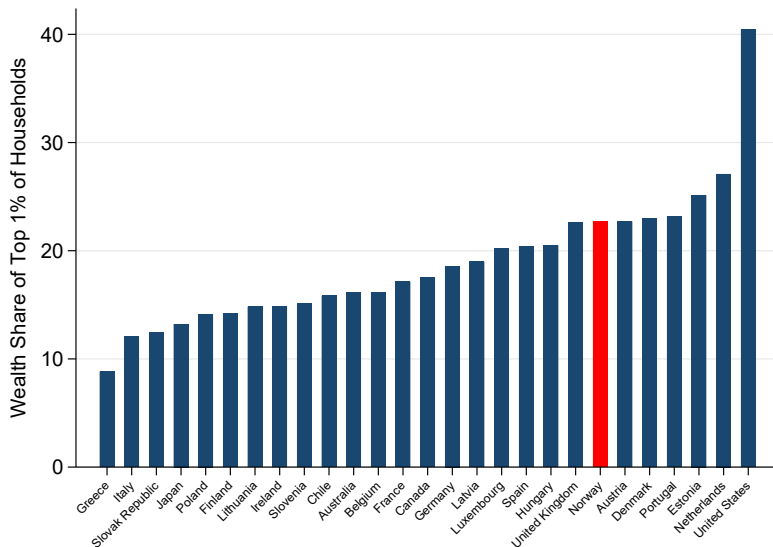
# Conclusions

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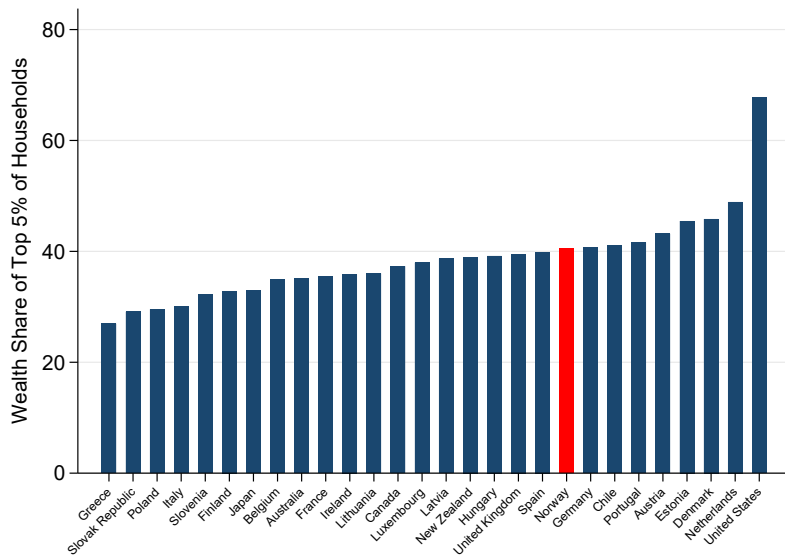
- Document persistence of wealth over the life cycle
- Characterise non-linear persistence and mobility
  - Top of the distribution cushioned against falls
- Uncover typical trajectories of individuals through the wealth distribution
- Intergenerational background an important predictor of **whole** history
  - But limited explanatory power
- Education is key for movements through the wealth distribution

Extra

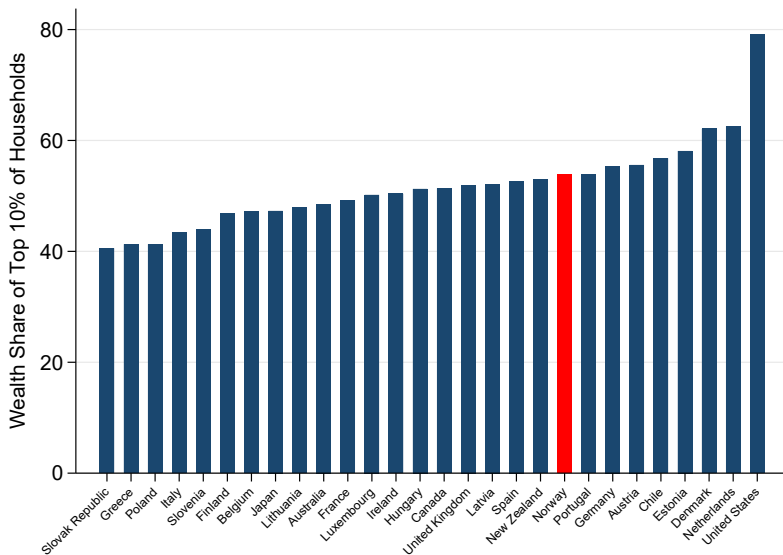
# Norway in Context

[◀ Back](#)

