

Grokking the Coding Interview: Patterns for Coding Questions

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Introduction

Pattern: Sliding Window

Pattern: Two Pointers

Pattern: Fast & Slow pointers

Pattern: Merge Intervals

Pattern: Cyclic Sort

Pattern: In-place Reversal of a LinkedList

Pattern: Tree Breadth First Search

Pattern: Tree Depth First Search

Pattern: Two Heaps

Pattern: Subsets

Pattern: Modified Binary Search

Pattern: Bitwise XOR

Pattern: Top 'K' Elements

Pattern: K-way merge

Pattern : 0/1 Knapsack ^ (Dynamic Programming)

- Introduction
- 0/1 Knapsack (medium)
- Equal Subset Sum Partition (medium)
- Subset Sum (medium)
- Minimum Subset Sum Difference (hard) (selected)
- Problem Challenge 1
- Solution Review: Problem Challenge 1
- Problem Challenge 2

Minimum Subset Sum Difference (hard)

We'll cover the following

- Problem Statement
- *
- Example 1:
- Example 2:
- Example 3:
- Basic Solution
- Code
- Time and Space complexity
- Top-down Dynamic Programming with Memoization
- Code
- Bottom-up Dynamic Programming
- Code
- Time and Space complexity

Problem Statement

Given a set of positive numbers, partition the set into two subsets with minimum difference between their subset sums.

Example 1:

```
Input: {1, 2, 3, 9}
Output: 3
Explanation: We can partition the given set into two subsets where minimum absolute difference between the sum of numbers is '3'. Following are the two subsets: {1, 2, 3} & {9}.
```

Example 2:

```
Input: {1, 2, 7, 1, 5}
Output: 0
Explanation: We can partition the given set into two subsets where minimum absolute difference between the sum of number is '0'. Following are the two subsets: {1, 2, 5} & {7, 1}.
```

Example 3:

```
Input: {1, 3, 100, 4}
Output: 92
Explanation: We can partition the given set into two subsets where minimum absolute difference between the sum of numbers is '92'. Here are the two subsets: {1, 3, 4} & {100}.
```

Basic Solution

This problem follows the **0/1 Knapsack pattern** and can be converted into a **Subset Sum** problem.

Let's assume S1 and S2 are the two desired subsets. A basic brute-force solution could be to try adding each element either in S1 or S2 in order to find the combination that gives the minimum sum difference between the two sets.

So our brute-force algorithm will look like:

```
1 for each number 'i'
2 add number 'i' to S1 and recursively process the remaining numbers
3 add number 'i' to S2 and recursively process the remaining numbers
4 return the minimum absolute difference of the above two sets
```

Code

Here is the code for the brute-force solution:

 Java	 Python3	 C++	 JS
------------------------------------------------------------------------------------------	---------------------------------------------------------------------------------------------	-----------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------

```
1 class PartitionSet {
2
3     public int canPartition(int[] num) {
4         return this.canPartitionRecursive(num, 0, 0, 0);
5     }
6
7     private int canPartitionRecursive(int[] num, int currentIndex, int sum1, int sum2) {
8         // base check
9         if (currentIndex == num.length)
10             return Math.abs(sum1 - sum2);
11
12         // recursive call after including the number at the currentIndex in the first set
13         int diff1 = canPartitionRecursive(num, currentIndex+1, sum1+num[currentIndex], sum2);
14
15         // recursive call after including the number at the currentIndex in the second set
16         int diff2 = canPartitionRecursive(num, currentIndex+1, sum1, sum2+num[currentIndex]);
17
18         return Math.min(diff1, diff2);
19     }
}
```

Solution Review: Problem
Challenge 2

Pattern: Topological Sort (Graph)

- Introduction
- Topological Sort (medium)
- Tasks Scheduling (medium)
- Tasks Scheduling Order (medium)
- All Tasks Scheduling Orders (hard)
- Alien Dictionary (hard)
- Problem Challenge 1
- Solution Review: Problem Challenge 1
- Problem Challenge 2
- Solution Review: Problem Challenge 2

Miscellaneous

- Kth Smallest Number (hard)

