



Universität Zürich

# Dalitz plot

***Silvio Donato***

([silvio.donato@cern.ch](mailto:silvio.donato@cern.ch))

***<http://sdonato.web.cern.ch/sdonato/UZH>***

***PHYS451 - Experimental Particle Physics***

***Exercise class 3***

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# Exercise 4

- What are the particle in the final state of this experiment?
- Have you found any three-body resonance?
- What is the Dalitz plot?
  - Is there any symmetry? Why?
  - Have you found any two-body resonance?
- (Bonus) Measure the two-body resonance mass.

```
from ThreeBodyDecay import exp4
(part1,part2,part3) = exp4()
print type(part1) #TLorentzVector
help(part1)
```



# Exercise 5

- The  $\pi^0 \rightarrow \gamma\gamma$  in a very short time. Its mass is 140 GeV.
  - Plot the previous Dalitz plot.
- (Bonus) Improve the mass resolution exploiting the  $\pi^0$  mass. What is the effect on the three-body invariant mass?

```
from ThreeBodyDecay import exp5
(part1,part2,part3,part4,part5,part6) = exp5()
print type(part1) #TLorentzVector
help(part1)
```

# Part II

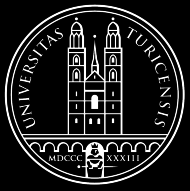
**Simulate a 3-body decay**



# Divide et impera

- The 3-body decay is a quite complex process.
- To solve it we:
  - split the problem in many simpler problems
- In the next slides we will simulate the Ex.1 problem:
  - $D_s^+ \rightarrow \phi(1020) + \pi^+ \rightarrow K^+ + K^- + \pi^+$

$$m(D_s^+) = 1968 \text{ MeV}, m(\pi^+) = 140 \text{ MeV}, m(K^+) = 493 \text{ MeV}.$$



# Divide et impera

- The 3-body decay with resonances is two 2-body decays.
- The two body decay is a two body decay at rest + boost
- The two body decay at rest of  $D_s^+$  and  $\phi$  is isotropic and with fixed energies.
- Eventually, we add background and resolution effects.



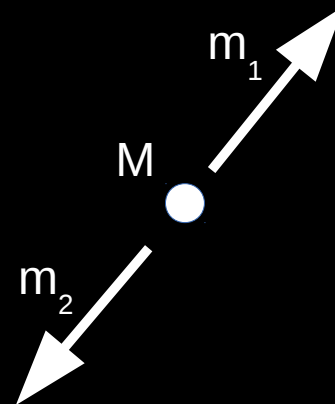
# Exercise 1

- Write a function that simulate the decay of a particle with mass  $M$  at rest into two particles with mass  $m_1$  and  $m_2$ .
- Checks:
  - Is the invariant mass of the pair of particles in the final states equal to the original particle mass  $M$ ?
  - Are the final state particles distributed isotropically?



## Exercise 2

- Write a function that simulate the decay of a particle with mass  $M$  into two particles with mass  $m_1$  and  $m_2$ .
- Checks:
  - Is the invariant mass of the pair of particles in the final states equal to the original particle mass  $M$ ?
  - Are the final state particles distributed isotropically?



```
def decayRestFrame(M,m1,m2):  
    part1 = TLorentzVector()  
    part2 = TLorentzVector()  
    [...]  
    return part1,part2
```

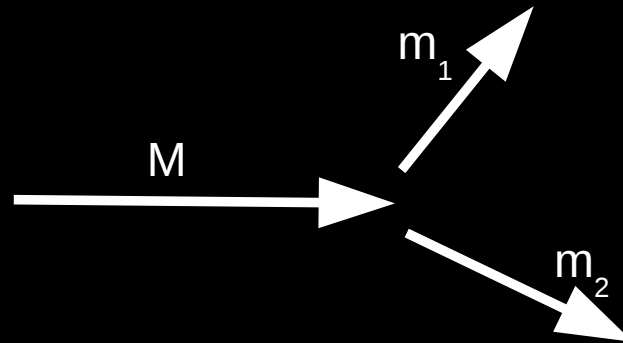
$$|\vec{p}_1| = |\vec{p}_2| = \frac{[(M^2 - (m_1 + m_2)^2)(M^2 - (m_1 - m_2)^2)]^{1/2}}{2M}$$





# Exercise 3

- Write a function that simulate the decay of a particle at rest with mass  $M$  into two particles with mass  $m_1$  and  $m_2$ .
- Checks:
  - Are the energy/momentum conserved?



