

<sup>1</sup> Using balanced acceptance sampling as a master  
<sup>2</sup> sample for environmental surveys

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## Abstract

Well designed environmental monitoring programmes for management organisations are important for evidence based decision making. However, many environmental problems are not single agency, single spatial scale issues. A master sample can be used to coordinate and scale monitoring designs to ensure consistency in information gathered and robustness of estimators at the different spatial scales. We propose using balanced acceptance sampling (BAS) to generate a master sample. Using Bas as a master sample is flexible, effective and improves on other methods previously explored. Some practical aspects of the design are addressed such as inclusion of legacy monitoring programmes, stratification, unequal probability sampling, rotating panel designs, and regional intensification. We explore the impact of including legacy monitoring through a simulation study. An example master sample is presented for environmental monitoring in New Zealand.

<sup>23</sup>      **Keywords:** Master Sample, Spatial Balance, Environmental Monitoring,  
<sup>24</sup>      Legacy Monitoring.

## <sup>25</sup>      1 Introduction

<sup>26</sup>      Conservation management groups rely on the results of environmental moni-  
<sup>27</sup>      toring to answer questions about the success of their programmes. Often this  
<sup>28</sup>      monitoring is not properly designed and fails to provide meaningful informa-  
<sup>29</sup>      tion to management (Legg & Nagy 2006; Nichols & Williams 2006; Field *et al.*  
<sup>30</sup>      2007). Extrapolating from these studies to answer larger scale questions can in-  
<sup>31</sup>      troduce bias into the estimates (Peterson *et al.* 1999). Material exists to assist  
<sup>32</sup>      in creating a well designed monitoring programme (Gitzzen 2012; Reynolds *et al.*  
<sup>33</sup>      2016; Vos *et al.* 2000) but coordination may be required to ensure it is carried  
<sup>34</sup>      out properly and that standard monitoring methods are applied. This requires  
<sup>35</sup>      collaboration on a set of standard best practices for field protocols, for example,  
<sup>36</sup>      the Department of Conservation's (DOC's) monitoring toolbox (Department of  
<sup>37</sup>      Conservation 2016). Once methods are consistent effort can be coordinated to  
<sup>38</sup>      ensure the locations sampled are representative of their target level of infer-  
<sup>39</sup>      ence and resources can be shared when objectives are. By agencies working  
<sup>40</sup>      together and through a well set out design process the chances of monitoring  
<sup>41</sup>      being successful are higher. Concerns about the extrapolating estimates is also  
<sup>42</sup>      reduced.

<sup>43</sup>      One way to coordinate monitoring effort is to develop a master sample; a

44 set of points that can be sub-sampled for different monitoring activities. This  
45 idea has been around for a while (King 1945) but only recently has been intro-  
46 duced to environmental monitoring (Larsen *et al.* 2008; Theobald 2016) with  
47 implementation in the Pacific Northwest of the United States. Having different  
48 studies draw samples from the master sample has the benefit of collaborating  
49 between groups to reduce effort as well as consistent design when making es-  
50 timates using data from multiple sources. Similar to providing standard field  
51 methods, the master sample provides standardised locations for sampling that  
52 ensures objective unbiased estimation of the population parameters of interest.  
53 This coordination reduces convenience or judgement sampling and helps requires  
54 the user to define the objectives and sample frame clearly before gaining access  
55 to the sample units. There are many ways to generate effective samples which  
56 could be used to coordinate monitoring. A simple random sample is unbiased  
57 but is less efficient than spatially balanced designs in the presence of spatial  
58 autocorrelation (Grafström & Lundström 2013). A design is spatially balanced  
59 if the sample is well-spread over the population — a sample with few clumps  
60 and voids. A systematic sample can be considered near perfect spatial balance  
61 but is less flexible to changes in sample size making it a poor choice.

62 Spatially balanced sampling designs are commonly used for sampling nat-  
63 ural resources and a variety of designs have been proposed. Stevens & Olsen  
64 (2004) introduced Generalized Random Tessellation Stratified (GRTS) design,  
65 a spatially balanced design that is frequently used in environmental monitoring.  
66 GRTS hierarchically orders a population using a base four numbering scheme

and then selects a systematic sample from the ordered population. Another spatially balanced design is the Local Pivotal Method (LPM) (Grafström *et al.* 2012). LPM iteratively updates each sampling unit's inclusion probability in a way that makes it very unlikely to include neighbouring units in a sample. Once  $n$  units have an inclusion probability of one, the sample is released. Although the spatial balance of LPM is better than GRTS, it is computationally prohibitive on large populations. For large populations, Grafström *et al.* (2014) introduced a new rapid implementation of LPM, called suboptimal LPM. LPM has better spatial balance, but suboptimal LPM is computationally feasible on large populations.

GRTS has been used to generate environmental monitoring master samples (Larsen *et al.* 2008). The design is particularly useful for generating master samples because GRTS points are ordered using a reverse hierarchical ordering strategy that ensures that all contiguous sub-samples are also spatially balanced (Stevens & Olsen 2004). By taking a large GRTS oversample, an ordered master sample can be obtained from which spatially balanced sub-samples can be drawn. However, once an oversample is chosen, it is not possible to generate additional points and this needs to be accounted for at the planning stage. Theobald (2016) also uses an adaptation of GRTS, Reversed Randomized Quadrant-Recursive Raster (RRQRR), implemented in ArcGIS software (Theobald *et al.* 2007) to coordinate monitoring effort. The authors' are not aware of an ordering strategy for the LPM methods and hence, it is not clear how these methods could be used for oversampling. Another spatially balanced

90 design is balanced acceptance sampling (BAS) (Robertson *et al.* 2013). It uses  
91 a quasi-random number sequence to generate spatially balanced points. Similar  
92 to GRTS, the outcome of the sequence is an ordered set of points such that any  
93 contiguous sub-sample maintains spatial balance. To generate a master sample  
94 with BAS, a random-start is chosen and after that an infinite set of points exist  
95 for the sample. Hence, the oversample size does not need to be specified for  
96 BAS.

