

# The Macroeconomic Consequences of Subsistence Self-Employment

Juan Herreño<sup>†</sup>   Sergio Ocampo<sup>‡</sup>

<sup>†</sup>UC San Diego

<sup>‡</sup>University of Western Ontario

# Self-employment in developing countries

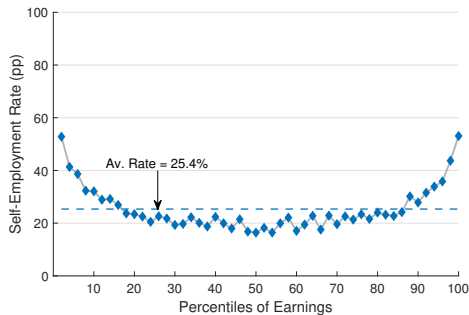
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Self-employment concentrated  
among the rich **and the poor**

(Data from 9 developing countries)

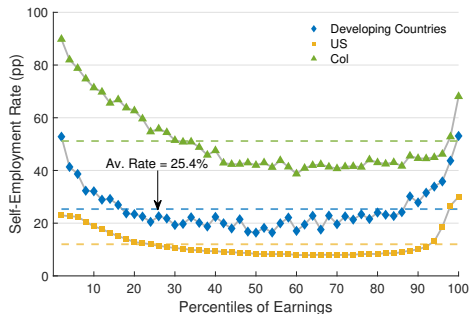


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## Policies aimed at the self-employed

- ▶ Grants, loans, transfers (varied designs and generosity)
- ▶ Policies meant to spur firm creation/growth but target the **self-employed** in practice
- ▶ Evidence of small effects on individual outcomes (income, firm creation, consumption)

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Effects of these policies (micro & macro) depend on many factors:

- ▶ Financial frictions affect occupational sorting (Buera, Kaboski, & Shin, 2015; Midrigan & Xu, 2014)
  - ▶ Self-employed choose worse technologies/smaller scale
- ▶ Subsistence concerns (Poshke, 2013; Breza, Kaur & Shamdashani, 2021)
  - ▶ Reflect labor rationing

## What we do

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  - ▶ Joint distribution of occupations and income
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  - ▶ Joint distribution of occupations and income
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3. Evaluate macro-effects of policies
  - 3.1 Micro loans and grants to the self-employed → loosen financial frictions
  - 3.2 Targeted transfers to the unemployed → insure labor risk

## What we find

1. Model consistent with joint distribution of occupations and income + labor market slack
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3. The (macro) elasticity of aggregate output to lending is **proportional** to the (micro) elasticity of individual self-employment income
  - ▶ The key is the muted response of wages to the reform (slack!)
  - ▶ TFP increases (loans improves selection into self-employment, only productive benefit)
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4. **Other Policies:** Generosity of the safety net to the unemployed is TFP enhancing (improves selection into self-employment **if well targeted**)

# Model

# A general equilibrium occupational choice model

- ▶ Heterogeneous agents:
  - ▶ Agents can be **Employed**, **Unemployed** or **Self-Employed**
  - ▶ Agents differ in Assets ( $a$ ), Idiosyncratic Productivity ( $z$ )

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  - ▶ Unemployed and Self-Employed have to wait for an **offer to become Employed**
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Similar structure adopted in Alves & Violante (2023) to study het. effects of monetary policy

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## Agents' problems

- ▶ Income of agents depends on occupation (wages, benefits, profits)
- ▶ Shocks also depend on occupations: Job offers to **U** and **SE** and job separations to **E**
  - ▶ All agents receive productivity shocks ( $z$ )

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Occupation	Flow Income ( $y$ )	Occupational Choice	Shocks	
Employed	$r \cdot a + w \cdot \epsilon(z)$	$U$ or $S$	$\gamma^z, \gamma^E$	← Job separation
Unemployed	$r \cdot a + b$	$S$	$\gamma^z, \gamma^U$	← Job offer
Self-employed	$r \cdot a + \pi(a, z)$	$U$	$\gamma^z, \gamma^S$	← Job offer
	$\uparrow$ $y^o(a, z)$		$\uparrow$ Prod.	

# Profits and value functions

## Self-employed profits:

$$\pi(a, z) = \max_{k \leq \lambda \cdot a, n} f(z, k, n) - (r + \delta) \cdot k - w \cdot n$$

- ▶ Collateral constraints depend on assets:  $k \leq \lambda \cdot a$

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## Value function for occupation $o \in \{E, U, S\}$ :

[details](#)

$$\rho V^o(a, z) = \max_{\text{s.t. } \underline{a} \leq a} u(c) + V_a^o \cdot \underbrace{(y^o(a, z) - c)}_{\dot{a}} + \frac{E[dV^o]}{dt}$$

- ▶ Standard Hamilton-Jacobi-Bellman formulation
- ▶ Change in value depends on savings:  $\dot{a} = y^o(a, z) - c$
- ▶ Last term captures productivity and occupational shocks

## Optimal choices

**Savings Choice,  $o \in \{E, U, S\}$ :**

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- Occ. choice defines regions  $\Omega^o \in \mathcal{S} \equiv [\underline{a}, \infty) \times \mathbb{R}_+$  where occupation 'o' prevails

$$\text{Example: } \Omega^U = \{(a, z) \in \mathcal{S} \mid V^U(a, z) > V^S(a, z)\}$$

