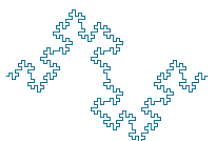


High-Throughput Sequencing Course

Gene-Set Analysis

Biostatistics and Bioinformatics



Summer 2018



Section 1

Introduction

WHAT IS GENE SET ANALYSIS?

Many names for gene set analysis:

- ▶ Pathway analysis
- ▶ Gene set enrichment analysis
- ▶ Go-term analysis
- ▶ Gene list enrichment analysis

SINGLE SNP/GENE ANALYSIS

- ▶ SNP/Gene: X_1, X_2, \dots, X_p
- ▶ Phenotype Y
- ▶ Study the relationship between X_i and Y
- ▶

$$Y = \beta_{i0} + \beta_{i1}X_i + Z_1$$

or

$$\text{logit}\{P(Y = 1)\} = \beta_{i0} + \beta_{i1}X_i$$

or other GLMs.

- ▶ Obtain the p -value P_i corresponding to the significance level of β_{i1} .
- ▶ Threshold p -values.

TYPICAL RESULTS OF GWAS ANALYSIS (SINGLE SNP APPROACH)

SNP	Nearest Gene	CA	European Americans ($N_{\text{obs}}=24,258$)			African Americans ($N_{\text{obs}}=9,846$)			American Indians ($N_{\text{obs}}=4,197$)			Mexican Americans and Hispanics ($N_{\text{obs}}=3,973$)			G
			CAF	β (SE)	P-value	CAF	β (SE)	P-value	CAF	β (SE)	P-value	CAF	β (SE)	P-value	
r1748195	ANGPTL3	C	0.66	0.03 (0.01)	1.93E-07	0.35	0.01 (0.01)	0.19	0.61	0.16 (0.07)	2.44E-02	0.60	0.04 (0.01)	1.17E-02	N
r1260326	GCCR	T	0.42	0.05 (0.01)	6.44E-13	0.16	0.05 (0.02)	9.98E-04	0.28	0.15 (0.09)	8.52E-02	0.33	0.06 (0.02)	1.97E-04	N
r780094	GCCR	A	0.40	0.06 (0.01)	1.69E-12	0.18	0.02 (0.01)	2.91E-02	0.25	0.04 (0.01)	3.23E-03	0.33	0.06 (0.02)	1.13E-03	Y
r17745738	MURPL	T	0.12	-0.07 (0.01)	5.71E-24	0.09	-0.03 (0.01)	2.53E-02	0.08	-0.07 (0.02)	2.20E-04	0.07	-0.09 (0.03)	7.40E-04	Y
r128	LPL	C	0.90	0.09 (0.01)	4.14E-39	0.93	0.08 (0.02)	2.62E-08	0.97	0.09 (0.03)	4.83E-03	0.93	0.09 (0.03)	6.31E-04	Y
r2197089	LPL	T	0.55	-0.03 (0.01)	4.97E-15	0.78	-0.01 (0.01)	7.45E-02	0.41	-0.05 (0.01)	2.57E-06	0.48	-0.05 (0.01)	4.01E-04	N
r2954029	TRMT1	A	0.54	0.05 (0.01)	1.13E-04	0.68	-0.01 (0.02)	0.46	-	-	-	0.62	0.06 (0.02)	9.28E-04	N
r174547	FADS1	T	0.66	-0.03 (0.01)	3.62E-10	0.91	-0.05 (0.01)	3.73E-04	0.21	-0.06 (0.02)	1.10E-04	0.39	-0.05 (0.02)	1.51E-03	Y
r28927680	APOA1/C3/A4/A5 gene cluster	C	0.93	-0.12 (0.01)	2.88E-38	0.84	-0.001 (0.01)	0.95	0.83	-0.13 (0.01)	6.33E-19	0.86	-0.08 (0.02)	2.15E-05	N
r964184	APOA1/C3/A4/A5 gene cluster	G	0.86	-0.14 (0.01)	1.91E-59	0.80	-0.02 (0.01)	4.87E-02	0.78	-0.17 (0.07)	1.43E-02	0.72	-0.14 (0.02)	1.04E-19	Y
r13155506	APOA1/C3/A4/A5 gene cluster	C	0.06	0.13 (0.01)	2.59E-33	0.06	0.11 (0.02)	2.08E-10	0.17	0.13 (0.01)	4.28E-20	0.14	0.13 (0.02)	3.08E-08	Y
r4775041	LPC	C	0.29	0.01 (0.01)	3.15E-02	0.14	0.03 (0.01)	4.29E-03	0.21	0.02 (0.01)	5.15E-02	0.18	0.01 (0.02)	0.58	N
r16996148	CLP3/PBANK1/NCAN	T	0.08	-0.04 (0.01)	3.91E-05	0.15	-0.001 (0.01)	0.77	0.04	-0.07 (0.03)	8.86E-03	0.06	-0.06 (0.03)	2.69E-02	N
r7679	PLTP	T	0.82	-0.02 (0.01)	2.84E-02	0.96	-0.01 (0.02)	0.61	0.94	-2.0E-03 (0.02)	0.93	0.89	-0.03 (0.03)	0.31	N

