

1 Template

```
1 #include <iostream>
2 #include <string>
3 #include <vector>
4 #include <sstream>
5 #include <map>
6 #include <set>
7 #include <queue>
8 #include <algorithm>
9 #include <cmath>
10 #include <cstdio>
11 #include <cstdlib>
12 #include <cstring>
13
14 using namespace std;
15 using ll = long long;
16
17 #define all(c) (c).begin(), (c).end()
18 #define rep(i,n) for(int i=0;i<(int)(n);i++)
19 #define pb(e) push_back(e)
20 #define mp(a, b) make_pair(a, b)
21 #define fr first
22 #define sc second
23
24 const ll INF=1e9;
25 const ll MOD=1e9+7;
26 int dx[4]={1,0,-1,0};
27 int dy[4]={0,1,0,-1};
28
29 int main() {
30     return 0;
31 }
```

2 Graph

2.1 二部マッチング

```
1 /*
2  * 二部マッチング
3  *  $O(|E| |V|)$ 
4  *
5  * http://poj.org/problem?id=3041
6  */
7
8 struct BipartiteMatching {
9     vector<vector<int>> > G;
10    vector<int> match;
11    vector<bool> used;
12
13    int V;
14    BipartiteMatching(int V):V(V){
15        G.resize(V);
16        match.resize(V);
```

```
17        used.resize(V);
18    }
19
20    void add_edge(int u,int v) {
21        G[u].push_back(v);
22        G[v].push_back(u);
23    }
24
25    bool dfs(int v) {
26        used[v]=true;
27        for(int i=0;i<G[v].size();i++){
28            int u=G[v][i];
29            int w=match[u];
30            if(w<0||!used[w]&&dfs(w)) {
31                match[v]=u;
32                match[u]=v;
33                return true;
34            }
35        }
36        return false;
37    }
38
39    int operator() () {
40        int res=0;
41        match.assign(V,-1);
42        for(int v=0;v<V;v++){
43            if(match[v]<0) {
44                used.assign(V,0);
45                if(dfs(v)) res++;
46            }
47        }
48        return res;
49    }
50 };
```

2.2 ダイクストラ

```
1 using Weight = ll;
2 struct Edge {
3     int to;
4     Weight cost;
5 };
6 struct Node {
7     int v;
8     Node(int v) : v(v) {}
9     bool operator<(const Node &rhs) const { return tie(v) < tie(rhs.v); }
10    bool operator==(const Node &rhs) const { return tie(v) == tie(rhs.v); }
11 };
12
13 namespace std {
14     template <>
15     struct hash<Node>{
16         size_t operator()(const Node &node) const {
17             size_t seed = 0;
18
19             size_t v_hash = hash<int>()(node.v);
20         }
```

```

21     seed ^= v_hash + 0x9e3779b9 + (seed << 6) + (seed >> 2);
22     return seed;
23 }
24 };
25 }
26 struct State : public Node {
27     Weight cost;
28     State(Node node, Weight cost) : Node(node), cost(cost) {}
29     bool operator<(const State &rhs) const { return cost > rhs.cost; }
30 };
31
32 unordered_map<Node, Weight> dijkstra(const vector<vector<Edge>> &adj,
33                                     const Node &source) {
34     unordered_map<Node, Weight> dist;
35     priority_queue<State> que;
36
37     que.push(State(source, 0));
38     dist[source] = 0;
39
40     while (que.size()) {
41         State s = que.top();
42         que.pop();
43         Node cur{s.v};
44
45         for (auto u : adj[s.v]) {
46             Node next{u.to};
47             if (!dist.count(next) || dist[next] > dist[cur] + u.cost) {
48                 dist[next] = dist[cur] + u.cost;
49                 que.push(State(next, dist[next]));
50             }
51         }
52     }
53
54     return dist;
55 }

```

2.3 最大流

```

1  /*
2  * 最大流
3  * Ford 法 Fulkerson
4  *  $O(F|E|)$ 
5  *
6  * http://poj.org/problem?id=3281
7  *
8  */
9
10 struct FordFulkerson{
11     struct Edge {
12         int to, cap, rev;
13         Edge(int to=0, int cap=0, int rev=0) :
14             to(to), cap(cap), rev(rev){}
15     };
16
17     int V;
18     vector<vector<Edge>> > G;
19     vector<bool> used;

