

The Macroeconomic Consequences of Subsistence Self-Employment

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Self-employment in developing countries

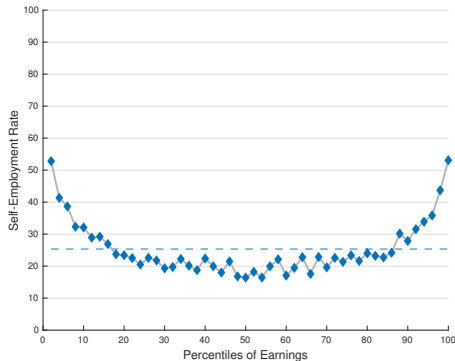
- ▶ High **self-employment rates** in developing countries (Poshke, 2019)
- ▶ High prevalence of *subsistence entrepreneurship* (Schoar, 2010)

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Self-employment concentrated
among the rich **and the poor**

(Data from 9 developing countries)



Policies aimed at the self-employed

- ▶ Grants, loans, transfers (varied designs and generosity)
- ▶ Policies meant to spur firm creation/growth but target the **self-employed** in practice
- ▶ Evidence of small effects on individual outcomes (income, firm creation, consumption)

(Angelucci, Karlan, & Zinman, 2015; Banerjee, Duflo, Glennerster, & Kinnan, 2015; Maeger, 2019)

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Effects of these policies (micro & macro) depend on many factors:

- ▶ Financial frictions affect occupational sorting (Buera, Kaboski, & Shin, 2015; Midrigan & Xu, 2014)
 - ▶ Self-employed choose worse technologies/smaller scale
- ▶ Subsistence concerns (Poshke, 2013; Breza, Kaur & Shamdashani, 2021)
 - ▶ Reflect labor rationing

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1. Study the effects of development policies when subsistence entrepreneurship is prevalent
 - ▶ Heterogeneous agents macro-development model
 - ▶ Financial and subsistence concerns (labor market frictions) driving occupational choices

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 - ▶ Joint distribution of occupations and income
 - ▶ Labor market response to labor demand shocks

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2. Use a set of cross-sectional moments to evaluate importance of subsistence concerns
 - ▶ Joint distribution of occupations and income
 - ▶ Labor market response to labor demand shocks
3. Evaluate macro-effects of policies
 - 3.1 Micro loans and grants to the self-employed (loosen financial frictions)
 - 3.2 Targeted transfers to the unemployed (insure labor risk)

What we find

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 - ▶ Hard to reject null effects with micro data (occ. choices, income, consumption)
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 - ▶ **Grants:** Negative TFP effects (increases scale of unproductive firms)
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4. Generosity of the safety net to the unemployed is TFP enhancing
(increases selection into self-employment)

Model

A general equilibrium occupational choice model

- ▶ Heterogeneous agents:
 - ▶ Agents can be **Employed**, **Unemployed** or **Self-Employed**
 - ▶ Agents differ in Assets (a), Idiosyncratic Productivity (z)

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Agents' problems

- ▶ Income of agents depends on occupation (wages, benefits, profits)
- ▶ Shocks also depend on occupations: Job offers to **U** and **SE** and job separations to **E**
 - ▶ All agents receive productivity shocks (z)

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Occupation	Flow Income (y)	Occupational Choice	Shocks	
Employed	$r \cdot a + w \cdot \epsilon(z)$	U or S	γ^z, γ^E	← Job separation
Unemployed	$r \cdot a + b$	S	γ^z, γ^U	← Job offer
Self-employed	$r \cdot a + \pi(a, z)$	U	γ^z, γ^S	← Job offer
	\uparrow $y^o(a, z)$		\uparrow Prod.	

Profits and value functions

Self-employed profits:

$$\pi(a, z) = \max_{k \leq \lambda \cdot a, n} f(z, k, n) - (r + \delta) \cdot k - w \cdot n$$

- ▶ Collateral constraints depend on assets: $k \leq \lambda \cdot a$

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Value function for occupation $o \in \{E, U, S\}$:

[details](#)

$$\rho V^o(a, z) = \max_{\text{s.t. } \underline{a} \leq a} u(c) + V_a^o \cdot \underbrace{(y^o(a, z) - c)}_{\dot{a}} + \frac{E[dV^o]}{dt}$$

- ▶ Standard Hamilton-Jacobi-Bellman formulation
- ▶ Change in value depends on savings: $\dot{a} = y^o(a, z) - c$
- ▶ Last term captures productivity and occupational shocks

Optimal choices

Savings Choice, $o \in \{E, U, S\}$:

$$c^o(a, z) = u'^{-1}(V_a^o(a, z))$$

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Occupational Choice:

Agents can move freely to unemployment or self-employment so

$$V^E(a, z) \geq \max \{ V^U(a, z), V^S(a, z) \}$$

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$$V^S(a, z) \geq V^U(a, z)$$

- Occ. choice defines regions $\Omega^o \in \mathcal{S} \equiv [\underline{a}, \infty) \times \mathbb{R}_+$ where occupation 'o' prevails

$$\text{Example: } \Omega^U = \{ (a, z) \in \mathcal{S} \mid V^U(a, z) > V^S(a, z) \}$$

