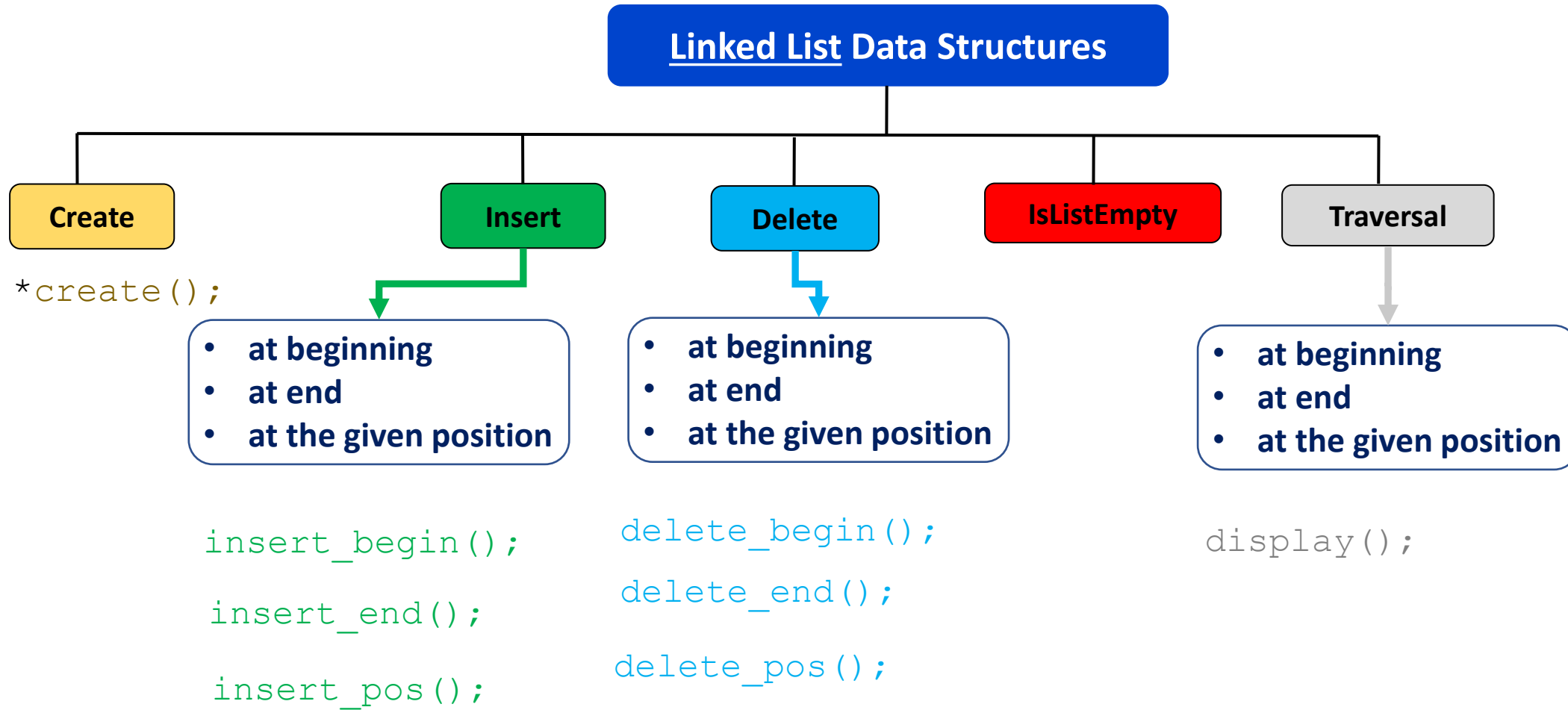


CS2x1:Data Structures and Algorithms

Koteswararao Kondepu

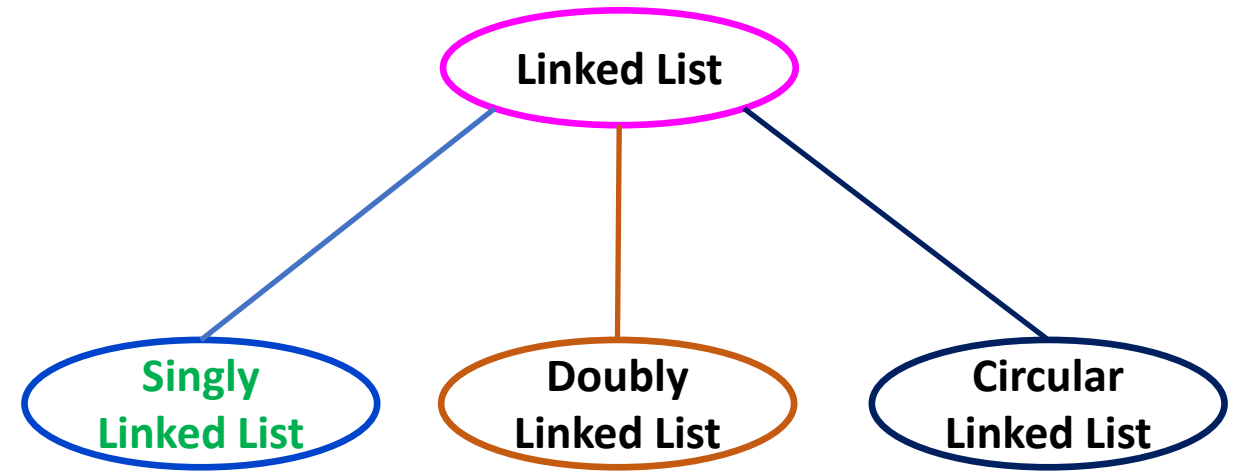
k.kondepu@iitdh.ac.in

Recap: Linked List Operations



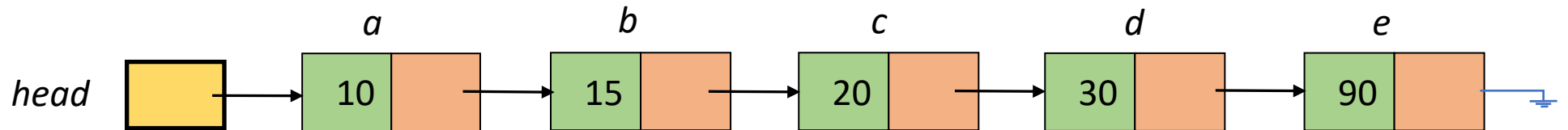
Outline

- Limitation of Singly Linked List
- Exercise on Singly Linked List
- Doubly Linked List Operations
- Exercise on Doubly Linked List
- Circular Linked List Operations
- Exercise on Circular Linked List



Exercise: Singly Linked List (1)

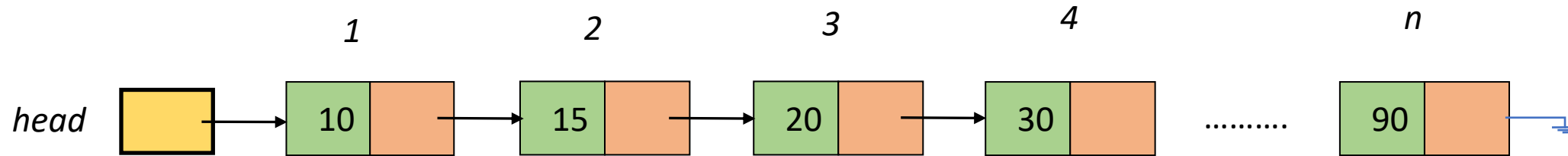
```
struct sll{
    int data;
    struct sll *next;
};
int a[5];
void cs201()
{
    struct sll *sllnewnode=malloc(sizeof(struct sll));
    printf("%d\n", sizeof(a));
    printf("%d\n", sizeof(sllnewnode));
    printf("%d\n", sizeof(sllnewnode)*5);
}
int main() {
    cs201();
    return 0;
}
```



Linked Lists may use more memory than the arrays

Exercise: Singly Linked List (2)

```
struct sll{  
    int data;  
    struct sll *next;  
};  
int a[5]= {10, 15, 20, 25, 30};
```



What is the time taken to access the k^{th} element in the given array and the given linked list?

