

# CS2x1:Data Structures and Algorithms

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# Recap

## ○ Queue (FIFO) Implementation

▪ EnQueue () ✓

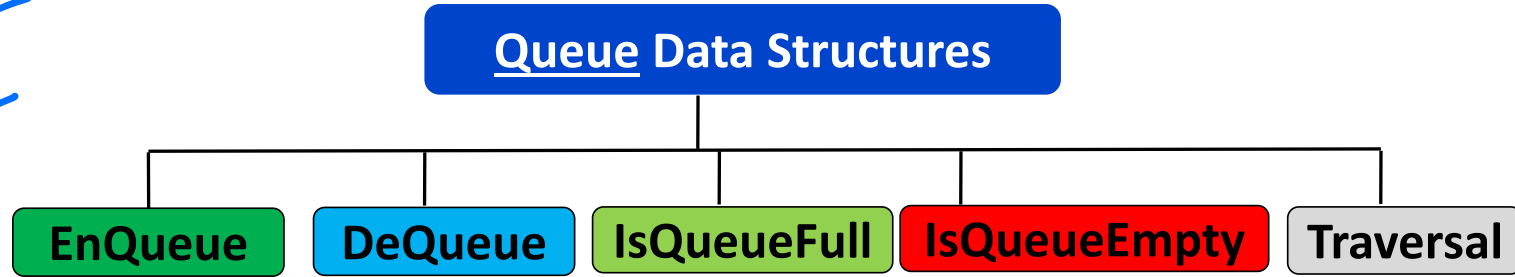
▪ DeQueue () ✓

▪ IsQueueFull ()

▪ IsQueueEmpty ()

▪ PrintQueue ()

## ○ Limitations:



# Outline

- Exercise on Stack and Queue
- Limitations of Queue data structures
- Circular Queue data structures
- Circular Queue operations
- Circular Queue exceptions
- Circular Queue implementation
- Circular Queue applications

**Definition**

**Operations**

**Exceptions**

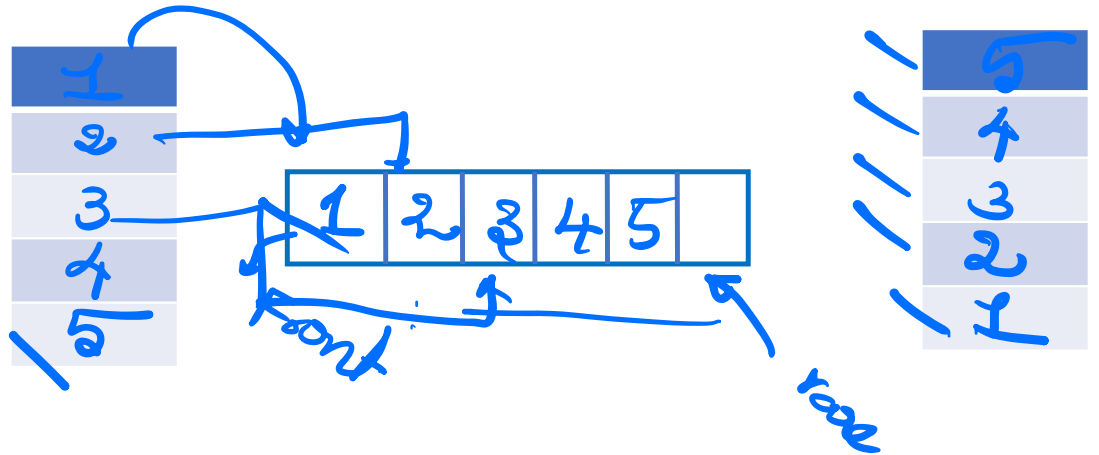
**Implementation**

**Applications**

## Exercise: Stack and Queue (1)

Given a 5 element stack S (from top to bottom: 1,2,3,4,5), and an empty queue Q, remove the elements one-by-one from S and insert them into Q, then remove them one-by-one from Q and re-insert them into S. S now looks like (from top to bottom)?

