Submission instructions

Submission in pairs unless otherwise authorized

- This notebook contains all the questions. You should follow the instructions below.
- Solutions for both theoretical and practical parts should be written in this notebook

Moodle submission

You should submit three files:

- IPYNB notebook:
 - All the wet and dry parts, including code, graphs, discussion, etc.
- PDF file:
 - Export the notebook to PDF. Make sure that all the cells are visible.
- Pickle files:
 - As requested in Q2.a and Q3.a
- PY file:
 - As requested in Q3.a

All files should be in the following format: "HW1_ID1_ID2.file" Good Luck!

Question 1

I. Softmax Derivative (10pt)

Derive the gradients of the softmax function and demonstrate how the expression can be reformulated solely by using the softmax function, i.e., in some expression where only softmax(x), but not x, is present). Recall that the softmax function is defined as follows:

$$softmax(x)_i = rac{e^{x_i}}{\sum_{j=1}^N e^{x_j}}$$

I. Softmax Derivative - Answer:

I)

$$\frac{\partial softmax(x_i)}{\partial x_k} = \frac{\partial}{\partial x_k} \left(\frac{e^{x_i}}{\sum_{i=1}^N e^{x_i}} \right)$$

Case i = k:

Applying the quotient rule:

$$\frac{\partial softmax(x_i)}{\partial x_k} = \frac{e^{x_i} \cdot \frac{\partial}{\partial x_k} \left(\sum_{j=1}^N e^{x_j}\right) - \left(\frac{\partial e^{x_i}}{\partial x_k}\right) \cdot \sum_{j=1}^N e^{x_j}}{\left(\sum_{j=1}^N e^{x_j}\right)^2} = \frac{e^{x_i} \cdot \sum_{j=1}^N e^{x_j} - e^{x_i} \cdot e^{x_k}}{\left(\sum_{j=1}^N e^{x_j}\right)^2}$$
$$= softmax(x_i) \cdot (1 - softmax(x_i))$$

Case $i \neq k$:

Note that $\frac{\partial e^{x_i}}{\partial x_k} = 0$, hence:

$$\frac{\partial softmax(x_i)}{\partial x_k} = -\frac{e^{x_i}e^{x_k}}{\left(\sum_{j=1}^N e^{x_j}\right)^2} = -softmax(x_i) \cdot softmax(x_k)$$

II. Cross-Entropy Gradient (10pt)

Derive the gradient of cross-entropy loss with regard to the inputs of a softmax function. i.e., find the gradients with respect to the softmax input vector θ , when the prediction is denoted by $\hat{y} = softmax(\theta)$. Remember the cross entropy function is:

$$CE(y,\hat{y}) = -\sum_i y_i log(\hat{y_i})$$

where y is the one-hot label vector, and \hat{y} is the predicted probability vector for all classes.

II. Cross-Entropy Gradient - Answer

II)

$$\frac{\partial CE(y, \hat{y})}{\partial \theta_k} = \frac{\partial CE(y, \hat{y})}{\partial \hat{y}} \cdot \frac{\partial softmax(\theta_i)}{\partial \theta_k}$$

Note that $\hat{y} = softmax(\theta_i)$

Case i = k:

$$\frac{\partial CE(y, \hat{y})}{\partial \theta_k} = \frac{\partial CE(y, \hat{y})}{\partial \hat{y}} \cdot softmax(\theta_i) \cdot (1 - softmax(\theta_i))$$

Case $i \neq k$:

$$\frac{\partial CE(y, \hat{y})}{\partial \theta_k} = \frac{\partial CE(y, \hat{y})}{\partial \hat{y}} \cdot -softmax(\theta_i) \cdot softmax(\theta_k)$$

Question 2

I. Derivative Of Activation Functions (10pt)

The following cell contains an implementation of some activation functions. Implement the corresponding derivatives.

```
import torch

def sigmoid(x):
    return 1 / (1 + torch.exp(-x))

def tanh(x):
    return torch.div(torch.exp(x) - torch.exp(-x), torch.exp(x) +
    torch.exp(-x))

def softmax(x):
    exp_x = torch.exp(x.T - torch.max(x, dim=-1).values).T #
Subtracting max(x) for numerical stability
    return exp_x / exp_x.sum(dim=-1, keepdim=True)
```

```
In [86]:

def d_sigmoid(x):
    """

    Derivative of the sigmoid function.
```

