

- 6.30** Write and test the function that “rotates” 90° clockwise a two-dimensional square array of ints. For example, it would transform the array

```
11 22 33
44 55 66
77 88 99
```

into the array

```
77 44 11
88 55 22
99 66 33
```

- 6.31** Write and run a program that reads an unspecified number of numbers and then prints them together with their deviations from their mean.

- 6.32** Write and test the following function:

```
double stdev(double x[], int n);
```

The function returns the *standard deviation* of a data set of n numbers x_0, \dots, x_{n-1} defined by the formula

$$s = \sqrt{\frac{\sum_{i=0}^{n-1} (x_i - \bar{x})^2}{n-1}}$$

where \bar{x} is the mean of the data. This formula says: square each deviation ($x[i] - \text{mean}$); sum those squares; divide that square root by $n-1$; take the square root of that sum.

- 6.33** Extend the program from Problem 6.31 so that it also computes and prints the Z-scores of the input data. The Z-scores of the n numbers x_0, \dots, x_{n-1} are defined by $z_i = (x_i - \bar{x})/s$. They normalize the given data so that they are centered about 0.0 and have standard deviation 1.0. Use the function defined in Problem 6.32.

- 6.34** In the imaginary “good old days” when a grade of “C” was considered “average,” teachers of large classes would often “curve” their grades according to the following distribution:

```
A:    1.5 ≤ z
B:    0.5 ≤ z < 1.5
C:   -0.5 ≤ z < 0.5
D:   -1.5 ≤ z < -0.5
F:    z < -1.5
```

If the grades were *normally distributed* (i.e., their density curve is bell-shaped), then this algorithm would produce about 7% A’s, 24% B’s, 38% C’s, 24% D’s, and 7% F’s. Here the z values are the Z scores described in Problem 6.33. Extend the program from Problem 6.33 so that it prints the “curved” grade for each of the test scores read.

- 6.35** Write and test a function that creates Pascal’s Triangle in the square matrix that is passed to it. For example, if the two-dimensional array `a` and the integer 4 were passed to the function, then it would load the following into `a`:

```
1 0 0 0 0
1 1 0 0 0
1 2 1 0 0
1 3 3 1 0
1 4 6 4 1
```

- 6.36** In the theory of games and economic behavior, founded by John von Neumann, certain two-person games can be represented by a single two-dimensional array, called the *payoff matrix*. Players can obtain optimal strategies when the payoff matrix has a saddle point. A *saddle point* is an entry in the matrix that is both the minimax and the maximin. The *minimax*