- (a) 1, 2, 3, 4, 5
- (b) 5, 1, 2, 3, 4
- (c) 5, 4, 3, 2, 1
- (d) 1, 3, 5, 2, 4



## Exercise: Queue (2)

Suppose you are given an implementation of a queue of integers. The operations that can be performed on the queue are:

- i. isEmpty(Q) — returns true if the queue is empty, false otherwise
- ii. Dequeue() — deletes the element at the front of the queue and returns its value.
- iii. Enqueue(Q, i) — inserts the integer  $i$  at the rear of the queue.

Consider the following function:

```
void f(queue Q) {  
    int i;  
    if (!isEmpty(Q)) {  
        i = Dequeue();  
        f(Q);  
        Enqueue(Q, i); }  
}
```

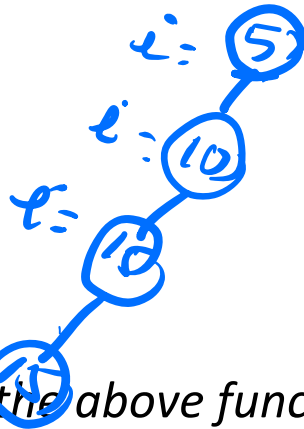
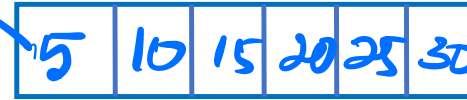
What operation is performed by the above function  $f$ ?

A Leaves the queue  $Q$  unchanged

B Reverses the order of the elements in the queue  $Q$

C Deletes the element at the front of the queue  $Q$  and inserts it at the rear keeping the other elements in the same order

D Empties the queue  $Q$



## Exercise: Stack and Queue (3)

*Which of the following is/are not a valid queue application(s)?*

(a) When printing jobs are submitted to printer → Queue

(b) Lines at tickets counters — Queue

☒ (c) Evaluating a mathematical expression → Stack

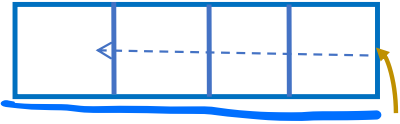
(d) Calls to large companies, when all lines are busy — Queue

# Queue: Limitations (1) *Real*



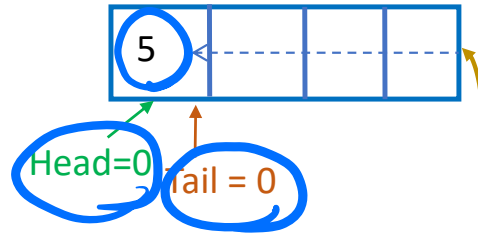
Head = Tail = -1

Q[0] Q[1] Q[2] Q[3]



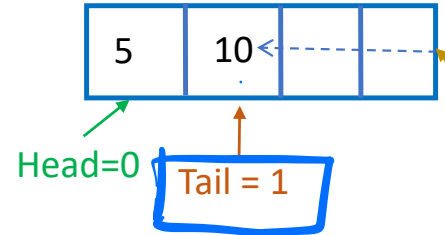
Enqueue (5)

Q[0] Q[1] Q[2] Q[3]



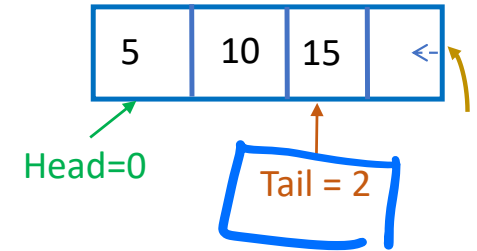
Enqueue (10)

Q[0] Q[1] Q[2] Q[3]



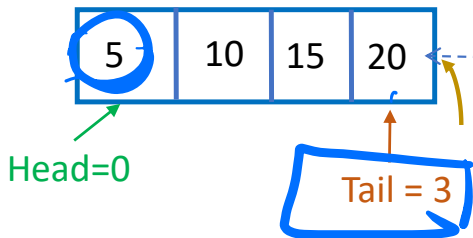
Enqueue (15)