II. Train a Fully Connected network on MNIST (30pt)

In the following exercise, you will create a classifier for the MNIST dataset. You should write your own training and evaluation code and meet the following constraints:

- You are only allowed to use torch tensor manipulations.
- You are NOT allowed to use:
 - Auto-differentiation backward()
 - Built-in loss functions
 - Built-in activations
 - Built-in optimization
 - Built-in layers (torch.nn) </h4>

- a) The required classifier class is defined.
 - You should implement the forward and backward passes of the model.
 - Train the model and plot the model's accuracy and loss (both on train and test sets) as a function of the epochs.
 - You should save the model's weights and biases. Change the student_ids to yours.

In this section, you **must** use the "set_seed" function with the given seed and **sigmoid** as an activation function.

```
In [88]:
         mport torch
        EPOCHS = 16
        BATCH SIZE = 32
            torch.backends.cudnn.deterministic = True
```

```
def one_hot(y, num_of_classes=10):
   hot = torch.zeros((y.size()[0], num_of_classes))
   hot[torch.arange(y.size()[0]), y] = 1
   return hot

def cross_entropy(y, y_hat):
   return -torch.sum(one_hot(y) * torch.log(y_hat)) / y.size()[0]
```

```
class FullyConnectedNetwork:
    def __init__(self, input_size, output_size, hidden_size1,
    activiation_func, lr=0.01):
        # parameters
        self.input_size = input_size
        self.output_size = output_size
        self.hidden_size1 = hidden_size1

        # activation function
        self.activation_func = activiation_func

# weights
        self.W1 = torch.randn(self.input_size, self.hidden_size1)
        self.b1 = torch.zeros(self.hidden_size1)

        self.W2 = torch.randn(self.hidden_size1, self.output_size)
        self.b2 = torch.zeros(self.output_size)

        self.lr = lr
```

```
def forward(self, x):
function and store al
       z2 = torch.matmul(self.a1, self.W2) + self.b2
entropy
       # Gradient for the hidden Layer (backpropagation)
Layer
       # Gradient for the weights and biases of the first layer
```

```
In [128...
students_ids = "321817405_208912675"
model345 = FullyConnectedNetwork(784, 10,128, torch.sigmoid)
##torch.save({"W1": model.W1, "W2": model.W2, "b1": model.b1, "b2":
model.b2}, f"HW1_Q2_{students_ids}.pkl")
```

- b) Train the model with various learning rates (at least 3).
 - Plot the model's accuracy and loss (both on train and test sets) as a function of the epochs.
 - Discuss the differences in training with different learning rates. Support your answer with plots.

```
In [126...
         set seed(SEED)
         model1 = FullyConnectedNetwork(784, 10, 128, sigmoid, lr=0.01)
         model2 = FullyConnectedNetwork(784, 10, 128, sigmoid, lr=0.05)
             # Initialize lists to store training losses and test accuracies
```

```
for epoch in range(EPOCHS):
    running_loss = 0.0

    for i, data in enumerate(train_dataloader, 0):
        inputs, labels = data
        y_hat = model.forward(inputs) # Forward pass
        model.backward(inputs, labels, y_hat) # Backward pass

(using stored a1 and z1)
        update_parameters(model) # Make sure this function is

defined elsewhere

    loss = cross_entropy(labels, y_hat)
        running_loss += loss

    accuracy, _ = evaluate(model, test_dataloader)
        train_losses.append(running_loss / len(train_dataloader))
        test_accuracies.append(accuracy)

# Return the Lists containing the metrics for plotting
    return train_losses, test_accuracies
```

```
In [9]: # Assume train() is called for each model and returns losses and
accuracies
train_losses1, test_accuracies1 = train(model1, train_dataloader,
test_dataloader)
train_losses2, test_accuracies2 = train(model2, train_dataloader,
test_dataloader)
train_losses3, test_accuracies3 = train(model3, train_dataloader,
test_dataloader)

# Plot accuracy and loss for all models
plt.figure(figsize=(12, 6))

# Plot training losses
plt.subplot(1, 2, 1)
plt.plot(train_losses1, label='Model 1 (lr = 0.01)', color='blue')
plt.plot(train_losses2, label='Model 2 (lr = 0.05)', color='green')
plt.plot(train_losses3, label='Model 3 (lr = 0.1)', color='red')
plt.xlabel('Epochs')
plt.ylabel('Loss')
plt.title('Training loss')
plt.legend()
```

```
plt.grid()

# Plot test accuracies

plt.subplot(1, 2, 2)

plt.plot(test_accuracies1, label='Model 1 (lr = 0.01)', color='blue')

plt.plot(test_accuracies2, label='Model 2 (lr = 0.05)', color='green')

plt.plot(test_accuracies3, label='Model 3 (lr = 0.1)', color='red')

plt.xlabel('Epochs')

plt.ylabel('Accuracy')

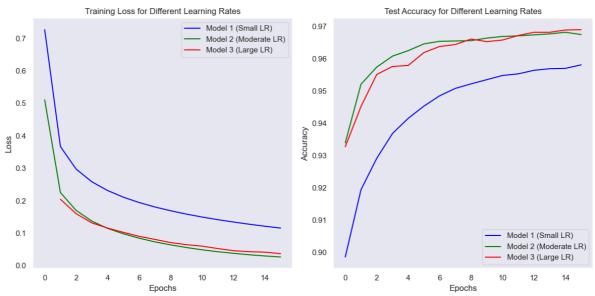
plt.title('Test Accuracy')

plt.legend()

plt.grid()

plt.tight_layout()

plt.show()
```



