

Competitive Programming Notebook

Programadores Roblox

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DP

\mathbf{Lis}

1.2Lcs

1.3Knapsack

```
1 // dp[i][j] => i-esimo item com j-carga sobrando na
      mochila
2 // O(N * W)
4 for(int j = 0; j < MAXN; j++) {
      dp[0][j] = 0;
6 }
7 for(int i = 1; i <= N; i++) {</pre>
      for(int j = 0; j <= W; j++) {</pre>
          if(items[i].first > j) {
9
10
               dp[i][j] = dp[i-1][j];
           }
               dp[i][j] = max(dp[i-1][j], dp[i-1][j-
13
       items[i].first] + items[i].second);
14
          }
      }
15
16 }
```

String $\mathbf{2}$

Geometry 3

3.1Point Location

```
2 int32_t main(){
       sws;
       int t; cin >> t;
       while (t - -) {
           int x1, y1, x2, y2, x3, y3; cin >> x1 >> y1
      >> x2 >> y2 >> x3 >> y3;
1.0
           int deltax1 = (x1-x2), deltay1 = (y1-y2);
           int compx = (x1-x3), compy = (y1-y3);
13
14
           int ans = (deltax1*compy) - (compx*deltay1);
           if(ans == 0){cout << "TOUCH\n"; continue;}</pre>
           if(ans < 0){cout << "RIGHT\n"; continue;}</pre>
18
           if(ans > 0){cout << "LEFT\n"; continue;}</pre>
19
20
21
       return 0;
22 }
```

Convex Hull

```
#include <bits/stdc++.h>
3 using namespace std;
4 #define int long long
5 typedef int cod;
7 struct point
```

```
cod x,y;
      point(cod x = 0, cod y = 0): x(x), y(y)
       double modulo()
       {
           return sqrt(x*x + y*y);
      point operator+(point o)
           return point(x+o.x, y+o.y);
      point operator - (point o)
           return point(x - o.x , y - o.y);
      point operator*(cod t)
           return point(x*t, y*t);
      point operator/(cod t)
           return point(x/t, y/t);
       cod operator*(point o)
           return x*o.x + y*o.y;
      }
       cod operator^(point o)
           return x*o.y - y * o.x;
      }
      bool operator < (point o)</pre>
           if(x != o.x) return x < o.x;
           return y < o.y;</pre>
      }
49 };
int ccw(point p1, point p2, point p3)
52 {
       cod cross = (p2-p1) ^ (p3-p1);
       if(cross == 0) return 0;
      else if(cross < 0) return -1;</pre>
       else return 1;
59 vector <point> convex_hull(vector<point> p)
60 {
       sort(p.begin(), p.end());
      vector < point > L,U;
      //Lower
       for(auto pp : p)
           while(L.size() >= 2 and ccw(L[L.size() - 2],
      L.back(), pp) == -1)
               // Ãľ -1 pq eu nÃčo quero excluir os
       colineares
               L.pop_back();
           L.push_back(pp);
      reverse(p.begin(), p.end());
      //Upper
       for(auto pp : p)
```

