

Competitive Programming Notebook

Programadores Roblox

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DP

1.2Knapsack

 $_{
m Lis}$

```
1 // dp[i][j] => i-esimo item com j-carga sobrando na
      mochila
2 // O(N * W)
_{4} for(int j = 0; j < MAXN; j++) {
      dp[0][j] = 0;
7 for(int i = 1; i <= N; i++) {</pre>
      for(int j = 0; j <= W; j++) {</pre>
          if(items[i].first > j) {
9
10
               dp[i][j] = dp[i-1][j];
               dp[i][j] = max(dp[i-1][j], dp[i-1][j-
      items[i].first] + items[i].second);
15
16 }
```

1.3 Lcs

DS

Ordered Set E Map

#include < ext/pb_ds/assoc_container.hpp>

3 #include < ext/pb_ds/tree_policy.hpp>

```
4 using namespace __gnu_pbds;
                                                            36
5 using namespace std;
7 template < typename T > using ordered_multiset = tree < T, 38</pre>
       null_type, less_equal <T>, rb_tree_tag,
      tree_order_statistics_node_update>;
8 template <typename T> using o_set = tree<T, null_type</pre>
       , less<T>, rb_tree_tag,
      tree_order_statistics_node_update>;
9 template <typename T, typename R> using o_map = tree<</pre>
      T, R, less<T>, rb_tree_tag,
      tree_order_statistics_node_update>;
11 int main() {
   int i, j, k, n, m;
   o_set<int>st;
1.3
    st.insert(1);
    st.insert(2);
    cout << *st.find_by_order(0) << endl; /// k-esimo</pre>
      elemento
    cout << st.order_of_key(2) << endl; ///numero de</pre>
      elementos menores que k
    o_map < int , int > mp;
    mp.insert({1, 10});
19
20
    mp.insert({2, 20});
    cout << mp.find_by_order(0)->second << endl; /// k-11
21
      esimo elemento
                                                            12
    cout << mp.order_of_key(2) << endl; /// numero de</pre>
                                                            13
      elementos (chave) menores que k
                                                            14
    return 0;
24 }
                                                            1.6
        Segtree Iterativa
```

```
T res_l = neutral_value, res_r =
neutral_value;
   for (1 += n, r += n + 1; 1 < r; 1 >>= 1, r
>>= 1) {
        if (1 & 1) res_l = combine(res_l, tree[l
        if (r & 1) res_r = combine(tree[--r],
res_r);
    return combine(res_1, res_r);
}
void update(int pos, T new_val) {
```

tree[i] = combine(tree[i * 2], tree[i * 2

2.3Dsu

* pos + 1]);

1 // Exemplo de uso:

5 template <typename T> 6 struct SegTree {

int n;

+ 1]):

11

13

14

15

16

18

20

21

24

26

27

28

29

3.2

33

34 35

2 // SegTree < int > st(vetor); 3 // range query e point update

> vector < T> tree; T neutral_value = 0;

T combine(T a, T b) {

return a + b:

n = data.size();

SegTree(const vector < T > & data) {

for (int i = 0; i < n; i++)</pre>

T range_query(int 1, int r) {

tree[pos += n] = new_val;

for (pos >>= 1; pos > 0; pos >>= 1)

tree[pos] = combine(tree[2 * pos], tree[2

tree[n + i] = data[i];

for (int i = n - 1; i > 0; --i)

tree.resize(2 * n, neutral_value);

```
1 struct DSU {
     vector < int > par, rank, sz;
     int c;
     DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
     1, 1), c(n) {
          for (int i = 1; i <= n; ++i) par[i] = i;</pre>
     }
     int find(int i) {
          return (par[i] == i ? i : (par[i] = find(par[
     i])));
     bool same(int i, int j) {
         return find(i) == find(j);
     int get_size(int i) {
          return sz[find(i)];
     int count() {
          return c; // quantos componentes conexos
     int merge(int i, int j) {
```