```

```

20
21 FordFulkerson(int V) : V(V) {
22     G.resize(V);
23     used.assign(V, false);
24 }
25
26 void add_edge(int from, int to, int cap) {
27     G[from].pb(Edge(to, cap, G[to].size()));
28     G[to].pb(Edge(from, 0, G[from].size()-1));
29 }
30
31 int dfs(int v, int t, int f) {
32     if(v==t) return f;
33     used[v]=true;
34     for(int i=0; i<G[v].size(); i++) {
35         Edge &e=G[v][i];
36
37         if(!used[e.to] && e.cap>0) {
38             int d=dfs(e.to, t, min(f, e.cap));
39             if(d>0) {
40                 e.cap-=d;
41                 G[e.to][e.rev].cap+=d;
42                 return d;
43             }
44         }
45     }
46     return 0;
47 }
48
49 int max_flow(int s, int t) {
50     int flow=0;
51     while(1) {
52         used.assign(V, false);
53         int f=dfs(s, t, INF);
54         if(f==0) break;
55         flow+=f;
56     }
57
58     return flow;
59 }
60 };

```

2.4 最小費用流

```

1
2 struct MinumumCostFlow {
3     static const int MAX_V = 10004;
4     typedef pair<int, int> P;
5     struct Edge {
6         int to, cost, cap, rev;
7         Edge(int to = 0, int cap = 0, int cost = 0, int rev = 0)
8             : to(to), cap(cap), cost(cost), rev(rev) {}
9     };
10
11     int V;
12     vector<Edge> G[MAX_V];
13     int h[MAX_V];

```

```

14 int dist[MAX_V];
15 int prev_v[MAX_V], prev_e[MAX_V];
16
17 void add_edge(int from, int to, int cap, int cost) {
18     G[from].push_back(Edge(to, cap, cost, G[to].size()));
19     G[to].push_back(Edge(from, 0, -cost, G[from].size() - 1));
20 }
21
22 int operator()(int s, int t, int f) {
23     int res = 0;
24     fill(h, h + V, 0);
25
26     while (f > 0) {
27         priority_queue<P, vector<P>, greater<P>> que;
28         fill(dist, dist + V, INF);
29         dist[s] = 0;
30         que.push(P(0, s));
31
32         while (que.size()) {
33             P p = que.top();
34             que.pop();
35             int v = p.second;
36             if (dist[v] < p.first) continue;
37             rep(i, G[v].size()) {
38                 Edge &e = G[v][i];
39                 if (e.cap > 0 &&
40                     dist[e.to] > dist[v] + e.cost + h[v] - h[e.to]) {
41                     dist[e.to] = dist[v] + e.cost + h[v] - h[e.to];
42                     prev_v[e.to] = v;
43                     prev_e[e.to] = i;
44                     que.push(P(dist[e.to], e.to));
45                 }
46             }
47         }
48         if (dist[t] == INF) return -1;
49         rep(v, V) h[v] += dist[v];
50
51         int d = f;
52         for (int v = t; v != s; v = prev_v[v]) {
53             d = min(d, G[prev_v[v]][prev_e[v]].cap);
54         }
55         f -= d;
56         res += d * h[t];
57
58         for (int v = t; v != s; v = prev_v[v]) {
59             Edge &e = G[prev_v[v]][prev_e[v]];
60             e.cap -= d;
61             G[v][e.rev].cap += d;
62         }
63     }
64
65     return res;
66 }
67 };

