Final Oral Exam

Relational Learning and Fairness

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November 26, 2019

Outline

1. Topic Blockmodel

2. Monotonic Fairness

3. Elicited Monotonic Fairness

Topic Blockmodel: Introduction

Problem: Lots of communications observed over network connections, how do we improve inference about the people based on the communications?

Topic Blockmodel: Introduction

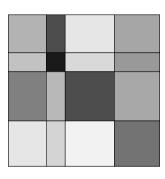
- Problem: Lots of communications observed over network connections, how do we improve inference about the people based on the communications?
- *Intuition*: Individuals in one homogeneous group should behave similarly when interacting with individuals of another homogeneous group.

Topic Blockmodel: Introduction

- Problem: Lots of communications observed over network connections, how do we improve inference about the people based on the communications?
- *Intuition*: Individuals in one homogeneous group should behave similarly when interacting with individuals of another homogeneous group.
- Model: Use a stochastic blockmodel to assign individuals to communities, and a topic model for the communications from each community to each other.

Background: Stochastic Blockmodels

- Boolean Stochastic Blockmodel:^a
 - Each of n individuals are assigned to one of K communities
 - Each pair of communities (i,j) has an edge probability P_{ij} , probability that node in i has edge with any node in j.
- Can move from boolean to other distributions...

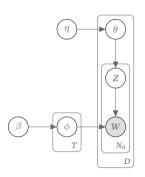


^aY. Wang and Wong 1987; Snijders and Nowicki 1997.

Background: Latent Dirichlet Allocation

Topic Modeling: ^a Each document has a topic distribution θ from which each topic z is drawn, and each word w is drawn from the word distribution ϕ for its corresponding topic.

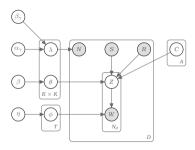
$$egin{array}{ll} heta_d & \sim & {\sf Dirichlet}(\eta) \\ \phi_t & \sim & {\sf Dirichlet}(eta) \\ z_{dn} & \sim & {\sf Multinomial}(heta_d) \\ w_{dn} & \sim & {\sf Multinomial}(\phi_{(z_dn)}) \end{array}$$



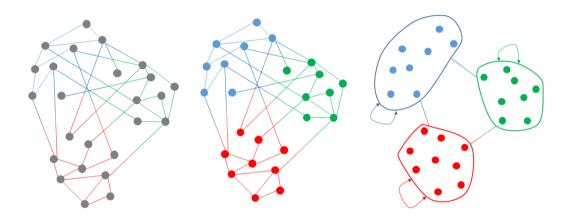
^aBlei, Na, and Jordan 2003.

Topic Blockmodel

- Draw community memberships: $Z \sim \mathsf{CRP}(\alpha)$
- Draw expected of word counts $\lambda_{\it ij} \sim {\sf Gamma}(\alpha_{\gamma}, \beta_{\gamma})$
- Draw topic distributions: $heta_{ii} \sim \mathsf{Dirichlet}(\eta)$
- Draw word distributions: $\phi_t \sim \text{Dirichlet}(\beta)$
- For each sender s to receiver r,
 - Draw a number of words $n_{sr} \sim \mathsf{Poisson}(\lambda_{(C_s)(C_r)})$
 - For each of n_{ii} words:
 - Draw a topic: $Z_{wsr} \sim \mathsf{Multinomial}(\theta_{(C_{\mathrm{s}})(C_{\mathrm{r}})})$
 - Draw a word: $W_{wsr} \sim ext{Multinomial}(\phi_{(Z_{ver})})$



Topic Blockmodel



Count Modeling

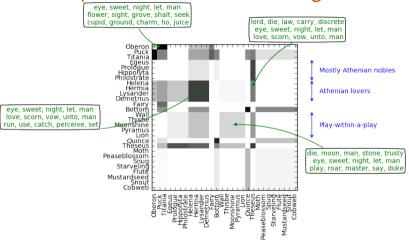
We model not just the *content* but also the *frequency*

$$\lambda_{ij} \sim \mathsf{Gamma}(\alpha_{\gamma}, \beta_{\gamma})$$

$$N_{sr} \sim \mathsf{Poisson}(\lambda_{(C_s)(C_r)})$$

Captures information from communication frequency / intensity, not just what they discuss