18

19

```
if ((i = find(i)) == (j = find(j))) return
                                                                     auto qr = query(rc(p), mid + 1, r, L, R);
20
                                                          60
       -1;
                                                          61
                                                                     return merge(ql, qr);
           else --c;
                                                          62
           if (rank[i] > rank[j]) swap(i, j);
                                                          63
                                                                 11 query(int 1, int r) { return query(1, 0, n -
          par[i] = j;
                                                                 1, 1, r); }
           sz[j] += sz[i];
                                                                 void update(int p, int 1, int r, int L, int R, 11
24
                                                          64
           if (rank[i] == rank[j]) rank[j]++;
                                                                  val, bool repl = 0) {
                                                                     push(p, 1, r);
26
           return ;
                                                          6.5
                                                                     if (1 > R || r < L) return;
27
                                                          66
28 };
                                                                     if (1 >= L && r <= R) {
                                                          67
                                                                          lazy[p] = val;
                                                          68
  2.4 Segtree Sum
                                                          69
                                                                          replace[p] = repl;
                                                          7.0
                                                                          push(p, 1, r);
                                                          7.1
                                                                     } else {
1 struct SegTree {
      ll merge(ll a, ll b) { return a + b; }
                                                          72
                                                                          int mid = (1 + r) / 2;
                                                                          update(lc(p), l, mid, L, R, val, repl);
                                                          73
      const ll neutral = 0;
                                                                          update(rc(p), mid + 1, r, L, R, val, repl
      int n;
                                                                 );
      vector<1l> t, lazy;
      vector < bool > replace;
                                                                          t[p] = merge(t[lc(p)], t[rc(p)]);
                                                                     }
      inline int lc(int p) { return p * 2; }
                                                          76
                                                                 }
      inline int rc(int p) { return p * 2 + 1; }
                                                          7.7
                                                                  void sumUpdate(int 1, int r, 11 val) { update(1,
      void push(int p, int l, int r) {
                                                          78
9
                                                                 0, n - 1, l, r, val, 0); }
          if (replace[p]) {
10
                                                                  void assignUpdate(int 1, int r, 11 val) { update
11
              t[p] = lazy[p] * (r - l + 1);
               if (1 != r) {
                                                                 (1, 0, n - 1, 1, r, val, 1); }
12
                                                          80 } segsum;
1.3
                   lazy[lc(p)] = lazy[p];
                   lazy[rc(p)] = lazy[p];
1.4
                                                                  Psum 2d
                                                             2.5
                   replace[lc(p)] = true;
                   replace[rc(p)] = true;
16
              }
                                                           _{1} // retangulo retorna a psum2d do intervalo inclusivo
          } else if (lazy[p] != 0) {
18
                                                           vector < vector < int >> psum(n+1, vector < int > (m+1, 0));
              t[p] += lazy[p] * (r - l + 1);
19
               if (1 != r) {
20
                                                           4 for (int i=1; i<n+1; i++){</pre>
                   lazy[lc(p)] += lazy[p];
                                                                 for (int j=1; j<m+1; j++){</pre>
                   lazy[rc(p)] += lazy[p];
                                                                     cin >> psum[i][j];
23
                                                                     psum[i][j] += psum[i-1][j]+psum[i][j-1]-psum[
24
                                                                 i-1][j-1];
25
          replace[p] = false;
          lazy[p] = 0;
26
                                                           9 }
      void build(int p, int 1, int r, const vector<11>
28
                                                           11 // y1 eh variavel reservada
      &v) {
                                                           int retangulo(int x1, int yy1, int x2, int yy2){
29
          if (1 == r) {
                                                                 x2 = min(x2, n), yy2 = min(yy2, m);
                                                           13
              t[p] = v[1];
3.0
                                                          14
                                                                 x1 = max(0LL, x1-1), yy1 = max(0LL, yy1-1);
31
          } else {
                                                          15
               int mid = (1 + r) / 2;
32
                                                                 return psum[x2][yy2]-psum[x1][yy2]-psum[x2][yy1]+
                                                           16
               build(lc(p), l, mid, v);
                                                                 psum[x1][yy1];
               build(rc(p), mid + 1, r, v);
34
3.5
               t[p] = merge(t[lc(p)], t[rc(p)]);
          }
36
                                                             2.6 Segtree Gcd
      }
37
       void build(int _n) {
          n = _n;
                                                           int gcd(int a, int b) {
39
                                                                 if (b == 0)
           t.assign(n * 4, neutral);
40
          lazy.assign(n * 4, 0);
                                                                     return a;
41
                                                           3
          replace.assign(n * 4, false);
                                                           4
                                                                 return gcd(b, a % b);
42
                                                           5 }
43
      void build(const vector<11> &v) {
44
          n = (int)v.size();
                                                           7 class SegmentTreeGCD {
46
           t.assign(n * 4, neutral);
                                                           8 private:
           lazy.assign(n * 4, 0);
                                                                 vector < int> tree;
47
                                                           9
                                                                 int n;
           replace.assign(n * 4, false);
                                                          10
          build(1, 0, n - 1, v);
                                                          11
49
50
      }
                                                          12
                                                                 void build(const vector<int>& arr, int node, int
      void build(ll *bg, ll *en) {
                                                                 start, int end) {
5.1
           build(vector<11>(bg, en));
                                                                     if (start == end) {
52
                                                          13
53
                                                                          tree[node] = arr[start];
                                                          14
54
      11 query(int p, int l, int r, int L, int R) {
                                                                     } else {
                                                          15
          push(p, 1, r);
                                                                          int mid = (start + end) / 2;
           if (1 > R || r < L) return neutral;</pre>
                                                                          \verb|build(arr, 2 * node + 1, start, mid);|\\
56
                                                          1.7
           if (1 >= L && r <= R) return t[p];</pre>
                                                                          build(arr, 2 * node + 2, mid + 1, end);
                                                           18
           int mid = (1 + r) / 2;
                                                                          tree[node] = gcd(tree[2 * node + 1], tree
58
                                                          19
           auto ql = query(lc(p), l, mid, L, R);
                                                                 [2 * node + 2]);
59
```

```
idx += idx & -idx:
           }
20
21
                                                           22
                                                                      }
                                                                  }
                                                           23
      void update(int node, int start, int end, int idx 24
                                                                 int query(int idx) {
23
       , int value) {
                                                                      return sum(idx);
          if (start == end) {
                                                                  }
24
                                                           26
               tree[node] = value;
                                                                  int range_query(int 1, int r) {
                                                                      return sum(r) - sum(1 - 1);
          } else {
26
                                                           28
               int mid = (start + end) / 2;
27
                                                           29
               if (idx <= mid) {</pre>
                                                           30 };
                   update(2 * node + 1, start, mid, idx, 31
29
        value);
                                                           32 BIT fenwick(n);
                                                           33 for(int i = 1; i <= n; i++) {
               } else {
                   update(2 * node + 2, mid + 1, end,
                                                                  fenwick.update(i, arr[i]);
31
                                                           34
      idx, value);
                                                           35
              }
32
               tree[node] = gcd(tree[2 * node + 1], tree
                                                                   Graph
       [2 * node + 2]);
           }
                                                              3.1 Lca
      }
3.5
36
       int query(int node, int start, int end, int 1,
37
                                                           1 // LCA - CP algorithm
      int r) {
                                                            2 // preprocessing O(NlogN)
                                                            3 // lca O(logN)
           if (r < start || 1 > end) {
              return 0;
39
                                                            4 // Uso: criar LCA com a quantidade de vÃlrtices (n) e
           }
40
                                                                   lista de adjacÃłncia (adj)
           if (1 <= start && end <= r) {</pre>
41
                                                            5 // chamar a funÃgÃčo preprocess com a raiz da Ãąrvore
              return tree[node];
42
           }
                                                            7 struct LCA {
           int mid = (start + end) / 2;
44
                                                                 int n, l, timer;
           int left_gcd = query(2 * node + 1, start, mid g
45
                                                                 vector < vector < int >> adj;
      , l, r);
                                                                  vector < int > tin, tout;
                                                           10
          int right_gcd = query(2 * node + 2, mid + 1, 11
46
                                                                  vector < vector < int >> up;
      end, 1, r);
          return gcd(left_gcd, right_gcd);
47
                                                                  LCA(int n, const vector < vector < int >> & adj) : n(n)
48
                                                                  , adj(adj) {}
49
                                                           14
