

Cheat Sheet for EE463

Performance Parameters

$$I_{rms} = \sqrt{\frac{1}{T} \int i^2 dt}$$

$$CrestFactor = \frac{V_{peak}}{V_{rms}}$$

$$DistortionFactor = \frac{I_{1rms}}{I_{rms}} = \frac{1}{\sqrt{1+THD^2}}$$

ϕ : phase difference between fundamentals of current and voltage

$$DisplacementPowerFactor = \cos(\phi)$$

$$TruePowerFactor = \frac{P}{S} = DPF \frac{I_{1,RMS}}{I_{RMS}}$$

$$THD = \sqrt{(\frac{I_{rms}}{I_{1rms}})^2 - 1}$$

Single Phase Diode Rectifier

$$V_{av} = \frac{2\sqrt{2}V_s}{\pi} (\text{Full wave}), V_{av} = \frac{\sqrt{2}V_s}{\pi} (\text{Half wave})$$

u: commutation period

$$\cos(u) = 1 - \frac{2\omega L_s I_d}{\sqrt{2}V_s} \quad (\text{Full wave})$$

$$\cos(u) = 1 - \frac{\omega L_s I_d}{\sqrt{2}V_s} \quad (\text{Half wave})$$

$$A_u = \int_0^u V_s \sqrt{2} \sin(\omega t) d\omega t = \omega L_s I_d$$

$$\text{Commutation Loss : } \frac{2\omega L_s I_d}{2\pi} \quad (\text{Full wave})$$

$$\frac{\omega L_s I_d}{2\pi} \quad (\text{Half wave})$$

$$I_{d,avg} = \frac{\int_b^f i(\theta) d\theta}{\pi}$$

$$I_{d,shortcircuit} = \frac{V_s}{\omega L_s}$$

Three Phase Rectifier

- Half Wave

$$V_{av} = \frac{3\sqrt{6}V_s}{2\pi} = \frac{3\sqrt{2}V_{ll}}{2\pi}$$

- Full Wave

Full Bridge Rectifier Average Output V_s : rms value of source voltage

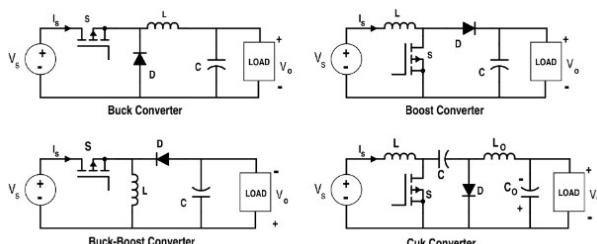
$$V_{av} = \frac{3\sqrt{6}V_s}{\pi} - \frac{3wL_s I_d}{\pi}$$

Comparison of Rectifiers

| Type | Vout | ΔV_{out} | fripple |
|---------------------|--|--|---------|
| Single Phase | $\frac{2\sqrt{2}}{\pi} V_{ph} = 207 \text{ V}$ | $\sqrt{2}V_{ph} = 325 \text{ V}$ | 100 Hz |
| 3-phase Half Bridge | $\frac{3\sqrt{2}}{2\pi} V_{l-l} = 270 \text{ V}$ | $\frac{\sqrt{2}}{2} V_{ph} = 162.5 \text{ V}$ | 150 Hz |
| 3-phase Full Bridge | $\frac{3\sqrt{2}}{\pi} V_{l-l} = 540 \text{ V}$ | $(1 - \frac{\sqrt{3}}{2})\sqrt{2}V_{l-l} = 75.8 \text{ V}$ | 300 Hz |

Converters

Converters



Buck Converter (Step-Down)

$$\text{Gain: } V_o = DV_d$$

$$V_L = V_d - V_o \text{ (On)}, \quad V_L = -V_o \text{ (Off)}$$

$$\text{Inductor Ripple: } \Delta I_L = \frac{V_o(1-D)}{L f_s}$$

$$\text{Voltage Ripple: } \frac{\Delta V_o}{V_o} = \frac{1-D}{8LCf_s^2}$$

$$\text{CCM/DCM Boundary: } I_{LB} = \frac{\Delta I_L}{2} = \frac{DT_s(V_d)(1-D)}{2L}$$

$$\text{CCM/DCM Boundary: } L_{min} = \frac{DT_s(V_d - V_o)}{2I_{LB}} = \frac{RT_s(1-D)}{2}$$