## Norway in Context: Top 5% Share [◀ Back](#)

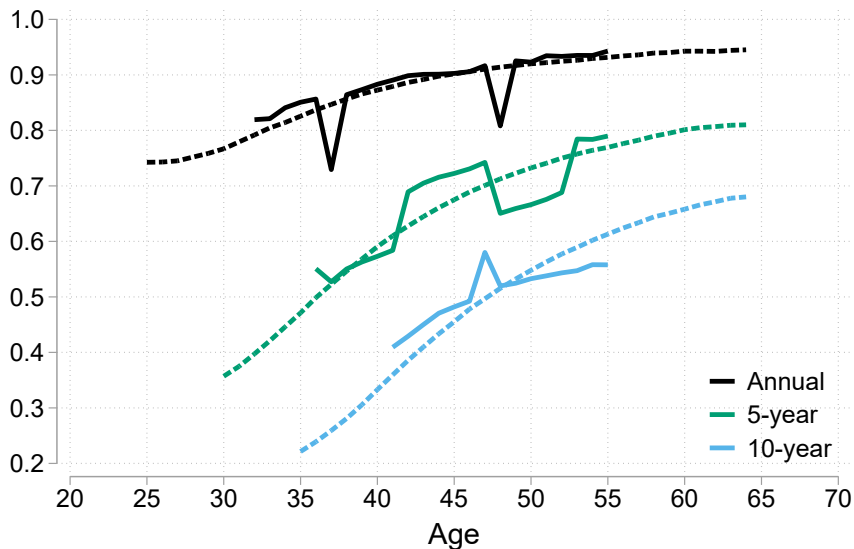


## Norway in Context: Top 10% Share [◀ Back](#)



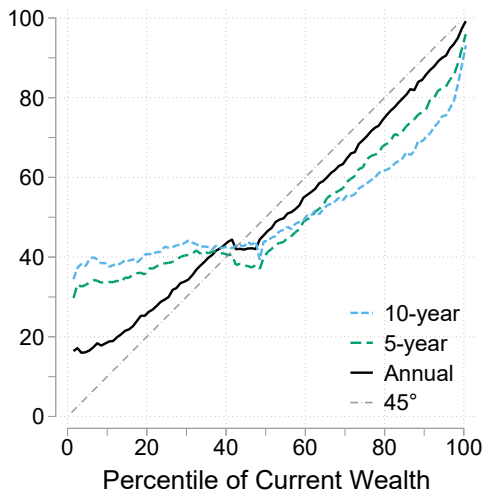
# Persistence in Wealth Rank: Within Cohort ◀

All Cohorts vs 1960-1964 Birth Cohort



# How Non-Linear is Wealth Mobility? [◀ back](#)

Age 31

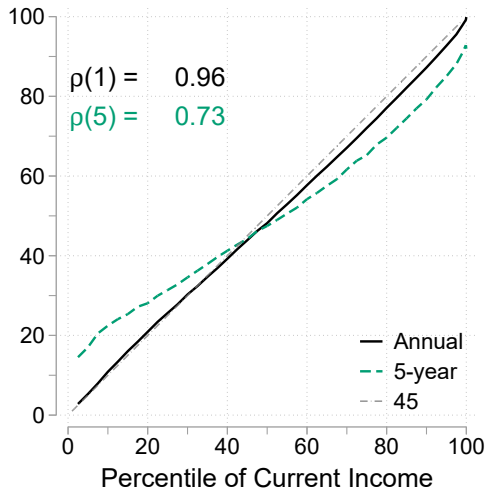




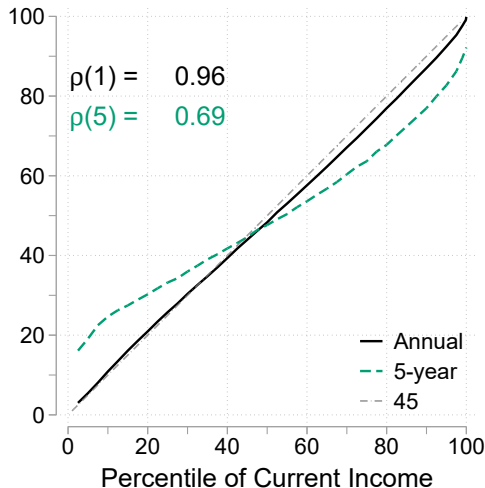
# How Non-Linear is Income Mobility in Norway?

[◀ back](#)[▶ USA](#)