Q[0] Q[1] Q[2] Q[3] Q[4]



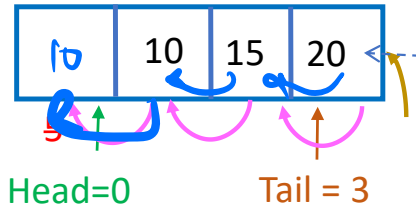
Enqueue (20)

Q[0] Q[1] Q[2] Q[3]



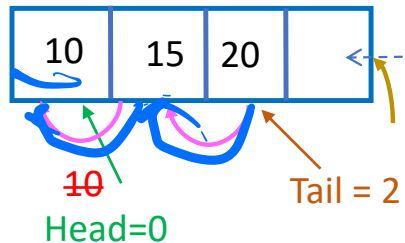
Dequeue ()

Q[0] Q[1] Q[2] Q[3]

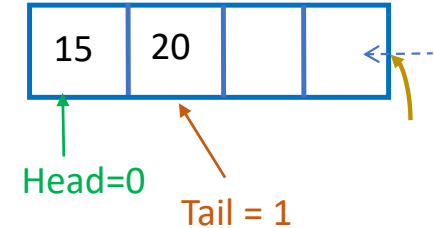


Dequeue ()

Q[0] Q[1] Q[2] Q[3]



Q[0] Q[1] Q[2] Q[3]

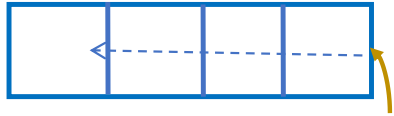


**Inefficient**

# Queue: Limitations (2)

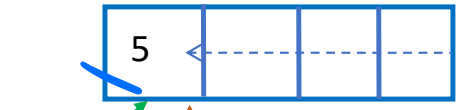
Head = Tail = -1

Q[0] Q[1] Q[2] Q[3]



Enqueue (5)

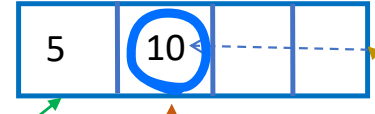
Q[0] Q[1] Q[2] Q[3]



Head=0  
Tail=0

Enqueue (10)

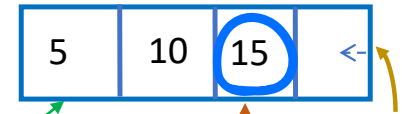
Q[0] Q[1] Q[2] Q[3]



Head=0  
Tail=1

Enqueue (15)

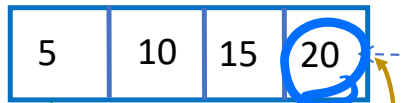
Q[0] Q[1] Q[2] Q[3] Q[4]



Head=0  
Tail=2

Enqueue (20)

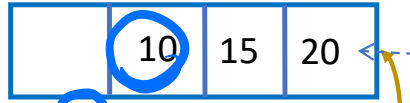
Q[0] Q[1] Q[2] Q[3]



Head=0  
Tail=3

Dequeue ()

Q[0] Q[1] Q[2] Q[3]



Head=1  
Tail=3

Dequeue ()

Q[0] Q[1] Q[2] Q[3]



Head=2  
Tail=3

Dequeue ()

Q[0] Q[1] Q[2] Q[3]



Head=3  
Tail=3

Ineffective: Suffers due to queue is full

$(Tail + 1) \% Queue\_Size$   
Head  
(0 = 3)



# Circular Queue: EnQueue Example

Head = Tail = -1

Qsize = 4

$$0 = 0 \% 4$$

Case 1: Tail = Tail + 1; ✓

Tail = Tail % Qsize;

Queue[Tail] = Val;

