



OWL 2

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OWL 2

Main References

W3C OWL Working Group (2009) OWL2 Web Ontology Language Document Overview.

<http://www.w3.org/TR/2009/REC-owl2-overview-20091027/>

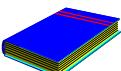
Dean M, Schreiber G (2004) OWL Web Ontology Language Reference. W3C Recommendation.

<http://www.w3.org/TR/owl-ref/>



Gómez-Pérez, A.; Fernández-López, M.; Corcho, O. **Ontological Engineering**. Springer Verlag. 2003

Capítulo 4: Ontology languages



Baader F, McGuinness D, Nardi D, Patel-Schneider P (2003)

The Description Logic Handbook: Theory, implementation and applications.

Cambridge University Press, Cambridge, United Kingdom



Jena web site:

<http://jena.sourceforge.net/>

Jena API:

http://jena.sourceforge.net/tutorial/RDF_API/

Jena tutorials:

<http://www.ibm.com/developerworks/xml/library/j-jena/index.html>

<http://www.xml.com/pub/a/2001/05/23/jena.html>



Pellet:

<http://clarkparsia.com/pellet>

RACER:

<http://www.racer-systems.com/>

FaCT++:

<http://owl.man.ac.uk/factplusplus/>

HermiT:

<http://hermit-reasoner.com/>

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What doesn't RDFS give us?

- **RDFS is too weak to describe resources in sufficient detail**
 - No localised range and domain constraints
 - Can't say that the range of hasEducationalMaterial is Slides when applied to TheoreticalSession and Code when applied to HandsonSession
 - TheoreticalSession hasEducationalMaterial Slides
 - HandsonSession hasEducationalMaterial Code
 - No existence/cardinality constraints
 - Can't say:
 - Sessions must have some EducationalMaterial
 - Sessions have at least one Presenter
 - No boolean operators
 - Can't say:
 - Or / not
 - No transitive, inverse or symmetrical properties
 - Can't say that presents is the inverse property of isPresentedBy

Description Logics

- **A family of logic based Knowledge Representation formalisms**
 - Descendants of semantic networks and KL-ONE
 - Describe domain in terms of concepts (classes), roles (relationships) and individuals
 - Specific languages characterised by the constructors and axioms used to assert knowledge about classes, roles and individuals.
 - Example: ALC (the least expressive language in DL that is propositionally closed)
 - Constructors: boolean (and, or, not)
 - Role restrictions
- **Distinguished by:**
 - Model theoretic semantics
 - Decidable fragments of FOL
 - Closely related to Propositional Modal & Dynamic Logics
 - Provision of inference services
 - Sound and complete decision procedures for key problems
 - Implemented systems (highly optimised)

Structure of DL Ontologies

- A DL ontology can be divided into two parts:
 - **Tbox** (Terminological KB): a set of axioms that describe the structure of a domain :
 - $\text{Doctor} \sqsubseteq \text{Person}$
 - $\text{Person} \sqsubseteq \text{Man} \cup \text{Woman}$
 - $\text{HappyFather} \sqsubseteq \text{Man} \cap \forall \text{hasDescendant}.(\text{Doctor} \cup \forall \text{hasDescendant}.\text{Doctor})$
 - **Abox** (Assertional KB): a set of axioms that describe a specific situation :
 - $\text{John} \in \text{HappyFather}$
 - $\text{hasDescendant}(\text{John}, \text{Mary})$

Most common constructors in class definitions

- **Intersection:** $C_1 \cap \dots \cap C_n$ **Human** \cap **Male**
- **Union:** $C_1 \cup \dots \cup C_n$ **Doctor** \cup **Lawyer**
- **Negation:** $\neg C$ \neg **Male**
- **Nominals:** $\{x_1\} \cup \dots \cup \{x_n\}$ $\{\text{john}\} \cup \dots \cup \{\text{mary}\}$
- **Universal restriction:** $\forall P.C$ $\forall \text{hasChild}.\text{Doctor}$
- **Existential restriction:** $\exists P.C$ $\exists \text{hasChild}.\text{Lawyer}$
- **Maximum cardinality:** $\leq n P.C$ $\leq 3 \text{hasChild}.\text{Doctor}$
- **Minimum cardinality:** $\geq n P.C$ $\geq 1 \text{hasChild}.\text{Male}$
- **Specific Value:** $\exists P.\{x\}$ $\exists \text{hasColleague}.\{\text{Matthew}\}$
- **Nesting of constructors can be arbitrarily complex**
 - Person $\cap \forall \text{hasChild}.(\text{Doctor} \cup \exists \text{hasChild}.\text{Doctor})$
- **Lots of redundancy**
 - $A \cup B$ is equivalent to $\neg(\neg A \cap \neg B)$
 - $\exists P.C$ is equivalent to $\neg \forall P. \neg C$

Description Logics



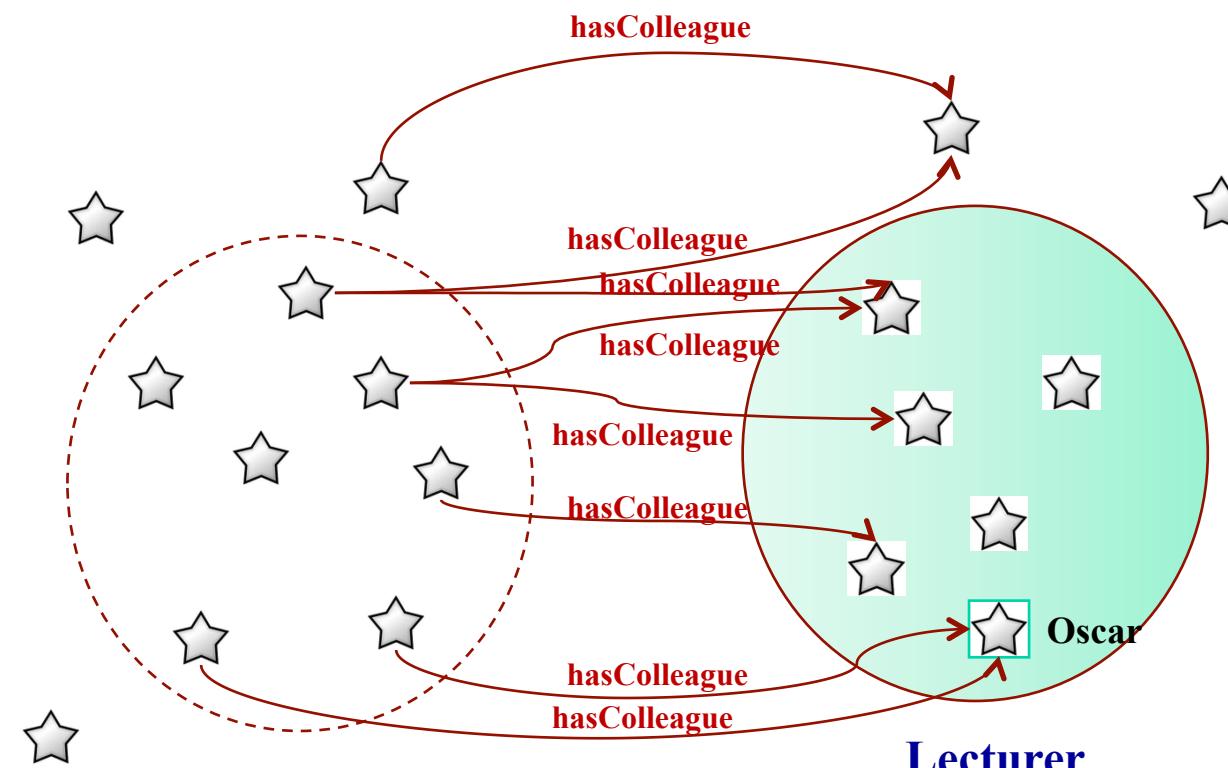
Understand the meaning of universal and existential restrictions

- Decide which is the set that we are defining with different expressions, taking into account Open and Close World Assumptions

Do we understand these constructors?

- $\exists \text{hasColleague}.\text{Lecturer}$
- $\forall \text{hasColleague}.\text{Lecturer}$
- $\exists \text{hasColleague}.\{\text{Oscar}\}$
- $\leq 2 \text{ hasColleague}$

NOT $\exists \text{hasColleague}.\text{Lecturer}$



Most common axioms in definitions

- **Classes**

– Subclass	$C_1 \sqsubseteq C_2$	$\text{Human} \sqsubseteq \text{Animal} \cap \text{Biped}$
– Equivalence	$C_1 \equiv C_2$	$\text{Man} \equiv \text{Human} \cap \text{Male}$
– Disjointness	$C_1 \cap C_2 \sqsubseteq \perp$	$\text{Male} \cap \text{Female} \sqsubseteq \perp$

- **Properties/roles**

– Subproperty	$P_1 \sqsubseteq P_2$	$\text{hasDaughter} \sqsubseteq \text{hasChild}$
– Equivalence	$P_1 \equiv P_2$	$\text{cost} \equiv \text{price}$
– Inverse	$P_1 \equiv P_2^{-}$	$\text{hasChild} \equiv \text{hasParent}^{-}$
– Transitive	$P^+ \sqsubseteq P$	$\text{ancestor}^{+} \sqsubseteq \text{ancestor}$
– Functional	$T \sqsubseteq \leq 1 P$	$T \sqsubseteq \leq 1 \text{hasMother}$
– InverseFunctional	$T \sqsubseteq \leq 1 P^{-}$	$T \sqsubseteq \leq 1 \text{hasPassportID}^{-}$
– And also... Reflexive, Irreflexive, Symmetric, Asymmetric		

- **Individuals**

– Equivalence	$\{x_1\} \equiv \{x_2\}$	$\{\text{oeg:OscarCorcho}\} \equiv \{\text{img:Oscar}\}$
– Different	$\{x_1\} \equiv \neg \{x_2\}$	$\{\text{john}\} \equiv \neg \{\text{peter}\}$
– Negative object property and datatype property assertions	$\neg \{P \text{ a1 a2}\}$	$\neg \{\text{hasChild john peter}\}$

- **Most axioms are reducible to inclusion (\sqsubseteq)**

- $C \equiv D$ iff both $C \sqsubseteq D$ and $D \sqsubseteq C$; C disjoint D iff $C \sqsubseteq \neg D$

DL constructors and DL languages

Construct	Syntax	Language			
Concept	A	FL ₀	FL ⁺	AL	S ¹⁴
Role name	R				
Intersection	C ∩ D				
Value restriction	∀R.C				
Limited existential quantification	∃ R				
Top or Universal	T				
Bottom	⊥				
Atomic negation	¬A				
Negation ¹⁵	¬ C				
Union	C ∪ D				
Existential restriction	∃ R.C				
Number restrictions	(≥ n R) (≤ n R)				
Nominals	{a ₁ ... a _n }				
Role hierarchy	R ⊑ S				
Inverse role	R [*]				
Qualified number restriction	(≥ n R.C) (≤ n R.C)				

OWL1 is SHOIN(D+)
OWL2 is SROIQ(D+)

→ {Colombia, Argentina, México, ...} → MercoSur countries

→ ≤2 hasChild.Female, ≥1 hasParent.Male

Other:

Concrete datatypes: hasAge.(<21)

Transitive roles: hasChild* (descendant)

Role composition: hasParent o hasBrother (uncle)

¹² Names previously used for Description Logics were: terminological knowledge representation languages, concept languages, term subsumption languages, and KL-ONE-based knowledge representation languages.

¹³ In this table, we use A to refer to atomic concepts (concepts that are the basis for building other concepts), C and D to any concept definition, R to atomic roles and S to role definitions. FL is used for structural DL languages and AL for attributive languages (Baader et al., 2003).

¹⁴ S is the name used for the language ALC_{R+}, which is composed of ALC plus transitive roles.

¹⁵ ALC and ALCUE are equivalent languages, since union (U) and existential restriction (E) can be represented using negation (C).

Some basic DL modelling guidelines

- **X must be Y, X is an Y that...** $\rightarrow X \subseteq Y$
- **X is exactly Y, X is the Y that...** $\rightarrow X = Y$
- **X is not Y (*not the same as X is whatever it is not Y*)** $\rightarrow X \subseteq \neg Y$
- **X and Y are disjoint** $\rightarrow X \cap Y \subseteq \perp$
- **X is Y or Z** $\rightarrow X \sqsubseteq Y \cup Z$
- **X is Y for which property P has only instances of Z as values** $\rightarrow X \subseteq Y \cap (\forall P.Z)$
- **X is Y for which property P has at least an instance of Z as a value** $\rightarrow X \subseteq Y \cap (\exists P.Z)$
- **X is Y for which property P has at most 2 values** $\rightarrow X \subseteq Y \cap (\leq 2.P)$
- **Individual X is a Y** $\rightarrow X \in Y$

Description Logics Formalisation



Develop a sample ontology in the domain of people, pets, vehicles, and newspapers

- Understand how to formalise knowledge in description logics



Chunk 1. Formalize in DL

1. Concept definitions:

Grass and trees must be plants. Leaves are parts of a tree but there are other parts of a tree that are not leaves. A dog must eat bones, at least. A sheep is an animal that must only eat grass. A giraffe is an animal that must only eat leaves. A mad cow is a cow that eats brains that can be part of a sheep.

2. Restrictions:

Animals or part of animals are disjoint with plants or parts of plants.

3. Properties:

Eats is applied to animals. Its inverse is eaten_by.

4. Individuals:

Tom.

Flossie is a cow.

Rex is a dog and is a pet of Mick.

Fido is a dog.

Tibbs is a cat.



Chunk 2. Formalize in DL

1. Concept definitions:

Bicycles, buses, cars, lorries, trucks and vans are vehicles. There are several types of companies: bus companies and haulage companies.

An elderly person must be adult. A kid is (exactly) a person who is young. A man is a person who is male and is adult. A woman is a person who is female and is adult. A grown up is a person who is an adult. And old lady is a person who is elderly and female. Old ladies must have some animal as pets and all their pets are cats.

2. Restrictions:

Youngs are not adults, and adults are not youngs.

3. Properties:

Has mother and has father are subproperties of has parent.

4. Individuals:

Kevin is a person.