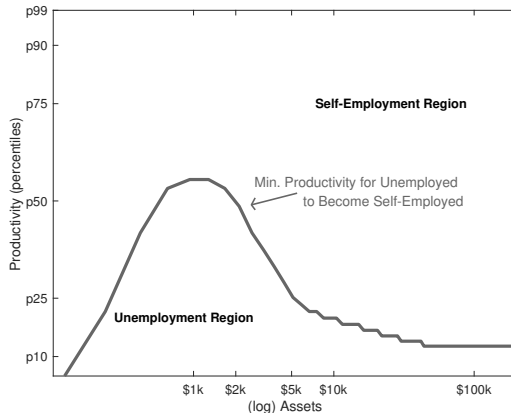
# (Stationary) Equilibrium

- ▶ Solve agents' problems given prices
  - ▶ Value functions solved as HJB variational inequalities.
- ▶ Small open economy:  $r = r^*$
- ▶ Wage ( $w$ ) clears labor market:
  - ▶ Labor demand firms of the self-employed:  $N^d = \int n^*(a, z) dG^S$
  - ▶ Labor supply from the employed:  $N^s = \int \epsilon(z) dG^E$
- ▶ Stationary distribution of agents:  $G^E, G^U, G^S$ 
  - ▶ Solve system of Kolmogorov-Forward-Equations
  - ▶ Reflects both exogenous shocks and endogenous occ. choice

details

# Main mechanism: Occupational choice

Toy model (intuition)



- ▶ (Min) Productivity threshold for self-employment
- ▶ Subsistence concerns: Low threshold for poor agents → Unproductive self-employed

# Calibration and Model Performance

## Parametrization

- ▶ Interest rate:  $r^* = 3\%$
- ▶ Collateral constraint:  $\lambda = 1.42$  to match debt-to-asset ratio of large Mexican firms
- ▶ Utility and production function:  $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$  and  $f(z, k, n) = z(k^\alpha n^{1-\alpha})^\nu$

$$\sigma = 2 \quad \alpha = 0.3 \quad \nu = 0.85$$

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## Internally calibrated parameters:

- ▶ Labor income is a function of productivity:  $\epsilon(z) = z^\eta$
- ▶ Shocks follow Poisson processes with arrival rates:  $\gamma^z, \gamma^E, \gamma^U, \gamma^S$
- ▶  $z$  discretized with transition matrix  $Pr^z(z'|z)$ 
  - ▶ Discretization from AR(1) process - Rowenhurst (1995) method

## Model performance: Targeted moments

Occupational Rates	Data	Model	Income Moments	Data	Model
Unemployment	4.4	4.1	$\text{std}(y_t^S)$	0.86	0.86
Self-employment	26.7	26.2	$\text{std}(y_t^E)$	0.54	0.58
Employment	69.1	69.7	$\text{corr}(y_t^S, y_{t+1}^S)$	0.59	0.59
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### Data from ENOE:

[sample details](#) [more moments](#)

- ▶ Household Survey - Quarterly rotating panel (up to 5 quarters)
- ▶ Information on labor status, search activities, transitions, and earnings
- ▶ **Key:** Observe transitions and earnings dynamics

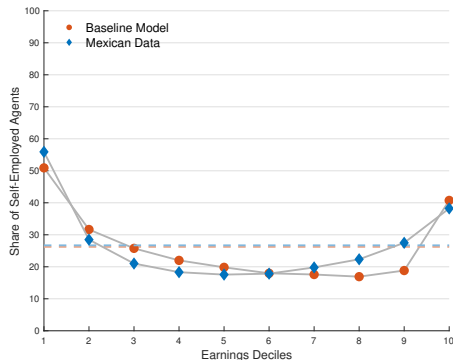


# Model performance: Untargeted moments

## 1. Model matches joint distribution of occupations and income

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## 2. Model matches reaction after labor demand shocks

- ▶ Development Literature on response of local labor market to labor demand shocks  
Imbert and Papp (2015), Breza, Kaur & Shamdasani (2021) and Muralidharan, Niehaus & Sukhtankar (2017)
- ▶ Low *elasticity of wages to labor demand*  $\left(\frac{\Delta \log w}{\Delta \log N} < 1\right)$ : self-employment “hides” slack
- ▶ Model elasticity  $\frac{\Delta \log w}{\Delta \log N} = 0.16$  (vs 1.6 with only financial frictions)
  - ▶ **Key:** Occupational transitions  $SE \rightarrow U$  rather than  $SE \rightarrow E$
  - ▶ Model also matches partial crowd-out of private labor demand from job-guarantee programs

# Credit Expansions Under Subsistence Self-Employment

# The effects of credit expansions

We increase access to credit by modifying borrowing constraint

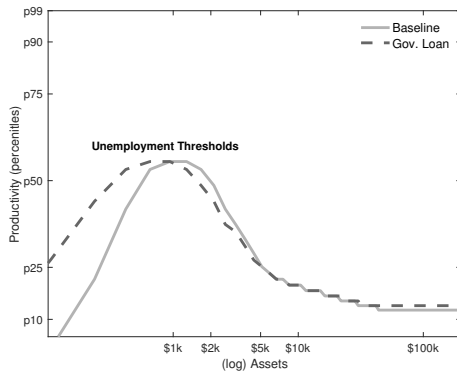
$$k \leq \lambda \cdot a + \phi$$

$\phi \approx \$540 \frac{\text{USD}}{\text{Q}}$  as in RCT loans from Compartamos Banco (Angelucci, Karlan, Zinman, 2015)

1. Contrast *micro* effects of loans on earnings with RCT evidence + Role of GE
2. Obtain *macro* effect on output and productivity by aggregating
3. Contrast effects with/without subsistence self-employment

## 1.1 Earnings effects of credit expansions

- ▶ Credit  $\uparrow$  20% and SE-earnings  $\uparrow$  0.95% in equilibrium  $\rightarrow$  (micro) elasticity of 0.048
  - ▶ Earnings up  $41 \frac{\text{USD}}{Q}$ , comparable with RCT result of  $55 \frac{\text{USD}}{Q}$  increase in business earnings
  - ▶ Level change “small” throughout the distribution but impacts occupational choice