50 public:
                                                           15
                                                                  void dfs(int v, int p) {
      SegmentTreeGCD(const vector<int>& arr) {
                                                                      tin[v] = ++timer;
51
                                                           16
          n = arr.size();
52
                                                                      up[v][0] = p;
                                                           17
                                                                      for (int i = 1; i <= 1; ++i)</pre>
53
           tree.resize(4 * n);
                                                           1.8
           build(arr, 0, 0, n - 1);
54
                                                                          up[v][i] = up[up[v][i-1]][i-1];
                                                           19
55
                                                           20
      void update(int idx, int value) {
56
                                                                      for (int u : adj[v]) {
                                                           21
          update(0, 0, n - 1, idx, value);
57
                                                          22
                                                                          if (u != p)
                                                                              dfs(u, v);
                                                           23
      int query(int 1, int r) {
5.9
                                                           24
          return query(0, 0, n - 1, 1, r);
                                                           2.5
61
                                                           26
                                                                      tout[v] = ++timer;
62 }:
                                                                  }
                                                           27
                                                           28
  2.7 Bit
                                                                  bool is_ancestor(int u, int v) {
                                                           29
                                                                      return tin[u] <= tin[v] && tout[u] >= tout[v
                                                           30
1 class BIT {
                                                                  ];
      vector<int> bit:
2
                                                           3.1
                                                                  }
3
      int n:
                                                           32
       int sum(int idx) {
                                                           33
                                                                  int lca(int u, int v) {
           int result = 0;
                                                                      if (is_ancestor(u, v))
                                                           34
           while (idx > 0) {
                                                                          return u;
                                                                      if (is_ancestor(v, u))
              result += bit[idx];
                                                           36
               idx -= idx & -idx;
                                                           37
                                                                          return v;
           }
                                                                      for (int i = 1; i >= 0; --i) {
9
                                                           38
           return result;
                                                           39
                                                                          if (!is_ancestor(up[u][i], v))
1.0
      }
                                                           40
                                                                              u = up[u][i];
12
                                                           41
                                                                      return up[u][0];
13 public:
                                                           42
      BIT(int size) {
14
                                                           43
15
         n = size;
          bit.assign(n + 1, 0); // BIT indexada em 1
                                                                  void preprocess(int root) {
                                                                      tin.resize(n);
1.7
                                                           46
      void update(int idx, int delta) {
                                                                      tout.resize(n);
18
                                                           47
          while (idx <= n) {
                                                                      timer = 0;
19
                                                           48
               bit[idx] += delta;
                                                                      1 = ceil(log2(n));
                                                           49
20
```

```
up.assign(n, vector<int>(1 + 1));
5.0
                                                           1.8
51
           dfs(root, root);
                                                                  int count() {
                                                           19
                                                                       return c; // quantos componentes conexos
52
                                                           20
53 };
                                                           21
                                                                  int merge(int i, int j) {
                                                           22
        Floyd Warshall
                                                                      if ((i = find(i)) == (j = find(j))) return
                                                           23
                                                                       else --c:
                                                           2.4
1 // SSP e acha ciclos.
                                                                       if (rank[i] > rank[j]) swap(i, j);
                                                           25
2 // Bom com constraints menores.
                                                                      par[i] = j;
3 // 0(n^3)
                                                                       sz[j] += sz[i];
                                                           27
                                                           28
                                                                       if (rank[i] == rank[j]) rank[j]++;
5 int dist[501][501];
                                                           29
                                                                       return ;:
                                                           30
7 void floydWarshall() {
                                                           31 };
      for(int k = 0; k < n; k++) {
                                                           32
           for(int i = 0; i < n; i++) {</pre>
9
                                                           33 struct Edge {
               for(int j = 0; j < n; j++) {</pre>
                   dist[i][j] = min(dist[i][j], dist[i][34
                                                                 int u, v, w;
                                                                 bool operator <(Edge const & other) {</pre>
      k] + dist[k][j]);
                                                           3.6
                                                                      return weight <other.weight;</pre>
               }
                                                           37
           }
13
                                                           38 }
14
                                                           3.9
15 }
                                                           40 vector < Edge > kruskal(int n, vector < Edge > edges) {
16 void solve() {
                                                                  vector < Edge > mst;
                                                           41
17
      int m, q;
                                                                  DSU dsu = DSU(n + 1);
                                                           42
18
      cin >> n >> m >> q;
                                                           43
                                                                  sort(edges.begin(), edges.end());
      for(int i = 0; i < n; i++) {</pre>
19
                                                                  for (Edge e : edges) {
                                                           44
          for(int j = i; j < n; j++) {
20
                                                                      if (dsu.find(e.u) != dsu.find(e.v)) {
               if(i == j) {
                                                                           mst.push_back(e);
                                                           46
                   dist[i][j] = dist[j][i] = 0;
22
                                                           47
                                                                           dsu.join(e.u, e.v);
               } else {
23
                                                           48
                   dist[i][j] = dist[j][i] = linf;
                                                           49
2.5
                                                           50
                                                                  return mst;
           }
                                                           51 }
      }
27
      for(int i = 0; i < m; i++) {</pre>
28
                                                                    Topological Sort
29
           int u, v, w;
           cin >> u >> v >> w; u--; v--;
30
           dist[u][v] = min(dist[u][v], w);
                                                           vector < int > adj [MAXN];
                                                            vector < int > estado(MAXN); // 0: nao visitado 1:
           dist[v][u] = min(dist[v][u], w);
32
33
                                                                  processamento 2: processado
                                                            3 vector < int > ordem;
      floydWarshall();
34
35
      while (q - -) {
                                                            4 bool temCiclo = false;
          int u, v;
36
           cin >> u >> v; u--; v--;
                                                            6 void dfs(int v) {
37
           if(dist[u][v] == linf) cout << -1 << '\n';</pre>
                                                                 if(estado[v] == 1) {
           else cout << dist[u][v] << '\n';</pre>
                                                                      temCiclo = true;
3.9
                                                                       return:
41 }
                                                           10
                                                                  if(estado[v] == 2) return;
  3.3 Kruskal
                                                                  estado[v] = 1;
                                                           12
                                                                  for(auto &nei : adj[v]) {
                                                           13
                                                                      if(estado[v] != 2) dfs(nei);
                                                           14
1 // Ordena as arestas por peso, insere se ja nao
                                                           1.5
      estiver no mesmo componente
                                                           16
                                                                  estado[v] = 2;
2 // O(E log E)
                                                           17
                                                                  ordem.push_back(v);
                                                                  return:
4 struct DSU {
      vector < int > par, rank, sz;
                                                              3.5
                                                                   Bellman Ford
      int c;
      DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
      1, 1), c(n) {
                                                            1 struct Edge {
          for (int i = 1; i <= n; ++i) par[i] = i;
                                                                 int u, v, w;
      }
1.0
      int find(int i) {
           return (par[i] == i ? i : (par[i] = find(par[ 5 // se x = -1, nÃčo tem ciclo
                                                            _{6} // se x != -1, pegar pais de x pra formar o ciclo
      i])));
12
      bool same(int i, int j) {
                                                            8 int n, m;
          return find(i) == find(j);
                                                            9 vector < Edge > edges;
14
                                                           10 vector < int > dist(n);
15
      int get_size(int i) {
                                                           vector < int > pai(n, -1);
16
           return sz[find(i)];
                                                           12
```