Fred is a person who has a pet called Tibbs.

Joe is a person who has at most one pet. He has a pet called Fido.

Minnie is a female, elderly, who has a pet called Tom.



Chunk 3. Formalize in DL

1. Concept definitions:

A magazine is a publication. Broadsheets and tabloids are newspapers. A quality broadsheet is a type of broadsheet. A red top is a type of tabloid. A newspaper is a publication that must be either a broadsheet or a tabloid.

White van mans must read only tabloids.

2. Restrictions:

Tabloids are not broadsheets, and broadsheets are not tabloids.

3. Properties:

The only things that can be read are publications.

4. Individuals:

Daily Mirror

The Guardian and The Times are broadsheets

The Sun is a tabloid



Chunk 4. Formalize in DL

1. Concept definitions:

A pet is a pet of something. An animal must eat something. A vegetarian is an animal that does not eat animals nor parts of animals. Ducks, cats and tigers are animals. An animal lover is a person who has at least three pets. A pet owner is a person who has animal pets. A cat liker is a person who likes cats. A cat owner is a person who has cat pets. A dog liker is a person who likes dogs. A dog owner is a person who has dog pets.

2. Restrictions:

Dogs are not cats, and cats are not dogs.

3. Properties:

Has pet is defined between persons and animals. Its inverse is is_pet_of.

4. Individuals:

Dewey, Huey, and Louie are ducks.

Fluffy is a tiger.

Walt is a person who has pets called Huey, Louie and Dewey.



Chunk 5. Formalize in DL

1. Concept definitions

A driver must be adult. A driver is a person who drives vehicles. A lorry driver is a person who drives lorries. A haulage worker is who works for a haulage company or for part of a haulage company. A haulage truck driver is a person who drives trucks and works for part of a haulage company. A van driver is a person who drives vans. A bus driver is a person who drives buses. A white van man is a man who drives white things and vans.

2. Restrictions:

--

3. Properties:

The service number is an integer property with no restricted domain

4. Individuals:

Q123ABC is a van and a white thing.

The42 is a bus whose service number is 42.

Mick is a male who read Daily Mirror and drives Q123ABC.



Chunk 1. Formalisation in DL

$grass \subseteq plant$

$tree \subseteq plant$

$leaf \subseteq \exists partOf.tree$

$dog \subseteq \exists eats.bone$

$sheep \subseteq animal \cap \forall eats.grass$

$giraffe \subseteq animal \cap \forall eats.leaf$

$madCow \equiv cow \cap \exists eats.(brain \cap \exists partOf.sheep)$

$(animal \cup \exists partOf.animal) \cap (plant \cup \exists partOf.plant) \subseteq \perp$



Chunk 2. Formalisation in DL

$bicycle \subseteq vehicle; bus \subseteq vehicle; car \subseteq vehicle; lorry \subseteq vehicle; truck \subseteq vehicle$

$busCompany \subseteq company; haulageCompany \subseteq company$

$elderly \subseteq person \cap adult$

$kid = person \cap young$

$man = person \cap male \cap adult$

$woman = person \cap female \cap adult$

$grownUp = person \cap adult$

$oldLady = person \cap female \cap elderly$

$oldLady \subseteq \exists hasPet.animal \cap \forall hasPet.cat$

$young \cap adult \subseteq \perp$

$hasMother \subseteq hasParent$

$hasFather \subseteq hasParent$



Chunk 3. Formalisation in DL

magazine \subseteq *publication*

broadsheet \subseteq *newspaper*

tabloid \subseteq *newspaper*

qualityBroadsheet \subseteq *broadsheet*

redTop \subseteq *tabloid*

newspaper \subseteq *publication* \cap (*broadsheet* \cup *tabloid*)

whiteVanMan \subseteq $\forall \text{reads}.\text{tabloid}$

tabloid \cap *broadsheet* $\subseteq \perp$



Chunk 4. Formalisation in DL

$pet \equiv \exists isPetOf.T$

$animal \subseteq \exists eats.T$

$vegetarian \equiv animal \cap \forall eats.\neg animal \cap \forall eats.\neg(\exists partOf.animal)$

$duck \subseteq animal; cat \subseteq animal; tiger \subseteq animal$

$animalLover \equiv person \cap (\geq 3 hasPet)$

$petOwner \equiv person \cap \exists hasPet.animal$

$catLike \equiv person \cap \exists likes.cat; catOwner \equiv person \cap \exists hasPet.cat$

$dogLike \equiv person \cap \exists likes.dog; dogOwner \equiv person \cap \exists hasPet.dog$

$dog \cap cat \subseteq \perp$



Chunk 5. Formalisation in DL

$driver \subseteq adult$

$driver \equiv person \cap \exists drives.vehicle$

$lorryDriver \equiv person \cap \exists drives.lorry$

$haulageWorker \equiv \exists worksFor.(haulageCompany \cup \exists partOf.haulageCompany)$

$haulageTruckDriver \equiv person \cap \exists drives.truck \cap \exists worksFor.(\exists partOf.haulageCompany)$

$vanDriver \equiv person \cap \exists drives.van$

$busDriver \equiv person \cap \exists drives.bus$

$whiteVanMan \equiv man \cap \exists drives.(whiteThing \cap van)$

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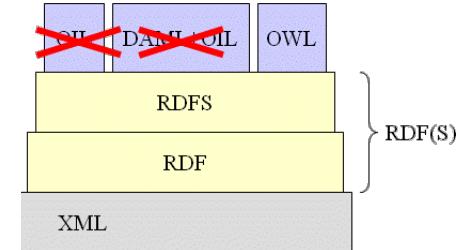
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OWL (1.0 and 1.1)

February 2004

Web Ontology Language

Built on top of RDF(S)



Three layers:

- OWL Lite
 - A small subset of primitives
 - Easier for frame-based tools to transition to
- OWL DL
 - Description logic
 - Decidable reasoning
- OWL Full
 - RDF extension, allows metaclasses

Several syntaxes:

- Abstract syntax
- Manchester syntax
- RDF/XML

OWL 2 (I). New features

- October 2009
- New features
 - Syntactic sugar
 - Disjoint union of classes
 - New expressivity
 - Keys
 - Property chains
 - Richer datatypes, data ranges
 - Qualified cardinality restrictions
 - Asymmetric, reflexive, and disjoint properties
 - Enhanced annotation capabilities
- New syntax
 - OWL2 Manchester syntax

OWL 2 (II). Three new profiles

- **OWL2 EL**
 - Ontologies that define very large numbers of classes and/or properties,
 - Ontology consistency, class expression subsumption, and instance checking can be decided in polynomial time.
- **OWL2 QL**
 - Sound and complete query answering is in LOGSPACE (more precisely, in AC^0) with respect to the size of the data (assertions),
 - Provides many of the main features necessary to express conceptual models (UML class diagrams and ER diagrams).
 - It contains the intersection of RDFS and OWL 2 DL.
- **OWL2 RL**
 - Inspired by Description Logic Programs and pD*.
 - Syntactic subset of OWL 2 which is amenable to implementation using rule-based technologies, and presenting a partial axiomatization of the OWL 2 RDF-Based Semantics in the form of first-order implications that can be used as the basis for such an implementation.
 - Scalable reasoning without sacrificing too much expressive power.
 - Designed for
 - OWL applications trading the full expressivity of the language for efficiency,
 - RDF(S) applications that need some added expressivity from OWL 2.

OWL: Most common constructors

Intersection:	$C_1 \cap \dots \cap C_n$	intersectionOf	$\text{Human} \cap \text{Male}$
Union:	$C_1 \cup \dots \cup C_n$	unionOf	$\text{Doctor} \cup \text{Lawyer}$
Negation:	$\neg C$	complementOf	$\neg \text{Male}$
Nominals:	$\{x_1\} \cup \dots \cup \{x_n\}$	oneOf	$\{\text{john}\} \cup \dots \cup \{\text{mary}\}$
Universal restriction:	$\forall P.C$	allValuesFrom	$\forall \text{hasChild}.\text{Doctor}$
Existential restriction:	$\exists P.C$	someValuesFrom	$\exists \text{hasChild}.\text{Lawyer}$
Maximum cardinality:	$\leq n P.[C]$	maxCardinality (qualified or not)	$\leq 3 \text{hasChild}[\text{.Doctor}]$
Minimum cardinality:	$\geq n P.[C]$	minCardinality (qualified or not)	$\geq 1 \text{hasChild}[\text{.Male}]$
Exact cardinality:	$= n P.[C]$	exactCardinality (qualified or not)	$= 1 \text{hasMother}[\text{.Female}]$
Specific Value:	$\exists P.\{x\}$	hasValue	$\exists \text{hasColleague}.\{\text{Matthew}\}$
Local reflexivity:	--	hasSelf	$\text{Narcisist} \equiv \text{Person} \cap \text{hasSelf}(\text{loves})$
Keys	--	hasKey	$\text{hasKey}(\text{Person}, \text{passportNumber}, \text{country})$
Subclass	$C_1 \subseteq C_2$	subClassOf	$\text{Human} \subseteq \text{Animal} \cap \text{Biped}$
Equivalence	$C_1 \equiv C_2$	equivalentClass	$\text{Man} \equiv \text{Human} \cap \text{Male}$
Disjointness	$C_1 \cap C_2 \subseteq \perp$	disjointWith, AllDisjointClasses	$\text{Male} \cap \text{Female} \subseteq \perp$
DisjointUnion	$C \equiv C_1 \cup \dots \cup C_n \text{ and}$ $C_i \cap C_j \subseteq \perp \text{ for all } i \neq j$	disjointUnionOf	$\text{Person} \text{ DisjointUnionOf } (\text{Man}, \text{Woman})$

Metaclasses and annotations on axioms are also valid in OWL2, and declarations of classes have to be provided.

Full list available in reference specs and in the Quick Reference Guide: <http://www.w3.org/2007/OWL/refcard>

OWL: Most common constructors

Subproperty	$P_1 \sqsubseteq P_2$	subPropertyOf	$\text{hasDaughter} \sqsubseteq \text{hasChild}$
Equivalence	$P_1 = P_2$	equivalentProperty	$\text{cost} = \text{price}$
DisjointProperties	$P_1 \cap \dots \cap P_n \sqsubseteq \perp$	disjointObjectProperties	$\text{hasDaughter} \cap \text{hasSon} \sqsubseteq \perp$
Inverse	$P_1 = P_2^{-}$	inverseOf	$\text{hasChild} = \text{hasParent-}$
Transitive	$P^+ \subseteq P$	TransitiveProperty	$\text{ancestor}^+ \subseteq \text{ancestor}$
Functional	$T \sqsubseteq \text{1}P$	FunctionalProperty	$T \sqsubseteq \text{1} \text{hasMother}$
InverseFunctional	$T \sqsubseteq \text{1}P^{-}$	InverseFunctionalProperty	$T \sqsubseteq \text{1} \text{hasPassportID-}$
Reflexive		ReflexiveProperty	
Irreflexive		IrreflexiveProperty	
Asymmetric		AsymmetricProperty	
Property chains	$P = P_1 \circ \dots \circ P_n$	propertyChainAxiom	$\text{hasUncle} \sqsubseteq \text{hasFather} \circ \text{hasBrother}$
Equivalence	$\{x_1\} = \{x_2\}$	sameIndividualAs	$\{\text{oeg:OscarCorcho}\} = \{\text{img:Oscar}\}$
Different	$\{x_1\} = \neg \{x_2\}$	differentFrom, AllDifferent	$\{\text{john}\} = \neg \{\text{peter}\}$
NegativePropertyAssertion		NegativeDataPropertyAssertion	$\neg \{\text{hasAge john 35}\}$
		NegativeObjectPropertyAssertion	$\neg \{\text{hasChild john peter}\}$

Besides, top and bottom object and datatype properties exist

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Basic Inference Tasks

- **Subsumption – check knowledge is correct (captures intuitions)**
 - Does C **subsume** D w.r.t. ontology O? (in *every* model I of O, $C^I \subseteq D^I$)
- **Equivalence – check knowledge is minimally redundant (no unintended synonyms)**
 - Is C **equivalent** to D w.r.t. O? (in *every* model I of O, $C^I = D^I$)
- **Consistency – check knowledge is meaningful (classes can have instances)**
 - Is C **satisfiable** w.r.t. O? (there exists *some* model I of O s.t. $C^I \neq \emptyset$)
- **Instantiation and querying**
 - Is x an **instance** of C w.r.t. O? (in *every* model I of O, $x^I \in C^I$)
 - Is (x,y) an **instance** of R w.r.t. O? (in *every* model I of O, $(x^I, y^I) \in R^I$)
- **All reducible to KB satisfiability or concept satisfiability w.r.t. a KB**
- **Can be decided using highly optimised tableaux reasoners**

Description Logics Reasoning



Develop a sample ontology in the domain of people, pets, vehicles, and newspapers

- Understand the basic reasoning mechanisms of description logics

Subsumption

Automatic classification: an ontology built collaboratively

Instance classification

Detecting redundancy

Consistency checking: unsatisfiable restrictions in a Tbox (are the classes coherent?)



Interesting results (I). Automatic classification

And old lady is a person who is elderly and female.

Old ladies must have some animal as pets and all their pets are cats.