- (i) $O(1)$; $O(1)$
- (ii) $O(k)$; $O(k)$
- (iii) $O(1)$; $O(k)$
- (iv) $O(k)$; $O(1)$

Nodes are stored *in-contiguously*, the time required to access individual elements greatly increased within the list

Exercise: Singly Linked List (3)

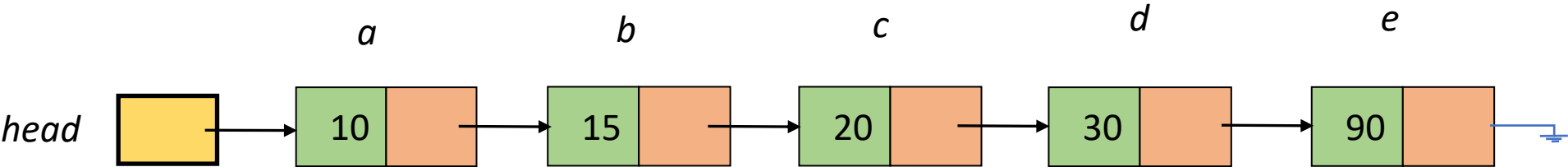
```
struct sll{
    int data;
    struct sll *next;
};
int a[5]= {10, 15, 20, 25, 30};

printf("%d\n", a);
printf("%d\n", a+1);
printf("%d\n", a+2);
printf("%d\n", a+3);
printf("%d\n", a+4);
```

30	4
25	3
20	2
15	1
10	0

&a=8288

Nodes are not stored in-contiguously, the time required to access individual elements greatly increased within the list



```
void create(){
    struct sll *aa=malloc(sizeof(struct sll));
    printf("%ld\n", aa);
}
```

```
create();
create();
create();
create();
create();
```

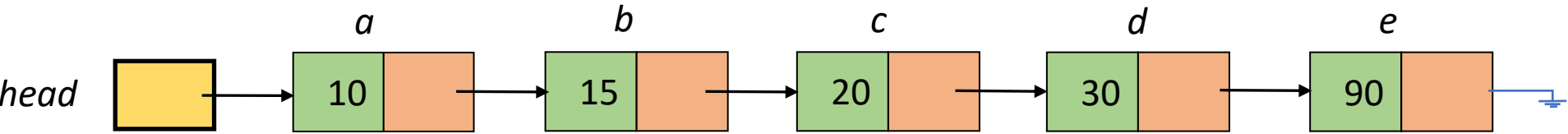
Exercise: Singly Linked List (4)

```
struct sll{
    int data;
    struct sll *next;
};
int a[5]= {10, 15, 20, 25, 30};

printf("%d\n", *(a+4));
printf("%d\n", *(a+3));
printf("%d\n", *(a+2));
printf("%d\n", *(a+1));
printf("%d\n", *a);
```

	30	4
	25	3
	20	2
	15	1
&a=8288	10	0

Difficulties arises in linked-list when it comes to reverse traversing



```
void create(){
    struct sll *aa=malloc(sizeof(struct sll));
    printf("%ld\n", aa);
}

create();
create();
create();
create();
```

```
struct node *tail
tail = head;
while ( tail -> next != NULL)
    tail = tail -> next
```

Exercise: Singly Linked List (4)

Consider the following function to traverse a linked:

```
void traverse(struct Node *head)
{
    while (head->next != NULL)
    {
        printf("%d ", head->data);
        head = head->next;
    }
}
```

Which of the following is FALSE about above function?

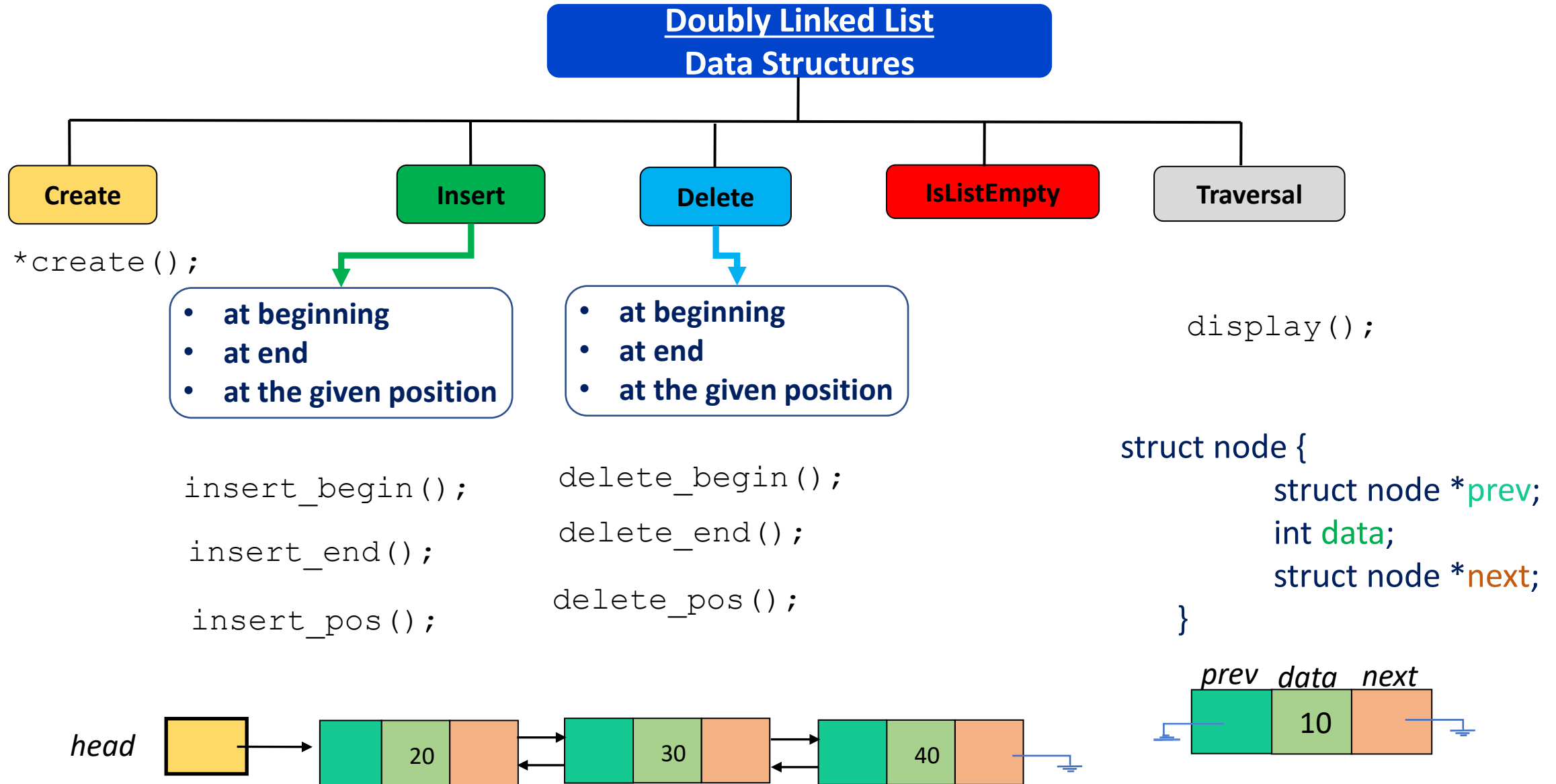
- A. The function may crash when the linked list is empty
- B. The function doesn't print the last node when the linked list is not empty
- C. The function is implemented incorrectly because it changes head
- D. All of the above

Limitations: Singly Linked List

- Limitations:

- a) Linked Lists may use more memory than the arrays
- b) Nodes in a linked-list are accessed in order from beginning, thus the linked lists are inherently sequential access → **no direct access**
- c) Nodes are stored in-contiguously, the time required to access individual elements greatly increased within the list
- d) Difficulties arises in linked-list when it comes to reverse traversing

Doubly Linked List: Operations

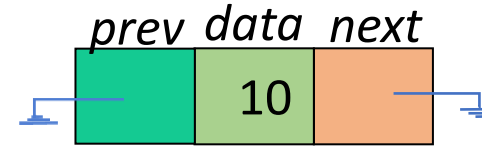


Doubly Linked List: Insert at the beginning or Insert at the head

Steps:

(i) Creating a node with data

newnode



struct node {

struct node **prev*;

int *data*;

struct node **next*;

}

*struct node *newnode = malloc (sizeof (struct node));*

newnode → data = 10; //Entering data

newnode → next = NULL; //making node next to NULL

newnode → prev = NULL;



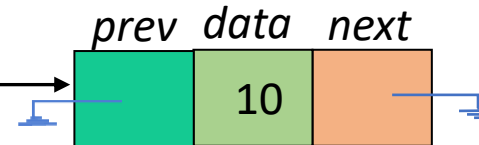
*struct node *head = NULL*

(ii) Adding a node to an empty linked list

if (head == NULL)

head = newnode

newnode

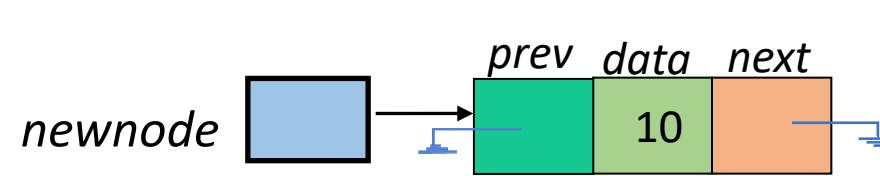


head



Doubly Linked List: Insert at the beginning or Insert at the head

Steps:



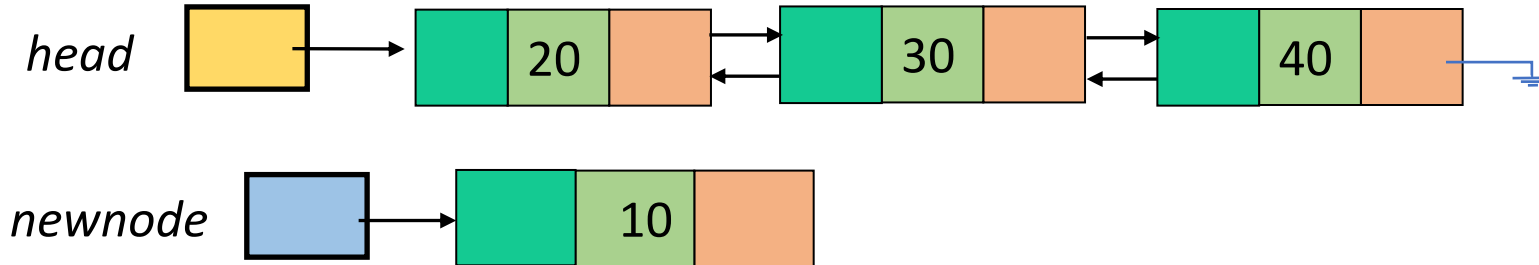
```
struct node {  
    struct node *prev;  
    int data;  
    struct node *next;  
}
```

(iii) Adding a node to the beginning of a linked list

a) Update the next pointer of new node → the current head, and the current head previous → new node

newnode → next = head

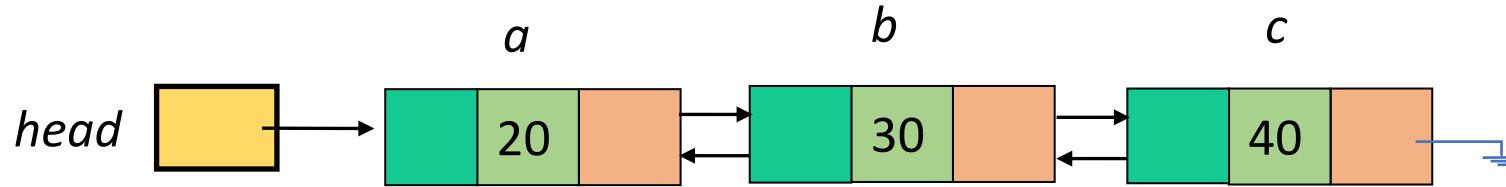
head → prev = newnode



b) Update the head pointer to the new node

head = newnode

Doubly Linked List: Example



- $head \rightarrow data = ?$
- $head \rightarrow next \rightarrow next \rightarrow data = ?$
- $c \rightarrow prev \rightarrow prev \rightarrow data = ?$
- $head \rightarrow next \rightarrow next \rightarrow next \rightarrow data = ?$
- $c \rightarrow prev \rightarrow prev \rightarrow prev \rightarrow data = ?$

Doubly Linked List: traversal or display

Steps:

(i) Check if the linked list empty or not

```
if (head == NULL)
    printf ("Linked List is Empty\n");
```

head  *struct node *head = NULL*

(ii) List Traversal: Each node present in the list must be visited and display the data value



① *struct node *traversal traversal* 

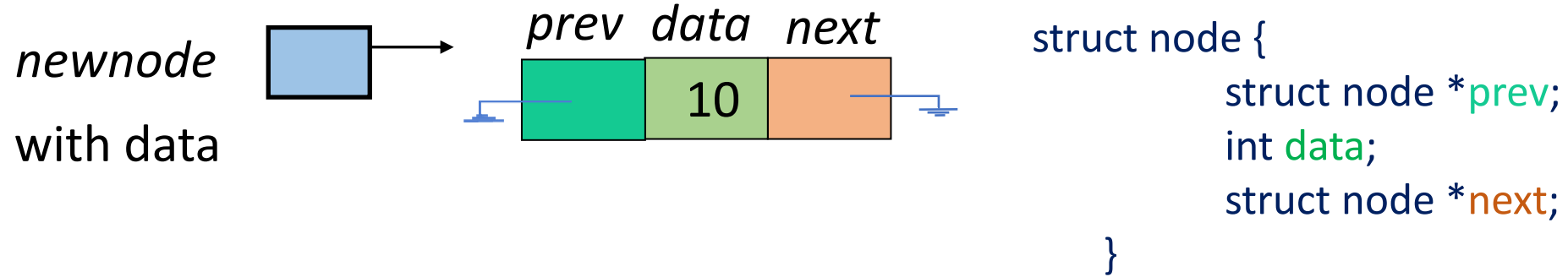
② *traversal = head;*

③ *while (traversal != NULL)*
 display the element: traversal → data
 traversal = traversal → next

Doubly Linked List: Insert at the end or Insert at the tail

Steps:

(i) Creating a node with data



(ii) Adding a node to at the end of a linked list

a) Traversal the list till the tail pointer

*struct node *tail*

newnode



tail = head;

while (tail → next != NULL)

tail = tail → next

head



tail



b) tail node pointer points to the new node

tail → next = newnode

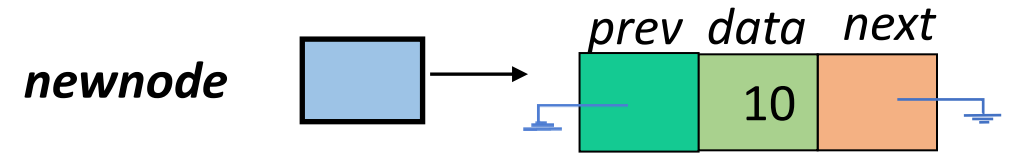
c) **new node prev pointer points to the tail node**

newnode → prev = tail

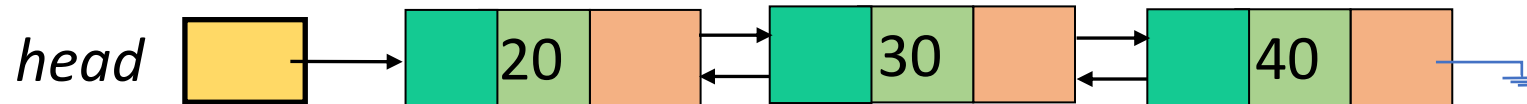
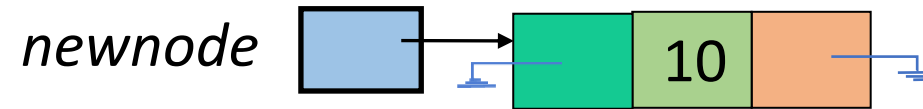
Doubly Linked List: Insert at the given position

Steps:

(i) Creating a node with data



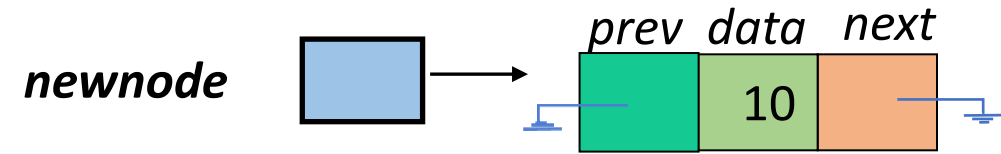
(ii) Adding a node to at the given position



Doubly Linked List: Insert at the given position

Steps:

(i) Creating a node with data



(ii) Adding a node to at the given position

a) Traversal the list till the *position - 1*

*struct node *position*

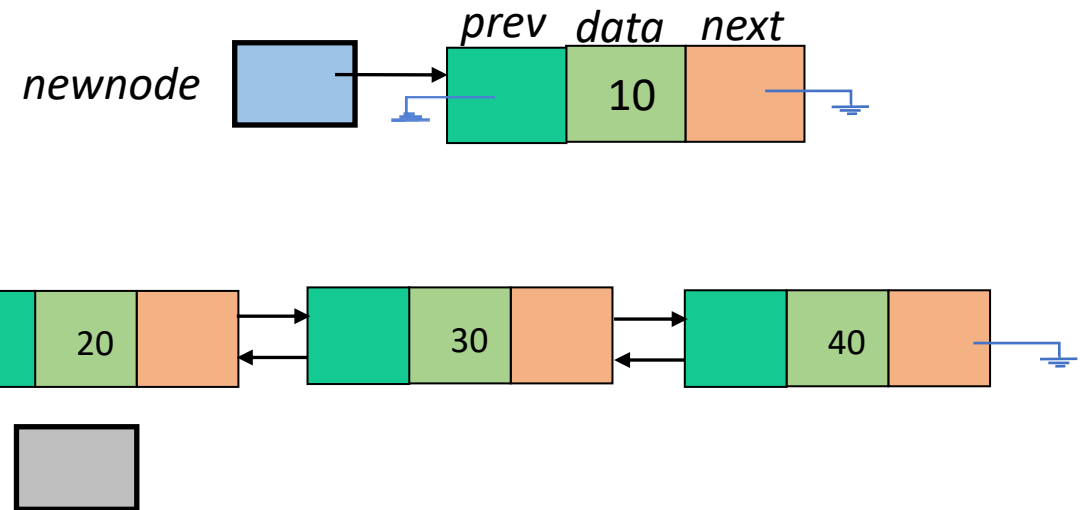
position = head

i = 0

while (i < pos-1)

position = position → next

i++;



