



NTNU

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# SMILE – Homomorphic Encryption

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# Outline



What is Homomorphic Encryption

Use-Cases for Homomorphic Encryption Including Border Control

Types of Homomorphic Encryption Crypto Schemes

Open Source Libraries Based Solutions for the Untrusted Cloud Systems



# What is Homomorphic Encryption?

- **Purpose:** Computation on encrypted data
  - data can remain **confidential** while it is processed in **untrusted environments**.
  - **Homomorphism:** is a structure-preserving map between two algebraic structures
    - describes the transformation of one data set into another while preserving relationships between elements in both sets.
  - Greek words for “**same structure.**”
  - **Traditional Encryption vs Homomorphic Encryption**
    - **Homomorphic encryption** allows computation to be performed directly on **encrypted** data without requiring access to a secret key.
    - The result of such a computation remains in **encrypted** form, **and** can at a later point be revealed by the owner of the secret key.

# What is Homomorphic Encryption?

No Trusted  
Third-  
Parties

- Data remains secure and private in untrusted environments
- The data stays encrypted at all times, which minimizes the likelihood that sensitive information ever gets compromised.

Tradeoff  
between data  
usability and  
privacy

- There is no need to mask or drop any features in order to preserve the privacy of data.
- All features may be used in an analysis, without compromising privacy.

Quantum-  
safe

- Fully homomorphic encryption schemes are resilient against quantum attacks

# What is Homomorphic Encryption?

## Limitations

Poor  
performance

- Between slow computation speed, fully homomorphic encryption remains problematic for computationally-heavy applications

Large Memory  
Consumption

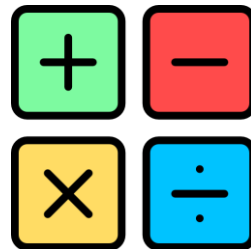
- Compared to plaintext operations making them sometimes impractical for the database queries

# What is Homomorphic Encryption?

operation(plain)

Public key: (23,143)

Private key: (47,143)



**Private** What is the area? Width:7 height:3

**Public**



$$2 \times 126 = 252$$

$$\text{Enc}(\text{width}) = \text{width}^e \bmod N$$

$$\text{Enc}(\text{width}) = 7^{23} \bmod 143$$

$$\text{Enc}(\text{width}) = 2$$

$$\text{Enc}(\text{height}) = \text{height}^e \bmod N$$

$$\text{Enc}(\text{height}) = 3^{23} \bmod 143$$

$$\text{Enc}(\text{height}) = 126$$

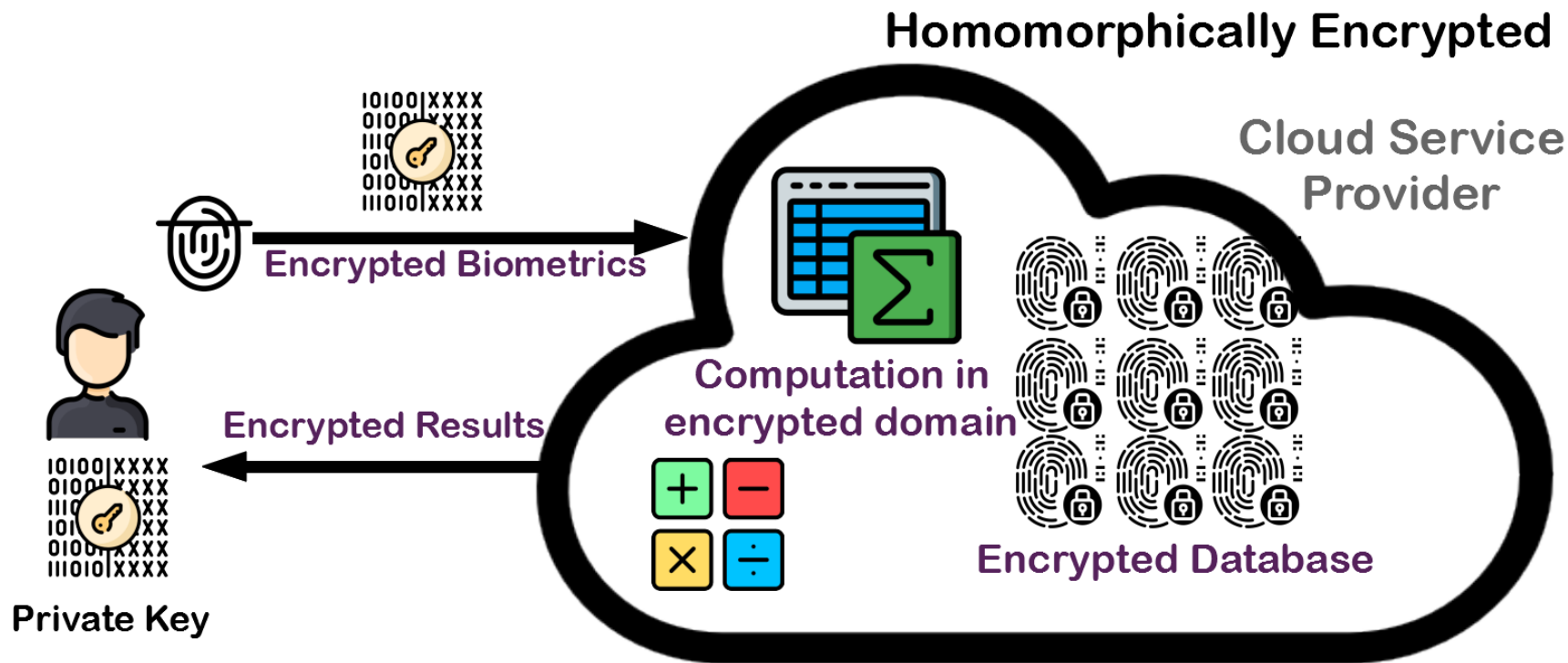
$$\text{area} = \text{cipher}^d \bmod N$$