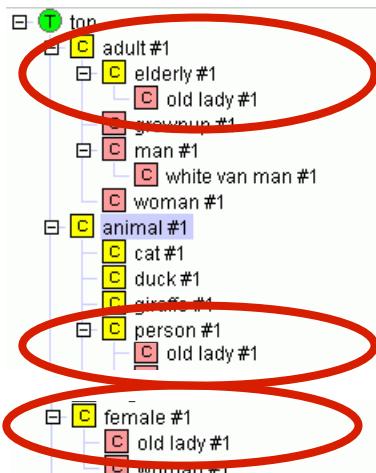
$$\text{elderly} \subseteq \text{person} \cap \text{adult}$$

$$\text{woman} = \text{person} \cap \text{female} \cap \text{adult}$$

$$\text{catOwner} = \text{person} \cap \exists \text{hasPet.cat}$$

$$\text{oldLady} = \text{person} \cap \text{female} \cap \text{elderly}$$

$$\text{oldLady} \subseteq \exists \text{hasPet.animal} \cap \forall \text{hasPet.cat}$$



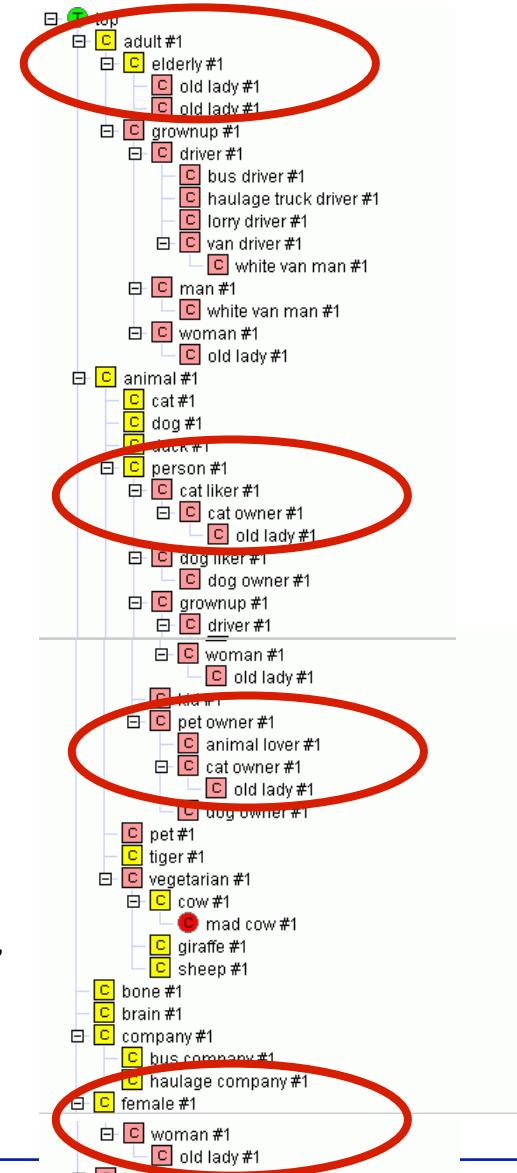
We obtain:

Old ladies must be women.

Every old lady must have a pet cat

Hence, every old lady must be a cat owner

$$\text{oldLady} \subseteq \text{woman} \cap \text{elderly} \cap \text{catOwner}$$





Interesting results (II). Instance classification

A pet owner is a person who has animal pets

Old ladies must have some animal as pets and all their pets are cats.

Has pet has domain person and range animal

Minnie is a female, elderly, who has a pet called Tom.

$\text{petOwner} \equiv \text{person} \cap \exists \text{hasPet}. \text{animal}$

$\text{oldLady} \subseteq \exists \text{hasPet}. \text{animal} \cap \forall \text{hasPet}. \text{cat}$

$\text{hasPet} \subseteq (\text{person}, \text{animal})$

$\text{Minnie} \in \text{female} \cap \text{elderly}$

$\text{hasPet}(\text{Minnie}, \text{Tom})$

We obtain:

Minnie is a person

Hence, Minnie is an old lady

Hence, Tom is a cat

$\text{Minnie} \in \text{person}; \text{Tom} \in \text{animal}$

$\text{Minnie} \in \text{petOwner}$

$\text{Minnie} \in \text{oldLady}$

$\text{Tom} \in \text{cat}$



Interesting results (III). Instance classification and redundancy detection

An animal lover is a person who has at least three pets

Walt is a person who has pets called Huey, Louie and Dewey.

$animalLover \equiv person \cap (\geq 3 hasPet)$

$Walt \in person$

$hasPet(Walt, Huey)$

$hasPet(Walt, Louie)$

$hasPet(Walt, Dewey)$

We obtain:

Walt is an animal lover

Walt is a person is redundant

$Walt \in animalLover$



Interesting results (IV). Instance classification

A van is a type of vehicle

A driver must be adult

A driver is a person who drives vehicles

A white van man is a man who drives vans and white things

White van mans must read only tabloids

Q123ABC is a white thing and a van

Mick is a male who reads Daily Mirror and drives Q123ABC

$van \subseteq vehicle$

$driver \subseteq adult$

$driver \equiv person \cap \exists drives.vehicle$

$whiteVanMan \equiv man \cap \exists drives.(van \cap whiteThing)$

$whiteVanMan \subseteq \forall reads.tabloid$

$Q123ABC \in whiteThing \cap van$

$Mick \in male$

$reads(Mick, DailyMirror)$

$drives(Mick, Q123ABC)$

We obtain:

Mick is an adult

Mick is a white van man

Daily Mirror is a tabloid

$Mick \in adult$

$Mick \in whiteVanMan$

$DailyMirror \in tabloid$



Interesting results (V). Consistency checking

Cows are vegetarian.

A vegetarian is an animal that does not eat animals nor parts of animals.

A mad cow is a cow that eats brains that can be part of a sheep

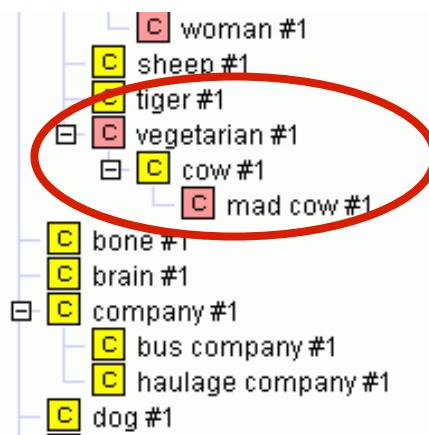
$cow \subseteq vegetarian$

$vegetarian \equiv animal \cap \forall eats.\neg animal \cap$

$\forall eats.\neg(\exists partOf.animal))$

$madCow \equiv cow \cap \exists eats.(brain \cup \exists partOf.sheep)$

$(animal \cup \exists partOf.animal) \cap (plant \cup \exists partOf.plant) \subseteq \perp$



We obtain:
Mad cow is unsatisfiable

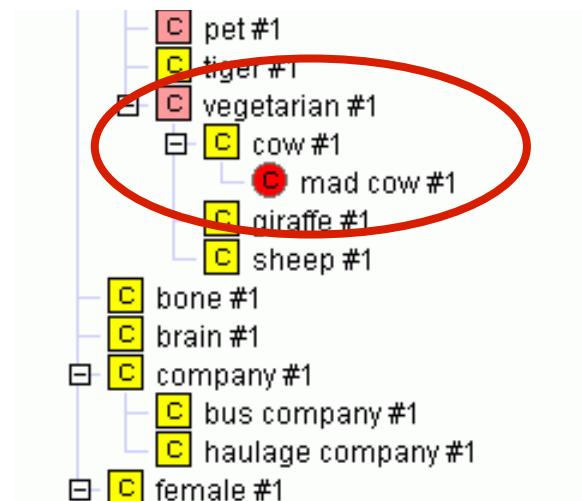
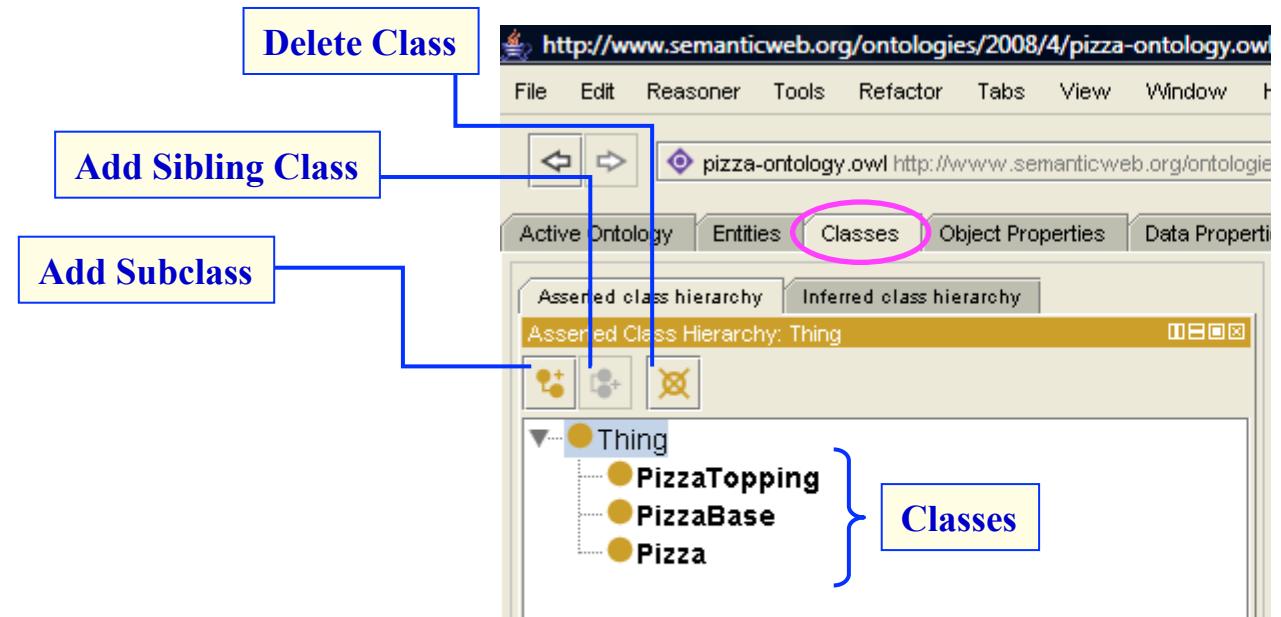


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 - 2.1. OWL primitives
 - 2.2. Reasoning with OWL
3. OWL Development Tools: Protégé
 - 3.1 Basic OWL edition
 - 3.2 Advanced OWL edition: restrictions, disjointness, etc.

Named Classes

- An OWL ontology contains **classes**, all of them subclasses of *owl:Thing*.
 - OWL classes are interpreted as sets of individuals or sets of objects.
 - The class Thing is the class that represents the set containing all individuals.
- Creating classes in the pizza example: Pizza, PizzaBase, and PizzaTopping.

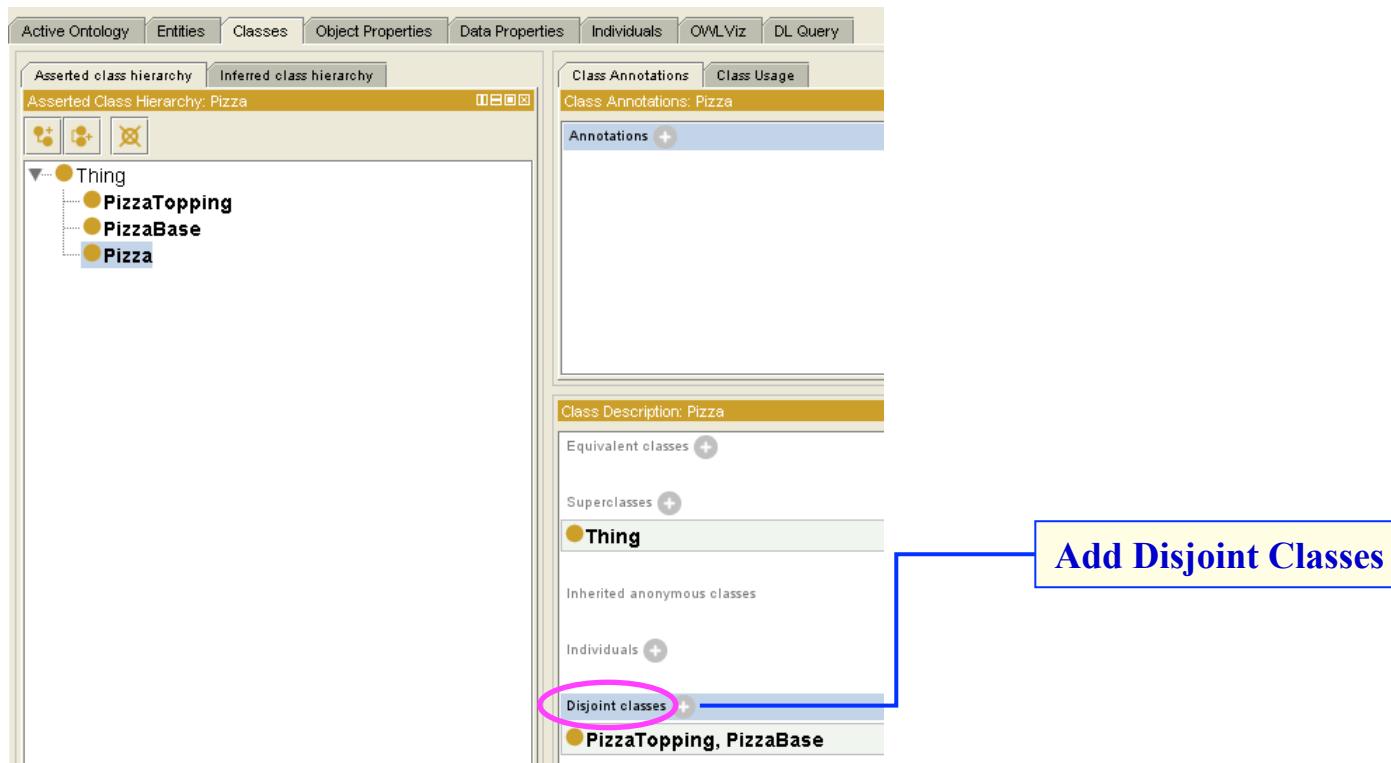


Disjoint Classes (I)

- OWL Classes are assumed to ‘**overlap**’
 - We therefore cannot assume that an individual is not a member of a particular class simply because it has not been asserted to be a member of that class.
- In order to ‘separate’ a group of classes we must make them **disjoint** from one another.
 - This ensures that an individual which has been asserted to be a member of one of the classes in the group cannot be a member of any other classes in that group.

