

# Competitive Programming Notebook

Programadores Roblox

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# 1 String

## 1.1 Trie Ponteiros

```

1 // Trie por ponteiros
2 // Inserir, busca e consulta de prefixo em O(N)
3
4 struct Node {
5     Node *filhos[26] = {};
6     bool acaba = false;
7     int contador = 0;
8 };
9
10 void insere(string s, Node *raiz) {
11     Node *cur = raiz;
12     for(auto &c : s) {
13         cur->contador++;
14         if(cur->filhos[c - 'a'] != NULL) {
15             cur = cur->filhos[c - 'a'];
16             continue;
17         }
18         cur->filhos[c - 'a'] = new Node();
19         cur = cur->filhos[c - 'a'];
20     }
21     cur->contador++;
22     cur->acaba = true;
23 }
24
25 bool busca(string s, Node *raiz) {
26     Node *cur = raiz;
27     for(auto &c : s) {
28         if (cur->filhos[c - 'a'] != NULL) {
29             cur = cur->filhos[c - 'a'];
30             continue;
31         }
32         return false;
33     }
34     return cur->acaba;
35 }
36
37 // Retorna se Ã prefixo e quantas strings tem s como
38 // prefixo
39 int isPref(string s, Node *raiz) {
40     Node *cur = raiz;
41     for(auto &c : s) {
42         if (cur->filhos[c - 'a'] != NULL) {
43             cur = cur->filhos[c - 'a'];
44             continue;
45         }
46         return -1;
47     }
48     return cur->contador;
49 }

```

## 1.2 Trie

```

1 // Trie por array
2 // Inserir, busca e consulta de prefixo em O(N)
3
4 int trie[MAXN][26];
5 int tot_nos = 0;
6 vector<bool> acaba(MAXN, false);
7 vector<int> contador(MAXN, 0);
8
9 void insere(string s) {
10     int no = 0;
11     for(auto &c : s) {
12         if(trie[no][c - 'a'] == 0) {
13             trie[no][c - 'a'] = ++tot_nos;
14         }
15         no = trie[no][c - 'a'];
16         contador[no]++;

```

```

17     }
18     acaba[no] = true;
19 }
20
21 bool busca(string s) {
22     int no = 0;
23     for(auto &c : s) {
24         if(trie[no][c - 'a'] == 0) {
25             return false;
26         }
27         no = trie[no][c - 'a'];
28     }
29     return acaba[no];
30 }
31
32 int isPref(string s) {
33     int no = 0;
34     for(auto &c : s) {
35         if(trie[no][c - 'a'] == 0){
36             return -1;
37         }
38         no = trie[no][c - 'a'];
39     }
40     return contador[no];
41 }

```

## 1.3 Hashing

```

1 // String Hash template
2 // constructor(s) - O(|s|)
3 // query(l, r) - returns the hash of the range [l,r]
4 // from left to right - O(1)
5 // query_inv(l, r) from right to left - O(1)
6 // patrocinado por tiagodfs
7
8 struct Hash {
9     const int X = 2147483647;
10    const int MOD = 1e9+7;
11    int n; string s;
12    vector<int> h, hi, p;
13    Hash() {}
14    Hash(string s): s(s), n(s.size()), h(n), hi(n), p
15    (n) {
16        for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1)
17        % MOD;
18        for (int i=0;i<n;i++)
19            h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD;
20        for (int i=n-1;i>=0;i--)
21            hi[i] = (s[i] + (i+1<n ? hi[i+1]:0) * X)
22            % MOD;
23    }
24    int query(int l, int r) {
25        int hash = (h[r] - (l ? h[l-1]*p[r-l+1]%MOD :
26        0));
27        return hash < 0 ? hash + MOD : hash;
28    }
29    int query_inv(int l, int r) {
30        int hash = (hi[l] - (r+1 < n ? hi[r+1]*p[r-l
31        +1] % MOD : 0));
32        return hash < 0 ? hash + MOD : hash;
33    }
34 };

```

## 1.4 Lcs

```

1 int lcs(string &s1, string &s2) {
2     int m = s1.size();
3     int n = s2.size();
4
5     vector<vector<int>> dp(m + 1, vector<int>(n + 1,
6     0));

```

```

7   for (int i = 1; i <= m; ++i) {
8       for (int j = 1; j <= n; ++j) {
9           if (s1[i - 1] == s2[j - 1])
10              dp[i][j] = dp[i - 1][j - 1] + 1;
11           else
12              dp[i][j] = max(dp[i - 1][j], dp[i][j
13 - 1]);
14       }
15   }
16   return dp[m][n];
17 }

```

## 1.5 Countpermutations

```

1 // Returns the number of distinct permutations
2 // that are lexicographically less than the string t
3 // using the provided frequency (freq) of the
4 // characters
5 // 0(n*freq.size())
6 int countPermLess(vector<int> freq, const string &t)
7 {
8     int n = t.size();
9     int ans = 0;
10
11     vector<int> fact(n + 1, 1), invfact(n + 1, 1);
12     for (int i = 1; i <= n; i++)
13         fact[i] = (fact[i - 1] * i) % MOD;
14     invfact[n] = fexp(fact[n], MOD - 2, MOD);
15     for (int i = n - 1; i >= 0; i--)
16         invfact[i] = (invfact[i + 1] * (i + 1)) % MOD;
17
18     // For each position in t, try placing a letter
19     // smaller than t[i] that is in freq
20     for (int i = 0; i < n; i++) {
21         for (char c = 'a'; c < t[i]; c++) {
22             if (freq[c - 'a'] > 0) {
23                 freq[c - 'a']--;
24                 int ways = fact[n - i - 1];
25                 for (int f : freq)
26                     ways = (ways * invfact[f]) % MOD;
27                 ans = (ans + ways) % MOD;
28                 freq[c - 'a']++;
29             }
30         }
31         if (freq[t[i] - 'a'] == 0) break;
32         freq[t[i] - 'a']--;
33     }
34     return ans;
35 }

```

## 1.6 Z Function

```

1 vector<int> z_function(string s) {
2     int n = s.size();
3     vector<int> z(n);
4     int l = 0, r = 0;
5     for (int i = 1; i < n; i++) {
6         if (i < r) {
7             z[i] = min(r - i, z[i - l]);
8         }
9         while (i + z[i] < n && s[z[i]] == s[i + z[i]])
10            z[i]++;
11     }
12     if (i + z[i] > r) {
13         l = i;
14         r = i + z[i];
15     }
16 }
17 return z;