dfs(nei, v);

36

```
for (int i = 0; i < n; i++) {</pre>
                                                                      }
1.3
                                                           3.7
14
           x = -1;
                                                           38
                                                                  }
           for (Edge &e : edges) {
                                                           39 }
15
               if (dist[e.u] + e.w < dist[e.v]) {</pre>
                                                           40
16
                   dist[e.v] = max(-INF, dist[e.u] + e.w_{41} while((1 << LOG) <= n) LOG++;
      ):
                                                              3.8
                                                                   Dijkstra
                   pai[e.v] = e.u;
                   x = e.v;
19
               }
20
                                                           1 // SSP com pesos positivos.
           }
21
                                                           _{2} // O((V + E) log V).
      }
22
                                                           4 vector<int> dijkstra(int S) {
24 // achando caminho (se precisar)
                                                                  vector < bool > vis(MAXN, 0);
25 for (int i = 0; i < n; i++) x = pai[x];</pre>
                                                                  vector<11> dist(MAXN, LLONG_MAX);
                                                           6
                                                                  dist[S] = 0;
27 vector < int > ciclo;
                                                                  priority_queue<pii, vector<pii>, greater<pii>> pq
                                                           8
28 for (int v = x;; v = pai[v]) {
      cycle.push_back(v);
29
                                                                 pq.push({0, S});
      if (v == x && ciclo.size() > 1) break;
                                                                  while(pq.size()) {
                                                           10
31 }
                                                                      11 v = pq.top().second;
s2 reverse(ciclo.begin(), ciclo.end());
                                                           12
                                                                      pq.pop();
                                                                      if(vis[v]) continue;
                                                           13
  3.6 Dfs
                                                                      vis[v] = 1;
                                                           14
                                                                      for(auto &[peso, vizinho] : adj[v]) {
                                                           15
                                                           16
                                                                          if(dist[vizinho] > dist[v] + peso) {
int dfs(int x, int p) {
                                                                               dist[vizinho] = dist[v] + peso;
      for (auto e : adj[x]) {
                                                           17
          if (e != p) {
                                                                               pq.push({dist[vizinho], vizinho});
                                                           18
              dfs(e, x);
                                                           19
                                                                      }
                                                           2.0
                                                                  }
      }
                                                           21
                                                                  return dist;
7 }
                                                           22
                                                           23 }
  3.7 Lca Jc
                                                                   String
1 int LOG;
                                                                    Z Function
                                                              4.1
3 int get_lca(int a, int b) {
      if(profundidade[b] > profundidade[a]) {
                                                            vector < int > z_function(string s) {
           swap(a, b);
                                                                 int n = s.size();
                                                                 vector < int > z(n);
       int k = profundidade[a] - profundidade[b]; //
                                                            4
                                                                  int 1 = 0, r = 0;
      tanto que tenho que subir
                                                                  for(int i = 1; i < n; i++) {</pre>
      for(int j = LOG-1; j >= 0; j--) {
                                                                      if(i < r) {
           if((1 << j) & k) {
9
                                                                          z[i] = min(r - i, z[i - 1]);
               a = cima[a][j];
10
                                                                      while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
13
      if(a == b) return a; // ja to no lca
                                                                          z[i]++;
14
                                                                      }
      for(int j = LOG-1; j >= 0; j--) { // subo com os
15
                                                                      if(i + z[i] > r) {
                                                           12
       dois atÃľ chegar no lca fazendo binary lifting
                                                                          1 = i;
         if(cima[a][j] != cima[b][j]) {
16
                                                                          r = i + z[i];
                                                           1.4
               a = cima[a][j];
                                                           15
               b = cima[b][j];
1.8
                                                                  }
                                                           16
19
           }
                                                                  return z;
                                                           1.7
      }
20
                                                           18 }
      return cima[a][0];
21
22 }
                                                                   Trie Ponteiros
23
24 void dfs(int v, int p) {
      if(v != 1) profundidade[v] = profundidade[p] + 1; _{\scriptscriptstyle 1} // Trie por ponteiros
25
       cima[v][0] = p;
                                                          2 // InserÃğÃčo, busca e consulta de prefixo em O(N)
26
       for(int j = 1; j < LOG; j++) {</pre>
          if (cima[v][j-1] != -1) {
                                                            4 struct Node {
28
               cima[v][j] = cima[cima[v][j-1]][j-1];
                                                                  Node *filhos[26] = \{\};
                                                           5
                                                                  bool acaba = false;
3.0
           } else {
31
               cima[v][j] = -1;
                                                                  int contador = 0;
           }
                                                            8 };
      }
33
      for(auto &nei : adj[v]) {
                                                           void insere(string s, Node *raiz) {
          if(nei != p) {
                                                                Node *cur = raiz;
3.5
```

12

for(auto &c : s) {

```
cur -> contador++:
                                                                 for(auto &c : s) {
1.3
                                                           3.4
14
           if(cur->filhos[c - 'a'] != NULL) {
                                                           35
                                                                     if(trie[no][c - 'a'] == 0){
               cur = cur->filhos[c - 'a'];
1.5
                                                           36
                                                                           return -1;
               continue;
                                                           3.7
16
                                                                      no = trie[no][c - 'a'];
           }
           cur->filhos[c - 'a'] = new Node();
18
                                                           39
           cur = cur->filhos[c - 'a'];
19
                                                           40
                                                                  return contador[no];
                                                           41 }
2.0
      cur -> contador++;
21
                                                              4.4 Kmp
      cur -> a caba = true;
23 }
24
                                                           vector < int > kmp (string s) {
25 bool busca(string s, Node *raiz) {
                                                                  int n = (int)s.length();
                                                           2
      Node *cur = raiz;
                                                                  vector < int > p(n+1);
                                                            3
      for(auto &c : s) {
27
                                                            4
                                                                  p[0] = -1;
          if (cur->filhos[c - 'a'] != NULL) {
28
                                                                  for (int i = 1; i < n; i++) {</pre>
                                                            5
29
               cur = cur->filhos[c - 'a'];
                                                                      int j = p[i-1];
               continue:
3.0
                                                                       while (j \ge 0 \&\& s[j] != s[i-1])
                                                                           j = p[j-1];
32
          return false;
                                                                      p[i] = j+1;
                                                            9
      }
33
                                                           1.0
      return cur->acaba;
34
                                                                  return p;
35 }
                                                           12 }
_{
m 37}^{
m 37} // Retorna se 
m 	ilde{A}l' prefixo e quantas strings tem s como 
m 4.5~Hashing
       prefixo
38 int isPref(string s, Node *raiz) {
                                                            1 // String Hash template
      Node *cur = raiz;
39
                                                            2 // constructor(s) - O(|s|)
      for(auto &c : s) {
40
                                                            3 // query(1, r) - returns the hash of the range [1,r]
          if (cur->filhos[c - 'a'] != NULL) {
4.1
                                                                  from left to right - O(1)
               cur = cur->filhos[c - 'a'];
42
                                                            _4 // query_inv(l, r) from right to left - O(1)
43
               continue;
                                                            5 // patrocinado por tiagodfs
          }
44
          return -1:
                                                            7 struct Hash {
      }
46
                                                                  const int X = 2147483647;
      return cur->contador;
                                                                  const int MOD = 1e9+7;
48 }
                                                            9
                                                                  int n; string s;
                                                           10
  4.3 Trie
                                                                  vector < int > h, hi, p;
                                                                  Hash() {}
                                                            12
                                                                  Hash(string s): s(s), n(s.size()), h(n), hi(n), p
                                                            13
1 // Trie por array
2 // InserÃgÃčo, busca e consulta de prefixo em O(N)
                                                                       for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1)</pre>
                                                                   % MOD;
4 int trie[MAXN][26];
                                                                      for (int i=0;i<n;i++)</pre>
                                                            15
5 int tot_nos = 0;
                                                                          h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD;
                                                            16
6 vector < bool > acaba(MAXN, false);
                                                                       for (int i=n-1; i>=0; i--)
                                                           1.7
vector < int > contador (MAXN, 0);
                                                                           hi[i] = (s[i] + (i+1 < n ? hi[i+1]:0) * X)
                                                           18
                                                                  % MOD;
9 void insere(string s) {
                                                           19
     int no = 0;
10
                                                                  int query(int 1, int r) {
      for(auto &c : s) {
                                                                      int hash = (h[r] - (1 ? h[1-1]*p[r-1+1]%MOD :
                                                           21
           if(trie[no][c - 'a'] == 0) {
12
              trie[no][c - 'a'] = ++tot_nos;
13
                                                                       return hash < 0 ? hash + MOD : hash;</pre>
                                                           22
14
                                                           23
           no = trie[no][c - 'a'];
1.5
                                                                  int query_inv(int 1, int r) {
                                                           24
16
           contador[no]++;
                                                                      int hash = (hi[1] - (r+1 < n ? hi[r+1]*p[r-1]
                                                           2.5
17
                                                                  +1] % MOD : 0));
      acaba[no] = true;
18
                                                                       return hash < 0 ? hash + MOD : hash;</pre>
                                                           26
19 }
                                                           27
20
                                                           28 };
21 bool busca(string s) {
      int no = 0;
                                                              4.6 Lcs
      for(auto &c : s) {
23
          if(trie[no][c - 'a'] == 0) {
                                                            int lcs(string &s1, string &s2) {
2.5
               return false;
           }
                                                                  int m = s1.size();
          no = trie[no][c - 'a'];
                                                                  int n = s2.size();
27
                                                            3
      return acaba[no];
                                                                  vector < vector < int >> dp(m + 1, vector < int > (n + 1,
29
30 }
                                                                  0)):
32 int isPref(string s) {
                                                                  for (int i = 1; i <= m; ++i) {</pre>
      int no = 0;
                                                                      for (int j = 1; j <= n; ++j) {
```

```
if (s1[i - 1] == s2[j - 1])
                                                                        ll area = area_triangulo(x1, y1, x2, y2, x3, y3);
                                                                1.6
10
                    dp[i][j] = dp[i - 1][j - 1] + 1;
                                                               17
                                                                        11 tot_borda = pontos_borda(x1, y1, x2, y2) +
                                                                        pontos_borda(x2, y2, x3, y3) + pontos_borda(x3,
                     dp[i][j] = max(dp[i - 1][j], dp[i][j
                                                                        y3, x1, y1);
12
       - 1]);
                                                                        ll ans = (area - tot_borda) / 2 + 1;
13
           }
                                                                 19
       }
                                                                        \operatorname{cout} << \operatorname{ans} << \operatorname{endl};
14
                                                                 20
1.5
       return dp[m][n];
                                                                        return 0;
16
                                                                 22
17 }
                                                                 23 }
```