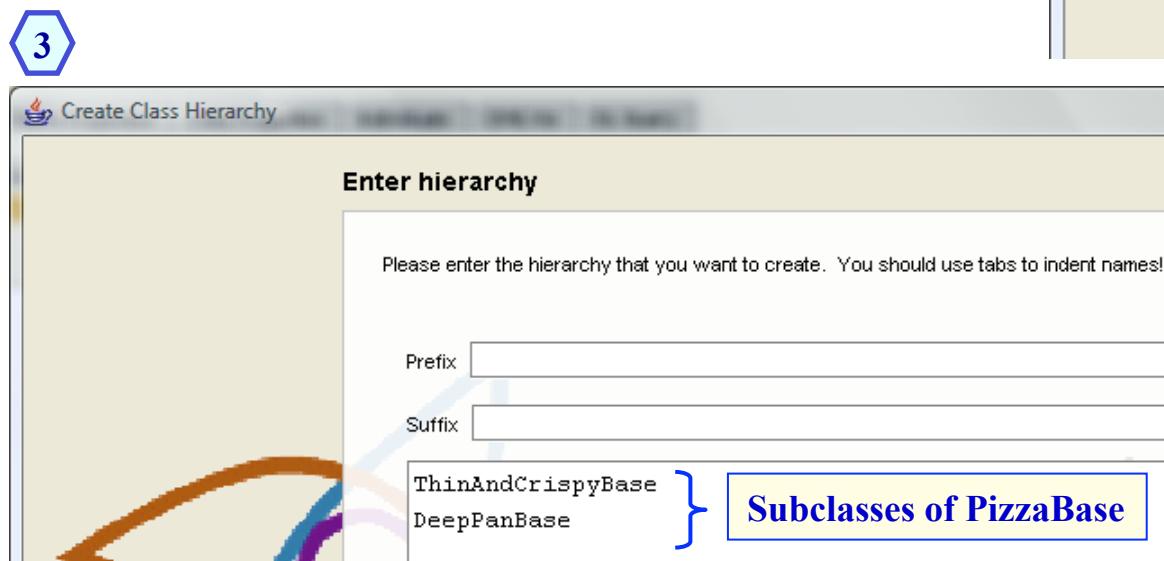
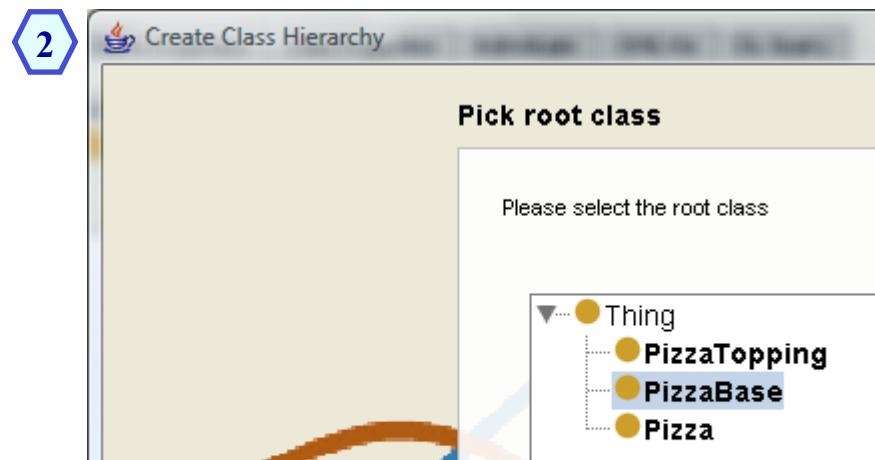
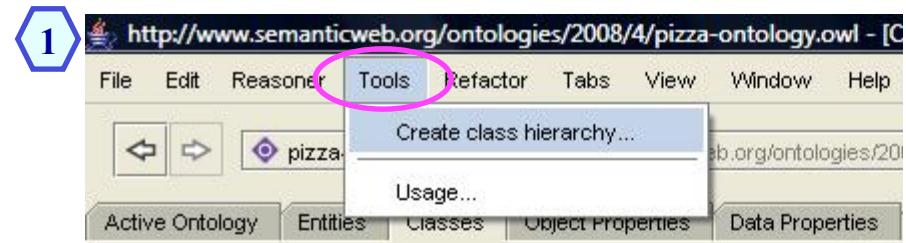
Disjoint Classes (II)

- Making the classes Pizza, PizzaTopping and PizzaBase **disjoint** from one another.
- This means that it is not possible for an individual to be a member of a combination of these classes – it would not make sense for an individual to be a Pizza and a PizzaBase.

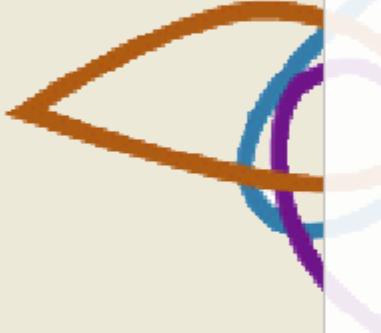


Named Classes (III)

Creating subclasses in the pizza example: ThinAndCrispyBase and DeepPanBase.



Class Hierarchy (I)

 Create Class Hierarchy

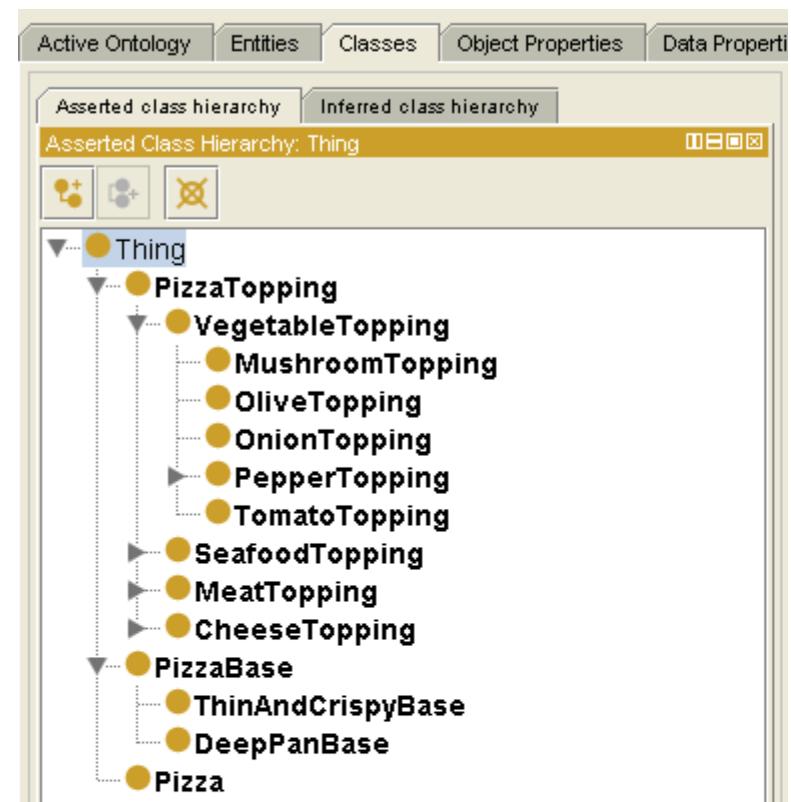
Enter hierarchy

Please enter the hierarchy that you want to

Prefix:

Suffix: Topping

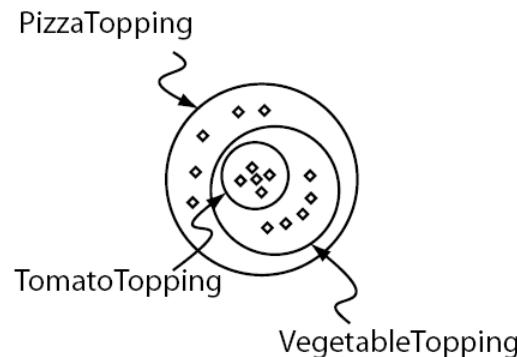
- Roquefort
- Meat
 - Ham
 - Pepperoni
 - Salami
 - SpicyBeef
- Seafood
 - Anchovy
 - Prawn
 - Tuna
- Vegetable
 - Mushroom
 - Olive
 - Onion
 - Pepper
 - JalapeñoPepper
 - Tomato



Class Hierarchy (II)

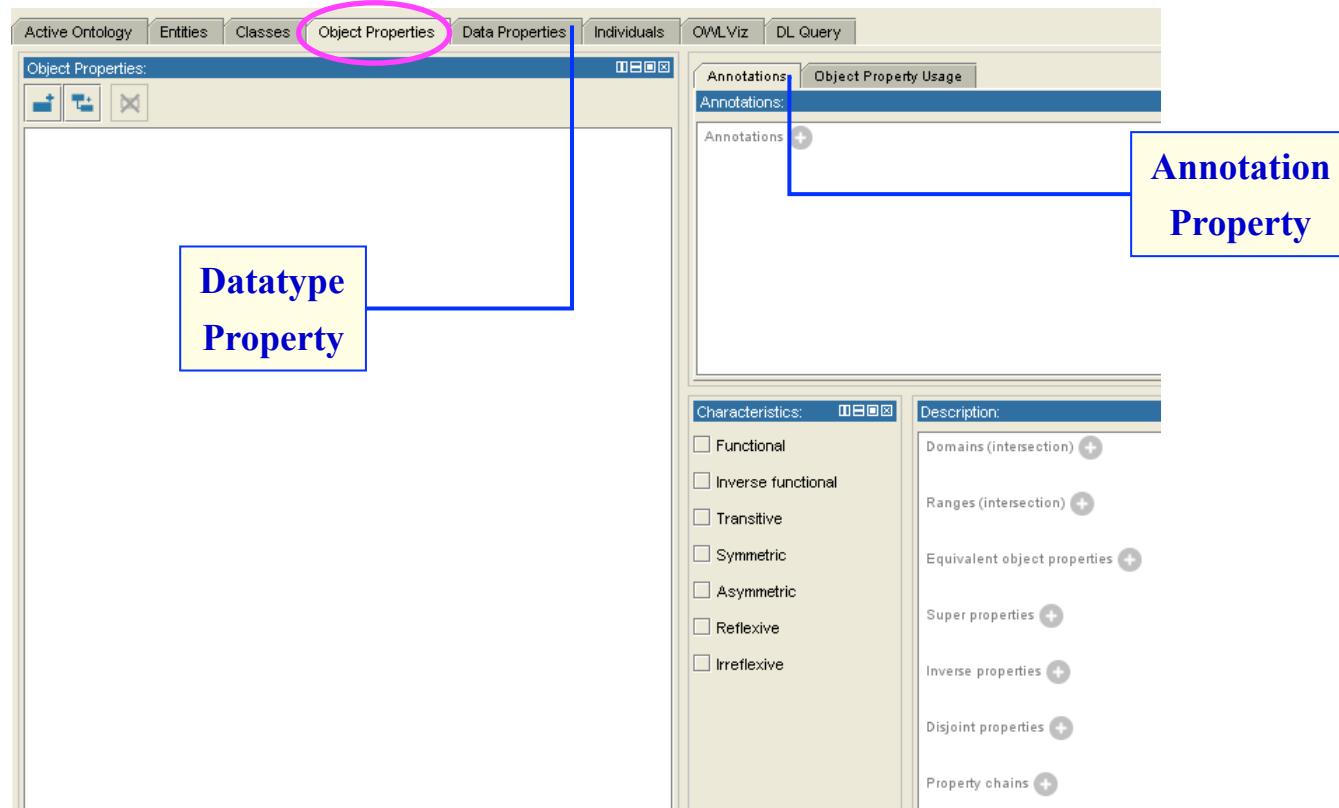
The Meaning of Subclass: all individuals that are members of the class TomatoTopping are members of the class VegetableTopping and members of the class PizzaTopping as we have stated that TomatoTopping is a subclass of VegetableTopping which is a subclass of PizzaTopping.

In OWL subclass means necessary implication. In other words, if VegetableTopping is a subclass of PizzaTopping then ALL instances of VegetableTopping are instances of PizzaTopping, without exception — if something is a VegetableTopping then this implies that it is also a PizzaTopping.



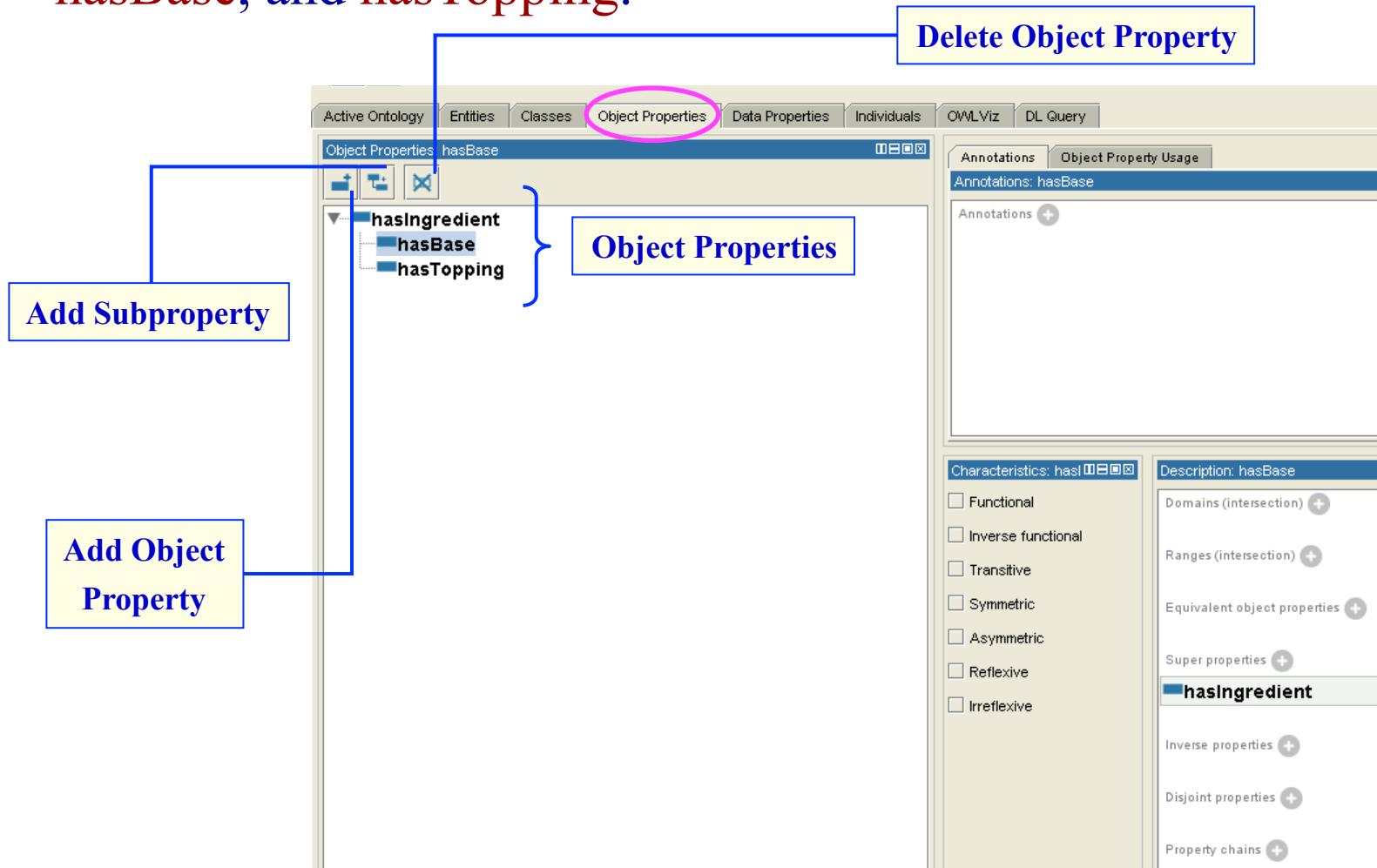
OWL Properties

OWL Properties represent relationships. There are two main types: Object properties and Datatype properties. OWL also has a third type of property: Annotation properties.