```

```

18 }

```

## 1.7 Kmp

```

1 vector<int> kmp(string s) {
2     int n = (int)s.length();
3     vector<int> p(n+1);
4     p[0] = -1;
5     for (int i = 1; i < n; i++) {
6         int j = p[i-1];
7         while (j >= 0 && s[j] != s[i-1])
8             j = p[j-1];
9         p[i] = j+1;
10    }
11    return p;
12 }

```

## 2 String copy

### 2.1 Trie Ponteiros

```

1 // Trie por ponteiros
2 // Inserir e buscar prefixo, busca e consulta de prefixo em O(N)
3
4 struct Node {
5     Node *filhos[26] = {};
6     bool acaba = false;
7     int contador = 0;
8 };
9
10 void insere(string s, Node *raiz) {
11     Node *cur = raiz;
12     for (auto &c : s) {
13         cur->contador++;
14         if (cur->filhos[c - 'a'] != NULL) {
15             cur = cur->filhos[c - 'a'];
16             continue;
17         }
18         cur->filhos[c - 'a'] = new Node();
19         cur = cur->filhos[c - 'a'];
20     }
21     cur->contador++;
22     cur->acaba = true;
23 }
24
25 bool busca(string s, Node *raiz) {
26     Node *cur = raiz;
27     for (auto &c : s) {
28         if (cur->filhos[c - 'a'] != NULL) {
29             cur = cur->filhos[c - 'a'];
30             continue;
31         }
32         return false;
33     }
34     return cur->acaba;
35 }
36
37 // Retorna se Ãl prefixo e quantas strings tem s como
38 // prefixo
39 int isPref(string s, Node *raiz) {
40     Node *cur = raiz;
41     for (auto &c : s) {
42         if (cur->filhos[c - 'a'] != NULL) {
43             cur = cur->filhos[c - 'a'];
44             continue;
45         }
46         return -1;
47     }
48     return cur->contador;
49 }

```

## 2.2 Hashing

```

1 // String Hash template
2 // constructor(s) - O(|s|)
3 // query(l, r) - returns the hash of the range [l,r]
  from left to right - O(1)
4 // query_inv(l, r) from right to left - O(1)
5 // patrocinado por tiagodfs
6
7 mt19937 rng(time(nullptr));
8
9 struct Hash {
10     const int X = rng();
11     const int MOD = 1e9+7;
12     int n; string s;
13     vector<int> h, hi, p;
14     Hash() {}
15     Hash(string s): s(s), n(s.size()), h(n), hi(n), p
      (n) {
16         for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1)
            % MOD;
17         for (int i=0;i<n;i++)
18             h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD;
19         for (int i=n-1;i>=0;i--)
20             hi[i] = (s[i] + (i+1<n ? hi[i+1]:0) * X)
                % MOD;
21     }
22     int query(int l, int r) {
23         int hash = (h[r] - (l ? h[l-1]*p[r-l+1]%MOD :
            0));
24         return hash < 0 ? hash + MOD : hash;
25     }
26     int query_inv(int l, int r) {
27         int hash = (hi[l] - (r+1 < n ? hi[r+1]*p[r-l
            +1] % MOD : 0));
28         return hash < 0 ? hash + MOD : hash;
29     }
30 };

```

## 2.3 Lcs

```

1 int lcs(string &s1, string &s2) {
2     int m = s1.size();
3     int n = s2.size();
4
5     vector<vector<int>> dp(m + 1, vector<int>(n + 1,
        0));
6
7     for (int i = 1; i <= m; ++i) {
8         for (int j = 1; j <= n; ++j) {
9             if (s1[i - 1] == s2[j - 1])
10                 dp[i][j] = dp[i - 1][j - 1] + 1;
11             else
12                 dp[i][j] = max(dp[i - 1][j], dp[i][j
                    - 1]);
13         }
14     }
15
16     return dp[m][n];
17 }

```

## 2.4 Countpermutations

```

1 // Returns the number of distinct permutations
2 // that are lexicographically less than the string t
3 // using the provided frequency (freq) of the
  characters
4 // O(n*freq.size())
5 int countPermLess(vector<int> freq, const string &t)
    {
6     int n = t.size();
7     int ans = 0;

```

```

8
9     vector<int> fact(n + 1, 1), invfact(n + 1, 1);
10    for (int i = 1; i <= n; i++)
11        fact[i] = (fact[i - 1] * i) % MOD;
12    invfact[n] = fexp(fact[n], MOD - 2, MOD);
13    for (int i = n - 1; i >= 0; i--)
14        invfact[i] = (invfact[i + 1] * (i + 1)) % MOD
        ;
15
16    // For each position in t, try placing a letter
  smaller than t[i] that is in freq
17    for (int i = 0; i < n; i++) {
18        for (char c = 'a'; c < t[i]; c++) {
19            if (freq[c - 'a'] > 0) {
20                freq[c - 'a']--;
21                int ways = fact[n - i - 1];
22                for (int f : freq)
23                    ways = (ways * invfact[f]) % MOD;
24                ans = (ans + ways) % MOD;
25                freq[c - 'a']++;
26            }
27        }
28        if (freq[t[i] - 'a'] == 0) break;
29        freq[t[i] - 'a']--;
30    }
31    return ans;
32 }

```

## 2.5 Z Function

```

1 vector<int> z_function(string s) {
2     int n = s.size();
3     vector<int> z(n);
4     int l = 0, r = 0;
5     for(int i = 1; i < n; i++) {
6         if(i < r) {
7             z[i] = min(r - i, z[i - 1]);
8         }
9         while(i + z[i] < n && s[z[i]] == s[i + z[i]])
10             z[i]++;
11     }
12     if(i + z[i] > r) {
13         l = i;
14         r = i + z[i];
15     }
16 }
17 return z;
18 }

```

## 2.6 Kmp

```

1 vector<int> kmp(string s) {
2     int n = (int)s.length();
3     vector<int> p(n+1);
4     p[0] = -1;
5     for (int i = 1; i < n; i++) {
6         int j = p[i-1];
7         while (j >= 0 && s[j] != s[i-1])
8             j = p[j-1];
9         p[i] = j+1;
10    }
11    return p;
12 }