## Age 35-44



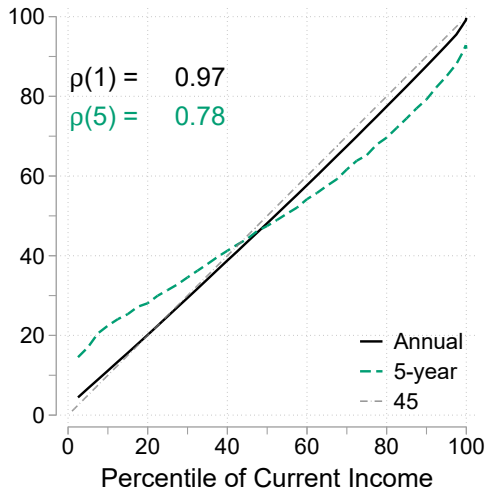
## All



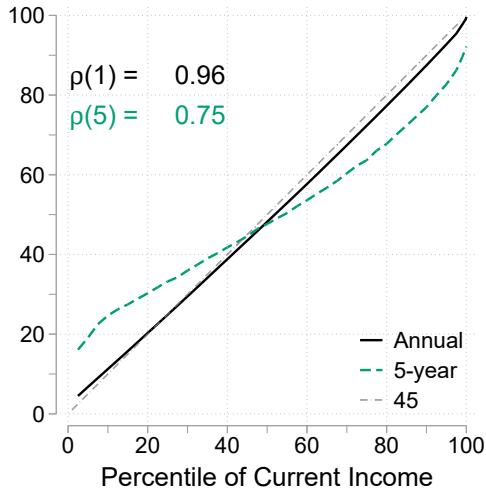
Source: GRID database for 2005

# How Non-Linear is Income Mobility in the U.S.? [◀ back](#)

Age 35-44



All

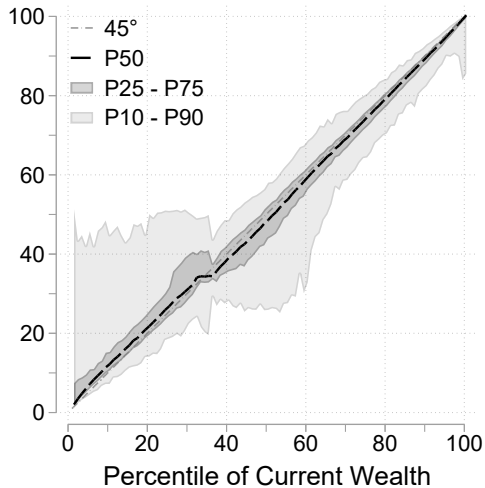


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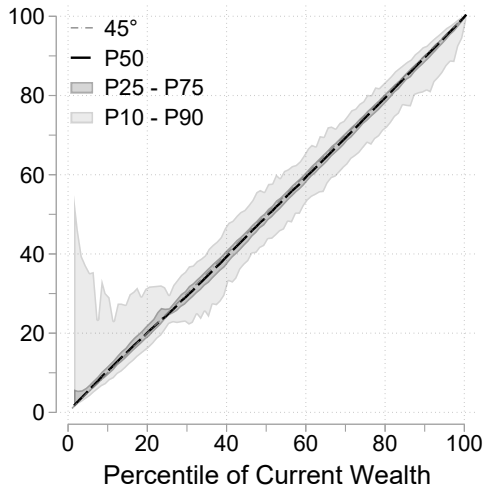
# The Distribution of Rank Changes (1-year)

[◀ back](#)[▶ 10y Chg](#)

## Age 35 – Cond. pct



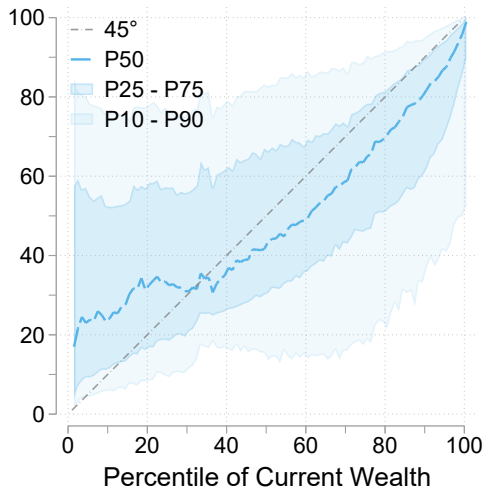
## Age 45 – Cond. pct



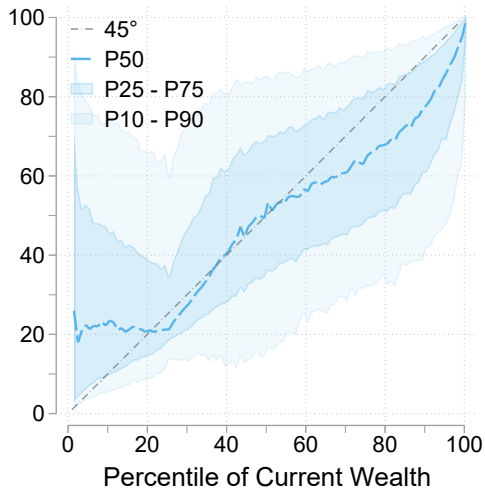
# The Distribution of Rank Changes (10-year)

[◀ back](#)

## Age 35

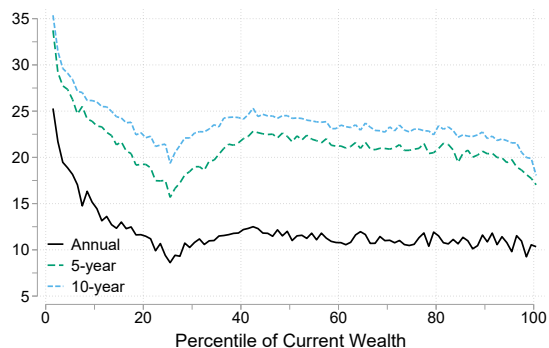
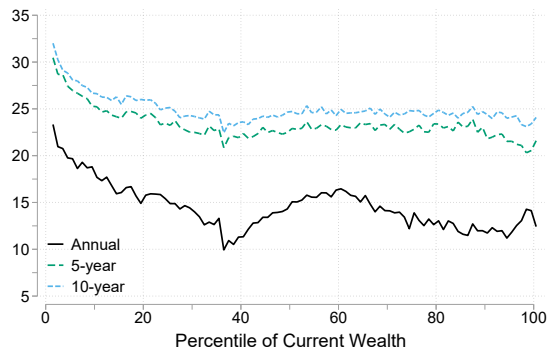


## Age 45



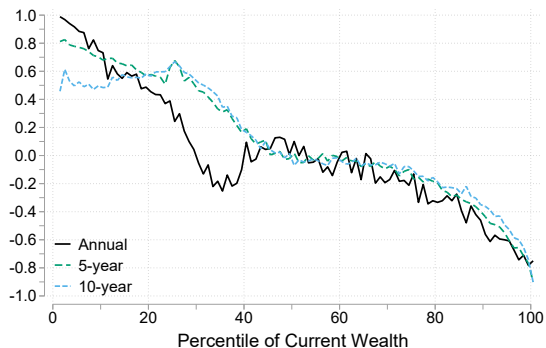
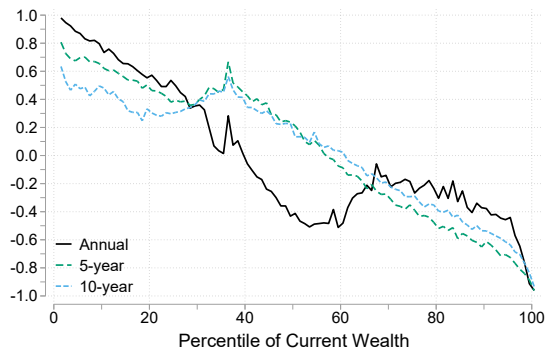
Over longer horizons more evenly spread and dispersion growing