4.7 Countpermutations

1 // Returns the number of distinct permutations

```
_2 // that are lexicographically less than the string t _2
3 // using the provided frequency (freq) of the
       characters
4 // O(n*freq.size())
5 int countPermLess(vector<int> freq, const string &t)
       int n = t.size();
6
       int ans = 0;
       vector < int > fact(n + 1, 1), invfact(n + 1, 1);
       for (int i = 1; i <= n; i++)
1.0
                                                            11
          fact[i] = (fact[i - 1] * i) % MOD;
                                                            12
       invfact[n] = fexp(fact[n], MOD - 2, MOD);
                                                            13
       for (int i = n - 1; i \ge 0; i - -)
13
                                                            14
           invfact[i] = (invfact[i + 1] * (i + 1)) % MOD 15
14
                                                            16
15
                                                            17
       // For each position in t, try placing a letter
16
                                                            18
       smaller than t[i] that is in freq
                                                            19
       for (int i = 0; i < n; i++) {</pre>
                                                            20
           for (char c = 'a'; c < t[i]; c++) {</pre>
18
                                                            21
               if (freq[c - 'a'] > 0) {
                   freq[c - 'a']--;
20
                    int ways = fact[n - i - 1];
21
                    for (int f : freq)
                                                            23
                        ways = (ways * invfact[f]) % MOD; 24
23
                    ans = (ans + ways) % MOD;
                    freq[c - 'a']++;
25
                                                           27
           }
27
           if (freq[t[i] - 'a'] == 0) break;
28
                                                            29
           freq[t[i] - 'a']--;
       }
3.0
                                                            3.1
3.1
       return ans;
32 }
                                                            33
```

5 Geometry

15

Lattice Points

```
1 ll gcd(ll a, ll b) {
      return b == 0 ? a : gcd(b, a % b);
2
3 }
_4 ll area_triangulo(ll x1, ll y1, ll x2, ll y2, ll x3, _{_{43}}
      11 y3) {
       return abs(x1 * (y2 - y3) + x2 * (y3 - y1) + x3 *
       (y1 - y2));
6 }
7 ll pontos_borda(ll x1, ll y1, ll x2, ll y2) {
      return gcd(abs(x2 - x1), abs(y2 - y1));
9 }
10
11 int32_t main() {
      ll x1, y1, x2, y2, x3, y3;
12
      cin >> x1 >> y1;
13
      cin >> x2 >> y2;
14
      cin >> x3 >> y3;
```

Inside Polygon

```
1 // Convex O(logn)
 3 bool insideT(point a, point b, point c, point e){
       int x = ccw(a, b, e);
       int y = ccw(b, c, e);
      int z = ccw(c, a, e);
       return !((x==1 or y==1 or z==1) and (x==-1 or y
       ==-1 or z==-1));
 8 }
10 bool inside(vp &p, point e){ // ccw
      int 1=2, r=(int)p.size()-1;
       while(1<r){
           int mid = (1+r)/2;
           if(ccw(p[0], p[mid], e) == 1)
               l = mid + 1;
           elsef
               r = mid;
      // bordo
      // if(r==(int)p.size()-1 and ccw(p[0], p[r], e)
       ==0) return false;
       // if(r==2 and ccw(p[0], p[1], e)==0) return
       false;
       // if(ccw(p[r], p[r-1], e) == 0) return false;
       return insideT(p[0], p[r-1], p[r], e);
28 // Any O(n)
30 int inside(vp &p, point pp){
       // 1 - inside / 0 - boundary / -1 - outside
       int n = p.size();
       for(int i=0;i<n;i++){</pre>
           int j = (i+1)%n;
34
35
           if(line({p[i], p[j]}).inside_seg(pp))
36
               return 0;
37
       int inter = 0;
3.8
39
       for(int i=0;i<n;i++){</pre>
40
           int j = (i+1)\%n;
           if(p[i].x \le pp.x and pp.x \le p[j].x and ccw(p
41
       [i], p[j], pp)==1)
               inter++; // up
           else if(p[j].x <= pp.x and pp.x < p[i].x and</pre>
       ccw(p[i], p[j], pp) == -1)
               inter++; // down
       }
46
       if(inter%2==0) return -1; // outside
47
       else return 1; // inside
48
49 }
         Point Location
```

```
2 int32_t main(){
```