```

## 3 DS

### 3.1 Segtree Iterativa

```

1 // Exemplo de uso:
2 // SegTree<int> st(vetor);

```

```

3 // range query e point update
4
5 template <typename T>
6 struct SegTree {
7     int n;
8     vector<T> tree;
9     T neutral_value = 0;
10    T combine(T a, T b) {
11        return a + b;
12    }
13
14    SegTree(const vector<T>& data) {
15        n = data.size();
16        tree.resize(2 * n, neutral_value);
17
18        for (int i = 0; i < n; i++)
19            tree[n + i] = data[i];
20
21        for (int i = n - 1; i > 0; --i)
22            tree[i] = combine(tree[i * 2], tree[i * 2
23 + 1]);
24    }
25
26    T range_query(int l, int r) {
27        T res_l = neutral_value, res_r =
28        neutral_value;
29
30        for (l += n, r += n + 1; l < r; l >>= 1, r
31 >>= 1) {
32            if (l & 1) res_l = combine(res_l, tree[l
33 ++]);
34            if (r & 1) res_r = combine(tree[--r],
35 res_r);
36        }
37
38        return combine(res_l, res_r);
39    }
40
41    void update(int pos, T new_val) {
42        tree[pos += n] = new_val;
43
44        for (pos >>= 1; pos > 0; pos >>= 1)
45            tree[pos] = combine(tree[2 * pos], tree[2
46 * pos + 1]);
47    }
48 };

```

### 3.2 Segtree Gcd

```

1 int gcd(int a, int b) {
2     if (b == 0)
3         return a;
4     return gcd(b, a % b);
5 }
6
7 class SegmentTreeGCD {
8 private:
9     vector<int> tree;
10    int n;
11
12    void build(const vector<int>& arr, int node, int
13 start, int end) {
14        if (start == end) {
15            tree[node] = arr[start];
16        } else {
17            int mid = (start + end) / 2;
18            build(arr, 2 * node + 1, start, mid);
19            build(arr, 2 * node + 2, mid + 1, end);
20            tree[node] = gcd(tree[2 * node + 1], tree
21 [2 * node + 2]);
22        }
23    }
24 }

```

```

23 void update(int node, int start, int end, int idx
24 , int value) {
25     if (start == end) {
26         tree[node] = value;
27     } else {
28         int mid = (start + end) / 2;
29         if (idx <= mid) {
30             update(2 * node + 1, start, mid, idx,
31 value);
32         } else {
33             update(2 * node + 2, mid + 1, end,
34 idx, value);
35         }
36         tree[node] = gcd(tree[2 * node + 1], tree
37 [2 * node + 2]);
38     }
39 }
40
41 int query(int node, int start, int end, int l,
42 int r) {
43     if (r < start || l > end) {
44         return 0;
45     }
46     if (l <= start && end <= r) {
47         return tree[node];
48     }
49     int mid = (start + end) / 2;
50     int left_gcd = query(2 * node + 1, start, mid
51 , l, r);
52     int right_gcd = query(2 * node + 2, mid + 1,
53 end, l, r);
54     return gcd(left_gcd, right_gcd);
55 }
56
57 public:
58 SegmentTreeGCD(const vector<int>& arr) {
59     n = arr.size();
60     tree.resize(4 * n);
61     build(arr, 0, 0, n - 1);
62 }
63
64 void update(int idx, int value) {
65     update(0, 0, n - 1, idx, value);
66 }
67
68 int query(int l, int r) {
69     return query(0, 0, n - 1, l, r);
70 }
71 };

```

### 3.3 Merge Sort Tree

```

1 struct SegTree {
2     int n;
3     vector<vector<int>> tree;
4
5     SegTree(vector<int> &a) {
6         n = a.size();
7         tree.resize(4 * n);
8         build(1, 0, n - 1, a);
9     }
10
11    void build(int x, int lx, int rx, vector<int> &a)
12    {
13        if (lx == rx) {
14            tree[x] = { a[lx] };
15            return;
16        }
17        int mid = lx + (rx - lx)/2;
18        build(2 * x, lx, mid, a);
19        build(2 * x + 1, mid + 1, rx, a);
20        auto &L = tree[2 * x], &R = tree[2 * x + 1];
21        tree[x].resize(L.size() + R.size());
22        merge(L.begin(), L.end(), R.begin(), R.end(),
23 tree[x].begin());

```

```

22     }
23
24     int query(int x, int lx, int rx, int l, int r) {
25         if (lx >= l && rx <= r) {
26             auto &v = tree[x];
27             return v.end() - upper_bound(v.begin(), v
28 .end(), r);
29         }
30         if (rx < l || lx > r) {
31             return 0;
32         }
33         int mid = lx + (rx - lx)/2;
34         return query(2 * x, lx, mid, l, r) + query(2
35 * x + 1, mid + 1, rx, l, r);
36     }
37
38     int query(int l, int r) {
39         return query(1, 0, n - 1, l, r);
40     }
41 }
42
43 // Checar se o range Ã todo distinto
44 // Cada cara e sua prÃxima apariÃÃo a direita,
45 // conta quantos caras que a prÃxima apariÃÃo a
46 // direita ta dentro do range ainda
47
48 vector<int> nr(n);
49 map<int, int> mp;
50 for (int i = n - 1; i >= 0; i--) {
51     auto it = mp.find(a[i]);
52     nr[i] = it != mp.end() ? it->second : n;
53     mp[a[i]] = i;
54 }
55 SegTree seg(nr);

```

### 3.4 Ordered Set E Map

```

1
2 #include<ext/pb_ds/assoc_container.hpp>
3 #include<ext/pb_ds/tree_policy.hpp>
4 using namespace __gnu_pbds;
5 using namespace std;
6
7 template<typename T> using ordered_multiset = tree<T,
8     null_type, less_equal<T>, rb_tree_tag,
9     tree_order_statistics_node_update>;
10
11 template<typename T> using o_set = tree<T, null_type
12     , less<T>, rb_tree_tag,
13     tree_order_statistics_node_update>;
14
15 template<typename T, typename R> using o_map = tree<
16     T, R, less<T>, rb_tree_tag,
17     tree_order_statistics_node_update>;
18
19 int main() {
20     int i, j, k, n, m;
21     o_set<int> st;
22     st.insert(1);
23     st.insert(2);
24     cout << *st.find_by_order(0) << endl; /// k-esimo
25     elemento
26     cout << st.order_of_key(2) << endl; /// numero de
27     elementos menores que k
28     o_map<int, int> mp;
29     mp.insert({1, 10});
30     mp.insert({2, 20});
31     cout << mp.find_by_order(0)->second << endl; /// k-
32     esimo elemento
33     cout << mp.order_of_key(2) << endl; /// numero de
34     elementos (chave) menores que k
35     return 0;
36 }