```

```

1 // Verified http://abc014.contest.atcoder.jp/tasks/abc014\_4
2 struct LCA {
3     int N;
4     int root;
5     int log2_n;
6     vector<vector<int>> parent;
7     vector<int> depth;
8     vector<vector<int>> G;
9     LCA(int N, int root=0) : N(N), root(root) {
10         log2_n = log2(N) + 1;
11         parent.resize(log2_n);
12         rep(i, log2_n) parent[i].resize(N);
13         depth.resize(N);
14         G.resize(N);
15     }
16     void add_edge(int v, int u) {
17         G[v].pb(u);
18     }
19     void init() {
20         dfs(root, -1, 0);
21         rep(k, log2_n-1) rep(v, N) {
22             if (parent[k][v] < 0) parent[k+1][v] = -1;
23             else parent[k+1][v] = parent[k][parent[k][v]];
24         }
25     }
26     void dfs(int v, int p, int d) {
27         parent[0][v] = p;
28         depth[v] = d;
29         rep(i, G[v].size()) {
30             if (G[v][i] != p) dfs(G[v][i], v, d+1);
31         }
32     }
33     int operator()(int u, int v) {
34         if (depth[u] > depth[v]) swap(u, v);
35         rep(k, log2_n) {
36             if ((depth[v] - depth[u]) >> k & 1) {
37                 v = parent[k][v];
38             }
39         }
40         if (v == u) return u;
41
42         for (int k = log2_n-1; k >= 0; k--) {
43             if (parent[k][u] != parent[k][v]) {
44                 u = parent[k][u];
45                 v = parent[k][v];
46             }
47         }
48         return parent[0][u];
49     }
50     int dist(int v, int u) {
51         int a = operator()(v, u);
52         return depth[v] - depth[a] + depth[u] - depth[a];
53     }
54 };

```

2.5 最小共通祖先

3 Math

3.1 繰り返し 2 乗法

```
1 ll mod_pow(ll a, int n, int m) {
2     if (n == 0)
3         return 1;
4     else if (n % 2 == 1)
5         return (a * mod_pow((a * a) % m, n >> 1, m)) % m;
6     else
7         return mod_pow((a * a) % m, n >> 1, m);
8 }
```

3.2 コンビネーション

```
1 /*
2  * 前処理  $O(N)$ 
3  * クエリ  $O(1)$ 
4  *
5  * Verified
6  * http://yukicoder.me/problems/184
7  */
8
9 template<class T, size_t N, T MOD>
10 struct Combination {
11     typedef T int_type;
12     vector<int_type> fact, factr, inv;
13     Combination() {
14         fact.resize(2*N+1);
15         factr.resize(2*N+1);
16         inv.resize(2*N+1);
17         fact[0]=factr[0]=1;
18         inv[1]=1;
19         for(int i=2; i<=2*N; i++) inv[i] = inv[MOD % i] * (MOD - MOD / i) % MOD;
20         for(int i=1; i<=2*N; i++) fact[i]=fact[i-1]*i%MOD, factr[i]=factr[i-1]*inv[i]%MOD;
21     }
22
23     int_type C(int n, int r) {
24         if(r<0 || r>n) return 0;
25         return factr[r]*fact[n]%MOD*factr[n-r]%MOD;
26     }
27
28     int_type P(int n, int r) {
29         if(r<0 || r>n) return 0;
30         return fact[n]*factr[n-r]%MOD;
31     }
32
33     int_type H(int n, int r) {
34         if(n==0 && r==0) return 1;
35         return C(n+r-1, r);
36     }
37 };
```

4 DataStructure

4.1 Segment Tree

```
1 // Verified
2 // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=DSL\_2\_A
3 //
4
5
6 template<class T>
7 struct SegTree {
8     typedef T int_type;
9     static const size_t MAX_N = 1 << 17;
10    static const int_type INIT_VAL = (int_type(1)<<31)-1;
11    int_type data[2 * MAX_N - 1];
12    size_t n;
13    SegTree(size_t n_) {
14        n=1;
15        while(n < n_) n*=2;
16        rep(i, 2*n-1) data[i]=INIT_VAL;
17    }
18    void update(size_t k, int_type a) {
19        k+=n-1;
20        data[k]=a;
21        while(k>0) {
22            k=(k-1)/2;
23            data[k]=min(data[k*2+1], data[k*2+2]);
24        }
25    }
26
27    int_type query(size_t a, size_t b, size_t k, size_t l, size_t r) {
28        if(r<=a || b<=l) return INIT_VAL;
29        if(a<=l && r<=b) return data[k];
30        else {
31            int_type vl = query(a, b, k*2+1, l, (l+r)/2);
32            int_type vr = query(a, b, k*2+2, (l+r)/2, r);
33            return min(vl, vr);
34        }
35    }
36    int_type query(size_t a, size_t b) {
37        return query(a, b, 0, 0, n);
38    }
39 };
```