## 1.2 General equilibrium effects of credit expansions

- ▶ **Key:** Muted response of wages, up only 0.06% (consistent with wage elasticity)
- ▶ Labor earnings increase 0.04 (composition effect from SE)
- ▶ Re-composition of labor force out of self-employment

Moment		Moment	
% $\Delta$ Wage	0.06	$\Delta$ Employment	0.08
% $\Delta$ Income(E)	0.04	$\Delta$ Unemployment	0.16
% $\Delta$ Income (S)	<b>0.95</b>	$\Delta$ Self-employment	<b>-0.24</b>

## 2. Aggregate effects of credit expansions

	Output	TFP	Assets	Consumption
% $\Delta$	0.20	0.15	-0.40	0.02

- ▶ (Macro) elasticity of output is proportional (micro) elasticity of income

$$\varepsilon_Y^{\text{macro}} = 0.011 = S \times \varepsilon_y^{\text{micro}}$$

- ▶ TFP increases due to selection **out of** self-employment
- ▶ *Insurance* from loans changes consumption/savings choices
  - ▶ Crowd-out private assets
  - ▶ Increase consumption... of the unemployed!  $\% \Delta(C^U) = 1.25$

### 3. The role of subsistence self-employment

Two economies without subsistence self-employment:

1. **No unemployment risk:**  $\gamma^E = 0$  and  $\gamma^U, \gamma^S \rightarrow \infty$

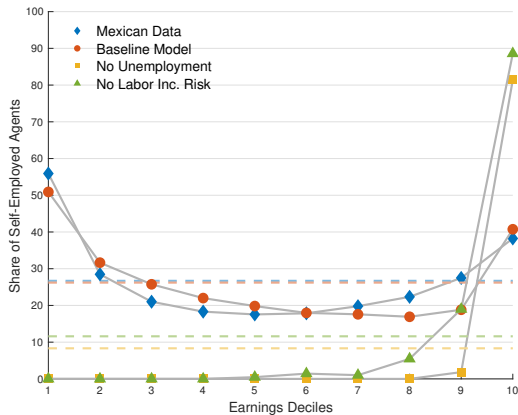
- ▶ Without unemployment risk occupational choice reflects productivity

2. **No labor-income risk:**  $\gamma^Z = 0$

- ▶ Without labor-income risk savings reflect presence of collateral constraint
- ▶ Recalibrate to match the same targets (when possible)
- ▶ Comparable to standard macro-development framework (e.g., Buera, Kaboski, Shin, 2020)



## Without unemployment risk self-employment concentrated at the top



- No subsistence-concerns  $\rightarrow$  self-employment selection based on  $a/z$

## Aggregate effects of credit without subsistence self-employment

	Baseline	No Unemp. Risk	No Labor Inc. Risk
Elasticities			
Output to credit supply	0.011	0.091	0.065
Wage to labor demand	0.16	0.36	2.32
Change in Variables (pp)			
Output	0.20	0.37	0.47
TFP	0.15	0.42	0.10
Wage	0.06	0.54	0.53
Self-employment	−0.24	0.07	0.05
Income (SE)	0.95	−0.38	−0.10
Assets	−0.40	−2.45	−2.14
Lending	20.00	4.03	7.27

# Policy Design and Subsistence Self-Employment

# The self-employed are sensitive to policy design

## Three examples

1. **Micro grants:** Subsidized version of loans above (common in practice; Meager, 2019)
2. **Transfers to the unemployed:** Common in many countries, can improve search (Acemoglu & Shimer, 1999, 2000; Chetty, 2008)
3. **Transfers to the non-employed:** Reflects limited implementation capacity (intuition extends to universal transfers)

## Micro grants - Negative selection

- ▶ Relaxation of collateral constraint  $k \leq \lambda a + \phi$  + Recipients pay 0 to rent capital
- ▶  $\phi$ : Ave. loan size of micro-credit interventions in Mexico Angelucci, Karlan, Zinman (2015)

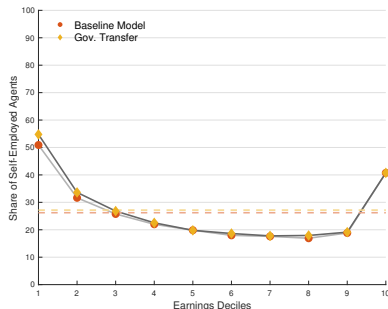
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### Policy effects:

occ. choice SE inc.

Moment	
$\Delta$ Employment	-0.24
$\Delta$ Unemployment	-0.72
$\Delta$ Self-employment	0.96
% $\Delta$ Wage	0.32
% $\Delta$ Income(E)	0.50
% $\Delta$ Income (S)	-2.40
% $\Delta$ TFP	-0.45



Decrease in  $z$  threshold for

self-employment

## Transfers to the unemployed - Subsistence concerns

The policy grants \$20 USD ( 10% of min wage) to the unemployed

$$y^U = r \cdot a + b + b_{UB}$$

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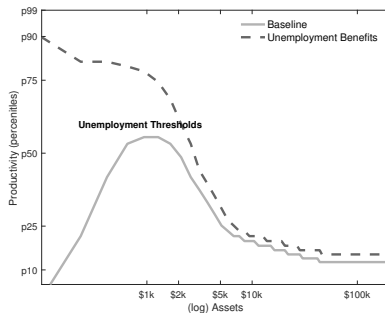
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occ. choice SE inc. SE prod.

Moment	
$\Delta$ Employment	0.06
$\Delta$ Unemployment	0.85
$\Delta$ Self-employment	-0.90
% $\Delta$ Wage	-0.16
% $\Delta$ Income(E)	-0.40
% $\Delta$ Income (S)	3.70
% $\Delta$ TFP	0.42



Increase in productivity selection



## Transfers to the non-employed - Back to negative selection

Hard to effectively target transfers to the unemployed

- Likely that transfers go to low-earning self-employed too

The policy grants \$20 USD to the unemployed + self-employed (income below minimum wage)

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	Output	TFP	Assets	Consumption
% $\Delta$	-0.04	-0.32	-1.90	-0.61

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- ▶ Transfers affect asset accumulation
- ▶ Occ. Choice: More self-employment
- ▶ Small micro effects on income distribution

occ. choice

SE inc.

# Conclusions

- ▶ High SE among the poor in developing economies
- ▶ Subsistence self-employment shapes economies response to shocks and policy
- ▶ Policies that alleviate subsistence concerns improve productivity
- ▶ Policies that target the self-employed can backfire

# Thank You

Please send your questions to

[juanherreno@ucsd.edu](mailto:juanherreno@ucsd.edu)

or

[socampod@uwo.ca](mailto:socampod@uwo.ca)

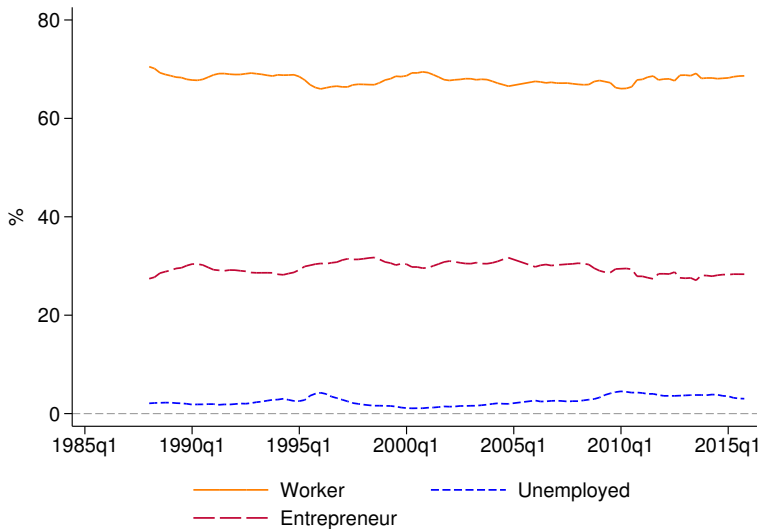
# Appendix

# Data Appendix

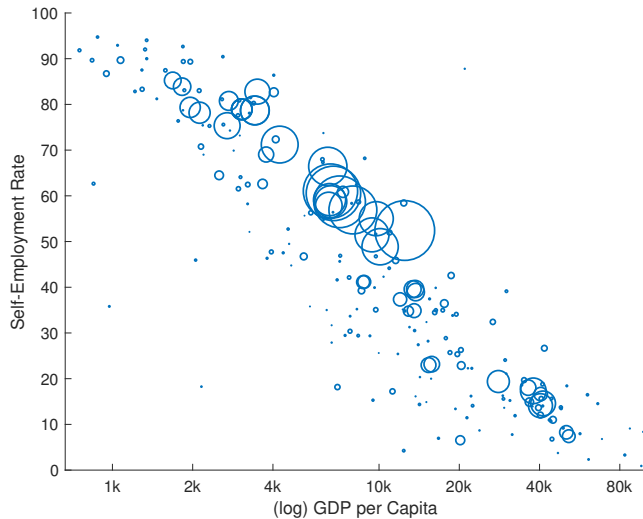
- ▶ Our Sample: 1995Q1 - 2015Q4.
  - ▶ Males, Head of households, Prime age workers (23 to 65)
  - ▶ Ten largest municipalities
  - ▶ Unbalanced panel for 250 thousand individuals ( 1m obs.)
- ▶ Labor Status (Self-Reported)
  - ▶ Employed: Has a job, has a supervisor
  - ▶ Unemployed: Does not have a job, is looking for one
  - ▶ Self-Employed: Has a job, reports to be his own employer



# Workforce composition in Mexico: Time series

[back](#)

# Self-employment across countries

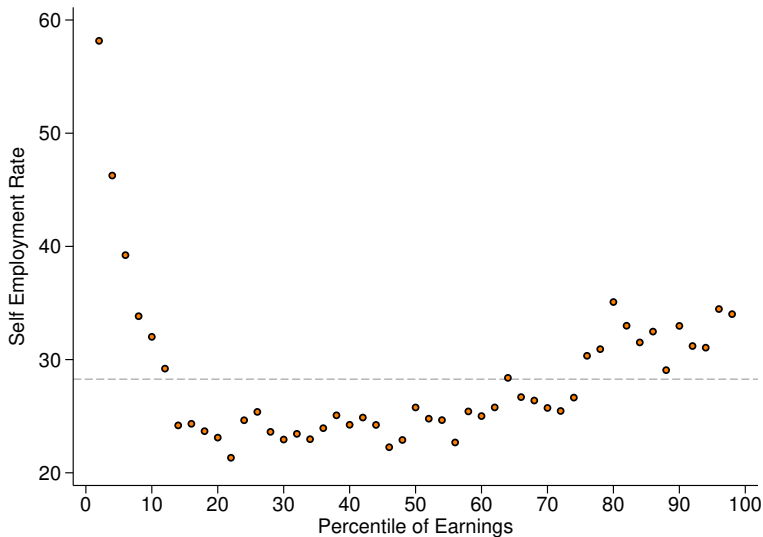
[back](#)

- ▶ Run a regression of the form:

$$\log(w_{i,t}) = \alpha + \gamma_t + \beta X_{i,t} + \eta_{i,t}$$

- ▶ Rank  $\hat{\eta}_{i,t}$  and classify them in bins of 3% of the sample
- ▶ Compute the statistics for each bin
- ▶ Results are robust to direct earnings comparison