9 10

11

12

14

16 17

18 19 20

21

22

23

24

25

26

27

28

30

3.1

33

34

35

36

37

3.8

39

40

41 42

43 44

4.5

46

47 48

50

53

54

57 **}**

58

64

65

67

68

69

70

73 74

75

78

7.9

80

while(U.size() >= 2 and ccw(U[U.size()-2], U 19

```
// bordo
       .back(), pp) == -1)
                                                                    // if(r==(int)p.size()-1 and ccw(p[0], p[r], e)
8.1
           {
                                                             21
                U.pop_back();
                                                                    ==0) return false;
82
                                                                    // if(r==2 and ccw(p[0], p[1], e)==0) return
           U.push_back(pp);
                                                                    false:
84
                                                                    // if(ccw(p[r], p[r-1], e) == 0) return false;
85
                                                             23
                                                                    return insideT(p[0], p[r-1], p[r], e);
86
                                                             2.4
       L.pop_back();
                                                             25 }
87
       L.insert(L.end(), U.begin(), U.end()-1);
88
                                                             26
       return L:
89
                                                             27
90 }
                                                             28 // Any O(n)
91
92 cod area(vector<point> v)
                                                             30 int inside(vp &p, point pp){
                                                                    // 1 - inside / 0 - boundary / -1 - outside
93 {
                                                             3.1
       int ans = 0;
                                                                    int n = p.size();
94
                                                             32
       int aux = (int)v.size();
                                                             33
                                                                    for(int i=0;i<n;i++){</pre>
                                                                        int j = (i+1) \%n;
       for(int i = 2; i < aux; i++)</pre>
96
                                                             34
                                                                        if(line({p[i], p[j]}).inside_seg(pp))
            ans += ((v[i] - v[0])^(v[i-1] - v[0]))/2;
98
                                                             36
                                                                            return 0;
                                                             37
99
                                                                    int inter = 0;
       ans = abs(ans);
100
                                                             38
       return ans;
                                                                    for(int i=0;i<n;i++){</pre>
                                                             39
                                                                        int j = (i+1) \%n;
102 }
                                                             40
                                                                        if(p[i].x \le pp.x and pp.x \le p[j].x and ccw(p
                                                             41
int bound(point p1 , point p2)
                                                                    [i], p[j], pp)==1)
                                                                            inter++; // up
105 {
       return __gcd(abs(p1.x-p2.x), abs(p1.y-p2.y));
                                                                        else if(p[j].x <= pp.x and pp.x < p[i].x and</pre>
106
                                                             43
107 }
                                                                    ccw(p[i], p[j], pp) == -1)
                                                                            inter++; // down
108 //teorema de pick [pontos = A - (bound+points)/2 + 1] 44
109
110 int32_t main()
                                                             46
                                                                    if(inter%2==0) return -1; // outside
111 {
                                                             47
                                                             48
                                                                    else return 1; // inside
                                                             49 }
       int n:
       cin >> n;
114
115
                                                                    Graph
                                                               4
       vector < point > v(n);
       for(int i = 0; i < n; i++)</pre>
                                                               4.1 Kruskal
118
119
            cin >> v[i].x >> v[i].y;
120
                                                              1 // Ordena as arestas por peso, insere se ja nao
                                                                    estiver no mesmo componente
       vector <point> ch = convex_hull(v);
                                                              2 // O(E log E)
        cout << ch.size() << '\n';
124
                                                             4 struct DSU {
       for(auto p : ch) cout << p.x << " " << p.y << "\n _5
                                                                    vector < int > par, rank, sz;
                                                                    int c;
                                                                    DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
126
       return 0;
                                                                    1, 1), c(n) {
128 }
                                                                        for (int i = 1; i <= n; ++i) par[i] = i;</pre>
   3.3 Inside Polygon
                                                                    int find(int i) {
                                                             10
                                                                        return (par[i] == i ? i : (par[i] = find(par[
 1 // Convex O(logn)
                                                                    il))):
                                                                    }
                                                             12
 3 bool insideT(point a, point b, point c, point e){
                                                                    bool same(int i, int j) {
                                                             13
       int x = ccw(a, b, e);
                                                                        return find(i) == find(j);
 4
                                                             14
       int y = ccw(b, c, e);
                                                                    }
       int z = ccw(c, a, e);
                                                             16
                                                                    int get_size(int i) {
       return !((x==1 or y==1 or z==1) and (x==-1 or y
                                                                        return sz[find(i)];
                                                             17
                                                                    }
       ==-1 \quad or \quad z==-1));
                                                             18
 8 }
                                                                    int count() {
                                                             19
                                                             20
                                                                        return c; // quantos componentes conexos
10 bool inside(vp &p, point e){ // ccw
                                                             21
       int 1=2, r=(int)p.size()-1;
                                                                    int merge(int i, int j) {
11
                                                             22
       while(1<r){
                                                                        if ((i = find(i)) == (j = find(j))) return
12
                                                             23
            int mid = (1+r)/2;
13
           if(ccw(p[0], p[mid], e) == 1)
                                                             24
                                                                        else --c;
               1 = mid + 1:
                                                                        if (rank[i] > rank[j]) swap(i, j);
1.5
                                                             2.5
            else{
16
                                                             26
                                                                        par[i] = j;
                                                                        sz[j] += sz[i];
                r=mid;
           }
                                                                        if (rank[i] == rank[j]) rank[j]++;
                                                             28
18
```

