## Central Limit Theorem

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The Central Limit Theorem (CLT) states that given a sufficiently large sample size from a population with finite variance, the mean of all samples from the same population will be approximately equal to the mean of the population. The samples means will follow an approximate normal distribution pattern centered at the population mean and the variance being approximately equal to the variance of the population divided by each sample's size.

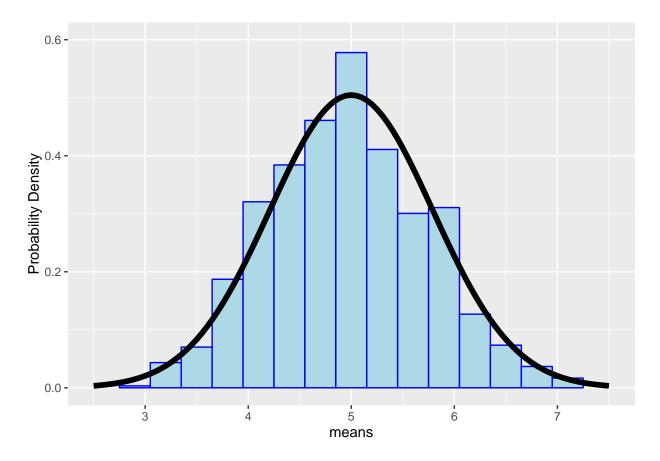
In this part I investigate the exponential distribution in R and compare it with the CLT. The exponential distribution can be simulated in R with rexp(n, lambda) where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda.

Here, I investigate the distribution of averages of 40 exponentials and do a thousand simulations for lambda=0.2:

According to the CLT, the samples means are distributed approximately normally. I create a function norm\_approx to compare the distribution of the means with:

```
norm_approx <- function(x,mean,sd,n){
    dnorm(x,mean = mean,sd=sd/sqrt(n))
}</pre>
```

Here, I plot the normalized histogram of the means and compare it with norm\_approx:



Samples means and their standard deviation are

c(mean(means),sd(means))

## ## [1] 4.9719720 0.7847246

These values are in good agreement with the mean and the standard deviation of the  $norm\_approx$ , namely c(1/lambda,1/lambda/sqrt(40))

## [1] 5.0000000 0.7905694