Homework 1 (due Nov. 29th)
(This project should be implemented in Python.
It can be done in groups of at most 2 students)

In this project, you will implement an interpreter for a language called MatLang (Matrix Language).

MatLang language statements will be as follows:
1. Matlang programs will have two sections: The first will be a variable definitions section, followed by the executable statements section.
2. Variable definitions section will allow scalar, one-dimensional, two dimensional number variable definitions. For example:

    ```
    scalar    x
    vector    y[4]
    matrix    z[3,4]
    ```
    Assume all array dimensions are given as integer constants. In the above example **x** is a scalar variable, **y** is a vector (i.e. matrix of size 4x1) and **z** is a 3x4 matrix. Assume that each line contains a single definition. A definition cannot be written on more than one line.
3. Executable statements will consist of one line statements and for loop compound statements.   Note that no nested for loops are allowed.
4. One line statements are either assignment statements or print statements which print the value(s) of a scalar, vector, or a matrix variable or a separator.
5. A vector or a matrix varieble can be assigned values in curly brackets. Note that such assignment should fit on line. For the vector **y[4]** and **z[3,4],** the following example assignment can be made:

    ```
    y = { 1 2 3 4 }
    z   = {1 2 3 4 5 3 2 2 2 1   0 1 }
    ```
    Note that array indices start with 1.
6. There are no if statements in the language.
7. As operations in expressions, you are required to implement only multiplication, addition and subtraction: ***,+,–** . These are binary operand operations. Unary minus operation is *not* supported. Note that these are to be interpreted as either matrix or scalar operations depending on the context (i.e. type of operands). When a scalar expression multiplies a matrix or a vector, its meaning is multiplication of each individual component of a matrix or vector.
8. A function **tr(expr)** is also available which transposes a scalar, vector or a matrix.
9. A function **sqrt(expr)** is also available which takes square root of a scalar expression.
10. A function **choose(expr1,expr2,expr3,expr4)** which returns **expr2** if **expr1** is equal to 0, returns **expr3** if **expr1** is positive and returns **expr4** if **expr1** is negative. Note that **expr1**, **expr2**, **expr3** and **expr4** are expressions that evaluate to a scalar.
11. On a line, everything after the **#** sign are considered as comments.
12. For loop will have the following formats:

    ```
    for (id in expr1:expr2:expr3) {
        .....
        .....
    }
    ```
    Here, **id** is a variable, **expr1** is starting value of **id**, **expr2** is the bound on the value of **id** during the loop iteration and **expr3** is the added value to **id** at each iteration.

    For loop can also have the following syntax:

    ```
    for (id1,id2 in expr1:expr2:expr3, expr4:expr5: expr6) {
        .....
        .....
    }
    ```

This will be equivalent to doubly nested loops in languages like C/Java. You can assume that the values of ids `id1,id2` and expressions `expr1,expr2,expr3,expr4,expr5` and `expr6` cannot be changed inside the for loop body. You can also assume that `expr1 < expr2` and `expr4 < expr5` and that `expr3` and `expr6` evaluate to a positive value.

13. `print(id)` statement, prints the value of variable `id`.
14. `printsep()` statement, prints a separator line "----------"

Some example programs in the MatLang language are given below. Note that MatLang language programs have .mat extension.

ex1.mat	Output

<pre># this program computes fibonacci 	
# numbers 	
 	
# variable definitions 	
scalar i
scalar n
vector x[2]
vector y[2]
matrix A[2,2]
matrix B[2,2]
 	
# statements 	
n = 10
x = { 1 1 }
A = { 1 1 1 0 }
B = { 1 0 0 1 }
print(x)
for(i in 1:n:1) {
  B = A*B
  y = B*x
  print(y[1])
}</pre>
	<pre>1
	1
	2
	3
	5
	8
	13
	21
	34
	55
	89
	144</pre>

ex2.mat	Output

<pre># variable definitions 	
vector z[3]
vector y[4]
matrix A[2,2]
matrix B[2,3]
 	
z = A*B*y</pre>
	<pre>Error (Line 6): matrix dimensions in
	expression do not match.</pre>

ex3.mat	Output

<pre># this program implements google 	
# web page ranking alg. (simplified 	
# version) 	
 	
matrix   A[3,3]
vector   x[3]
vector   y[3]
scalar   r
scalar   i
 	
A = { 0.5 0 0.5 0 0 0.5 0.5 1 0 }
x = { 1 1 1 }
for(i in 1:10:1) {</pre>
	<pre>0.7071068
	0.6123724
	0.4677072
	0.3852759
	0.3093592
	0.2509747
	0.2028243
	0.1641555
	0.1327838
	0.1074308
	------------ 	
	1.2148438
	0.6240234</pre>

	1.1611328
| ```
  y = A*x
  r = sqrt(tr(y-x)*(y-x))
  print(r)
  x = y
}
printsep()
print(x)
``` | |

ex4.mat	Output
| ```
matrix    A[4,4]
vector    x[4]
vector    xy2[4]
scalar    s

A = {0 1 2 3 4 5 6 7 8 9 1 1 1 2 3 4 }
x = {1 1 1 1 }
xy2 = { 2 1 3 1 }

s = tr(x)*A*xy2
print(s)
``` | 94 |

ex5.mat	Output
| ```
# count how many elements are
# greater than or equal to 4
matrix    A[4,4]
scalar    count
scalar    incr
scalar    i
scalar    j

A = {0 1 2 3 4 5 6 7 8 9 1 1 1 2 3 4}
count = 0
for (i,j in 1:4:1,1:4:1) {
    incr  = choose(A[i,j]-4,1,1,0)
    count = count + incr
}
print(count)
``` | 7 |

Grading

Your project will be graded according to the following criteria:

Documentation (written document describing how you implemented your project)	12%
Comments in your code	8%
Implementation and tests	80%

You will be provided with instructions on how to submit your completed project.

Late Submission

If the project is submitted late, the following penalties will be applied:
- 0 < hours late <= 24 :   25%
- 24 < hours late <= 48 :   50%
- hours late > 48 :   100%

Timestamping
Project file should include your names in it. Please timestamp your project file using
https://opentimestamps.org/ before you submit it.   Keep the project file and its corresponding
timestamp .ots file.