

STD – 10

MATHS

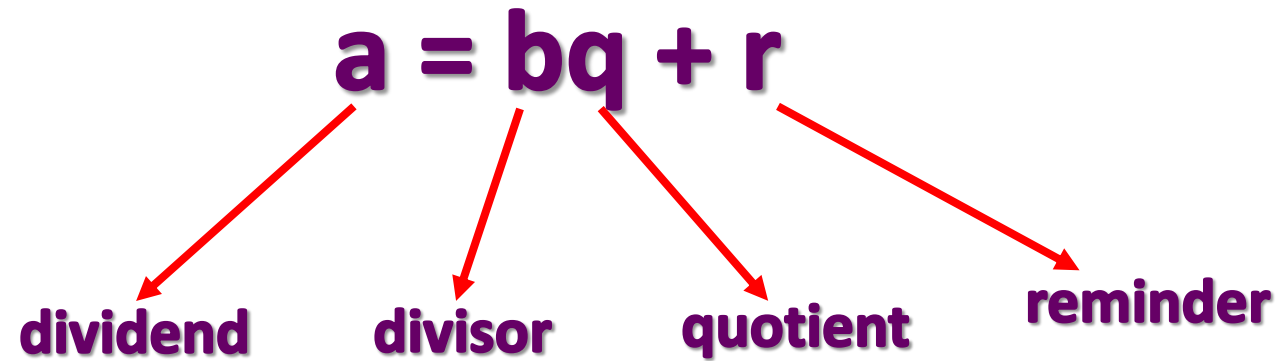
CHAPTER - 1

REAL NUMBER

EXERCISE -1.1(Q.1)

Euclid's division lemma(Algorithm)

- If a and b are two positive integers then they must satisfy the condition.
- $a = bq + r$ where $0 \leq r < b$



Use of Euclid division lemma

For division

Find H.C.F

EX. Find H.C.F OF 45 AND 6.

Step . 1 $45 > 6$

So that $a = 45$, $b = 6$

$$\begin{array}{r} 7 \\ 6 \overline{)45} \\ \underline{42} \\ 3 \end{array}$$

We get $q = 7$, $r = 3$

Use Euclid division lemma

$$a = bq + r$$

$$45 = (6 \times 7) + 3$$

Step . 1 $6 > 3$

So that $a = 6, b = 3$

$$\begin{array}{r} 2 \\ 3\overline{)6} \\ \underline{6} \\ 0 \end{array}$$

We get $q = 2, r = 0$

Use Euclid division lemma

$$6 = (3 \times 2) + 0$$

We have $r = 0$, so that our method stops here. Since, in the last step the divisor is 3, therefore, $\text{HCF} = (45, 6) = 3$.

Q.1 Use Euclid's division algorithm to find HCF.

(i) 135 and 225

➤ **225 is greater than 135. Therefore, by Euclid's division algorithm,**

a = 225 , b = 135

$$\begin{array}{r} 1 \\ 135 \overline{) 225} \\ \underline{-135} \\ 90 \end{array}$$

we get, $q = 1$ $r = 90$

Use Euclid division lemma

$$a = bq + r$$

$$225 = (135 \times 1) + 90$$

Now, remainder $90 \neq 0$, thus again use division lemma

$$a = 135, b = 90$$

$$\begin{array}{r} 1 \\ 90 \overline{) 135} \\ \underline{- 90} \\ 45 \end{array}$$

we get, $q = 1$, $r = 45$

According to Euclid division lemma

$$135 = (90 \times 1) + 45$$

Again, $45 \neq 0$, thus again use division lemma

$$a = 90 \quad b = 45$$

$$\begin{array}{r} 2 \\ 45 \overline{) 90} \\ \underline{- 90} \\ 00 \end{array}$$

we get, $q = 2$ $r = 0$

**We have $r = 0$, so that our method stops here. Since, in the last step, the divisor is 45,
therefore, HCF = (225 , 135)
= 45.**

(ii) 196 and 38220

➤ **38220 is greater than 196, Therefore, by Euclid's division algorithm,**

$$\mathbf{a = 38220 \quad , \quad b = 196}$$

$$\begin{array}{r} 195 \\ 196 \overline{) 38220} \\ \underline{- 38220} \\ 0 \end{array}$$

we have, $q = 195$, $r = 0$

Use Euclid division lemma

$$**38220 = (196 \times 195) + 0**$$

We have $r = 0$, so that our method stops here. Since, in the last step, the divisor is 195,

$$**\text{so that } \text{HCF} = (196 , 38220) \\ = 195**$$

(iii) 867 and 255

➤ **867 is greater than 255, Therefore, by Euclid's division algorithm,**

$$a = 867 \quad b = 255$$

$$\begin{array}{r} 3 \\ 255 \overline{) 867} \\ \underline{- 765} \\ 102 \end{array}$$

we get, $q = 3$, $r = 102$

$$**867 = (255 \times 3) + 102**$$

Again, $102 \neq 0$, therefore again use division lemma

$$**a = 255 \quad b = 102**$$

$$\begin{array}{r} 2 \\ 102 \overline{) 255} \\ \underline{- 204} \\ 51 \end{array}$$

we have, $q = 2$, $r = 51$

$$\mathbf{255 = (102 \times 2) + 51}$$

Again, $51 \neq 0$, so that use Euclid's division lemma

$$\mathbf{a = 102 \quad b = 51}$$

$$\begin{array}{r} 2 \\ 51 \overline{) 102} \\ \underline{- 102} \\ 0 \end{array}$$

**We have $r = 0$, so that our method stops here. Since, in the last step, the divisor is 51, so that $\text{HCF} = (867 , 255)$
 $= 51$**

Thanks



For watching