

SPIFI Improvements Report

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Introduction

The basis of the broader project to which this team's efforts contribute is to expand upon an existing technology called Spatial Frequency Modulated Single Detector Imaging (SPIFI). This team created simulation software and measurement software dealing with potential improvements to the SPIFI technique. The simulation served as a proof-of-concept as well as a helpful guide for what has come to be known as "2D-SPIFI". The measurement software is used to implement photon-counting rather than conventional detection methods.

Background

SPIFI is a revolutionary imaging technique that allows a line to be scanned across an object by a single laser at one time, without using a raster pattern along the line. This represents a performance change from $O[n^2]$ to $O[n]$ for a square object with side length n . SPIFI accomplishes this by encoding the information about an object in a frequency change which maps directly to a spatial line that spans the object, and which evolves in time as the line sweeps over the object. Traditionally, scanning more than a single point at a time would require multiple collectors to be able to resolve which photons were used to scan what part of the object (e.g. using a camera). Figure 1 depicts part of a very simple SPIFI system being used to image a gray cube.

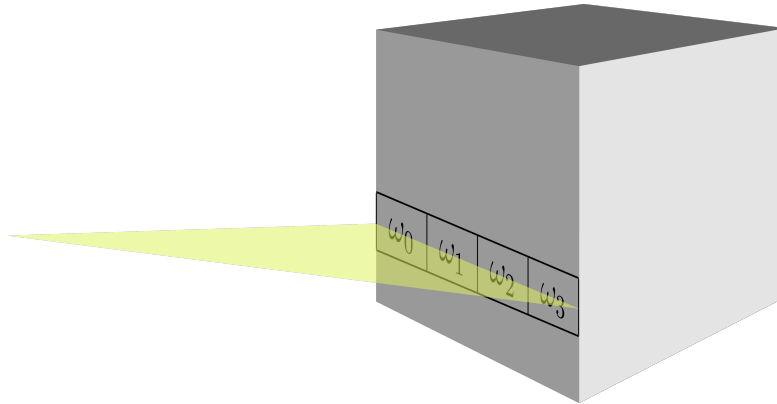


Figure 1: Visual Depiction of Spatial Frequency Mapping

The four ω s in boxes represent different, unique frequencies along the

plane of light hitting the object. Of course, in practice the frequency modulation is smoother and the resolution of the imaging is determined by how many "boxes" one can make on the face of the object. The sheet of light is mechanically swept across the object, and as it moves the frequencies each evolve at different rates. Figure 2 shows how frequency varies in time as the sheet of light sweeps over the object.

