# Competitive Programming Notebook

## Programadores Roblox

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# DP

#### $_{ m Lis}$ 1.1

#### 1.2Lcs

#### 1.3Knapsack

```
1 // dp[i][j] => i-esimo item com j-carga sobrando na
      mochila
2 // O(N * W)
4 for(int j = 0; j < MAXN; j++) {</pre>
       dp[0][j] = 0;
6 }
7 for(int i = 1; i <= N; i++) {</pre>
      for(int j = 0; j <= W; j++) {</pre>
          if(items[i].first > j) {
               dp[i][j] = dp[i-1][j];
10
           }
11
12
               dp[i][j] = max(dp[i-1][j], dp[i-1][j-
13
       items[i].first] + items[i].second);
14
           }
15
16 }
```

### String

### 3 Geometry

### Graph

#### Kruskal 4.1

```
_{1} // Ordena as arestas por peso, insere se ja nao
      estiver no mesmo componente
2 // O(E log E)
4 struct DSU {
      vector < int > par, rank, sz;
      DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
      1, 1), c(n) {
          for (int i = 1; i <= n; ++i) par[i] = i;</pre>
9
      int find(int i) {
          return (par[i] == i ? i : (par[i] = find(par[ 5 int dist[501][501];
      i])));
      }
      bool same(int i, int j) {
13
          return find(i) == find(j);
15
      int get_size(int i) {
16
          return sz[find(i)];
      }
18
      int count() {
          return c; // quantos componentes conexos
20
21
      int merge(int i, int j) {
22
           if ((i = find(i)) == (j = find(j))) return
23
           else --c:
24
           if (rank[i] > rank[j]) swap(i, j);
          par[i] = j;
26
          sz[j] += sz[i];
27
```

```
if (rank[i] == rank[j]) rank[j]++;
28
29
           return j;
30
31 };
33 struct Edge {
       int u, v, w;
      bool operator <(Edge const & other) {</pre>
3.5
           return weight <other.weight;
37
38 }
40 vector < Edge > kruskal(int n, vector < Edge > edges) {
      vector < Edge > mst;
41
       DSU dsu = DSU(n + 1);
42
       sort(edges.begin(), edges.end());
43
44
       for (Edge e : edges) {
           if (dsu.find(e.u) != dsu.find(e.v)) {
45
               mst.push_back(e);
47
                dsu.join(e.u, e.v);
48
       }
49
       return mst;
5.0
51 }
```

### Topological Sort

```
vector < int > adj [MAXN];
vector <int> estado(MAXN); // 0: nao visitado 1:
     processamento 2: processado
3 vector<int> ordem;
4 bool temCiclo = false;
6 void dfs(int v) {
     if(estado[v] == 1) {
          temCiclo = true;
          return;
10
11
      if(estado[v] == 2) return;
     estado[v] = 1;
12
      for(auto &nei : adj[v]) {
          if(estado[v] != 2) dfs(nei);
14
15
16
      estado[v] = 2;
      ordem.push_back(v);
17
```