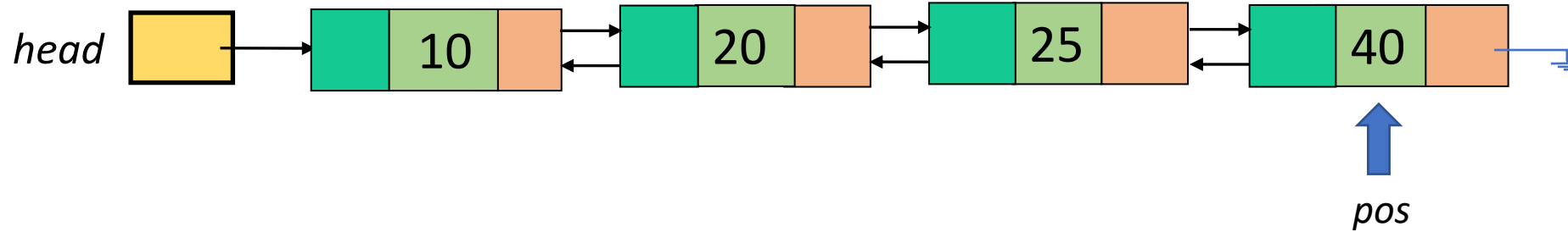
b) Point new node *prev* to the position node and *next* to the next node of the position node

① *newnode → prev = position;* ② *newnode → next = position → next*

c) Point position next *prev* to the newnode and position next to the new node

③ *position → next → prev = newnode;* ④ *position → next = newnode*

Exercise: Doubly Linked List (1)



```
struct node {  
    struct node *prev;  
    int data;  
    struct node *next;  
}
```

Q: Insert the given newnode after the provided position?

Note: (i) multiple options are possible

(ii) the order of the given instructions are to be followed



```
struct node *newnode = malloc(sizeof(struct node));
```

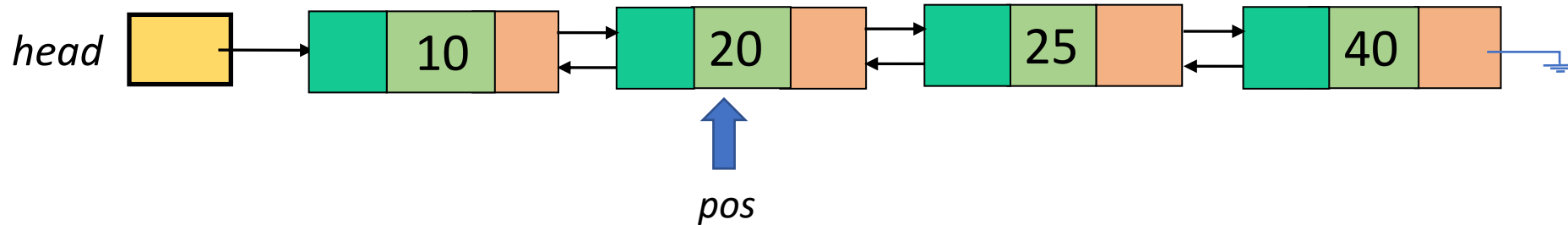
(a) *newnode* → *next* = *pos*
pos → *next* = *newnode*
newnode → *prev* = NULL

(c) *newnode* → *prev* = *pos*
pos → *next* = *newnode*
newnode → *next* = NULL

(b) *pos* → *next* = *newnode*
newnode → *prev* = *pos*
newnode → *next* = NULL

(d) *newnode* → *prev* = NULL
newnode → *next* = *pos*
pos → *next* = *newnode*

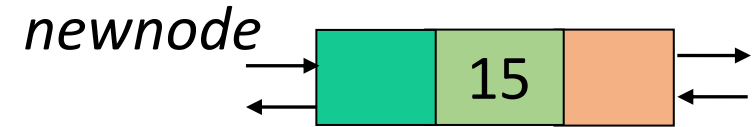
Exercise: Doubly Linked List (2)



```
struct node {  
    struct node *prev;  
    int data;  
    struct node *next;  
}
```

Q: Insert the given newnode before the provided position?

Note: the order of the given instructions are to be followed



(a) $\text{newnode} \rightarrow \text{next} = \text{pos}$

$\text{newnode} \rightarrow \text{prev} = \text{pos} \rightarrow \text{prev}$

$\text{pos} \rightarrow \text{prev} \rightarrow \text{next} = \text{newnode}$

$\text{pos} \rightarrow \text{prev} = \text{newnode}$

$\text{struct node } * \text{newnode} = \text{malloc}(\text{sizeof}(\text{struct node}));$

(c) $\text{pos} \rightarrow \text{prev} \rightarrow \text{next} = \text{newnode}$

$\text{newnode} \rightarrow \text{prev} = \text{pos} \rightarrow \text{prev}$

$\text{pos} \rightarrow \text{prev} = \text{newnode}$

$\text{pos} \rightarrow \text{prev} \rightarrow \text{next} = \text{newnode}$

(b) $\text{pos} \rightarrow \text{prev} \rightarrow \text{next} = \text{newnode}$

$\text{pos} \rightarrow \text{prev} = \text{newnode}$

$\text{newnode} \rightarrow \text{prev} = \text{pos} \rightarrow \text{prev}$

$\text{pos} \rightarrow \text{prev} \rightarrow \text{next} = \text{newnode}$

(d) $\text{newnode} \rightarrow \text{prev} = \text{pos}$

$\text{newnode} \rightarrow \text{next} = \text{pos} \rightarrow \text{next}$

$\text{pos} \rightarrow \text{next} \rightarrow \text{prev} = \text{newnode}$

$\text{pos} \rightarrow \text{next} = \text{newnode}$

Doubly Linked List: delete at the beginning or delete at the head

Steps:

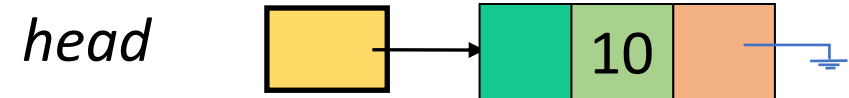
(i) Deleting a node from the empty list



```
If (head == NULL)
    printf("List is Empty\n")
```

(ii) Deleting a node at the beginning of linked list when only one node exist

```
struct node *delbegin
```



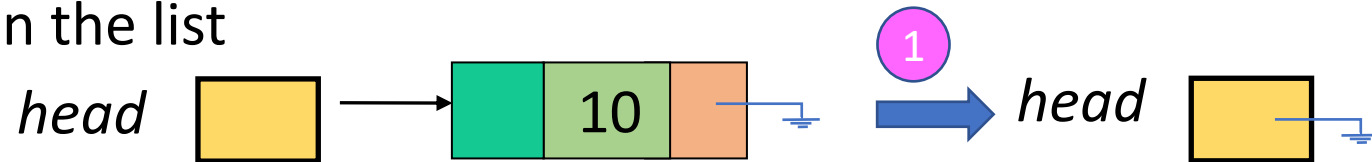
a) Point the head node to the delete pointer

```
delbegin = head
```



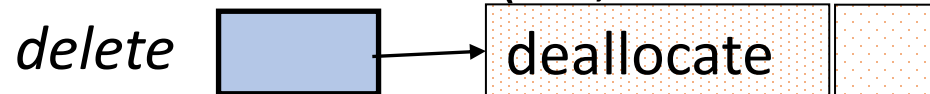
b) delete the node in case of single node in the list

```
If (head → next == NULL)
    head = head → next
```



c) physically deleting the node from the node (i.e., return the allocated node memory to head)

```
free (delbegin)
```



Doubly Linked List: delete at the beginning or delete at the head

Steps:

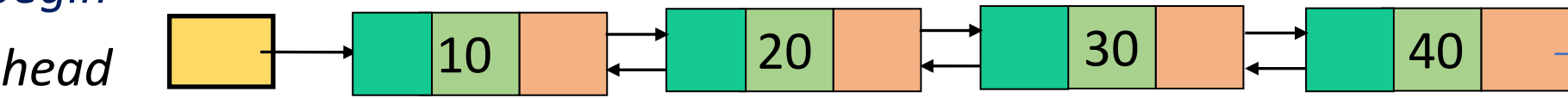
(i) Deleting a node from the empty list



(ii) Deleting a node at the beginning of linked list

a) Point the head node to the delete pointer

*struct node *delbegin*



b) point head to next node of the head and *head prev* to NULL

delbegin = head

delbegin



1

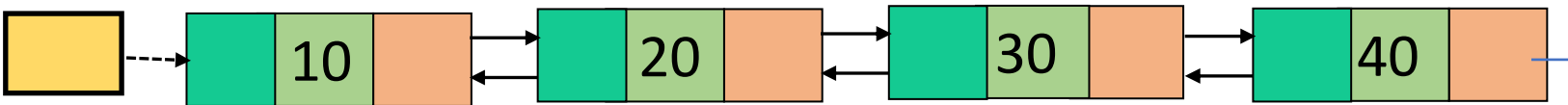
head = head → next

2

head → prev = NULL

c) physically deleting the node from the node (i.e., return the allocated node memory to head)

head



free (delete)

delete



Doubly Linked List: delete at the end or delete at the tail

Steps:

(i) Deleting a node from the linked list with one node

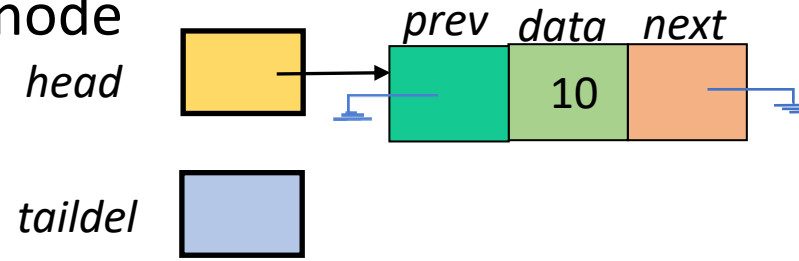
```
struct node *taildel
```

```
taildel = head
```

```
If (head → next == NULL)
```

```
    head = NULL
```

```
    free (taildel)
```

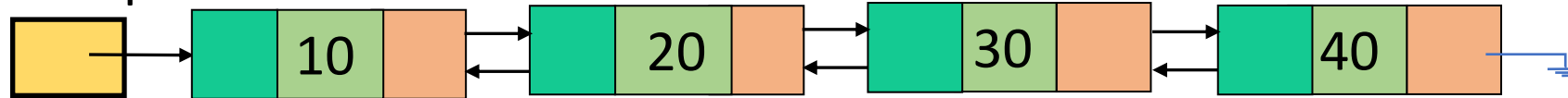


(ii) Deleting a node at the end of linked list

a) Point the head to the delete pointer

```
taildel = head
```

```
head
```

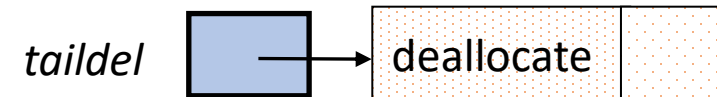


b) Traversal to the tail node

```
while ( tail → next != NULL)
```

```
    tail = tail → next
```

```
taildel → prev → next = NULL
```



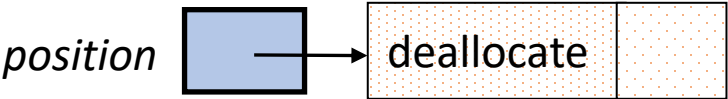
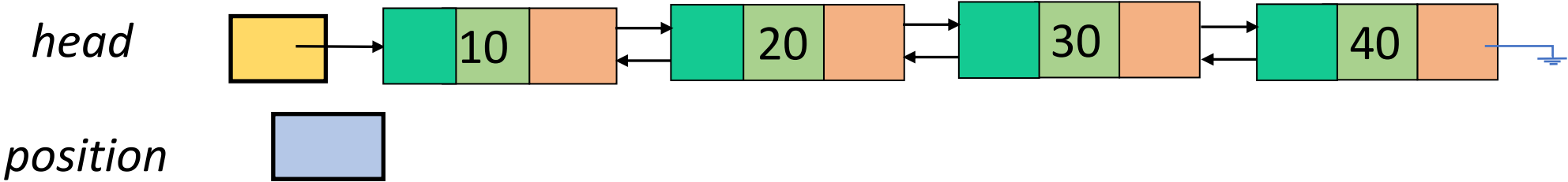
c) free tail node

```
free (taildel)
```

Linked List: delete at the given position



Steps:



Linked List: delete at the given position

Steps:

(iii) Deleting a node at the given position

a) Traversal the list till the *position - 1*

*struct node *position*

position = head

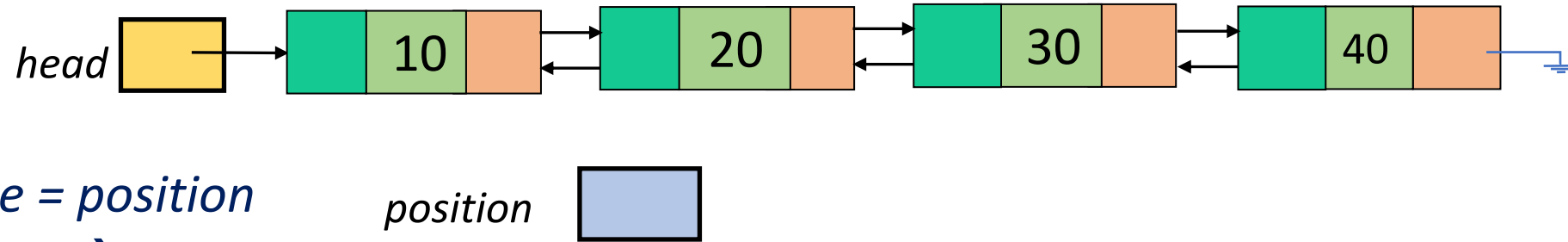
i = 0

while (i < pos)

positionprevnode = position

position = position → next

i++;



① *position → next → prev = position → prev;*

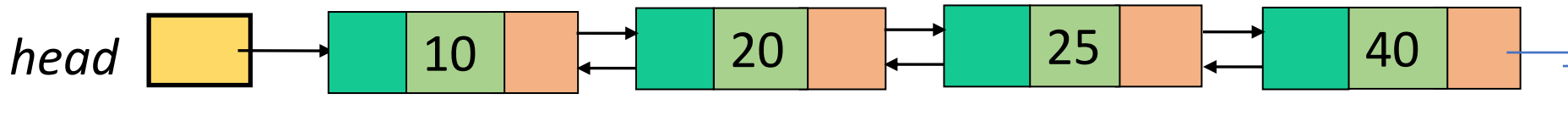
② *position → prev → next = position → next*

Note: assume the position is not the first and last position

free (position)



Exercise: Doubly Linked List (3)



```
struct node {  
    struct node *prev;  
    int data;  
    struct node *next;  
}
```

Q: Map the node delete options?

Note: the order of the given instructions are to be followed

```
struct node *delnode = malloc(sizeof(struct node));
```

(a) $pos \rightarrow prev \rightarrow next = NULL$

(i) To delete the first node of the given list

(b) $head = head \rightarrow next$
 $head \rightarrow prev = NULL$

(ii) To delete the last node of the given list

(c) $pos \rightarrow prev \rightarrow next = pos \rightarrow next$
 $pos \rightarrow next \rightarrow prev = pos \rightarrow prev$

(iii) To delete the node after the given position (*pos*)

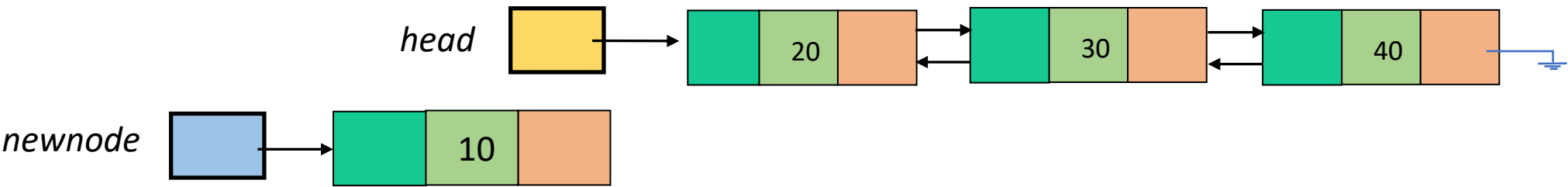
(d) $pos \rightarrow next \rightarrow next \rightarrow pre = pos$
 $pos \rightarrow next = pos \rightarrow next \rightarrow next$

(iv) To delete the node from the given position (*pos*)

Exercise: Doubly Linked List (4)

Q: Fill the following table with the number of pointer operations need to be changed for each doubly linked list operation ?