}

} else {

23

```
dist[i][j] = dist[j][i] = linf;
29
          return ;
                                                           2.4
30
                                                           25
31 };
                                                                      }
                                                           26
                                                           27
32
                                                                  for(int i = 0; i < m; i++) {</pre>
33 struct Edge {
     int u, v, w;
                                                                      int u, v, w;
34
                                                           29
                                                                      cin >> u >> v >> w; u--; v--;
      bool operator <(Edge const & other) {</pre>
                                                           30
                                                                      dist[u][v] = min(dist[u][v], w);
          return weight <other.weight;</pre>
3.6
                                                           3.1
                                                                      dist[v][u] = min(dist[v][u], w);
37
                                                           32
38 }
                                                           33
                                                                  floydWarshall();
39
                                                           34
40 vector < Edge > kruskal (int n, vector < Edge > edges) {
                                                           35
                                                                  while(q--) {
41
      vector < Edge > mst;
                                                           3.6
                                                                    int u, v;
      DSU dsu = DSU(n + 1);
                                                                      cin >> u >> v; u--; v--;
                                                           37
42
     sort(edges.begin(), edges.end());
                                                                      if(dist[u][v] == linf) cout << -1 << '\n';</pre>
43
                                                           38
      for (Edge e : edges) {
                                                                      else cout << dist[u][v] << '\n';</pre>
44
                                                           39
45
           if (dsu.find(e.u) != dsu.find(e.v)) {
                                                           40
               mst.push_back(e);
                                                           41 }
46
               dsu.join(e.u, e.v);
                                                              4.4 Bellman Ford
          }
48
      }
49
      return mst;
50
                                                           1 struct Edge {
51 }
                                                                 int u, v, w;
                                                            3 };
  4.2
        Topological Sort
                                                            _{5} // se x = -1, nÃčo tem ciclo
                                                            6 // se x != -1, pegar pais de x pra formar o ciclo
vector < int > adj[MAXN];
vector < int > estado(MAXN); // 0: nao visitado 1:
                                                            8 int n, m;
      processamento 2: processado
                                                           9 vector < Edge > edges;
3 vector < int > ordem;
                                                           10 vector < int > dist(n);
4 bool temCiclo = false;
                                                           vector < int > pai(n, -1);
6 void dfs(int v) {
                                                           12
                                                                  for (int i = 0; i < n; i++) {</pre>
                                                           13
     if(estado[v] == 1) {
          temCiclo = true;
                                                                      x = -1;
                                                           14
                                                                      for (Edge &e : edges) {
                                                           1.5
9
          return;
                                                                          if (dist[e.u] + e.w < dist[e.v]) {</pre>
10
                                                                               dist[e.v] = max(-INF, dist[e.u] + e.w
      if(estado[v] == 2) return;
                                                           17
11
      estado[v] = 1;
                                                                               pai[e.v] = e.u;
      for(auto &nei : adj[v]) {
1.3
                                                                               x = e.v;
                                                           19
           if(estado[v] != 2) dfs(nei);
                                                                          }
                                                           20
1.5
                                                                      }
                                                           2.1
      estado[v] = 2;
                                                           22
17
      ordem.push_back(v);
                                                           23
      return:
18
                                                           24 // achando caminho (se precisar)
                                                           25 for (int i = 0; i < n; i++) x = pai[x];</pre>
  4.3 Floyd Warshall
                                                           26
                                                           27 vector < int > ciclo;
1 // SSP e acha ciclos.
                                                           28 for (int v = x;; v = pai[v]) {
2 // Bom com constraints menores.
                                                                  cycle.push_back(v);
                                                           29
3 // O(n<sup>3</sup>)
                                                           30
                                                                  if (v == x && ciclo.size() > 1) break;
                                                           31 }
5 int dist[501][501];
                                                           32 reverse(ciclo.begin(), ciclo.end());
7 void floydWarshall() {
                                                              4.5 Dfs
      for(int k = 0; k < n; k++) {
           for(int i = 0; i < n; i++) {</pre>
                                                         1 int dfs(int x, int p) {
               for(int j = 0; j < n; j++) {</pre>
                   dist[i][j] = min(dist[i][j], dist[i][ 2 for (auto e : adj[x]) {
                                                                      if (e != p) {
      k] + dist[k][j]);
                                                                          dfs(e, x);
               }
                                                                      }
13
                                                            6
14
      }
                                                            7 }
15 }
16 void solve() {
                                                              4.6 Dijkstra
17
      int m, q;
      cin >> n >> m >> q;
18
      for(int i = 0; i < n; i++) {</pre>
                                                          1 // SSP com pesos positivos.
                                                           2 // O((V + E) log V).
         for(int j = i; j < n; j++) {</pre>
2.0
               if(i == j) {
                   dist[i][j] = dist[j][i] = 0;
                                                            4 vector < int > dijkstra(int S) {
22
```