Conclusions

- Where to Go from Here

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```
18     return Math.min(01111, 01112);
19 }
20
21 public static void main(String[] args) {
22     PartitionSet ps = new PartitionSet();
23     int[] num = {1, 2, 3, 9};
24     System.out.println(ps.canPartition(num));
25     num = new int[]{1, 2, 7, 1, 5};
26     System.out.println(ps.canPartition(num));
27     num = new int[]{1, 3, 100, 4};
28     System.out.println(ps.canPartition(num));
```

RUN

SAVE

RESET

Close

1.356s

Output

```
3
0
92
```

Time and Space complexity

Because of the two recursive calls, the time complexity of the above algorithm is exponential $O(2^n)$, where 'n' represents the total number. The space complexity is $O(n)$ which is used to store the recursion stack.

Top-down Dynamic Programming with Memoization

We can use memoization to overcome the overlapping sub-problems.

We will be using a two-dimensional array to store the results of the solved sub-problems. We can uniquely identify a sub-problem from 'currentIndex' and 'Sum1' as 'Sum2' will always be the sum of the remaining numbers.

Code

Here is the code:

```
Java Python3 C++ JS
```

```
1 class PartitionSet {
2
3     public int canPartition(int[] num) {
4         int sum = 0;
5         for (int i = 0; i < num.length; i++)
6             sum += num[i];
7
8         Integer[][] dp = new Integer[num.length][sum + 1];
9         return this.canPartitionRecursive(dp, num, 0, 0, 0);
10    }
11
12    private int canPartitionRecursive(Integer[][] dp, int[] num, int currentIndex, int sum1, int sum2) {
13        // base check
14        if(currentIndex == num.length)
15            return Math.abs(sum1 - sum2);
16
17        // check if we have not already processed similar problem
18        if(dp[currentIndex][sum1] == null) {
19            // recursive call after including the number at the currentIndex in the first set
20            int diff1 = canPartitionRecursive(dp, num, currentIndex + 1, sum1 + num[currentIndex], sum2);
21
22            // recursive call after including the number at the currentIndex in the second set
23            int diff2 = canPartitionRecursive(dp, num, currentIndex + 1, sum1, sum2 + num[currentIndex]);
24
25            dp[currentIndex][sum1] = Math.min(diff1, diff2);
26        }
27
28        return dp[currentIndex][sum1];
    }
```

RUN

SAVE

RESET

Close

1.677s

Output