Operations	begin	end	Middle (pos)
Insert			
delete			



(a) $newnode \rightarrow next = head$
 $head \rightarrow prev = newnode$
 $newnode \rightarrow prev = NULL$
 $head = newnode$

(b) $newnode \rightarrow prev = pos$
 $pos \rightarrow next = newnode$
 $newnode \rightarrow next = NULL$

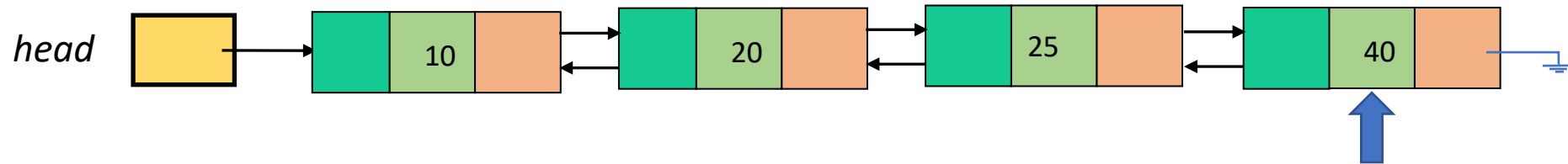
(c) $newnode \rightarrow next = pos$
 $newnode \rightarrow prev = pos \rightarrow prev$
 $pos \rightarrow prev \rightarrow next = newnode$
 $pos \rightarrow prev = newnode$

Limitations: Doubly Linked List

```
struct node {  
    struct node *prev;  
    int data;  
    struct node *next;  
}
```

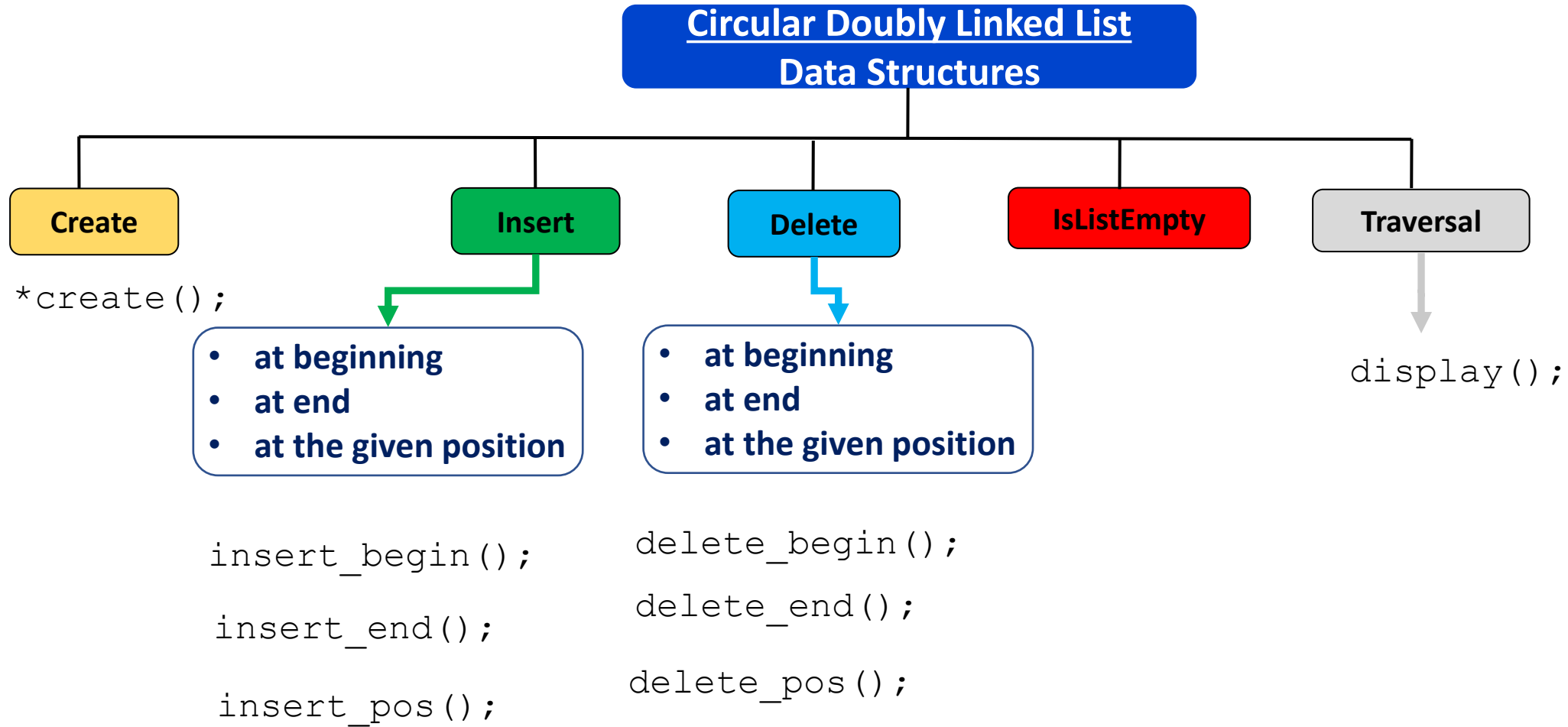
○ Limitations:

- a) Each node requires an extra pointer → more space
- b) More operations required to add new node or delete node → requires an additional care to avoid loops



- c) Traversal to the last node → find a last node in the given linked list
- d) Requires an additional time for reverse traversing

Circular Doubly Linked List: Operations



Circular Doubly Linked List: Insert at the beginning or Insert at the head

Steps:

(i) Creating a node with data

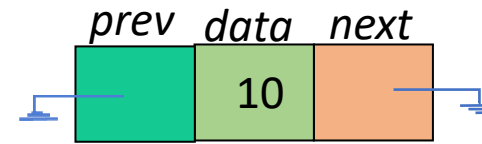
```
struct node *newnode = malloc (sizeof (struct node));
```

```
newnode → prev = NULL;
```

```
newnode → data = 10; //Entering data
```

```
newnode → next = NULL; //making node next to NULL
```

newnode



struct node {

struct node *prev;

int data;

struct node *next;

}

head



struct node *head = NULL

(ii) Adding a node to an empty linked list

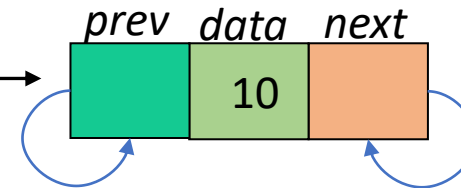
```
if (head == NULL)
```

```
head = newnode
```

```
newnode → prev = head;
```

```
newnode → next = head;
```

newnode



head



Exercise: Operation → Adding a node to an empty list

Q: Map the following linked lists “to insert an element to empty list”:

*(i) newnode → prev = head;
newnode → next = head;*

(a) Single Linked List

*(ii) newnode → prev = NULL;
newnode → next = NULL;*

(b) Circular Single Linked List

(iii) newnode → next = NULL;

(c) Doubly Linked List

(iv) newnode → next = head;

(d) Circular Doubly Linked List

Circular Doubly Linked List: Insert at the beginning or Insert at the head

Steps:

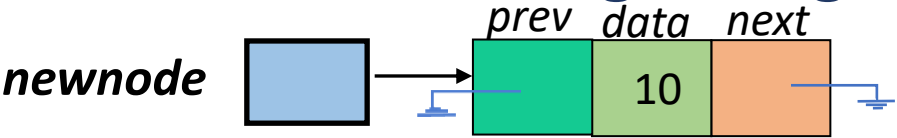
(i) Creating a node with data

```
struct node *newnode = malloc(sizeof(struct node));
```

```
newnode → prev = NULL;
```

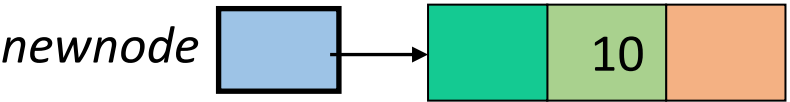
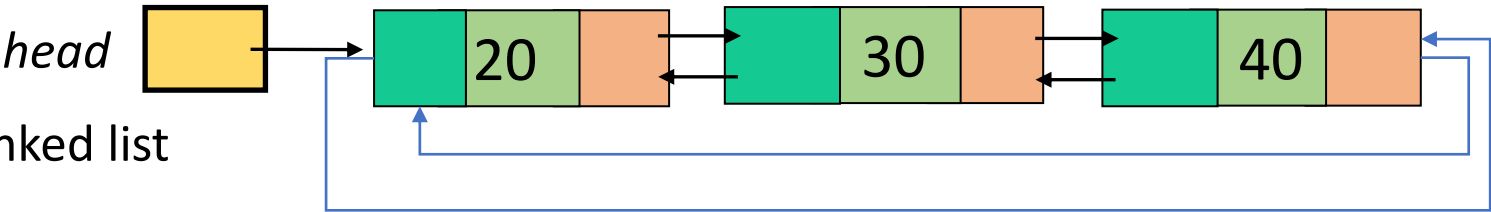
```
newnode → data = 10;
```

```
newnode → next = NULL;
```



```
struct node {  
    struct node *prev;  
    int data;  
    struct node *next;  
}
```

(ii) Adding a node to the beginning of a linked list



Circular Doubly Linked List: Insert at the beginning or Insert at the head

Steps:

(i) Traversal the list till the last node pointing to the head



newnode



head



begin

*struct node *begin*

begin = head → prev

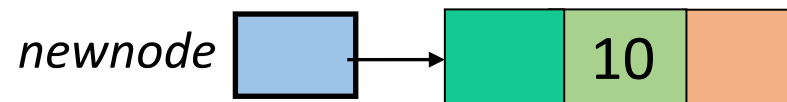
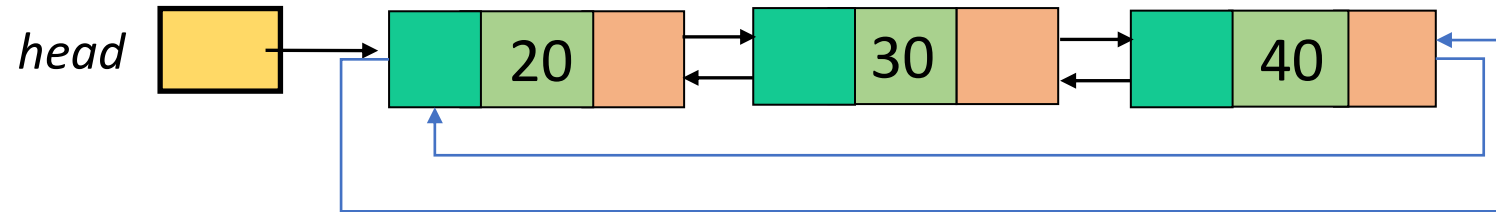
① *begin->next = newnode;*

② *newnode->prev=begin;*

③ *head->prev=newnode;*

④ *newnode->next=head;*

⑤ *head=newnode;*



Circular Doubly Linked List: traversal or display

Steps:

(i) Check if the linked list empty or not

```
if (head == NULL)
    printf ("Linked List is Empty\n");
```

head  \rightarrow `struct node *head = NULL`

(ii) List Traversal: Each node present in the list must be visited and display the data value

① `struct node *traversal`


② `traversal = head;`

traversal 

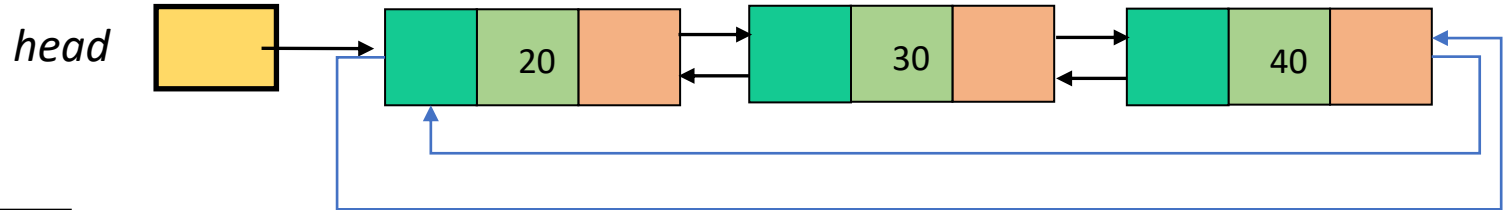
③ `while (traversal \rightarrow next \neq head)`

display the element: traversal \rightarrow data

traversal = traversal \rightarrow next

traversal \neq NULL 

④ ***display the last element: traversal \rightarrow data***



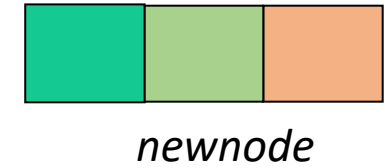
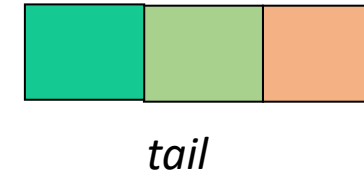
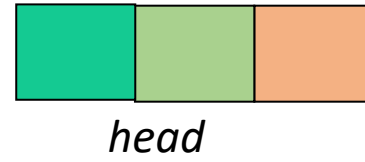
Circular Doubly Linked List: Insert at the end or Insert at the tail

Steps:

(i) Traversal the list till the last node pointing to the head

*struct node *tail*

tail = head → prev

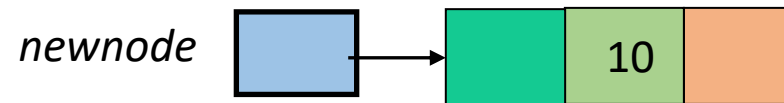
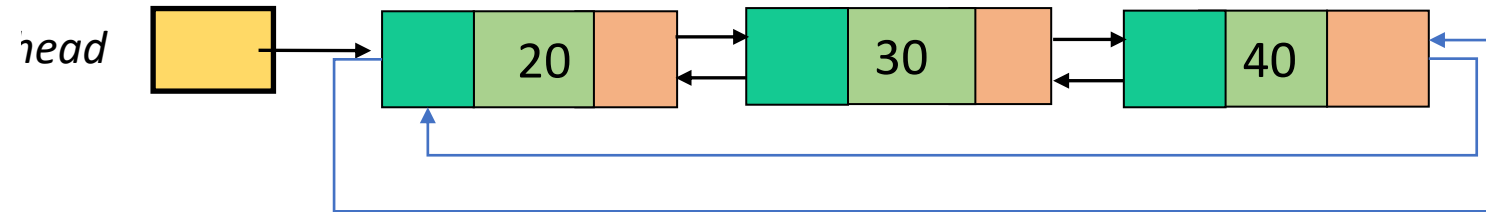


① *tail->next = newnode;*

② *newnode->prev = tail;*

③ *head->prev = newnode;*

④ *newnode->next = head;*



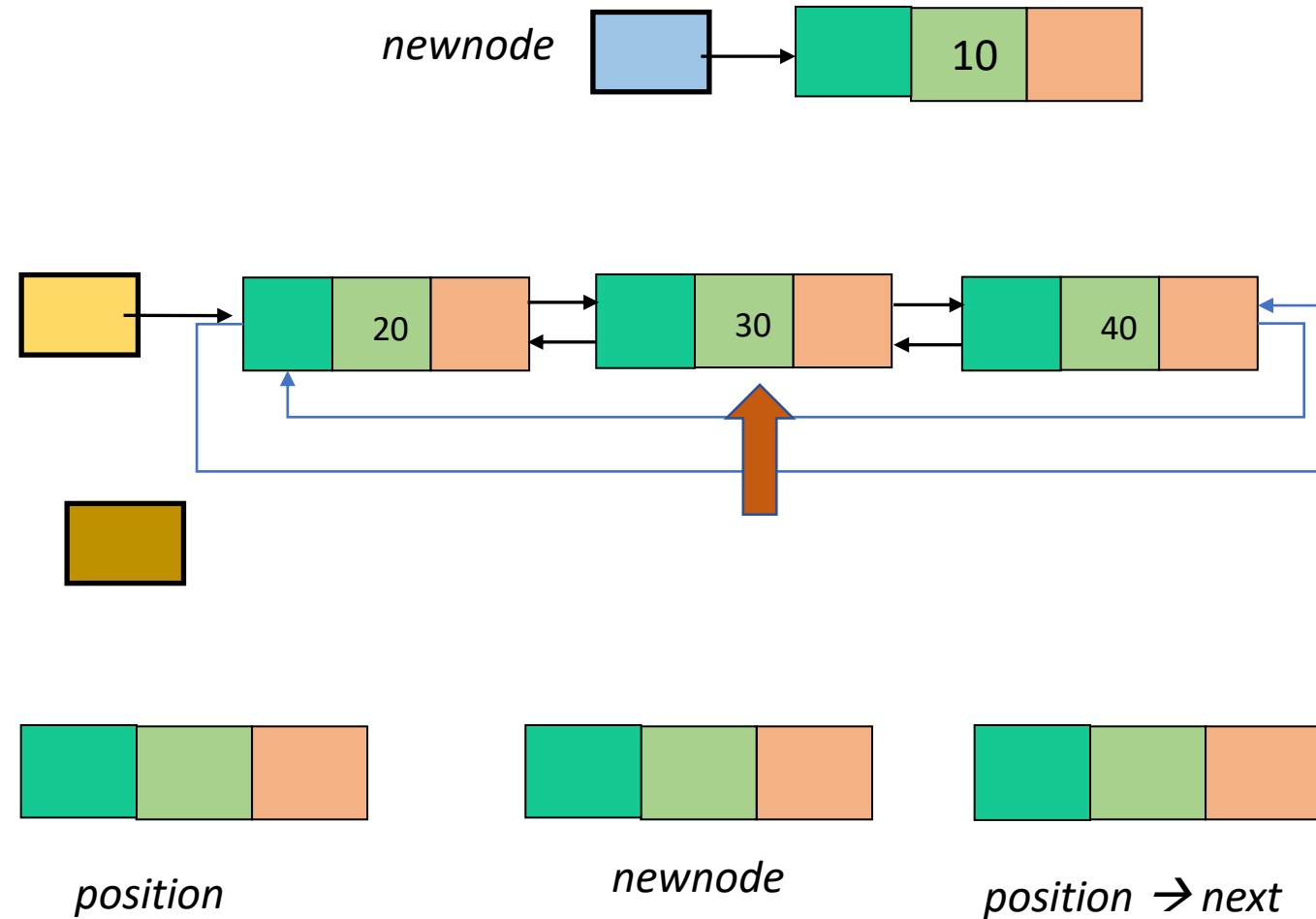
Circular Doubly Linked List: Insert at the given position

