

How to Explore “The Antlion’s Pit in a Morning Glory”

— *Instructions for the Mathematical Discovery Tool* —

This guide explains how to use the provided Python code to experience the gravitational pull of the Collatz Conjecture through visual exploration.

1. Prerequisites

To run the visualizer, make sure you have Python installed. The script depends on the following high-performance libraries:

- NumPy – for numerical computation
- Matplotlib – for high-fidelity polar coordinate plotting

2. Running the Visualizer

1. Save the provided Python script as a .py file (e.g., antlion_pit.py).
2. Open the file in your preferred IDE or code editor (e.g., VS Code, Jupyter Notebook, Spyder).
3. At the bottom of the script, locate the line
visualize_binary_log_antlion_pit(27) and replace 27 with any integer you’d like to explore.
4. Run the script to generate the semi-circular “Pit” chart.

3. Key Observations

- **Entry Point (Large Red Circle):** This marks the starting value’s position in binary logarithmic space.
- **Red Lines (3n+1 Jumps):** These represent odd-number operations. Notice how small these “leaps for freedom” are—insufficient to escape the pit’s pull.
- **Blue Lines (n/2 Falls):** These represent even-number operations. They act as sharp, direct slides toward the central 2^n Tower Axis—this is the system’s structural gravity.
- **Exit (Green Point):** Every number, regardless of size, ultimately spirals into this singular destination: 1.

4. Recommended Challenges

To fully appreciate the dynamics of the Antlion's Pit, try visualizing these starting values:

- **27:** The "Pit Master." Watch its famously chaotic journey unfold over 111 steps before surrendering to gravity.
- **31:** Another complex traveler, weaving a dense maze of red and blue before converging.
- **5, 21, 85:** These numbers align at the same angle, revealing their shared "convergence slide."
- **Powers of 2 (e.g., 1024):** Observe the pure vertical descent—an unbroken fall along the Tower's spine.

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