Let n denote the number of steps and let m denote the array length.

- 1. DP. $O(n \cdot \min(n, m))$.
- 2. If we cannot stay in the same place: DP, the answer is

$$\binom{n}{n/2} - \sum_{i \geq 1} \left(\binom{n}{n/2 - (i-1)m - (2i-1)} - \binom{n}{n/2 + im + 2i} \right) - \sum_{i \geq 1} \left(\binom{n}{n/2 + im + (2i-1)} - \binom{n}{n/2 - im - 2i} \right).$$

O(n). https://www.zhihu.com/question/346654767/answer/1110765408

Now we can stay in the same place, and the answer is

$$\sum_{n' \le n, \ n' \text{ even}} \binom{n}{n'} \left[\binom{n'}{n'/2} - \sum_{i \ge 1} \left(\binom{n'}{n'/2 - (i-1)(m-1) - (2i-1)} - \binom{n'}{n'/2 + i(m-1) + 2i} \right) - \sum_{i \ge 1} \left(\binom{n'}{n'/2 + i(m-1) + (2i-1)} - \binom{n'}{n'/2 - i(m-1) - 2i} \right) \right].$$

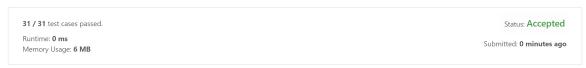
We can compute the solution in $O(n \cdot \frac{n}{m})$ time, by preprocessing factorial mod p and its inverse, then each binomial can be computed in O(1) time.

If $m \leq \sqrt{n}$, use the first algorithm, otherwise use the second algorithm. $O(n\sqrt{n})$.

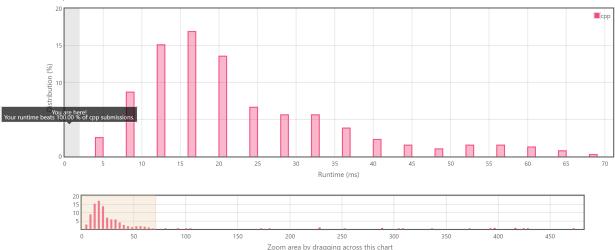
- 3. Another way to derive: https://hyper-meta.blogspot.com/2023/10/the-long-journey-from-on2-to-on15.html.
- 4. $\tilde{O}(\sqrt{n})$ using polynomials or linear recursions. see my article https://zhuanlan.zhihu.com/p/344219746.

Number of Ways to Stay in the Same Place After Some Steps

Submission Detail







References