vector < bool > vis(MAXN, 0);

```
6 DS
      vector<ll> dist(MAXN, LLONG_MAX);
      dist[S] = 0;
      priority_queue <pii, vector <pii>, greater <pii>> pq
                                                            6.1 Ordered Set E Map
      pq.push({0, S});
      while(pq.size()) {
10
          11 v = pq.top().second;
          pq.pop();
          if(vis[v]) continue;
                                                          4 using namespace __gnu_pbds;
13
          vis[v] = 1;
                                                          5 using namespace std;
          for(auto &[peso, vizinho] : adj[v]) {
15
               if(dist[vizinho] > dist[v] + peso) {
                   dist[vizinho] = dist[v] + peso;
                   pq.push({dist[vizinho], vizinho});
18
              }
19
          }
                                                                , less <T>, rb_tree_tag,
20
21
      return dist;
22
23 }
                                                          10
       Math
                                                          11 int main() {
                                                         12
                                                             int i, j, k, n, m;
       Crivo
  5.1
                                                              o_set<int>st;
                                                              st.insert(1);
                                                         14
                                                          15
                                                              st.insert(2):
1 // O(n*log(log(n)))
                                                          16
2 bool composto [MAX]
                                                                elemento
3 for(int i = 1; i <= n; i++) {</pre>
                                                          17
      if(composto[i]) continue;
                                                               elementos menores que k
      for(int j = 2*i; j <= n; j += i)</pre>
                                                              o_map < int , int > mp;
                                                          18
           composto[j] = 1;
                                                              mp.insert({1, 10});
                                                         1.9
7 }
                                                              mp.insert({2, 20});
                                                         20
                                                         21
  5.2
        Exgcd
                                                                esimo elemento
1 // O retorno da funcao eh {n, m, g}
2 // e significa que gcd(a, b) = g e
                                                              return 0;
                                                         24 }
_3 // n e m sao inteiros tais que an + bm = g
4 array<11, 3> exgcd(int a, int b) {
                                                                 Psum 2d
      if(b == 0) return {1, 0, a};
      auto [m, n, g] = exgcd(b, a % b);
      return {n, m - a / b * n, g};
8 }
        Fexp
  5.3
                                                          6 for (int i=1; i<n+1; i++){</pre>
1 // a^e mod m
2 // O(log n)
                                                          8
                                                                    char x; cin >> x;
4 ll fexp(ll a, ll e, ll m) {
                                                                -1][j] - v[i-1][j-1];
      a %= m;
      ll ans = 1;
      while (e > 0){
                                                                -1][j-1];
          if (e & 1) ans = ansa % m;
          a = aa % m;
                                                         12 }
          e /= 2;
                                                         13
10
      }
11
12
      return ans%m;
                                                         17 cin >> x >> y >> z >> w;
      Equacao Diofantina
                                                                 << end1;
_1 // resolve equacao ax + by = c
                                                            6.3 Dsu
2 // retorno {existe sol., x, y, g}
3 array<11, 4> find_any_solution(11 a, 11 b, 11 c) {
      auto[x, y, g] = exgcd(a, b);
                                                          1 struct DSU {
      if (c % g) return {false, 0, 0, 0};
      x *= c / g;
                                                                int c;
                                                          3
      y *= c / g;
      return {true, x, y, g};
                                                                1, 1), c(n) {
9 }
```

```
2 #include < ext/pb_ds/assoc_container.hpp >
3 #include <ext/pb_ds/tree_policy.hpp>
7 template < typename T> using ordered_multiset = tree < T,</pre>
      null_type, less_equal < T>, rb_tree_tag,
      tree_order_statistics_node_update>;
s template <typename T> using o_set = tree<T, null_type
      tree_order_statistics_node_update>;
9 template <typename T, typename R> using o_map = tree <</pre>
      T, R, less<T>, rb_tree_tag,
      tree_order_statistics_node_update>;
    cout << *st.find_by_order(0) << endl; /// k-esimo
    cout << st.order_of_key(2) << endl; ///numero de</pre>
    cout << mp.find_by_order(0) -> second << endl; /// k -</pre>
    cout << mp.order_of_key(2) << endl; /// numero de</pre>
     elementos (chave) menores que k
```

```
1 // entrada: matrix com ponto e X
2 // saber em O(1) quantidade de X em um retangulo
4 vector < vector < int >> v(n+1, vector < int > (n+1, 0));
      for (int j=1; j<n+1; j++){</pre>
           if (x == 'X') v[i][j] += 1 + v[i][j-1] + v[i]
           else v[i][j] = v[i][j-1] + v[i-1][j] - v[i
14 // Pegar retÃćngulo (x, y) - (z, w)
15 // ponto superior esquerdo e inferior direito
18 cout << v[z][w] - v[x-1][w] - v[z][y-1] + v[x-1][y-1]
```

```
vector < int > par, rank, sz;
DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
    for (int i = 1; i <= n; ++i) par[i] = i;</pre>
```

```
n = (int)v.size();
                                                          4.5
      int find(int i) {
                                                                     t.assign(n * 4, neutral);
                                                          46
                                                                     lazy.assign(n * 4, 0);