# Self-employment and earnings distribution: Raw data

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# Model Appendix

## Agent's problem: Value functions

[back](#)

Employed agents:

$$\begin{aligned}\rho V^E(a, z) &= \max_c u(c) + V_a^E(a, z) \dot{a} + \gamma^E \left( V^U(a, z) - V^E(a, z) \right) \\ &\quad + \gamma^z \int \left( V^E(a, z') - V^E(a, z) \right) d\Pr^z(z'|z) \\ \text{s.t.} \quad \dot{a} &= w\epsilon(z) + ra - c, \quad a \geq \underline{a}.\end{aligned}$$

Unemployed and Self-employed agents,  $o \in \{U, S\}$ :

$$\begin{aligned}\rho V^o(a, z) &= \max_c u(c) + V_a^o(a, z) \dot{a} + \gamma^o \max \left\{ V^E(a, z, \epsilon) - V^o(a, z), 0 \right\} \\ &\quad + \gamma^z \int \left( V^o(a, z') - V^o(a, z) \right) d\Pr^z(z'|z) \\ \text{s.t.} \quad \dot{a} &= b\mathbb{1}_{o=U} + \pi(a, z)\mathbb{1}_{o=S} + ra - c, \quad a \geq \underline{a}.\end{aligned}$$

## Agent's distribution: Kolmogorov Forward Equations

[back](#)

- Characterize stationary distributions  $\{G^o\}_{o \in \{E, U, S\}}$  by their densities  $\{g^o\}_{o \in \{E, U, S\}}$

$$0 = -\frac{\partial}{\partial a} \left[ \dot{a} g^E(a, z) \right] - \left( \gamma^E + \gamma^z \right) g^E(a, z) \quad \leftarrow \text{Holds for } (a, z) \in \Omega^E$$
$$+ \gamma^z \int \text{Pr}^z(z|z') g^E(a, z') dz' + \gamma^U g^U(a, z) + \gamma^S g^S(a, z) \mathbb{1}_{\{(a, z) \in \Omega^E\}}$$

$$0 = -\frac{\partial}{\partial a} \left[ \dot{a} g^U(a, z) \right] - \left( \gamma^U + \gamma^z \right) g^U(a, z) \quad \leftarrow \text{Holds for } (a, z) \in \Omega^U$$
$$+ \gamma^z \int \text{Pr}^z(z|z') g^U(a, z') dz' + \gamma^E g^E(a, z),$$

$$0 = -\frac{\partial}{\partial a} \left[ \dot{a} g^S(a, z) \right] - \left( \gamma^S \mathbb{1}_{\{(a, z) \in \Omega^E\}} + \gamma^z \right) g^S(a, z) \quad \leftarrow \text{Holds for } (a, z) \notin \Omega^U$$
$$+ \gamma^z \int \text{Pr}^z(z|z') g^S(a, z') dz' + \gamma^E g^E(a, z) \mathbb{1}_{\{(a, z) \notin \Omega^U\}},$$

## Model performance: Untargeted moments

[back](#)

### Occupational Transition Rates

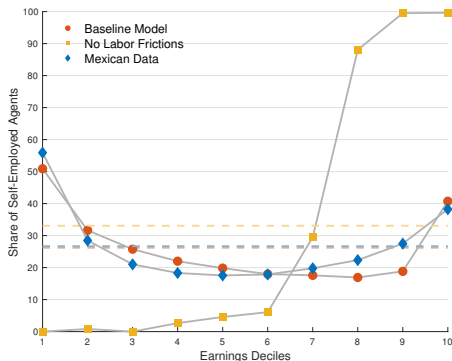
	Data	Model		Data	Model		Data	Model
$U \rightarrow U$	27.4	29.3	$S \rightarrow U$	1.9	4.6	$E \rightarrow U$	3.1	2.5
$U \rightarrow S$	14.6	23.6	$S \rightarrow S$	76.8	62.2	$E \rightarrow S$	8.1	12.8
$U \rightarrow E$	58.0	47.1	$S \rightarrow E$	21.3	33.1	$E \rightarrow E$	88.8	84.7

### Income Moments

	Data	Model		Data	Model
$\text{corr}(y_t^E, y_{t+1}^S)$	0.43	0.39	$\text{corr}(y_t^S, y_{t+1}^E)$	0.43	0.34



# Model Performance: The role of labor vs financial frictions

[back](#)

- ▶ Model without labor frictions misses Self-employment *out-of-necessity*
- ▶ There is also no unemployment risk for employed agents
- ▶ Self-employment is only taken by agents who can generate higher profits than wages

# Toy Model Appendix

# Selection into self-employment

[back 1](#)[back 2](#)

**Static Model** Continuum of unemployed ( $U$ ) agents

- ▶ Choose to stay unemployed ( $U$ ) or become self-employed ( $SE$ )
- ▶ Heterogeneity: Assets ( $a$ ) and productivity ( $z$ )
- ▶ CRRA utility:  $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$

# Selection into self-employment

[back 1](#)[back 2](#)

**Static Model** Continuum of unemployed ( $U$ ) agents

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## Unemployment

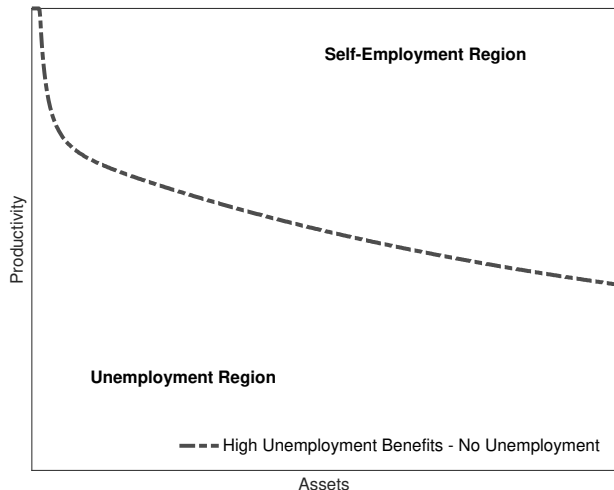
- ▶  $U$  get a job with probability  $p$
- ▶ If employed, consume:  $a + w$
- ▶ If not, consume:  $a + b$