4.2 StarrySky Tree

```
1 // Verified
2 // http://code-festival-2015-final-open.contest.atcoder.jp/tasks/codefestival\_2015\_final\_d
3 // http://judge.u-aizu.ac.jp/onlinejudge/cdescription.jsp?cid=RitsCamp16Day3&pid=F
4
5 template<class T>
6 struct StarrySkyTree {
7     using int_type = T;
8     vector<T> data;
9     vector<T> lazy;
10    int N;
```

```

11 StarrySkyTree(int n) {
12     N=1;
13     while(N<n) N<<=1;
14     data.assign(2*N-1, 0);
15     lazy.assign(2*N-1, 0);
16 }
17 // [a,b)
18 void add(int a,int b, int_type val) {
19     add(a,b,val,0,0,N);
20 }
21 int_type get(int a,int b) {
22     return get(a,b,0,0,N);
23 }
24
25 void add(int a,int b,int_type val, int k,int l,int r) {
26     if(r<=a || b<=l) return;
27     if(a<=l && r<=b) {
28         lazy[k]+=val;
29         return;
30     }
31     add(a,b,val,k*2+1,l,(l+r)/2);
32     add(a,b,val,k*2+2,(l+r)/2,r);
33     data[k]=max(data[k*2+1]+lazy[k*2+1], data[k*2+2]+lazy[k*2+2]);
34 }
35
36 int_type get(int a,int b, int k,int l, int r) {
37     if(r<=a || b<=l) return -INF;
38     if(a<=l && r<=b) return data[k]+lazy[k];
39     auto lval = get(a,b,k*2+1,l,(l+r)/2);
40     auto rval = get(a,b,k*2+2,(l+r)/2,r);
41     return max(lval, rval)+lazy[k];
42 }
43 };

```

4.3 Treap

```

1 int xor128() {
2     static int x = 123456789, y = 362436069, z = 521288629, w = 88675123;
3     int t;
4     t = (x ^ (x << 11));
5     x = y;
6     y = z;
7     z = w;
8     return (w = (w ^ (w >> 19)) ^ (t ^ (t >> 8)));
9 }
10
11 struct Node {
12     int val;
13     Node *ch[2];
14     // 優先度
15     int pri;
16     // 部分木の個数
17     int cnt;
18     // 部分木の値の和
19     int s;
20     Node(int val, int p) : val(val), pri(p), cnt(1), s(val) {
21         ch[0] = ch[1] = nullptr;

```

```

22     }
23 };
24 int count(Node *n) { return n == nullptr ? 0 : n->cnt; }
25 int sum(Node *n) { return n == nullptr ? 0 : n->s; }
26
27 Node *update(Node *n) {
28     n->cnt = count(n->ch[0]) + count(n->ch[1]) + 1;
29     n->s = sum(n->ch[0]) + sum(n->ch[1]) + n->val;
30     return n;
31 }
32
33 Node *merge(Node *l, Node *r) {
34     if (l == nullptr || r == nullptr) return l == nullptr ? r : l;
35     if (l->pri > r->pri) {
36         l->ch[1] = merge(l->ch[1], r);
37         return update(l);
38     } else {
39         r->ch[0] = merge(l, r->ch[0]);
40         return update(r);
41     }
42 }
43
44 pair<Node *, Node *> split(Node *t, int k) {
45     if (t == nullptr) return make_pair(nullptr, nullptr);
46     int c = count(t->ch[0]);
47     if (k <= c) {
48         auto s = split(t->ch[0], k);
49         t->ch[0] = s.second;
50         return make_pair(s.first, update(t));
51     } else {
52         auto s = split(t->ch[1], k - c - 1);
53         t->ch[1] = s.first;
54         return make_pair(update(t), s.second);
55     }
56 }
57
58 Node *insert(Node *t, int k, int val) {
59     Node *m = new Node(val, xor128() % 1007);
60     auto p = split(t, k);
61     return merge(merge(p.first, m), p.second);
62 }
63
64 Node *erase(Node *t, int k) {
65     auto p1 = split(t, k);
66     auto p2 = split(p1.second, 1);
67     return merge(p1.first, p2.second);
68 }
69
70 // を挿入すべき場所を探す val
71 int upper_bound(Node *t, int val) {
72     if (t == nullptr) return 0;
73     if (t->val > val)
74         return upper_bound(t->ch[0], val);
75     else
76         return upper_bound(t->ch[1], val) + count(t->ch[0]) + 1;
77 }
78