97 The sampling method chosen should be flexible enough for a variety of users  
98 and study designs to be effective for coordination. Monitoring can take place  
99 on different spatial scales such as a national monitoring programme or a local  
100 one, investigating the impact of management action. When designing an in-  
101 dividual study, identifying heterogeneity and using stratification (Yoccoz *et al.*  
102 2001) or unequal probability sampling (Stevens 1997) can produce more precise  
103 estimates. The study may need a unique balance of status and trend estimation  
104 which can be done by defining panels that have different revisit schema (Skalski  
105 1990; McDonald 2003; Stevens & Olsen 1999). In all these cases the sub-samples  
106 used must be unbiased and representative.

107 The purpose of this paper is to develop a master sample for environmental  
108 monitoring with a focus on terrestrial sampling of an area frame in which all  
109 sub-samples have positive area. We investigate using BAS to generate a master  
110 sample; how the points will be generated and then used in a wide variety of ways.  
111 These include adapting to different spatial scales, stratification and unequal  
112 probability sampling, changes in boundaries or resources, revisit structure

113 (panel design), and how to include legacy monitoring programmes. We will then  
114 provide an example for how this could be applied at the regional and national  
115 level in New Zealand.

## 116 2 Methods

### 117 2.1 Point selection

Two-dimensional BAS points are drawn from a random-start Halton sequence  $\{\mathbf{x}_k\}_{k=1}^{\infty} \subset [0, 1]^2$ . The  $i$ th coordinate of each point in the sequence has an associated base  $b_i$ , with  $b_1 = 2$  and  $b_2 = 3$ . The  $i$ th coordinate of the  $k$ th point in this sequence is (Robertson et al. 2017)

$$x_k^{(i)} = \sum_{j=0}^{\infty} \left\{ \left\lfloor \frac{u_i + k}{b_i^j} \right\rfloor \bmod b_i \right\} \frac{1}{b_i^{j+1}},$$

118 where  $u_i$  is a random non-negative integer and  $\lfloor x \rfloor$  is the floor function — the  
119 largest integer that is less than or equal to  $x$ . The two-dimensional random-start  
120 Halton sequence is

$$\{\mathbf{x}_k\}_{k=1}^{\infty} = \left\{ x_k^{(1)}, x_k^{(2)} \right\}_{k=1}^{\infty}. \quad (1)$$

121 Setting  $u_1 = u_2 = 0$  gives the classical Halton sequence (Halton 1960). The  
122 points from eqn (1) are scaled to a minimal bounding box enclosing the study  
123 area and the first  $n$  scaled points in the study area define the BAS sample. The  
124 BAS points are kept in the same order as they appear in eqn (1) and will have  
125 good spatial spread over the study area. Furthermore, any continuous subset  
126 of the BAS sample will also have good spatial spread (Robertson et al. 2017).

127 Figure 1 shows an example of how this sequence creates spread by systematically  
128 choosing between boxes generated by the choice of the co-prime bases.

129 The random integer vector in the sequence  $\mathbf{u} = (u_1, u_2) \in [0, 10^7]^2$  is chosen  
130 so that  $\mathbf{x}_1$  falls within the sample area (Robertson *et al.* 2017). This gives  
131  $O(\lambda 10^{14})$  possible BAS samples of size  $n$ , where  $\lambda$  is the fraction of the bounding  
132 box occupied by the study area. By ensuring the random start comes from a  
133 large set of integers, the BAS points are uniformly distributed (Robertson *et al.*  
134 2013). Once the random-start is selected an infinite number of BAS points exist  
135 over the study which constitutes the master sample. Higher dimensional points  
136 can be defined by using different co-prime bases for each additional dimension  
137 (e.g.  $b_3 = 5$  when sampling from a  $[0, 1]^3$ ).

## 138 2.2 Spatial Scales

139 The Master sample should work at different spatial scales to answer national,  
140 regional, and local objectives. Let  $A$  be a measurable subset of the study area  
141 for which the master sample is defined. Because the master sample  $\{\mathbf{x}_k\}_{k=1}^\infty$   
142 is uniformly distributed over  $[0, 1]^2$  (Wang & Hickernell 2000), there exists a  
143 subsequence  $\{\mathbf{z}_j\}_{j=1}^\infty \subset \{\mathbf{x}_k\}_{k=1}^\infty$  such that each  $\mathbf{z}_j \in A$ . Furthermore,  $\{\mathbf{z}_j\}_{j=1}^n$   
144 is a BAS sample of size  $n$  drawn from  $A$ , with its random start and bounding  
145 box defined by the master sample. Hence, BAS samples can be drawn from the  
146 master sample at any spatial scale within the study area of the master sample.

147 What this means is that a national sample can share locations with moni-  
148 toring at the local level. Let's say that nationally 1000 sites are generated, each

149 with a unique order. If a sample of a region is taken and by chance 10 of these  
150 sites are shared, then the first ten sites in the regional sample are monitored by  
151 the national programme.