Coded allele (CA): coded allele frequency (CAF); beta coefficient (β); standard error (SE); data not available (-); generalized (G); yes (Y); no (N). Generalization is defined here as a significant association ($p < 0.05$) and a similar direction of effect (β) compared with European Americans for the same test of association, across all racial/ethnic populations.
doi:10.1371/journal.pgen.1002138.t004

Figure: An example from Dumitrescu et al. (2011).

TYPICAL RESULTS OF GWAS ANALYSIS (SINGLE SNP APPROACH)

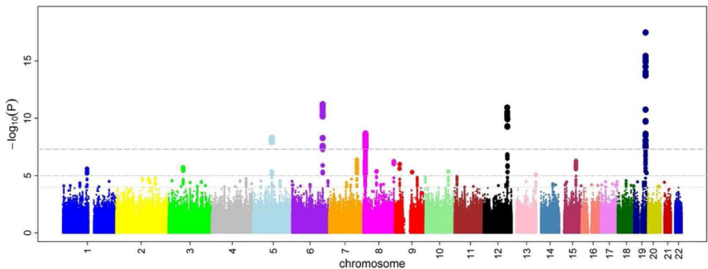


Figure: An example from Gibson (2010).

GENE SET ANALYSIS (GSA)

- ▶ An analysis to investigate the relationship between a disease phenotype and a set of genes on the basis of shared biological or functional properties.
- ▶ Gene set: a set of genes
 - ▶ Genes involved in a pathway
 - ▶ Genes corresponding to a Gene Ontology term
 - ▶ Genes mentioned in a paper to have certain similarities

GOAL OF GSA

Goal: give **one** number to measure the significance of a **gene set** as a whole.

- ▶ Are many genes in the pathway differentially expressed (up-regulated/down-regulated)?
- ▶ What is the probability of observing these changes just by chance?

WHY GSA?

Single SNP approach: List top 20-50 most-significant SNPs and their neighboring genes.

GSA approach: List the pathways that have genes in the pathway have consistent trend to affect the phenotype.

WHY GSA?

Single SNP approach: List top 20-50 most-significant SNPs and their neighboring genes.

- [Assumption 1](#): Single gene work solely to largely increase the disease susceptibility

GSA approach: List the pathways that have genes in the pathway have consistent trend to affect the phenotype.

- [Assumption 1](#): Multiple Genes in the same pathway work together to confer disease susceptibility.

WHY GSA?

Single SNP approach: List top 20-50 most-significant SNPs and their neighboring genes.

- [Assumption 1](#): Single gene work solely to largely increase the disease susceptibility
- [Assumption 2](#): The most associated gene is the best candidate for therapeutic intervention.

GSA approach: List the pathways that have genes in the pathway have consistent trend to affect the phenotype.