          return (par[i] == i ? i : (par[i] = find(par[47
                                                                     replace.assign(n * 4, false);
                                                                     build(1, 0, n - 1, v);
      bool same(int i, int j) {
                                                                 }
10
                                                          50
          return find(i) == find(j);
                                                                 void build(ll *bg, ll *en) {
                                                          51
                                                                     build(vector<11>(bg, en));
                                                          5.2
      int get_size(int i) {
13
                                                          53
          return sz[find(i)];
                                                                 11 query(int p, int l, int r, int L, int R) {
                                                          54
      }
                                                                     push(p, 1, r);
15
                                                          55
      int count() {
                                                          56
                                                                     if (1 > R || r < L) return neutral;</pre>
                                                                     if (1 >= L && r <= R) return t[p];</pre>
          return c; // quantos componentes conexos
                                                          5.7
                                                                     int mid = (1 + r) / 2;
                                                          58
18
19
      int merge(int i, int j) {
                                                          59
                                                                     auto ql = query(lc(p), l, mid, L, R);
          if ((i = find(i)) == (j = find(j))) return
                                                                     auto qr = query(rc(p), mid + 1, r, L, R);
20
                                                          60
                                                          61
                                                                     return merge(ql, qr);
           else --c:
                                                          62
                                                                 11 query(int 1, int r) { return query(1, 0, n -
          if (rank[i] > rank[j]) swap(i, j);
                                                          63
23
          par[i] = j;
                                                                 1, 1, r); }
          sz[j] += sz[i];
                                                                 void update(int p, int l, int r, int L, int R, 11
24
                                                          64
           if (rank[i] == rank[j]) rank[j]++;
                                                                  val, bool repl = 0) {
25
                                                                     push(p, 1, r);
26
           return j;
                                                          6.5
      }
                                                                     if (1 > R || r < L) return;</pre>
27
                                                                     if (1 >= L && r <= R) {
28 };
                                                          6.7
                                                                         lazy[p] = val;
                                                          68
  6.4 Segtree Sum
                                                          69
                                                                         replace[p] = repl;
                                                                         push(p, 1, r);
                                                          70
                                                                     } else {
                                                          71
struct SegTree {
                                                                         int mid = (1 + r) / 2;
      ll merge(ll a, ll b) { return a + b; }
                                                          7.2
                                                          73
                                                                         update(lc(p), l, mid, L, R, val, repl);
      const ll neutral = 0;
      int n;
                                                          74
                                                                         update(rc(p), mid + 1, r, L, R, val, repl
                                                                 );
      vector<1l> t, lazy;
      vector < bool > replace;
                                                          75
                                                                          t[p] = merge(t[lc(p)], t[rc(p)]);
                                                                     }
      inline int lc(int p) { return p * 2; }
                                                          76
      inline int rc(int p) { return p * 2 + 1; }
                                                                 void sumUpdate(int 1, int r, 11 val) { update(1,
      void push(int p, int 1, int r) {
9
           if (replace[p]) {
                                                                 0, n - 1, 1, r, val, 0); }
1.0
              t[p] = lazy[p] * (r - l + 1);
                                                                 void assignUpdate(int 1, int r, 11 val) { update
                                                                 (1, 0, n - 1, 1, r, val, 1); }
               if (1 != r) {
                   lazy[lc(p)] = lazy[p];
                                                          80 } segsum;
13
                   lazy[rc(p)] = lazy[p];
                                                             6.5 Bit
                   replace[lc(p)] = true;
1.5
                   replace[rc(p)] = true;
16
               }
                                                          1 class BIT {
          } else if (lazy[p] != 0) {
                                                              vector<int> bit;