### 152 2.3 Stratification and Unequal probability

153 Stratification with the master sample is essentially the same as taking a sub-  
154 sample for a specific measurable subset of the study area as described above.  
155 The  $i$ th stratum (measurable) has a subsequence  $\{\mathbf{z}_j\}_{j=1}^{\infty} \subset \{\mathbf{x}_k\}_{k=1}^{\infty}$  such that  
156 each  $\mathbf{z}_j$  is in the stratum. The BAS sample for the  $i$ th stratum is  $\{\mathbf{z}_j\}_{j=1}^{n_i}$ ,  
157 where  $n_i$  is the sample size required. Hence, each stratum has its own BAS  
158 sample with its random start and bounding box defined by the master sample.  
159 In practice, each strata has the number of points required by taking a subset of  
160 the master sample for that strata.

161 If unequal probability sampling is required, a third dimension is added to the  
162 bounding box. This extra dimension allows BAS to sample from an arbitrary  
163 inclusion density function  $\pi(\mathbf{x})$  using an acceptance/rejection sampling strategy  
164 (Robertson *et al.* 2013). Specifically, a point  $\mathbf{x}_k = (x_k^{(1)}, x_k^{(2)}, x_k^{(3)})$  is accepted  
165 if  $(x_k^{(1)}, x_k^{(2)})$  is in the study area and  $\pi(x_k^{(1)}, x_k^{(2)}) \leq \alpha x_k^{(3)}$ , where  $\alpha$  is a scaling  
166 factor to ensure  $\max_{\mathbf{x}} \pi(\mathbf{x}) = 1$ . The impact of this is that some of the master  
167 sample points in eqn (1) will be skipped. This changes the density of BAS points,  
168 where fewer points are drawn from areas where  $\pi(\mathbf{x})$  is low. The resulting sample  
169 will still maintain order of the master sample but be missing points that were  
170 rejected due to unequal probability sampling.

171 **2.4 Changing boundaries and resources**

172 For long-term monitoring programmes, the boundaries of study regions may  
173 change over time. This is easy to accommodate with the master sample, pro-  
174 vided the changes are within the initial bounding box. Let  $A$  be a measurable  
175 study area whose boundaries changed, defining a new measurable study area  $B$   
176 with  $A \cap B \neq \emptyset$ . If there are no sampled BAS points in  $A \cap B$ , points from the  
177 master sample are drawn to sample  $B$ . Otherwise, let  $\mathbf{x}_k$  be the sampled point  
178 in  $A \cap B$  with the largest index  $k$ . A BAS sample in  $B$ , that includes sampled  
179 points from  $A \cap B$ , is achieved if all master sample points that fall in  $B$  with  
180 indices less than  $k$  are sampled. If a smaller sample is desired in  $B$ , potentially  
181 due to a change in resources, then points with the larger indices in  $B$  are re-  
182 moved. In the same sense if more points are required then points can be added  
183 from the master sample in  $B$  until the new sample size is achieved. Ensuring  
184 that BAS samples are drawn from each study region means that spatial balance  
185 and good sampling properties are maintained. This is demonstrated in Figure  
186 2, where the region is expanded but resources are not. The highest index points  
187 from  $A \cap B$  are dropped for new points in  $\bar{A} \cap B$ , the additional region.

188 **2.5 Panel design**

189 In environmental surveys that are repeated through time some samples may be  
190 visited frequently and others potentially once. This can allow better estimation  
191 of status when only new samples are included during each session or trend where  
192 the same samples are visited more frequently (Urquhart & Kincaid 1999). A

193 panel is defined as all samples that have the same visitation schedule. The  
194 points within a panel as well as between panels must be representative and  
195 unbiased. A panel design is achieved using the master sample by choosing the  
196 subset of points  $\{\mathbf{z}_j\}_{j=1}^{\infty}$  that fall within the sample frame and then selecting in  
197 order points for each panel matched to how they will be sampled in time. Thus,  
198 for panel 1 with 10 points we have the sample  $\{\mathbf{z}_j\}_{j=1}^{10}$  and panel 2 with an  
199 additional 10 is  $\{\mathbf{z}_j\}_{j=11}^{20}$ . When establishing the sample each year, some points  
200 within the panel may not be able to be sampled. If this occurs, then those  
201 locations are not truly part of the sample frame and are removed from  $\{\mathbf{z}_j\}_{j=1}^{\infty}$ .  
202 In the example above, if a single point is removed from panel 1, then  $\{\mathbf{z}_{11}\}$   
203 is now actually  $\{\mathbf{z}_{10}\}$  and replaces the missing point in panel 1. By defining  
204 the panels this way the overall sample is still a BAS design as well each panel.  
205 Once a full rotation of all samples has been carried out, if additional points  
206 are needed, they are added from the unsampled points in the master sample  
207 in the order that they appear. Note, when this occurs each panel may not be  
208 a true BAS sample but as shown in the legacy plots simulation below, adding  
209 BAS points to an existing sample does not significantly impact estimation and  
210 the sample will still be equi-probable and give unbiased estimators. If budgets  
211 change, points should be removed by last in, first out. Table 1 shows an example  
212 panel design.

213 **2.6 Incorporating legacy monitoring**

214 A master sample is intended for coordinating large scale monitoring. Often,  
215 there is legacy monitoring that may already be well designed and this should  
216 be accommodated. We will consider two different types of monitoring: sim-  
217 ple random sampling (SRS) and random-start systematic sampling (SS). These  
218 monitoring approaches are equi-probable designs, where each sampling unit has  
219 an equal chance of being included in a sample, but differ in extremes of spatial  
220 balance. If the existing monitoring is insufficient then the master sample must  
221 be able to augment sampling in the area. BAS points can intensify the legacy  
222 points by generating them independently. For unbiased estimation inclusion  
223 probabilities need to be computed. For a population of  $N$  units, the inclusion  
224 probability of the  $i$ th unit is assumed to be  $\pi_i = (n_l + n_b)/N$  because both  
225 sets of units were selected using equal probable designs, where  $n_l$  and  $n_b$  denote  
226 the number of legacy and BAS units respectively. The approach keeps the de-  
227 sign and analysis simple but potentially loses the appearance of spatial balance.  
228 Another method is to alter the inclusion probabilities around the legacy plots  
229 before sampling to ensure that none of the augmented samples are close to the  
230 legacy plots but this is at the expense of complexity of design and analysis as  
231 shown in (Foster *et al.* 2017). If this approach is desired a BAS master sample  
232 can accommodate the change in inclusion probabilities which is described above.  
233 We will call the altered inclusion probability sample aBAS from here on out.