- [Assumption 1](#): Multiple Genes in the same pathway work together to confer disease susceptibility.
- [Assumption 2](#): Targeting susceptibility pathways have clinical implications for finding additional drug targets.

WHY GSA?

- Interpretation of genome-wide results
- Gene-sets are (typically) fewer than all the genes and have more descriptive names
- Difficult to manage a long list of significant genes
- Integrates external information into the analysis
- Less prone to false-positives on the gene-level
- Top genes might not be the interesting ones, several coordinated smaller changes
- Detect patterns that would be difficult to discern simply by manually going through, *e.g.*, the list of differentially expressed genes

Section 2

Statistical Issues

TWO TYPES OF NULLS

- Self-contained analysis: None of those genes in the gene set are associated with the phenotype.
- Competitive analysis: None of those genes in the gene set are associated with the phenotype.

TWO TYPES OF NULLS

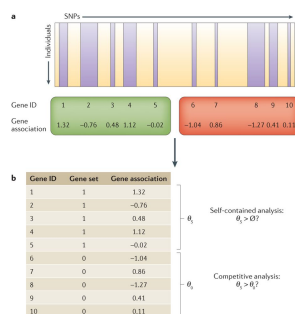
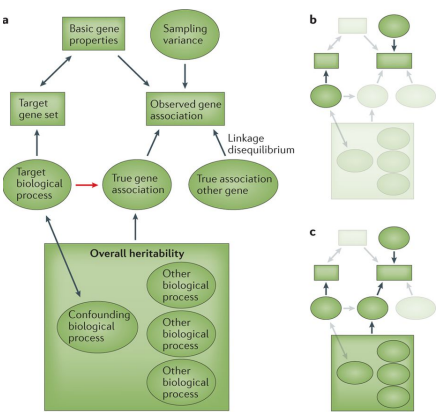


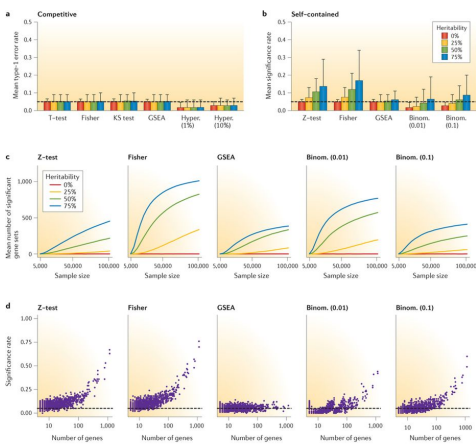
Figure: Schematic of the two-tier structures of GSA Leeuw et al. (2016).