Object Properties

Creating object properties in the pizza example: hasIngredient, hasBase, and hasTopping.



Inverse Properties

Each object property may have a corresponding **inverse property**.

If some property links individual a to individual b, then its inverse property links individual b to individual a.

Creating inverse properties in the pizza example: **isIngredientOf**.

The screenshot shows the Protégé ontology editor interface. The top menu bar includes Active Ontology, Entities, Classes, Object Properties, Data Properties, Individuals, OWLViz, and DL Query. The main window has tabs for Object Properties: **hasIngredient** and Annotations: **hasIngredient**. The left panel displays a tree view of properties: **isIngredientOf** (selected), **hasIngredient** (expanded), **hasBase**, and **hasTopping**. The right panel contains sections for Characteristics: **has** (with checkboxes for Functional, Inverse functional, Transitive, Symmetric, Asymmetric, Reflexive, Irreflexive) and Description: **hasIngredient** (with buttons for Domains (intersection), Ranges (intersection), Equivalent object properties, Super properties, Inverse properties, Disjoint properties, and Property chains). The 'Inverse properties' button is highlighted with a pink oval.

OWL Object Properties Characteristics (I)

OWL allows the meaning of properties to be enriched through the use of property characteristics.

Functional Properties

Inverse Functional Properties

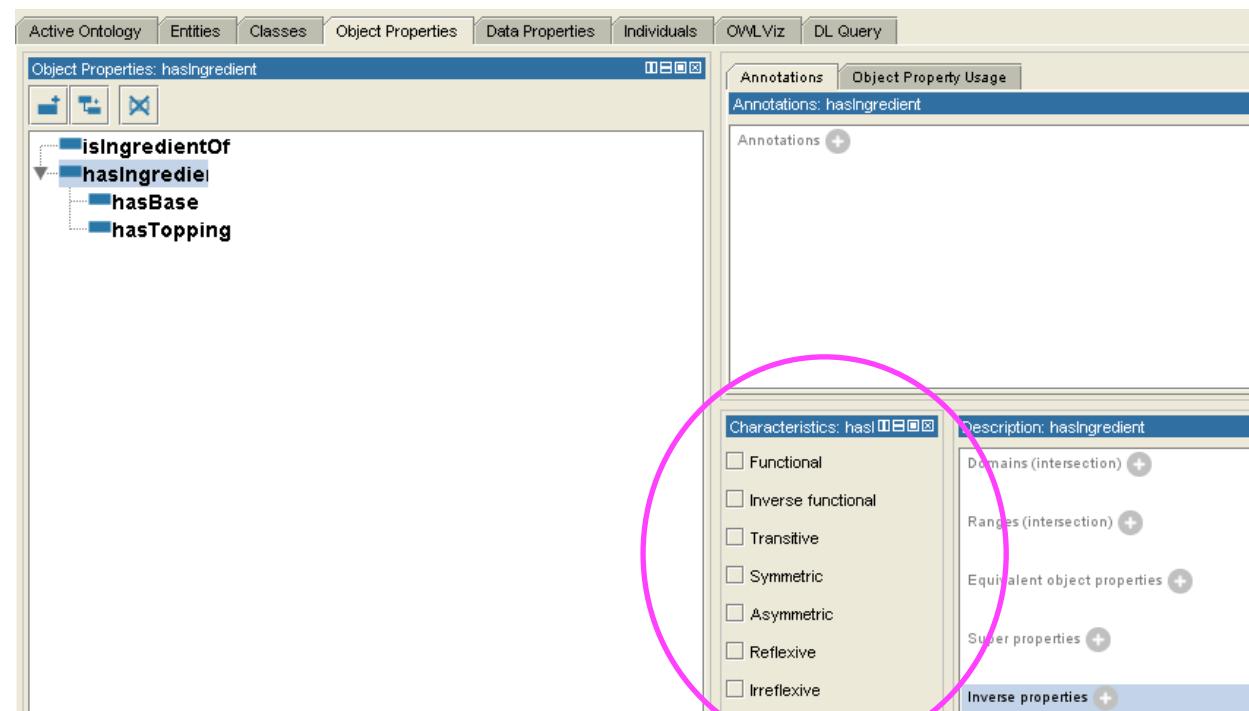
Transitive Properties

Symmetric Properties

Antisymmetric Properties

Reflexive Properties

Irreflexive Properties



Functional Properties

If a property is **functional**, for a given individual, there can be at most one individual that is related to the individual via the property.

The screenshot shows the Protégé ontology editor interface. On the left, the 'Object Properties' tab is selected, showing the 'hasIngredient' property. Below it, the 'Annotations' tab is selected, showing annotations for 'hasIngredient'. A checkbox labeled 'Functional' is circled in red. On the right, a diagram illustrates the functional nature of the 'hasBirthMother' property. It shows three individuals: Jean, Peggy, and Margaret. Arrows from Jean point to both Peggy and Margaret, labeled 'hasBirthMother'. A dashed arrow from Peggy points back to Jean. A dashed arrow from Margaret points back to Jean. A callout box states 'hasBirthMother is functional' and 'Implies Peggy and Margaret are the same individual'.

Active Ontology Entities Classes Object Properties Data Properties Individuals OWLviz DL Query

Object Properties: hasIngredient

Annotations Object Property Annotations: hasIngredient

Annotations +

Characteristics: has

Functional

Inverse functional

Transitive

Symmetric

Asymmetric

Reflexive

Irreflexive

hasBirthMother is functional

Implies Peggy and Margaret are the same individual

Jean → hasBirthMother → Peggy
Jean → hasBirthMother → Margaret

Inverse Functional Properties

If a property is **inverse functional** then it means that the inverse property is functional. For a given individual, there can be at most one individual related to that individual via the property.

The screenshot shows the OWL Viz interface with the following details:

- Object Properties: hasIngredient** panel:
 - Properties listed: isIngredientOf, hasIngredient, hasBase, hasTopping.
- Annotations: hasIngredient** panel:
 - Annotations listed: Annotations +
- Characteristics: has** panel:
 - Checkboxes for characteristics:
 - Functional
 - Inverse functional (this checkbox is highlighted with a pink oval)
 - Transitive
 - Symmetric
 - Asymmetric
 - Reflexive
 - Irreflexive

isBirthMotherOf is inverse functional
This is the inverse property of hasBirthMother — since hasBirthMother is functional, isBirthMotherOf is inverse functional

Implies same individual

Transitive Properties

If a property is **transitive**, and the property relates individual a to individual b, and also individual b to individual c, then we can infer that individual a is related to individual c via the property.

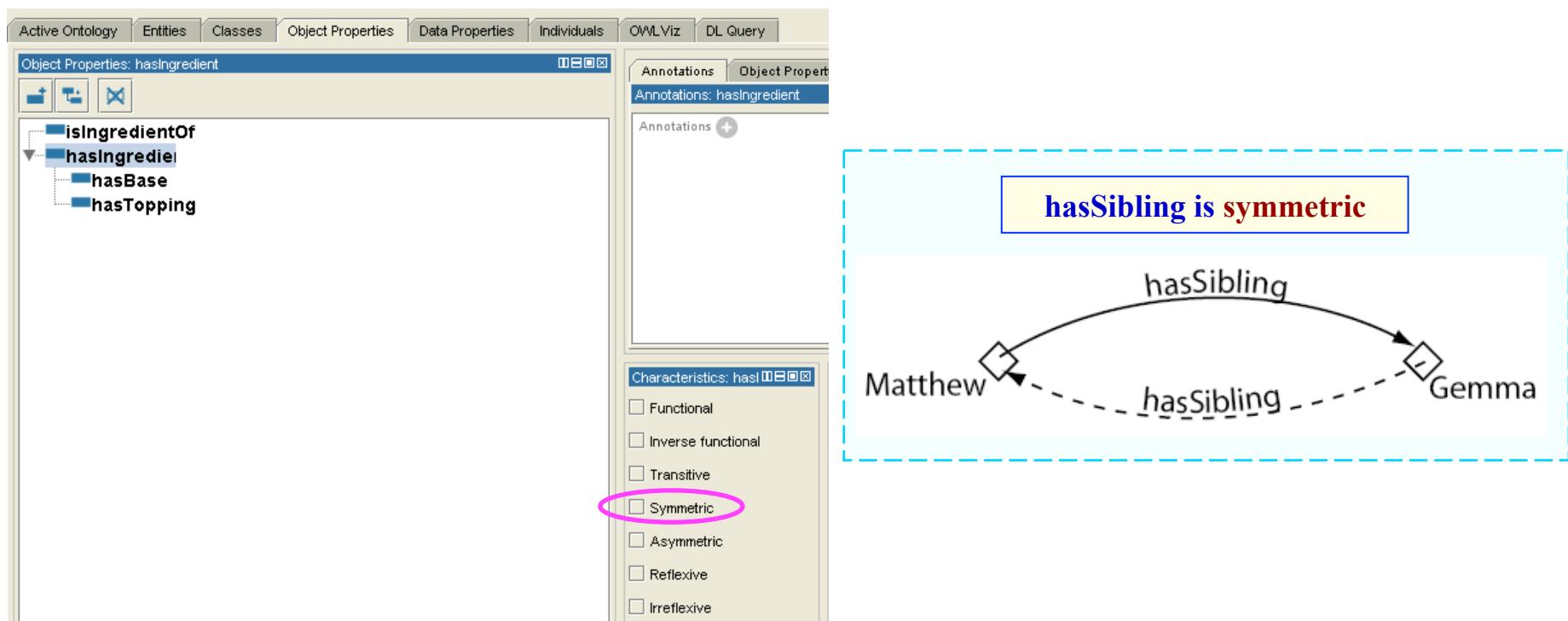
The screenshot shows a user interface for managing ontology properties. On the left, under 'Object Properties: hasIngredient', there is a tree view with nodes: 'isIngredientOf', 'hasIngredient' (selected), 'hasBase', and 'hasTopping'. On the right, under 'Annotations: hasIngredient', there is a list of characteristics. One of these, 'Transitive', is highlighted with a pink oval. Below this interface, a diagram illustrates transitivity for the 'hasAncestor' property. A dashed blue box encloses the text 'hasAncestor is transitive' and three diamond-shaped individuals: 'Matthew', 'Peter', and 'William'. Arrows labeled 'hasAncestor' point from Matthew to Peter and from Peter to William. Dashed lines connect Matthew to Peter and Peter to William, indicating inferred relationships.

hasAncestor is transitive

```
graph LR; Matthew -- hasAncestor --> Peter; Peter -- hasAncestor --> William;
```

Symmetric Properties

If a property is **symmetric**, and the property relates individual a to individual b then individual b is also related to individual a via the property.



Antisymmetric Properties

If a property is **antisymmetric**, and the property relates individual a to individual b then individual b cannot be related to individual a via the property.

The screenshot shows the Protégé ontology editor interface. On the left, the 'Object Properties: hasIngredient' panel lists properties: isIngredientOf, hasIngredient, hasBase, and hasTopping. On the right, the 'Annotations: hasIngredient' panel shows characteristics: Functional, Inverse functional, Transitive, Symmetric, Asymmetric (which is checked), Reflexive, and Irreflexive. A red circle highlights the 'Asymmetric' checkbox. To the right of the annotations is a diagram enclosed in a dashed blue border:

isChildOf is antisymmetric

```
graph TD; Robert -- isChildOf --> David; Robert -- isChildOf --> Bill; David -- isChildOf --> Bill; Robert <-- isChildOf --> X[isChildOf];
```

The diagram illustrates the 'isChildOf' property. It shows three individuals: Robert, David, and Bill. Arrows indicate relationships: Robert is the child of David and Robert is the child of Bill. David is the child of Bill. A self-loop arrow on Robert is labeled 'X isChildOf'. This visualizes why 'isChildOf' is antisymmetric: if Robert is the child of David, then David cannot be the child of Robert.

Reflexive Properties

A property is said to be **reflexive** when the property must relate individual a to itself.

The screenshot shows the Protégé ontology editor interface. On the left, the 'Object Properties' tab is selected, displaying the 'hasIngredient' property. This property is defined by the 'hasIngredientOf' class and has three subclasses: 'hasBase' and 'hasTopping'. On the right, the 'Annotations' tab is selected for the 'hasIngredient' property, showing an empty annotations section. Below these tabs, the 'Characteristics' panel lists various property characteristics. The 'Reflexive' checkbox is checked and highlighted with a red oval. To the right of the interface, a diagram illustrates reflexivity. A dashed blue border encloses a yellow box containing the text 'knows is reflexive'. Inside this box is a circular diagram with three nodes: 'Snowy', 'George', and 'Simon'. A curved arrow labeled 'knows' points from 'George' to 'George', indicating that the 'knows' property is reflexive for the individual 'George'.