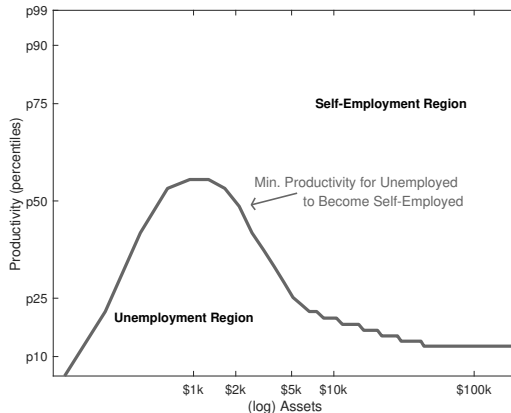
(Stationary) Equilibrium

- ▶ Solve agents' problems given prices
 - ▶ Value functions solved as HJB variational inequalities.
- ▶ Small open economy: $r = r^*$
- ▶ Wage (w) clears labor market:
 - ▶ Labor demand firms of the self-employed: $N^d = \int n^*(a, z) dG^S$
 - ▶ Labor supply from the employed: $N^s = \int \epsilon(z) dG^E$
- ▶ Stationary distribution of agents: G^E, G^U, G^S
 - ▶ Solve system of Kolmogorov-Forward-Equations
 - ▶ Reflects both exogenous shocks and endogenous occ. choice

details

Main mechanism: Occupational choice

Toy model (intuition)



- ▶ (Min) Productivity threshold for self-employment
- ▶ Subsistence concerns: Low threshold for poor agents → Unproductive self-employed

Calibration and Model Performance

Parametrization

- ▶ Interest rate: $r^* = 3\%$
- ▶ Collateral constraint: $\lambda = 1.42$ to match debt-to-asset ratio of large Mexican firms
- ▶ Utility and production function: $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$ and $f(z, k, n) = z(k^\alpha n^{1-\alpha})^\nu$

$$\sigma = 2 \quad \alpha = 0.3 \quad \nu = 0.85$$

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Internally calibrated parameters:

- ▶ Labor income is a function of productivity: $\epsilon(z) = z^\eta$
- ▶ Shocks follow Poisson processes with arrival rates: $\gamma^z, \gamma^E, \gamma^U, \gamma^S$
- ▶ z discretized with transition matrix $Pr^z(z'|z)$
 - ▶ Discretization from AR(1) process - Rowenhurst (1995) method

Model performance: Targeted moments

Occupational Rates	Data	Model	Income Moments	Data	Model
Unemployment	4.4	4.1	$\text{std}(y_t^S)$	0.86	0.86
Self-employment	26.7	26.2	$\text{std}(y_t^E)$	0.54	0.58
Employment	69.1	69.7	$\text{corr}(y_t^S, y_{t+1}^S)$	0.59	0.59
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Data from ENOE:

[sample details](#) [more moments](#)

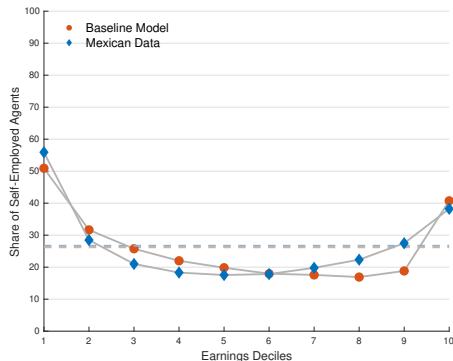
- ▶ Household Survey - Quarterly rotating panel (up to 5 quarters)
- ▶ Information on labor status, search activities, transitions, and earnings
- ▶ **Key:** Observe transitions and earnings dynamics

Model performance: Untargeted moments

1. Joint distribution of occupations and income

- ▶ Model matches profile of self-employment across earnings
 - ▶ **Key:** Subsistence concerns of the unemployed → Occupational Choice
- ▶ Model with only financial frictions fails in doing so

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2. Reaction after labor demand shocks

- ▶ Dev. Literature on response of local labor market to labor demand shocks

Imbert and Papp (2015), Breza, Kaur & Shamdasani (2021) and Muralidharan, Niehaus & Sukhtankar (2017)
- ▶ Low response of wages $\left(\frac{\Delta \log w}{\Delta \log N} < 1\right)$: self-employment “hides” slack
- ▶ Model simulation $\frac{\Delta \log w}{\Delta \log N} = 0.16$ (vs 1.6 with only financial frictions)
 - ▶ **Key:** Occupational transitions $SE \rightarrow U$ rather than $SE \rightarrow E$

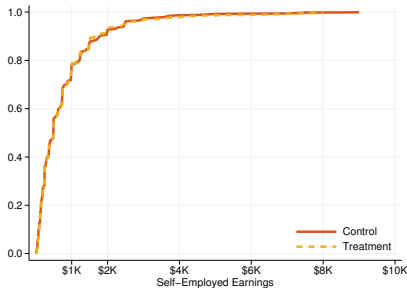
Development Policies

What are the (macro) effects of policies aimed at self-employed?

- ▶ Literature finds overall small effects of micro-credit programs on individuals
 - ▶ Angelucci, Karlan, Zinman (2015): “small effects on 37 outcomes” from loans to women entrepreneurs in Mexico
 - ▶ Loans have high interest rates (110 APR) and group liability (10-50 women per group)
 - ▶ Maeger (2019): “the impact on household business and consumption variables is unlikely to be transformative and may be negligible”
 - ▶ Meta-study (Bosnia, Ethiopia, India, Mexico, Mongolia, Morocco and The Philippines)
 - ▶ Varied conditions (13% to 100% APR, individual or group liability, rural or urban, women and men, collateralized or not)

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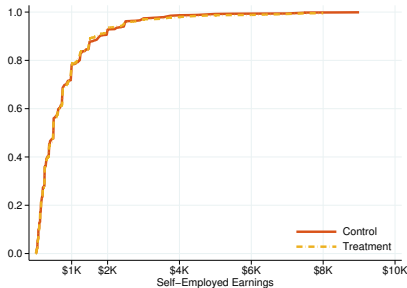
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- ▶ Effects of a \$540 dollar loan on business income
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Objective:

1. Can the model match the muted effects at the micro-level?
2. Test macro effects of policies using the model

Policy design

1. **Micro-Loans:** Credit lines of around USD \$500 to rent physical capital
2. **Micro-Grants:** Zero interest lease of around USD \$500 of physical capital
3. **Transfers to Unemployed:** Transfer of around USD \$20 to unemployed individuals

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-
1. Do small micro effects imply negligible macro effects?
 2. How does design of policy affect micro vs macro effects?