UNDERLYING MECHANISM



Leeuw et al., 2016

SELF-CONTAINED TESTS INFLATE TYPE I ERROR



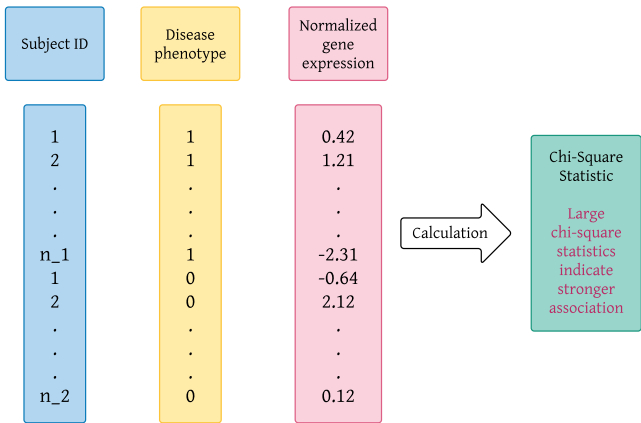
Section 3

Method: Gen-Gen/GSEA

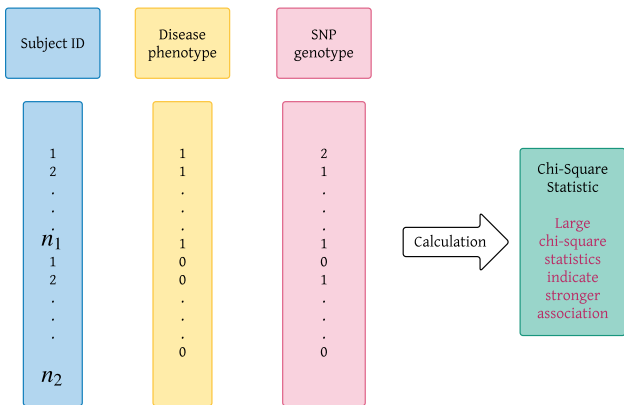
GEN-GEN/GSEA

- Gen-Gen: Kai Wang, Mingyao Li, and Maja Bucan (Dec. 2007). “Pathway-based approaches for analysis of genomewide association studies”. In: *Am J Hum Genet* 81.6, pp. 1278–83. DOI: 10.1086/522374
- GSEA: Aravind Subramanian et al. (Oct. 2005). “Gene set enrichment analysis: a knowledge-based approach for interpreting genome-wide expression profiles”. In: *Proc Natl Acad Sci U S A* 102.43, pp. 15545–50. DOI: 10.1073/pnas.0506580102

MICROARRAY DATA



SINGLE NUCLEOTIDE POLYMORPHISM DATA



SUMMARIZE SNP ASSOCIATE ON ONE GENE

- Map SNP V_i to gene j (\mathcal{G}_j) if the SNP is located within the gene or if the gene is the closest gene to the SNP.
- In total N genes.
- When one SNP is located within shared regions of two overlapping genes, the SNP is mapped to both genes.
- For each gene, assign the highest statistic value among all SNPs mapped to the gene as the statistic value of the gene, $r_j = \max_{v_i \in \mathcal{G}_j} t_i$.

ENRICHMENT SCORE

- A given gene set \mathcal{S} , $\text{Card}(\mathcal{S}) = N_H$.
- Calculate association chi-square statistics r_j , $j = 1, \dots, N$.
- **The larger the r_j is, the more associated gene O_j with the phenotype.**
- Rank the association statistics from **the largest to the smallest**, denoted by

$$r_{(1)} \geq r_{(2)} \geq \dots \geq r_{(N)}.$$

- Calculate a weighted Kolmogrov-Smirnov like running sum statistic

$$\text{ES}(\mathcal{S}) = \max_{1 \leq j \leq N} \left\{ \sum_{j^* \in \mathcal{S}, j^* \leq j} \frac{|r_{(j^*)}|^p}{N_R} - \sum_{j^* \notin \mathcal{S}, j^* \leq j} \frac{1}{N - N_H} \right\},$$

$$\text{where } N_R = \sum_{j^* \in \mathcal{S}} |r_{(j^*)}|^p.$$

ENRICHMENT SCORE

Weighted Kolmogrov-Smirnov like running sum statistic

$$\text{ES}(\mathcal{S}) = \max_{1 \leq j \leq N} \left\{ \sum_{j^* \in \mathcal{S}, j^* \leq j} \frac{|r_{(j^*)}|^p}{N_R} - \sum_{j^* \notin \mathcal{S}, j^* \leq j} \frac{1}{N - N_H} \right\},$$

where $N_R = \sum_{j^* \in \mathcal{S}} |r_{(j^*)}|^p$.

- p is a parameter that gives higher weight to genes with extreme statistics.
- Common choice $p = 1$.
- $p = 0$ leads to regular KS statistic, usually not as powerful as $p = 1$.

NORMALIZED ENRICHMENT SCORE

- ▶ The enrichment score $ES(\mathcal{S})$ relies on the maximum statistic, so that a larger gene set \mathcal{S} tends to produce larger $ES(\mathcal{S})$.
- ▶ Two-step normalization procedure:
 1. Permute the phenotype label of all samples
 2. During each permutation π , repeat the calculation of the enrichment score $ES(\mathcal{S}, \pi)$.
- ▶ Then

$$NES(\mathcal{S}) = \frac{ES(\mathcal{S}) - \text{mean}\{ES(\mathcal{S}, \pi)\}}{\text{sd}\{ES(\mathcal{S}, \pi)\}}$$

- ▶ The NES adjusts for different sizes of genes.
- ▶ THE NES preserves correlations between SNPs on the same gene.

