CSCI 420 Computer Graphics
Lecture 22

Visualization

Height Fields and Contours
Scalar Fields
Volume Rendering
Vector Fields
[Angel Ch. 11]

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Scientific Visualization

- Generally do not start with a 3D triangle model
- Must deal with very large data sets
  - MRI, e.g. 512 x 512 x 200 = 50MB points
  - Visible Human 512 x 512 x 1734 = 433 MB points
- Visualize both real-world and simulation data
- User interaction
- Automatic search for relevant data

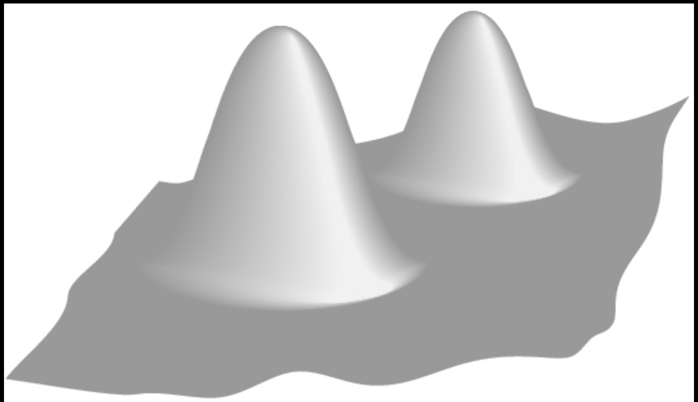
Types of Data

- Scalar fields (3D volume of scalars)
  - E.g., x-ray densities (MRI, CT scan)
- Vector fields (3D volume of vectors)
  - E.g., velocities in a wind tunnel
- Tensor fields (3D volume of tensors [matrices])
  - E.g., stresses in a mechanical part
- Static or dynamic through time

Height Field

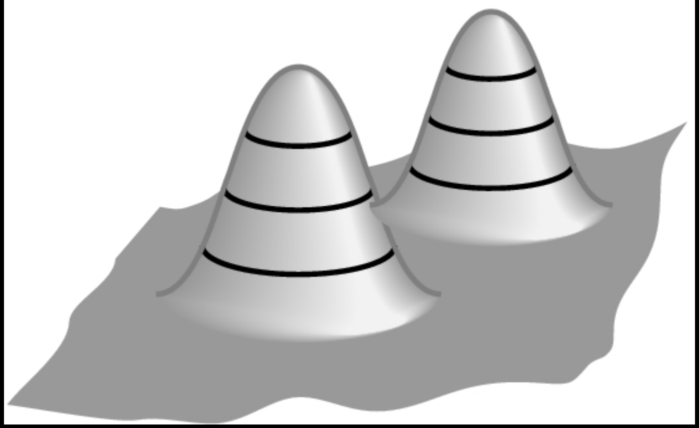
- Visualizing an explicit function

$$z = f(x,y)$$



- Adding contour curves

$$f(x,y) = c$$



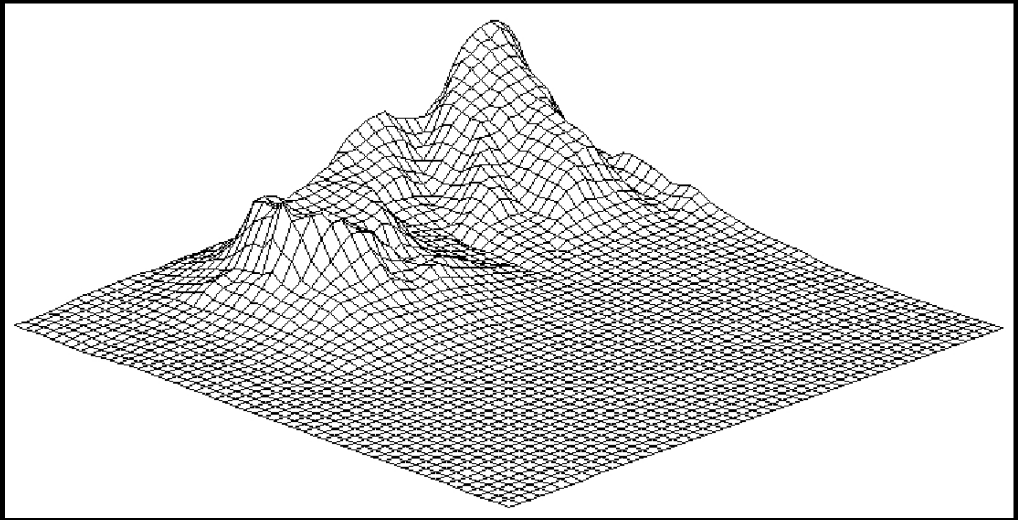
Visualizing the Height Field: Meshes

- Function is sampled (given) at x_i, y_j, $0 \leq i, j \leq n$
- Assume equally spaced

$$x_i = x_0 + i\Delta x$$
$$y_j = y_0 + j\Delta y$$

$$z_{ij} = f(x_i, y_j)$$

- Generate quadrilateral or triangular mesh
- [Assignment 1]



Visualizing the Height Field: Contour Curves

- Recall: implicit curve f(x,y) = 0
- $f(x,y) < 0$ inside, $f(x,y) > 0$ outside
- Here: contour curve at f(x,y) = c
- Implicit function f sampled at regular intervals for x,y

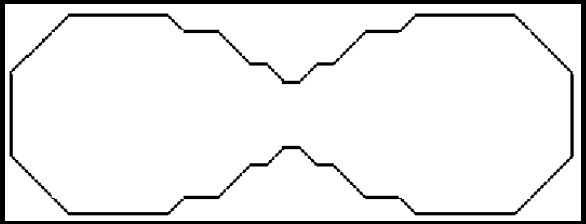
$$x_i = x_0 + i\Delta x$$
$$y_j = y_0 + j\Delta y$$

- How can we draw the curve?

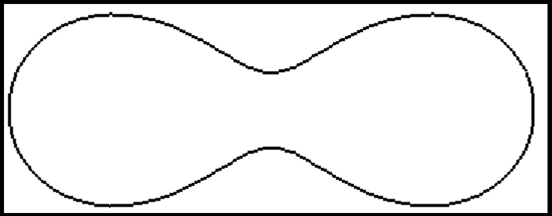
Contour Curves Examples

- Ovals of Cassini, 50 x 50 grid

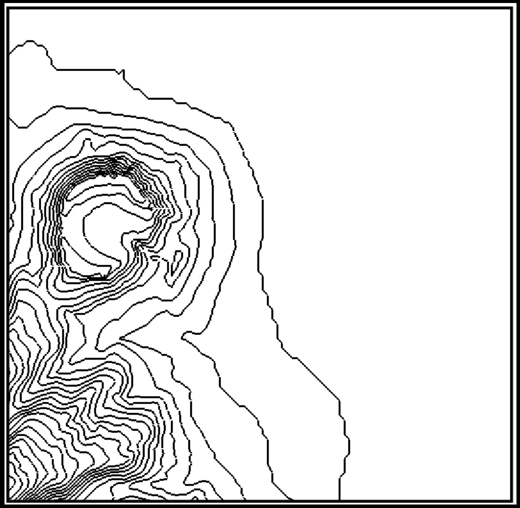
$$f(x,y) = (x^2 + y^2 + a^2)^2 - 4a^2x^2 - b^4$$
$$a = 0.49, b = 0.5$$



Midpoint



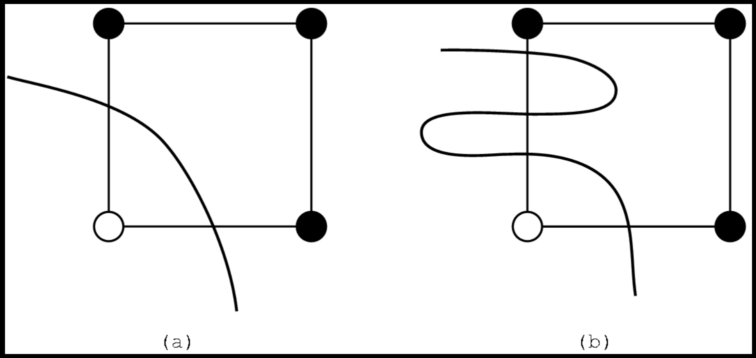
Interpolation



Contour plot of Honolulu data

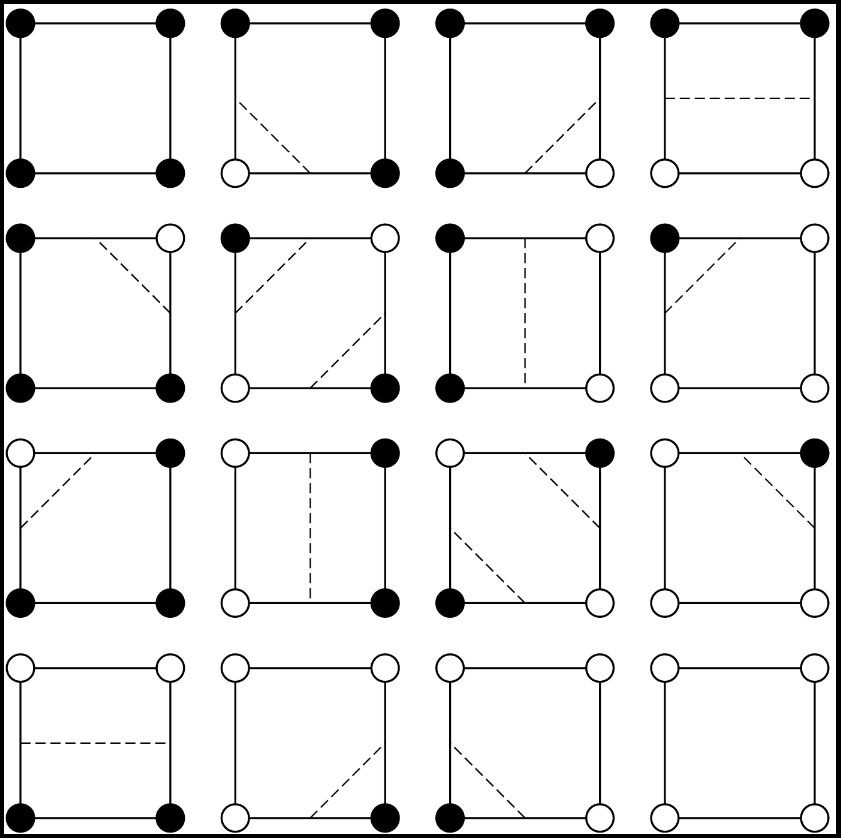
Marching Squares

- Sample function f at every grid point x_i, y_j
- For every point $f_{i\,j} = f(x_i, y_j)$ either $f_{i\,j} \le c$ or $f_{i\,j} > c$
- Distinguish those cases for each corner x
  - White: $f_{i\,j} \le c$
  - Black: $f_{i\,j} > c$
- Now consider cases for curve
- Assume “smooth”

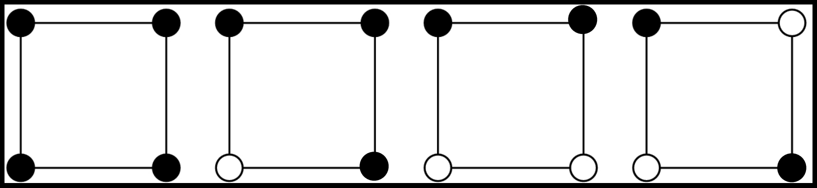


Cases for Vertex Labels

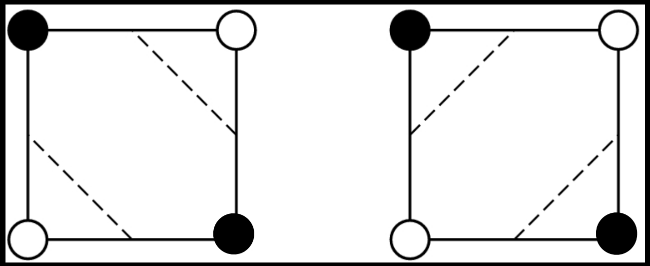
16 cases for vertex labels



4 unique cases modulo symmetries

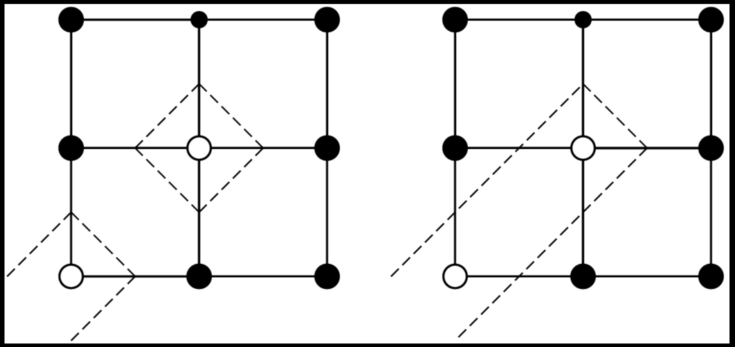


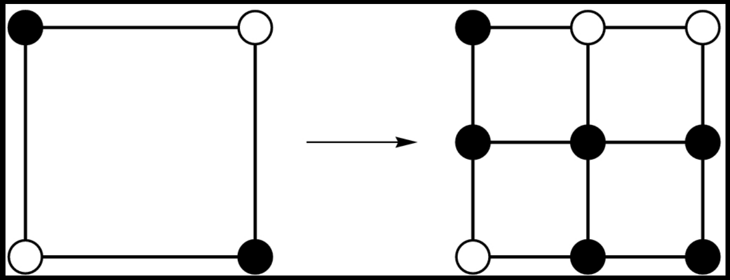
Ambiguities of Labelings



Ambiguous labels

Different resulting contours





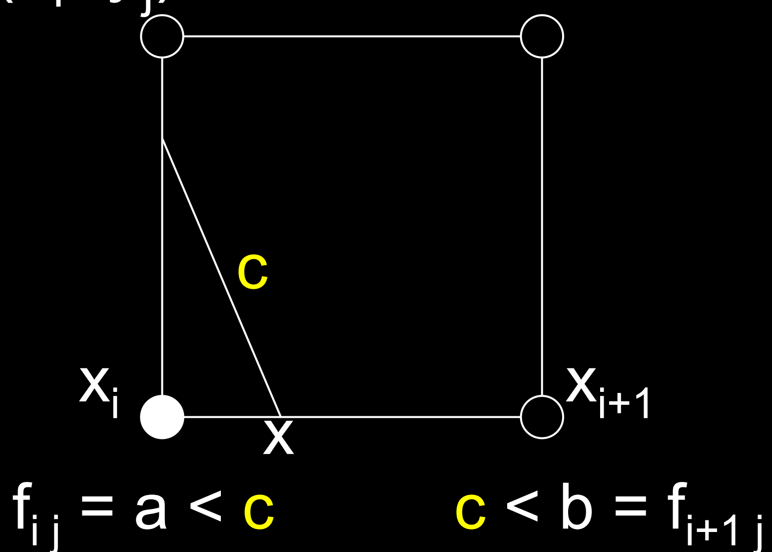
Resolution by subdivision
(if such higher resolution available / possible)

Interpolating Intersections

- Approximate intersection
  - Midpoint between x_i, x_{i+1} and y_j, y_{j+1}
  - Better: interpolate
- If $f_{i\,j} = a$ is closer to c than $b = f_{i+1\,j}$ then intersection is closer to (x_i, y_j):

$$\frac{x - x_i}{x_{i+1} - x} = \frac{c - a}{b - c}$$

- Analogous calculation for y direction



Outline

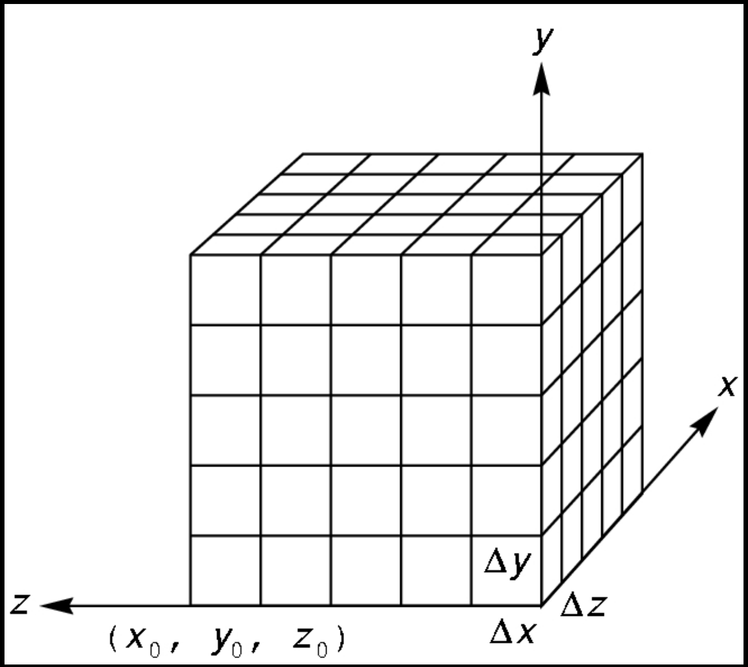
- Height Fields and Contours
- Scalar Fields
- Volume Rendering
- Vector Fields

Scalar Fields

- Volumetric data sets
- Example: tissue density
- Assume again regularly sampled

$$x_i = x_0 + i\Delta x$$
$$y_j = y_0 + j\Delta y$$
$$z_k = z_0 + k\Delta z$$

- Represent as voxels

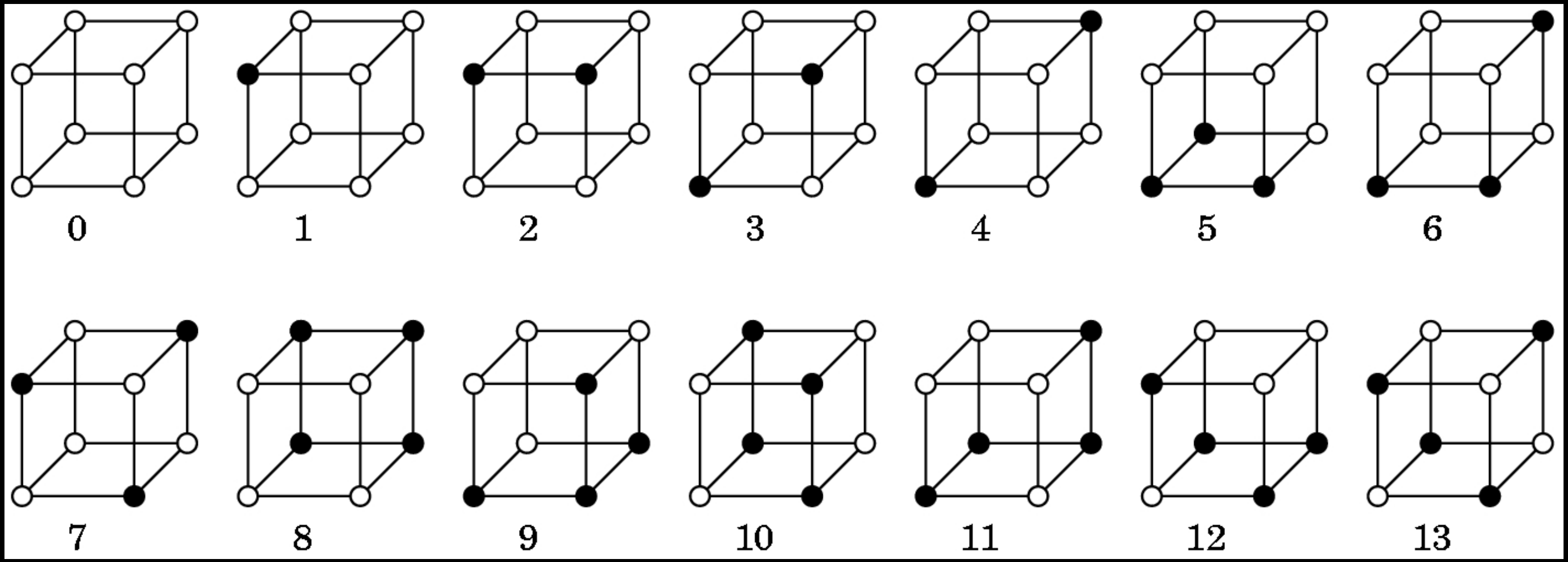


Isosurfaces

- $f(x,y,z)$ represents volumetric data set
- Two rendering methods
  - Isosurface rendering
  - Direct volume rendering (use all values [next])
- Isosurface given by $f(x,y,z) = c$
- Recall implicit surface $g(x, y, z)$:
  - $g(x, y, z) < 0$ inside
  - $g(x, y, z) = 0$ surface
  - $g(x, y, z) > 0$ outside
- Generalize right-hand side from 0 to c

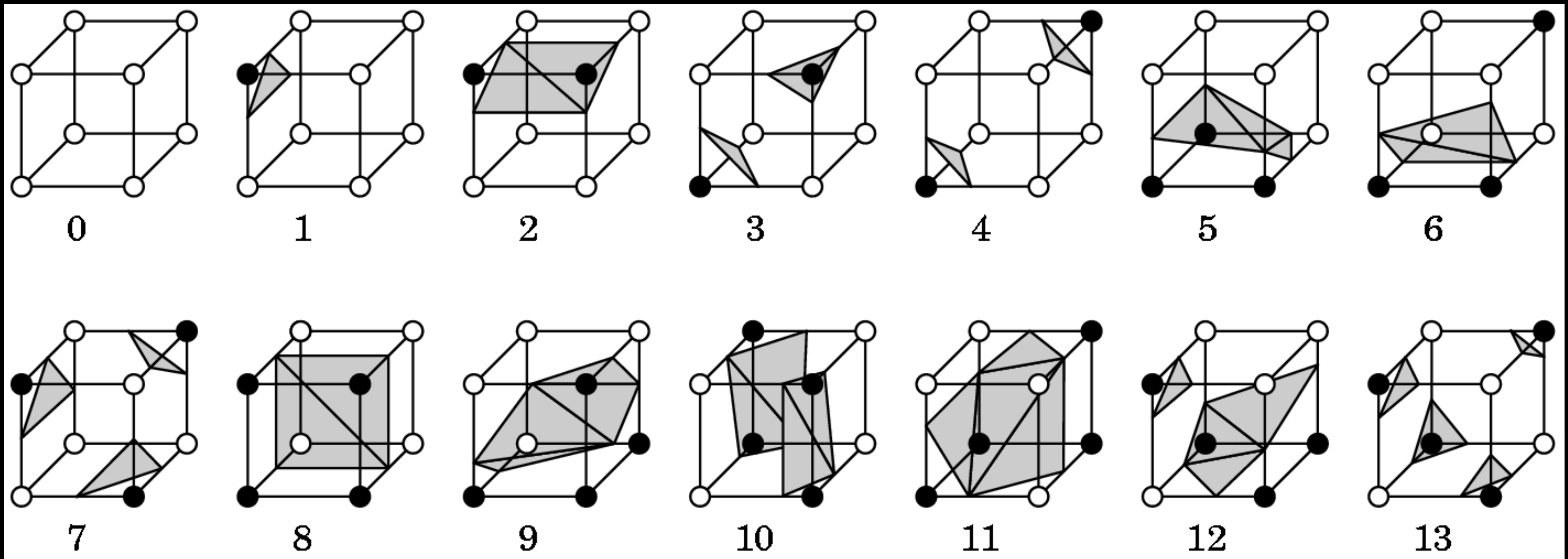
Marching Cubes

- Display technique for isosurfaces
- 3D version of marching squares
- 14 cube labelings (after elimination of symmetries)



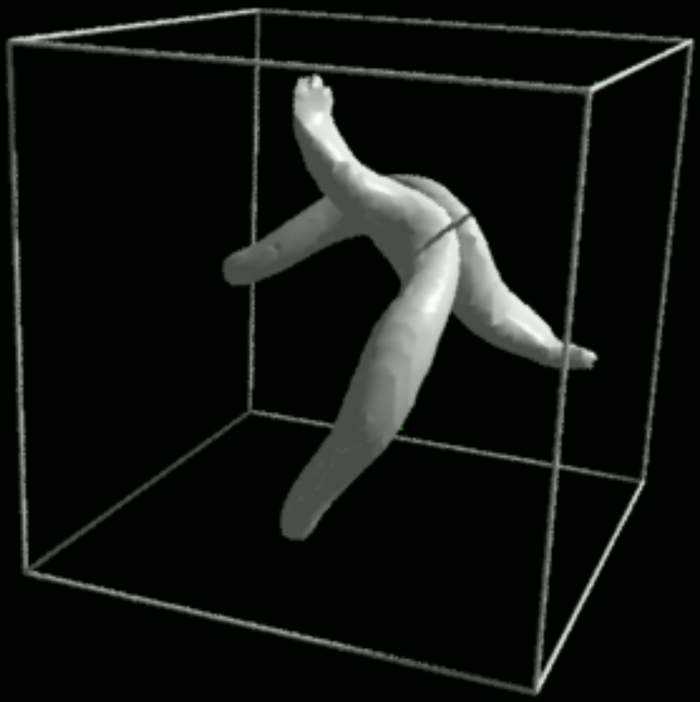
Marching Cube Tessellations

- Generalize marching squares, just more cases
- Interpolate as in 2D
- Ambiguities similar to 2D

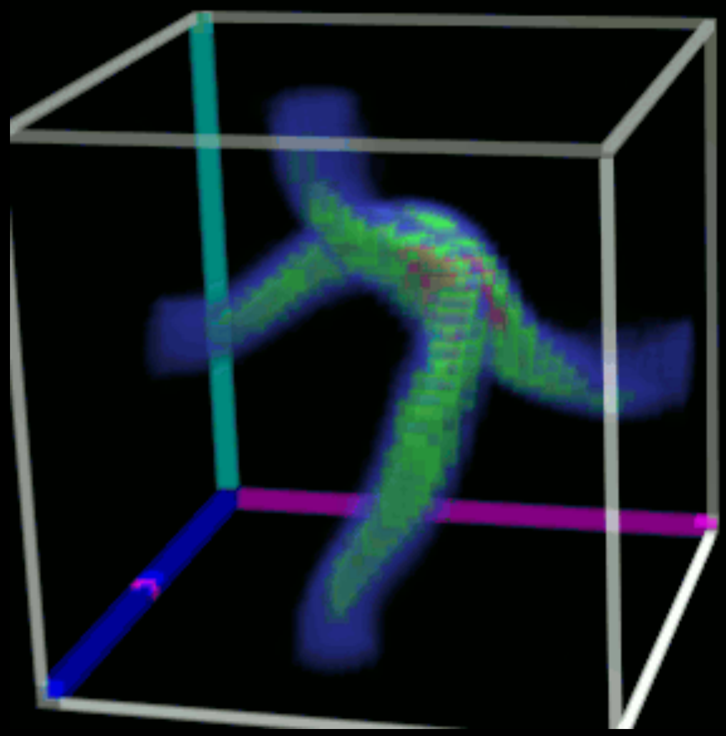


Volume Rendering

- Sometimes isosurfaces are unnatural or do not give sufficient information
- Use all voxels and transparency (α-values)



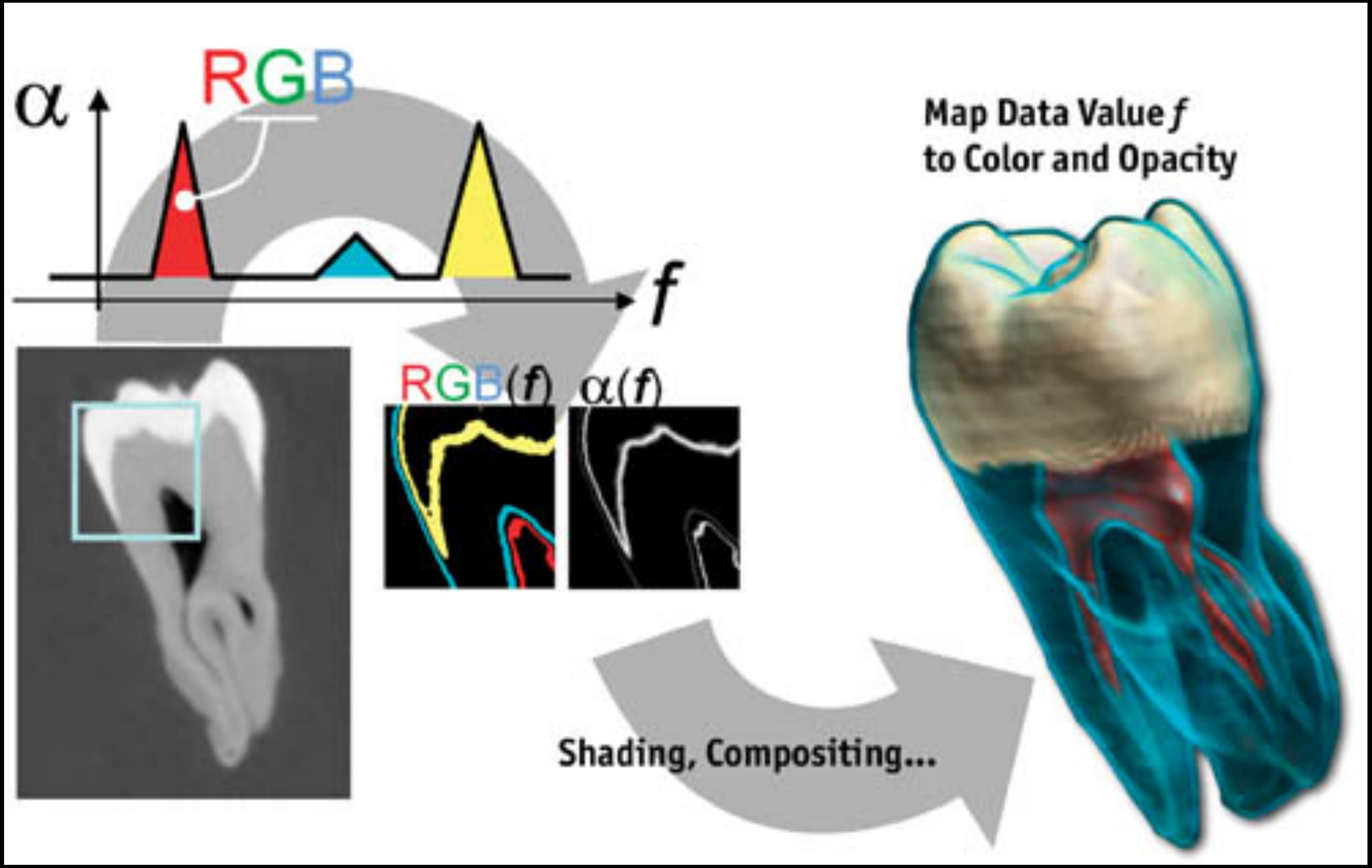
Ray-traced isosurface



Volume rendering

Volume Rendering Example

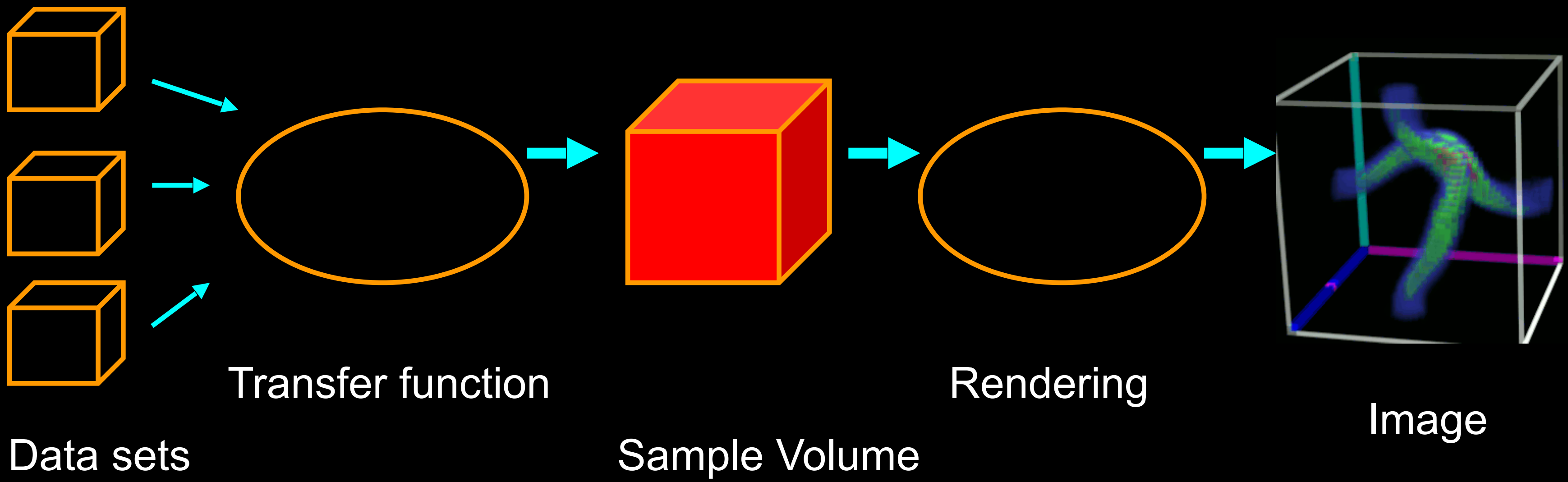
Rendering 3d tooth volume data



Source:
Nvidia

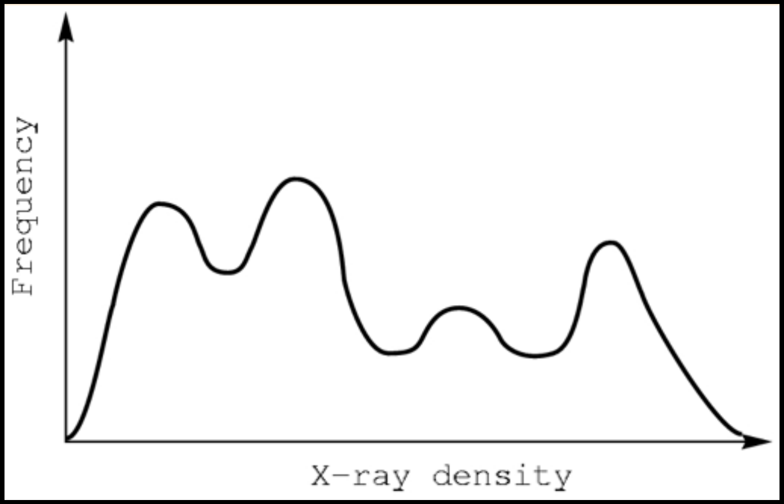
Volume Rendering Pipeline

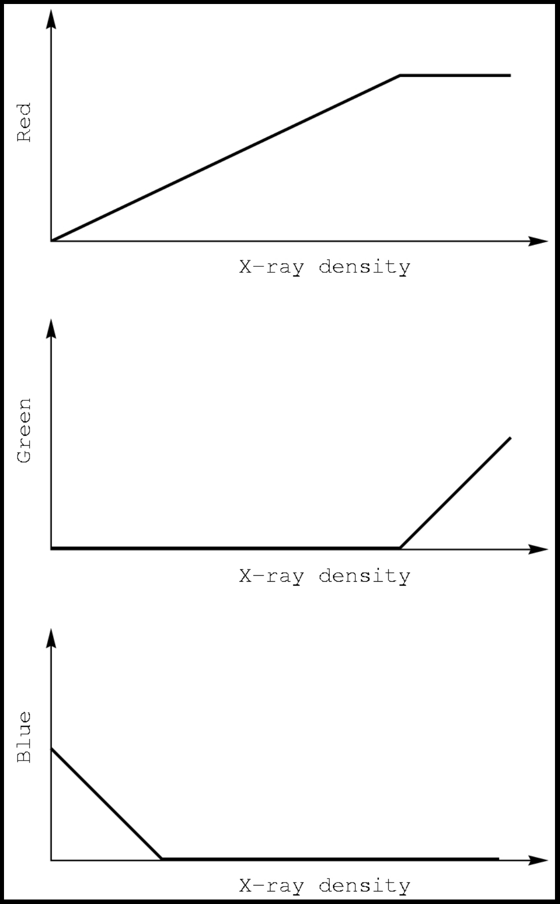
- Transfer function: converts input data set to colors and opacities
  - Example input: 256 x 256 x 256 x 8 bytes = 128 MB
  - Convert to 24 bit color, 8 bit opacity



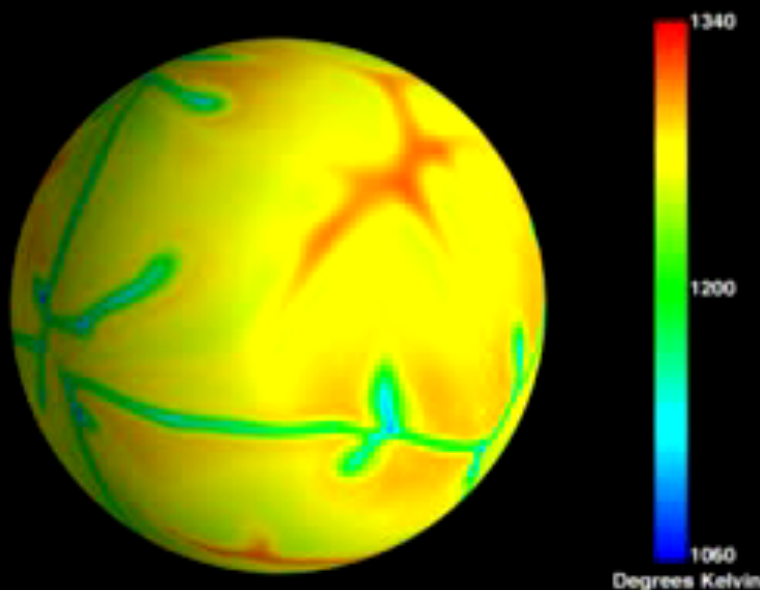
Transfer Functions

- Transform scalar data values to RGBA values
- Apply to every voxel in volume
- Highly application dependent
- Start from data histogram
- Opacity for emphasis

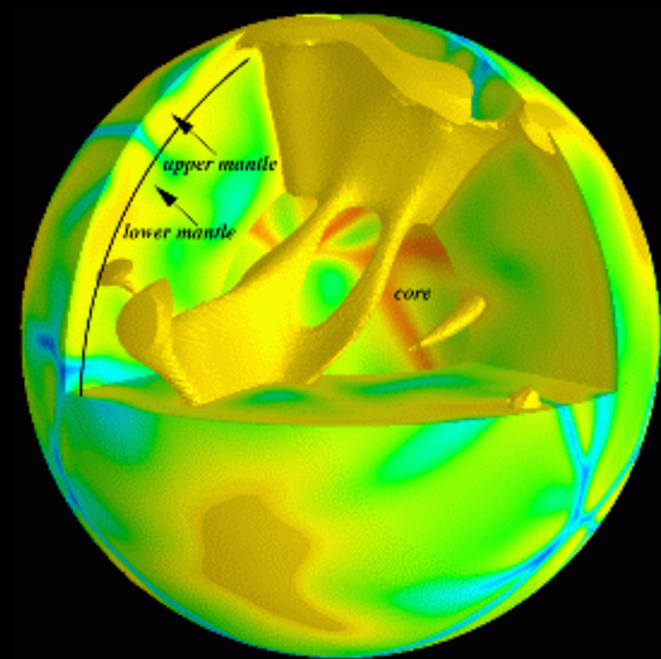




Transfer Function Example



Mantle Heat Convection



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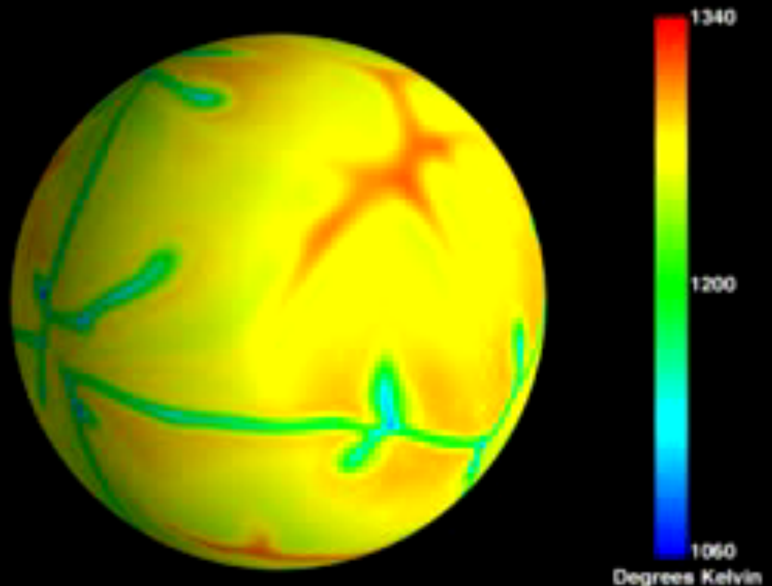
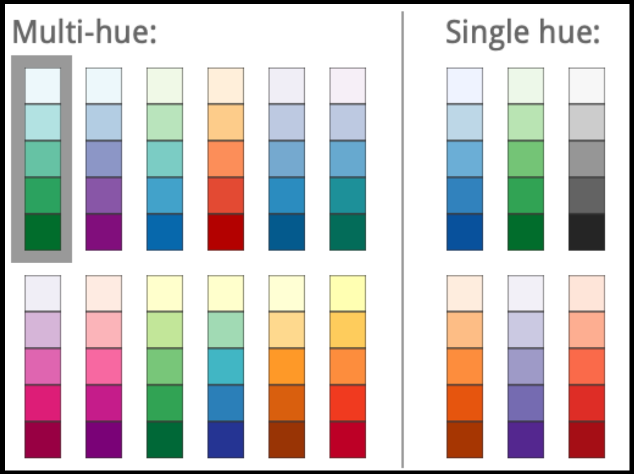
Side note on colormaps



You should not use the jet colormap

Modern, perceptual colormaps at colorbrewer.org (or in matplotlib)

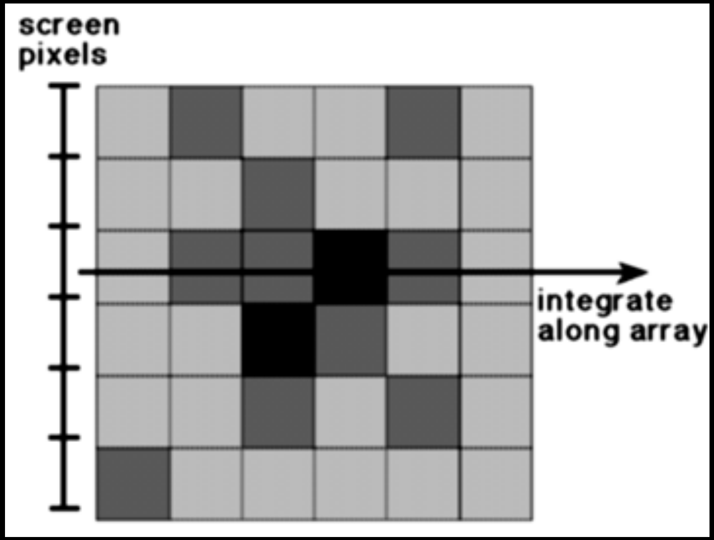


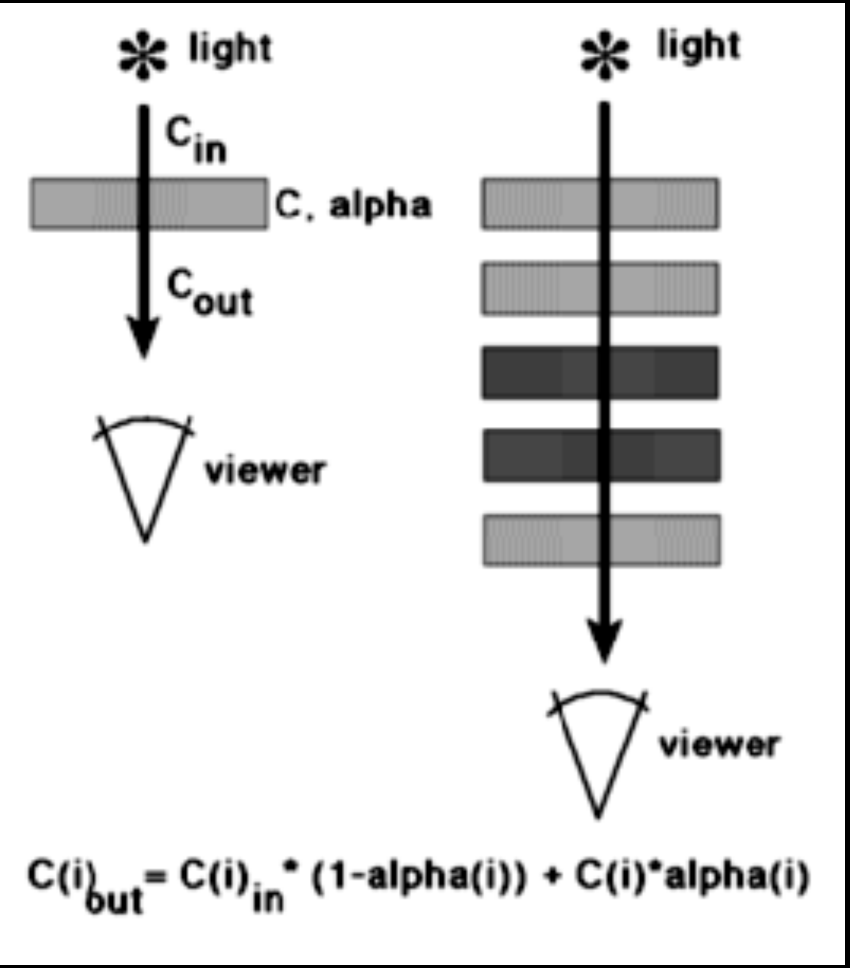
Volume Ray Casting

- Three volume rendering techniques
  - Volume ray casting
  - Splatting
  - 3D texture mapping
- Ray Casting
  - Integrate color through volume
  - Consider lighting (surfaces?)
  - Use regular x,y,z data grid when possible
  - Finite elements when necessary (e.g., ultrasound)
  - 3D-rasterize geometrical primitives

Accumulating Opacity

- α = 1.0 is opaque
- Composite multiple layers according to opacity
- Use local gradient of opacit for enhanced
  display of boundaries





Surface vs. Volume Rendering

- 3D model of surfaces
- Convert to triangles
- Draw primitives
- Lose or disguise data
- Good for opaque objects

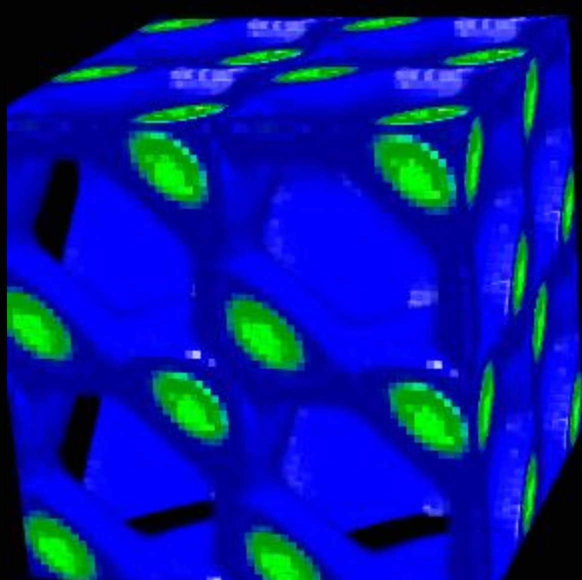
- Scalar field in 3D
- Convert it to RGBA values
- Render volume “directly”
- See data as given
- Good for complex objects

Sample Applications

- Medical
  - Computed Tomography (CT)
  - Magnetic Resonance Imaging (MRI)
  - Ultrasound
- Engineering and Science
  - Computational Fluid Dynamic (CFD)
  - Aerodynamic simulations
  - Meteorology
  - Astrophysics

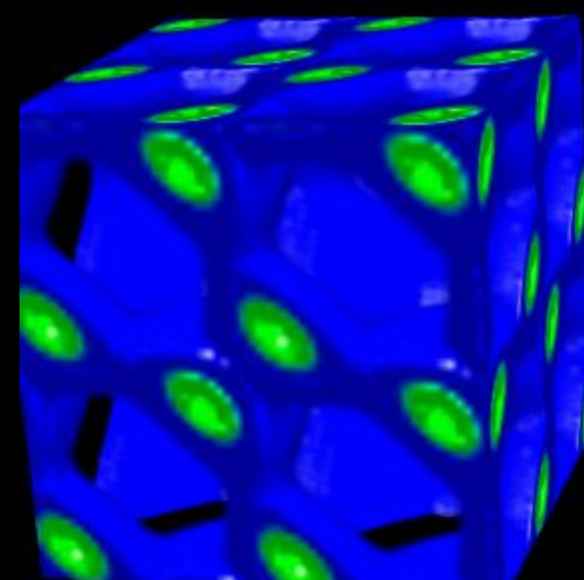
Trilinear Interpolation

- Interpolate to compute RGBA away from grid
- Nearest neighbor yields blocky images
- Use trilinear interpolation
- 3D generalization of bilinear interpolation



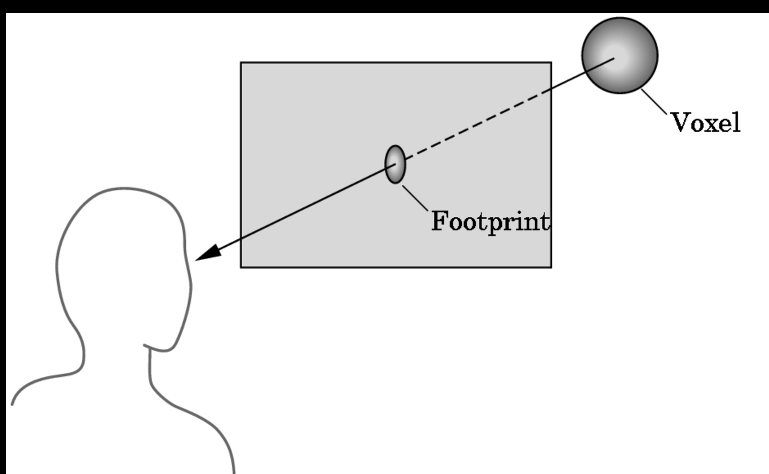
Nearest neighbor

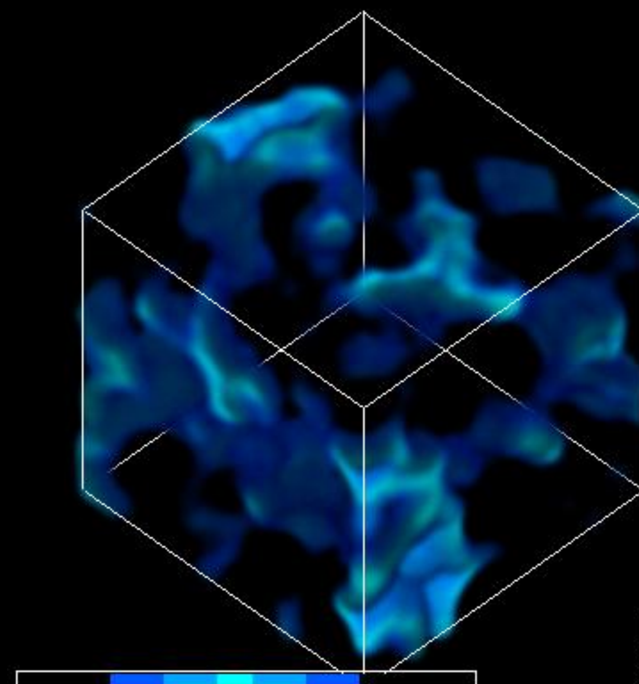
Trilinear interpolation



Splatting

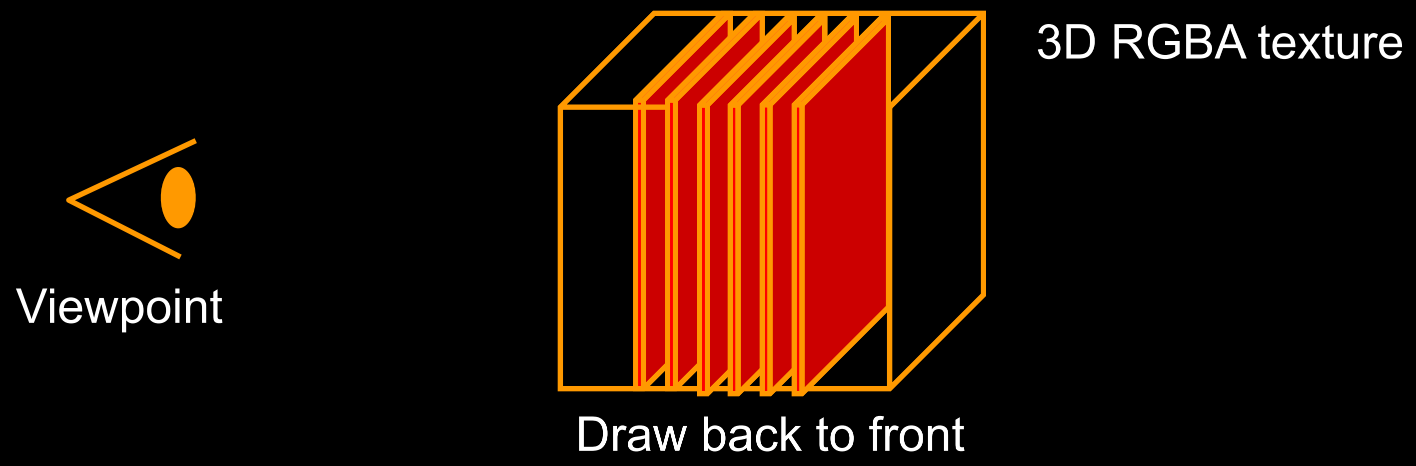
- Alternative to ray tracing
- Assign shape to each voxel (e.g., Gaussian)
- Project onto image plane (splat)
- Draw voxels back-to-front
- Composite (α-blend)



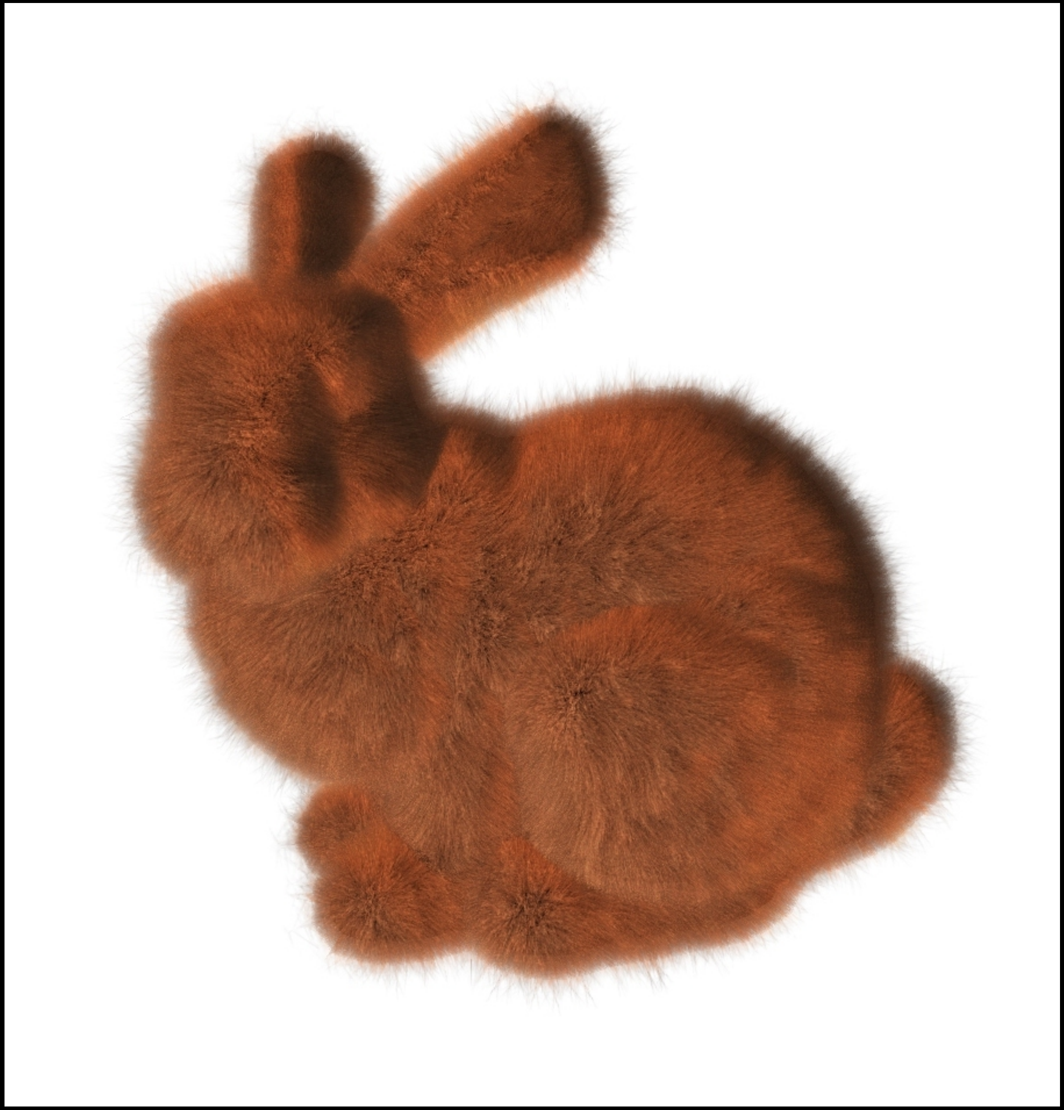


3D Textures

- Alternative to ray tracing, splatting
- Build a 3D texture (including opacity)
- Draw a stack of polygons, back-to-front
- Efficient if supported in graphics hardware
- Few polygons, much texture memory



Example: 3D Textures

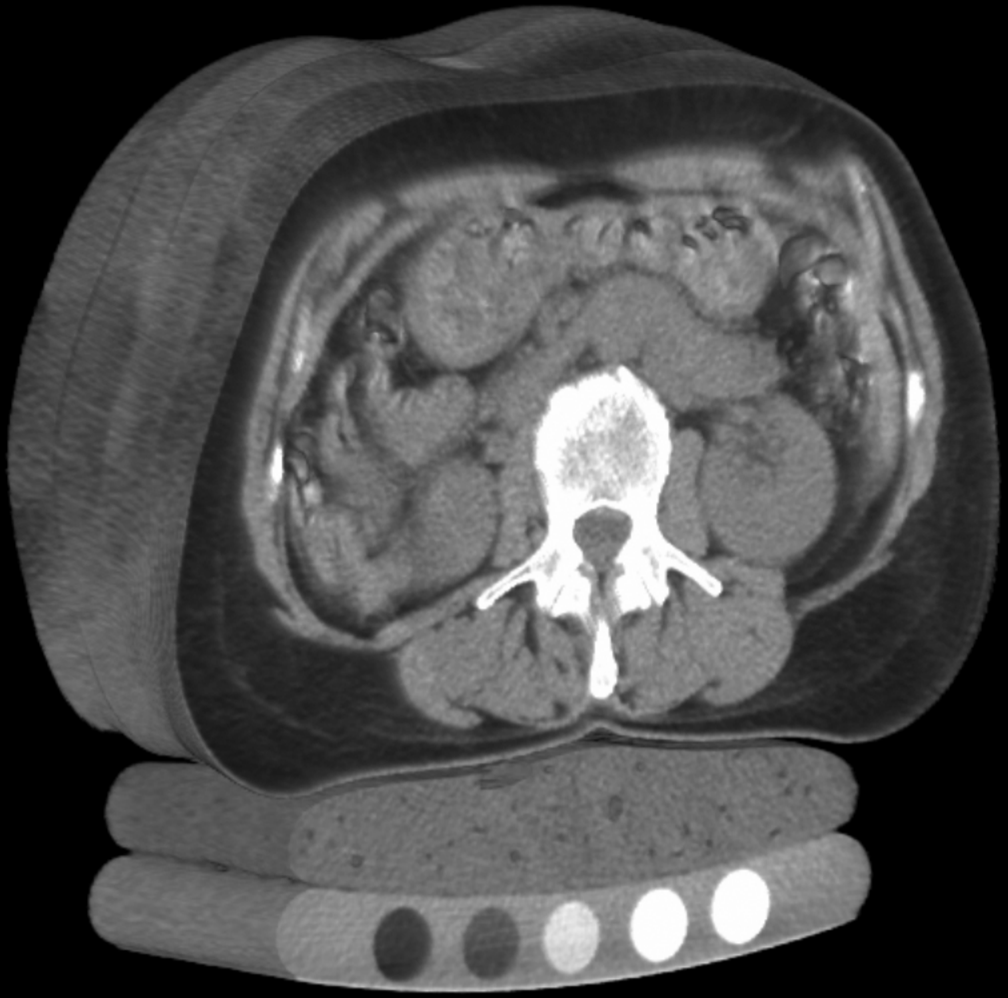


Emil Praun'01

Other Techniques

- Use CSG for cut-aways

Human torso



Source: Wikipedia

Acceleration of Volume Rendering

- Basic problem: Huge data sets
- Must program for locality (cache)
- Divide into multiple blocks if necessary
  - Example: marching cubes
- Use error measures to stop iteration
- Exploit parallelism