```
3
0
92
```

Bottom-up Dynamic Programming

Let's assume 'S' represents the total sum of all the numbers. So, in this problem, we are trying to find a subset whose sum is as close to ' $S/2$ ' as possible, because if we can partition the given set into two subsets of an equal sum, we get the minimum difference, i.e. zero. This transforms our problem to [Subset Sum](#), where we try to find a subset whose sum is equal to a given number— ' $S/2$ ' in our case. If we can't find such a subset, then we will take the subset which has the sum closest to ' $S/2$ '. This is easily possible, as we will be calculating all possible sums with every subset.

Essentially, we need to calculate all the possible sums up to ' $S/2$ ' for all numbers. So how can we populate the array `db[TotalNumbers][S/2+1]` in the bottom-up fashion?

For every possible sum 's' (where $0 \leq s \leq S/2$), we have two options:

1 Exclude the number. In this case, we will see if we can get the sum 's' from the subset excluding this

1. Exclude the number. In this case, we will see if we can get the sum 's' from the subset excluding this number => `dp[index-1][s]`

2. Include the number if its value is not more than 's'. In this case, we will see if we can find a subset to get the remaining sum => `dp[index-1][s-num[index]]`

If either of the two above scenarios is true, we can find a subset with a sum equal to 's'. We should dig into this before we can learn how to find the closest subset.

Let's draw this visually, with the example input $\{1, 2, 3, 9\}$. Since the total sum is '15', we will try to find a subset whose sum is equal to the half of it, i.e. '7'.

num\sum	0	1	2	3	4	5	6	7
1	T							
$\{1, 2\}$	T							
$\{1, 2, 3\}$	T							
$\{1, 2, 3, 9\}$	T							

'0' sum can always be found through an empty set

1 of 11

num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
$\{1, 2\}$	T							
$\{1, 2, 3\}$	T							
$\{1, 2, 3, 9\}$	T							

With only one number, we can form a subset only when the required sum is equal to that number

2 of 11

num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
$\{1, 2\}$	T	T						
$\{1, 2, 3\}$	T							
$\{1, 2, 3, 9\}$	T							

sum: 1, index:1=> `(dp[index-1][sum] , as the 'sum' is less than the number at index '1' (i.e., 1 < 2))`

3 of 11

num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
$\{1, 2\}$	T	T	T					
$\{1, 2, 3\}$	T							
$\{1, 2, 3, 9\}$	T							

sum: 2, index:1=> `(dp[index-1][sum] || dp[index-1][sum-2])`

4 of 11

num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
$\{1, 2\}$	T	T	T	T				
$\{1, 2, 3\}$	T							
$\{1, 2, 3, 9\}$	T							

sum: 3, index:1=> `(dp[index-1][sum] || dp[index-1][sum-2])`

5 of 11

num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
$\{1, 2\}$	T	T	T	T	F	F	F	F
$\{1, 2, 3\}$	T							
$\{1, 2, 3, 9\}$	T							

{1,2,3}	T							
{1,2,3}	T							

sum: 4-7, index:1=> (dp[index-1][sum] || dp[index-1][sum-2])

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num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F	F
{1,2,3}	T	T	T	T				
{1,2,3,9}	T							

sum: 1,2,3, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

7 of 11

num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F	F
{1,2,3}	T	T	T	T	T			
{1,2,3,9}	T							

sum: 4, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

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num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F	F
{1,2,3}	T	T	T	T	T	T	T	
{1,2,3,9}	T							

sum: 5,6, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

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num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F	F
{1,2,3}	T	T	T	T	T	T	T	F
{1,2,3,9}	T							

sum: 7, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

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num\sum	0	1	2	3	4	5	6	7
1	T	T	F	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F	F
{1,2,3}	T	T	T	T	T	T	T	F
{1,2,3,9}	T	T	T	T	T	T	T	F

sum: 1-7, index:1=> (dp[index-1][sum] , as the 'sum' is always less than the number (9))

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The above visualization tells us that it is not possible to find a subset whose sum is equal to '7'. So what is the closest subset we can find? We can find the subset if we start moving backwards in the last row from the bottom right corner to find the first 'T'. The first "T" in the diagram above is the sum '6', which means that we can find a subset whose sum is equal to '6'. This means the other set will have a sum of '9' and the minimum difference will be '3'.

DIFFICULTY: MEDIUM

Code

Here is the code for our bottom-up dynamic programming approach:

```
Java Python3 C++ JS
1 class PartitionSet {
2
3     public int canPartition(int[] num) {
4         int sum = 0;
5         for (int i = 0; i < num.length; i++)
6             sum += num[i];
7
8         int n = num.length;
9         boolean[][] dp = new boolean[n][sum/2 + 1];
10
11        // populate the sum=0 columns, as we can always form '0' sum with an empty set
12        for(int i=0; i < n; i++)
13            dp[i][0] = true;
14
15        // with only one number, we can form a subset only when the required sum is equal to that number
16        for(int s=1; s <= sum/2 ; s++) {
17            dp[0][s] = (num[0] == s ? true : false);
18        }
19
20        // process all subsets for all sums
21        for(int i=1; i < num.length; i++) {
22            for(int s=1; s <= sum/2; s++) {
23                // if we can get the sum 's' without the number at index 'i'
24                if(dp[i-1][s]) {
25                    dp[i][s] = dp[i-1][s];
26                } else if (s >= num[i]) {
27                    // else include the number and see if we can find a subset to get the remaining sum
28                    dp[i][s] = dp[i-1][s-num[i]];
29                }
30            }
31        }
32    }
33
34    return dp[n-1][sum/2];
35}

```

RUN **SAVE** **RESET** **CLOSE**

Output 3
0
92

1.460s

Time and Space complexity

The above solution has the time and space complexity of $O(N * S)$, where 'N' represents total numbers and 'S' is the total sum of all the numbers.

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Subset Sum (medium)

Problem Challenge 1

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