

# How to Explore “The Antlion’s Pit in a Morning Glory”

## — *Instructions for the Mathematical Discovery Tool* —

This guide explains how to use the provided Python code to experience the gravitational pull of the Collatz Conjecture through visual exploration.

### 1. Prerequisites

To run the visualizer, make sure you have Python installed. The script depends on the following high-performance libraries:

- NumPy – for numerical computation
- Matplotlib – for high-fidelity polar coordinate plotting

### 2. Running the Visualizer

1. Save the provided Python script as a .py file (e.g., antlion\_pit.py).
2. Open the file in your preferred IDE or code editor (e.g., VS Code, Jupyter Notebook, Spyder).
3. At the bottom of the script, locate the line `visualize_binary_log_antlion_pit(27)` and replace 27 with any integer you’d like to explore.
4. Run the script to generate the semi-circular “Pit” chart.

### 3. Key Observations

- **Entry Point (Large Red Circle):** This marks the starting value’s position in binary logarithmic space.
- **Red Lines (3n+1 Jumps):** These represent odd-number operations. Notice how small these “leaps for freedom” are—insufficient to escape the pit’s pull.
- **Blue Lines (n/2 Falls):** These represent even-number operations. They act as sharp, direct slides toward the central  $2^n$  Tower Axis—this is the system’s structural gravity.
- **Exit (Green Point):** Every number, regardless of size, ultimately spirals into this singular destination: 1.

## 4. Recommended Challenges

To fully appreciate the dynamics of the Antlion's Pit, try visualizing these starting values:

- **27:** The "Pit Master." Watch its famously chaotic journey unfold over 111 steps before surrendering to gravity.
- **31:** Another complex traveler, weaving a dense maze of red and blue before converging.
- **5, 21, 85:** These numbers align at the same angle, revealing their shared "convergence slide."
- **Powers of 2 (e.g., 1024):** Observe the pure vertical descent—an unbroken fall along the Tower's spine.

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