Results - Shakespeare's A Midsummer Night's Dream



(Darkness indicates frequency / intensity)

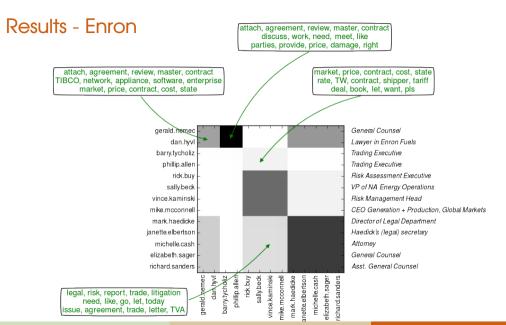


Table: Log predictive likelihood (\pm one standard error) of document text, conditioned on sender and recipient where applicable.

Model	ENRON	Shakespeare
LDA	$-410,110.2\pm50.8$	48,716.2 \pm 4.6
ART	$-365,600.5 \pm 47.7$	$-47,\!495.5\pm4.8$
CNT	$-368,983.5 \pm 89.2$	-46,076.6 \pm 3.9
Topic Blockmodel	-345.632.5 \pm 4.1	$-46,275.9 \pm 4.0$

Table: Log predictive likelihood (\pm one standard error) of document recipient, conditioned on document content and sender where applicable.

Model	ENRON	Shakespeare
ART	$-204,585.3 \pm 6.4$	$-19,809.7\pm1.1$
CNT	$-216,\!278.9 \pm < \!0.1$	$-19,703.3 \pm < 0.1$
Poisson-SBM	$-160,984.7 \pm 148.6$	$-14,587.2 \pm 35.9$
Topic Blockmodel	-137,199.8 \pm 53.2	-12,997.8 \pm 20.6

Table: Log predictive likelihood (\pm one standard error) of document sender and recipient, conditioned on document content where applicable.

Model	ENRON	Shakespeare
ART	-416,588.6 \pm 6.8	$-39,580.0 \pm 1.0$
CNT	-432,557.7 \pm < 0.1	$-39,406.7 \pm < 0.1$
Poisson-SBM	$-347,479.6 \pm 148.6$	$-31,400.3 \pm 35.9$
Topic Blockmodel	-321,127.8 \pm 53.3	-29,614.0 \pm 20.6

Table: Log predictive likelihood (\pm one standard error) of sender and recipient counts.

Model	ENRON	Shakespeare
Poisson-SBM Topic Blockmodel	-92,851.2 \pm 12.1 -88,730.4 \pm 3.1	$-103,411.4 \pm 0.6$ $-102,549.8 \pm 0.2$

Conclusion

Questions?

Monotonic Fairness: Introduction

- *Problem*: Although we can create fair(er) prediction and classification systems, they tend to create resentment which undermines their support.

Monotonic Fairness: Introduction

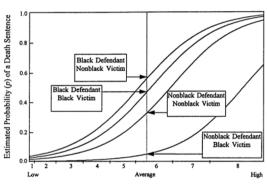
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- Intuition: If we define resentment as seeing someone "worse" get a "better" outcome, we can form models that avoid that outcome.