Small learning rates (blue) lead to slow convergence and lower final accuracy due to minimal weight updates. Moderate learning rates (green) strike the best balance, achieving rapid loss reduction and the highest accuracy with stability. Large learning rates (red) converge quickly but may cause fluctuations and risk instability if increased further. Overall, the moderate learning rate provides the best performance and generalization.

Question 3

I. Implement and Train a CNN (30pt)

As you might know, there are many dogs on campus. Sometimes, understanding the emotions of a dog can be challenging, and people might mistakenly try to pet it when it is sad or angry. As a data scientist, you have

been asked to assist Technion's students. Your task is to create a "dog emotion classifier.

Your code should meet the following constraints:

- Your classifier must be CNN based
- You are not allowed to use any pre-trained model

To satisfy your boss, your model must achieve at least 70% accuracy on the test set. Your boss also emphasized that the model will be deployed on smartphones, so it should have a small number of parameters. 25% of your grade for this task will be based on the number of parameters your model uses — fewer parameters will yield a higher grade.

Stages

- 1. Perform a short EDA (Exploratory Data Analysis).
- 2. Train the model and plot its accuracy and loss (for both the training and validation sets) as a function of the epochs.
- 3. Report the test set accuracy.
- 4. Discuss the progress you made and describe your final model.

Your data is in hw1_data/dog_emotion.

You can define a custom dataset (as in tutorial 3) or use

torchvision.datasets.ImageFolder.

Submission

In addition to the code in the notebook, you should submit:

- a .py file containing your model class.
- a .pkl file containing the weight of your model

1. EDA:

```
import numpy as np
import matplotlib.pyplot as plt
from torchvision import datasets

# EDA Function
def perform_eda(dataset, train_loader):
```

```
# 1. Label Distribution
   # 3. Color Histograms
channel
```

```
# Integrating EDA
```



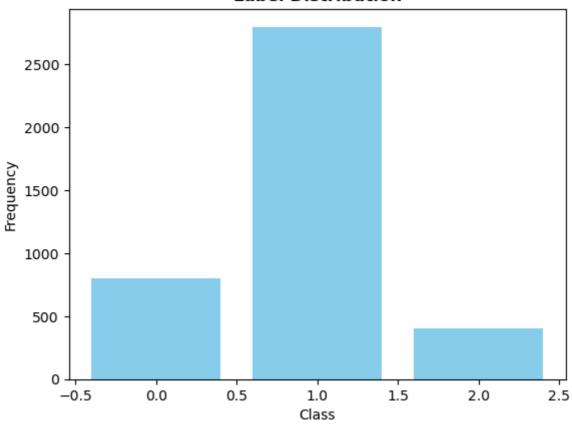
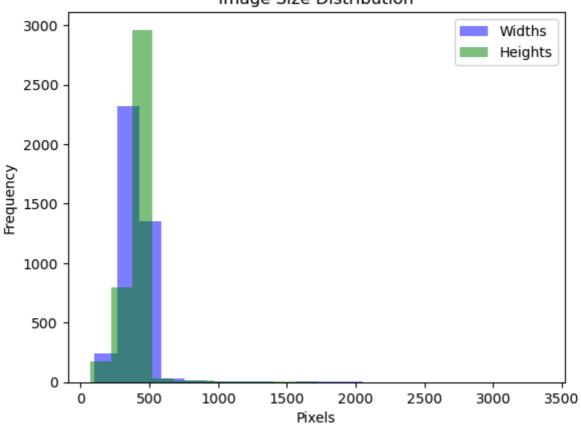


