

## Programming Language

**Purpose** Parse an unambiguous, infix-notation language.

### Exercises

This homework concerns the language we saw in class that unambiguously deals with summation and products:

$\langle \text{AE} \rangle ::= \langle \text{PROD} \rangle + \langle \text{AE} \rangle \quad (1)$

$\quad \quad \quad | \langle \text{PROD} \rangle \quad (2)$

$\langle \text{PROD} \rangle ::= \langle \text{ATOM} \rangle * \langle \text{PROD} \rangle \quad (3)$

$\quad \quad \quad | \langle \text{ATOM} \rangle \quad (4)$

$\langle \text{ATOM} \rangle ::= \langle \text{num} \rangle \quad (5)$

$\quad \quad \quad | \{ \langle \text{AE} \rangle \} \quad (6)$

**Exercise 1** Show the following strings are an AE with a step by step derivation. Use a block comment, and label each expansion with the rule it follows:

```
"5"  
"{5}"  
"{2 + 5}"  
"{{{2 + 5}} * {5 * {{3 + 6}}}}"
```

**Exercise 2** Define an abstract syntax tree structure using `define-type` which captures this language. Note that you should have one type per non-terminal!

**Exercise 3** Design your `parse-ae` function which takes in a `Sexpr` and outputs an AE.

**Exercise 4** Design your `parse` function which composes `parse-ae` and `string->sexpr`. Test this function on the above strings.

**Exercise 5** Explain the relationship between how many constructors are in the output and how many steps there were to derive the string from  $\langle \text{AE} \rangle$ .

**Exercise 6** Some of parentheses in the final string given above seem excessive; they are not. Identify a pair of seemingly-excessive parentheses and explain why they are not.

**Exercise 7** Replace the right-most sum with a product in the final string. Now are any of the parenthesis excessive? If so, why?

**Exercise 8** Leave a comment describing how you feel about programming with an unambiguous, infix-notation language.