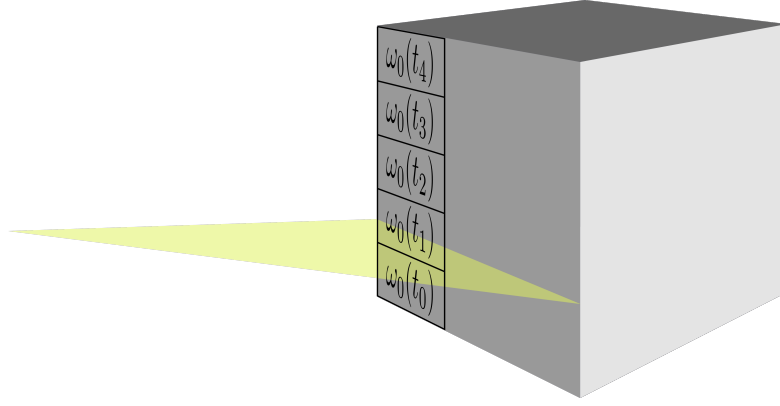


Figure 2: Visual Depiction of Temporal Frequency Mapping

$\omega_{0,0}$	$\omega_{1,0}$	$\omega_{2,0}$	$\omega_{3,0}$	$\omega_{4,0}$	$\omega_{5,0}$
$\omega_{0,1}$	$\omega_{1,1}$	$\omega_{2,1}$	$\omega_{3,1}$	$\omega_{4,1}$	$\omega_{5,1}$
$\omega_{0,2}$	$\omega_{1,2}$	$\omega_{2,2}$	$\omega_{3,2}$	$\omega_{4,2}$	$\omega_{5,2}$
$\omega_{0,3}$	$\omega_{1,3}$	$\omega_{2,3}$	$\omega_{3,3}$	$\omega_{4,3}$	$\omega_{5,3}$
$\omega_{0,4}$	$\omega_{1,4}$	$\omega_{2,4}$	$\omega_{3,4}$	$\omega_{4,4}$	$\omega_{5,4}$
$\omega_{0,5}$	$\omega_{1,5}$	$\omega_{2,5}$	$\omega_{3,5}$	$\omega_{4,5}$	$\omega_{5,5}$

Figure 3: Total Frequency Mapping Over an Object

Figure 3 shows the net result of these temporal and spacial frequency mappings; each inscribed ω is unique to the section of the x/y plane that bounds it. After passing through the object, the light is gathered back into a

well-collimated beam and collected by a single-pixel detector. Then decomposing the measured signal into the frequencies that make it up allows for inspection of how the laser interacted with the object at specific points on its surface. Each of these tiny "boxes" as seen in Figure 3 can be interpreted directly as a pixel. This is done by measuring the attenuation of the specific frequency. For example, considering once again Figure 3, suppose that the measured signal has almost none of the frequency $\omega_{2,2}$ in it, but has nearly all of the $\omega_{0,0}$ that it started with. This means that light in the upper-left corner of the object faced almost no resistance, while nearly all of that which traveled through $(x, y) = (2, 2)$ was blocked. It's then reasonable to conclude that the object is shaped such that it is relatively thick at $(2, 2)$, and relatively thin at $(0, 0)$.

This frequency mapping is achieved by spreading the laser into a sheet and then passing it through a SPIFI mask. Designs of these masks vary, but they can all be understood in the same manner through their transfer function acting on the laser. Figure ?? shows the signal transfer system, starting with some laser given by $u(x)$. The modulation function shown, $m(x, t)$, is then applied, followed by the laser passing through the object which itself applies some unknown transfer function $g(x)$. The final result measured on the detector is an intensity, so only the square of the signal is observable.

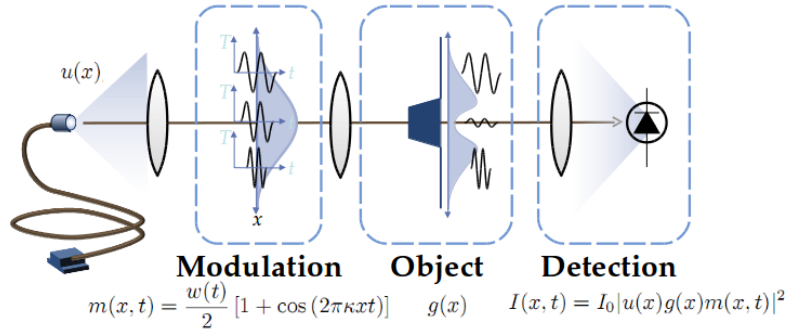


Figure 4: A Simple SPIFI System

The transfer function $g[x, y]$ is determined by the object being imaged, and represents an attenuation of amplitude of specific sections of the xy plane based on the object's ability to absorb and reflect light. Typically this function is used to describe the object, and once found will immediately yield

an image of the object.