Micro Loans

- ▶ Relaxation of collateral constraint $k \leq \lambda a + \underline{\lambda}$
- ▶ Policy is self-financed. Recipients pay $(r + \delta)$ to rent capital
- ▶ $\underline{\lambda}$: Ave. loan size of micro-credit interventions in Mexico Angelucci, Karlan, Zinman (2015)

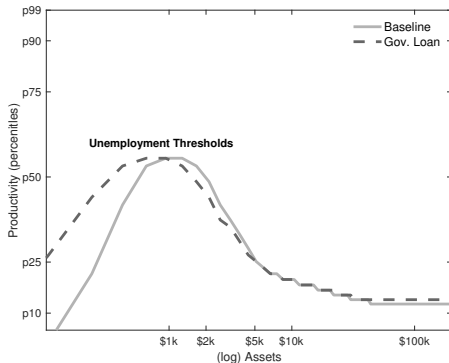
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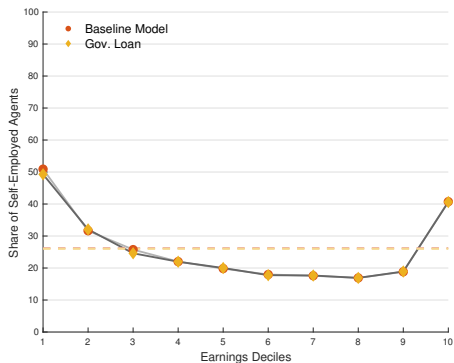
Policy effects:

Moment		Moment	
% Δ Wage	0.06	Δ Employment	0.08
% Δ Income(E)	0.04	Δ Unemployment	0.16
% Δ Income (S)	0.95	Δ Self-employment	-0.24

Micro Loans - Occupational Choices

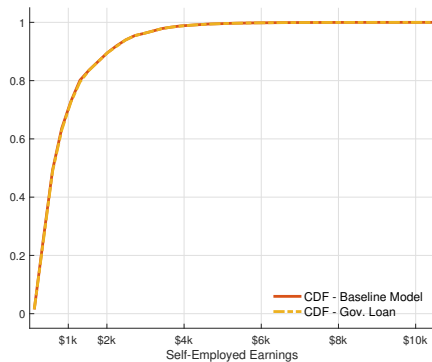


Some changes in thresholds



Small effects across distribution of income

Micro Loans - Self-Employment Income



Negligible effects in the distribution

Micro Loans - Aggregate effects are non-negligible

	Output	TFP	Assets	Consumption
% Δ	0.20	0.15	-0.40	0.02

- ▶ Small changes in selection into SE \rightarrow Effects in agg. TFP
- ▶ Decrease in assets from insurance effect of loans (loosen collateral constraint)
- ▶ Heterogeneity in consumption effects, e.g., $\% \Delta(C^U) = 1.25$
- ▶ Small welfare gains for poor agents 0.1pp

Micro Grants

- ▶ Relaxation of collateral constraint $k \leq \lambda a + \underline{\lambda}$ + Recipients pay 0 to rent capital
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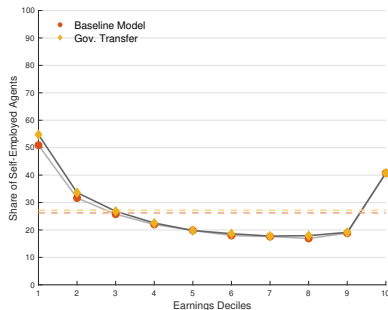
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Policy effects:

occ. choice SE inc.

Moment	
Δ Employment	-0.24
Δ Unemployment	-0.72
Δ Self-employment	0.96
% Δ Wage	0.32
% Δ Income(E)	0.50
% Δ Income (S)	-2.40



Decrease in threshold

Micro Grants - Aggregate effects are non-negligible

	Output	TFP	Assets	Consumption
% Δ	0.23	-0.45	-1.11	0.15

- ▶ Small changes in selection into SE \rightarrow Effects in agg. TFP
- ▶ Decrease in assets from insurance effect of loans (loosen collateral constraint)
- ▶ Heterogeneity in consumption effects, e.g., $\% \Delta(C^U) = -2.38$
- ▶ Small but broad welfare gains 0.7pp

Transfers to the unemployed

The policy grants \$20 USD (10% of min wage) to the unemployed (Similar to Δ in profits from other policies)

$$y^U = r \cdot a + b + b_{UB}$$

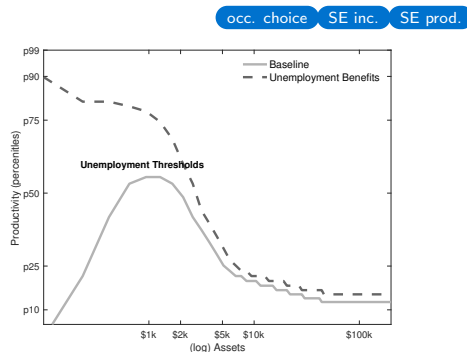
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Moment	
Δ Employment	0.06
Δ Unemployment	0.85
Δ Self-employment	-0.90
% Δ Wage	-0.16
% Δ Income(E)	-0.40
% Δ Income (S)	3.70