# Rank Changes: Standard Deviation [◀ back](#)



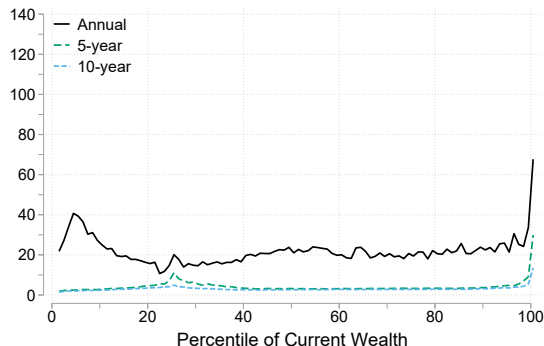
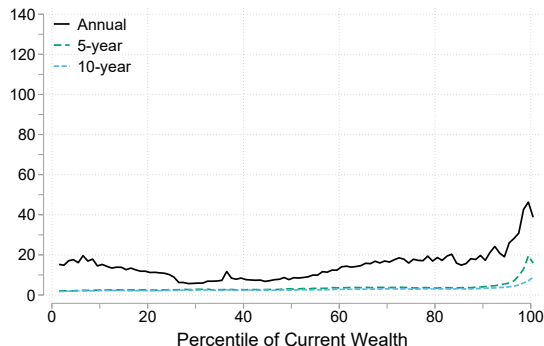
- Dispersion grows slowly with time horizon
- Dispersion level depends (asymmetrically) on rank: Lower dispersion at the top!

# Rank Changes: Skewness

[◀ back](#)

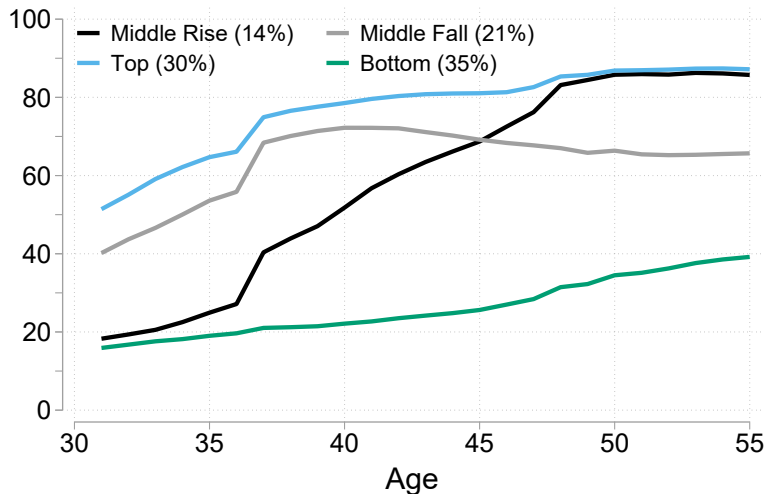
- Skewness decreases by construction
- Changes in ranks: No way to go but up/down for low/high ranks

## Rank Changes: Kurtosis [◀ back](#)



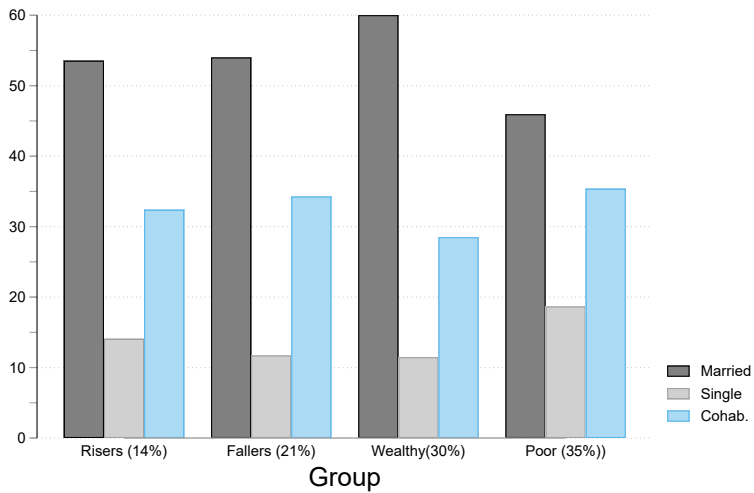
- Distribution of rank changes is *leptokurtic*
- Most individuals experience small changes with some individuals having large changes
- Holds across ranks but is particularly so at short horizon (1y) and upper tail

# Home-ownership Rates by Cluster

[◀ Back](#)



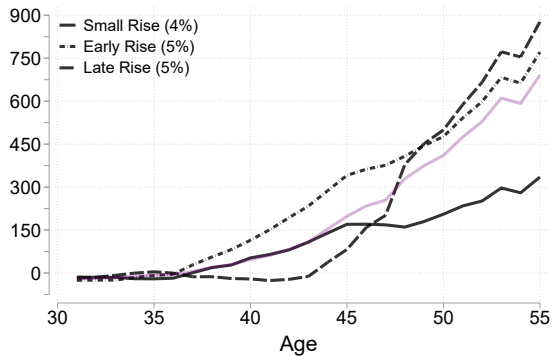
## Civil Status at Age 55 by Cluster

[◀ Back](#)

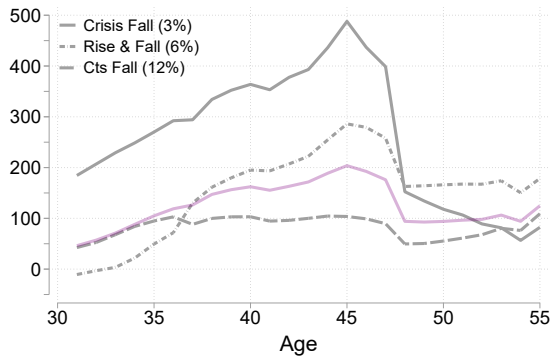
# Sub-Clusters - Wealth Level

[◀ back](#)