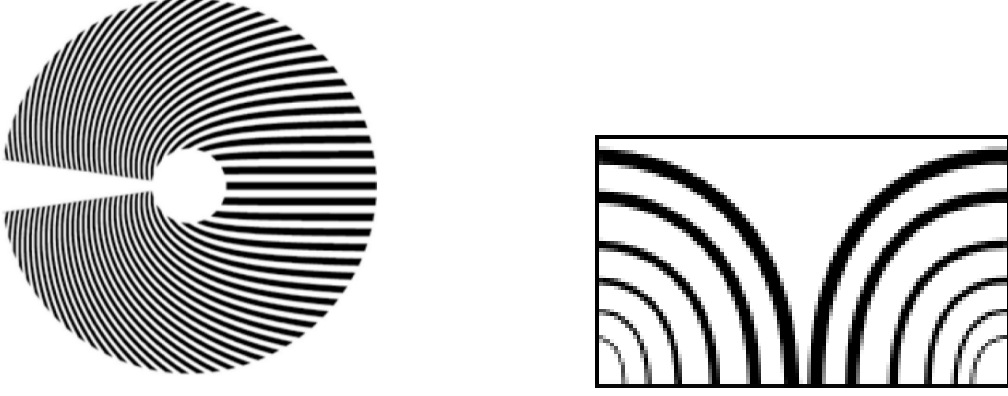


Figure 5: Left: A Circular SPIFI Grating - Right: A Rectangular SPIFI Grating

Examples of typical SPIFI masks are shown in Figure 5. For the common circular grating - similar to the one in the figure - the form of the pattern in polar coordinates is

$$\text{pattern}[r, t] = \frac{1}{2} + \frac{1}{2} \cos [2\pi f_m k_p r t]. \quad (1)$$

Here, f_m is the rotational of the grating, and k_p is a constant that has to do with the density of the lines in the pattern.

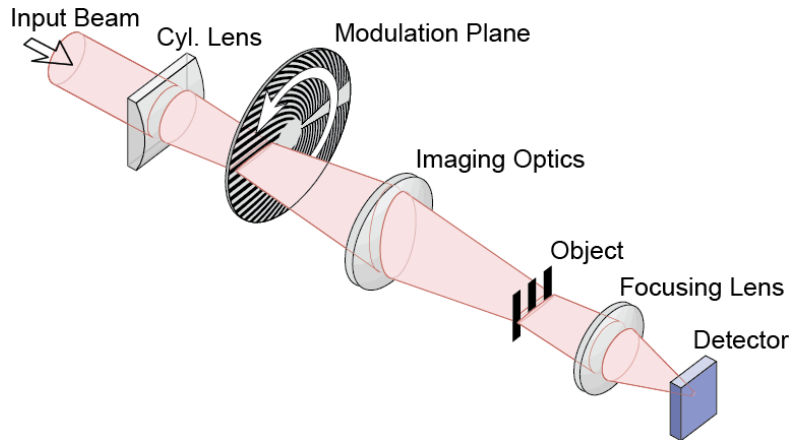


Figure 6: A Simple SPIFI System Using a Circular Grating

As shown in Figure 6, this function modulates the laser as it passes through the grating as a line, and then is scanned along the object from top to bottom by a mechanical apparatus twisting a lens or mirror. A transformation from Equation 1 to the $m[x, y, t]$ transfer function requires sampling the output in intervals of $\tau_m = 1/f_m$, the period of the pattern's spinning.

Once the light has been scanned over the object, the intensity recorded by the detector during τ_m can be Fourier-transformed to find the contributions from each frequency at a given time. The time-domain and frequency-domain plots of this for some unknown object looks like Figure 7.