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- Problem: Although we can create fair(er) prediction and classification systems, they tend to create resentment which undermines their support.
- Intuition: If we define resentment as seeing someone "worse" get a "better" outcome, we can form models that avoid that outcome.
- Model: Modify existing fair neural network models with a monotonic neural network to guarantee that resentment doesn't occur

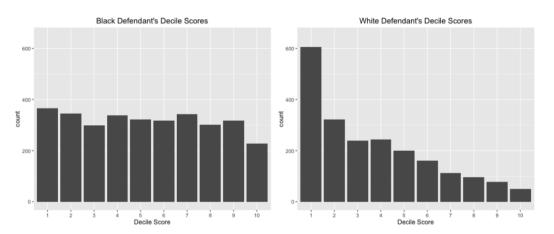
Old Systemic Bias

Estimated Race of Defendant and Race of Victim Effects in Jury Death Sentencing Decisions Among All Death Eligible Cases Philadelphia 1983-93

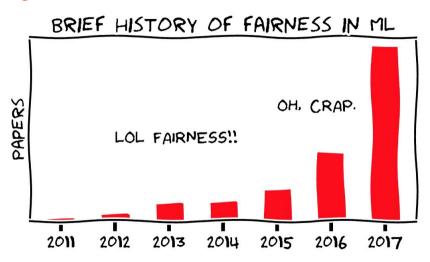


Defendant Culpability Index and Scale Score Estimated in a Logistic Regression Analysis

New Systemic Bias



Growing Awareness



Fairness in ML generally has 3 steps:

- Conceptualize



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- Measure



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- Prevent



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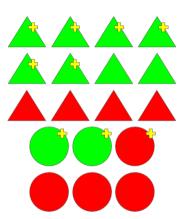
- Conceptualize
- Measure
- Prevent
 - Cheaply, hopefully



Concepts of fairness: Equality of Outcome

Equality of Outcome: "Each group should have the same outcome on average"

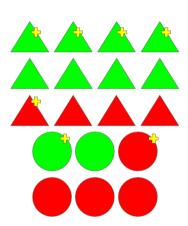
$$\mathbb{E}[\hat{Y}|A=a] = \mathbb{E}[\hat{Y}|A=a']$$



Concepts of fairness: Equality of Odds

Equality of Odds: "The average prediction should be independent of protected class for people with the same outcome."

$$\mathbb{E}[\hat{Y}|A=\alpha,Y=y] = \mathbb{E}[\hat{Y}|A=\alpha',Y=y]$$

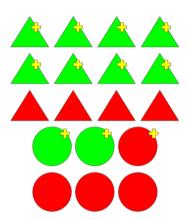


Concepts of fairness: Equality of Opportunity

Equality of Opportunity: "For people who deserve the favorable outcome, the probability of receiving the favorable prediction should be independent of class

$$\Pr[\hat{Y} = 1 | A = a, Y = 1] =$$

 $\Pr[\hat{Y} = 1 | A = a', Y = 1]$



Concepts of fairness: Individual Fairness

Individual fairness: similar individuals should be treated similarly

- $d\left(\hat{f}(X_i), \hat{f}(X_j)\right) \leq D(X_i, X_j)$
- Essentially a requirement of Lipschitz continuity with bounded smoothness.

Individual Resentment

An individual may still experience *resentment* when:

- They receive a less favorable outcome,
- Another person receives a more favorable outcome,
- And either:
 - The other person is identical except for a protected attribute
 - The other person has "worse" non-protected attributes

Individual Resentment

Definition

Protected Attribute Resentment (Class Resentment): Individual u experiences class resentment under function f if $\exists A' \in \mathcal{A}$ s.t. $f(X_u, A') > f(X_u, A_u)$.

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Definition

Non-Protected Attribute Resentment (Score Resentment): Individual u experiences score resentment under function f if \exists $(X',A') \in (\mathcal{X},\mathcal{A})$ such that X_u is objectively "better" than X' but $f(X',A') > f(X_u,A_u)$. (A' may be A_u .)

COMPAS Resentment

Defendant A

Caucasian

25 y.o

4 priors

No juvenile charges

Felony, Violent charge

Robbery, no weapon



Defendant B

African-American

25 y.o

3 priors

No juvenile charges

Felony, Non-Violent charge

Grand Theft, 3rd Deg.