```

### 3.5 Sparse Table

```

1 // 1-index, 0(1)
2 struct SparseTable {
3     vector<vector<int>> st;
4     int max_log;
5     SparseTable(vector<int>& arr) {
6         int n = arr.size();
7         max_log = floor(log2(n)) + 1;
8         st.resize(n, vector<int>(max_log));
9         for (int i = 0; i < n; i++) {
10             st[i][0] = arr[i];
11         }
12         for (int j = 1; j < max_log; j++) {
13             for (int i = 0; i + (1 << j) <= n; i++) {
14                 st[i][j] = max(st[i][j - 1], st[i +
15 (1 << (j - 1))][j - 1]);
16             }
17         }
18     }
19     int query(int L, int R) {
20         int tamanho = R - L + 1;
21         int k = floor(log2(tamanho));
22         return max(st[L][k], st[R - (1 << k) + 1][k]);
23     };
24 };

```

### 3.6 Psum 2d

```

1 vector<vector<int>> psum(h+1, vector<int>(w+1, 0));
2
3 for (int i=1; i<=h; i++){
4     for (int j=1; j<=w; j++){
5         cin >> psum[i][j];
6         psum[i][j] += psum[i-1][j]+psum[i][j-1]-psum[
7 i-1][j-1];
8     }
9 }
10
11 // retorna a psum2d do intervalo inclusivo [(a, b), (
12 c, d)]
13 int retangulo(int a, int b, int c, int d){
14     c = min(c, h), d = min(d, w);
15     a = max(0LL, a-1), b = max(0LL, b-1);
16
17     return v[c][d]-v[a][d]-v[c][b]+v[a][b];
18 }

```

### 3.7 Segtree Sum

```

1 struct SegTree {
2     ll merge(ll a, ll b) { return a + b; }
3     const ll neutral = 0;
4     int n;
5     vector<ll> t, lazy;
6     vector<bool> replace;
7     inline int lc(int p) { return p * 2; }
8     inline int rc(int p) { return p * 2 + 1; }
9     void push(int p, int l, int r) {
10         if (replace[p]) {
11             t[p] = lazy[p] * (r - l + 1);
12             if (l != r) {
13                 lazy[lc(p)] = lazy[p];
14                 lazy[rc(p)] = lazy[p];
15                 replace[lc(p)] = true;
16                 replace[rc(p)] = true;
17             }
18         } else if (lazy[p] != 0) {
19             t[p] += lazy[p] * (r - l + 1);
20             if (l != r) {
21                 lazy[lc(p)] += lazy[p];
22                 lazy[rc(p)] += lazy[p];
23             }
24         }
25     }
26 };

```

```

24     }
25     replace[p] = false;
26     lazy[p] = 0;
27 }
28 void build(int p, int l, int r, const vector<ll>
&v) {
29     if (l == r) {
30         t[p] = v[l];
31     } else {
32         int mid = (l + r) / 2;
33         build(lc(p), l, mid, v);
34         build(rc(p), mid + 1, r, v);
35         t[p] = merge(t[lc(p)], t[rc(p)]);
36     }
37 }
38 void build(int _n) {
39     n = _n;
40     t.assign(n * 4, neutral);
41     lazy.assign(n * 4, 0);
42     replace.assign(n * 4, false);
43 }
44 void build(const vector<ll> &v) {
45     n = (int)v.size();
46     t.assign(n * 4, neutral);
47     lazy.assign(n * 4, 0);
48     replace.assign(n * 4, false);
49     build(1, 0, n - 1, v);
50 }
51 void build(ll *bg, ll *en) {
52     build(vector<ll>(bg, en));
53 }
54 ll query(int p, int l, int r, int L, int R) {
55     push(p, l, r);
56     if (l > R || r < L) return neutral;
57     if (l >= L && r <= R) return t[p];
58     int mid = (l + r) / 2;
59     auto ql = query(lc(p), l, mid, L, R);
60     auto qr = query(rc(p), mid + 1, r, L, R);
61     return merge(ql, qr);
62 }
63 ll query(int l, int r) { return query(1, 0, n -
1, l, r); }
64 void update(int p, int l, int r, int L, int R, ll
val, bool repl = 0) {
65     push(p, l, r);
66     if (l > R || r < L) return;
67     if (l >= L && r <= R) {
68         lazy[p] = val;
69         replace[p] = repl;
70         push(p, l, r);
71     } else {
72         int mid = (l + r) / 2;
73         update(lc(p), l, mid, L, R, val, repl);
74         update(rc(p), mid + 1, r, L, R, val, repl);
75     }
76     t[p] = merge(t[lc(p)], t[rc(p)]);
77 }
78 void sumUpdate(int l, int r, ll val) { update(1,
0, n - 1, l, r, val, 0); }
79 void assignUpdate(int l, int r, ll val) { update
(1, 0, n - 1, l, r, val, 1); }
80 } segsum;

```

### 3.8 Dsu

```

1 struct DSU {
2     vector<int> par, rank, sz;
3     int c;
4     DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
1, 1), c(n) {
5         for (int i = 1; i <= n; ++i) par[i] = i;
6     }

```

```

7     int find(int i) {
8         return (par[i] == i ? i : (par[i] = find(par[
i])));
9     }
10    bool same(int i, int j) {
11        return find(i) == find(j);
12    }
13    int get_size(int i) {
14        return sz[find(i)];
15    }
16    int count() {
17        return c; // quantos componentes conexos
18    }
19    int merge(int i, int j) {
20        if ((i = find(i)) == (j = find(j))) return
-1;
21        else --c;
22        if (rank[i] > rank[j]) swap(i, j);
23        par[i] = j;
24        sz[j] += sz[i];
25        if (rank[i] == rank[j]) rank[j]++;
26        return j;
27    }
28 };

```

### 3.9 Bit

```

1 struct BIT {
2     int n;
3     vector<int> bit;
4     BIT(int n = 0) : n(n), bit(n + 1, 0) {}
5     void add(int i, int delta) {
6         for (; i <= n; i += i & -i) bit[i] += delta;
7     }
8     int sum(int i) {
9         int r = 0;
10        for (; i > 0; i -= i & -i) r += bit[i];
11        return r;
12    }
13    int range_sum(int l, int r){
14        if (r < 1) return 0;
15        return sum(r) - sum(l - 1);
16    }
17 };

```

## 4 Search and sort

### 4.1 Pilha Monotonic

```

1 vector<int> find_esq(vector<int> &v, bool maior) {
2     int n = v.size();
3     vector<int> result(n);
4     stack<int> s;
5
6     for (int i = 0; i < n; i++) {
7         while (!s.empty() && (maior ? v[s.top()] <= v
[i] : v[s.top()] >= v[i])) {
8             s.pop();
9         }
10        if (s.empty()) {
11            result[i] = -1;
12        } else {
13            result[i] = v[s.top()];
14        }
15        s.push(i);
16    }
17    return result;
18 }
19
20 // maior = true -> encontra o primeiro maior Ãa
direita