Irreflexive Properties

If a property is **irreflexive**, it can be described as a property that relates an individual a to individual b, where individual a and individual b are not the same.

The screenshot shows the OWL Viz interface with the following details:

- Object Properties: hasIngredient** tab is selected.
- Annotations** tab is selected in the annotations panel.
- Characteristics: has** tab is selected in the characteristics panel.
- Annotations** panel shows no annotations for the property.
- Characteristics** panel shows the following options:
 - Functional
 - Inverse functional
 - Transitive
 - Symmetric
 - Asymmetric
 - Reflexive
 - Irreflexive
- A callout box with a blue border and yellow background contains the text **isMotherOf is irreflexive**.
- Below the callout box is a diagram illustrating the **isMotherOf** property. It features a circle labeled **isMotherOf** with an 'X' inside. Two individuals, **Alice** and **Bob**, are represented by diamond shapes. A curved arrow points from Alice to Bob, labeled **isMotherOf**. Alice is also connected to herself by a self-loop arrow labeled **isMotherOf**.

Exercise



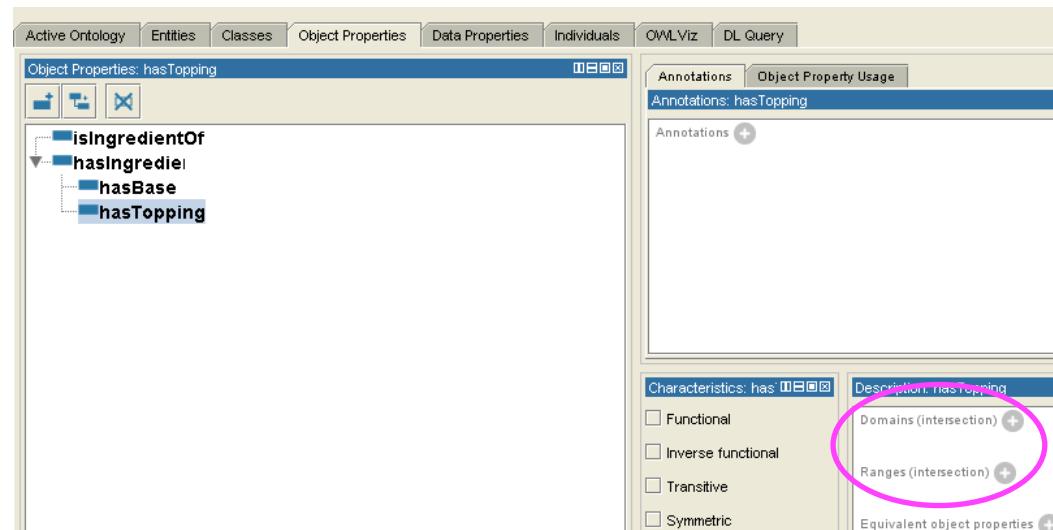
Modelling that a pizza has only one pizza base; and that if a pizza topping has ingredients, then the pizza itself contains also such ingredients.

OWL Properties: Domain and Range (I)

Properties may have a **domain** and a **range** specified.

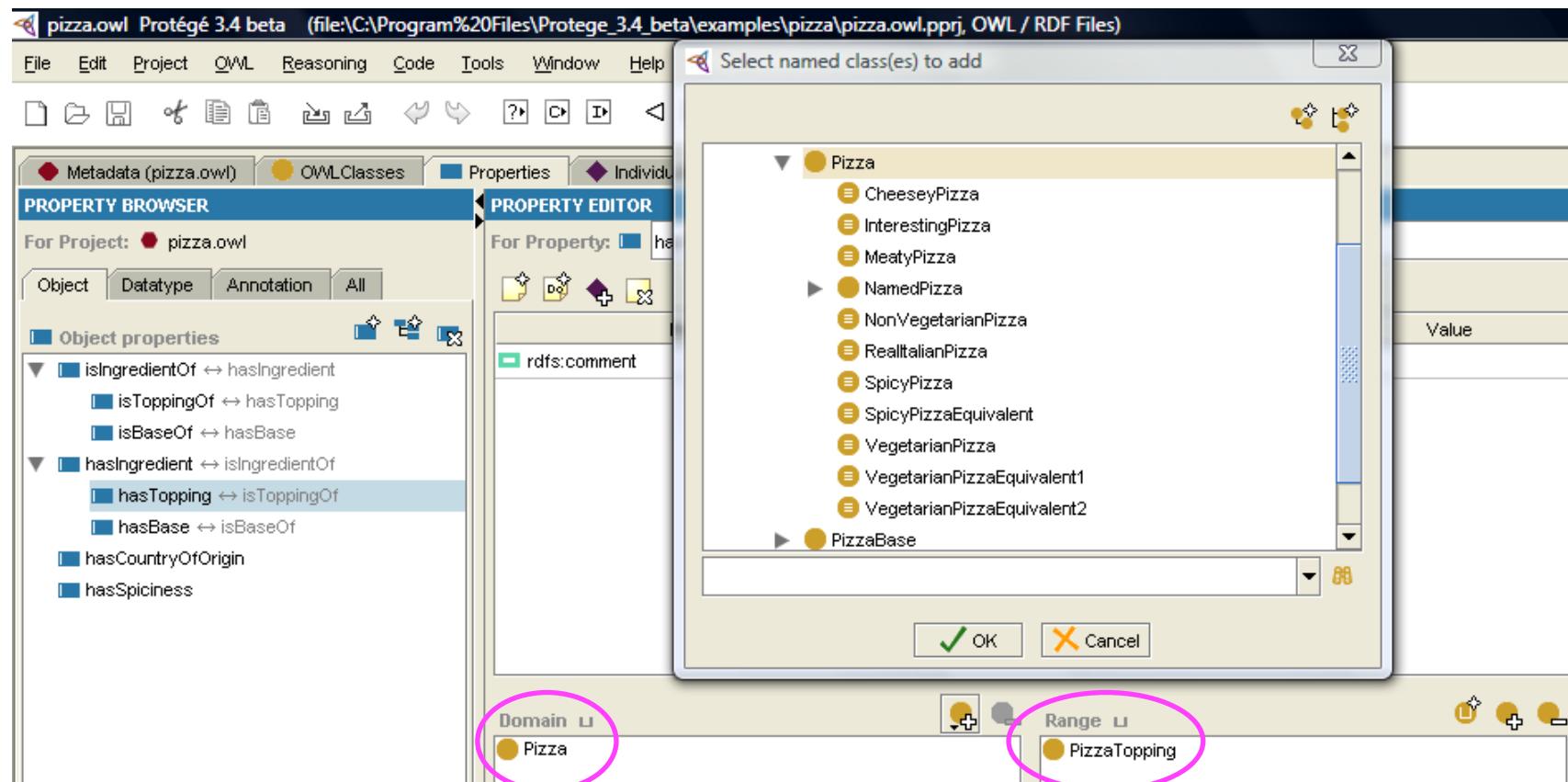
Properties link individuals from the domain to individuals from the range.

Specifying the **domain** (**Pizza**) and **range** (**PizzaTopping**) of hasTopping property.



OWL Properties: Domain and Range (II)

Protege 3.4



Property Restrictions

A **restriction** describes an anonymous class (an unnamed class). The anonymous class contains all of the individuals that satisfy the restriction (i.e. all of the individuals that have the relationships required to be a member of the class).

Restrictions are used in OWL class descriptions to specify anonymous superclasses of the class being described.

Existential restrictions describe classes of individuals that participate in at least one relationship along a specified property to individuals that are members of a specified class.

For example, “the class of individuals that have at least one (**some**) hasTopping relationship to members of MozzarellaTopping”.

Universal restrictions describe classes of individuals that for a given property only have relationships along this property to individuals that are members of a specified class.

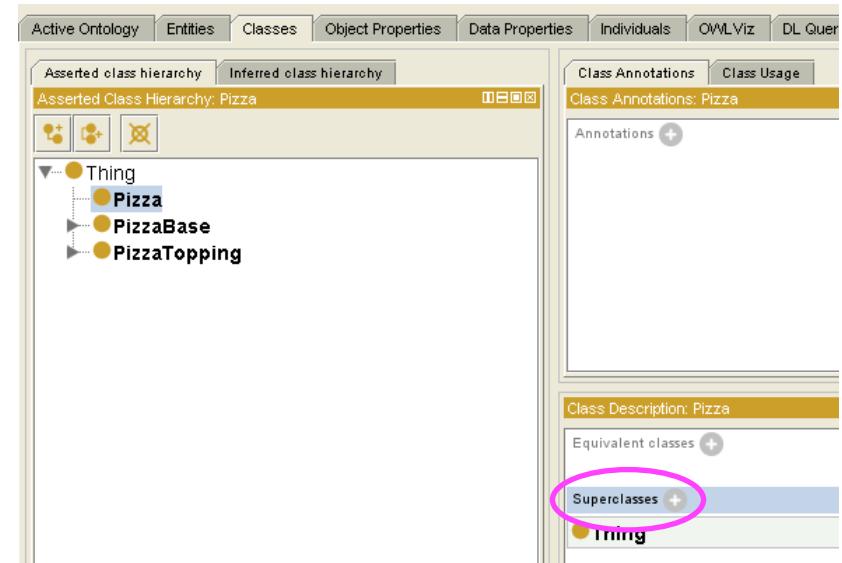
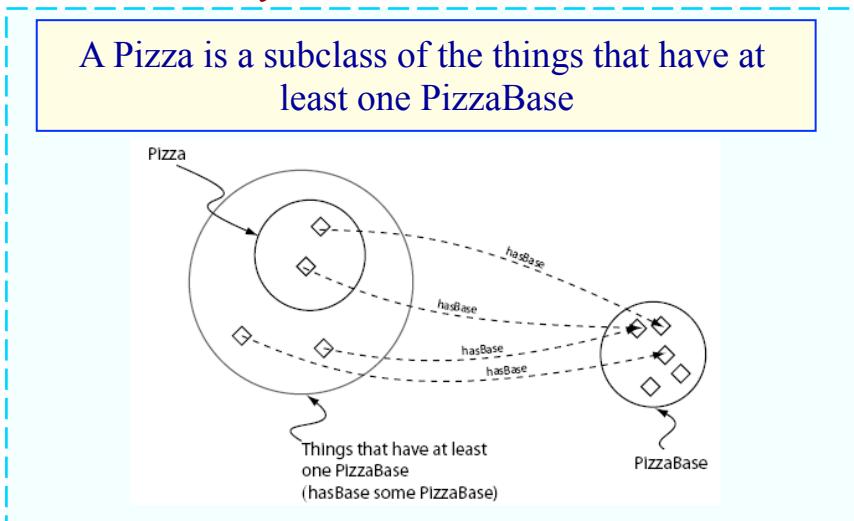
For example, “the class of individuals that **only** have hasTopping relationships to members of VegetableTopping”.

Existential Restrictions (I)

An existential restriction describes a class of individuals that have at least one (some) relationship along a specified property to an individual that is a member of a specified class.

Existential restrictions are also known as Some Restrictions, or as some values from restrictions.

Adding a **restriction** to Pizza that specifies a Pizza must have a PizzaBase (**hasBase some PizzaBase**). You are creating a *necessary condition*.



Existential Restrictions (II)

Protege 3.4

The screenshot shows the Protege 3.4 interface with the following details:

- Subclass Explorer:** Shows the asserted hierarchy for the project "pizza.owl". The "Pizza" class is selected.
- Class Editor:** For the class "Pizza".
 - Properties:** rdfs:comment and rdfs:label are listed with values "Pizza" and "en" respectively.
 - Create Restriction Dialog:** A modal window titled "Create Restriction" is open.
 - Restricted Property:** "hasBase" is selected.
 - Restriction:** "someValuesFrom" is selected from a dropdown menu.
 - Filler:** "hasBase some PizzaBase" is entered.
 - Buttons:** Save (green checkmark) and Cancel (red X).
- Annotations:** An annotation for "Pizza" is present: (instance of owl:Class) and Inferred View.
- Asserted Conditions:** Shows conditions for "NECESSARY & SUFFICIENT" and "NECESSARY".
- Disjoints:** An empty section.

Existential Restrictions (III)

Adding two restrictions to say that a MargheritaPizza has the toppings MozzarellaTopping and TomatoTopping.

If something is a member of the class MargheritaPizza it is necessary for it to be a member of: the class NamedPizza, the anonymous class of things that are linked to at least one member of the class MozzarellaTopping via the property hasTopping, and the anonymous class of things that are linked to at least one member of the class TomatoTopping via the property hasTopping.

Protege 3.4

The screenshot shows the Protege 3.4 interface with the following details:

- SUBCLASS EXPLORER:** Shows the asserted hierarchy under the project "pizza.owl". Classes include Pizza, CheeseyPizza, InterestingPizza, MeatyPizza, NamedPizza, American, AmericanHot, Cajun, Capriccosa, Caprina, Fiorentina, FourSeasons, FruttiDiMare, Giardiniera, LaReine, Margherita, and Mushroom. Margherita is currently selected.
- CLASS EDITOR:** For the class Margherita.
 - Properties:** Shows rdfs:comment and rdfs:label entries.
 - hasTopping:** Contains three restrictions:
 - hasTopping only (MozzarellaTopping or TomatoTopping)
 - hasTopping some TomatoTopping
 - hasTopping some MozzarellaTopping
 - hasBase:** Shows hasBase some PizzaBase.

Exercise



Create an **American Pizza** that is almost the same as a Margherita Pizza but with an extra topping of pepperoni.

Exercise: Solution



Create an **American Pizza** that is almost the same as a Margherita Pizza but with an extra topping of pepperoni.

The screenshot shows the Protégé 4.3 interface with the following details:

- SUBCLASS EXPLORER:** Shows the asserted hierarchy under the project "pizza.owl".
 - Pizza:** CheeseyPizza, InterestingPizza, MeatyPizza.
 - NamedPizza:** American (selected), AmericanHot, Cajun, Capricciosa, Caprina, Fiorentina, FourSeasons, FruttiDiMare, Giardiniera, LaReine, Margherita, Mushroom.
- CLASS EDITOR:** For Class: American.
 - Properties:** rdfs:comment, rdfs:label.
 - Value:** Americana.
- Object Properties:** hasTopping some PeperoniSausageTopping, hasTopping some TomatoTopping, hasTopping some MozzarellaTopping.
- Base:** hasBase some PizzaBase.