```

```

79 // 番目の大きいやつ x
80 int get(Node *t, int x) {
81     int c = count(t->ch[0]);
82     if (c == x) return t->val;
83     if (x < c)
84         return get(t->ch[0], x);
85     else
86         return get(t->ch[1], x - c - 1);
87 }

```

4.4 UnionFind

```

1 #include <vector>
2 template<typename T>
3 class UnionFind {
4     int size_;
5     std::vector<T> par;
6     std::vector<T> rank;
7
8 public:
9     UnionFind(int size_) : size_(size_) {
10         par.resize(size_);
11         rank.resize(size_);
12
13         for(int i=0; i<size_; i++) {
14             par[i] = i;
15             rank[i] = 0;
16         }
17     }
18
19     T find(T x) {
20         return par[x] == x ? x : par[x] = find(par[x]);
21     }
22
23     void unite(T x, T y) {
24         x = find(x);
25         y = find(y);
26         if(x == y) return;
27
28         if(rank[x] < rank[y]) {
29             par[x] = y;
30         }
31         else {
32             par[y] = x;
33             if(rank[x] == rank[y]) rank[x]++;
34         }
35     };

```

5 String

5.1 ローリングハッシュ

```

1 struct RollingHash {
2     typedef long long int_type;
3     typedef pair<int_type, int_type> hash_type;

```

```

4
5     int_type base1;
6     int_type base2;
7     int_type mod1;
8     int_type mod2;
9     vector<int_type> hash1;
10    vector<int_type> hash2;
11    vector<int_type> pow1;
12    vector<int_type> pow2;
13
14    RollingHash() : base1(1009), base2(1007), mod1(1000000007), mod2(1000000009) {}
15
16    void init(const string &s) {
17        int n = s.size();
18
19        hash1.assign(n+1, 0);
20        hash2.assign(n+1, 0);
21        pow1.assign(n+1, 1);
22        pow2.assign(n+1, 1);
23
24        for(int i=0; i<n; i++) {
25            hash1[i+1] = (hash1[i]+s[i]) * base1 % mod1;
26            hash2[i+1] = (hash2[i]+s[i]) * base2 % mod2;
27            pow1[i+1] = pow1[i] * base1 % mod1;
28            pow2[i+1] = pow2[i] * base2 % mod2;
29        }
30    }
31
32    hash_type get(int l, int r) {
33        int_type t1 = ((hash1[r] - hash1[l] * pow1[r-l]) % mod1 + mod1) % mod1;
34        int_type t2 = ((hash2[r] - hash2[l] * pow2[r-l]) % mod2 + mod2) % mod2;
35        return make_pair(t1, t2);
36    }
37
38    RollingHash::hash_type concat(hash_type h1, hash_type h2, int h2_len) {
39        return make_pair((h1.fr*pow1[h2_len]+h2.fr)%mod1, (h1.sc*pow2[h2_len]+h2.sc)%mod2);
40    }
41
42 };

```

6 Geometry

6.1 幾何

```

1 #include <complex>
2 #include <vector>
3 #include <cmath>
4 #include <utility>
5 #include <cassert>
6 #include <cmath>
7
8 const double EPS=1e-10;
9
10 #define equals(a, b) (fabs((a)-(b))<EPS)
11 #define X real()