```

```

21 vector<int> find_dir(vector<int> &v, bool maior) {
22     int n = v.size();
23     vector<int> result(n);
24     stack<int> s;
25     for (int i = n - 1; i >= 0; i--) {
26         while (!s.empty() && (maior ? v[s.top()] <= v
27 [i] : v[s.top()] >= v[i])) {
28             s.pop();
29         }
30         if (s.empty()) {
31             result[i] = -1;
32         } else {
33             result[i] = v[s.top()];
34         }
35         s.push(i);
36     }
37     return result;

```

## 4.2 Mergeandcount

```

1 // Realiza a mesclagem de dois subarrays e conta o
2 // número de trocas necessárias.
3 int mergeAndCount(vector<int> &v, int l, int m, int r) {
4     int x = m - 1 + 1; // Tamanho do subarray
5     // esquerdo.
6     int y = r - m; // Tamanho do subarray direito.
7     // Vetores temporários para os subarray esquerdo
8     // e direito.
9     vector<int> left(x), right(y);
10    for (int i = 0; i < x; i++) left[i] = v[l + i];
11    for (int j = 0; j < y; j++) right[j] = v[m + 1 +
12 j];
13    int i = 0, j = 0, k = 1;
14    int swaps = 0;
15    while (i < x && j < y) {
16        if (left[i] <= right[j]) {
17            // Se o elemento da esquerda for menor ou
18            // igual, coloca no vetor original.
19            v[k++] = left[i++];
20        } else {
21            // Caso contrario, coloca o elemento da
22            // direita e conta as trocas.
23            v[k++] = right[j++];
24            swaps += (x - i);
25        }
26    }
27    // Adiciona os elementos restantes do subarray
28    // esquerdo (se houver).
29    while (i < x) v[k++] = left[i++];
30    // Adiciona os elementos restantes do subarray
31    // direito (se houver).
32    while (j < y) v[k++] = right[j++];
33    return swaps; // Retorna o numero total de
34    // trocas realizadas.
35 }
36 int mergeSort(vector<int> &v, int l, int r) {
37     int swaps = 0;
38     if (l < r) {
39         // Encontra o ponto medio para dividir o
40         // vetor.
41         int m = l + (r - l) / 2;

```

```

42 // Chama merge sort para a metade esquerda.
43 swaps += mergeSort(v, l, m);
44 // Chama merge sort para a metade direita.
45 swaps += mergeSort(v, m + 1, r);
46 // Mescla as duas metades e conta as trocas.
47 swaps += mergeAndCount(v, l, m, r);
48 }
49 return swaps; // Retorna o numero total de
50 // trocas no vetor.
51 }
52 }

```

## 5 Math

### 5.1 Combinatorics

```

1 const int MAXN_FATORIAL = 200005;
2 const int MOD = 1e9 + 7;
3 // DEFINE INT LONG LONG PLMDS
4 int fat[MAXN_FATORIAL], fati[MAXN_FATORIAL];
5 // (a^b) % m em O(log b)
6 // coloque o fexp
7 int inv(int n) { return fexp(n, MOD - 2); }
8 void precalc() {
9     fat[0] = 1;
10    fati[0] = 1;
11    for (int i = 1; i < MAXN_FATORIAL; i++) fat[i] =
12    (fat[i - 1] * i) % MOD;
13    fati[MAXN_FATORIAL - 1] = inv(fat[MAXN_FATORIAL -
14    1]);
15    for (int i = MAXN_FATORIAL - 2; i >= 0; i--) fati
16    [i] = (fati[i + 1] * (i + 1)) % MOD;
17 }
18 int choose(int n, int k) {
19     if (k < 0 || k > n) return 0;
20     return ((fat[n] * fati[k]) % MOD) * fati[n - k])
21     % MOD;
22 }
23 // n! / (n-k)!
24 int perm(int n, int k) {
25     if (k < 0 || k > n) return 0;
26     return (fat[n] * fati[n - k]) % MOD;
27 }
28 // C_n = (1 / (n+1)) * C(2n, n)
29 int catalan(int n) {
30     if (n < 0 || 2 * n >= MAXN_FATORIAL) return 0;
31     int c2n_n = choose(2 * n, n);
32     return (c2n_n * inv(n + 1)) % MOD;
33 }

```

### 5.2 Equacao Diofantina

```

1 int extended_gcd(int a, int b, int& x, int& y) {
2     if (a == 0) {
3         x = 0;
4         y = 1;
5         return b;
6     }
7     int x1, y1;
8     int gcd = extended_gcd(b % a, a, x1, y1);
9     x = y1 - (b / a) * x1;
10    y = x1;
11    return gcd;

```



```

12 }
13
14 bool solve(int a, int b, int c, int& x0, int& y0) {
15     int x, y;
16     int g = extended_gcd(abs(a), abs(b), x, y);
17     if (c % g != 0) {
18         return false;
19     }
20     x0 = x * (c / g);
21     y0 = y * (c / g);
22     if (a < 0) x0 = -x0;
23     if (b < 0) y0 = -y0;
24     return true;
25 }

```

### 5.3 Discrete Log

```

1 // Returns minimum x for which a^x = b (mod m), a and
2 // if the answer dont need to be greater than some
3 // value, the vector<int> can be removed
4 int discrete_log(int a, int b, int m) {
5     a %= m, b %= m;
6     int n = sqrt(m) + 1;
7
8     int an = 1;
9     for (int i = 0; i < n; ++i)
10         an = (an * 111 * a) % m;
11
12     unordered_map<int, vector<int>> vals;
13     for (int q = 0, cur = b; q <= n; ++q) {
14         vals[cur].push_back(q);
15         cur = (cur * 111 * a) % m;
16     }
17
18     int res = LLONG_MAX;
19
20     for (int p = 1, cur = 1; p <= n; ++p) {
21         cur = (cur * 111 * an) % m;
22         if (vals.count(cur)) {
23             for (int q: vals[cur]) {
24                 int ans = n * p - q;
25                 res = min(res, ans);
26             }
27         }
28     }
29     return res;
30 }