234 A simulation study was carried out to investigate the impact of choosing  
235 different methods to incorporate legacy monitoring. The sampling frame was

236 defined as  $100 \times 100$  raster in  $[0, 1]^2$ . The response value for each raster cell  
237 was defined as the integral of  $f(\mathbf{x})$  over the cell. Three different functions were  
238 estimated, a strong spatial trend (Robertson *et al.* 2013; Grafström *et al.* 2012),  
239 a peak function, and a bird (cyclical trend) function. Scenarios similar to Foster  
240 *et al.* 2017 using the program R (R Core Team 2015) were run. We assumed  
241 an arbitrary overall sample size of  $n = 60$ . Legacy plots ( $n_l \in 3, 4, \dots, 57$ ) were  
242 generated either as simple random samples (SRS) or random-start systematic  
243 samples (SS). More samples ( $n_b = 60 - n_l$ ) were then included using GRTS  
244 (Kincaid & Olsen 2016), BAS, and aBAS (Foster 2016). SRS were added to  
245 SS legacy plots as well. Each scenario was run 1000 times estimating the sam-  
246 ple mean. A detailed description of the simulation and functions used can be  
247 accessed in the supplementary material.

248 Balanced acceptance sampling generally has better spatial balance than  
249 GRTS (Robertson *et al.* 2013), aBAS has the appearance of better spatial bal-  
250 ance as the proportion of legacy plots increases when they are simple random  
251 samples (Foster *et al.* 2017). The results of the simulation can be seen in Figure  
252 3 and Tables 2 & 3. Based on these simulations, augmenting legacy monitoring  
253 with BAS or GRTS is reasonable. Altering inclusion probabilities does not seem  
254 necessary for augmenting a legacy sample. In fact, there are cases when this can  
255 be dangerous as seen by the aBAS spikes (high standard deviation) in Figure 3.  
256 This is because the legacy monitoring may happen to coincide with a particular  
257 trend in the population and forcing monitoring away from the legacy plots can  
258 be problematic. Spatially balanced unequal probability sampling is only use-

ful (i.e. reduces the variance of an estimator) if the inclusion probabilities are positively correlated with the response. We suggest that unequal probability sampling be only undertaken in response to information about the population being monitored and not legacy plots. However, there are practical constraints on sampling that might make it unpopular for monitoring sites to fall directly next to each other, which is possible in the described approach. This makes aBAS attractive in the field but we recommend using model based estimation and not design to control for the increased uncertainty using the method.

Estimation when including legacy plots is straightforward assuming the legacy monitoring has known inclusion probabilities. However, spatially balanced designs use a local neighbourhood variance (LNV) (Stevens & Olsen 2003) and as the proportion of legacy plots is increased the LNV underestimates true variance (Foster *et al.* 2017). If the legacy plots and the augmented sampling are considered two groups with sample size  $n_l$  and  $n_b$  ( $n_l + n_b = n$ ) respectively, then a weighted variance estimator for the sample mean  $\bar{y}$  would be

$$\hat{var}(\bar{y}) = \frac{n_l}{n} \times \hat{var}(\bar{y}_l) + \frac{n_b}{n} \times \hat{var}(\bar{y}_b). \quad (2)$$

Here  $\hat{var}(\bar{y}_l)$  is the estimated variance of a Horvitz-Thompson mean using the legacy points and  $var(\bar{y}_b)$  is the LNV estimated variance of the mean using BAS points. This corrects the underestimation of LNV and should be used any time there are four or more spatially balanced points as suggested in the spsurvey package in R (Kincaid & Olsen 2016) and three or more legacy points. Note that the weighted mean estimate remains unchanged as a result of equal

<sup>280</sup> probability sampling using either BAS or GRTS to augment legacy monitoring.

### <sup>281</sup> **3 Application: New Zealand terrestrial monitoring**

<sup>283</sup> There currently exists a national monitoring programme in New Zealand ad-  
<sup>284</sup> ministered jointly by the Ministry for the Environment (MFE) and Department  
<sup>285</sup> of Conservation (DOC) for the purpose of carbon monitoring on an 8-km sys-  
<sup>286</sup> tematic grid (Coomes *et al.* 2002). The Department of Conservation added  
<sup>287</sup> monitoring of birds, mammals and vegetation at  $\approx$  1400 locations falling within  
<sup>288</sup> public conservation land (PCL) with a  $[(1 - 4)^5]$  revisit scheme where a single  
<sup>289</sup> panel is measured each year (Tier 1 monitoring). The programme focusses on  
<sup>290</sup> status and long-term trend monitoring at the national scale. It is not able to  
<sup>291</sup> provide evidence of the success of management at a local scale or in response  
<sup>292</sup> to a particular action. However, for large parks (e.g. Fiordland National Park)  
<sup>293</sup> Tier 1 can provide estimates of park or region level ecological integrity.

<sup>294</sup> Ecosystems across the PCL have been identified as high priority and are  
<sup>295</sup> labelled Ecosystem Management Units (EMUs) in response to intermediate  
<sup>296</sup> outcome objective (IOO) 1.1 – “A full range of New Zealand’s ecosystems is  
<sup>297</sup> conserved to a healthy functioning state” (Department of Conservation 2013).