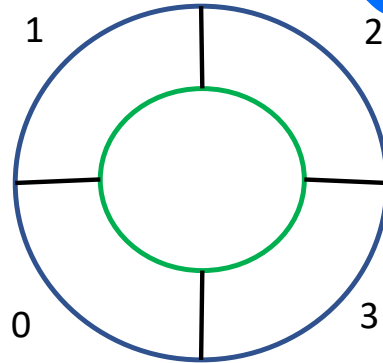
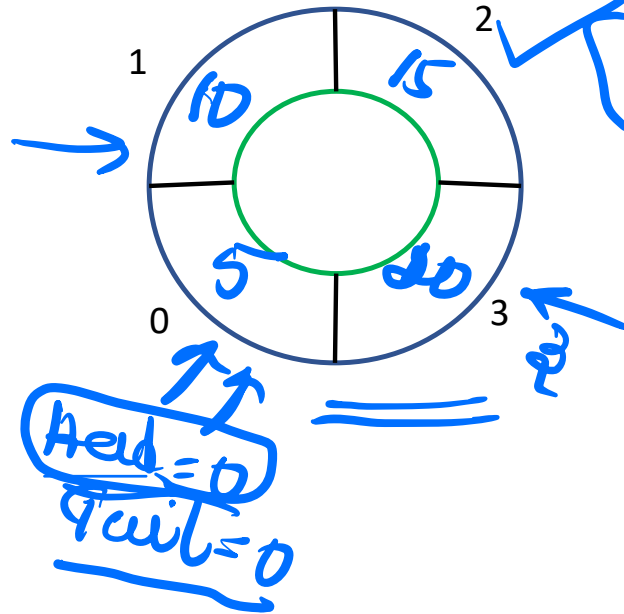
Head = (Tail + 1) % Qsize

if (Head == -1)

Head = Head + 1;

Case 2: if ((Tail + 1) % Qsize == Head)

Overflow;



# Implementation: EnQueue

## Circular Queue Data Structures

EnQueue

DeQueue

IsQueueFull

IsQueueEmpty

Traversal

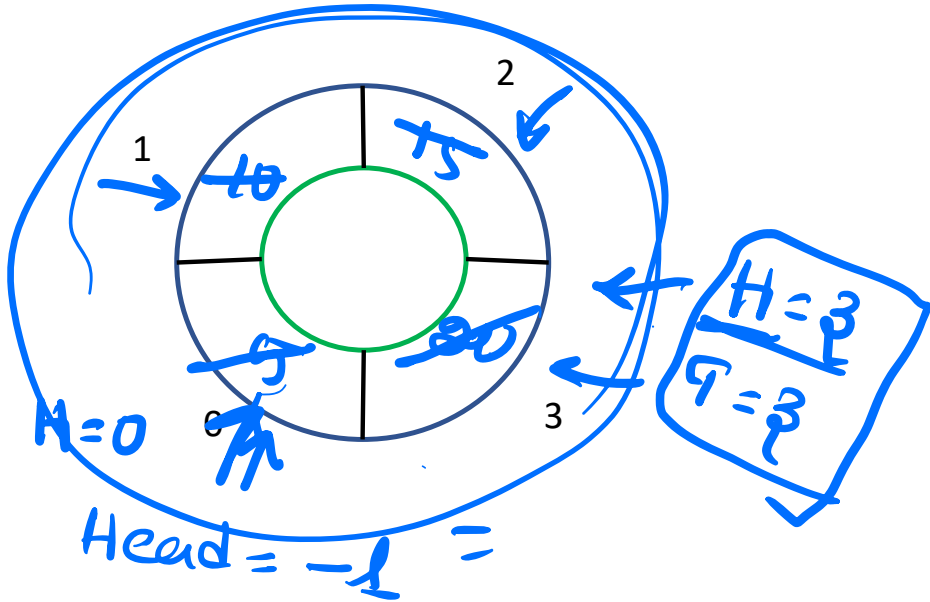
Head = Tail = -1

```
void Enqueue() {
    int Element;
    if (!IsQFull()) {
        printf("Enter the element to be Enqueued...\n");
        scanf("%d", &Element);
        Tail++;
        Tail = Tail % QSize;
        Queue[Tail] = Element;
        if (Head == -1)
            Head++;
    } else
        printf("Element cannot be inserted as Queue is full\n");
}
```

```
int IsQFull() {
    if ((Tail + 1) % QSize == Head)
        return 1;
    else
        return 0;
}
```