## Risers



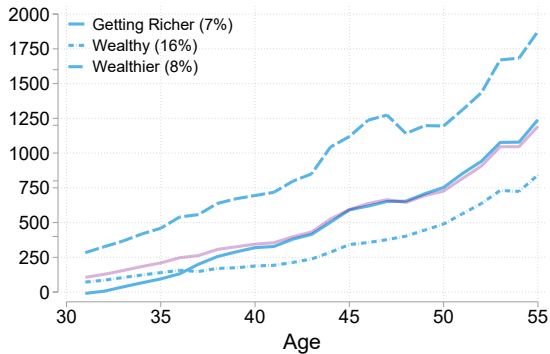
## Fallers



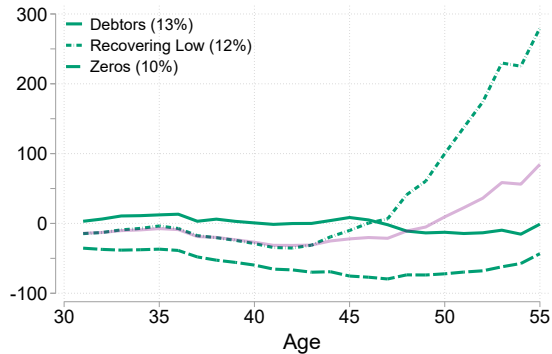
# Sub-Clusters - Wealth Level

[◀ back](#)

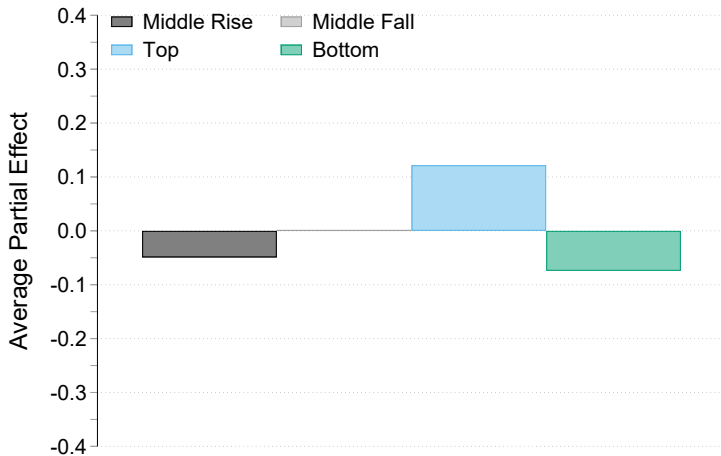
## Wealthy



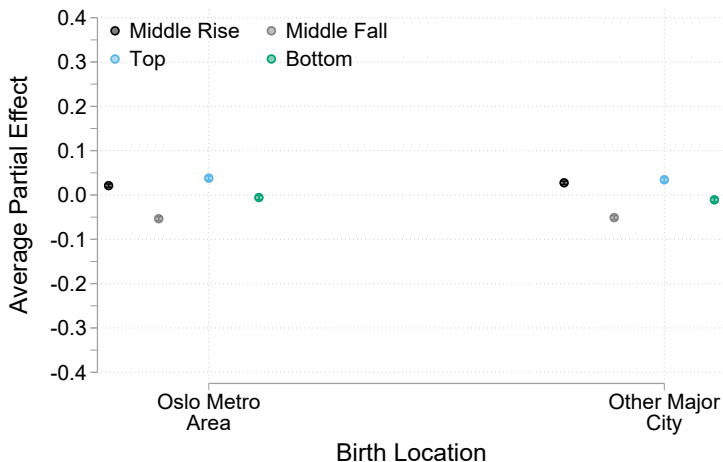
## Poor



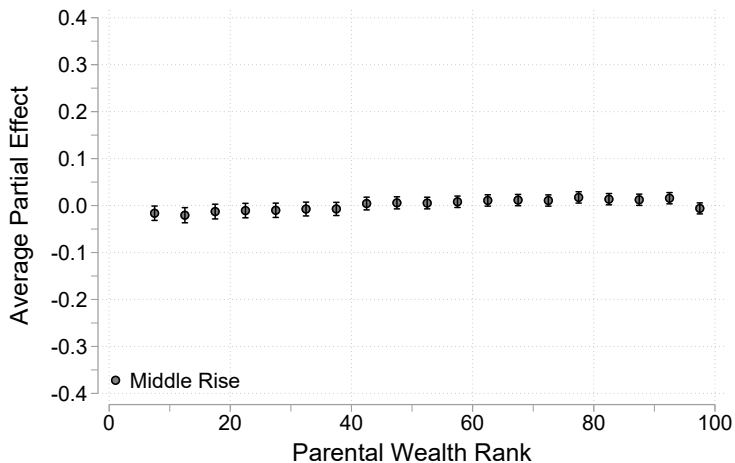
# Sex Average Partial Effect

[◀ back](#)

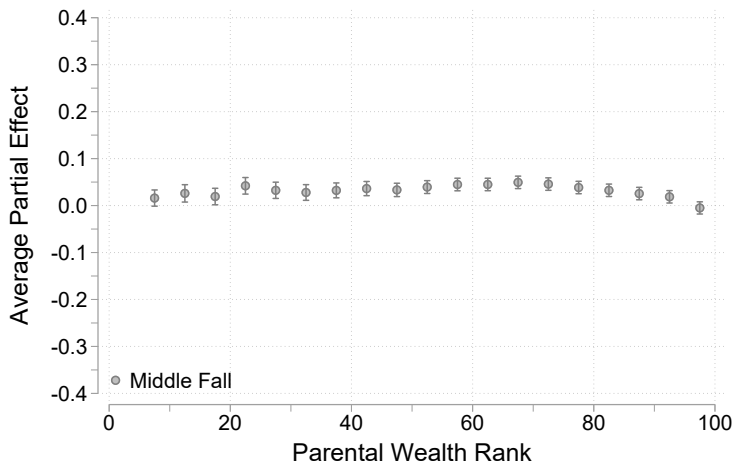
# Where Is The Land of Opportunity? Norway