<sup>298</sup> These areas are of special interest and have a high level of investment through  
<sup>299</sup> management activity. To assess the management outcomes of IOO 1.1 and re-  
<sup>300</sup> port on success or adapt management for improvement, Tier 1 monitoring must

<sup>301</sup> be augmented within the EMU sites. For this purpose DOC requires a national  
<sup>302</sup> sample that incorporates the already existing systematic Tier 1 sample.

<sup>303</sup> A national sample of New Zealand using BAS can make up the master  
<sup>304</sup> sample, with the existing Tier 1 points included. For efficiency each island  
<sup>305</sup> (North Island, South Island, Stewart Island, Chatham Islands, etc.) will be  
<sup>306</sup> stratified and have their own bounding box and random seed. The seed chosen  
<sup>307</sup> for the South Island was  $\mathbf{u} = (4887260, 18041662)$  with minimum bounding box  
<sup>308</sup> in NZTM

$$[1089354, 1721164] \times [4747979, 5516919].$$

<sup>309</sup> These values define the scaling needed to map the random start Halton points  
<sup>310</sup> to the South Island of New Zealand (NZ). For example, the first point is

$$\begin{aligned}\mathbf{x}_1 &= (631810x_1^{(1)} + 1089354, 768940x_1^{(2)} + 4747979) \\ &\approx (1235673, 5075613).\end{aligned}$$

<sup>311</sup> To sample EMUs in NZ using the master sample, select all sites that fall  
<sup>312</sup> within EMU polygons. The actual required sample size, and what is measured  
<sup>313</sup> should reflect the monitoring objectives and follow a similar process as outlined  
<sup>314</sup> by (Reynolds *et al.* 2016). See Figure 4 for an example of clipping the master  
<sup>315</sup> sample on the South Island into the first 500 samples that fall within EMUs.

<sup>316</sup> The NEXT Foundation currently manages biodiversity at Abel Tasman Na-  
<sup>317</sup> tional Park (ATNP), one of DOC's EMUs, in a partnership with DOC. Based  
<sup>318</sup> on their agreement, the Tomorrow Accord, the NEXT Foundation is managing

319 ATNP while ecological integrity is in a transitional phase. DOC will take over  
320 management activity once the park is in a maintenance phase. Monitoring needs  
321 to be undertaken to establish the current state of ATNP and then to determine  
322 when ecological integrity has been restored. One of the indicators of ecological  
323 integrity was focussed on bird abundance and distribution through the park.  
324 A sample size of  $n_{total} = 65$  was chosen based on a precision analysis using  
325 simr (Green & MacLeod 2016) and historical bird count data from the Eglinton  
326 Valley. Temporal variation was expected to be less than spatial, therefore 15  
327 samples were selected to be measured annually, and the other 50 on a rotating  
328 5-year panel  $[1 - 0, (1 - 4)^5]$ . From the Tier 1 programme mentioned above,  
329 there were four legacy samples in the sample frame. If DOC implemented an  
330 EMU monitoring programme that had 500 augmented sites on the South Island,  
331 then there would be an additional seven points that were already monitored and  
332 funded by DOC using the master sample. These points are included in the ro-  
333 tating panel on years corresponding to the years they are to be sampled. See  
334 Figure 5 for an example of the selected points in this monitoring programme.  
335 Abel Tasman National Park is an example of localised monitoring using the  
336 master sample that can contribute to national estimates of bird abundance and  
337 distribution. DOC gets better precision with the increased sampling in ATNP  
338 and the NEXT Foundation saves resources by using DOC's national investment  
339 in monitoring explicitly in their design.

340 The master sample above is entirely defined by the seed **u** and the bounding  
341 box. Hence, there is no need for a repository to hold the coordinates. Compu-

342 tationally the master sample is easy to run on the fly. Generating 65 points for  
343 Abel Tasman National Park in Figure 5 takes  $\approx 0.5$  seconds on a desktop com-  
344 puter. See supplementary materials for R script to generate a master sample in  
345 New Zealand.

## 346 4 Discussion

347 A master sample can be a useful tool to organise environmental monitoring  
348 at different spatial scales as previously done using GRTS or RRQRR (Larsen  
349 *et al.* 2008; Theobald 2016). By using BAS instead of GRTS there is better  
350 spatial balance (Robertson *et al.* 2013) and no need for an oversample. It is also  
351 possible to add an extra dimension to do unequal probability sampling leading  
352 to an overall more flexible design. Depending on the population being sampled,  
353 spatial balance may or may not lead to a more precise sample than simple  
354 random sampling. However, it is likely that some spatial balance will improve  
355 efficiency for most designs. Not needing to oversample to create a master sample  
356 using BAS means that it will remain relevant at any scale that monitoring takes  
357 place no matter how localised. If an extra dimension is needed, for instance  
358 to take a proportional to surface area sample across mountainous regions with  
359 steep surfaces, the master sample can be adapted to incorporate this. Another  
360 benefit of BAS as a master sample is that it is computationally fast and easy  
361 to program. This reduces the effort needed for storing a million or more points  
362 on a file for others to use. Instead a user can run a provided R script loading

363 their region as a shape file and generate their sample quickly and locally with  
364 unique IDs provided to keep track of sampling.

365 In our experience, any large scale long-term monitoring will need to incor-  
366 porate already existing monitoring programmes that are proven effective. This  
367 was a requirement in developing a master sample for New Zealand. We have  
368 shown that there is no major issue with incorporating legacy monitoring into the  
369 design but recommend that all sites are rigorously vetted to ensure no known  
370 biases are included if historically the sites were judgement samples or for other  
371 reasons. Using panel designs can help incorporate the already existing visitation  
372 schedule of the legacy plots into an efficient monitoring design. We also recom-  
373 mend against incorporating legacy plots by selecting them if the BAS sample is  
374 nearby, based on some criteria.