## Self-Employment

- ▶  $SE$  produce using own assets
- ▶ Consume:  $a + za^\alpha$

Mechanisms behind policies depend on **selection into self-employment**

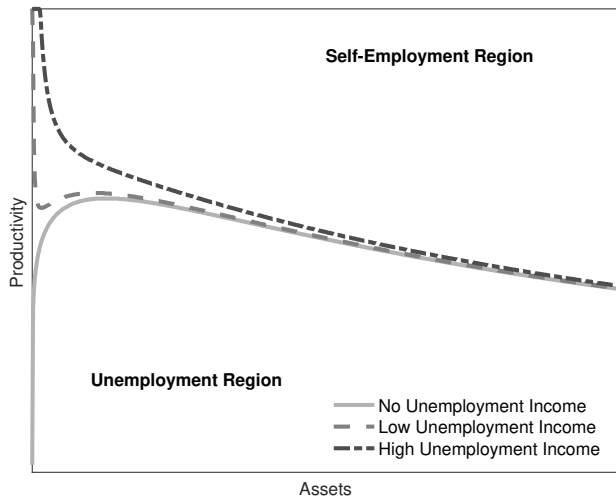
# Self-employment as an outside option to employment

[back 1](#)[back 2](#)

High unemployment benefits ( $b$ ) or  
no unemployment ( $p = 1$ )

- ▶ “Positive” selection to SE
- ▶ Productive/Wealthy agents
- ▶ No low-earning SE

# Self-employment as an outside option to unemployment

[back 1](#)[back 2](#)

Selection breaks for resource constrained agents:

- ▶ Poor + Unemployed

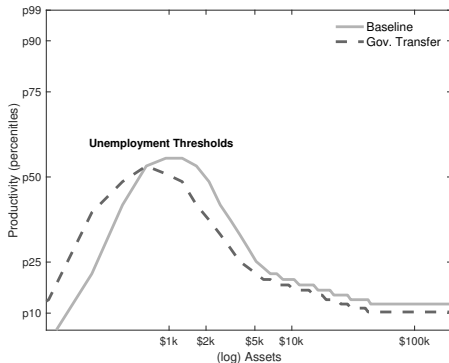
- Unproductive SE

- Low-earning SE

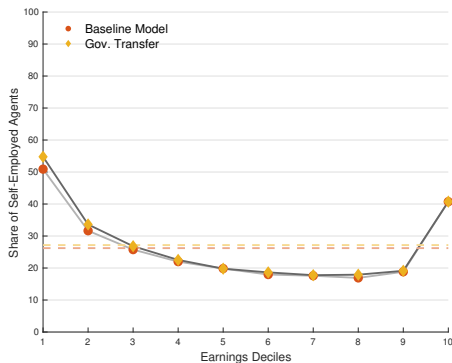
- ▶ Large share of SE if lots of poor/constrained agents

# Policy Appendix

# Micro Transfers - Occupational Choices

[back](#)

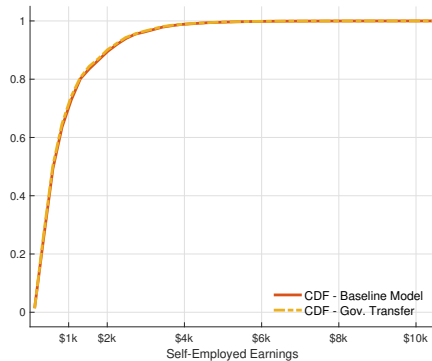
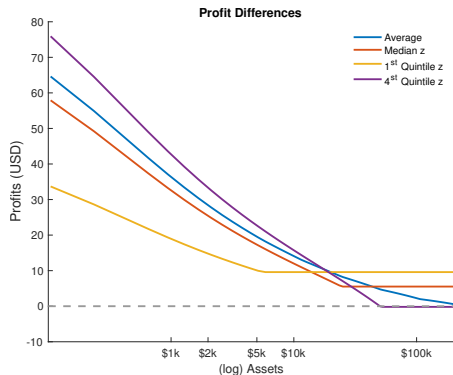
Some changes in thresholds



Small effects across distribution of income



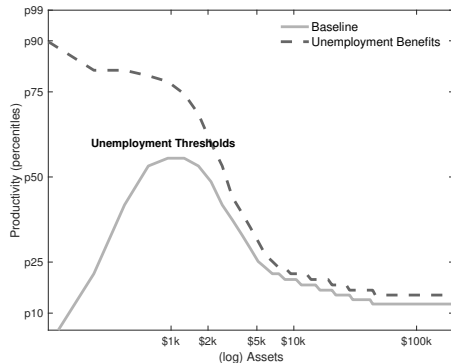
# Micro Transfers - Self-Employment Income

[back](#)