Boost Converter (Step-Up)

$$\text{Gain: } V_o = \frac{V_d}{1-D}$$

$$V_L = V_d \text{ (On)}, \quad V_L = V_d - V_o \text{ (Off)}$$

$$\text{Inductor Ripple: } \Delta I_L = \frac{V_d D}{L f_s}$$

$$\text{Voltage Ripple: } \frac{\Delta V_o}{V_o} = \frac{D}{RCf_s}$$

$$\text{CCM/DCM Boundary: } I_{LB} = \frac{\Delta I_L}{2} = \frac{V_d DT_s}{2L}$$

$$\text{Min Inductance: } L_{min} = \frac{D(1-D)^2 R}{2f_s}$$

Buck-Boost Converter

$$\text{Gain: } V_o = -V_d \frac{D}{1-D}$$

$$V_L = V_d \text{ (On)}, \quad V_L = V_o \text{ (Off)}$$

$$\text{Inductor Ripple: } \Delta I_L = \frac{V_d D}{L f_s}$$

$$\text{Voltage Ripple: } \frac{\Delta V_o}{V_o} = \frac{D}{RCf_s}$$

$$\text{CCM/DCM Boundary: } I_{LB} = \frac{\Delta I_L}{2} = \frac{V_d DT_s}{2L}$$

$$\text{Min Inductance: } L_{min} = \frac{(1-D)^2 R}{2f_s}$$

Cuk Converter

$$\text{Gain: } V_o = -V_d \frac{D}{1-D}$$

$$V_{L1} = V_d \text{ (On)}, \quad V_{L1} = V_d - V_{C1} \text{ (Off)}$$

$$\text{Inductor Ripple (L}_1\text{): } \Delta I_{L1} = \frac{V_d D}{L_1 f_s}$$

$$\text{Inductor Ripple (L}_2\text{): } \Delta I_{L2} = \frac{V_d D}{L_2 f_s}$$

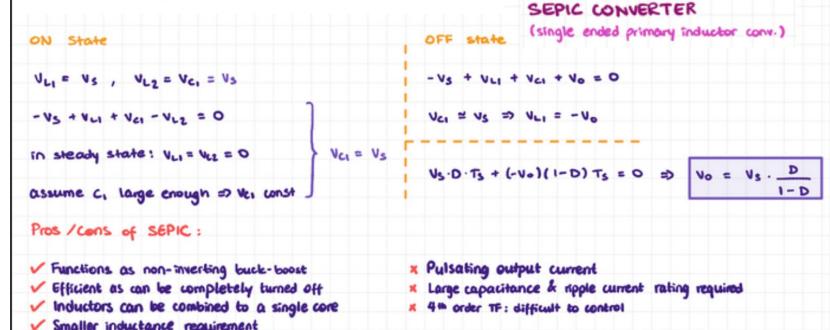
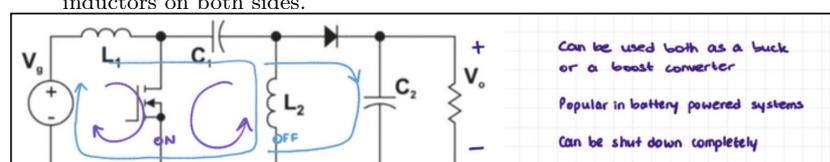
$$\text{Voltage Ripple (C}_o\text{): } \frac{\Delta V_o}{V_o} = \frac{1-D}{8L_2 C_2 f_s^2}$$

$$\text{CCM/DCM Boundary: } I_{LB1} = \frac{V_d DT_s}{2L_1} \quad (\text{for L}_1)$$

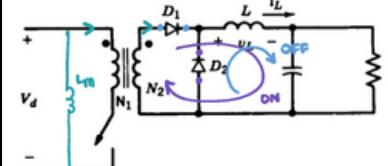
$$\text{Min Inductance (L}_1\text{): } L_{1,min} = \frac{(1-D)^2 R}{2Df_s}$$

$$\text{Min Inductance (L}_2\text{): } L_{2,min} = \frac{(1-D)R}{2f_s}$$

Cuk Feature: Input and Output currents are continuous (low ripple) due to inductors on both sides.



FORWARD CONVERTER

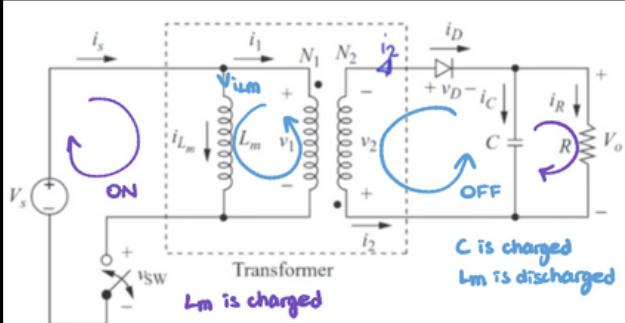
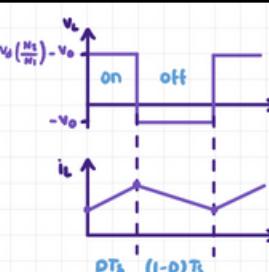