Image Size Distribution



Average image Size: (417.82, 388.91_/

2. Model Training:

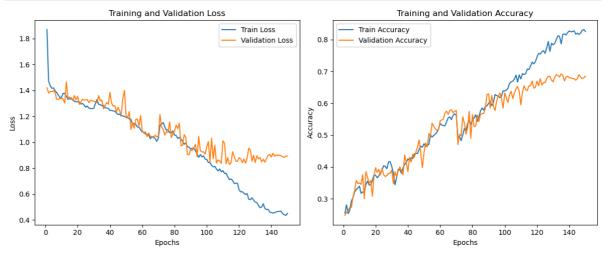
```
In [34]:
          mport torch
          mport torch.nn as nn
```

```
train dataset =
datasets.ImageFolder(root='hw1_data/dog_emotion/train',
transform=transform test)
datasets.ImageFolder(root='hw1_data/dog_emotion/test',
transform=transform_test)
batch_size=batch_size, shuffle=True)
    val loader = torch.utils.data.DataLoader(val dataset,
batch size=batch size, shuffle=False)
# CNN Model
 class DogEmotionCNN(nn.Module):
        super(DogEmotionCNN, self).__init__()
        self.conv1 = nn.Sequential(
```

```
self.conv7 = nn.Sequential(
   nn.MaxPool2d(2)
```

```
# Plot Function
# Main Execution
```

```
# Initialize model
# Train the model
```



```
In [37]: # Function to evaluate the model on the test set

def evaluate_model(model, test_loader, criterion):
    model.eval() # Set the model to evaluation mode
```

```
Out[37]:
```

```
In [ ]:
        students_ids = "321817405_208912675"
        #model = DogEmotionCNN()
```

4. Discussion

The training loss steadily decreases, showing effective learning, while the validation loss generally declines with some fluctuations, stabilizing around epoch 60. Training accuracy consistently improves, and validation accuracy follows a similar trend, though slightly lower and more variable. Both metrics plateau toward the end, with minimal overfitting evident as the validation performance closely matches the training performance. This indicates good generalization of the model.

II. Analyzing a Pre-trained CNN (Filters) (10pt)

In this part, you are going to analyze a (large) pre-trained model. Pre-trained models are quite popular these days, as big companies can train really large models on large datasets (something that personal users can't do as they lack the sufficient hardware). These pre-trained models can be used to fine-tune on other/small datasets or used as components in other tasks (like using a pre-trained classifier for object detection).

All pre-trained models expect input images normalized in the same way, i.e. mini-batches of 3-channel RGB images of shape (3 x H x W), where H and W are expected to be at least 224. The images have to be loaded in to a range of [0, 1] and then normalized using mean = [0.485, 0.456, 0.406] and std = [0.229, 0.224, 0.225].

You can use the following transform to normalize:

```
normalize = transforms.Normalize(mean=[0.485, 0.456, 0.406], std= [0.229, 0.224, 0.225]) Read more here
```