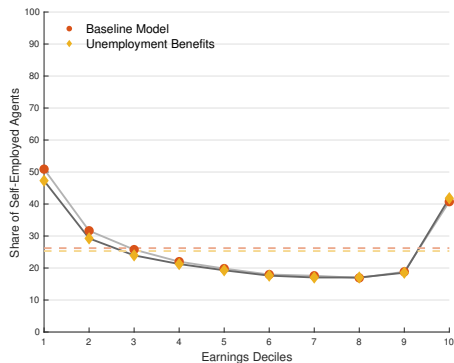
Small profit gains to poor & productive

Negligible effects in the distribution

# Unemployment benefits - Occupational Choices

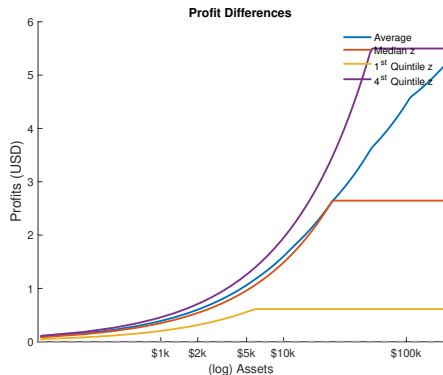
[back](#)

Increase in productivity selection

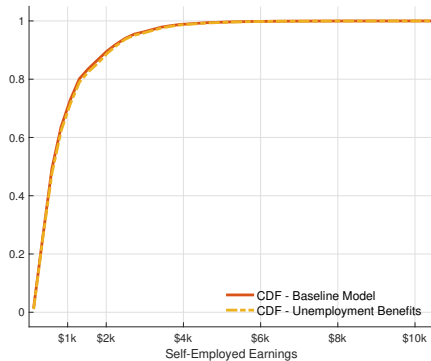


Lower mass of low-earning SE

# Unemployment benefits - Self-Employment Income

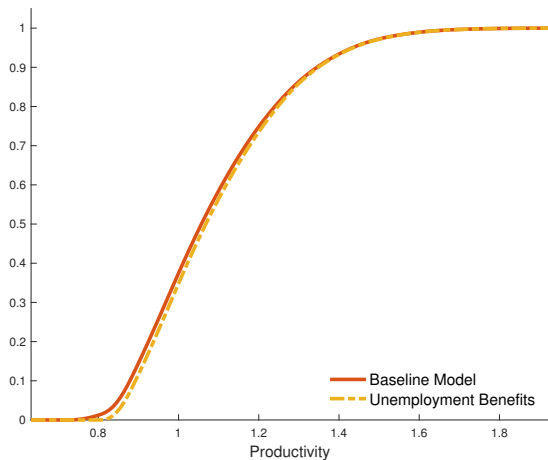
[back](#)

Productive SE take advantage of  $w \downarrow$



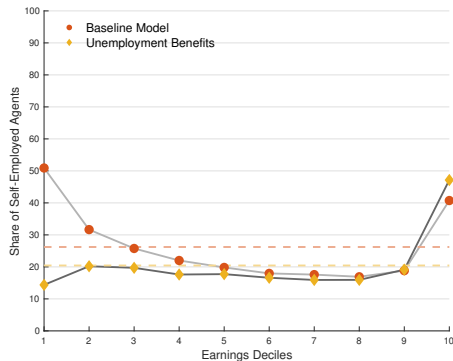
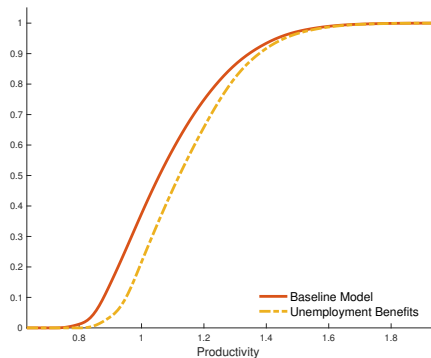
Noticeable effects on earnings

# Unemployment benefits - Productivity Distribution

[back](#)

Change in selection improves productivity

# Unemployment Benefits: Self-employment $\downarrow$ among the poor

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## Unemployment benefits: productivity $\uparrow$ , unemployment $\uparrow$

[back](#)

Moment	GE	Moment	GE
% $\Delta$ Wage	-2.0	$\Delta$ Employment	0.46
% $\Delta$ Output	-2.3	$\Delta$ Self-employment	-5.8
% $\Delta$ TFP	<b>2.9</b>	$\Delta$ Unemployment	<b>5.1</b>

## Credit Deepening: Relaxing Collateral Constraints

- ▶ Financial frictions prevent self-employed to produce at optimal scale
- ▶ Capture financial reform as credit deepening

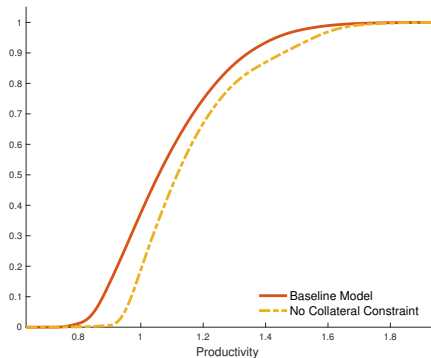
$$k \leq (\lambda + \lambda_{CD}) \cdot a$$

Two exercises:

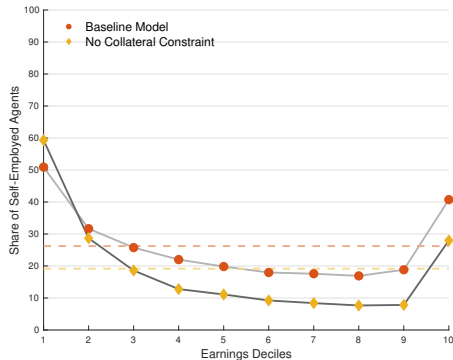
1. Relaxed collateral constraint:  $\lambda_{CD} > 0$  (In paper)
2. No collateral constraint:  $\lambda_{CD} \rightarrow \infty$

more

## Elimination of Collateral Constraints: $\lambda_{CD} \rightarrow \infty$



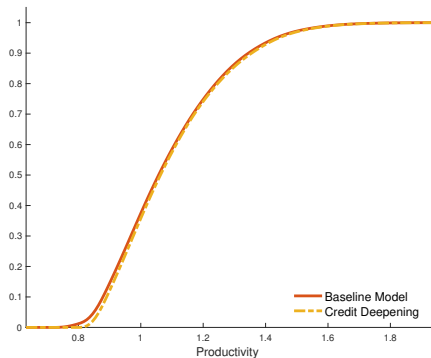
Productivity distribution improves  
TFP  $\uparrow$  11%