Using a Reasoner

One of the key features of ontologies that are described using OWL-DL is that they can be processed by a **reasoner**.

One of the main services offered by a reasoner is to test whether or not one class is a subclass of another class. By performing such tests on the classes in an ontology it is possible for a reasoner to compute the **inferred ontology class hierarchy**.

Another standard service that is offered by reasoners is **consistency checking**. Based on the description (conditions) of a class the reasoner can check whether or not it is possible for the class to have any instances. A class is deemed to be inconsistent if it cannot possibly have any instances.

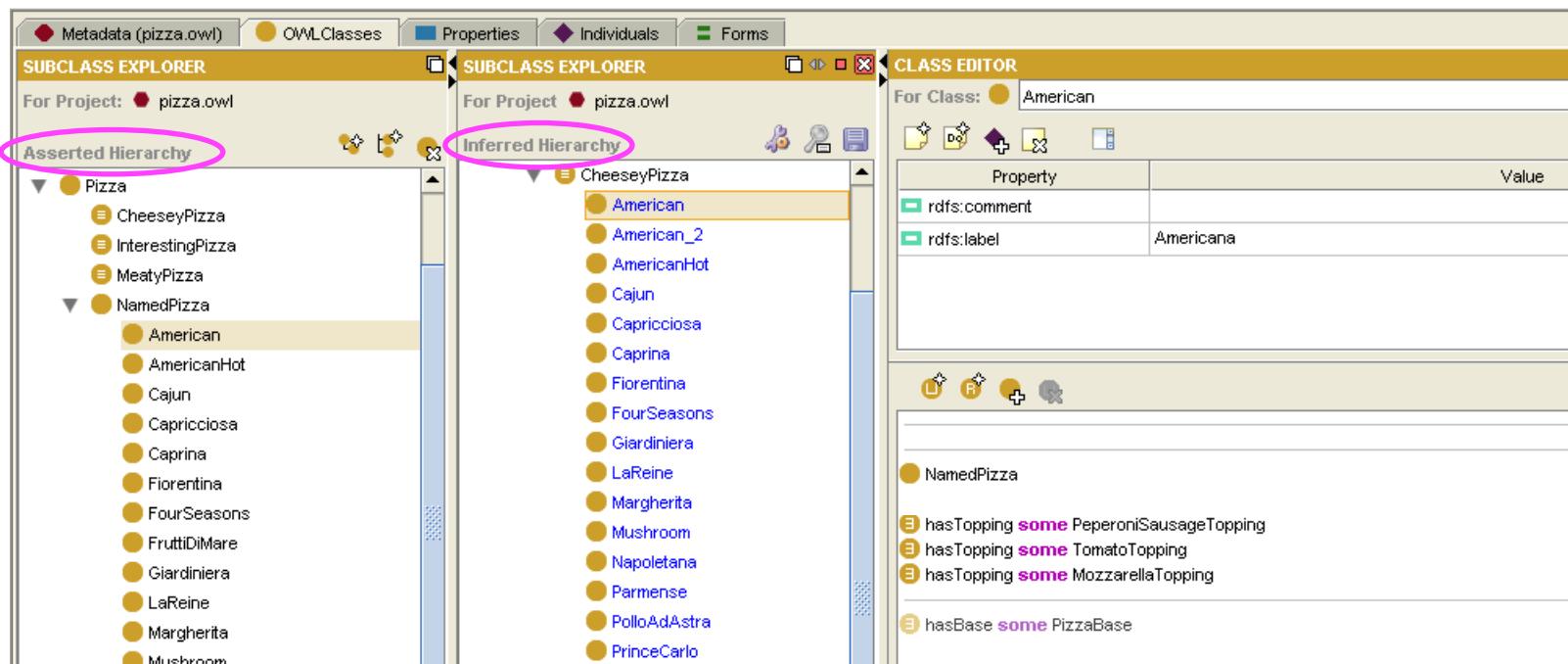
Inferring Ontology Class Hierarchy

The ontology can be ‘sent to the reasoner’ to automatically compute the classification hierarchy.

The ‘manually constructed’ class hierarchy is called the **asserted hierarchy**.

The class hierarchy that is automatically computed by the reasoner is called the **inferred hierarchy**.

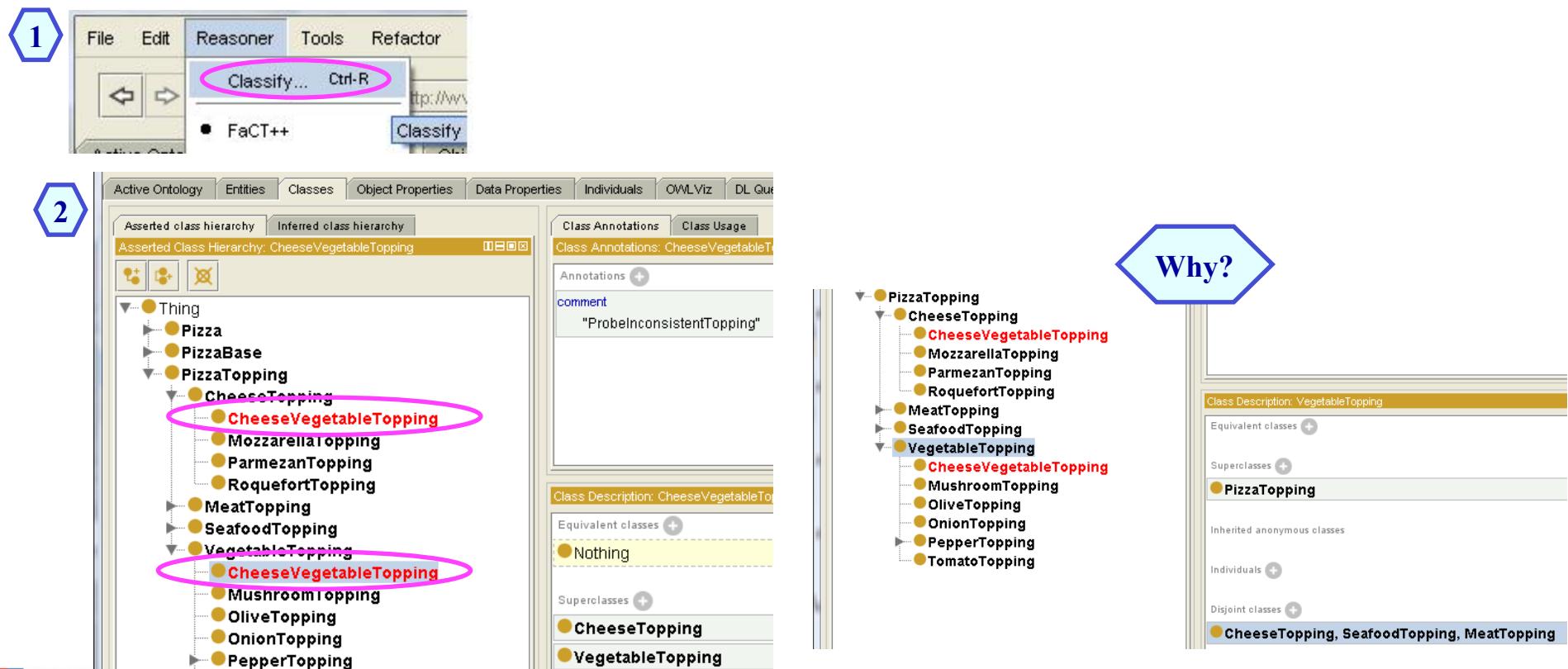
Protege 3.4. Pellet 1.5.1



Checking Ontology Consistency

This strategy is often used as a check so that we can see that we have built our ontology correctly.

Creating a **CheesyVegetableTopping** as subclass of CheesyTopping and VegetableTopping.



Necessary and Sufficient Conditions (I)

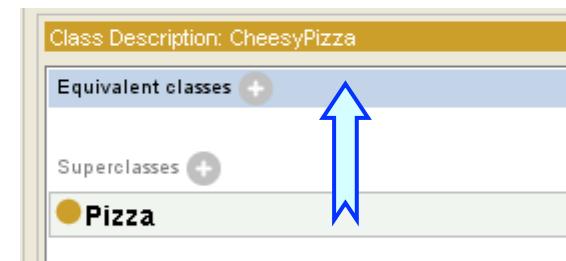
All of the classes that we have created so far have only used necessary conditions to describe them.

Necessary conditions can be read as: “If something is a member of this class then it is necessary to fulfil these conditions”.

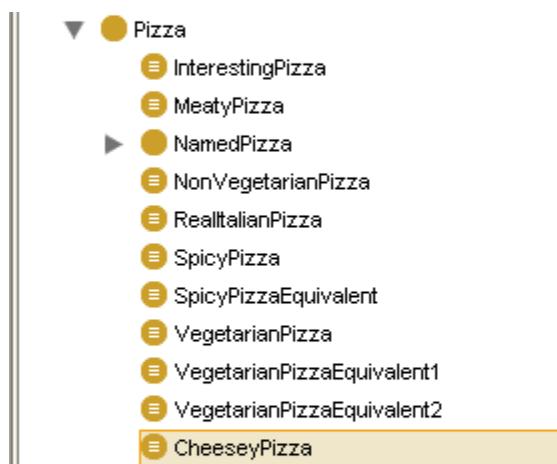
A class that only has necessary conditions is known as a Primitive Class or Partial Class.

With necessary conditions alone, we cannot say that, “*If something fulfils these conditions then it must be a member of this class*”. To make this possible we need to change the conditions from necessary conditions to **necessary AND sufficient conditions**.

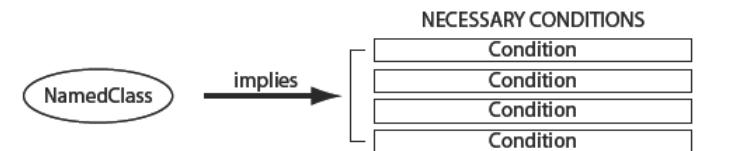
A class that has at least one set of necessary and sufficient conditions is known as a Defined Class or Complete Class.



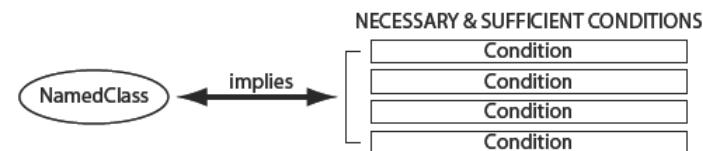
Necessary and Sufficient Conditions (II)



Protege 3.4



If an individual is a member of 'NamedClass' then it must satisfy the conditions. However if some individual satisfies these necessary conditions, we cannot say that it is a member of 'Named Class' (the conditions are not 'sufficient' to be able to say this) - this is indicated by the direction of the arrow.



If an individual is a member of 'NamedClass' then it must satisfy the conditions. If some individual satisfies the conditions then the individual must be a member of 'NamedClass' - this is indicated by the double arrow.



Universal Restrictions (I)

All of the restrictions that we have created so far have been existential ones (some).

However, existential restrictions do not mandate that the only relationships for the given property that can exist must be to individuals that are members of the specified filler class. To restrict the relationships for a given property to individuals that are members of a specific class we must use a **universal restriction**.

Universal restrictions constrain the relationships along a given property to individuals that are members of a specific class.

For example the universal restriction $\forall s \text{ Topping Mozzarella} \text{ Topping}$ describes the individuals all of whose hasTopping relationships are to members of the class MozzarellaTopping.

Universal Restrictions (II)

Creating a Vegetarian Pizza that only have toppings that are CheeseTopping or VegetableTopping.

Protege 3.4

The screenshot shows the Protege 3.4 interface. A modal dialog box titled "Create Restriction" is open, showing the "Restriction" tab selected. In the "Restricted Property" list, "hasTopping" is selected. In the "Restriction" list, "allValuesFrom" is selected. Below the dialog, the main Protege window shows a class named "Pizza" with several subclasses listed. One subclass, "VegetarianPizza", has a restriction applied: "hasTopping only (VegetarianTopping or CheeseTopping)". This restriction is highlighted with a pink oval. The "Asserted Conditions" panel on the right shows the restriction being asserted under the "NECESSARY & SUFFICIENT" section.



Automatic Classification and Open World Assumption (I)

We want to use the reasoner to automatically compute the superclass-subclass relationship (subsumption relationship) between MargheritaPizza and VegetarianPizza.

We believe that MargheritaPizza should be vegetarian pizza (they should be subclasses of VegetarianPizza). This is because they have toppings that are essentially vegetarian toppings — by our definition, vegetarian toppings are members of the classes CheeseTopping or VegetableTopping and their subclasses.

Having previously created a definition for VegetarianPizza (using a set of necessary and sufficient conditions) we can use the reasoner to perform automatic classification and determine the vegetarian pizzas in our ontology.



Automatic Classification and Open World Assumption (II)

MargheritaPizza has not been classified as subclass of VegetarianPizza.

Reasoning in OWL (Description Logics) is based on what is known as the **open world assumption (OWA)**. The open world assumption means that we cannot assume something does not exist until it is explicitly stated that it does not exist.