48

49 };

```
SWS:
                                                             5.0
                                                             int ccw(point p1, point p2, point p3)
4
       int t; cin >> t;
                                                             52
                                                             53
                                                                     cod cross = (p2-p1) ^ (p3-p1);
       while (t - -) {
                                                                     if(cross == 0) return 0;
                                                                    else if(cross < 0) return -1;</pre>
                                                             55
           int x1, y1, x2, y2, x3, y3; cin >> x1 >> y1
                                                             56
                                                                    else return 1;
       >> x2 >> y2 >> x3 >> y3;
                                                             57 }
10
                                                             58
           int deltax1 = (x1-x2), deltay1 = (y1-y2);
                                                             59 vector <point> convex_hull(vector<point> p)
12
                                                             60 {
13
           int compx = (x1-x3), compy = (y1-y3);
                                                             61
                                                                    sort(p.begin(), p.end());
                                                                    vector < point > L,U;
14
                                                             62
           int ans = (deltax1*compy) - (compx*deltay1); 63
15
16
                                                                    //Lower
           if(ans == 0){cout << "TOUCH\n"; continue;}</pre>
17
                                                             65
                                                                    for(auto pp : p)
           if(ans < 0){cout << "RIGHT\n"; continue;}</pre>
                                                             66
           if(ans > 0){cout << "LEFT\n"; continue;}</pre>
                                                                         while(L.size() >= 2 and ccw(L[L.size() - 2],
19
                                                             67
20
                                                                     L.back(), pp) == -1)
21
       return 0;
                                                             68
                                                                        {
22 }
                                                                             // Ãľ -1 pq eu nÃčo quero excluir os
                                                                     colineares
  5.4 Convex Hull
                                                                             L.pop_back();
                                                                         }
#include <bits/stdc++.h>
                                                             72
                                                                         L.push_back(pp);
                                                             73
                                                             74
3 using namespace std;
                                                                    reverse(p.begin(), p.end());
4 #define int long long
                                                             75
5 typedef int cod;
                                                             76
                                                                    //Upper
                                                             7.7
                                                                     for(auto pp : p)
                                                             78
7 struct point
                                                             79
8 {
                                                                         while(U.size() >= 2 and ccw(U[U.size()-2], U
                                                             80
       cod x,y;
       point(cod x = 0, cod y = 0): x(x), y(y)
                                                                     .back(), pp) == -1)
10
                                                             81
                                                                         -{
                                                             82
                                                                             U.pop_back();
12
       double modulo()
                                                             8.3
13
                                                             84
                                                                         U.push_back(pp);
14
                                                                    }
           return sqrt(x*x + y*y);
                                                             85
15
                                                             86
                                                             87
                                                                     L.pop_back();
                                                                    L.insert(L.end(), U.begin(), U.end()-1);
                                                             88
18
       point operator+(point o)
                                                                     return L;
                                                             89
19
                                                             90 }
           return point(x+o.x, y+o.y);
20
21
       }
                                                             91
                                                             92 cod area(vector < point > v)
       point operator - (point o)
22
                                                             93 -{
                                                             94
                                                                     int ans = 0;
           return point(x - o.x , y - o.y);
24
                                                                    int aux = (int)v.size();
                                                             9.5
                                                                     for(int i = 2; i < aux; i++)</pre>
                                                             96
       point operator*(cod t)
26
                                                             97
27
                                                                         ans += ((v[i] - v[0])^(v[i-1] - v[0]))/2;
           return point(x*t, y*t);
                                                             98
                                                                    }
       }
                                                             99
29
                                                                    ans = abs(ans);
                                                             100
30
       point operator/(cod t)
                                                                    return ans;
3.1
                                                             102 }
           return point(x/t, y/t);
32
       }
                                                             103
33
                                                             104 int bound(point p1 , point p2)
34
       cod operator*(point o)
                                                             105
                                                             106
                                                                     return __gcd(abs(p1.x-p2.x), abs(p1.y-p2.y));
36
                                                             107 }
           return x*o.x + y*o.y;
37
                                                             108 //teorema de pick [pontos = A - (bound+points)/2 + 1]
       }
       cod operator^(point o)
                                                             109
39
                                                             110 int32_t main()
40
                                                             111 {
41
           return x*o.y - y * o.x;
                                                             112
42
                                                                    int n;
                                                             113
43
       bool operator < (point o)</pre>
                                                                    cin >> n;
                                                             114
44
           if (x != o.x) return x < o.x;
                                                             115
45
                                                                     vector < point > v(n);
46
           return y < o.y;</pre>
                                                                     for(int i = 0; i < n; i++)</pre>
47
                                                             118
```

119

cin >> v[i].x >> v[i].y;

```
}
                                                                 return {y, x - (a / b) * y};
120
                                                           4
                                                          5 }
       vector <point> ch = convex_hull(v);
122
                                                           7 int mod_inverse(int a, int m) {
123
       cout << ch.size() << '\n';
                                                                 auto [x, y] = extended_gcd(a, m);
       for(auto p : ch) cout << p.x << " " << p.y << "\n 9
                                                                 return (x % m + m) % m;
                                                                  Fexp
       return 0;
127
                                                             6.5
128 }
                                                           1 // a^e mod m
       Math
                                                           2 // O(log n)
                                                           4 int fexp(int a, int e, int m) {
       Divisores
   6.1
                                                                 a %= m;
                                                                 int ans = 1;
 _{1} // Retorna um vetor com os divisores de x
                                                                 while (e > 0){
 2 // eh preciso ter o crivo implementado
                                                                    if (e & 1) ans = ans*a % m;
                                                                     a = a*a % m;
 3 // O(divisores)
                                                                     e /= 2;
 5 vector < int > divs(int x){
                                                                 }
       vector < int > ans = {1};
                                                          12
                                                                 return ans%m;
       vector<array<int, 2>> primos; // {primo, expoente 13 }
                                                             6.6 Discrete Log
       while (x > 1) {
          int p = crivo[x], cnt = 0;
10
                                                          1 // Returns minimum x for which a^x = b (mod m), a and
           while (x % p == 0) cnt++, x /= p;
11
                                                                  m are coprime.
           primos.push_back({p, cnt});
                                                           _{2} // if the answer dont need to be greater than some
13
                                                                value, the vector < int > can be removed
                                                         3 int discrete_log(int a, int b, int m) {
       for (int i=0; i<primos.size(); i++){</pre>
1.5
                                                               a \%= m, b \%= m;
           int cur = 1, len = ans.size();
                                                                 int n = sqrt(m) + 1;
           for (int j=0; j<primos[i][1]; j++){</pre>
18
                                                                 int an = 1;
               cur *= primos[i][0];
                                                                 for (int i = 0; i < n; ++i)</pre>
               for (int k=0; k<len; k++)</pre>
20
                                                                     an = (an * 111 * a) % m;
                                                          9
                   ans.push_back(cur*ans[k]);
           }
22
                                                                 unordered_map <int, vector <int>> vals;
                                                          11
23
                                                                 for (int q = 0, cur = b; q <= n; ++q) {</pre>
                                                          12
24
                                                                     vals[cur].push_back(q);
                                                          1.3
       return ans;
25
                                                                     cur = (cur * 111 * a) % m;
                                                          14
26 }
                                                          15
                                                          16
         Equacao Diofantina
                                                                 int res = LLONG_MAX;
                                                          17
                                                          18
 1 // resolve equacao ax + by = c
                                                          19
                                                                 for (int p = 1, cur = 1; p <= n; ++p) {
 2 // retorno {existe sol., x, y, g}
                                                                     cur = (cur * 111 * an) % m;
                                                          20
 3 array<11, 4> find_any_solution(11 a, 11 b, 11 c) {
                                                          21
                                                                     if (vals.count(cur)) {
       auto[x, y, g] = exgcd(a, b);
                                                                         for (int q: vals[cur]){
       if (c % g) return {false, 0, 0, 0};
                                                                             int ans = n * p - q;
                                                          23
       x *= c / g;
                                                                             res = min(res, ans);
       y *= c / g;
                                                          2.5
       return {true, x, y, g};
                                                                     }
                                                          26
 9 }
                                                          27
                                                                 }
                                                          28
                                                                 return res;
   6.3 Crivo
                                                          29 }
                                                                   Exgcd
                                                             6.7
 1 // O(n*log(log(n)))
 2 bool composto[MAX]
 3 for(int i = 1; i <= n; i++) {</pre>
                                                          1 // O retorno da funcao eh {n, m, g}
       if(composto[i]) continue;
                                                          2 // e significa que gcd(a, b) = g e
       for(int j = 2*i; j <= n; j += i)</pre>
                                                          _3 // n e m sao inteiros tais que an + bm = g
           composto[j] = 1;
                                                           4 array<11, 3> exgcd(int a, int b) {
                                                                if(b == 0) return {1, 0, a};
                                                                 auto [m, n, g] = exgcd(b, a % b);
   6.4 Mod Inverse
                                                                 return {n, m - a / b * n, g};
                                                           8 }
 1 array<int, 2> extended_gcd(int a, int b) {
   if (b == 0) return {1, 0};
                                                                  Segment Sieve
                                                             6.8
       auto [x, y] = extended_gcd(b, a % b);
```

