```
In [5]: #Write a program that finds the closest pair of points in a set of 2D points
        import math
        def calculate_distance(point1, point2):
            Calculate the Euclidean distance between two points.
            return math.sqrt((point1[0] - point2[0])**2 + (point1[1] - point2[1])**;
        def closest_pair_brute_force(points):
            Find the closest pair of points using the brute force approach.
            min_distance = float('inf')9
            closest_pair = (None, None)
            n = len(points)
            for i in range(n):
                for j in range(i + 1, n):
                    distance = calculate_distance(points[i], points[j])
                    if distance < min_distance:</pre>
                        min_distance = distance
                        closest_pair = (points[i], points[j])
            return closest_pair, min_distance
        points = [(2, 3), (12, 30), (40, 50), (5, 1), (12, 10), (3, 4)]
        closest_pair, min_distance = closest_pair_brute_force(points)
        print(f"The closest pair of points is: {closest_pair}")
        print(f"The distance between them is: {min_distance}")
```

The closest pair of points is: ((2, 3), (3, 4))
The distance between them is: 1.4142135623730951

```
In [18]:
         import matplotlib.pyplot as plt
         def is_left_turn(p, q, r):
             """Returns True if r is to the left of line pq, False if r is to the rig
             return (q[0] - p[0]) * (r[1] - p[1]) - (q[1] - p[1]) * (r[0] - p[0])
         def convex_hull(points):
             n = len(points)
             if n < 3:
                 return points
             hull = []
             # Iterate through each pair of points
             for i in range(n):
                 for j in range(i + 1, n):
                     left_turn = None
                     for k in range(n):
                          if k == i or k == j:
                              continue
                          turn = is_left_turn(points[i], points[j], points[k])
                          if turn != 0:
                              if left turn is None:
                                  left_turn = turn
                              elif left turn * turn < 0:</pre>
                                  break
                     else:
                          hull.append((points[i], points[j]))
             # Filter unique points
             unique_points = set()
             for edge in hull:
                 unique_points.add(edge[0])
                 unique_points.add(edge[1])
             return list(unique points)
         def plot_convex_hull(points, hull_points):
             plt.figure()
             plt.scatter(*zip(*points), label='Points')
             for i, point in enumerate(points):
                  plt.annotate(f'P{i+1}', (point[0]+0.2, point[1]-0.2))
             hull_points.append(hull_points[0]) # to close the hull
             plt.plot(*zip(*hull_points), label='Convex Hull')
             plt.legend()
             plt.show()
         points = [(10, 0), (11, 5), (5, 3), (9, 3.5), (15, 3), (12.5, 7), (6, 6.5),
         hull_points = convex_hull(points)
         hull_points = sorted(hull_points)
```

```
In [8]:
         #Write a program to find the closest pair of points in a given set using the
         import math
         def euclidean distance(p1, p2):
             return math.sqrt((p1[0] - p2[0]) ** 2 + (p1[1] - p2[1]) ** 2)
         def closest_pair(points):
             n = len(points)
             if n < 2:
                 return None, float('inf')
             min distance = float('inf')
             closest_points = None
             for i in range(n):
                 for j in range(i + 1, n):
                     distance = euclidean_distance(points[i], points[j])
                     if distance < min_distance:</pre>
                          min_distance = distance
                         closest_points = (points[i], points[j])
             return closest_points, min_distance
         # Example usage
         points = [(10, 0), (11, 5), (5, 3), (9, 3.5), (15, 3), (12.5, 7), (6, 6.5),
         closest_points, min_distance = closest_pair(points)
         print(f"The closest pair of points is: {closest_points}")
         print(f"The minimum distance is: {min_distance:.4f}")
         The closest pair of points is: ((9, 3.5), (7.5, 4.5))
         The minimum distance is: 1.8028
         def dice throw(num sides, num dice, target):
In [10]:
             dp = [[0] * (target + 1) for _ in range(num_dice + 1)]
             dp[0][0] = 1
             for i in range(1, num_dice + 1):
                 for j in range(1, target + 1):
                     dp[i][j] = 0
                     for k in range(1, num_sides + 1):
                         if j - k >= 0:
                              dp[i][j] += dp[i-1][j-k]
             return dp[num dice][target]
         num_sides = 6
         num_dice = 3
         target = 8
         print(f"Number of ways to get a sum of {target} with {num dice} dice each h₀
```

Number of ways to get a sum of 8 with 3 dice each having 6 sides: 21

```
In [11]: from itertools import combinations
         def knapsack_exhaustive(weights, values, capacity):
             num_items = len(weights)
             max_value = 0
             best_combination = []
             # Iterate through all possible subsets of items
             for i in range(1, num_items + 1):
                 for subset in combinations(range(num items), i):
                     total_weight = sum(weights[j] for j in subset)
                     total_value = sum(values[j] for j in subset)
                     # Check if this subset is the best one found so far
                     if total_weight <= capacity and total_value > max_value:
                         max_value = total_value
                         best_combination = subset
             return best_combination, max_value
         # Example usage
         weights = [2, 3, 4, 5]
         values = [3, 4, 5, 6]
         capacity = 5
         best_combination, max_value = knapsack_exhaustive(weights, values, capacity)
         print(f"The best combination of items is: {best_combination}")
         print(f"The maximum value is: {max_value}")
         The best combination of items is: (0, 1)
         The maximum value is: 7
```

In [ ]: