

Introduction to AI - assignment 4

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1 Introduction

In this assignment we provide a Bayesian Network for the hurricane problem from assignment 1.

2 Bayesian Network construction

We built our BN in the following manner. The nodes of the BN are as described in the assignment:

3 types of variables (BN nodes): **blockages** (one for each edge) **flooding** (one for each vertex,) and **evacuees** present (one for each vertex).

Each **flooding** node of vertex v point to all **blockage** nodes of edges $\{\{v, u\} : u \in V\}$.

All **blockage** nodes of edges $\{\{v, u\} : v, u \in V\}$ point to **evacuees** nodes of vertices u and v .

3 Probabilistic reasoning algorithm

Our probability reasoning algorithm is the simple *Enumeration Algorithm*.

4 Run example

4.1 First example - the setting that was given in the assignment

In this example we check that the following path is free of blocked edges: 1,2

4.1.1 Input

file: "input_graph2.txt"

```
#V 4          ; number of vertices n in graph (from 1 to n)
```

```
#V 0 F 0.2    ; Vertex 0, probability flooding 0.2
```

```
#V 1 F 0.4    ; Vertex 1, probability flooding 0.4
```

```
#E0 0 1 1 ; Edge0 between vertices 0 and 1, weight 1
```

```
#E1 1 2 3 ; Edge1 between vertices 1 and 2, weight 3
#E2 2 3 3 ; Edge2 between vertices 2 and 3, weight 3
#E3 1 3 4 ; Edge3 between vertices 1 and 3, weight 4
```

4.1.2 Output

Vertex0

```
P(Flood)=20.0%
P(!Flood)=80.0%
P(Evacuees|!Blockage0 )=0.1%
P(Evacuees|Blockage0 )=40.0%
P(!Evacuees|!Blockage0 )=99.9%
P(!Evacuees|Blockage0 )=60.0%
```

$P(\text{Evacuees } 0 \mid []) = 0.13334032$

Vertex1

```
P(Flood)=40.0%
P(!Flood)=60.0%
P(Evacuees|!Blockage0 !Blockage1 !Blockage3 )=0.1%
P(Evacuees|!Blockage0 !Blockage1 Blockage3 )=40.0%
P(Evacuees|!Blockage0 Blockage1 !Blockage3 )=40.0%
P(Evacuees|!Blockage0 Blockage1 Blockage3 )=16.000000000000004%
P(Evacuees|Blockage0 !Blockage1 !Blockage3 )=40.0%
P(Evacuees|Blockage0 !Blockage1 Blockage3 )=16.000000000000004%
P(Evacuees|Blockage0 Blockage1 !Blockage3 )=16.000000000000004%
P(Evacuees|Blockage0 Blockage1 Blockage3 )=6.400000000000001%
P(!Evacuees|!Blockage0 !Blockage1 !Blockage3 )=99.9%
P(!Evacuees|!Blockage0 !Blockage1 Blockage3 )=60.0%
P(!Evacuees|!Blockage0 Blockage1 !Blockage3 )=60.0%
P(!Evacuees|!Blockage0 Blockage1 Blockage3 )=84.0%
P(!Evacuees|Blockage0 !Blockage1 !Blockage3 )=60.0%
P(!Evacuees|Blockage0 !Blockage1 Blockage3 )=84.0%
P(!Evacuees|Blockage0 Blockage1 !Blockage3 )=84.0%
P(!Evacuees|Blockage0 Blockage1 Blockage3 )=93.6%
```

$P(\text{Evacuees } 1 \mid []) = 0.13003669191184003$

Vertex2

```
P(Flood)=0.0%
P(!Flood)=100.0%
P(Evacuees|!Blockage1 !Blockage2 )=0.1%
P(Evacuees|!Blockage1 Blockage2 )=40.0%
```

$P(\text{Evacuees} | \text{Blockage1 } !\text{Blockage2}) = 40.0\%$
 $P(\text{Evacuees} | \text{Blockage1 Blockage2}) = 16.000000000000004\%$
 $P(!\text{Evacuees} | !\text{Blockage1 } !\text{Blockage2}) = 99.9\%$
 $P(!\text{Evacuees} | !\text{Blockage1 Blockage2}) = 60.0\%$
 $P(!\text{Evacuees} | \text{Blockage1 } !\text{Blockage2}) = 60.0\%$
 $P(!\text{Evacuees} | \text{Blockage1 Blockage2}) = 84.0\%$