### 4.3 Floyd Warshall

```
1 // SSP e acha ciclos.
2 // Bom com constraints menores.
3 // O(n<sup>3</sup>)
7 void floydWarshall() {
       for(int k = 0; k < n; k++) {</pre>
           for(int i = 0; i < n; i++) {</pre>
               for(int j = 0; j < n; j++) {
10
                    dist[i][j] = min(dist[i][j], dist[i][
11
       k] + dist[k][j]);
               }
           }
14
15 }
16 void solve() {
      int m, q;
17
       cin >> n >> m >> q;
18
       for(int i = 0; i < n; i++) {</pre>
1.9
           for(int j = i; j < n; j++) {
20
               if(i == j) {
21
                    dist[i][j] = dist[j][i] = 0;
22
```

```
1 // a^e mod m
               } else {
                                                           2 // O(log n)
24
                   dist[i][j] = dist[j][i] = linf;
2.5
          }
                                                           4 ll fexp(ll a, ll e, ll m) {
                                                                 a %= m;
                                                                  ll ans = 1;
      for(int i = 0; i < m; i++) {</pre>
28
                                                                  while (e > 0){
           int u, v, w;
           cin >> u >> v >> w; u--; v--;
                                                                      if (e & 1) ans = ansa % m;
3.0
           dist[u][v] = min(dist[u][v], w);
                                                                      a = aa \% m;
31
                                                                      e /= 2;
           dist[v][u] = min(dist[v][u], w);
      }
                                                                  }
33
                                                           11
      floydWarshall();
                                                           12
                                                                  return ans%m;
      while (q - -) {
                                                           13 }
3.5
          int u, v;
36
                                                                    Equação Diofantina
           cin >> u >> v; u--; v--;
3.7
           if(dist[u][v] == linf) cout << -1 << '\n';</pre>
38
39
           else cout << dist[u][v] << '\n';</pre>
                                                            1 // resolve equacao ax + by = c
                                                            2 // retorno {existe sol., x, y, g}
40
41 }
                                                            3 array<11, 4> find_any_solution(11 a, 11 b, 11 c) {
                                                                  auto[x, y, g] = exgcd(a, b);
  4.4 Dijkstra
                                                                  if (c % g) return {false, 0, 0, 0};
                                                                  x *= c / g;
                                                            6
                                                                  y *= c / g;
1 // SSP com pesos positivos.
                                                                  return {true, x, y, g};
_{2} // O((V + E) log V).
                                                           9 }
4 vector < int > dijkstra(int S) {
      vector < bool > vis(MAXN, 0);
                                                             6
                                                                  \mathbf{DS}
      vector <11 > dist(MAXN, LLONG_MAX);
      dist[S] = 0;
      priority_queue <pii, vector <pii>, greater <pii>> pq 6.1 Ordered Set E Map
9
      pq.push({0, S});
                                                            # include < ext/pb_ds/assoc_container.hpp>
      while(pq.size()) {
10
          11 v = pq.top() second;
                                                            # include < ext/pb_ds/tree_policy.hpp>
          pq.pop();
                                                            4 using namespace __gnu_pbds;
           if(vis[v]) continue;
                                                           5 using namespace std;
13
14
           vis[v] = 1;
          for(auto &[peso, vizinho] : adj[v]) {
                                                            7 template < typename T > using ordered_multiset = tree < T,</pre>
15
               if(dist[vizinho] > dist[v] + peso) {
                                                                  null_type, less_equal < T>, rb_tree_tag,
16
                   dist[vizinho] = dist[v] + peso;
                                                                  tree_order_statistics_node_update>;
                   pq.push({dist[vizinho], vizinho});
                                                           8 template <typename T> using o_set = tree<T, null_type</pre>
1.8
                                                                  , less <T>, rb_tree_tag,
               }
19
          }
                                                                  tree_order_statistics_node_update>;
20
      }
                                                            9 template <typename T, typename R> using o_map = tree <
21
                                                                  T, R, less<T>, rb_tree_tag,
22
      return dist;
23
                                                                  tree_order_statistics_node_update>;
                                                           11 int main() {
       Math
                                                           12 int i, j, k, n, m;
                                                                o_set<int>st;
                                                           13
       \operatorname{Crivo}
  5.1
                                                           14
                                                                st.insert(1):
                                                           1.5
                                                                st.insert(2):
1 // O(n*log(log(n)))
                                                                cout << *st.find_by_order(0) << endl; /// k-esimo</pre>
                                                           16
2 bool composto[MAX]
                                                                  elemento
3 for(int i = 1; i <= n; i++) {</pre>
                                                                cout << st.order_of_key(2) << endl; ///numero de</pre>
                                                           1.7
      if(composto[i]) continue;
                                                                 elementos menores que k
                                                                o_map < int , int > mp;
      for(int j = 2*i; j <= n; j += i)
                                                           18
                                                                mp.insert({1, 10});
           composto[j] = 1;
                                                           19
7 }
                                                                mp.insert({2, 20});
                                                           20
                                                                cout << mp.find_by_order(0)->second << endl; /// k-</pre>
                                                           21
  5.2 Exgcd
                                                                  esimo elemento
                                                                cout << mp.order_of_key(2) << endl; /// numero de</pre>
                                                                  elementos (chave) menores que k
1 // O retorno da funcao eh {n, m, g}
2 // e significa que gcd(a, b) = g e
                                                           23
                                                                return 0;
3 // n e m sao inteiros tais que an + bm = g
4 array<11, 3> exgcd(int a, int b) {
                                                             6.2 Dsu
      if(b == 0) return {1, 0, a};
      auto [m, n, g] = exgcd(b, a % b);
                                                            1 struct DSU {
      return {n, m - a / b * n, g};
                                                                 vector < int > par, rank, sz;
8 }
                                                            2
  5.3 Fexp
                                                                  DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
                                                                  1, 1), c(n) {
```

```
6 for (int k = 0; k < 32; k++) {</pre>
6
      int find(int i) {
                                                         if (check_kth_bit(x, k)) {
        return (par[i] == i ? i : (par[i] = find(par[ 8
                                                           cout << k << ' ';
      i])));
                                                    10 }
     }
9
      bool same(int i, int j) {
                                                        cout << '\n';
10
                                                    11
        return find(i) == find(j);
                                                    12 }
11
12
                                                    13
     int get_size(int i) {
                                                    14 int count_on_bits(int x) {
         return sz[find(i)];
                                                    int ans = 0;
14
15
                                                    16
                                                        for (int k = 0; k < 32; k++) {
     int count() {
                                                         if (check_kth_bit(x, k)) {
16
         return c; // quantos componentes conexos
                                                           ans++;
17
                                                    18
                                                        }
                                                    19
     int merge(int i, int j) {
                                                        }
19
                                                    20
         if ((i = find(i)) == (j = find(j))) return
                                                    21
                                                        return ans;
                                                    22 }
         else --c;
         if (rank[i] > rank[j]) swap(i, j);
                                                    24 bool is_even(int x) {
22
         par[i] = j;
                                                    25
                                                       return ((x & 1) == 0);
23
                                                    26 }
         sz[j] += sz[i];
         if (rank[i] == rank[j]) rank[j]++;
                                                    27
2.5
         return j;
                                                    28 int set_kth_bit(int x, int k) {
     }
                                                    29 return x | (1 << k);
27
                                                    30 }
28 };
                                                    31
      Primitives
                                                    32 int unset_kth_bit(int x, int k) {
                                                    33 return x & (~(1 << k));
                                                    34 }
      General
                                                    35
                                                    36 int toggle_kth_bit(int x, int k) {
                                                    37  return x ^ (1 << k);</pre>
      \mathbf{Bitwise}
  8.1
                                                    38 }
                                                    39
                                                    40 bool check_power_of_2(int x) {
int check_kth_bit(int x, int k) {
                                                    return count_on_bits(x) == 1;
```

```
return (x >> k) & 1;
3 }
```