



$$\textcircled{1} \quad y = \sin(\theta_1) + \sin(\theta_1 + \theta_2)$$

$$\textcircled{2} \quad x = \cos \theta_1 + \cos(\theta_1 + \theta_2)$$

$$x^2 + y^2 = 2 + 2(\cos(\theta_1 + \theta_2) \cos \theta_1 + \sin(\theta_1 + \theta_2) \sin \theta_1)$$

$$\boxed{\frac{x^2 + y^2 - 2}{2} = \cos \theta_2} \quad \textcircled{3}$$

Simplifying &  
Substituting in eqn (2)

$$x = \frac{2 \cos 2\theta_1 + \theta_2}{2} \cos \theta_2 / 2$$

$$\cos^{-1}\left(\frac{x}{2 \cos \theta_2}\right) = \frac{2\theta_1 + \theta_2}{2} \rightarrow \theta_1 = \cos^{-1} \frac{x}{2 \cos \theta_2} - \frac{\theta_2}{2}$$

$$\boxed{\theta_1 = \cos^{-1} \frac{x}{2 \cos \theta_2} - \frac{\theta_2}{2}}$$

Substitute  $\theta_1$  from (3)