```

### 5.4 Segment Sieve

```

1 // Retorna quantos primos tem entre [l, r] (inclusivo)
2 // precisa de um vetor com os primos atÃ sqrt(r)
3 int seg_sieve(int l, int r){
4     if (l > r) return 0;
5     vector<bool> is_prime(r - l + 1, true);
6     if (l == 1) is_prime[0] = false;
7
8     for (int p : primos){
9         if (p * p > r) break;
10        int start = max(p * p, (l + p - 1) / p * p);
11        for (int j = start; j <= r; j += p){
12            if (j >= 1) {
13                is_prime[j - l] = false;
14            }
15        }
16    }
17
18    return accumulate(all(is_prime), 0ll);
19 }

```

### 5.5 Totient

```

1 // phi(n) = n * (1 - 1/p1) * (1 - 1/p2) * ...
2 int phi(int n) {
3     int result = n;
4     for (int i = 2; i * i <= n; i++) {
5         if (n % i == 0) {
6             while (n % i == 0)
7                 n /= i;
8             result -= result / i;
9         }
10    }
11    if (n > 1) // SE n sobrou, ele Ã um fator primo
12        result -= result / n;
13    return result;
14 }
15
16 // crivo phi
17 const int MAXN_PHI = 1000001;
18 int phiv[MAXN_PHI];
19 void phi_sieve() {
20     for (int i = 0; i < MAXN_PHI; i++) phiv[i] = i;
21     for (int i = 2; i < MAXN_PHI; i++) {
22         if (phiv[i] == i) {
23             for (int j = i; j < MAXN_PHI; j += i)
24                 phiv[j] -= phiv[j] / i;
25         }
26     }

```

### 5.6 Menor Fator Primo

```

1 const int MAXN = 1000001; // Limite para o Crivo.
2 int spf[MAXN];
3 vector<int> primos;
4
5 void crivo() {
6     for (int i = 2; i * i < MAXN; i++) {
7         if (spf[i] == i) {
8             for (int j = i * i; j < MAXN; j += i) {
9                 if (spf[j] == j) {
10                     spf[j] = i;
11                 }
12             }
13         }
14     }
15
16     for (int i = 2; i < MAXN; i++) {
17         if (spf[i] == i) {
18             primos.push_back(i);
19         }
20     }
21
22     map<int, int> fatora(int n) {
23         map<int, int> fatores;
24         while (n > 1) {
25             fatores[spf[n]]++;
26             n /= spf[n];
27         }
28         return fatores;
29     }
30
31     int numero_de_divisores(int n) {
32         if (n == 1) return 1;
33         map<int, int> fatores = fatora(n);
34         int nod = 1;
35         for (auto &[primo, expoente] : fatores) nod *= (
36             expoente + 1);
37         return nod;
38     }
39 // DEFINE INT LONG LONG

```

```

40 int soma_dos_divisores(int n) {
41     if (n == 1) return 1;
42     map<int, int> fatores = fatorar(n);
43     int sod = 1;
44     for (auto &[primo, expoente] : fatores) {
45         int termo_soma = 1;
46         int potencia_primo = 1;
47         for (int i = 0; i < expoente; i++) {
48             potencia_primo *= primo;
49             termo_soma += potencia_primo;
50         }
51         sod *= termo_soma;
52     }
53     return sod;
54 }

```

## 5.7 Exgcd

```

1 // 0 retorno da funcao eh {n, m, g}
2 // e significa que gcd(a, b) = g e
3 // n e m sao inteiros tais que an + bm = g
4 array<ll, 3> exgcd(int a, int b) {
5     if(b == 0) return {1, 0, a};
6     auto [m, n, g] = exgcd(b, a % b);
7     return {n, m - a / b * n, g};
8 }

```

## 5.8 Fexp

```

1 // a^e mod m
2 // O(log n)
3
4 int fexp(int a, int e, int m) {
5     a %= m;
6     int ans = 1;
7     while (e > 0) {
8         if (e & 1) ans = ans * a % m;
9         a = a * a % m;
10        e /= 2;
11    }
12    return ans % m;
13 }

```

## 5.9 Divisores

```

1 // Retorna um vetor com os divisores de x
2 // eh preciso ter o crivo implementado
3 // O(divisores)
4
5 vector<int> divs(int x) {
6     vector<int> ans = {1};
7     vector<array<int, 2>> primos; // {primo, expoente}
8
9     while (x > 1) {
10        int p = crivo[x], cnt = 0;
11        while (x % p == 0) cnt++, x /= p;
12        primos.push_back({p, cnt});
13    }
14
15    for (int i=0; i<primos.size(); i++) {
16        int cur = 1, len = ans.size();
17
18        for (int j=0; j<primos[i][1]; j++) {
19            cur *= primos[i][0];
20            for (int k=0; k<len; k++)
21                ans.push_back(cur*ans[k]);
22        }
23    }
24
25    return ans;
26 }

```

## 5.10 Crivo

```

1 // O(n*log(log(n)))
2 bool composto[MAX]
3 for(int i = 1; i <= n; i++) {
4     if(composto[i]) continue;
5     for(int j = 2*i; j <= n; j += i)
6         composto[j] = 1;
7 }

```

## 5.11 Mod Inverse

```

1 array<int, 2> extended_gcd(int a, int b) {
2     if (b == 0) return {1, 0};
3     auto [x, y] = extended_gcd(b, a % b);
4     return {y, x - (a / b) * y};
5 }
6
7 int mod_inverse(int a, int m) {
8     auto [x, y] = extended_gcd(a, m);
9     return (x % m + m) % m;
10 }

```

## 5.12 Base Calc

```

1 int char_to_val(char c) {
2     if (c >= '0' && c <= '9') return c - '0';
3     else return c - 'A' + 10;
4 }
5
6 char val_to_char(int val) {
7     if (val >= 0 && val <= 9) return val + '0';
8     else return val - 10 + 'A';
9 }
10
11 int to_base_10(string &num, int bfrom) {
12     int result = 0;
13     int pot = 1;
14     for (int i = num.size() - 1; i >= 0; i--) {
15         if (char_to_val(num[i]) >= bfrom) return -1;
16         result += char_to_val(num[i]) * pot;
17         pot *= bfrom;
18     }
19     return result;
20 }
21
22 string from_base_10(int n, int bto) {
23     if (n == 0) return "0";
24     string result = "";
25     while (n > 0) {
26         result += val_to_char(n % bto);
27         n /= bto;
28     }
29     reverse(result.begin(), result.end());
30     return result;
31 }
32
33 string convert_base(string &num, int bfrom, int bto) {
34     {
35         int n_base_10 = to_base_10(num, bfrom);
36         return from_base_10(n_base_10, bto);
37     }
38 }