# Circular Queue: DeQueue Example

Head = Tail = -1  
QSize = 4



Case 1: *if (Head == -1)*  
*Queue empty;*

Case 2: *if (Tail == Head)*

$Head = -1$   
 $Tail = -1$

Case 3: *if (Tail != Head)*

# Implementation: Circular DeQueue

## Circular Queue Data Structures

Head = Tail = -1

EnQueue

DeQueue

IsQueueFull

IsQueueEmpty

Traversal

```
void Dequeue() {
    if (!IsQEmpty()) {
        if (Head == Tail) {
            /*That means only one element is present*/
            printf("%d is deleted from the queue\n", Queue[Head]);
            Queue[Head] = -1;
            Head = Tail = -1;
        } else {
            printf("%d is deleted from the queue\n", Queue[Head]);
            Queue[Head] = -1;
            Head++;
            Head = Head % QSize;
        }
    } else {
        printf("Element cannot be deleted as Queue is already empty \n");
    }
}
```

```
int IsQueueEmpty() {
    if (Head == -1) {
        return 1;
    } else return 0;
}
```

## Exercise: Circular Queue (1)

A circular queue consists of size 8, and it contains: 10, 20, 30, 50, 50, 60, 80, 70  
[Note: the index starts from 0].

Following operations are performed on the circular queue: Dequeue (), Dequeue (), Enqueue (90), Dequeue (), Enqueue (20)

What are the values at Head and Tail points and the corresponding index values?

- (a) Head -> 30 & 2; Tail -> 70 & 7
- (b) Head -> 50 & 3; Tail -> 70 & 7
- (c) Head -> 50 & 3; Tail -> 90 & 1
- ☒ (d) Head -> 50 & 3; Tail -> 20 & 1



## Exercise: Circular Queue (2)

Given a circular queue with size 7. What is the final value at index 2, after the following code is executed:

[Note: the circular queue array index starts at 0]

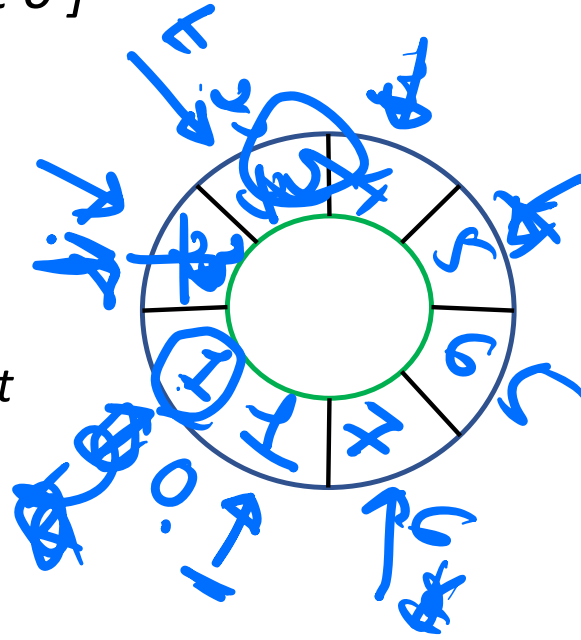
```
for (int k = 1; k <= 7; k++){  
    EnQueue(k);  
}  
for (int k = 1; k <= 5; k++){  
    int delete; //to store the dequeued/deleted element  
    delete = DeQueue();  
    EnQueue(delete);  
    Dequeue();  
}
```

(a) 4

(b) 3

(c) 5

(d) 7



## Exercise: Circular Queue (3)

Suppose a circular queue of capacity  $(n - 1)$  elements is implemented with an array of  $n$  elements. Assume that the insertion and deletion operation are carried out using REAR and FRONT as array index variables, respectively.

