

# ADVANCED METHODS IN NLP

## EXERCISE #2 SOLUTION

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### Question 1

- (b) Our method for grid searching works in the following manner: We first define our grid resolution and halting condition to be 0.1 and 1 respectively. Then, we run through all combinations of  $\lambda_1, \lambda_2, \lambda_3$  within the resolution intervals and afterwards divide our resolution by 2. When perplexity difference between searches reaches less than halting condition, we stop the grid search. Our results for resolution = 0.1 are:

$\lambda_2 \backslash \lambda_1$	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0	189.6	104.2	87.5	79.0	74.2	71.7	71.1	72.7	77.4	90.5
0.1	115.7	82.6	71.6	65.4	61.6	59.4	58.5	59.1	62.1	
0.2	94.7	72.7	64.3	59.5	56.6	54.9	54.6	56.3		
0.3	82.7	66.0	59.4	55.6	53.3	52.4	53.3			
0.4	74.6	61.3	55.9	52.9	51.4	51.8				
0.5	68.9	57.9	53.5	51.2	51.0					
0.6	64.6	55.3	51.9	51.1						
0.7	61.6	53.8	51.9							
0.8	59.6	53.7								
0.9	59.3									

When narrowing down to resolution = 0.5 our run meets the halting condition at:  $\lambda_1 = 0.35, \lambda_2 = 0.5, \lambda_3 = 0.15$  with **perplexity = 50.86**

## Question 2

(a)

$$\begin{aligned}
 \text{softmax}(\theta)_i &= \frac{\exp(\theta_i)}{\sum_j \exp(\theta_j)} \\
 \text{CE}(y, \hat{y}) &= - \sum y_i \log \hat{y}_i \quad \underbrace{\quad}_{\text{y is one-hot vector}} \quad \equiv \quad -1 \cdot \log(\hat{y}_i) \\
 &= -\log \left( \frac{\exp(\theta_i)}{\sum_j \exp(\theta_j)} \right) \\
 &= -\theta_i + \log \left( \sum_j \exp(\theta_j) \right) \\
 \left( \frac{\partial \text{CE}(y, \hat{y})}{\partial \theta} \right)_j &= \frac{\partial \text{CE}(y, \hat{y})}{\partial \theta_j}
 \end{aligned}$$

Scalar-wise:

$$\begin{aligned}
 \frac{\partial \text{CE}(y, \hat{y})}{\partial \theta_{j \neq i}} &= \frac{1 \cdot \exp(\theta_j)}{\sum_k \exp(\theta_k)} \\
 \frac{\partial \text{CE}(y, \hat{y})}{\partial \theta_i} &= -1 + \frac{1 \cdot \exp(\theta_i)}{\sum_k \exp(\theta_k)}
 \end{aligned}$$

Therefore, by deriving vector-wise we get:

$$\frac{\partial \text{CE}(y, \hat{y})}{\partial \theta} = \hat{y} - y$$

(b)

$$\begin{aligned}
 J &= \text{CE}(y, \hat{y}) \\
 \theta &= hW_2 + b_2 \\
 h &= \sigma(xW_1 + b_1) \\
 \frac{\partial J}{\partial \theta} &\underbrace{=}_{\text{section a}} \hat{y} - y \\
 \frac{\partial \theta}{\partial h} &= W_2 \\
 \frac{\partial h}{\partial x} &= \sigma'(xW_1 + b_1) \cdot W_1
 \end{aligned}$$

Now, by applying the chain rule we get:

$$\begin{aligned}\frac{\partial J}{\partial x} &= \frac{\partial J}{\partial \theta} \cdot \frac{\partial \theta}{\partial h} \cdot \frac{\partial h}{\partial x} \\ &= (\hat{y} - y) W_2^T \sigma'(x W_1 + b_1) \cdot W_1^T\end{aligned}$$

(d) Results:

#params: 104550

#train examples: 1118296

dev perplexity : **112.967665327**