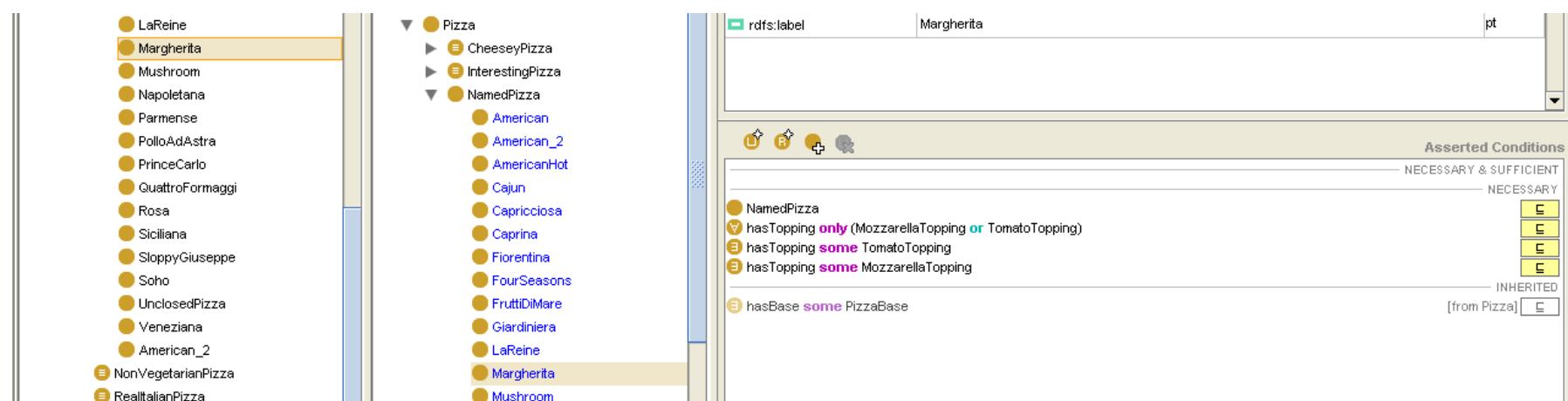
In the case of our pizza ontology, we have stated that MargheritaPizza has toppings that are kinds of MozzarellaTopping and also kinds of TomatoTopping. Because of the open world assumption, until we explicitly say that a MargheritaPizza **only** has these kinds of toppings, it is assumed (by the reasoner) that a MargheritaPizza could have other toppings.



Automatic Classification and Open World Assumption (III)

To specify explicitly that a MargheritaPizza has toppings that are kinds of MozzarellaTopping or kinds of MargheritaTopping and only kinds of MozzarellaTopping or MargheritaTopping, we must add what is known as a **closure axiom or restriction** on the hasTopping property.

Protege 3.4



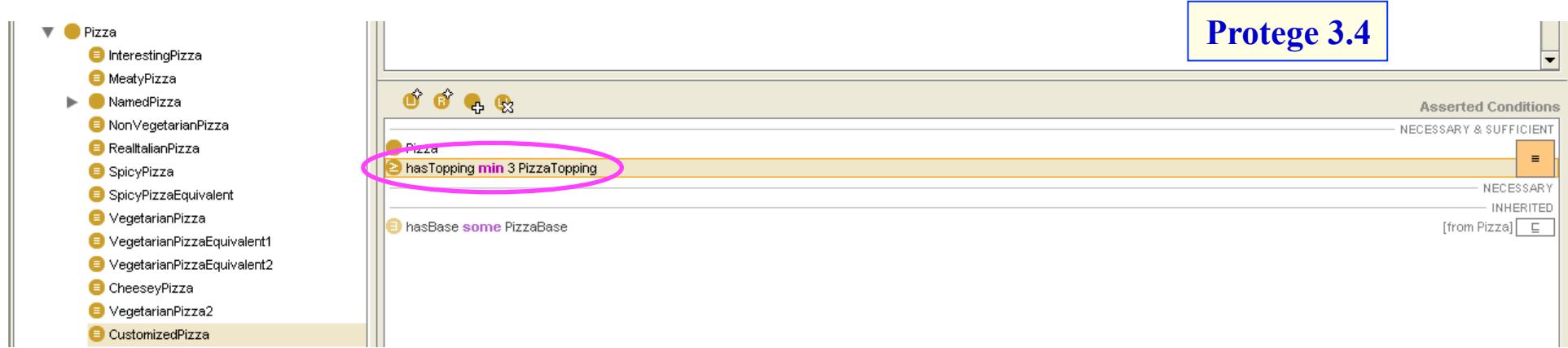
Cardinality Restrictions (I)

In OWL we can describe the class of individuals that have at least, at most or exactly a specified number of relationships with other individuals or datatype values. The restrictions that describe these classes are known as **Cardinality Restrictions**.

- A **Minimum Cardinality Restriction** specifies the minimum number of P relationships that an individual must participate in.
- A **Maximum Cardinality Restriction** specifies the maximum number of P relationships that an individual can participate in.
- A **Cardinality Restriction** specifies the exact number of P relationships that an individual must participate in.

Cardinality Restrictions (II)

Creating a Customized Pizza that has at least three toppings.



Qualified Cardinality Restrictions (I)

Qualified Cardinality Restrictions (QCR), which are more specific than cardinality restrictions in that they state the class of objects within the restriction.

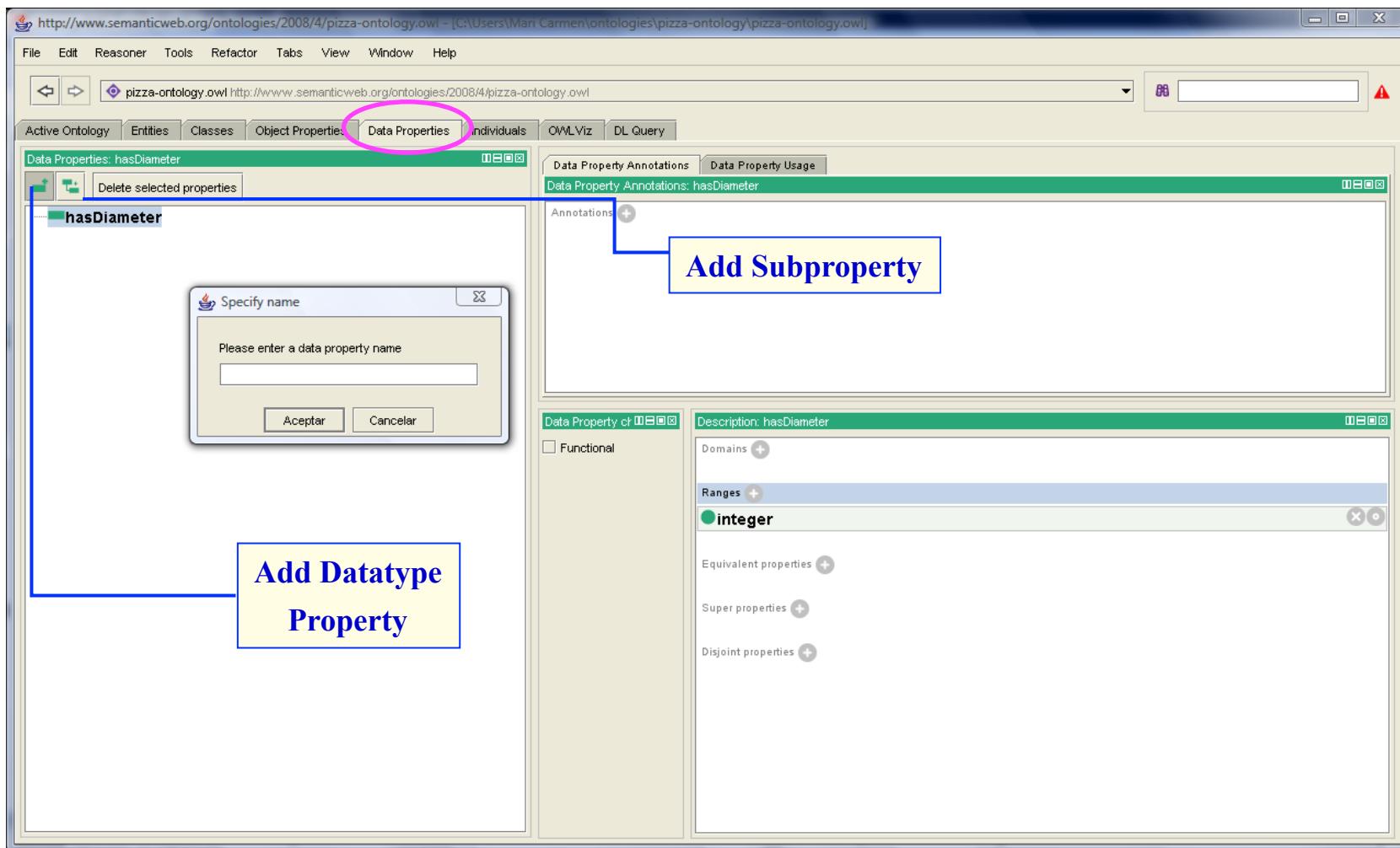
Creating a **Four Cheese Pizza**, as subclass of NamedPizza, which has exactly four cheese toppings.

Protege 3.4

The screenshot shows the Protege 3.4 interface for creating an ontology. On the left, the class hierarchy tree shows 'NamedPizza' as the root, with several subclasses listed: American, FourCheese (selected), AmericanHot, Cajun, Capricciosa, Caprina, Fiorentina, FourSeasons, FruttiDiMare, Giardiniera, LaReine, and Margherita. In the center, the 'Edit Class' dialog is open for 'FourCheese'. The 'Property' tab shows an asserted rdfs:comment. The 'Value' tab is empty. Below the tabs, the 'Asserted Conditions' section is visible, containing two conditions: 'NamedPizza' and 'hasTopping only (hasTopping exactly 4 CheeseTopping)'. The 'Lang' tab is also present. On the right, the 'Asserted Conditions' panel shows the asserted conditions again, with 'NECESSARY & SUFFICIENT' and 'NECESSARY' checked. The 'INHERITED' section shows '[from Pizza]' with a checkmark. The overall interface is light blue and white, typical of Protege's design.

Datatype Properties

Creating a datatype property in the pizza example: hasDiameter.



Restrictions and Boolean Class Constructors

OWL	DL Symbol	Manchester OWL Syntax Keyword	Example
someValuesFrom	\exists	some	hasChild some Man
allValuesFrom	\forall	only	hasSibling only Woman
hasValue	\ni	value	hasCountryOfOrigin value England
minCardinality	\geq	min	hasChild min 3
cardinality	$=$	exactly	hasChild exactly 3
maxCardinality	\leq	max	hasChild max 3

OWL	DL Symbol	Manchester OWL Syntax Keyword	Example
intersectionOf	\sqcap	and	Doctor and Female
unionOf	\sqcup	or	Man or Woman
complementOf	\neg	not	not Child

Exercise



Create a Meaty Pizza.

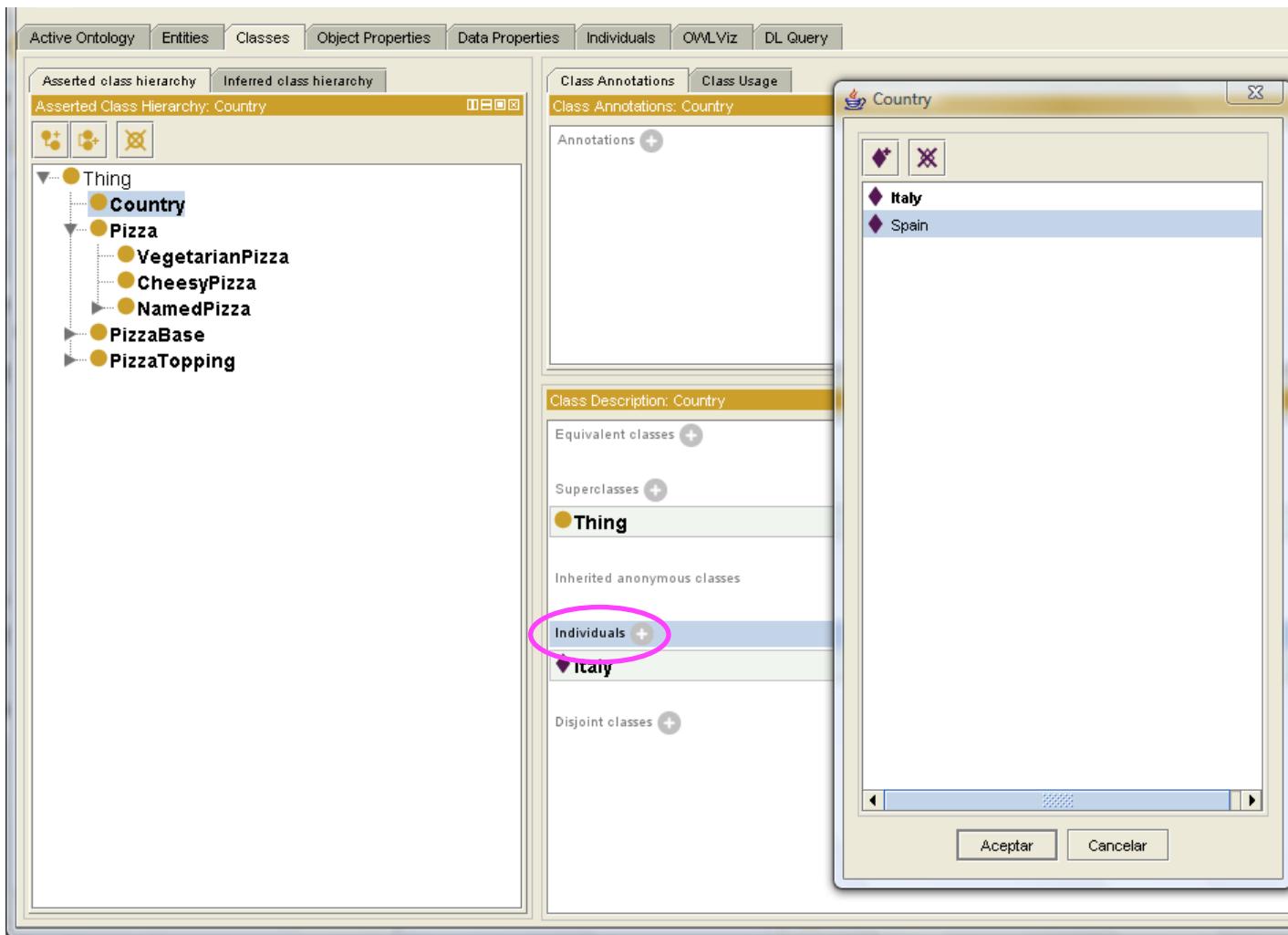
Create a Vegetarian Pizza, which have no meat and no fish toppings.

Create a Real Italian Pizza, which only have bases that are Thin and Crispy.

Create a subclass of Named Pizza with a topping of Mozzarella.

Individuals

Creating individuals of class Country.



hasValue Restriction

Specifying Italy as country of origin for Mozzarella.