Steps:

(i) Traversal the list till the last node pointing to the head

*struct node *position*

- ① *newnode* \rightarrow *prev* = *position*;
- ② *newnode* \rightarrow *next* = *position* \rightarrow *next*;
- ③ *position* \rightarrow *next* \rightarrow *prev* = *newnode*;
- ④ *position* \rightarrow *next* = *newnode*;



Circular Doubly Linked List: delete at the begin

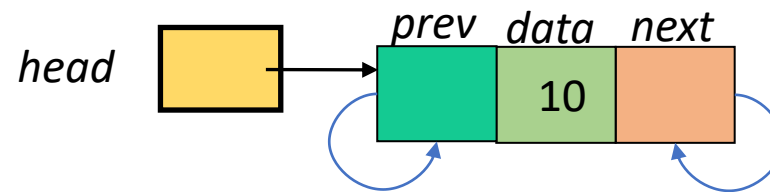
Steps:

(i) If list is empty

```
if (head == NULL)
    printf ("List is empty\n");
```

(ii) If the list contain only one node

```
struct node *delbegin
if (head → next == head )
    delbegin=head;
    head == NULL;
    //print the deleted node data
    free (delbegin)
```

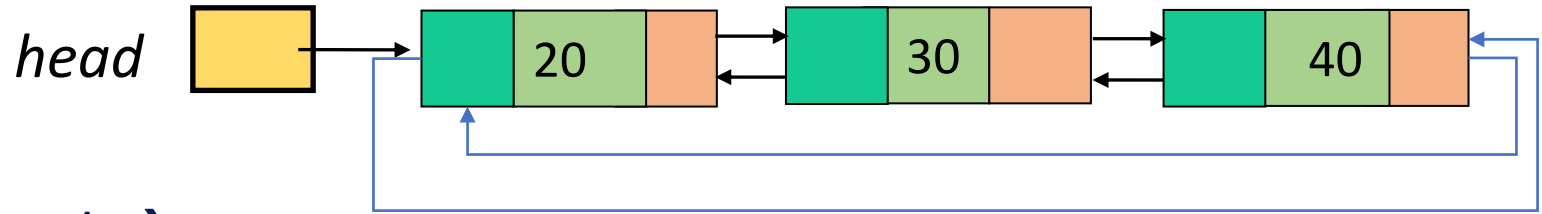


Circular Doubly Linked List: delete at the begin

Steps:

(iii) If the list contain more than one node

*struct node *delbegin*



① $head \rightarrow next \rightarrow prev = head \rightarrow prev;$

② $head \rightarrow prev \rightarrow next = head \rightarrow next;$

③ $head = head \rightarrow next;$

④ $free(delbegin)$



head



$head \rightarrow next$



$head \rightarrow prev$

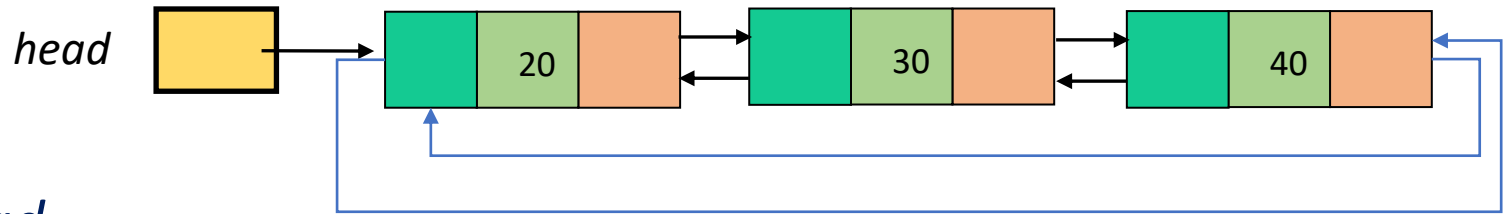
Circular Doubly Linked List: delete at the end

Steps:

(iv) If the list contain more than one node

*struct node *deltail*

deltail = head → prev



① *deltail → prev → next = head;*

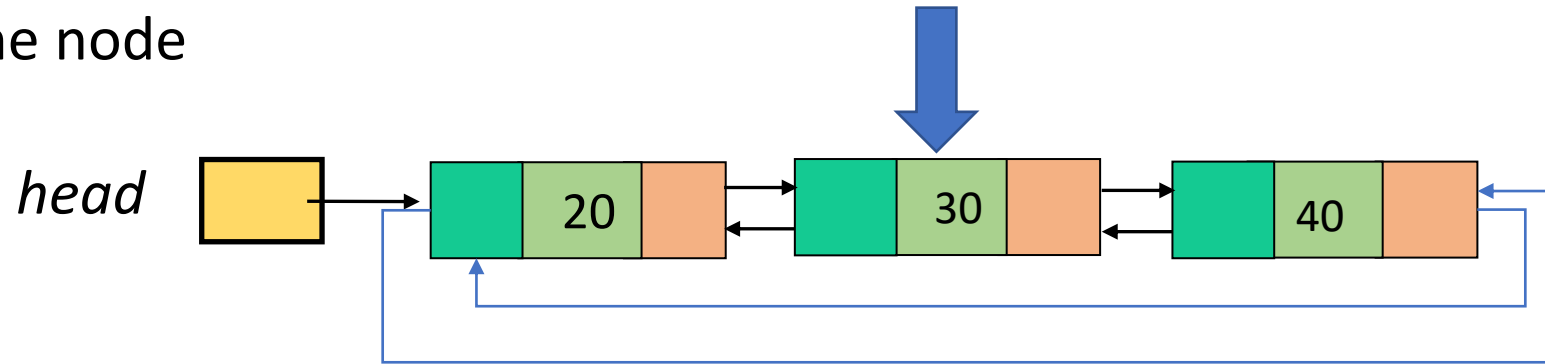
② *head → prev = deltail → prev;*

③ *free (deltail)*

Circular Doubly Linked List: delete at the position

Steps:

(v) If the list contain more than one node
*struct node *deltail*



① $position \rightarrow prev \rightarrow next = position \rightarrow next;$

② $position \rightarrow next \rightarrow prev = position \rightarrow prev;$

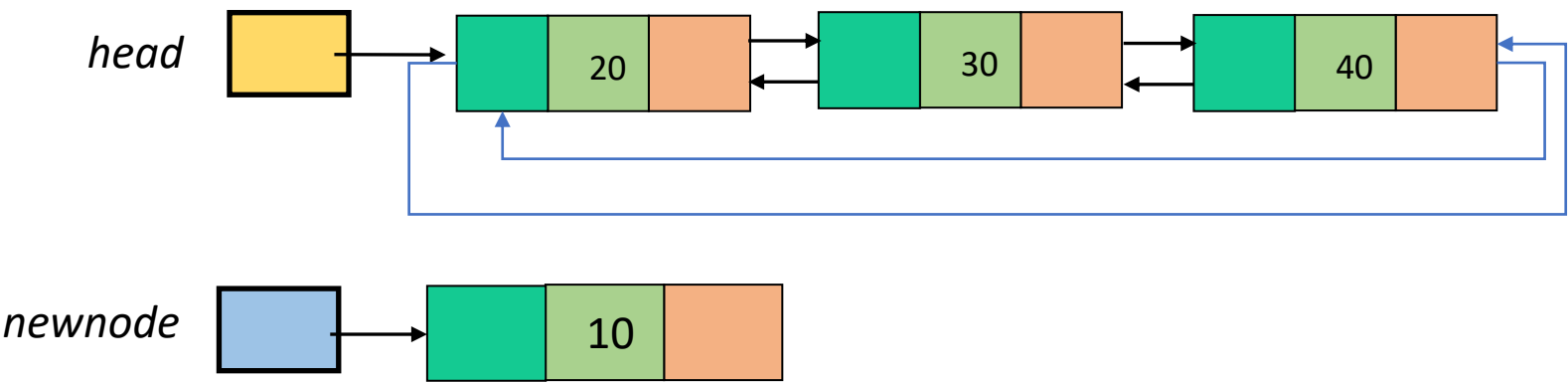
③ $free(deltail)$

position 

Exercise: Circular Linked List (1)

Q: Fill the following table with the number of pointer operations need to be changed for each doubly linked list operation ?

Operations	begin	end	Middle (pos)
Insert			
delete			



thank you!

email:

k.kondepu@iitdh.ac.in

NEXT Class: 08/05/2023