[◀ back](#)

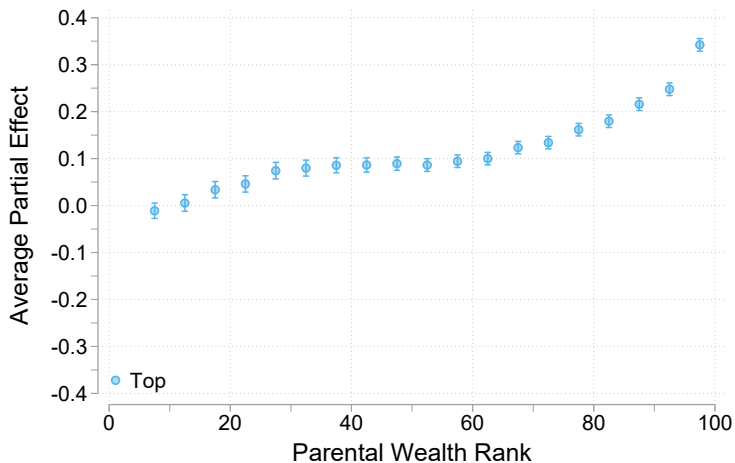
# The Non-Linear Effect of Parental Wealth: CI

[◀ back](#)

# The Non-Linear Effect of Parental Wealth: CI

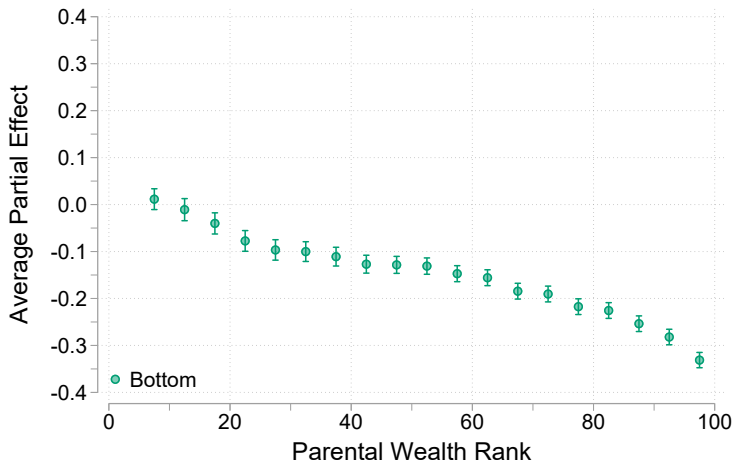
[◀ back](#)

# The Non-Linear Effect of Parental Wealth: CI

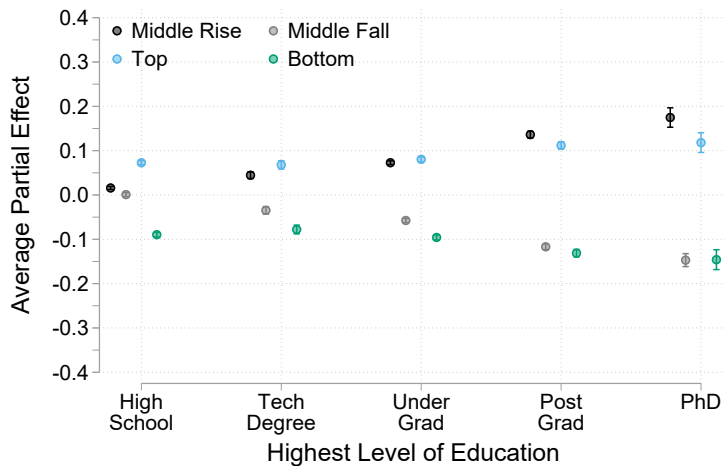
[◀ back](#)



# The Non-Linear Effect of Parental Wealth: CI

[◀ back](#)

# Learn & Rise?: CI

[◀ back](#)

## How Important Are Ex-Ante Explanations? [◀ back](#)

### Share of Cross-Group Variation Explained by Variable

Group	Full Model	Partial Contribution			
		Parent	Sex	Education	Birth Place
1	2.12	0.15	0.55	1.35	0.06
2	1.23	0.17	0.02	0.65	0.4
3	9.15	4.89	1.61	2.54	0.12
4	7.70	4.37	0.92	2.33	0.08
<b>All</b>	6.44	3.34	0.95	1.99	0.15

## How Important Are Ex-Ante Explanations? [◀ back](#)

### Share of Individuals Correctly Classified

Group	Full Model	Total Contribution*	Partial Contribution			
			Parent	Sex	Birth Place	Education
1	14.33	1.99	0.13	0.46	0.08	1.32
2	21.16	1.29	0.17	0.02	0.37	0.74
3	30.46	4.99	2.59	1.02	0.10	1.28
4	34.05	3.65	2.11	0.34	0.02	1.18
<b>All</b>	<b>27.44</b>	<b>3.28</b>	<b>1.52</b>	<b>0.49</b>	<b>0.13</b>	<b>1.14</b>

\* Contribution relative to random classification using population shares.