375 The master sample helps coordinate the locations sampled for environmental  
376 surveys. Every survey at the local and national level should still go through  
377 rigorous design. This means defining the objectives of monitoring clearly and  
378 the methods to use so that they are consistent with standard methodology as  
379 required by the objective. By following the steps outlined in Reynolds *et al.*  
380 (2016) and using the master sample for point generation we believe that the  
381 monitoring programmes undertaken at all levels will have improved efficiency  
382 and contribute to the overall knowledge of the population of interest.

<sup>383</sup> **5 Acknowledgements**

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## 474 6 Supporting Information

- 475 More information about the simulation study and the R code used to generate
- 476 the Master Sample for New Zealand can be found in the supplementary text.

## 477 7 Data Availability

- 478 We present a maintained version of the R code to generate a master sample
- 479 in New Zealand, including a shape file example on github for access to readers
- 480 familiar with R. <https://github.com/ogansell/MSampNZ>.

<sup>481</sup> **8 Author Contribution**

<sup>482</sup> All authors had significant contributions to this research. The paper was ini-  
<sup>483</sup> tiated by a requirement from the Department of Conservation for coordinated  
<sup>484</sup> monitoring of ecosystems at the national level. This work fell directly to Ollie  
<sup>485</sup> Gansel and Paul van Dam-Bates and Blair Robertson collaborated. We were  
<sup>486</sup> funded as salary through our job roles at DOC and the University of Canterbury.

## 487 Figures and Tables

Table 1: Example of a panel design in which panel 1 is sampled annually and panels 2-4 are sampled with a 2 year break in between described as  $[1-0, (1-2)^3]$  in McDonald (2003). The sample size (n) and the points from the master sample are shown along with an X indicating that the panel is sampled on that occasion.  $\{\mathbf{z}\}_j$  is the master sample set that falls within this sample frame.

Panel	n	Sample	Sample Occasion									
			1	2	3	4	5	6	7	8	9	10
1	20	$\{\mathbf{z}\}_{j=1}^{20}$	X	X	X	X	X	X	X	X	X	X
2	10	$\{\mathbf{z}\}_{j=21}^{30}$	X			X			X			X
3	10	$\{\mathbf{z}\}_{j=31}^{40}$		X			X			X		
4	10	$\{\mathbf{z}\}_{j=41}^{50}$			X			X			X	

Table 2: Results from the simulation study testing the impact of adding new samples from altered balanced acceptance sampling (aBAS), balanced acceptance sampling (BAS) and generalised random tessellation stratified (GRTS) to existing simple random samples (SRS). The mean and (standard deviation) is presented. Three populations with varying spatial structure were tested. Population 1, a strong spatial trend. Population 2, a peak function. Population 3, a cyclical (bird) function. The proportion of legacy plots is out of  $n = 60$  for each population.

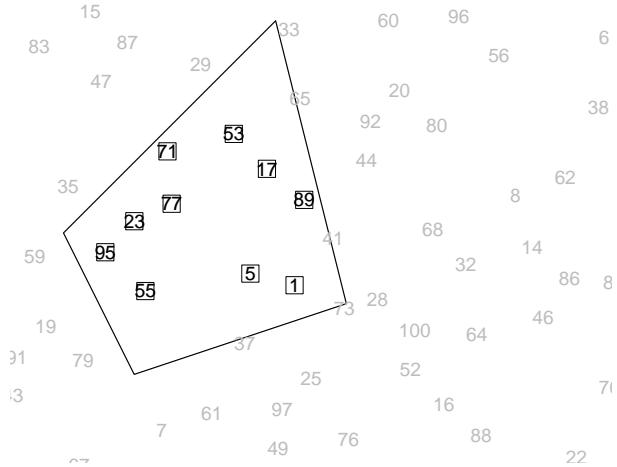
Population	Legacy	BAS	GRTS	aBAS
1	0.08	0.30 (0.008)	0.30 (0.009)	0.30 (0.043)
1	0.17	0.30 (0.009)	0.30 (0.010)	0.30 (0.021)
1	0.50	0.30 (0.014)	0.30 (0.015)	0.30 (0.036)
1	0.83	0.30 (0.018)	0.30 (0.018)	0.30 (0.030)
1	0.92	0.30 (0.018)	0.30 (0.018)	0.30 (0.026)
2	0.08	37.00 (15.9)	36.00 (14.5)	37.3 (19.3)
2	0.17	36.60 (15.1)	36.20 (16.7)	36.9 (19.7)
2	0.50	38.10 (20.7)	37.50 (21.2)	38.3 (29.5)
2	0.83	36.70 (25.5)	37.10 (25.2)	36.9 (26.9)
2	0.92	36.70 (24.2)	37.40 (23.6)	37.2 (25.7)
3	0.08	2.33 (0.29)	2.31 (0.30)	2.33 (0.39)
3	0.17	2.34 (0.32)	2.34 (0.34)	2.34 (0.42)
3	0.50	2.33 (0.40)	2.35 (0.43)	2.35 (0.69)
3	0.83	2.35 (0.50)	2.36 (0.48)	2.36 (0.62)
3	0.92	2.33 (0.48)	252.36 (0.49)	2.34 (0.51)

Table 3: Results from the simulation study testing the impact of adding new samples from altered balanced acceptance sampling (aBAS), balanced acceptance sampling (BAS), generalised random tessellation stratified (GRTS), and simple random sampling (SRS) to existing systematic samples (SS). The mean and (standard deviation) is presented. Three populations with varying spatial structure were tested. Population 1, a strong spatial trend. Population 2, a peak function. Population 3, a cyclical (bird) function. The proportion of legacy plots is out of  $n = 60$  for each population.