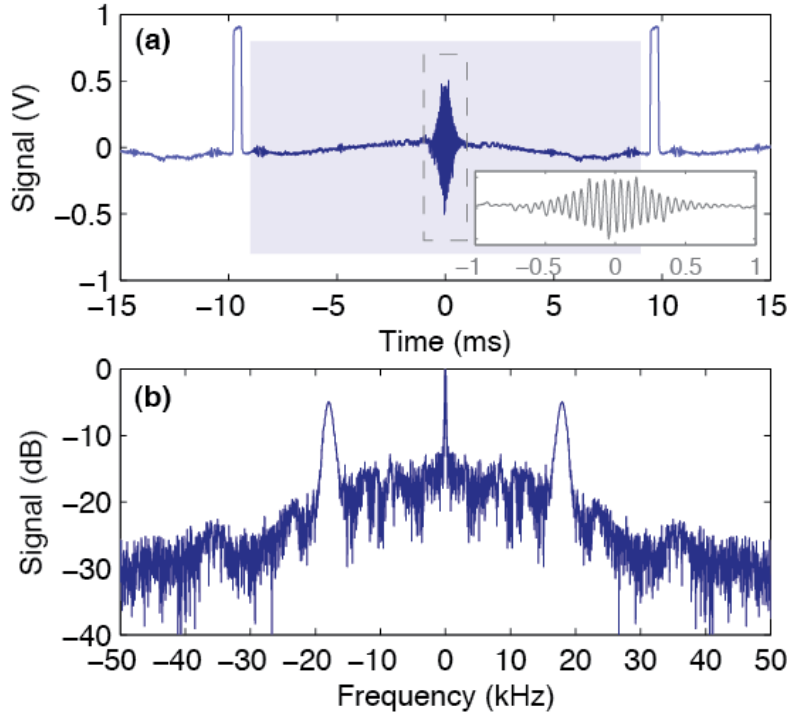


Figure 7: Top: Time-Domain SPIFI Output - Bottom: Corresponding Frequency-Domain SPIFI Output

Theory of 2D SPIFI

The focus of this project is to expand the capabilities of SPIFI by using a diffraction grating which, unlike those presented in the Background section, diffracts the entire beam in two dimensions at any one time, thereby eliminating the need to scan the laser along the object. Because using splitting the beam in two dimensions will allow scanning of the object to occur all at once, there's no need to accumulate readings over some time interval, and therefore real-time imaging is made much easier. A basic, somewhat crude example of a circular grating that could be used is presented in Figure 8.



Figure 8: Crude Rendering of a Potential 2-Dimensional SPIFI Grating

Keep in mind, this is only meant to show how the 2-dimensional diffraction gratings might be mounted on a wheel to modulate the laser. Figure 9 shows a low-density, possible pattern for one of these squares.

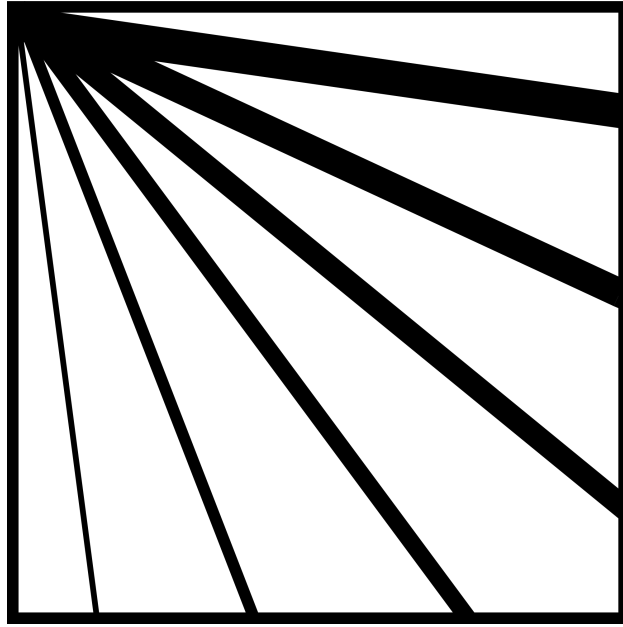


Figure 9: Possible Pattern for Single Square on 2-Dimensional SPIFI Grating

At the time of this writing, the idea for this technology is little more than a week old, and only one of these wheels has been produced and tested, so images of a real, working grating wheel are unavailable. The team's job will be to first construct a working simulation of one of these wheels given a wheel pattern, then to create a data collection routine for this new system- either from scratch or by modifying existing code written by the SPIFI team.