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Decile Score: 10

Preventing Resentment

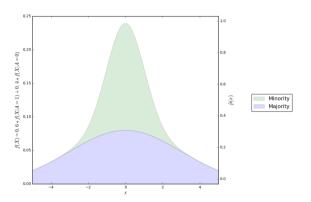
In order to prevent resentment, we propose a system which:

- Takes only non-protected attributes X (i.e. exclude protected attributes A) as input for prediction.
- Use a neural network which has an output function that is monotonic w.r.t. those dimensions X that are user specified

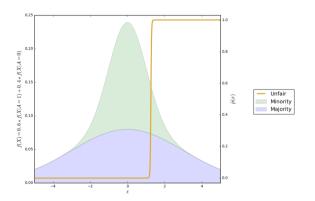
Preventing Resentment

We then train that function to minimize a weighted sum of prediction loss and group fairness loss.

$$Loss = (1 - \alpha) Loss_{Acc} + \alpha Loss_{Fair}$$



$$\begin{array}{l} \operatorname{Learn} f: \mathbb{R} \to [0,1] \\ \operatorname{Maximize} \sum f(X_l) X_l / \sum f(X_l) \\ \operatorname{s.t.} \sum f(X_l) / n = 0.25 \end{array}$$

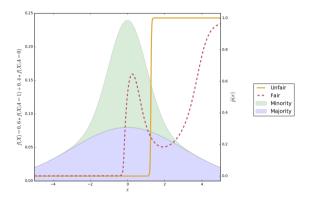


Learn
$$f: \mathbb{R} \to [0,1]$$

Maximize $\sum f(X_i)X_i/\sum f(X_i)$
s.t. $\sum f(X_i)/n = 0.25$

Add fairness:

$$\mathbb{E}[f|A=0] = \mathbb{E}[f|A=1]$$



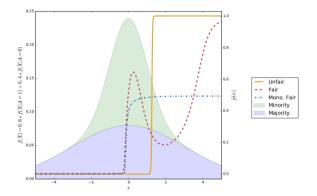
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s.t. $\sum f(X_i)/n = 0.25$

Add fairness:

$$\mathbb{E}[f|A=0] = \mathbb{E}[f|A=1]$$

and no resentment



Monotonic Neural Networks

As proposed by Sill 1998, redefine hidden nodes as:

$$h_{j,l} = \sigma \left(\sum_{i \in 1...|H_{l-1}|} oldsymbol{ au}(w_{i,j}^l) h_{j,l-1} + b_j^l
ight)$$

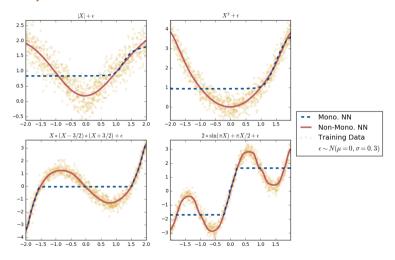
where $au:\mathbb{R} o \mathbb{R}_+$ and σ is monotonically non-decreasing

Mixed Monotonicity

If we don't apply τ to the weights in the first layer corresponding to dimension of X_j , then the function will not be monotonic w.r.t. X_j , even if we transform the weights in subsequent layers.

If we replace $\tau(w^1_{i,j})$ with $-\tau(w^1_{i,j})$ for some input dimension j, then the first layer (and all subsequent layers) will have a monotonic non-increasing relationship with that dimension.

Montonicity Demo



Datasets

We evaluate our model on three fairness-related data sets:

- Law school: 17,400 law school applicants, trying to predict law school grade as function of LSAT and undergrad GPA, protecting gender.