ON State

$$V_L = V_d \cdot \left(\frac{N_2}{N_1} \right) - V_o$$

OFF State

$$V_L = -V_o$$

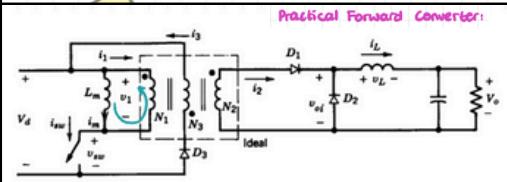


$$\left(V_d \left(\frac{N_2}{N_1} \right) - V_o \right) D = V_o (1-D)$$

$$V_d \cdot \frac{N_2}{N_1} \cdot D - V_o \cdot D = V_o - V_o \cdot D$$

$$V_o = V_d \frac{N_2}{N_1} D$$

Like a buck converter with added turns ratio



The energy stored in L_m , if discharged through the switch, could destroy the MOSFET. To prevent this, a snubber circuit could be added but would cause important losses. A practical solution is to add an extra winding:

With this implementation, the energy stored in L_m is discharged to the source.

$$i_1 = -i_{Lm}$$

$$N_1 i_1 = N_2 i_2 - N_3 i_3$$

$$N_1 i_1 = -N_3 i_3$$

Transformer Reset: $t_m < (1-D)T_s$

$$\text{Max Duty Cycle: } D_{max} = \frac{1}{1 + (N_3/N_1)}$$

$$V_{Lm} = V_1 = -V_S \frac{N_1}{N_3} = L_m \frac{di_{Lm}}{dt}$$

$$\frac{di_{Lm}}{dt} = -\frac{V_S}{L_m} \cdot \frac{N_1}{N_3}$$

$$\Delta B = \frac{L \cdot \Delta I}{N \cdot A e}$$

ON state

$$V_1 = V_S$$

$$V_2 = V_1 \frac{N_2}{N_1} = V_S \frac{N_2}{N_1}$$

$$V_3 = V_1 \frac{N_3}{N_1} = V_S \frac{N_3}{N_1}$$

$$V_{D3} = -V_2 - V_3 < 0 \Rightarrow D_3 \text{ is off}$$

$$V_{Lm} = V_S \quad \Delta i_{Lm} = \frac{V_S D T_s}{L_m}$$

$$i_{SW} = i_1 + i_{Lm}$$

OFF state

$$i_{Lm} = -i_1$$

$$V_S = -V_3$$

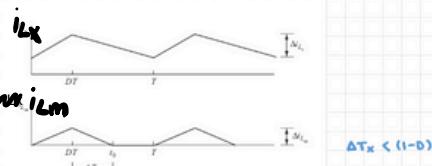
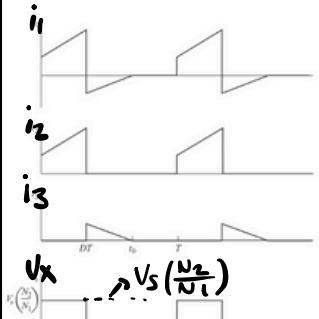
$$V_1 = V_S \frac{N_1}{N_3} = -V_S \frac{N_1}{N_3}$$

$$V_2 = V_S \frac{N_2}{N_1} = -V_S \frac{N_2}{N_1}$$

$$N_1 i_1 = N_2 i_2 - N_3 i_3$$

$$N_1 i_1 = -N_3 i_3$$

$$i_3 = -N_1 i_1$$



$$i_{Lm(max)} = \frac{V_S D T_s}{L_m} = \frac{V_S \cdot D \cdot T_s}{L_m}$$

$$\Delta T_X = \frac{V_S D T_s}{L_m} = D \cdot T_s \cdot \frac{N_2}{N_1} \frac{N_3}{N_1}$$

$$\Delta T_X = D T_s \frac{N_2}{N_1} < (1-D) T_s$$

$$D \left(1 + \frac{N_2}{N_1} \right) < 1$$

$$\text{usually, } N_1 = N_3$$

$$\Rightarrow D < 0.5$$

Advantages/Disadvantages over Flyback

- ✓ Better use of transformer (direct & higher power transfer)
- ✓ Gapless core can be used (higher $L_m \rightarrow$ less ripple)
- ✓ Output inductor + diode ensure continuous output current

FULL BRIDGE ISOLATING CONVERTER

Operation very similar to push-pull conv.

Switches 1 & 2 are operated together just as Sw_1 of push-pull.

Switches 3 & 4 are operated together just as Sw_2 of push-pull.

V_P ----- $-V_S$

V_X ----- $V_S \left(\frac{N_2}{N_1} \right)$

Practical Forward Converter:

- ✗ Possibly increased cost
- ✗ Gain changes a lot in DCM & may require closed-loop control
- ✗ Higher voltage requirement for MOSFET

Advantages / Disadvantages:

- ✓ Better usage of the core compared to Forward conv.
- ✓ Better B-H curve: uses both +/- regions
- ✗ Need to control 2 switches

Control of 4 Quadrant Converters

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER

Very similar to full-wave converter. Less switches are used: output voltage halved.

HALF BRIDGE ISOLATING CONVERTER