```

## 6 Graph

### 6.1 Dijkstra

```

1 // SSP com pesos positivos.
2 // O((V + E) log V).
3
4 vector<int> dijkstra(int S) {

```

```

5 vector<bool> vis(MAXN, 0);
6 vector<ll> dist(MAXN, LLONG_MAX);
7 dist[S] = 0;
8 priority_queue<pii, vector<pii>, greater<pii>> pq;
9 ;
10 pq.push({0, S});
11 while(pq.size()) {
12     ll v = pq.top().second;
13     pq.pop();
14     if(vis[v]) continue;
15     vis[v] = 1;
16     for(auto &[peso, vizinho] : adj[v]) {
17         if(dist[vizinho] > dist[v] + peso) {
18             dist[vizinho] = dist[v] + peso;
19             pq.push({dist[vizinho], vizinho});
20         }
21     }
22     return dist;
23 }

```

## 6.2 Floyd Warshall

```

1 // SSP e acha ciclos.
2 // Bom com constraints menores.
3 // O(n^3)
4
5 int dist[501][501];
6
7 void floydWarshall() {
8     for(int k = 0; k < n; k++) {
9         for(int i = 0; i < n; i++) {
10             for(int j = 0; j < n; j++) {
11                 dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j]);
12             }
13         }
14     }
15 }
16 void solve() {
17     int m, q;
18     cin >> n >> m >> q;
19     for(int i = 0; i < n; i++) {
20         for(int j = i; j < n; j++) {
21             if(i == j) {
22                 dist[i][j] = dist[j][i] = 0;
23             } else {
24                 dist[i][j] = dist[j][i] = linf;
25             }
26         }
27     }
28     for(int i = 0; i < m; i++) {
29         int u, v, w;
30         cin >> u >> v >> w; u--; v--;
31         dist[u][v] = min(dist[u][v], w);
32         dist[v][u] = min(dist[v][u], w);
33     }
34     floydWarshall();
35     while(q--) {
36         int u, v;
37         cin >> u >> v; u--; v--;
38         if(dist[u][v] == linf) cout << -1 << '\n';
39         else cout << dist[u][v] << '\n';
40     }
41 }

```

## 6.3 Eulerian Path

```

1 /**
2  * Versão que assume: #define int long long
3  *
4  * Retorna um caminho/ciclo euleriano em um grafo (se
5  * existir).

```

```

5 * - g: lista de adjacência (vector<vector<int>>).
6 * - directed: true se o grafo for dirigido.
7 * - s: vértice inicial.
8 * - e: vértice final (opcional). Se informado,
9   tenta caminho de s até e.
10 * - O(Nlog(N))
11 * Retorna vetor com a sequência de vértices, ou
12   vazio se impossível.
13 */
14 vector<int> eulerian_path(const vector<vector<int>>&
15     g, bool directed, int s, int e = -1) {
16     int n = (int)g.size();
17     // copia das adjacências em multiset para
18     // permitir remoção específica
19     vector<multiset<int>> h(n);
20     vector<int> in_degree(n, 0);
21     vector<int> result;
22     stack<int> st;
23     // preencher h e indegrees
24     for (int u = 0; u < n; ++u) {
25         for (auto v : g[u]) {
26             ++in_degree[v];
27             h[u].emplace(v);
28         }
29     }
30     st.emplace(s);
31     if (e != -1) {
32         int out_s = (int)h[s].size();
33         int out_e = (int)h[e].size();
34         int diff_s = in_degree[s] - out_s;
35         int diff_e = in_degree[e] - out_e;
36         if (diff_s * diff_e != -1) return {}; //
37         impossível
38     }
39     for (int u = 0; u < n; ++u) {
40         if (e != -1 && (u == s || u == e)) continue;
41         int out_u = (int)h[u].size();
42         if (in_degree[u] != out_u || (!directed && (
43             in_degree[u] & 1))) {
44             return {};
45         }
46     }
47     while (!st.empty()) {
48         int u = st.top();
49         if (h[u].empty()) {
50             result.emplace_back(u);
51             st.pop();
52         } else {
53             int v = *h[u].begin();
54             auto it = h[u].find(v);
55             if (it != h[u].end()) h[u].erase(it);
56             --in_degree[v];
57             if (!directed) {
58                 auto it2 = h[v].find(u);
59                 if (it2 != h[v].end()) h[v].erase(it2);
60                 --in_degree[u];
61             }
62             st.emplace(v);
63         }
64     }
65     for (int u = 0; u < n; ++u) {
66         if (in_degree[u] != 0) return {};
67     }
68     reverse(result.begin(), result.end());
69     return result;
70 }

```

## 6.4 Dinitz

```

1 // Complexidade: O(V^2E)
2
3 struct FlowEdge {

```

```

4     int from, to;
5     long long cap, flow = 0;
6     FlowEdge(int from, int to, long long cap) : from(
7         from), to(to), cap(cap) {}
8
9     struct Dinic {
10         const long long flow_inf = 1e18;
11         vector<FlowEdge> edges;
12         vector<vector<int>> adj;
13         int n, m = 0;
14         int s, t;
15         vector<int> level, ptr;
16         queue<int> q;
17
18         Dinic(int n, int s, int t) : n(n), s(s), t(t) {
19             adj.resize(n);
20             level.resize(n);
21             ptr.resize(n);
22         }
23
24         void add_edge(int from, int to, long long cap) {
25             edges.emplace_back(from, to, cap);
26             edges.emplace_back(to, from, 0);
27             adj[from].push_back(m);
28             adj[to].push_back(m + 1);
29             m += 2;
30         }
31
32         bool bfs() {
33             while (!q.empty()) {
34                 int from = q.front();
35                 q.pop();
36                 for (int id : adj[from]) {
37                     if (edges[id].cap == edges[id].flow)
38                         continue;
39                     if (level[edges[id].to] != -1)
40                         continue;
41                     level[edges[id].to] = level[from] +
42                         1;
43                     q.push(edges[id].to);
44                 }
45             }
46             return level[t] != -1;
47         }
48
49         long long dfs(int from, long long pushed) {
50             if (pushed == 0)
51                 return 0;
52             if (from == t)
53                 return pushed;
54             for (int& cid = ptr[from]; cid < (int)adj[
55                 from].size(); cid++) {
56                 int id = adj[from][cid];
57                 int to = edges[id].to;
58                 if (level[from] + 1 != level[to])
59                     continue;
60                 long long tr = dfs(to, min(pushed, edges[
61                     id].cap - edges[id].flow));
62                 if (tr == 0)
63                     continue;
64                 edges[id].flow += tr;
65                 edges[id ^ 1].flow -= tr;
66                 return tr;
67             }
68             return 0;
69         }
70
71         long long flow() {
72             long long f = 0;
73             while (true) {
74                 fill(level.begin(), level.end(), -1);
75                 level[s] = 0;