```

```

12 #define Y imag()
13
14 using namespace std;
15
16 typedef complex<double> Point;
17 typedef complex<double> Vector;
18
19 struct Segment {
20     Point p1, p2;
21 };
22 typedef Segment Line;
23
24 struct Circle {
25     Point c;
26     double r;
27     Circle(Point c=Point(), double r=0.0) :
28         c(c), r(r) {}
29 };
30
31 typedef vector<Point> Polygon;
32
33 double dot(Vector a, Vector b) {
34     return a.X*b.X + a.Y*b.Y;
35 }
36
37 double cross(Vector a, Vector b) {
38     return a.X*b.Y - a.Y*b.X;
39 }
40
41 Point project(Segment s, Point p) {
42     Vector base = s.p2-s.p1;
43     double r=dot(p-s.p1,base) / norm(base);
44     return s.p1+base*r;
45 }
46
47 Point reflect(Segment s, Point p) {
48     return p+(project(s,p)-p)*2.0;
49 }
50
51 enum CCW {
52     COUNTER_CLOCKWISE=1,
53     CLOCKWISE=-1,
54     ONLINE_BACK=2,
55     ONLINE_FRONT=-2,
56     ON_SEGMENT=0,
57 };
58
59 int ccw(Point p0, Point p1, Point p2) {
60     Vector a=p1-p0;
61     Vector b=p2-p0;
62     if(cross(a,b)>EPS) return CCW::COUNTER_CLOCKWISE;
63     if(cross(a,b)<=-EPS) return CCW::CLOCKWISE;
64     if(dot(a,b)<=-EPS) return CCW::ONLINE_BACK;
65     if(norm(a)<norm(b)) return CCW::ONLINE_FRONT;
66
67     return CCW::ON_SEGMENT;
68 }

```

```

69
70 double getDistance(Point a, Point b) {
71     return abs(a-b);
72 }
73
74 double getDistanceLP(Line l, Point p) {
75     return abs(cross(l.p2-l.p1, p-l.p1)/abs(l.p2-l.p1));
76 }
77
78 bool intersect(Point p1, Point p2, Point p3, Point p4) {
79     return (ccw(p1, p2, p3)*ccw(p1, p2, p4)<=0&&
80             ccw(p3, p4, p1)*ccw(p3, p4, p2)<=0);
81 }
82
83 bool intersect(Segment s1, Segment s2) {
84     return intersect(s1.p1, s1.p2, s2.p1, s2.p2);
85 }
86 bool intersect(Circle c, Line l) {
87     return getDistanceLP(l, c.c)<=c.r;
88 }
89
90 Point getCrossPoint(Segment s1, Segment s2) {
91     Vector base=s2.p2-s2.p1;
92     double d1=abs(cross(base, s1.p1-s2.p1));
93     double d2=abs(cross(base, s1.p2-s2.p1));
94     double t=d1/(d1+d2);
95     return s1.p1+(s1.p2-s1.p1)*t;
96 }
97 pair<Point, Point> getCrossPoints(Circle c, Line l) {
98     // assert(intersect(c, l));
99     Vector pr=project(l, c.c);
100     Vector e=(l.p2-l.p1)/abs(l.p2-l.p1);
101     double base=sqrt(c.r*c.r-norm(pr-c.c));
102
103     return make_pair(pr+e*base, pr-e*base);
104 }
105
106
107 pair<Point, Point> getCrossPoints(Circle c1, Circle c2) {
108     double d=abs(c1.c-c2.c);
109     double a=acos((c1.r*c1.r+d*d-c2.r*c2.r)/(2*c1.r*d));
110     double t=arg(c2.c-c1.c);
111
112     return make_pair(c1.c+polar(c1.r, t+a), c1.c+polar(c1.r, t-a));
113 }
114
115 // IN 2, ON 1, OUT 0
116 int contains(Polygon g, Point p) {
117     int n=g.size();
118     bool x=false;
119     for(int i=0; i<n; i++) {
120         Point a=g[i]-p, b=g[(i+1)%n]-p;
121         if(abs(cross(a,b))<EPS && dot(a,b)<EPS) return 1;
122         if(a.Y>b.Y) swap(a,b);
123         if(a.Y<EPS&&EPS<b.Y&&cross(a,b) > EPS) x=!x;
124     }
125

```

```
126     return x?2:0;
127 }
```