18
                                                          2
               t[p] += lazy[p] * (r - 1 + 1);
                                                                 int n;
               if (1 != r) {
                                                                 int sum(int idx) {
20
21
                   lazy[lc(p)] += lazy[p];
                                                                     int result = 0;
                                                                     while (idx > 0) {
                   lazy[rc(p)] += lazy[p];
                                                                         result += bit[idx];
          }
                                                                          idx -= idx & -idx;
          replace[p] = false;
                                                                     }
25
          lazy[p] = 0;
                                                                     return result;
      void build(int p, int l, int r, const vector<ll> 12
28
                                                          13 public:
          if (1 == r) {
                                                                 BIT(int size) {
                                                          14
              t[p] = v[1];
                                                                     n = size;
                                                                     bit.assign(n + 1, 0); // BIT indexada em 1
31
          } else {
                                                          16
               int mid = (1 + r) / 2;
                                                          17
32
               build(lc(p), l, mid, v);
33
                                                          18
                                                                 void update(int idx, int delta) {
                                                                     while (idx <= n) {</pre>
               build(rc(p), mid + 1, r, v);
                                                          19
3.4
               t[p] = merge(t[lc(p)], t[rc(p)]);
                                                          20
                                                                         bit[idx] += delta;
          }
                                                                         idx += idx & -idx;
36
                                                          21
37
                                                          22
      void build(int _n) {
                                                          23
38
          n = _n;
                                                          24
                                                                 int query(int idx) {
39
          t.assign(n * 4, neutral);
                                                                     return sum(idx);
                                                          25
          lazy.assign(n * 4, 0);
41
                                                          26
          replace.assign(n * 4, false);
                                                                 int range_query(int 1, int r) {
                                                          27
      }
                                                                     return sum(r) - sum(l - 1);
43
                                                          28
      void build(const vector<11> &v) {
                                                          29
44
```

```
30 };
                                                                  void update(int idx, int value) {
                                                           56
                                                           57
                                                                      update(0, 0, n - 1, idx, value);
32 BIT fenwick(n);
                                                           5.8
33 for(int i = 1; i <= n; i++) {
                                                           59
                                                                  int query(int 1, int r) {
      fenwick.update(i, arr[i]);
                                                           60
                                                                      return query(0, 0, n - 1, 1, r);
35
                                                           61
                                                           62 };
  6.6 Segtree Gcd
                                                                   Search
                                                              7
int gcd(int a, int b) {
      if (b == 0)
                                                                   \mathbf{Dfs}
                                                             7.1
          return a;
      return gcd(b, a % b);
                                                           1 // Printa os nÃşs na ordem em que sÃčo visitados
5 }
                                                            2 // Explora os nÃşs em profundidade
                                                            3 // Complexidade: O(V+A) V = v\tilde{A}irtices e A = arestas
7 class SegmentTreeGCD {
8 \ \text{private}:
                                                            4 // EspaÃğo: O(V)
                                                            5 // Uso: explorar caminhos e backtracking
      vector < int > tree;
1.0
      int n:
                                                            7 void dfs(vector<vector<int>>& grafo, int inicio){
                                                                 set < int > visited;
      void build(const vector<int>& arr, int node, int 8
12
                                                                  stack<int> pilha;
      start, int end) {
          if (start == end) {
                                                           1.0
13
               tree[node] = arr[start];
                                                                  pilha.push(inicio);
14
           } else {
15
                                                                  while(!pilha.empty()){
16
               int mid = (start + end) / 2;
                                                           13
               build(arr, 2 * node + 1, start, mid);
                                                                      int cur = pilha.top();