$$\text{area} = 252^{47} \bmod 123$$

$$\text{area} = 21$$

$$7 \times 3 = 21$$

# What is Homomorphic Encryption?



# Use-Cases

## Medical Records

- Analyze disease/treatment without disclosing
- Search DNA markers without revealing DNA

## SPAM Filtering

- Blacklisting Encrypted mails

## Biometric Matching

- Encrypted distance metrics
- Similarity



# Privacy Preserving Biometric Authentication

- Strong Authentication Method: Biometrics
  - Represents who you are
  - Unique, Universal, Permanent, and Collectable
- Security Concerns
  - Biometric identity stored at multiple service providers
  - Different proprietary protocols
  - Revealing Biometric ID during authentication



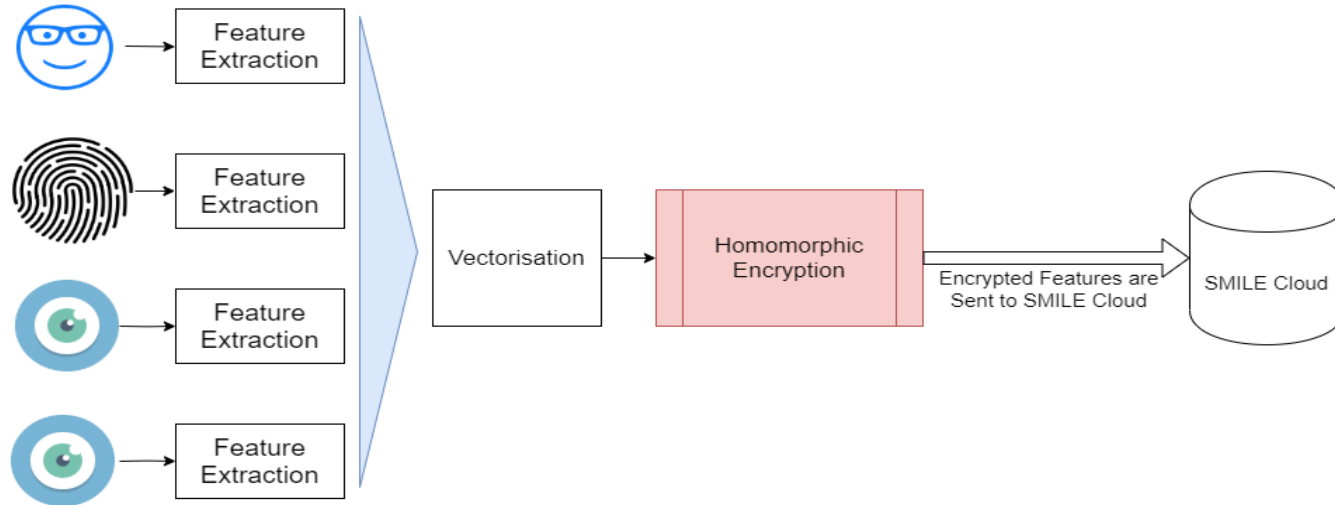
# Privacy Preserving Biometric Authentication

- Stolen biometrics
  - Cannot be revoked easily
- Being compromised
  - Captured, cloned or forged
  - Identity theft or individual profiling



# Privacy Preserving Biometric Authentication

- Face biometrics, fingerprint biometrics, and iris biometrics are protected by the **homomorphic encryption technique**. As shown in the figure below, feature vectors are extracted using smartphone technology and feature extraction algorithm.
- The homomorphic encryption is an additional layer of security to protect the privacy on top of the transport layer encryption such as SSL and TLS.



