

¹ GCM-Filters: A Python package for Diffusion-based ² Spatial Filtering of Gridded Data

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DOI: [10.21105/joss.0XXXX](https://doi.org/10.21105/joss.0XXXX)

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Editor: [Editor Name ↗](#)

Submitted: 01 January XXXX

Published: 01 January XXXX

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¹³ Summary

¹⁴ GCM-Filters is a python package that allows scientists to perform spatial filtering analysis
¹⁵ in an easy, flexible and efficient way. The package implements the filtering method that was
¹⁶ introduced by Grooms et al. (2021). The filtering algorithm is analogous to smoothing via
¹⁷ diffusion; hence the name *diffusion-based filters*. GCM-Filters can be used with either gridded
¹⁸ observational data or gridded data that is produced by General Circulation Models (GCMs)
¹⁹ of ocean, weather, and climate. Spatial filtering of observational or GCM data is a common
²⁰ analysis method in the Earth Sciences, for example to study oceanic and atmospheric motions
²¹ at different spatial scales or to develop subgrid-scale parameterizations for ocean models.

²² GCM-Filters provides filters that are highly configurable, with the goal to be useful for a wide
²³ range of scientific applications. The user has different options for selecting the filter scale and
²⁴ filter shape. The filter scale can be defined in several ways: a fixed length scale (e.g., 100
²⁵ km), a scale tied to a model grid scale (e.g., 1°), or a scale tied to a varying dynamical scale
²⁶ (e.g., the Rossby radius of deformation). As an example, [Figure 1](#) shows unfiltered and filtered
²⁷ relative vorticity, where the filter scale is set to a model grid scale of 4°. GCM-Filters also
²⁸ allows for anisotropic, i.e., direction-dependent, filtering. Finally, the filter shape – currently:
²⁹ either Gaussian or Taper – determines how sharply the filter separates scales above and below
³⁰ the target filter scale.

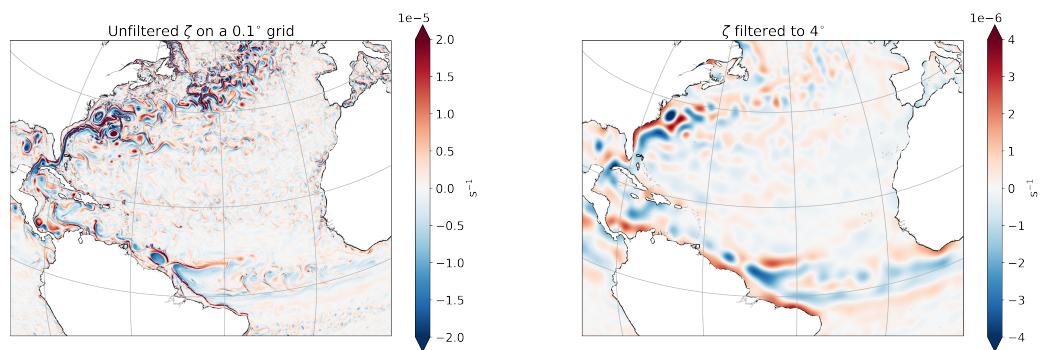


Figure 1: (Left) Snapshot of unfiltered surface relative vorticity $\zeta = \partial_x v - \partial_y u$ from a global 0.1° simulation with MOM6 (Adcroft et al., 2019). (Right) Relative vorticity filtered to 4° , obtained by applying GCM-Filters to the field ζ on the left. The plots are made with `matplotlib` (Hunter, 2007) and `cartopy` (Met Office, 2010 - 2015).

31 Statement of Need

32 Spatial filtering is commonly used as a scientific tool for analyzing gridded data. An example
 33 of an existing spatial filtering tool in python is SciPy's (Virtanen et al., 2020) `ndimage.gaussian_filter`
 34 function, implemented as a sequence of convolution filters. While being a valuable tool for image processing (or blurring), SciPy's Gaussian filter is of limited use for
 35 GCM data; it assumes a regular and rectangular Cartesian grid, employs a simple boundary condition, and the definitions of filter scale and shape have little or no flexibility. The python package GCM-Filters is specifically designed to filter GCM data, and seeks to solve a number of challenges for the user:

- 40 1. GCM data comes on irregular curvilinear grids with spatially varying grid-cell geometry.
 41 2. Continental boundaries require careful and special treatment when filtering ocean GCM output.
 42 3. Earth Science applications benefit from configurable filters, where the definition of filter scale and shape is flexible.
 43 4. GCM output is often too large to process in memory, requiring distributed and / or delayed execution.

47 The GCM-Filters algorithm (Grooms et al., 2021) applies a discrete Laplacian to smooth a field through an iterative process that resembles diffusion. The discrete Laplacian takes into
 48 account the varying grid-cell geometry and uses a no-flux boundary condition, mimicking how
 49 diffusion is internally implemented in GCMs. The no-flux boundary conditions ensures that
 50 the filter preserves the integral: $\int_{\Omega} \bar{f}(x, y) dA = \int_{\Omega} f(x, y) dA$, where f is the original field,
 51 \bar{f} the filtered field, and Ω the ocean domain. Conservation of the integral is a desirable filter
 52 property for many physical quantities, for example energy or ocean salinity. More details on
 53 the filter properties can be found in Grooms et al. (2021).

55 An important goal of GCM-Filters is to enable computationally efficient filtering. The user
 56 can employ GCM-Filters on either CPUs or GPUs, with NumPy (Harris et al., 2020) or CuPy
 57 (Okuta et al., 2017) input data. GCM-Filters leverages Dask (Dask Development Team,
 58 2016) and Xarray (Hoyer & Hamman, 2017) to support filtering of larger-than-memory
 59 datasets and computational flexibility.

60 Usage

61 The main GCM-Filters class that the user will interface with is the `gcm_filters.Filter`
62 object. When creating a filter object, the user specifies how they want to smooth their data,
63 including the desired filter shape and filter scale. At this stage, the user also picks the grid
64 type that matches their GCM data, given a predefined list of grid types. Each grid type
65 has an associated discrete Laplacian, and requires different *grid variables* that the user must
66 provide (the latter are usually available to the user as part of the GCM output). Currently,
67 GCM-Filters provides a number of different grid types and associated discrete Laplacians:

- 68 ■ Grid types with **scalar Laplacians** that can be used for filtering scalar fields, for example
69 temperature or vorticity (see [Figure 1](#)). The currently implemented grid types are
70 compatible with different ocean GCM grids including MOM5 (MOM 5 Development
71 Team, 2012), MOM6 (Adcroft et al., 2019) and the POP2 (Smith et al., 2010) tripole
72 grid.
73 ■ Grid types with **vector Laplacians** that can be used for filtering vector fields, for example
74 horizontal velocity (u, v). The currently implemented grid type is compatible with ocean
75 GCM grids that use an Arakawa C-grid convention; examples include MOM6 (Adcroft
76 et al., 2019) and the MITgcm (Campin et al., 2021).

77 Atmospheric model grids are not yet supported, but could be implemented within the GCM-F
78 ilters package. Users are encouraged to contribute more grid types and Laplacians via pull
79 requests.

80 Acknowledgements

81 This work was supported by the National Science Foundation grants OCE 1912302,
82 OCE 1912325, OCE 1912332, OCE 1912420, GEO 1912357, and the NOAA grant CVP
83 NA19OAR4310364. Busecke received support from the Gordon and Betty Moore Foundation.

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