$P(\text{Evacuees } 2 | []) = 0.033506896599999995$

Vertex3

 $P(\text{Flood}) = 0.0\%$
 $P(!\text{Flood}) = 100.0\%$
 $P(\text{Evacuees} | !\text{Blockage2 } !\text{Blockage3}) = 0.1\%$
 $P(\text{Evacuees} | !\text{Blockage2 Blockage3}) = 40.0\%$
 $P(\text{Evacuees} | \text{Blockage2 } !\text{Blockage3}) = 40.0\%$
 $P(\text{Evacuees} | \text{Blockage2 Blockage3}) = 16.000000000000004\%$
 $P(!\text{Evacuees} | !\text{Blockage2 } !\text{Blockage3}) = 99.9\%$
 $P(!\text{Evacuees} | !\text{Blockage2 Blockage3}) = 60.0\%$
 $P(!\text{Evacuees} | \text{Blockage2 } !\text{Blockage3}) = 60.0\%$
 $P(!\text{Evacuees} | \text{Blockage2 Blockage3}) = 84.0\%$

$P(\text{Evacuees } 3 | []) = 0.0255396766$

Edge0

 $P(\text{Blockage } 0 | !\text{flood0 } !\text{flood1}) = 0.001$
 $P(\text{Blockage } 0 | !\text{flood0 flood1}) = 0.6$
 $P(\text{Blockage } 0 | \text{flood0 } !\text{flood1}) = 0.6$
 $P(\text{Blockage } 0 | \text{flood0 flood1}) = 0.84$

$P(\text{Blockage } 0 | []) = 0.33168$

Edge1

 $P(\text{Blockage } 1 | !\text{flood1 } !\text{flood2}) = 0.001$
 $P(\text{Blockage } 1 | !\text{flood1 flood2}) = 0.19999999999999998$
 $P(\text{Blockage } 1 | \text{flood1 } !\text{flood2}) = 0.19999999999999998$
 $P(\text{Blockage } 1 | \text{flood1 flood2}) = 0.35999999999999999$

$P(\text{Blockage } 1 | []) = 0.0806$

Edge2

 $P(\text{Blockage } 2 | !\text{flood2 } !\text{flood3}) = 0.001$
 $P(\text{Blockage } 2 | !\text{flood2 flood3}) = 0.19999999999999998$

```
P(Blockage 2|flood2 !flood3)=0.19999999999999998
P(Blockage 2|flood2 flood3)=0.35999999999999999
```

```
P(Blockage 2 | []) = 0.00100000000000000002
```

```
Edge3
```

```
-----
P(Blockage 3|!flood1 !flood3)=0.001
P(Blockage 3|!flood1 flood3)=0.15
P(Blockage 3|flood1 !flood3)=0.15
P(Blockage 3|flood1 flood3)=0.27750000000000001
```

```
P(Blockage 3 | []) = 0.060599999999999999
```

```
-----
The probability that the given path is free from blockages is 0.91848060000000001
-----
```

4.1.3 Brief explanation

As we can see, since the probability of the flooding on the vertices of the path: 1, 2, 3 is low, the probability that the given path is free of blockages is high.

4.2 Second example

In this example we check that the following path is free of blocked edges: 0,2

4.2.1 Input

```
file: "input_graph1.txt"
```

```
#V 4          ; number of vertices n in graph (from 1 to n)
```

```
#V 0 F 0.8    ; Vertex 0, probability flooding 0.8
```

```
#V 1 F 0.5    ; Vertex 1, probability flooding 0.5
```

```
#V 2 F 0.5    ; Vertex 2, probability flooding 0.5
```

```
#V 3 F 0.2    ; Vertex 3, probability flooding 0.2
```

```
#E0 0 1 1 ; Edge0 between vertices 0 and 1, weight 1
```

```
#E1 0 2 1 ; Edge1 between vertices 0 and 2, weight 3
```

```
#E2 2 3 1 ; Edge2 between vertices 2 and 3, weight 3
```