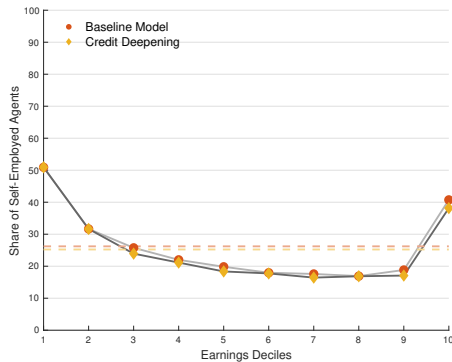
SE  $\downarrow$  bc strong GE effects: wages  $\uparrow$   
Subsistence concerns remain [more](#)



## Credit Deepening: $\lambda_{CD} > 0$

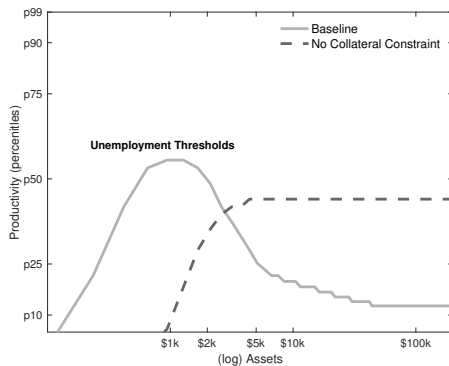
[back](#)

Productivity distribution improves



SE ↓ because wages ↑  
(subsistence SE persists)

# Elimination of Collateral Constraints

[back](#)

Does not solve occupational choices at the bottom

## Transfers to the self-employed

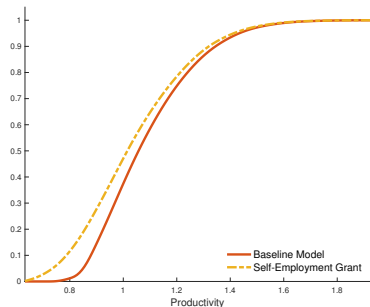
Transfers of 17% of labor incomes to the lowest 10% Banerjee, Niehaus, and Suri (2019)

$$y^S = r \cdot a + \pi(a, z) + b_{MG} \mathbb{1}_{MG}$$

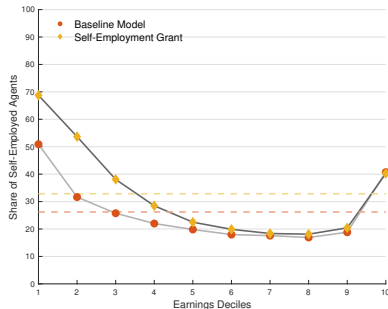
# Transfers to the self-employed

Transfers of 17% of labor incomes to the lowest 10% Banerjee, Niehaus, and Suri (2019)

$$y^S = r \cdot a + \pi(a, z) + b_{MG} \mathbb{1}_{MG}$$



Productivity distribution worsens (FOSD)



Self-employment ↑ among the poor  
(productive SE do not benefit)

## Transfers to the self-employed

Moment	GE	Moment	GE
% $\Delta$ Wage	1.0	$\Delta$ Employment	-2.5
% $\Delta$ Output	-2.4	$\Delta$ Self-employment	<b>6.6</b>
% $\Delta$ TFP	<b>-2.5</b>	$\Delta$ Unemployment	<b>-4.1</b>

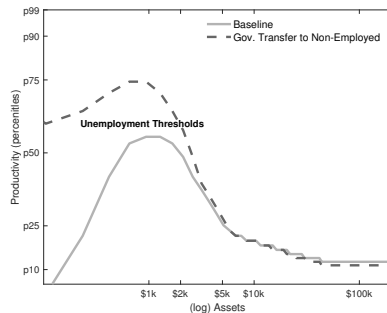
- ▶ Transfers heavily influence occupational choice
- ▶ Unemployed agents prefer self-employment regardless of productivity
- ▶ Aggregate productivity decreases as a result

# Transfers to the non-employed: Occupational choice

[back](#)

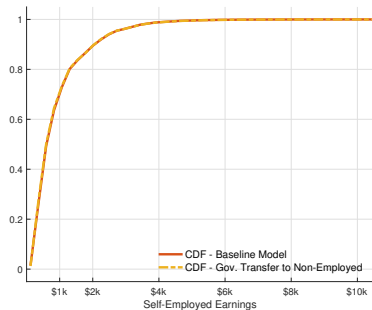
## Policy effects:

Moment		
$\Delta$ Employment	-0.22	
$\Delta$ Unemployment	-0.14	
$\Delta$ Self-employment	<b>0.36</b>	
% $\Delta$ Wage	-0.04	
% $\Delta$ Income(E)	-0.22	
% $\Delta$ Income (S)	<b>-1.40</b>	

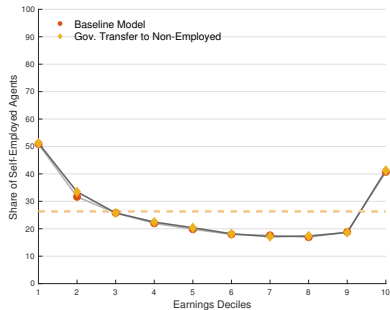


Increase in productivity selection

# Transfers to the non-employed: Self-employed income

[back](#)

Increase in productivity selection



Increase in productivity selection