TYPE I ERROR RATE

H_l : Gene set \mathcal{S}_l is not associated with the phenotype,
 $l = 1, \dots, m$.

	Claim significant	Claim non-significant	Total
True nulls	N_{00}	N_{01}	m_0
False nulls	N_{10}	N_{11}	m_1
Total	R	$m - R$	m

- ▶ $FDR = E(N_{00}/(R \vee 1))$.
- ▶ $FWER = P(N_{00} \geq 1)$.

CONTROL FDR

- ▶ NES^* : the normalized enrichment score in the observed data
- ▶

$$\widehat{FDR} = \frac{\% \text{ of all } (\mathcal{S}, \pi) \text{ with } NES(\mathcal{S}, \pi) \geq NES^*}{\% \text{ of observed } \mathcal{S} \text{ with } NES(\mathcal{S}) \geq NES^*}.$$

- ▶ Rationale
 - ▶ $FDR = E\{N_{00}/(R \vee 1)\}$.
 - ▶ N_{00}/m : Estimated by % of all (\mathcal{S}, π) with $NES(\mathcal{S}, \pi) \geq NES^*$.
 - ▶ R/m : Estimated by % of observed \mathcal{S} with $NES(\mathcal{S}) \geq NES^*$.
- ▶ Larger NES^* corresponds to smaller \widehat{FDR} .
- ▶ If $\widehat{FDR} \leq \alpha$, claim the corresponding gene set significant.

CONTROL FWER

- ▶ NES^* : the normalized enrichment score in the observed data
- ▶ $\widehat{FWER} = \%$ of all π with the highest $NES(\mathcal{S}, \pi) \geq NES^*$.
- ▶ Rationale:
 - ▶ $FWER = P(N_{00} \geq 1) = E\{I(N_{00} \geq 1)\}$.
 - ▶ Each permutation π can be viewed as a realization of the event. If the highest $NES(\mathcal{S}, \pi) \geq NES^*$, then there is a false rejection.
- ▶ Larger NES^* corresponds to smaller \widehat{FWER} .
- ▶ If $\widehat{FWER} \leq \alpha$, claim the corresponding gene set significant.

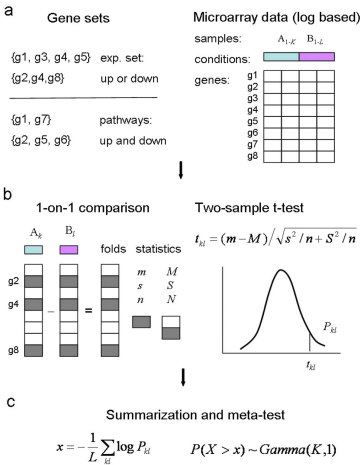
Section 4

Method: GAGE

GAGE

- ▶ **Luo2009GAGE**
- ▶ Gene expression data: RNA-Seq or Microarray

GAGE METHOD OVERVIEW



SETTING

- ▶ Gene: $i \in \{1, \dots, N\}$
- ▶ Condition/Phenotype: $s \in 0, 1$
 - ▶ Paired (1-on-1): *e.g.*, one condition *vs.* another condition:
 - ▶ Unpaired (grp-on-grp): *e.g.*, one phenotype *vs.* another phenotype:
- ▶ Subject:
 - ▶ Paired: $k \in \{1, \dots, K\}$
 - ▶ Unpaired: $k \in \{1, \dots, K_1\}$ for cases and $k \in \{1, \dots, K_0\}$ for controls.
- ▶ Gene expression:

$$G_{s,k,i} = \begin{cases} \text{Transcription level of gene } i & \text{Microarray} \\ \text{Read counts of gene } i / \text{Total counts} & \text{RNA-Seq} \end{cases}$$

log₂ FOLD CHANGE

- ▶ Compare the gene expressions between two conditions or two phenotypes
 - ▶ Paired (1-on-1): $X_{k,i} = G_{1,k,i} / G_{0,k,i}$
 - ▶ Unpaired (grp-on-grp): $X_i = \bar{G}_{1,i} / \bar{G}_{0,i}$
 - ▶ Efficient but not recommended (1-on-grp):
 $X_{k,i} = G_{1,k,i} / \bar{G}_{0,i}$