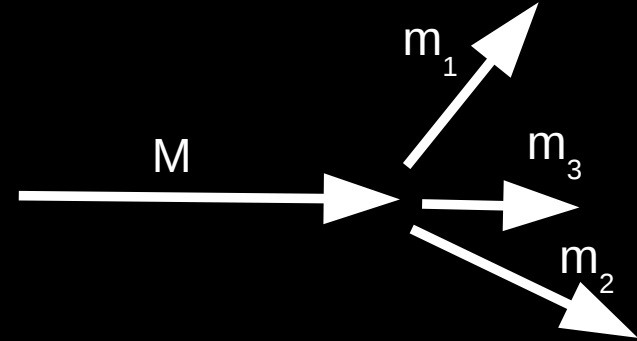
```
def decay(part,m1,m2):  
    M = part.M()  
    part1,part2=decayRestFrame(M,m1,m2)  
    [...]  
    return part1,part2
```

```
p = TLorentzVector(0,0,10,100)  
boost = part.BoostVector()  
p.Boost(-boost)  
# p is now in the rest frame
```



# Exercise 4

- Write a function that simulate the decay of a particle with mass  $M$  and  $p_Z$  into two particles with mass  $m_1$  and  $m_A$ , and the second one decays into  $m_1$  and  $m_2$ .
- Checks:
  - Are the energy/momentum conserved?



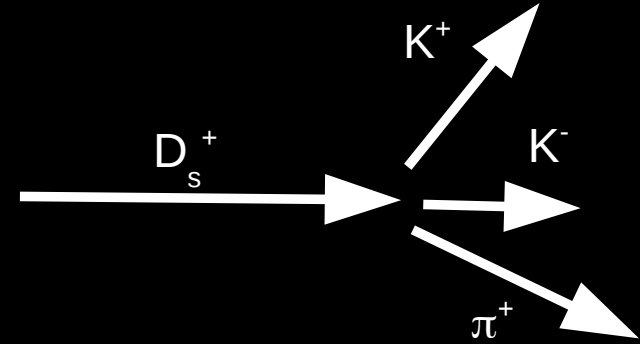
```
def generateEvent(M, m1, m2, m3, pZ=10, mA):  
    [...]  
    return part1,part2,part3
```

```
p = TLorentzVector(0,0,10,100)  
boost = part.BoostVector()  
p.Boost(-boost)  
# p is now in the rest frame
```



# Exercise 5

- Draw the Dalitz plot for
  - $D_s^+ \rightarrow \bar{K}^{*0} + \pi^+ \rightarrow K^+ + K^- + \pi^+$  (33%)
  - $D_s^+ \rightarrow \phi(1020) + \pi^+ \rightarrow K^+ + K^- + \pi^+$  (33%)
  - $D_s^+ \rightarrow K^+ + K^- + \pi^+$  [no resonance] (33%)





# Exercise 6

- Smear the particle momenta taking into account an angular resolution of  $\sim 1\%$  and an energy resolution of  $\sim 10\%$ .
- How does the Dalitz plot change? What is the dominant error?
  - Test other values.

```
rnd = TRandom3()
for i in range(1000):
    x = rnd.Gaus()
    #x is distributed as a Gaussian distribution
    #with mean 0 and sigma 1
```



# Exercise 7

- Add a non-resonant background with the three-particle invariant mass distributed as a decreasing exponential

```
rnd = TRandom3()
for i in range(1000):
    x = rnd.Exp(-2.5)
    #x is distributed as  $f(x) = \exp(-2.5 \cdot x)$ 
```