17
               build(arr, 2 * node + 2, mid + 1, end);
                                                                      pilha.pop();
                                                          15
               tree[node] = gcd(tree[2 * node + 1], tree 16
19
                                                                      if(visited.find(cur) == visited.end()){
       [2 * node + 2]);
                                                           1.7
                                                                          cout << cur << " ";
                                                           18
20
          }
                                                           19
                                                                          visited.insert(cur);
21
                                                           20
                                                                           for(int vizinho: grafo[cur]){
       void update(int node, int start, int end, int idx 21
23
                                                                               if(visited.find(vizinho) == visited.
       , int value) {
                                                                  end()){
           if (start == end) {
24
                                                                                   pilha.push(vizinho);
               tree[node] = value;
                                                                               }
           } else {
                                                           24
               int mid = (start + end) / 2;
                                                                          }
27
                                                                      }
               if (idx <= mid) {</pre>
                                                           26
                   update(2 * node + 1, start, mid, idx, ^{27}
29
        value):
               } else {
30
                                                             7.2 Bfs
                   update(2 * node + 2, mid + 1, end,
31
       idx. value):
                                                            1 // Printa os nÃşs na ordem em que sÃčo visitados
              }
32
               tree[node] = gcd(tree[2 * node + 1], tree 2 // Explora os nÃşs em largura (camadas)
                                                            3 // Complexidade: O(V+A) V = vÃl'rtices e A = arestas
       [2 * node + 2]);
34
           }
                                                            4 // EspaÃğo: O(V)
35
      }
                                                            5 // Uso: busca pelo caminho mais curto
36
       int query(int node, int start, int end, int 1,
                                                           void bfs(vector<vector<int>>&grafo, int inicio){
                                                                 set<int> visited;
      int r) {
           if (r < start || 1 > end) {
                                                                  queue < int > fila;
39
               return 0;
                                                           1.0
           }
                                                           11
                                                                  fila.push(inicio);
40
           if (1 <= start && end <= r) {</pre>
                                                                  visited.insert(inicio);
                                                           12
               return tree[node];
42
                                                           13
           }
                                                                  while(!fila.empty()){
44
           int mid = (start + end) / 2;
                                                                      int cur = fila.front();
           int left_gcd = query(2 * node + 1, start, mid 16
                                                                      fila.pop();
45
       , 1, r);
                                                                      cout << cur << " "; // printa o nÃş atual
          int right_gcd = query(2 * node + 2, mid + 1, 18
46
      end, 1, r);
          return gcd(left_gcd, right_gcd);
                                                                      for(int vizinho: grafo[cur]){
47
                                                           20
                                                                           if(visited.find(vizinho) == visited.end()
48
                                                           21
49
50 public:
                                                           22
                                                                               fila.push(vizinho);
      SegmentTreeGCD(const vector<int>& arr) {
                                                                               visited.insert(vizinho)
51
                                                           23
          n = arr.size():
                                                                          }
52
                                                           24
           tree.resize(4 * n);
                                                                      }
                                                           25
           build(arr, 0, 0, n - 1);
                                                                  }
5.4
                                                           26
                                                           27 }
5.5
```

8 Primitives

9 General

9.1 Struct

```
int check_kth_bit(int x, int k) {
   return (x >> k) & 1;
}

void print_on_bits(int x) {
   for (int k = 0; k < 32; k++) {
      if (check_kth_bit(x, k)) {
      cout << k << ', ';
   }
}</pre>
```

```
cout << '\n';
11
12 }
13
14 int count_on_bits(int x) {
int ans = 0;
    for (int k = 0; k < 32; k++) {
16
    if (check_kth_bit(x, k)) {
17
18
       ans++;
     }
19
20 }
21
    return ans;
22 }
24 bool is_even(int x) {
return ((x & 1) == 0);
28 int set_kth_bit(int x, int k) {
29 return x | (1 << k);
30 }
31
32 int unset_kth_bit(int x, int k) {
   return x & (~(1 << k));
3.3
34 }
35
36 int toggle_kth_bit(int x, int k) {
37 return x ^ (1 << k);
38 }
39
40 bool check_power_of_2(int x) {
return count_on_bits(x) == 1;
42 }
```