Increase in productivity selection

Transfers to the unemployed - Aggregate effects are non-negligible

	Output	TFP	Assets	Consumption
% Δ	0.25	0.42	-0.52	-0.26

- ▶ Changes in selection into SE \rightarrow Increase aggregate TFP
- ▶ Decrease in assets from insurance effect of payments
- ▶ Heterogeneity in consumption effects, e.g., $\% \Delta(C^U) = 3.95$
- ▶ Small welfare losses (0.9pp) due to lower (after-tax) wages

generosity

Transfers to the non-employed

Hard to effectively target transfers to the unemployed

- Likely that transfers go to low-earning self-employed too

The policy grants \$20 USD to the unemployed + self-employed (income below minimum wage)

$$y^U = r \cdot a + b + b_{UB} \quad y^S = r \cdot a + \pi + b_{UB}$$

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% Δ	-0.04	-0.32	-1.90	-0.61

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	Output	TFP	Assets	Consumption
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- ▶ Transfers affect asset accumulation
- ▶ Occ. Choice: More self-employment
- ▶ Small micro effects on income distribution

occ. choice

SE inc.

Conclusions

- ▶ High SE among the poor in developing economies
- ▶ Subsistence self-employment shapes economies response to shocks and policy
- ▶ Policies that alleviate subsistence concerns improve productivity
- ▶ Policies that target the self-employed can backfire

Thank You

Please send your questions to

juanherreno@ucsd.edu

or

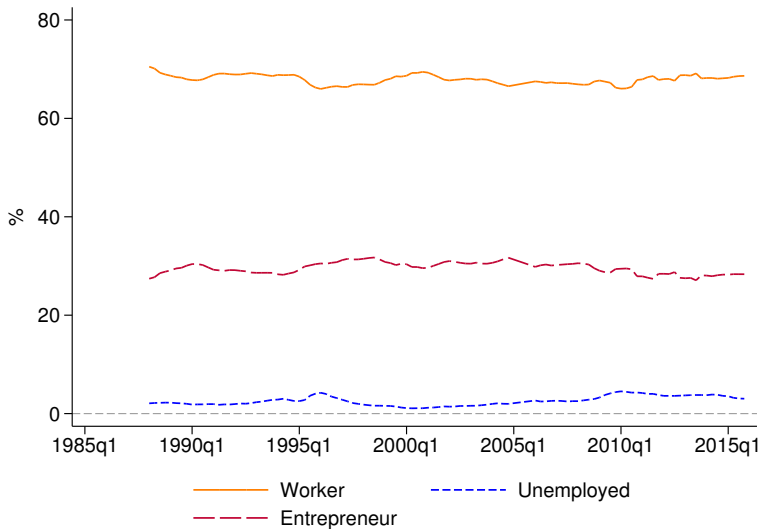
socampod@uwo.ca

Appendix

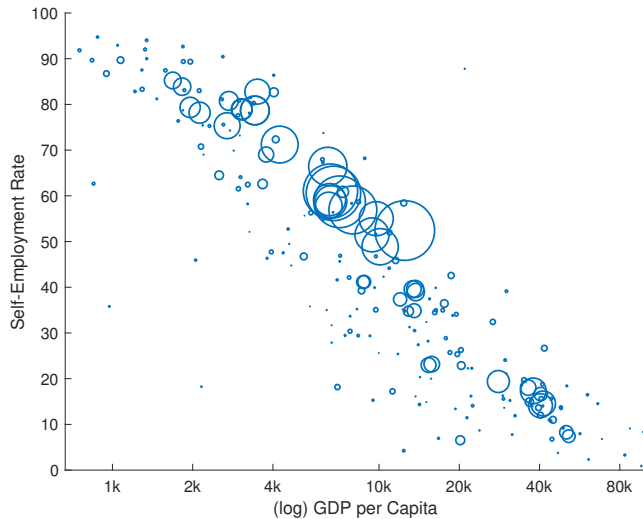
Data Appendix

- ▶ Our Sample: 1995Q1 - 2015Q4.
 - ▶ Males, Head of households, Prime age workers (23 to 65)
 - ▶ Ten largest municipalities
 - ▶ Unbalanced panel for 250 thousand individuals (1m obs.)
- ▶ Labor Status (Self-Reported)
 - ▶ Employed: Has a job, has a supervisor
 - ▶ Unemployed: Does not have a job, is looking for one
 - ▶ Self-Employed: Has a job, reports to be his own employer

Workforce composition in Mexico: Time series

[back](#)

Self-employment across countries

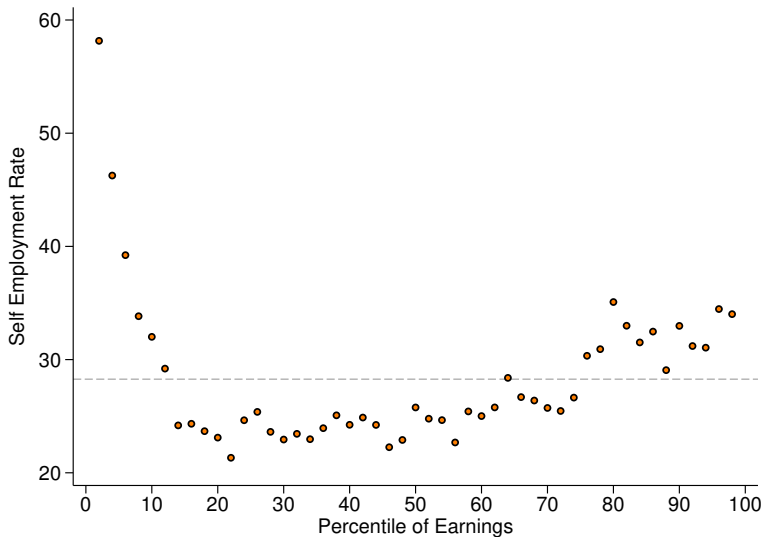
[back](#)