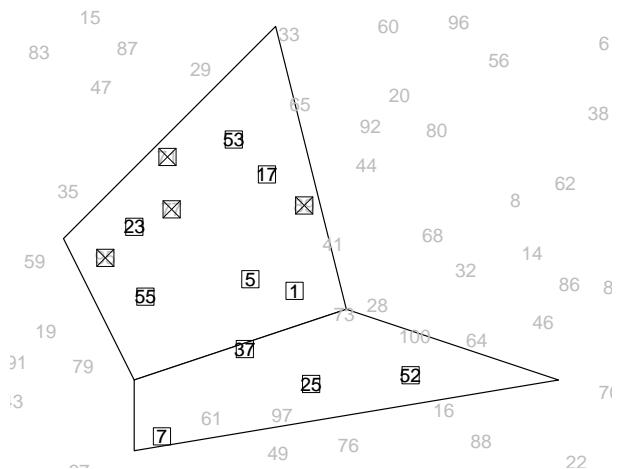
Population	Legacy	BAS	GRTS	SRS	aBAS
1	0.07	0.30 (0.006)	0.30 (0.007)	0.30 (0.018)	0.30 (0.017)
1	0.20	0.30 (0.006)	0.30 (0.008)	0.30 (0.017)	0.30 (0.033)
1	0.50	0.30 (0.007)	0.30 (0.009)	0.30 (0.014)	0.30 (0.027)
1	0.70	0.30 (0.008)	0.30 (0.010)	0.30 (0.013)	0.30 (0.020)
1	0.82	0.30 (0.012)	0.30 (0.013)	0.30 (0.014)	0.30 (0.018)
2	0.07	36.4 (15.0)	36.0 (13.6)	36.6 (24.1)	36.2 (17.8)
2	0.20	36.7 (12.0)	36.2 (14.0)	36.4 (22.7)	37.2 (18.2)
2	0.50	36.9 (12.0)	36.2 (12.2)	37.0 (17.5)	36.2 (40.2)
2	0.70	36.4 (11.0)	35.9 (10.5)	35.4 (13.8)	36.6 (16.8)
2	0.82	35.6 (11.0)	36.0 (9.2)	36.10 (10.7)	35.3 (12.0)
3	0.07	2.32 (0.32)	2.29 (0.31)	2.31 (0.51)	2.32 (0.44)
3	0.20	2.32 (0.26)	2.33 (0.29)	2.31 (0.46)	2.31 (0.43)
3	0.50	2.32 (0.24)	2.35 (0.28)	2.32 (0.37)	2.32 (0.40)
3	0.70	2.34 (0.26)	2.34 (0.27)	2.33 (0.32)	2.34 (0.34)
3	0.82	2.38 (0.27)	262.40 (0.28)	2.38 (0.31)	2.38 (0.35)

C	F
E	B
A	D

Figure 1: A Halton grid with (2,3) co-prime base. The order of points are alphabetical. If the first sample lands in B, the next five would land in (C, D, E, F, A). This structure repeats itself including within each rectangle.



(a)



(b)

Figure 2: Example of changing boundaries using the master sample showing some of the first 100 points in  $[0,1]$ , the order of which is shown by the numbers. A sample of 10 is then selected in the original study (a). In (b), an area is added to the study region but resources still only allow 10 samples. Points 71, 77, 89 and 95 are removed and replaced by 7, 25, 37 and 52 in the new region.

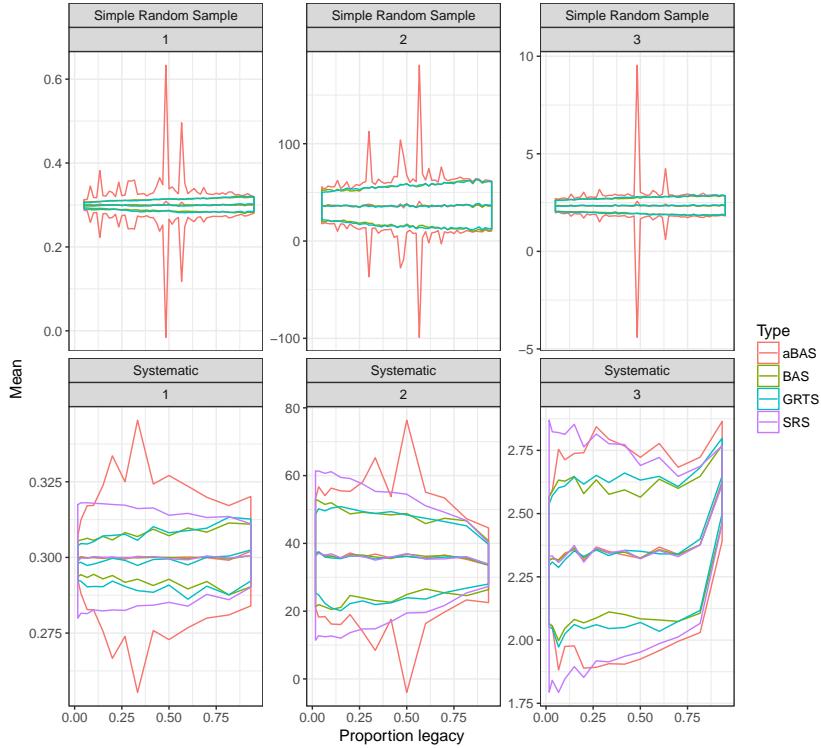
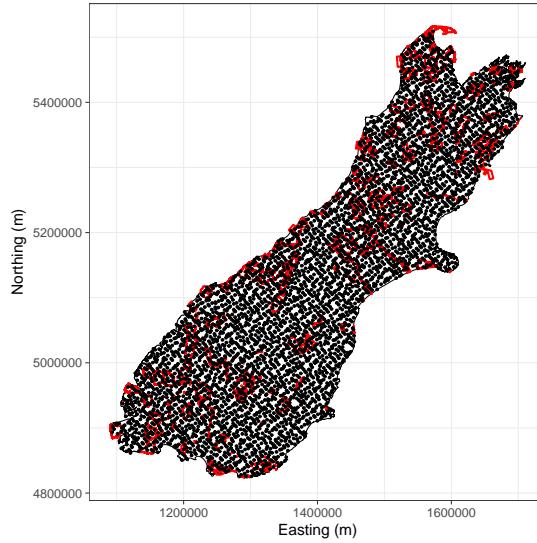
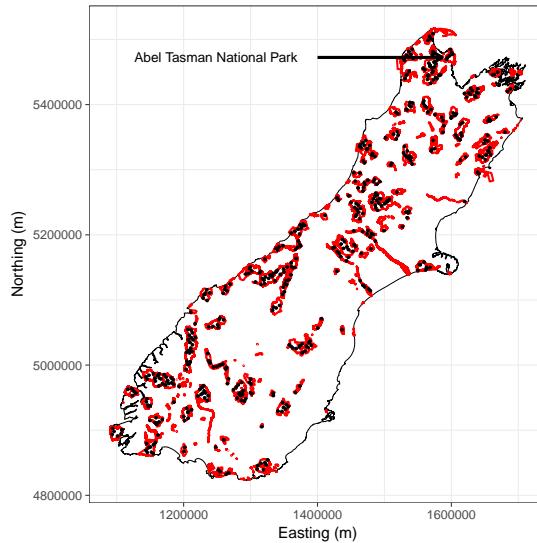