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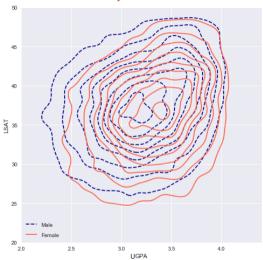
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Datasets

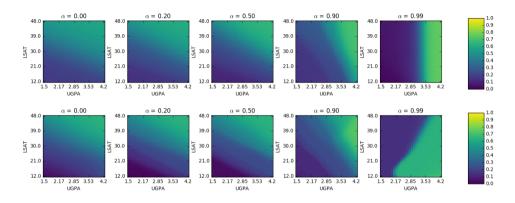
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- German Credit Data: 1,000 West German credit applications. Predict loan repayment based on employment, financial, and residency information while protecting (binary) age. 58 attributes with mixture of monotonicity.

Law School Gender Density



Law School Acceptance Functions



(α is fraction of loss from fairness)

Evaluation metrics

We follow the evaluation metrics of Zemel 2013 Learning Fair Representations.

- Discrimination: disparate impact i.e. absolute difference in expectation:

$$\left| \frac{\sum_{n:s_n=1} \hat{y}_n}{\sum_{n:s_n=1} 1} - \frac{\sum_{n:s_n=0} \hat{y}_n}{\sum_{n:s_n=0} 1} \right|$$

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Accuracy: inverse of mean absolute error

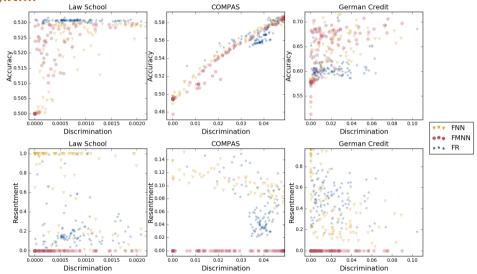
$$1 - \frac{1}{N} \sum_{n=1}^{N} |y_n - \hat{y}_n|$$

Evaluation metrics

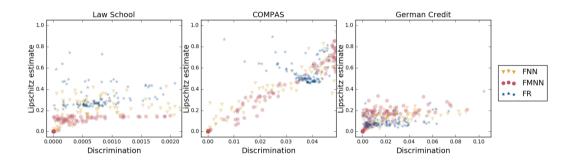
We add Resentment: fraction of people that find example in sample they resent

$$\frac{1}{N} \sum_{i=1}^{N} \max_{j \in \mathcal{N}_i} \left(1_{\hat{y}_i < \hat{y}_j} \right)$$





Lipschitz Smoothness



Eliciting Montonic Fairness: Introduction

 Problem: Axis-based monotonicity is too strict for fairness, and oracle info about which individuals are "better" is hard to systematize (even if we had an oracle).

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- Intuition: Lay people experience resentment, so we should be able to survey them and use that data to figure out what is a "better" set of attributes.

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- Intuition: Lay people experience resentment, so we should be able to survey them and use that data to figure out what is a "better" set of attributes.
- Model: Collect non-expert arbiter ratings on what the relative treatment of pairs of individuals should be. Combine this with historical data as input to a conditional neural network that can post hoc adjust between accuracy and resentment prevention.

Introduction

In practice we often wish to capture more complex definitions of "better" attribute sets that consider multiple attributes at once.

Imagine you're evaluating whether two defendants should get bail:

- Defendant A: 0 prior felonies, 1 prior misdemeanors
- Defendant B: 10 prior felonies, 0 prior misdemeanors

Monotonicity as previously discussed would say A and B are incomparable, but most people would agree that B should be less likely to get bail.

Preference Learning

Ultimately we have a problem of preference learning. We have two options, X_i and X_i , and want to learn a preference function between them.

Many approaches in the literature aim to learn personalized preference functions to recommend the best product *for an individual*. We wish to learn a population-wide preference function which will be applied universally.