- ▶ Run a regression of the form:

$$\log(w_{i,t}) = \alpha + \gamma_t + \beta X_{i,t} + \eta_{i,t}$$

- ▶ Rank $\hat{\eta}_{i,t}$ and classify them in bins of 3% of the sample
- ▶ Compute the statistics for each bin
- ▶ Results are robust to direct earnings comparison

Self-employment and earnings distribution: Raw data

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Model Appendix

Agent's problem: Value functions

[back](#)

Employed agents:

$$\begin{aligned}\rho V^E(a, z) &= \max_c u(c) + V_a^E(a, z) \dot{a} + \gamma^E \left(V^U(a, z) - V^E(a, z) \right) \\ &\quad + \gamma^z \int \left(V^E(a, z') - V^E(a, z) \right) d\Pr^z(z'|z) \\ \text{s.t.} \quad \dot{a} &= w\epsilon(z) + ra - c, \quad a \geq \underline{a}.\end{aligned}$$

Unemployed and Self-employed agents, $o \in \{U, S\}$:

$$\begin{aligned}\rho V^o(a, z) &= \max_c u(c) + V_a^o(a, z) \dot{a} + \gamma^o \max \left\{ V^E(a, z, \epsilon) - V^o(a, z), 0 \right\} \\ &\quad + \gamma^z \int \left(V^o(a, z') - V^o(a, z) \right) d\Pr^z(z'|z) \\ \text{s.t.} \quad \dot{a} &= b\mathbb{1}_{o=U} + \pi(a, z)\mathbb{1}_{o=S} + ra - c, \quad a \geq \underline{a}.\end{aligned}$$

Agent's distribution: Kolmogorov Forward Equations

[back](#)

- Characterize stationary distributions $\{G^o\}_{o \in \{E, U, S\}}$ by their densities $\{g^o\}_{o \in \{E, U, S\}}$

$$0 = -\frac{\partial}{\partial a} \left[\dot{a} g^E(a, z) \right] - \left(\gamma^E + \gamma^z \right) g^E(a, z) \quad \leftarrow \text{Holds for } (a, z) \in \Omega^E$$
$$+ \gamma^z \int \text{Pr}^z(z|z') g^E(a, z') dz' + \gamma^U g^U(a, z) + \gamma^S g^S(a, z) \mathbb{1}_{\{(a, z) \in \Omega^E\}}$$

$$0 = -\frac{\partial}{\partial a} \left[\dot{a} g^U(a, z) \right] - \left(\gamma^U + \gamma^z \right) g^U(a, z) \quad \leftarrow \text{Holds for } (a, z) \in \Omega^U$$
$$+ \gamma^z \int \text{Pr}^z(z|z') g^U(a, z') dz' + \gamma^E g^E(a, z),$$

$$0 = -\frac{\partial}{\partial a} \left[\dot{a} g^S(a, z) \right] - \left(\gamma^S \mathbb{1}_{\{(a, z) \in \Omega^E\}} + \gamma^z \right) g^S(a, z) \quad \leftarrow \text{Holds for } (a, z) \notin \Omega^U$$
$$+ \gamma^z \int \text{Pr}^z(z|z') g^S(a, z') dz' + \gamma^E g^E(a, z) \mathbb{1}_{\{(a, z) \notin \Omega^U\}},$$

Model performance: Untargeted moments

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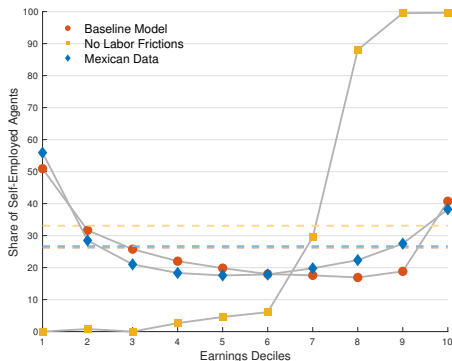
Occupational Transition Rates

	Data	Model		Data	Model		Data	Model
$U \rightarrow U$	27.4	29.3	$S \rightarrow U$	1.9	4.6	$E \rightarrow U$	3.1	2.5
$U \rightarrow S$	14.6	23.6	$S \rightarrow S$	76.8	62.2	$E \rightarrow S$	8.1	12.8
$U \rightarrow E$	58.0	47.1	$S \rightarrow E$	21.3	33.1	$E \rightarrow E$	88.8	84.7

Income Moments

	Data	Model		Data	Model
$\text{corr}(y_t^E, y_{t+1}^S)$	0.43	0.39	$\text{corr}(y_t^S, y_{t+1}^E)$	0.43	0.34

Model Performance: The role of labor vs financial frictions

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- ▶ Model without labor frictions misses Self-employment *out-of-necessity*
- ▶ There is also no unemployment risk for employed agents
- ▶ Self-employment is only taken by agents who can generate higher profits than wages

Toy Model Appendix

Selection into self-employment

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Static Model Continuum of unemployed (U) agents

- ▶ Choose to stay unemployed (U) or become self-employed (SE)
- ▶ Heterogeneity: Assets (a) and productivity (z)
- ▶ CRRA utility: $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$

Selection into self-employment

[back](#)

Static Model Continuum of unemployed (U) agents

- ▶ Choose to stay unemployed (U) or become self-employed (SE)
- ▶ Heterogeneity: Assets (a) and productivity (z)
- ▶ CRRA utility: $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$

Unemployment

- ▶ U get a job with probability p
- ▶ If employed, consume: $a + w$
- ▶ If not, consume: $a + b$