# How Important Are Ex-Ante Explanations? [◀ Back](#)

Two measures:

1. Distance Weighted Classification Rate  $\in [0, 1]$

$$1 - \frac{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) D(g(i), k)}{\sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k) D(g(i), k)} \quad \left( \text{in spirit of } \frac{ESS}{TSS} \right)$$

# How Important Are Ex-Ante Explanations? [◀ Back](#)

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2. Correct Classification Rate  $\in [0, 1]$

$$\frac{1}{N} \sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) \mathbb{1}[g(i) = k]$$

# How Important Are Ex-Ante Explanations? [◀ Back](#)

## Two measures:

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$$\frac{1}{N} \sum_{i=1}^N \sum_{k=1}^G \widehat{Pr}(g = k | X_i) \mathbb{1}[g(i) = k]$$

- Report Shapley-Owen decomposition of covariates
  - Order invariant & sums to statistic + Single value per covariate category

# How Important Are Ex-Ante Explanations? [◀ Back](#)

Total Contribution *	Partial Contribution			
	Parent	Sex	Education	Birth Place
<b>Share of Distance Variation Explained by Variable (pp)</b>				
6.44	2.32	3.38	0.65	0.08

\* Contribution relative to random classification using population shares.

[▶ Breakdown D](#)[▶ Breakdown C](#)



## How Important Are Ex-Ante Explanations? [◀ Back](#)

Total Contribution *	Partial Contribution			
	Parent	Sex	Education	Birth Place
<b>Share of Distance Variation Explained by Variable (pp)</b>				
6.44	3.34	0.95	1.99	0.158
<b>Share of Individuals Correctly Classified (pp)</b>				
3.28	1.52	0.49	0.13	1.14

\* Contribution relative to random classification using population shares.

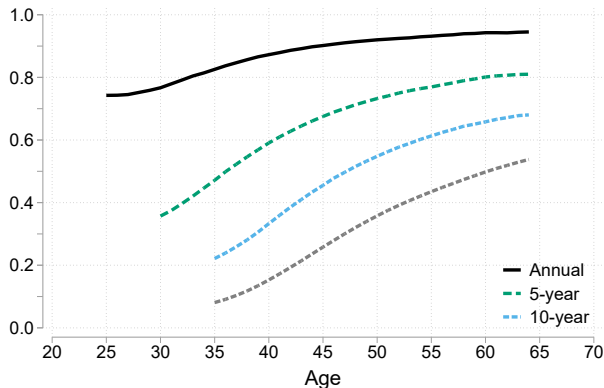
Share of individuals correctly classified by random classification 17.63% vs 21.02% with full model.

[▶ Breakdown D](#)

[▶ Breakdown C](#)

# Persistence in Wealth Rank: Higher at long-run [◀ back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$

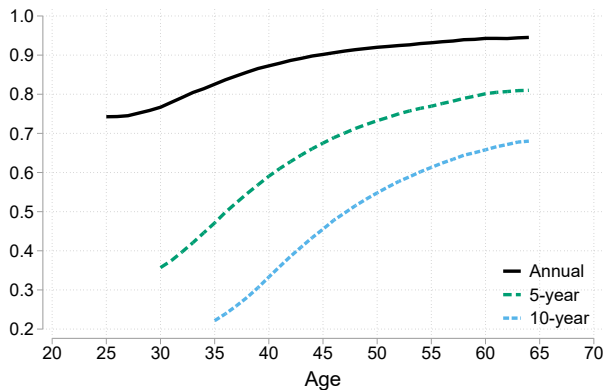


- **10y Iteration bias:** Dramatic bias! Actual  $\rho(10)$  is 50-250% implied persistence

# Persistence in Wealth Rank: Higher at long-run

[▶ 1960bc](#)[▶ 10yr](#)[◀ Back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$

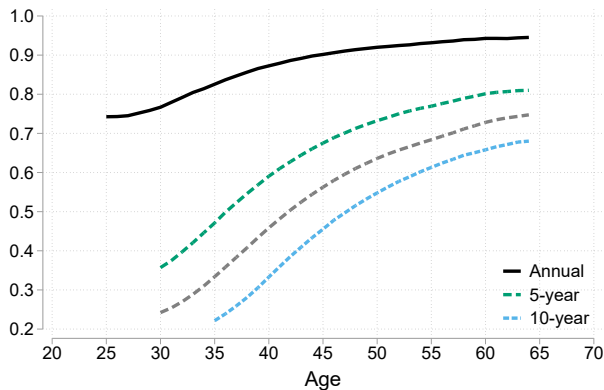


- Annual persistence is slow to stabilize, but eventually high ( $\rho_t(1) \approx 0.95$ )

# Persistence in Wealth Rank: Higher at long-run

[▶ 1960bc](#)[▶ 10yr](#)[◀ Back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$

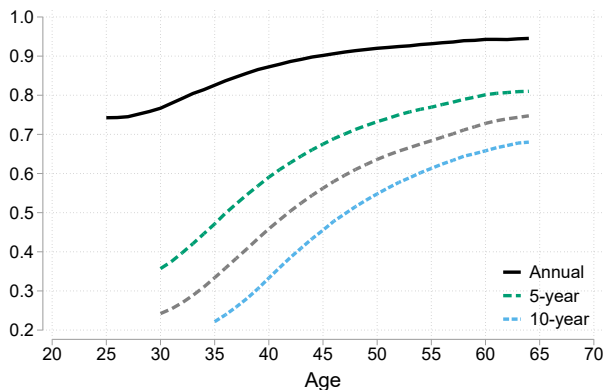


- **5y Iteration bias:** 5y Persistence higher than implied by annual  $\rho$

# Persistence in Wealth Rank: Higher at long-run

[▶ 1960bc](#)[▶ 10yr](#)[◀ Back](#)

$$y_{i,t} = \alpha_t(h) + \rho_t(h)y_{i,t-h} + u_{i,t}, \quad \text{for } h \in \{1, 5, 10\}$$