# Types of Homomorphic Encryption

Partially Homomorphic

Somewhat Homomorphic

Fully Homomorphic

# Partially Homomorphic Encryption

- When you can only perform certain mathematical operations on the ciphertext but not others
  - **RSA cryptosystem**: partially homomorphic with respect to **multiplication**
    - $[a] \times [b]$  OK
    - $[a] + [b]$  Not OK
  - **Caesar Cipher**: partially homomorphic with respect to **addition**
    - $[a] + [b]$  OK
    - $[a] \times [b]$  Not OK
  - **Paillier**: partially homomorphic with respect to **addition**
    - $[a] + [b]$  OK
    - $[a] \times b$  OK (Encrypted x Plain)
    - $[a] \times [b]$  Not OK

# Somewhat Homomorphic Encryption

- SHE is more general than PHE in the sense that it supports homomorphic operations with additions and multiplications. The drawback is that you can perform only a limited number homomorphic operations.

# Fully Homomorphic Encryption

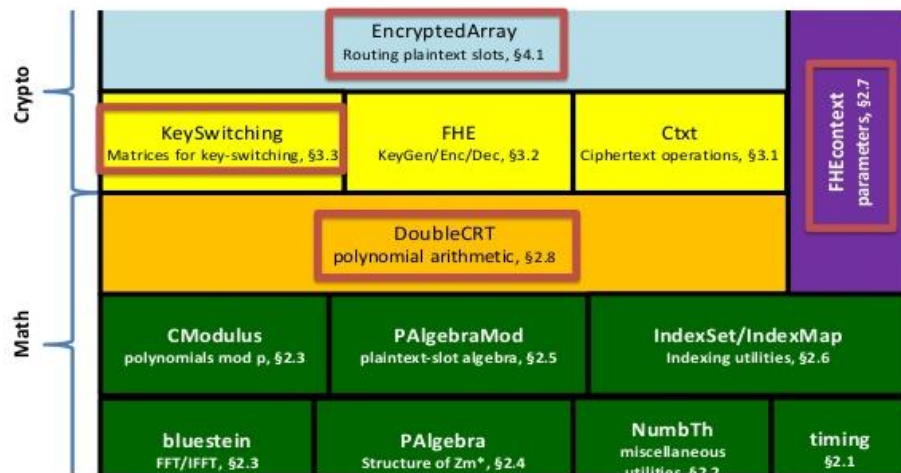
- When you can perform mathematical operations on the ciphertext
  - **BGV** and **BFV**
    - (Encrypted with Encrypted)
      - $[a] + [b]$  OK
      - $[a] - [b]$  Ok
      - $[a] \times [b]$  OK
    - (Encrypted with Plain)
      - $[a] + b$  OK
      - $[a] - b$  Ok
      - $[a] \times b$  OK

# Open Source Libraries for HE



- SEAL
- HeLib
- PALISADE

## Architecture of HElib





# Privacy-Preserving Area Solver

```
1 from Pyfhel import Pyfhel
2
3 print("1. Creating Context and KeyGen in a Pyfhel Object ")
4 HE = Pyfhel() # Creating empty Pyfhel object
5 HE.contextGen(p=65537, m=2048, flagBatching=True) # Generating context.
6 HE.keyGen() # Key Generation.
7
8 print("2. Encrypting integers")
9 integer1 = 7
10 integer2 = 3
11 ctxt1 = HE.encryptInt(integer1) # Encryption makes use of the public key
12 ctxt2 = HE.encryptInt(integer2) # For integers, encryptInt function is used.
13
14 print("3. Operating with encrypted integers")
15 ctxtSum = ctxt1 + ctxt2 # `ctxt1 += ctxt2` for quicker inplace operation
16 ctxtSub = ctxt1 - ctxt2 # `ctxt1 -= ctxt2` for quicker inplace operation
17 ctxtMul = ctxt1 * ctxt2 # `ctxt1 *= ctxt2` for quicker inplace operation
18
19 print("4. Decrypting result:")
20 resSum = HE.decryptInt(ctxtSum) # Decryption must use the corresponding function
21 # decryptInt.
22 resSub = HE.decryptInt(ctxtSub)
23 resMul = HE.decryptInt(ctxtMul)
24 print("\taddition:      decrypt(ctxt1 + ctxt2) = ", resSum)
25 print("\tsubtraction:    decrypt(ctxt1 - ctxt2) = ", resSub)
26 print("\tmultiplication:  decrypt(ctxt1 * ctxt2) = ", resMul)
```