- Load a pre-trained VGG16 with PyTorch using torchvision.models.vgg16(pretrained=True, progress=True, **kwargs) (read more here).
 Don't forget to use the model in evaluation mode (model.eval()).
- 2. Load the images in the hw1_data/birds folder and display them.
- 3. Pre-process the images to fit VGG16's architecture. What steps did you take?
- 4. Feed the images (forward pass) to the model. What are the outputs?
- 5. Choose an image of a dog in the hw1_data/dogs folder, display it and feed it to network. What are the outputs?
- 6. For the first 3 filters in the first layer of VGG16, plot their response (their output) for the image from section 5. Explain what do you see.

```
In [151...
```

```
import os
import torch
from torchvision import models, transforms
from PIL import Image
import matplotlib.pyplot as plt
import json

# Step 1: Load the pre-trained VGG16 model
device = torch.device("cuda" if torch.cuda.is_available() else "cpu") #
Check if CUDA is available
```

```
# Step 3: Load and display the images
images_folder = "hw1_data/birds" # Assuming images are in the "data"
folder
# Step 4: Pre-process the images
# Step 5: Process and predict each image
```

```
# Get the class label using the class index
predicted_class_label = class_names[predicted_class.item()]

# Display the image and predicted class
plt.imshow(img)
plt.show()

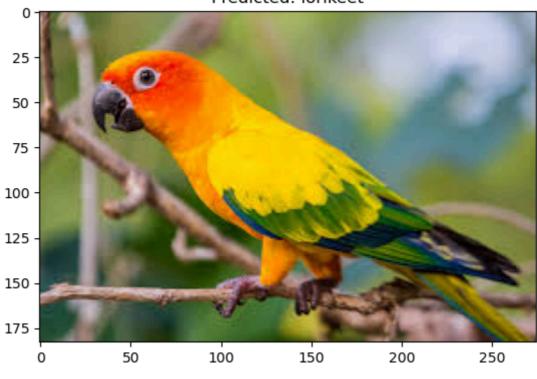
# Print the predicted class label for each image
print(f"Predicted label for {img_name}:
{predicted_class_label}")
```



Predicted label for bird 0.jpg: hummingbird

175 -

Predicted: lorikeet



Predicted label for bird_1.jpg: lorikeet

3. Steps that were taken:

- 1. Resize the images to 224x224 (expected input size for VGG16).
- 2. Normalize the images using the given mean and standard deviation.
- 3. Convert the images to tensors.

5:

```
In [165...
```

```
import os
import torch
from torchvision import models, transforms
from PIL import Image
import matplotlib.pyplot as plt
import json

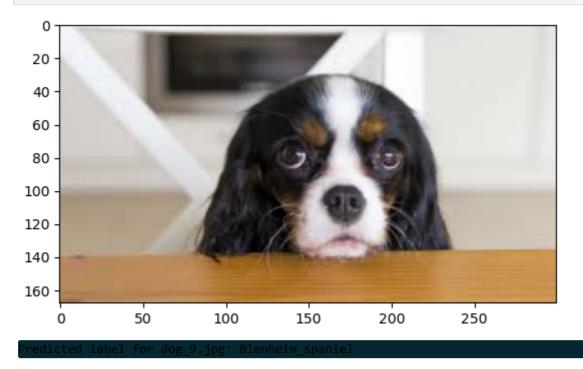
# Step 1: Load the pre-trained VGG16 model
vgg16 = models.vgg16(pretrained=True).to(device) # Move the model to
the appropriate device
vgg16.eval() # Set the model to evaluation mode

# Step 2: Load ImageNet class labels from the json file
LABELS_PATH = "hw1_data/imagenet_class_index.json"

with open(LABELS_PATH, 'r') as f:
    class_idx = json.load(f)
```

```
# Map class indices to their labels
class_names = {int(key): value[1] for key, value in class_idx.items()}
images_folder = "hw1_data/dogs" # Assuming images are in the "data"
# Step 4: Pre-process the images
   img_name = image_names[0] # Only process the first image
   img = Image.open(img_path).convert("RGB")
dimension and move to device
   # Perform forward pass
```

```
# Print the predicted class label for the first image
print(f"Predicted label for {img_name}: {predicted_class_label}")
```



6:

```
In [169...
           mport torch
          Check if CUDA is available
          LABELS_PATH = "hw1_data/imagenet_class_index.json"
          # Map class indices to their labels
```

```
images_folder = "hw1_data/dogs" # Assuming images are in the "data"
folder
# Step 4: Pre-process the image
    img_path = os.path.join(images_folder, img_name)
    img = Image.open(img_path).convert("RGB")
dimension and move to device
Layer
first layer of VGG16)
```

```
# Extract the first 3 feature maps
for i in range(3):
    feature_map = feature_maps[0, i].cpu().numpy() # Get the ith
feature map (channel)

    plt.subplot(1, 3, i+1)
    plt.imshow(feature_map, cmap='gray')
    plt.title(f"Filter {i+1}")
    plt.axis('off')

plt.show()

# Print the predicted class label for the first image
    output = vgg16(img_tensor)
    _, predicted_class = torch.max(output, 1)
    predicted_class_label = class_names[predicted_class.item()]
```

Filter 1



Filter 2



Filter 3