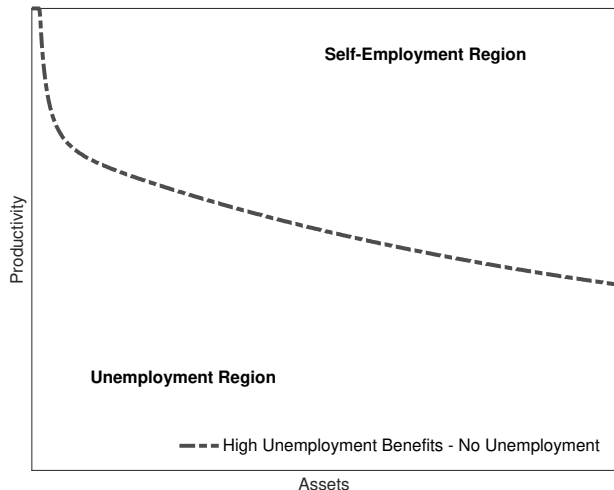
Self-Employment

- ▶ SE produce using own assets
- ▶ Consume: $a + za^\alpha$

Mechanisms behind policies depend on **selection into self-employment**

Self-employment as an outside option to employment

back

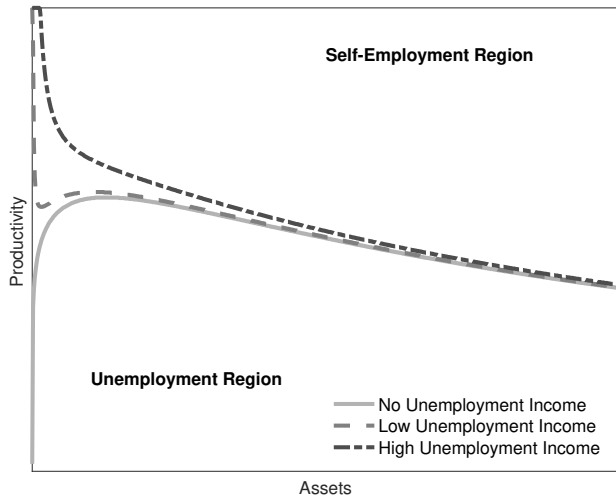


High unemployment benefits (b) or
no unemployment ($p = 1$)

- ▶ “Positive” selection to SE
- ▶ Productive/Wealthy agents
- ▶ No low-earning SE

Self-employment as an outside option to unemployment

back



Selection breaks for resource constrained agents:

- ▶ Poor + Unemployed

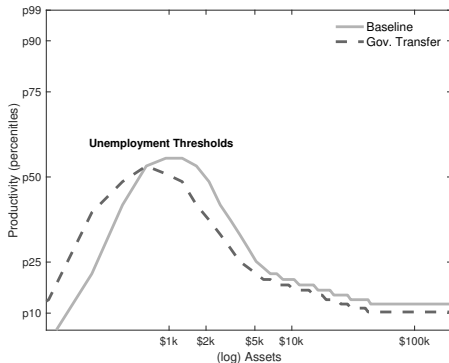
- Unproductive SE

- Low-earning SE

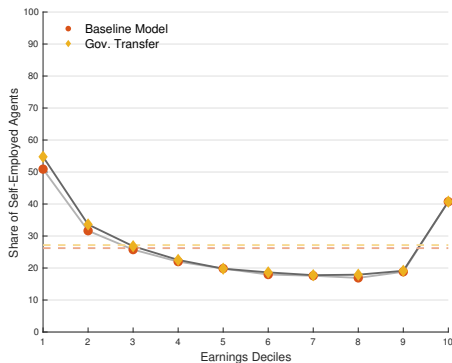
- ▶ Large share of SE if lots of poor/constrained agents

Policy Appendix

Micro Transfers - Occupational Choices

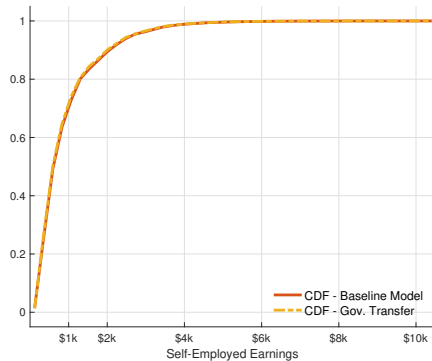
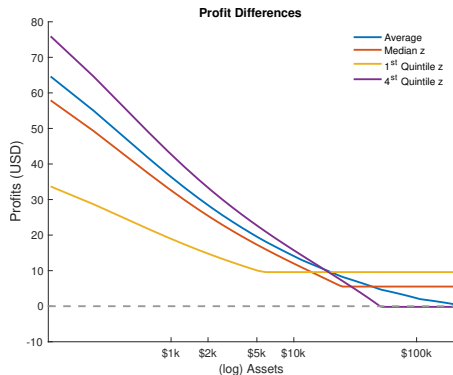
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Some changes in thresholds



Small effects across distribution of income

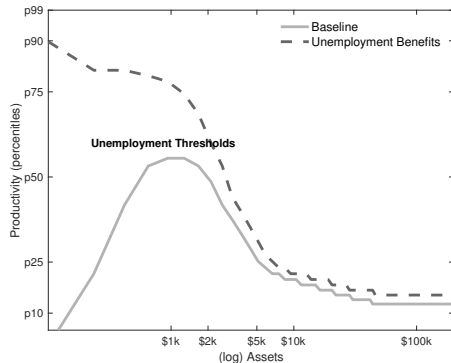
Micro Transfers - Self-Employment Income