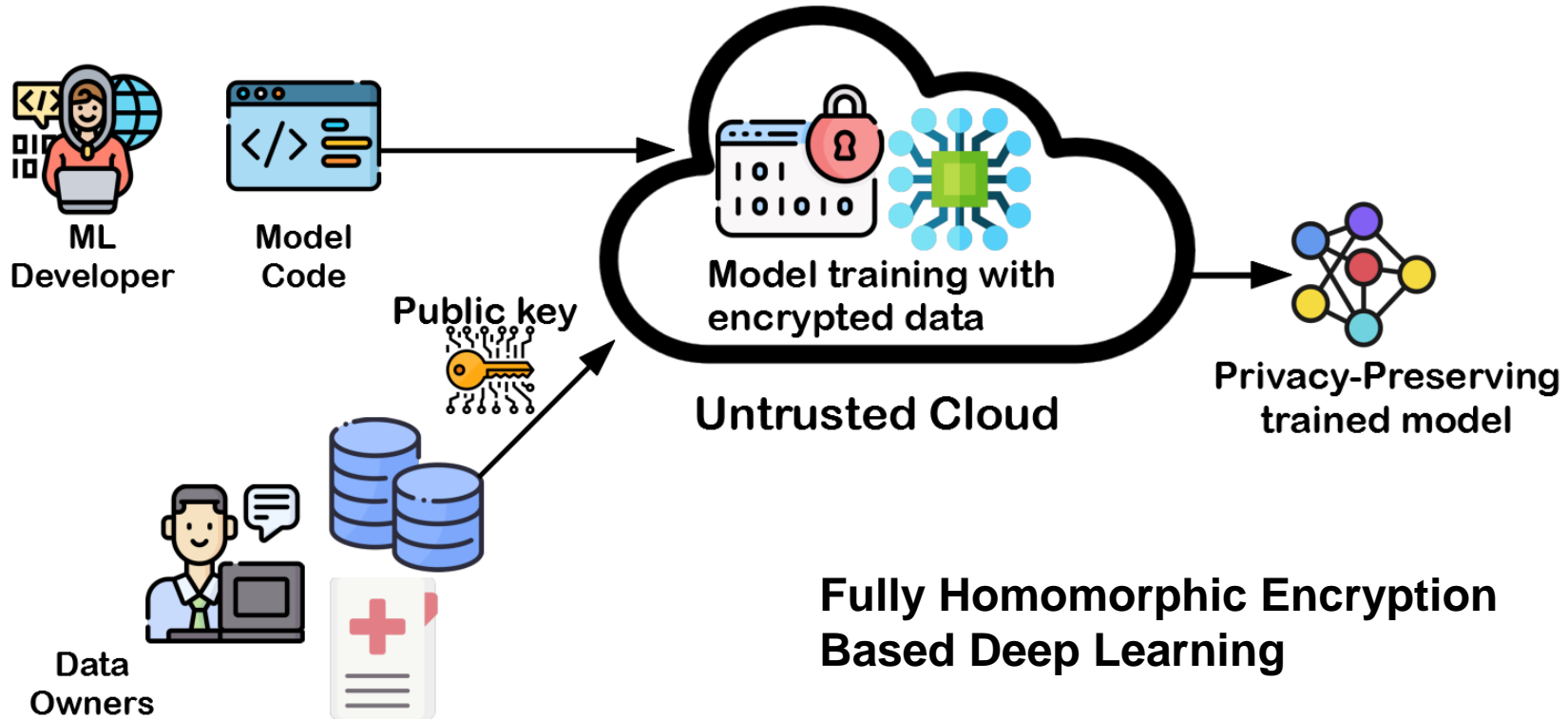
```
1. Creating Context and KeyGen in a Pyfhel Object
2. Encrypting integers
3. Operating with encrypted integers
4. Decrypting result:
   addition:      decrypt(ctxt1 + ctxt2) = 10
   subtraction:   decrypt(ctxt1 - ctxt2) = 4
   multiplication: decrypt(ctxt1 * ctxt2) = 21
```

# Homomorphic Encryption Applications

- Privacy-Preserving Machine Learning

**Homomorphic Encryption** + **Secure Machine Learning** = **Privacy Preserving Machine Learning**

# Homomorphic Encryption Applications



# Contact Information

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**Thank You!**