



**MANIPAL UNIVERSITY
JAIPUR**

(University under Section 2(f) of the UGC Act)



B.TECH. SECOND YEAR

(III SEM. CSE/IT/CCE)

ACADEMIC YEAR: 2020-2021



COURSE NAME: ENGINEERING MATHEMATICS III

COURSE CODE : MA 2101

LECTURE SERIES NO : UNIT-III (LECTURE NO. 14- 22)

CREDITS : 3

MODE OF DELIVERY : ONLINE (POWER POINT PRESENTATION)

FACULTY : DR. REEMA JAIN

EMAIL-ID : reema.jain@jaipur.manipal.edu

PROPOSED DATE OF DELIVERY: August 17, 2020



**MANIPAL UNIVERSITY
JAIPUR**

VISION

Global Leadership in Higher Education and Human Development

MISSION

- Be the most preferred University for innovative and interdisciplinary learning
- Foster academic, research and professional excellence in all domains
- Transform young minds into competent professionals with good human values

VALUES

Integrity, Transparency, Quality,
Team Work, Execution with Passion, Humane Touch

SESSION OUTCOME

**"TO UNDERSTAND THE
CONCEPT OF TREES AND
APPLY THE TREE
ALGORITHMS TO ANALYZE
THE SHORTEST PATH
PROBLEMS"**

ASSIGNMENT

QUIZ

MID TERM EXAMINATION –I & II

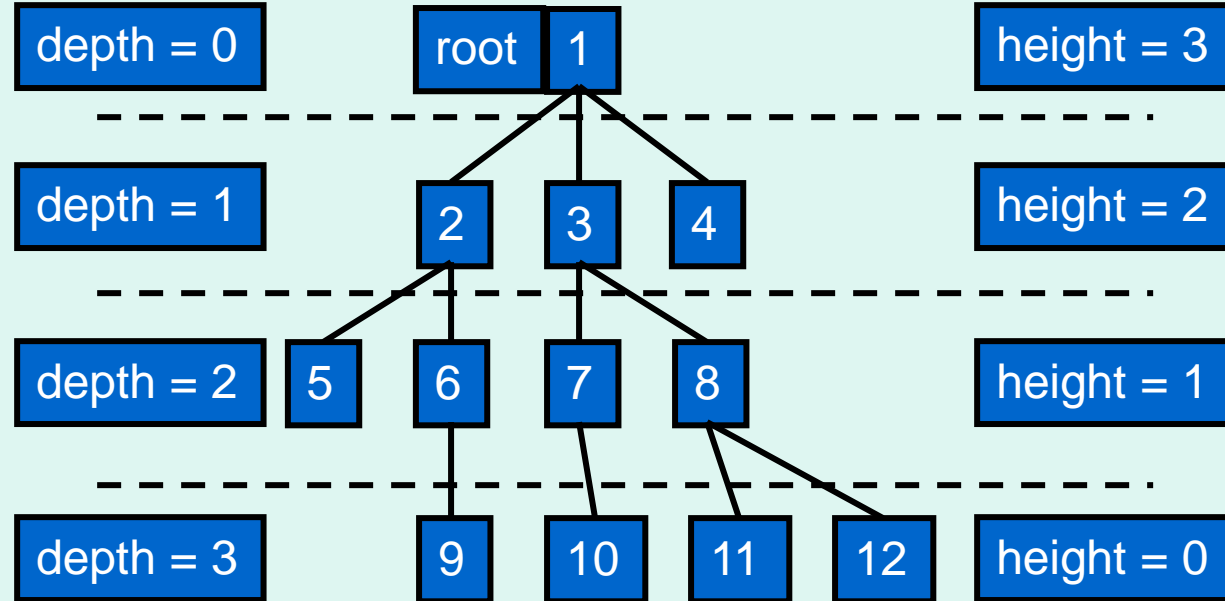
END TERM EXAMINATION

ASSESSMENT CRITERIA

PROGRAM OUTCOMES MAPPING WITH CO3

**ENGINEERING KNOWLEDGE: APPLY THE KNOWLEDGE
OF MATHEMATICS, SCIENCE, ENGINEERING
FUNDAMENTALS, AND AN ENGINEERING
SPECIALIZATION TO THE SOLUTION OF COMPLEX
ENGINEERING PROBLEMS.**

A Rooted Tree



Level of a vertex and tree height

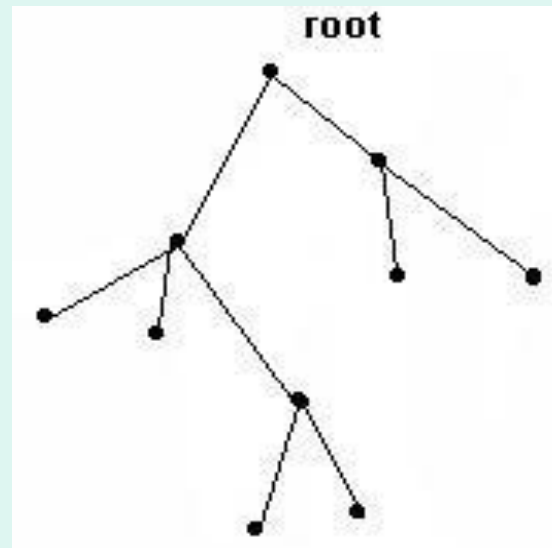
Let T be a rooted tree:

- The *level* $l(v)$ of a vertex v is the length of the simple path from v to the root of the tree
- The *height* h of a rooted tree T is the maximum of all level numbers of its vertices:

$$h = \max_{v \in V(T)} \{ l(v) \}$$

Example:

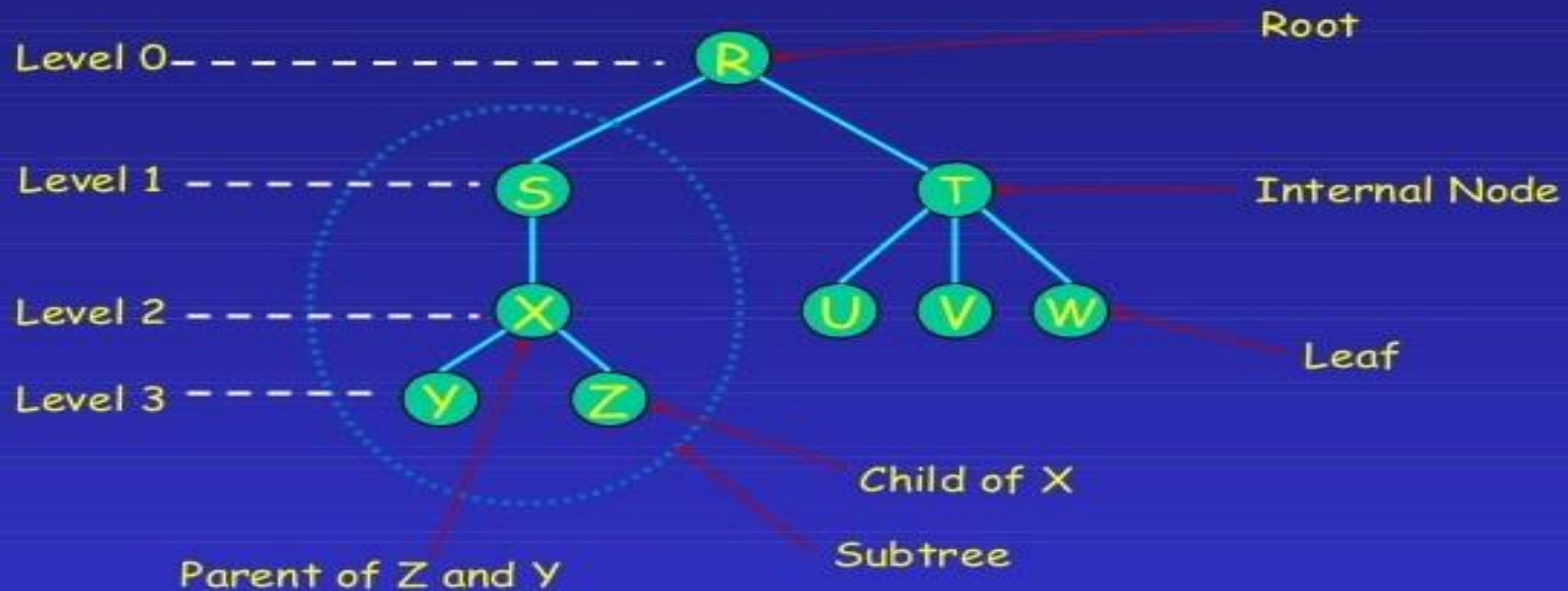
the tree on the right has height 3



Tree Anatomy

Tree Anatomy

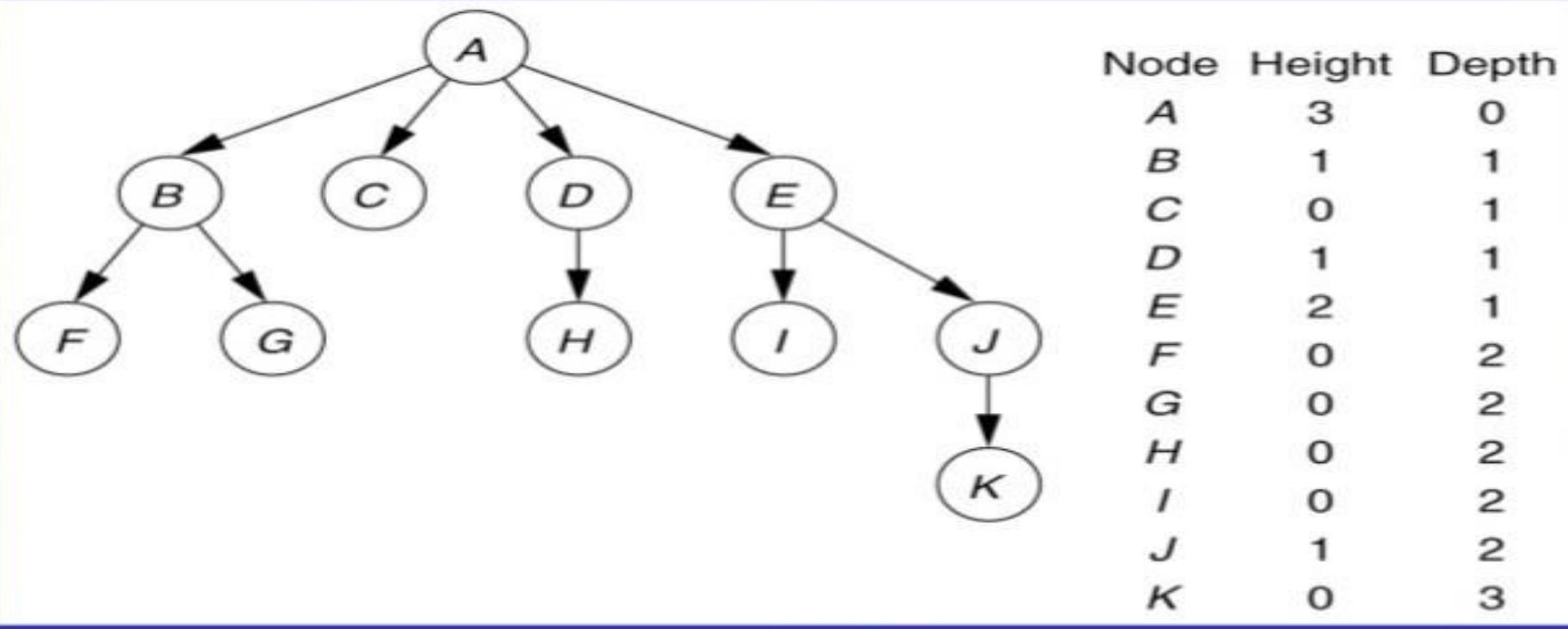
- The children of a node are, themselves, trees, called subtrees.



Tree Anatomy

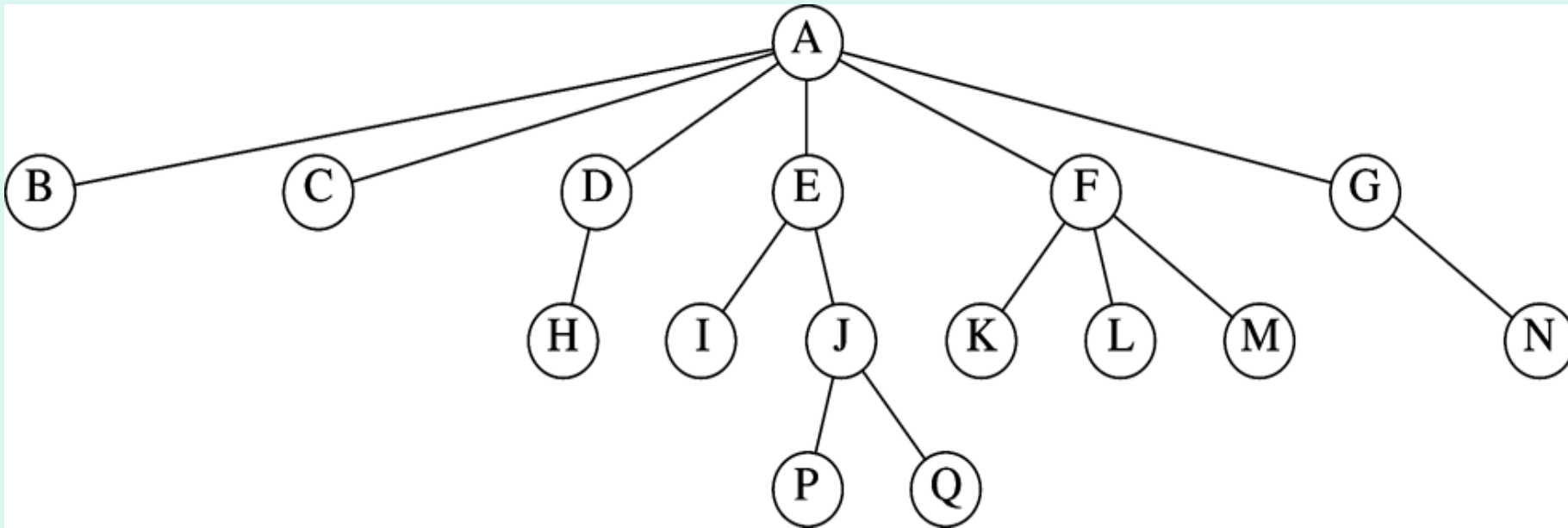
Figure

A tree, with height and depth information



Problems based on Rooted Tree

- Which are the parent nodes?
- Which are the child nodes?
- Which are the leaves?
- What is the height and depth of the tree?
- What is the height and depth of node *E*? Node *F*?



***m*-ary Tree**

A rooted tree is called an *m-ary tree* if every internal vertex has at most m children. The tree is called a *full m-ary tree* if every internal vertex has exactly m children. An *m-ary tree* with $m=2$ is called a *binary tree*.

- A full *m-ary tree* with i internal vertices contains $n = mi+1$ vertices.