30 }

31

```
1 // Retorna quantos primos tem entre [1, r] (inclusivo 32 int unset_kth_bit(int x, int k) {
                                                         33 return x & (~(1 << k));
2 // precisa de um vetor com os primos atÃľ sqrt(r)
                                                          34 }
3 int seg_sieve(int 1, int r){
                                                          3.5
      if (1 > r) return 0;
                                                          36 int toggle_kth_bit(int x, int k) {
      vector < bool > is_prime(r - l + 1, true);
                                                             return x ^ (1 << k);
                                                          37
5
      if (1 == 1) is_prime[0] = false;
                                                          38 }
                                                          3.9
      for (int p : primos){
                                                          40 bool check_power_of_2(int x) {
          if (p * p > r) break;
                                                          41
                                                               return count_on_bits(x) == 1;
           int start = max(p * p, (1 + p - 1) / p * p); 42 }
10
           for (int j = start; j <= r; j += p){</pre>
              if (j >= 1) {
12
                                                                  Search and sort
                   is_prime[j - 1] = false;
13
               }
14
                                                                   Mergeandcount
                                                            8.1
          }
15
16
1.7
      return accumulate(all(is_prime), 011);;
                                                           _{2} // Realiza a mesclagem de dois subarrays e conta o
19 }
                                                                nÞmero de trocas necessÃąrias.
                                                           3 int mergeAndCount(vector<int>& v, int 1, int m, int r
                                                                 ) {
       General
                                                                 int x = m - l + 1; // Tamanho do subarray
                                                           4
                                                                 esquerdo.
  7.1 Struct
                                                                 int y = r - m; // Tamanho do subarray direito.
                                                           6
                                                                 // Vetores temporarios para os subarray esquerdo
                                                           7
1 struct Pessoa {
                                                                 e direito.
      // Atributos
                                                                 vector < int > left(x), right(y);
      string nome;
      int idade:
                                                          1.0
                                                                 for (int i = 0; i < x; i++) left[i] = v[l + i];</pre>
                                                                 for (int j = 0; j < y; j++) right[j] = v[m + 1 +</pre>
                                                          11
      // Comparador
                                                                 j];
      bool operator < (const Pessoa & other) const {
         if(idade != other.idade) return idade > other <math>^{12}
                                                                 int i = 0, j = 0, k = 1;
      .idade:
                                                                 int swaps = 0;
                                                          14
          else return nome > other.nome;
                                                          15
10
                                                          1.6
                                                                 while (i < x && j < y) {
11 }
                                                                     if (left[i] <= right[j]) {</pre>
                                                          17
                                                                        // Se o elemento da esquerda for menor ou
  7.2 Bitwise
                                                                  igual, coloca no vetor original.
                                                                         v[k++] = left[i++];
int check_kth_bit(int x, int k) {
                                                          20
                                                                     } else {
                                                                         // Caso contrario, coloca o elemento da
    return (x >> k) & 1;
                                                          21
                                                                 direita e conta as trocas.
                                                                         v[k++] = right[j++];
                                                          22
5 void print_on_bits(int x) {
                                                          23
                                                                         swaps += (x - i);
   for (int k = 0; k < 32; k++) {
                                                                     }
                                                          2.4
      if (check_kth_bit(x, k)) {
                                                          2.5
         cout << k << ' ';
                                                          26
9
                                                          27
                                                                 // Adiciona os elementos restantes do subarray
    }
                                                                 esquerdo (se houver).
10
                                                                 while (i < x) v[k++] = left[i++];</pre>
    cout << '\n';
11
                                                          28
12 }
                                                          29
                                                                 // Adiciona os elementos restantes do subarray
1.3
                                                          3.0
14 int count_on_bits(int x) {
                                                                 direito (se houver).
   int ans = 0;
                                                                 while (j < y) v[k++] = right[j++];
15
    for (int k = 0; k < 32; k++) {
16
                                                          32
     if (check_kth_bit(x, k)) {
                                                                 return swaps; // Retorna o numero total de
18
        ans++;
                                                                 trocas realizadas.
      }
                                                          34 }
19
    }
20
                                                          35
    return ans;
                                                          36 int mergeSort(vector<int>& v, int 1, int r) {
22 }
                                                          37
                                                                 int swaps = 0;
                                                          38
                                                                 if (1 < r) {</pre>
24 bool is_even(int x) {
                                                          39
25 return ((x & 1) == 0);
                                                          40
                                                                    // Encontra o ponto medio para dividir o
                                                                 vetor.
                                                                    int m = 1 + (r - 1) / 2;
                                                          41
28 int set_kth_bit(int x, int k) {
                                                          42
   return x | (1 << k);
                                                                     // Chama merge sort para a metade esquerda.
```

44

45

swaps += mergeSort(v, 1, m);