Figure 3: Results from the simulation study testing the impact of adding new samples from altered balanced acceptance sampling (aBAS), balanced acceptance sampling (BAS), generalised random tessellation stratified (GRTS), and simple random sampling (SRS) to existing legacy monitoring locations. Three populations with varying spatial structure were tested. Population 1, a strong spatial trend. Population 2, a peak function. Population 3, a cyclical (bird) function.



(a)



(b)

Figure 4: South Island of New Zealand (a) shows the first 5000 points of the master sample overlayed on red ecosystem management units (EMUs). (b) shows a sample size of 500 of master sample points from (a) that fall within the EMUs in red. Abel Tasman National Park receives seven samples which are included as the first seven in Figure 5

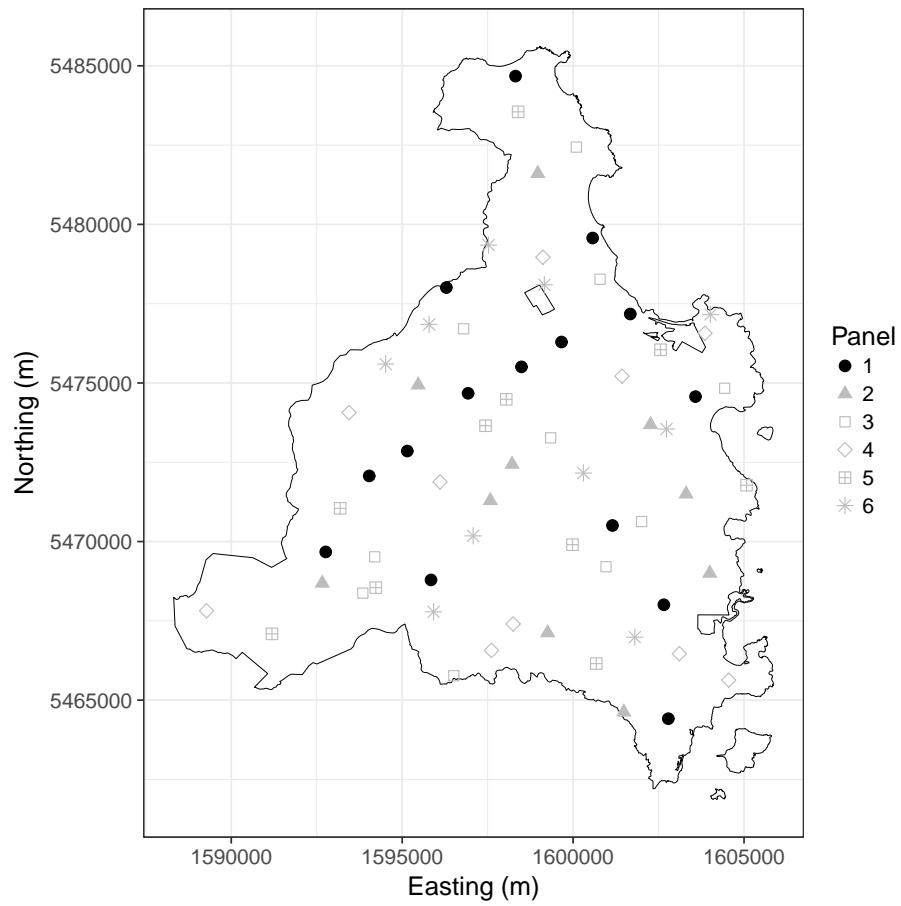


Figure 5: An example of bird monitoring in Abel Tasman National Park New Zealand. Panel 1 is measured annually while the other panels are on a 5-year rotation described as  $[1 - 0, (1 - 4)^5]$ . The first year, panels 1 and 2 would be sampled. This design gives excellent spatial coverage over the park each year ( $n = 25$ ) and over a 5-year period ( $n = 65$ ).