Initially,  $REAR = FRONT = 0$ . The conditions to detect queue full and queue empty are:

(A) Full:  $(REAR+1) \bmod n == FRONT$ , empty:  $REAR == FRONT$

(B) Full:  $(REAR+1) \bmod n == FRONT$ , empty:  $(FRONT+1) \bmod n == REAR$

(C) Full:  $REAR == FRONT$ , empty:  $(REAR+1) \bmod n == FRONT$

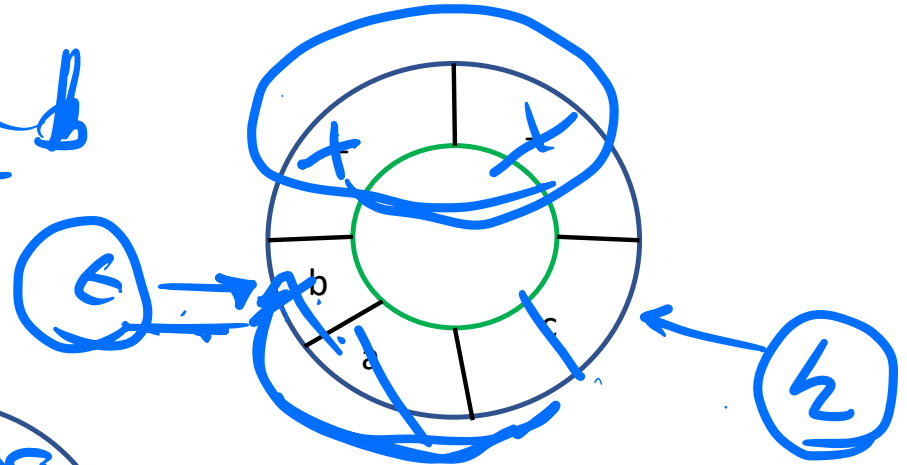
(D) Full:  $(FRONT+1) \bmod n == REAR$ , empty:  $REAR == FRONT$

# Exercise: Circular Queue (4)

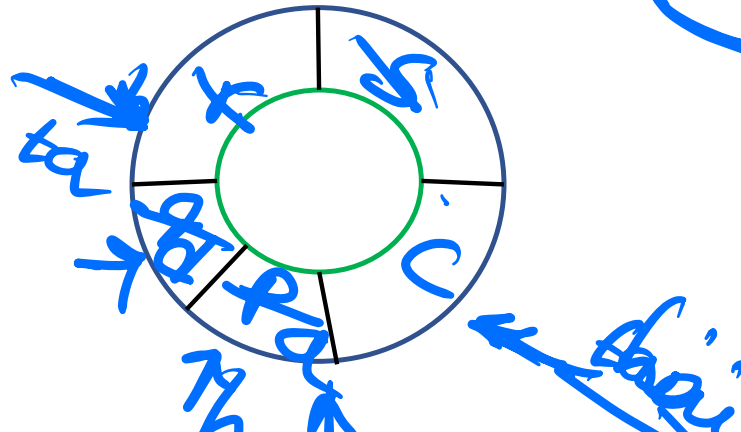
What is status of states of queue contents after the following sequence of steps

Enqueue x  
Dequeue  
Enqueue y  
Dequeue  
Dequeue

p q r s ca b



- a) x, y, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_
- b) x, \_\_\_\_\_, y, \_\_\_\_\_, \_\_\_\_\_
- c) \_\_\_\_\_, \_\_\_\_\_, x, y, \_\_\_\_\_
- d) \_\_\_\_\_, x, y, \_\_\_\_\_, \_\_\_\_\_







# thank you!

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**NEXT** Class: 26/04/2022