Model Structure

Re-encode Y_i into pairwise data Z_{ij} :

$$Z_{ij}^{obs} = \left\{egin{array}{ll} 1 & ext{if} & Y_i^{obs} = 1 ext{ and } Y_j^{obs} = 0 \ 2 & ext{if} & Y_i^{obs} = 0 ext{ and } Y_j^{obs} = 1 \ 3 & ext{if} & Y_i^{obs} = Y_j^{obs} \end{array}
ight..$$

Will use the same encodings for survey data for "more likely", "less likely", and "similarly likely"

Model Structure

Define a pairwise loss function using Z:

$$\mathcal{L}_{Z}(Z, \hat{p}, \mathcal{Z}) = -\frac{1}{|\mathcal{Z}|} \sum_{(i,j) \in \mathcal{Z}} \begin{pmatrix} \mathbf{1}_{Z_{ij}=1} \log (\hat{p}_{i}(1-\hat{p}_{j})) + \\ \mathbf{1}_{Z_{ij}=2} \log ((1-\hat{p}_{i})\hat{p}_{j}) + \\ \mathbf{1}_{Z_{ij}=3} \log (\hat{p}_{i}\hat{p}_{j} + (1-\hat{p}_{i})(1-\hat{p}_{j})) \end{pmatrix}$$

Model Loss

Define our neural network:

$$\mathsf{logit}\,(\hat{p}_i) = f_{\theta}(X_i,c)$$

Define the loss the minimize:

$$\mathcal{L} = \underbrace{\mathcal{L}_{Z}\left(Z_{ij}^{obs}, \hat{p}_{i} = f(X_{i}, c = 0), \mathcal{O}\right)}_{\mathcal{L}_{Z}^{obs}} + \underbrace{\mathcal{L}_{Z}\left(Z_{ij}^{arb}, \hat{p}_{i} = f(X_{i}, c = 1), \mathcal{A}\right)}_{\mathcal{L}_{Z}^{arb}} + g(\theta)$$

Optimize $\hat{\theta} = \arg\min_{\theta} \mathcal{L}$.

Synthetic Experiment Setup

$$eta_{obs} = [0.9, 1.1]$$
 $p_i^{obs} = rac{1}{1 + e^{-(X_ieta^{obs} - 1)}}$ $Y_i \sim \mathsf{Bernoulli}(p_i^{obs})$

$$X_i \sim N(0, 1)^2$$
 $eta_{arb} = [1.1, 0.9]$ $Z_{ij}^{arb} = egin{cases} 1 & ext{if} & X_i eta^{arb} > X_j eta^{arb} + 0.25 \ 2 & ext{if} & X_j eta^{arb} > X_i eta^{arb} + 0.25 \ 3 & ext{if} & |X_i eta^{arb} - X_j eta^{arb}| < 0.25 \end{cases}$

Synthetic Experiment Results

Recover P_i

True probability

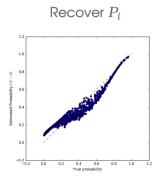
1.0

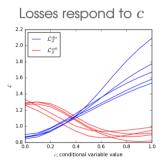
0.6

0.2

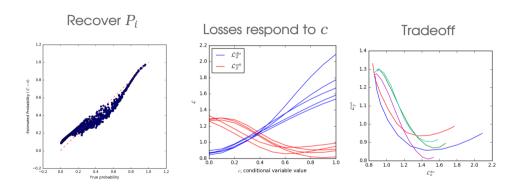
0.0 0.2

Synthetic Experiment Results





Synthetic Experiment Results



COMPAS Experiment Setup

Five arbiters each shown 100 pairs on individuals' attributes: age, (adult) priors count, juv. felony count, juv. misdemeanor count, juv. other counts, charge degree (fel. or mis.), and violent charge (T/F). Asked to rate as:

- "A is at least as likely to (re)offend" (Z=1)
- "B is at least as likely to (re)offend" (Z=2)
- "A and B are similarly likely to (re)offend" (Z=3)
- "No preference / any of the others are fair" (Ignored)

COMPAS Arbiter Results

- 298 dissimilar ($Z \in \{1,2\}$) ratings, 185 similar (Z=3) responses, 18 ratings ignored

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- Surprisingly accurate: 78% of dissimilar ratings correct, similar to COMPAS decile score difference of 3 ($\sim 54\%$ of pairs have decile score difference ≥ 3)