// Chama merge sort para a metade direita.

```
9
                                                                    String copy
           swaps += mergeSort(v, m + 1, r);
46
47
           // Mescla as duas metades e conta as trocas.
48
                                                               9.1
                                                                     Z Function
           swaps += mergeAndCount(v, 1, m, r);
49
                                                             vector <int> z_function(string s) {
51
                                                                   int n = s.size();
       return swaps; // Retorna o numero total de
                                                                   vector < int > z(n);
       trocas no vetor.
                                                                   int 1 = 0, r = 0;
53 }
                                                                   for(int i = 1; i < n; i++) {</pre>
                                                                       if(i < r) {</pre>
  8.2
       \mathbf{Dfs}
                                                                            z[i] = min(r - i, z[i - 1]);
                                                                        }
_{1} // Printa os nos na ordem em que s\tilde{\mathtt{A}}čo visitados
                                                                        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
2 // Explora em profundidade
_3 // Complexidade: O(V+A) V = vertices e A = arestas
                                                                            z[i]++;
4 // Espaco: O(V)
                                                                        }
                                                            11
5 // Uso: explorar caminhos e backtracking
                                                                        if(i + z[i] > r) {
                                                            12
                                                                            1 = i;
                                                            13
void dfs(vector<vector<int>>& grafo, int inicio){
                                                                            r = i + z[i];
      set < int > visited;
                                                                        }
                                                            1.5
      stack < int > pilha;
9
                                                            16
10
                                                            17
                                                                   return z;
      pilha.push(inicio);
                                                            18 }
12
       while(!pilha.empty()){
1.3
                                                                     Trie Ponteiros
14
           int cur = pilha.top();
           pilha.pop();
15
                                                             1 // Trie por ponteiros
16
                                                             _{2} // InserÃğÃčo, busca e consulta de prefixo em O(N)
           if(visited.find(cur) == visited.end()){
               cout << cur << " ";
18
                                                             4 struct Node {
               visited.insert(cur);
19
                                                                   Node *filhos[26] = \{\};
                                                                   bool acaba = false;
               for(int vizinho: grafo[cur]){
                                                                   int contador = 0;
                    if(visited.find(vizinho) == visited.
                                                             8 };
      end()){
                        pilha.push(vizinho);
                                                            void insere(string s, Node *raiz) {
                    }
24
                                                                   Node *cur = raiz;
               }
25
                                                                   for(auto &c : s) {
                                                            12
26
           }
                                                                        cur -> contador ++;
       }
27
                                                                        if(cur->filhos[c - 'a'] != NULL) {
                                                            14
                                                                            cur = cur->filhos[c - 'a'];
                                                            16
                                                                            continue;
  8.3
         Bfs
                                                                        }
                                                                        cur->filhos[c - 'a'] = new Node();
                                                            18
_{1} // Printa os nos na ordem em que s\tilde{\mathtt{A}}čo visitados
                                                                        cur = cur -> filhos[c - 'a'];
                                                            19
2 // Explora em largura (camadas)
                                                            20
_3 // Complexidade: O(V+A) V = vertices e A = arestas
                                                            21
                                                                   cur -> contador ++:
4 // Espaco: O(V)
                                                            22
                                                                   cur->acaba = true;
5 // Uso: busca pelo caminho mais curto
                                                            23 }
                                                            24
7 void bfs(vector<vector<int>>&grafo, int inicio){
                                                            25 bool busca(string s, Node *raiz) {
      set <int> visited:
                                                                   Node *cur = raiz:
                                                            26
                                                                   for(auto &c : s) {
       queue < int > fila;
                                                            27
                                                                        if (cur->filhos[c - 'a'] != NULL) {
1.0
                                                            28
       fila.push(inicio);
                                                                            cur = cur->filhos[c - 'a'];
11
                                                            29
       visited.insert(inicio);
                                                                            continue;
                                                            30
13
                                                            31
       while(!fila.empty()){
14
                                                            32
                                                                        return false;
                                                                   }
15
           int cur = fila.front();
                                                            33
           fila.pop();
                                                                   return cur->acaba;
                                                            34
16
                                                            35 }
           cout << cur << " "; // printa o nÃş atual
                                                            36
1.8
                                                            37 // Retorna se Ãľ prefixo e quantas strings tem s como
                                                                    prefixo
           for(int vizinho: grafo[cur]){
20
               if(visited.find(vizinho) == visited.end()38 int isPref(string s, Node *raiz) {
21
      ) {
                                                            39
                                                                   Node *cur = raiz;
                                                                   for(auto &c : s) {
22
                    fila.push(vizinho);
                                                            40
                                                                        if (cur->filhos[c - 'a'] != NULL) {
                    visited.insert(vizinho)
23
                                                            41
               }
                                                                            cur = cur->filhos[c - 'a'];
24
                                                            42
           }
25
                                                                            continue;
                                                                        }
       }
26
                                                            44
27 }
                                                                        return -1;
                                                            45
```

28 };

9.5 Lcs

int lcs(string &s1, string &s2) {

```
int m = s1.size();
                                                           2
47
      return cur -> contador;
                                                           3
                                                                  int n = s2.size();
48 }
                                                           4
                                                                  vector < vector < int >> dp(m + 1, vector < int > (n + 1,
                                                            5
  9.3 Kmp
                                                            6
                                                                  for (int i = 1; i <= m; ++i) {</pre>
vector<int> kmp(string s) {
                                                                      for (int j = 1; j <= n; ++j) {</pre>
                                                           8
      int n = (int)s.length();
                                                                          if (s1[i - 1] == s2[j - 1])
                                                           9
      vector < int > p(n+1);
                                                                               dp[i][j] = dp[i - 1][j - 1] + 1;
                                                           10
      p[0] = -1;
                                                           11
      for (int i = 1; i < n; i++) {</pre>
                                                                               dp[i][j] = max(dp[i - 1][j], dp[i][j]
          int j = p[i-1];
                                                                  - 1]);
           while (j \ge 0 \&\& s[j] != s[i-1])
                                                                      }
              j = p[j-1];
                                                           14
           p[i] = j+1;
                                                           15
      }
10
                                                           16
                                                                  return dp[m][n];
      return p;
                                                           17 }
12 }
                                                                   Countpermutations
                                                             9.6
  9.4 Hashing
                                                           1 // Returns the number of distinct permutations
1 // String Hash template
                                                           2 // that are lexicographically less than the string t
_2 // constructor(s) - O(|s|)
_3 // query(1, r) - returns the hash of the range [1,r] _3 // using the provided frequency (freq) of the
                                                                 characters
      from left to right - O(1)
                                                           4 // O(n*freq.size())
4 // query_inv(l, r) from right to left - O(1)
                                                           5 int countPermLess(vector<int> freq, const string &t)
5 // patrocinado por tiagodfs
                                                                  {
                                                                  int n = t.size();
7 struct Hash {
                                                                 int ans = 0;
      const int X = 2147483647;
9
      const int MOD = 1e9+7;
                                                                  vector < int > fact(n + 1, 1), invfact(n + 1, 1);
      int n; string s;
10
                                                                  for (int i = 1; i <= n; i++)</pre>
      vector < int > h, hi, p;
                                                                      fact[i] = (fact[i - 1] * i) % MOD;
      Hash() {}
12
                                                                  invfact[n] = fexp(fact[n], MOD - 2, MOD);
      Hash(string s): s(s), n(s.size()), h(n), hi(n), p^{12}
                                                                  for (int i = n - 1; i >= 0; i --)
                                                                      invfact[i] = (invfact[i + 1] * (i + 1)) % MOD
           for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1) 14
14
       % MOD;
          for (int i=0; i < n; i++)
                                                                  // For each position in t, try placing a letter
               h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD; 16
                                                                  smaller than t[i] that is in freq
           for (int i=n-1;i>=0;i--)
1.7
                                                                  for (int i = 0; i < n; i++) {</pre>
               hi[i] = (s[i] + (i+1 < n ? hi[i+1]:0) * X) 17
18
                                                                      for (char c = 'a'; c < t[i]; c++) {</pre>
      % MOD;
                                                                          if (freq[c - 'a'] > 0) {
                                                           19
19
                                                                              freq[c - 'a']--;
                                                           20
       int query(int 1, int r) {
                                                                               int ways = fact[n - i - 1];
          int hash = (h[r] - (1 ? h[1-1]*p[r-1+1]%MOD : 21
21
                                                                               for (int f : freq)
                                                           22
                                                                                  ways = (ways * invfact[f]) % MOD;
           return hash < 0 ? hash + MOD : hash;</pre>
                                                                               ans = (ans + ways) % MOD;
                                                           24
23
                                                                               freq[c - 'a']++;
      int query_inv(int 1, int r) {
           int hash = (hi[l] - (r+1 < n ? hi[r+1]*p[r-1]^{26}
25
       +1] % MOD : 0));
                                                                      if (freq[t[i] - 'a'] == 0) break;
           return hash < 0 ? hash + MOD : hash;</pre>
                                                                      freq[t[i] - 'a']--;
                                                           29
27
```

10 Primitives

return ans;

}

30

31