GENE SET AND T-STATISTIC

- ▶ Gene set of interest \mathcal{S}
- ▶ mean fold change: $m = \text{mean}_{i \in \mathcal{S}}(X_i)$ (gene set) *vs.*
 $M = \text{mean}_{i \in \{1, \dots, N\}}(X_i)$ (all genes)
- ▶ standard deviation folde change: $s = \text{sd}_{i \in \mathcal{S}}(X_i)$ (gene set)
vs. $S = \text{sd}_{i \in \{1, \dots, N\}}(X_i)$ (all genes)
- ▶ number of genes: n (gene set) *vs.* N (all genes)
- ▶ T-statistic:

$$T = (m - M) / \sqrt{s^2/n + S^2/\textcolor{red}{n}}$$

Remark:

- ▶ This is a two sample t-test between the interesting gene set containing n genes and a **virtual random set of the same size** derived from the background.
- ▶ Subscript k is left out for simplicity. We will discuss 1-on-1 setting (with subscript k) later.

P-VALUE

- ▶ Degree of freedom of T under the null

$$\text{df} = (n - 1) \frac{s^2 + S^2}{s^4 + S^4}.$$

- ▶ P -value:
 - ▶ Two sided: pathway set (genes may be het erogeneously regulated in either direction)
 - ▶ One sided: experimental set (genes are regulated in the same direction)
- ▶ Alternative choice of T : rank-based test (Wilcoxon Mann-Whitney test)

SUMMARIZING P-VALUES

Recall that for 1-on-1 (paired) setting, the P -value for gene set \mathcal{S} and subject k is $P_k(\mathcal{S})$.

$$X(\mathcal{S}) = \sum_k \log P_k(\mathcal{S}).$$

Under the null, $P_k(\mathcal{S})$ independently follows $\text{Unif}(0, 1)$, and then $X(\mathcal{S})$ follows $\text{Gamma}(K, 1)$.


CONTROLLING FDR


If multiple gene sets are of interest, multiple testing methods are applied to control FDR.


- fdrtool: Korbinian Strimmer (July 2008). “A unified approach to false discovery rate estimation”. In: *BMC Bioinformatics* 9, p. 303. DOI: 10.1186/1471-2105-9-303
- Benjamini and Hochberg (BH) procedure: Y. Benjamini and Y. Hochberg (1995). “Controlling the False Discovery Rate: A Practical and Powerful Approach to Multiple Testing”. In: *Journal of the Royal Statistical Society. Series B (Methodological)* 57.1, pp. 289–300. ISSN: 00359246. URL: <http://www.jstor.org/stable/2346101>


Section 5




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Introduction	Statistical Issues	Method: Gen-Gen/GSEA	Method: GAGE	References
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<p>10.1038/nrg.2016.29. URL: http://dx.doi.org/10.1038/nrg.2016.29.</p> <p> Strimmer, Korbinián (July 2008). “A unified approach to false discovery rate estimation”. In: <i>BMC Bioinformatics</i> 9, p. 303. DOI: 10.1186/1471-2105-9-303.</p> <p> Subramanian, Aravind et al. (Oct. 2005). “Gene set enrichment analysis: a knowledge-based approach for interpreting genome-wide expression profiles”. In: <i>Proc Natl Acad Sci U S A</i> 102.43, pp. 15545–50. DOI: 10.1073/pnas.0506580102.</p> <p> Wang, Kai, Mingyao Li, and Maja Bucan (Dec. 2007). “Pathway-based approaches for analysis of genomewide association studies”. In: <i>Am J Hum Genet</i> 81.6, pp. 1278–83. DOI: 10.1086/522374.</p>				