Procedure

Our team is tasked with developing simulations of 2-dimensional SPIFI systems, and with writing data collection software. Each task will occur in increments, and each will require a report as well as documentation.

Firstly, the simulation will be built up in the following steps:

1. Simulate 2D SPIFI using a perfectly continuous grating wheel
2. Incorporate gaps between patterns on the wheel
3. Incorporate refraction and diffraction caused by equipment

Documentation for this program will be made available in exhaustive pdf form as well as POSIX-compliant manual pages for the first incarnation, and subsequently updated for each change. The program will be written in an open language standard (C) using a free and open runtime for that language (the GNU Standard C library, compiled using the GNU C Compiler), and will be written and run on existing computers.

Secondly, data collection software will be written in the following two steps:

1. Analysis of existing codebase
2. Development of actual software

Data collection software already exists for simple, 1-dimensional SPIFI systems, so it may be advantageous to build the 2-dimensional analysis tool by writing a new version of this suite, or even to simply add it directly into the existing structure. Alternatively, if the current software is found to be devoid of functionality that can be used for the new system, or if it is deemed too bloated, slow, or incapable of interfacing properly with the detection hardware in some way, it would be more prudent to begin a new program and build it from the ground up. To determine which is better, the existing code will be analyzed, ideally in collaboration with the original team that wrote it - a coalition of researchers and research assistants from the Colorado School of Mines and the University of Colorado in Fort Collins, with the latter currently in charge of maintaining and updating. After the analysis, the actual code will have to be written. Whatever decision is reached regarding the use of the 1-dimensional analysis software, the final product *will* be written in

an open language standard, and utilize a free and open runtime (the existing software has equivalent versions written in C++ and C#, so it's impossible to say exactly what language and runtime will be used until the analysis is conducted, or even which will be used given that the existing software is used in some capacity). However, the current software is packaged as "Solutions" for the Microsoft IDE and Development Environment called Visual Studio. Therefore, even if neither of these codebases is used, Visual Studio must be used in their analysis. Not only is Visual Studio itself not free, it only runs on the proprietary operating system Windows version 7 or higher. Furthermore, the company Jet Brains produces a proprietary plugin for Visual Studio that makes working with C# so much easier, and consequentially saves developers so much time that the vast majority of companies that work with C# deem it worth the cost. Given this usefulness, and the fact that the head software engineer is already familiar with the plugin, it would be very difficult to complete the analysis of the existing data collection software inside of the estimated timeframe - certainly not with the 10 h/week estimate - without the use of the plugin.

Statement of Work

A breakdown of the costs of completing each part of the project is given in Table 1, and a timeline given for these tasks and their various parts, as well as the report to be presented on completion is given in Table 2 and the data is visualized in Chart 10.

Item	Unit Cost	Quantity	Unit	Cost
2D Simulation Software				
· Labor	\$63.00	28	day	\$1764.00
Data Collection Suite				\$6401.00
· Labor	\$63.00	87	day	\$5481.00
· Visual Studio License	\$500.00	1	ea	\$500.00
· Windows 10 Product License	\$120.00	1	ea	\$120.00
· JetBrains Resharper License	\$300.00	1	ea	\$300.00
Final Report				
· Labor	\$63.00	36	day	\$2268.00
· Overhead	50% of Labor	—	—	\$4756.50
Total Cost				\$15,189.00