Outline

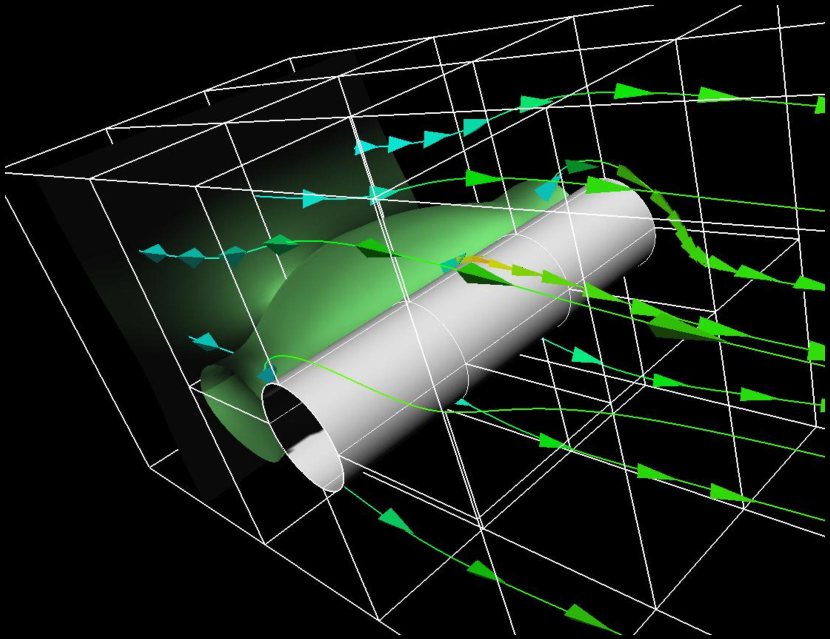
- Height Fields and Contours
- Scalar Fields
- Volume Rendering
- Vector Fields

Vector Fields

- Visualize vector at each (x,y,z) point
  - Example: velocity field
  - Example: hair
- Hedgehogs
  - Use 3D directed line segments (sample field)
  - Orientation and magnitude determined by vector
- Animation
  - Use for still image
  - Particle systems

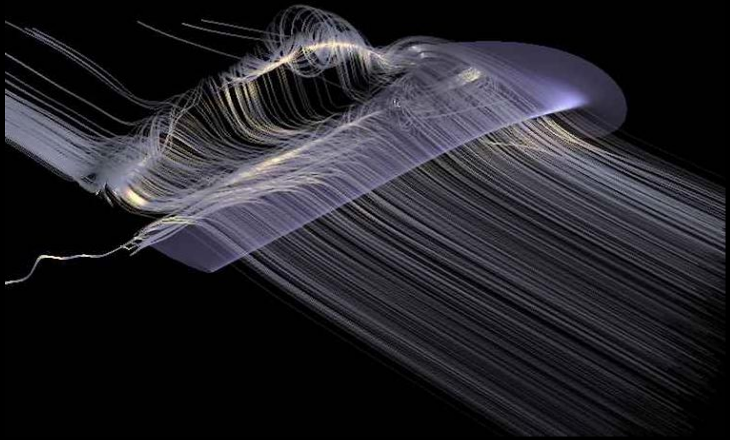
Blood flow in
human carotid artery

Using Glyphs and Streaklines

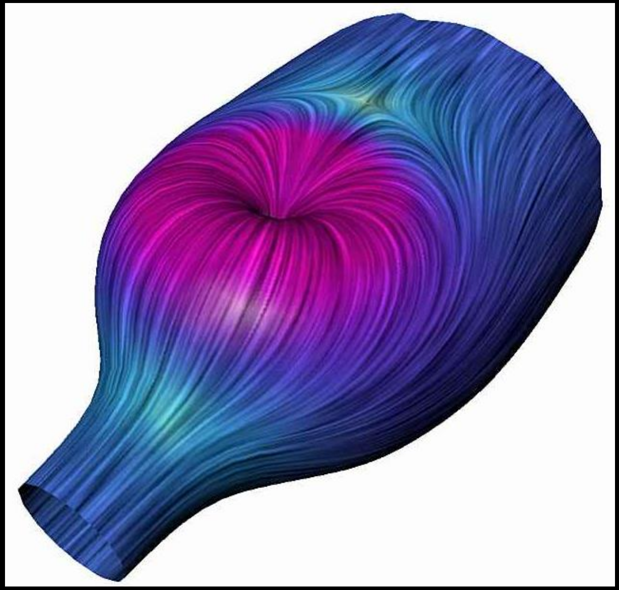


Glyphs for air flow

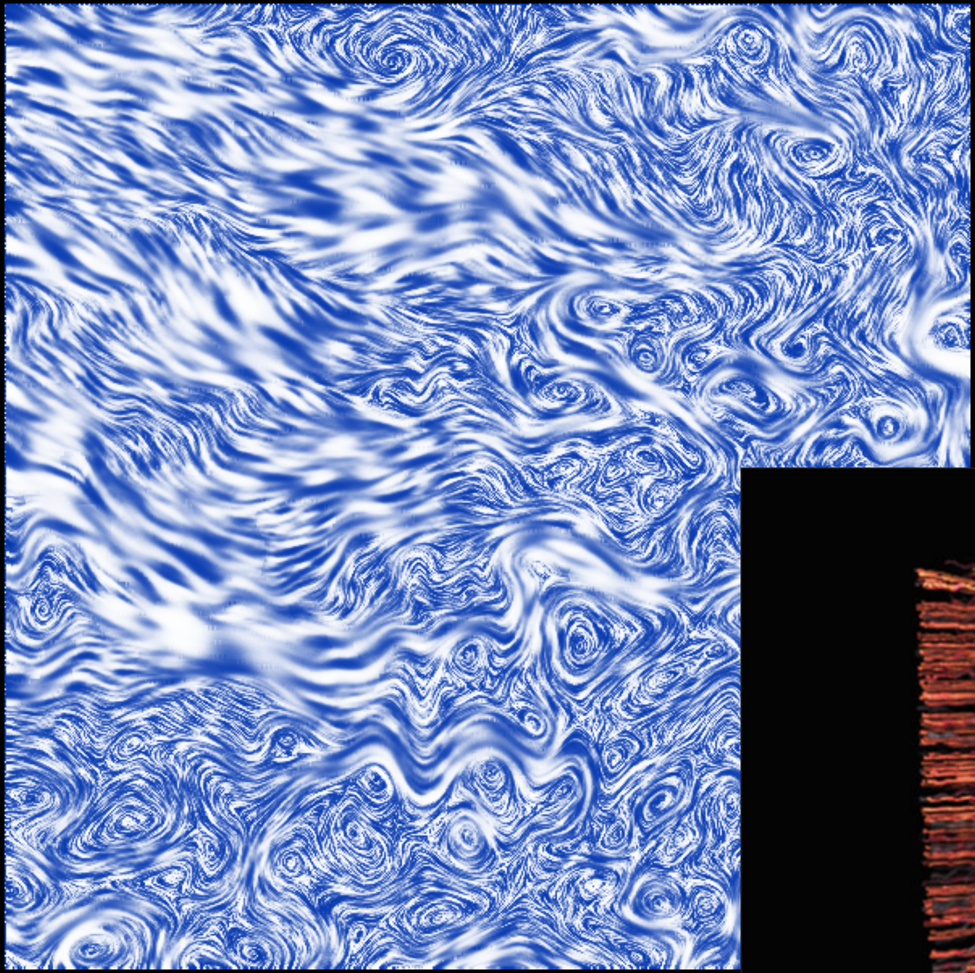
University of Utah



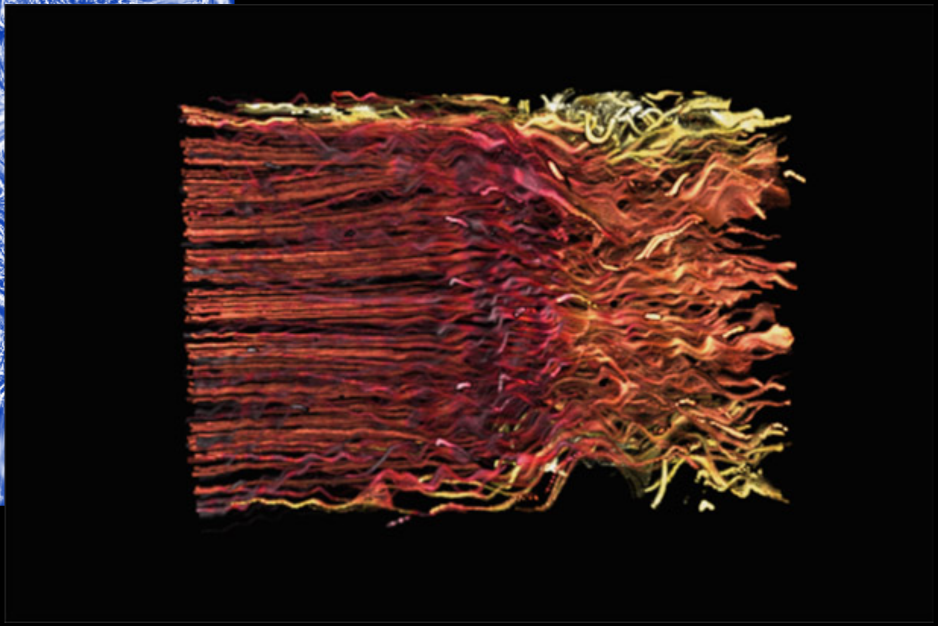
Glyph = marker (for example, an arrow) used for data visualization



More Flow Examples



Banks and Interrante



Summary

- Height Fields and Contours
- Scalar Fields
  – Isosurfaces
  – Marching cubes
- Volume Rendering
  – Volume ray tracing
  – Splatting
  – 3D Textures
- Vector Fields
  – Hedgehogs
  – Animated and interactive visualization