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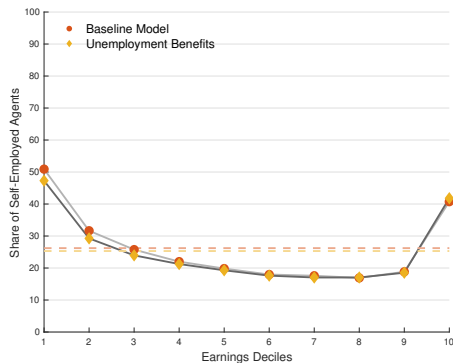
Small profit gains to poor & productive

Negligible effects in the distribution

Unemployment benefits - Occupational Choices

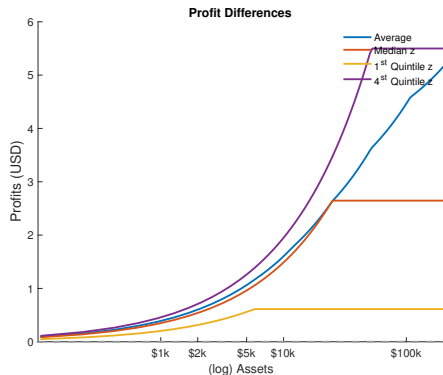
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Increase in productivity selection

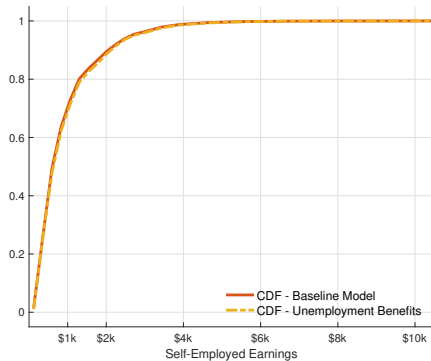


Lower mass of low-earning SE

Unemployment benefits - Self-Employment Income

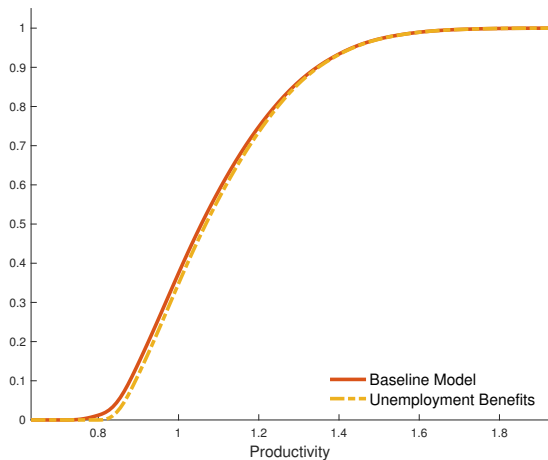
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Productive SE take advantage of $w \downarrow$



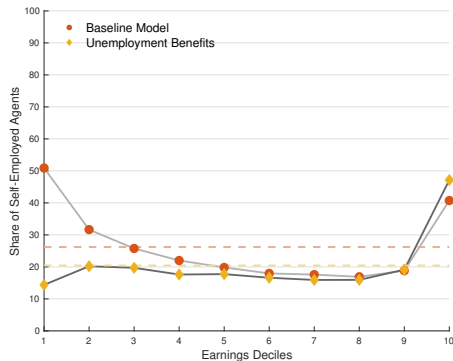
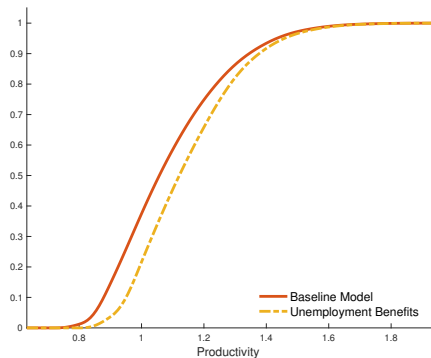
Noticeable effects on earnings

Unemployment benefits - Productivity Distribution

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Change in selection improves productivity

Unemployment Benefits: Self-employment \downarrow among the poor

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Unemployment benefits: productivity \uparrow , unemployment \uparrow

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Moment	GE	Moment	GE
% Δ Wage	-2.0	Δ Employment	0.46
% Δ Output	-2.3	Δ Self-employment	-5.8
% Δ TFP	2.9	Δ Unemployment	5.1

Credit Deepening: Relaxing Collateral Constraints

- ▶ Financial frictions prevent self-employed to produce at optimal scale
- ▶ Capture financial reform as credit deepening

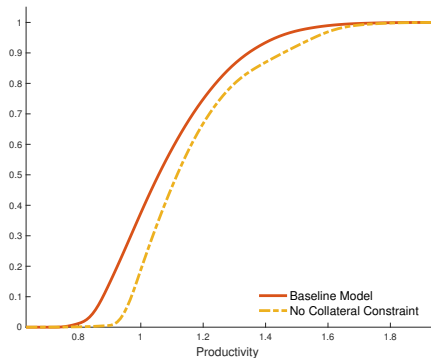
$$k \leq (\lambda + \lambda_{CD}) \cdot a$$

Two exercises:

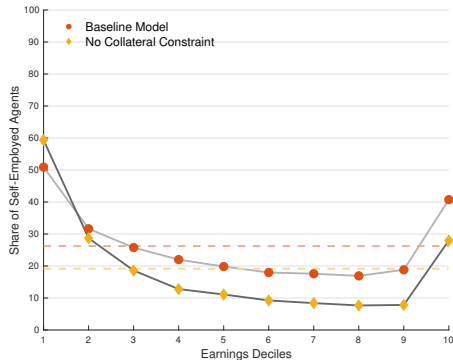
1. Relaxed collateral constraint: $\lambda_{CD} > 0$ (In paper)
2. No collateral constraint: $\lambda_{CD} \rightarrow \infty$

more

Elimination of Collateral Constraints: $\lambda_{CD} \rightarrow \infty$

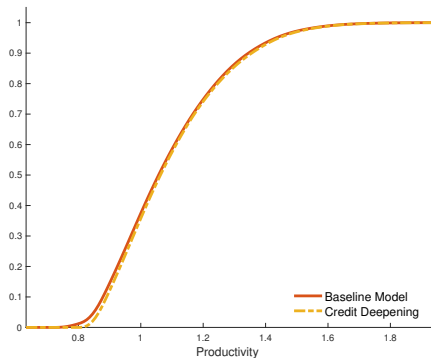


Productivity distribution improves
TFP \uparrow 11%

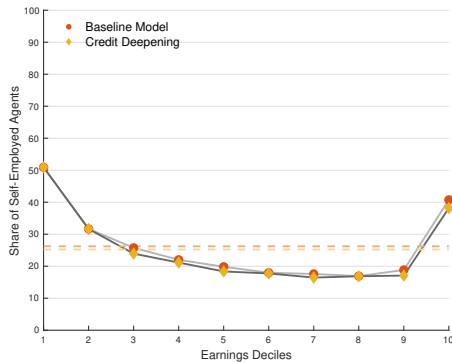


SE \downarrow bc strong GE effects: wages \uparrow
Subsistence concerns remain [more](#)

Credit Deepening: $\lambda_{CD} > 0$

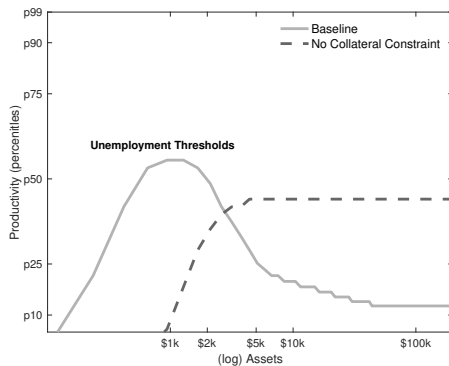
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Productivity distribution improves



SE ↓ because wages ↑
(subsistence SE persists)

Elimination of Collateral Constraints

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Does not solve occupational choices at the bottom

Transfers to the self-employed

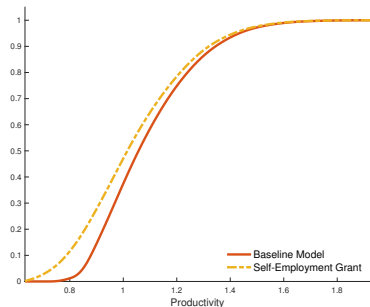
Transfers of 17% of labor incomes to the lowest 10% Banerjee, Niehaus, and Suri (2019)

$$y^S = r \cdot a + \pi(a, z) + b_{MG} \mathbb{1}_{MG}$$

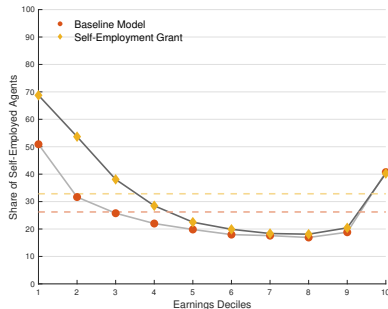
Transfers to the self-employed

Transfers of 17% of labor incomes to the lowest 10% Banerjee, Niehaus, and Suri (2019)

$$y^S = r \cdot a + \pi(a, z) + b_{MG} \mathbb{1}_{MG}$$



Productivity distribution worsens (FOSD)



Self-employment ↑ among the poor
(productive SE do not benefit)

Transfers to the self-employed

Moment	GE	Moment	GE
% Δ Wage	1.0	Δ Employment	-2.5
% Δ Output	-2.4	Δ Self-employment	6.6
% Δ TFP	-2.5	Δ Unemployment	-4.1

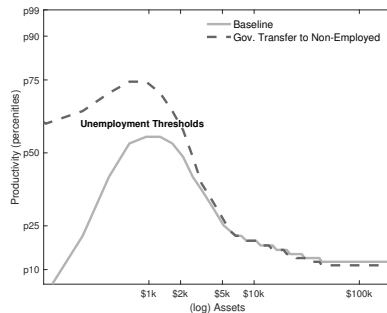
- ▶ Transfers heavily influence occupational choice
- ▶ Unemployed agents prefer self-employment regardless of productivity
- ▶ Aggregate productivity decreases as a result

Transfers to the non-employed: Occupational choice

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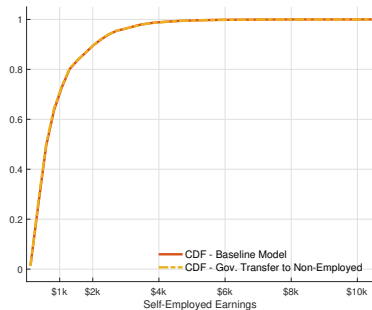
Policy effects:

Moment		
Δ Employment	-0.22	
Δ Unemployment	-0.14	
Δ Self-employment	0.36	
% Δ Wage	-0.04	
% Δ Income(E)	-0.22	
% Δ Income (S)	-1.40	

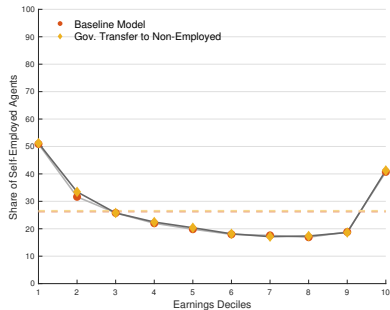


Increase in productivity selection

Transfers to the non-employed: Self-employed income

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Increase in productivity selection



Increase in productivity selection