Table 1: Cost Estimates for Project Deliverables

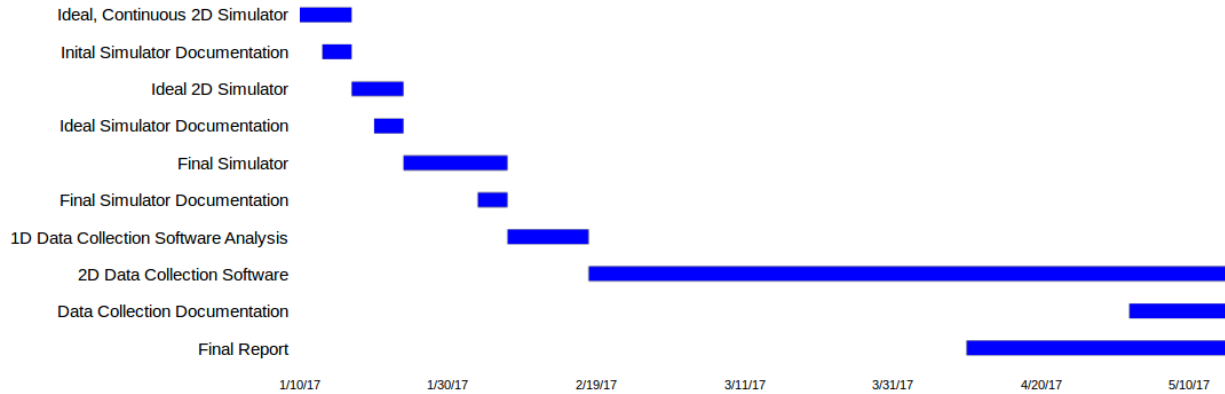


Figure 10: Project Timeline

Labor cost estimates are based on a rough \$44.00/hr starting pay for software engineers, equivalent to \$440.00 per 7 days or about \$63.00/day, assuming I spend 10 hours week (standard part-time employment hours/week) working on these tasks.

In short, the team requests \$15,189.50 to complete this project.

Deliverable	Start Date	Duration (Days)	End Date
Ideal, Continuous 2D Simulation	1/10/17	7	1/16/17
Initial Simulator Documentation	1/13/17	4	1/16/17
Ideal 2D Simulator	1/17/17	7	1/23/16
Ideal Simulator Documentation	1/20/17	4	1/23/17
Final Simulator	1/24/17	14	2/6/17
Final Simulator Documentation	2/3/17	4	2/6/17
1D Data Collection Software Analysis	2/7/17	11	2/17/17
2D Data Collection Software	2/18/17	87	5/15/17
Data Collection Documentation	5/2/17	14	5/15/17
Final Report	4/10/17	36	5/15/17

Table 2: Timeline Breakdown

Conclusion

The ability to reliably simulate 2D SPIFI systems is crucial to the ability of the other teams working on the broader project to ensure the diffraction patterns, wheel designs, and optical systems are correct implementations of the theory, and are operating properly when placed into the system. Furthermore, the entire point of performing SPIFI microscopy on an object is to collect the output signal data, making the production of data collection software imperative to the success of the project. The team feels that costs have been estimated accurately, and that said costs are well worth the advances to science this technology will bring.

Upon the project’s completion, each of these software suites and their corresponding source code will be made publicly available via a public source control repository hosted by GitLab. Specifically, both will be initiated as private repositories, but will be made public upon publication of the larger body of work this team is contributed to. As such, though links are provided in the Appendix, following them will be useless to anyone without access to the repositories, and will remain empty for a little while anyway. To request access to these repositories, contact the project lead and/or head software engineer. All links and contact information is available in Appendix A.

Appendix

A

A.1 Contact Information

- Project Lead: Dr. Jeff Squire, jsquiere@mines.edu
- Team Head Software Engineer: Brennan W. Fieck, bfeick@mines.edu

A.2 Links

- 2D SPIFI Grating Simulation Software
- Data Collection Suite
- Original SPIFI Article - hosted by Research Gate

References

- [1] Squier, Dr Jeff. Deluca, Dr Keith. et. al. *Super-Resolved Multimodal Multiphoton Microscopy with Spatial Frequency-Modulated Imaging*, Proceedings of the National Academy of Sciences, 2015.
- [2] Futia, Greg. Winters, Dave. Schlup, Philip. Bartels, Dr Randy. "Spatial Frequency Modulated Imaging on a Single Element Detector." Colorado School of Mines, Golden. May 24, 2011. Presentation.