4.2.2 Output

Vertex0

P(Flood)=80.0%
P(!Flood)=19.999999999999996%
P(Evacuees|!Blockage0 !Blockage1)=0.1%
P(Evacuees|!Blockage0 Blockage1)=40.0%
P(Evacuees|Blockage0 !Blockage1)=40.0%
P(Evacuees|Blockage0 Blockage1)=16.000000000000004%
P(!Evacuees|!Blockage0 !Blockage1)=99.9%
P(!Evacuees|!Blockage0 Blockage1)=60.0%
P(!Evacuees|Blockage0 !Blockage1)=60.0%
P(!Evacuees|Blockage0 Blockage1)=84.0%

P(Evacuees 0 | []) = 0.23206134805000003

Vertex1

P(Flood)=50.0%
P(!Flood)=50.0%
P(Evacuees|!Blockage0)=0.1%
P(Evacuees|Blockage0)=40.0%
P(!Evacuees|!Blockage0)=99.9%
P(!Evacuees|Blockage0)=60.0%

P(Evacuees 1 | []) = 0.2548039

Vertex2

P(Flood)=50.0%
P(!Flood)=50.0%
P(Evacuees|!Blockage1 !Blockage2)=0.1%
P(Evacuees|!Blockage1 Blockage2)=40.0%
P(Evacuees|Blockage1 !Blockage2)=40.0%
P(Evacuees|Blockage1 Blockage2)=16.000000000000004%
P(!Evacuees|!Blockage1 !Blockage2)=99.9%
P(!Evacuees|!Blockage1 Blockage2)=60.0%
P(!Evacuees|Blockage1 !Blockage2)=60.0%
P(!Evacuees|Blockage1 Blockage2)=84.0%

P(Evacuees 2 | []) = 0.22567338088000002

Vertex3

P(Flood)=20.0%
P(!Flood)=80.0%

$P(\text{Evacuees} | \text{!Blockage2}) = 0.1\%$
 $P(\text{Evacuees} | \text{Blockage2}) = 40.0\%$
 $P(\text{!Evacuees} | \text{!Blockage2}) = 99.9\%$
 $P(\text{!Evacuees} | \text{Blockage2}) = 60.0\%$

$P(\text{Evacuees } 3 | []) = 0.15437559999999997$

Edge0

$P(\text{Blockage } 0 | \text{!flood0 !flood1}) = 0.001$
 $P(\text{Blockage } 0 | \text{!flood0 flood1}) = 0.6$
 $P(\text{Blockage } 0 | \text{flood0 !flood1}) = 0.6$
 $P(\text{Blockage } 0 | \text{flood0 flood1}) = 0.84$

$P(\text{Blockage } 0 | []) = 0.6361$

Edge1

$P(\text{Blockage } 1 | \text{!flood0 !flood2}) = 0.001$
 $P(\text{Blockage } 1 | \text{!flood0 flood2}) = 0.6$
 $P(\text{Blockage } 1 | \text{flood0 !flood2}) = 0.6$
 $P(\text{Blockage } 1 | \text{flood0 flood2}) = 0.84$

$P(\text{Blockage } 1 | []) = 0.6361$

Edge2

$P(\text{Blockage } 2 | \text{!flood2 !flood3}) = 0.001$
 $P(\text{Blockage } 2 | \text{!flood2 flood3}) = 0.6$
 $P(\text{Blockage } 2 | \text{flood2 !flood3}) = 0.6$
 $P(\text{Blockage } 2 | \text{flood2 flood3}) = 0.84$

$P(\text{Blockage } 2 | []) = 0.3844$

 The probability that the given path is free from blockages is 0.22401684000000005

4.2.3 Brief explanation

As we can see, since the probability of the flooding on the vertices of the path: 0,2,3 is high, the probability that the given path is free of blockages is low.

5 How to run

In order to run the program, you should run the file **main.py**. In order to change the path that is desired to be checked for being block-free: change the input list in the 7-th line in that file:

```
ui.path_free_of_blockages(<input>))
```

or just use the querying user-interface system.