COMPAS Arbiter Results

- 298 dissimilar ($Z \in \{1,2\}$) ratings, 185 similar (Z=3) responses, 18 ratings ignored
- Surprisingly accurate: 78% of dissimilar ratings correct, similar to COMPAS decile score difference of 3 ($\sim 54\%$ of pairs have decile score difference ≥ 3)
- Disparate impact: when comparing African-American to Caucasian, rate former more likely to re-offend 65% of the time

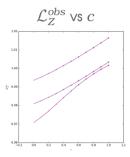
COMPAS Experiment Loss

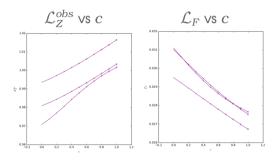
Add Equality of Odds loss:

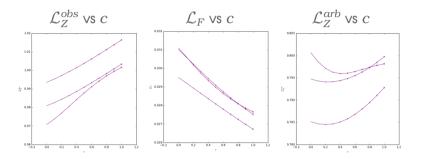
$$\mathcal{L}_F = \sum_{y} \sum_{a} \left(ar{\hat{y}}_{ay} - ar{\hat{y}}_{\cdot y}
ight)^2$$

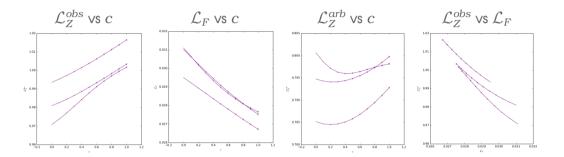
$$\mathcal{L} = \mathcal{L}_Z^{obs} + \mathcal{L}_Z^{arb} + \lambda_F \mathcal{L}_F + g(\theta)$$

Set $\lambda_F = 0.001$ for experiments.









Conclusion

Today we covered:

- How to model communities in networks based on the content and frequency of their members' communications,
- How to create fair functions that avoid resentment between users, and
- How to use arbiter ratings to determine who would resent whom (and how to avoid it).

Conclusion

Questions?

Abridged Bibliography I

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Proving Monotonicity

Define a monotonic non-decreasing (MND) function $f:\mathbb{R} \to \mathbb{R}$

$$\text{s.t. } f(x+dx)-f(x)=df\geq 0 \ \forall \ dx\geq 0.$$

Assume f,g are MND, h is monotone non-increasing (MNI), then:

Recursion: $f \circ g$ is MND

Negation: $f \circ h$ and $h \circ f$ are MNI

Linearity: if a > 0, af(x) + b is MND

Addition: f + g is MND

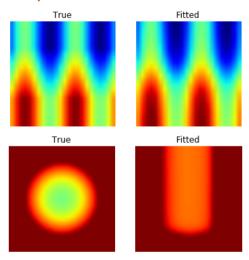
Proving Monotonicity

We can then prove the properties of our network:

- By Linearity, if $au(w^l_{i,j})>0$ then $au(w^l_{i,j})h_{j,l-1}+b^l_j$ is MND w.r.t. $h_{j,l-1}$
- By Addition, $\sum\limits_{i\in 1...|H_{l-1}|} au(w_{i,j}^l)h_{j,l-1}+b_j^l$ is MND w.r.t. each of $h_{j,l-1}$
- By Recursion, if σ is MND then $h_{i,j}^l\sigma\left(\sum_{i\in 1...|H_{l-1}|}\tau(w_{i,j}^l)h_{j,l-1}+b_j^l\right)$ is MND w.r.t. each of $h_{i,l-1}$

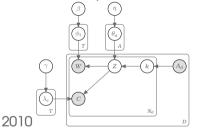
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Mixed Monotonicity Demo

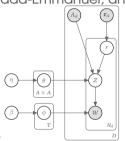


Related Models

Citation-Author Topic Model Tu et al.



Author-Recipient Topic Model
McCallum, Corrada-Emmanuel, and



X. Wang 2005