- **5y Iteration bias:** 5y Persistence higher than implied by annual  $\rho$
- Life cycle snapshots can be misleading! Short-run mobility  $\gg$  Long-run mobility

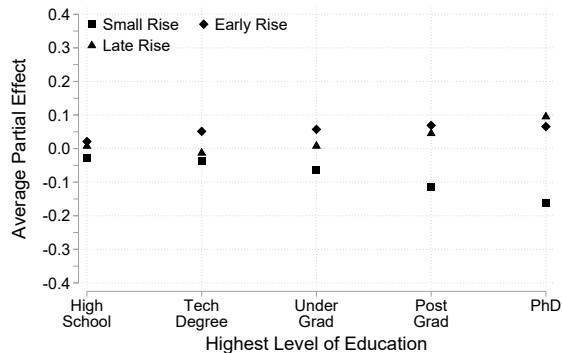
# What about heterogeneity within clusters? Middle Risers

[◀ Back](#)

## Parental Wealth



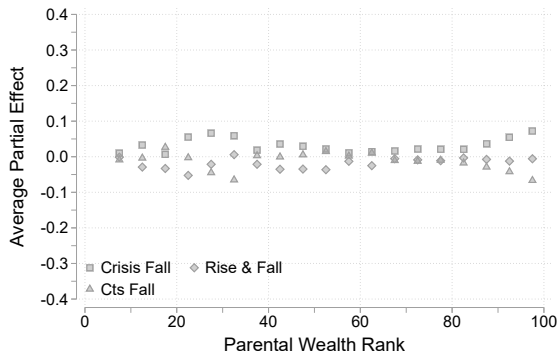
## Education



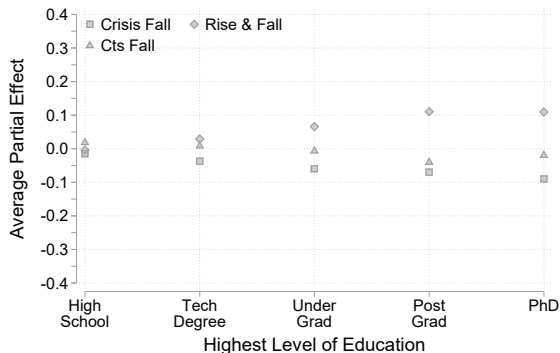
- Within Risers, movers not predicted by parental wealth
- Education predicts timing

## What about heterogeneity within clusters? Middle Fallers [◀ Back](#)

### Parental Wealth



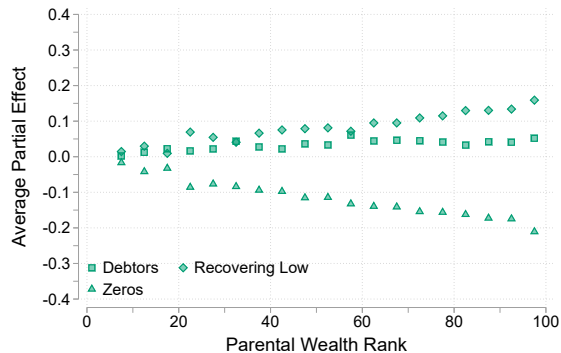
### Education



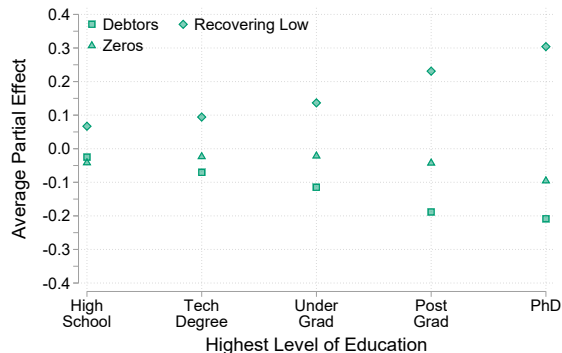
- Similar to Risers, little role for parental wealth
- But Education predicts dynamics

# What about heterogeneity within clusters? Bottom Group [◀ Back](#)

## Parental Wealth



## Education



- Among poor, parental wealth does not predict movements
- Education predicts recovery



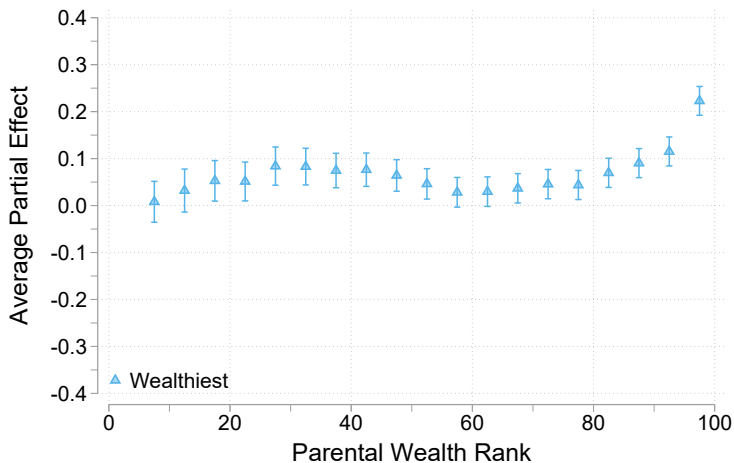
# The Non-Linear Effect of Parental Wealth for Wealthy: CI

[← back](#)

# The Non-Linear Effect of Parental Wealth for Wealthy: CI

[← back](#)

# The Non-Linear Effect of Parental Wealth for Wealthy: CI

[◀ back](#)

# Learn & Rise for Wealthy: CI

[◀ back](#)