```

```

73         q.push(s);
74         if (!bfs())
75             break;
76         fill(ptr.begin(), ptr.end(), 0);
77         while (long long pushed = dfs(s, flow_inf
78             )) {
79             f += pushed;
80         }
81     }
82     return f;
83 };

```

## 6.5 Khan

```

1 // topo-sort DAG
2 // lexicograficamente menor.
3 // N: número de vértices (1-indexado)
4 // adj: lista de adjacência do grafo
5
6 const int MAXN = 5 * 1e5 + 2;
7 vector<int> adj[MAXN];
8 int N;
9
10 vector<int> kahn() {
11     vector<int> indegree(N + 1, 0);
12     for (int u = 1; u <= N; u++) {
13         for (int v : adj[u]) {
14             indegree[v]++;
15         }
16     }
17     priority_queue<int, vector<int>, greater<int>> pq;
18     for (int i = 1; i <= N; i++) {
19         if (indegree[i] == 0) {
20             pq.push(i);
21         }
22     }
23     vector<int> result;
24     while (!pq.empty()) {
25         int u = pq.top();
26         pq.pop();
27         result.push_back(u);
28         for (int v : adj[u]) {
29             indegree[v]--;
30             if (indegree[v] == 0) {
31                 pq.push(v);
32             }
33         }
34     }
35     if (result.size() != N) {
36         return {};
37     }
38     return result;
39 }

```

## 6.6 Topological Sort

```

1 vector<int> adj[MAXN];
2 vector<int> estado(MAXN); // 0: não visitado 1:
3 // processamento 2: processado
4 vector<int> ordem;
5 bool temCiclo = false;
6
7 void dfs(int v) {
8     if(estado[v] == 1) {
9         temCiclo = true;
10        return;
11    }
12    if(estado[v] == 2) return;
13    estado[v] = 1;
14    for(auto &nei : adj[v]) {

```

```

14         if(estado[v] != 2) dfs(nei);
15     }
16     estado[v] = 2;
17     ordem.push_back(v);
18     return;
19 }

```

## 6.7 Acha Pontes

```

1 vector<int> d, low, pai;          // d[v] Tempo de
   descoberta (discovery time)
2 vector<bool> vis;
3 vector<int> pontos_articulacao;
4 vector<pair<int, int>> pontes;
5 int tempo;
6
7 vector<vector<int>> adj;
8
9 void dfs(int u) {
10     vis[u] = true;
11     tempo++;
12     d[u] = low[u] = tempo;
13     int filhos_dfs = 0;
14     for (int v : adj[u]) {
15         if (v == pai[u]) continue;
16         if (vis[v]) { // back edge
17             low[u] = min(low[u], d[v]);
18         } else {
19             pai[v] = u;
20             filhos_dfs++;
21             dfs(v);
22             low[u] = min(low[u], low[v]);
23             if (pai[u] == -1 && filhos_dfs > 1) {
24                 pontos_articulacao.push_back(u);
25             }
26             if (pai[u] != -1 && low[v] >= d[u]) {
27                 pontos_articulacao.push_back(u);
28             }
29             if (low[v] > d[u]) {
30                 pontes.push_back({min(u, v), max(u, v)});
31             }
32         }
33     }
34 }

```

## 6.8 Edmonds-karp

```

1 // Edmonds-Karp com scalling  $O(E \log(F))$ 
2
3 int n, m;
4 const int MAXN = 510;
5 vector<vector<int>> capacity(MAXN, vector<int>(MAXN, 0));
6 vector<vector<int>> adj(MAXN);
7
8 int bfs(int s, int t, int scale, vector<int>& parent) {
9     fill(parent.begin(), parent.end(), -1);
10    parent[s] = -2;
11    queue<pair<int, int>> q;
12    q.push({s, LLONG_MAX});
13
14    while (!q.empty()) {
15        int cur = q.front().first;
16        int flow = q.front().second;
17        q.pop();
18
19        for (int next : adj[cur]) {
20            if (parent[next] == -1 && capacity[cur][next] >= scale) {
21                parent[next] = cur;

```

```

22                int new_flow = min(flow, capacity[cur][next]);
23                if (next == t)
24                    return new_flow;
25                q.push({next, new_flow});
26            }
27        }
28    }
29
30    return 0;
31 }
32
33 int maxflow(int s, int t) {
34     int flow = 0;
35     vector<int> parent(MAXN);
36     int new_flow;
37     int scalling = 1ll << 62;
38
39     while (scalling > 0) {
40         while (new_flow = bfs(s, t, scalling, parent)) {
41             if (new_flow == 0) continue;
42             flow += new_flow;
43             int cur = t;
44             while (cur != s) {
45                 int prev = parent[cur];
46                 capacity[prev][cur] -= new_flow;
47                 capacity[cur][prev] += new_flow;
48                 cur = prev;
49             }
50             scalling /= 2;
51         }
52     }
53
54     return flow;
55 }

```

## 6.9 Kruskal

```

1 // Ordena as arestas por peso, insere se ja nao
   estiver no mesmo componente
2 //  $O(E \log E)$ 
3
4 struct DSU {
5     vector<int> par, rank, sz;
6     int c;
7     DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n + 1, 1), c(n) {
8         for (int i = 1; i <= n; ++i) par[i] = i;
9     }
10    int find(int i) {
11        return (par[i] == i ? i : (par[i] = find(par[i])));
12    }
13    bool same(int i, int j) {
14        return find(i) == find(j);
15    }
16    int get_size(int i) {
17        return sz[find(i)];
18    }
19    int count() {
20        return c; // quantos componentes conexos
21    }
22    int merge(int i, int j) {
23        if ((i = find(i)) == (j = find(j))) return -1;
24        else --c;
25        if (rank[i] > rank[j]) swap(i, j);
26        par[i] = j;
27        sz[j] += sz[i];
28        if (rank[i] == rank[j]) rank[j]++;
29        return j;
30    }

```

```

31 };
32
33 struct Edge {
34     int u, v, w;
35     bool operator <(Edge const & other) {
36         return weight < other.weight;
37     }
38 }
39
40 vector<Edge> kruskal(int n, vector<Edge> edges) {
41     vector<Edge> mst;
42     DSU dsu = DSU(n + 1);
43     sort(edges.begin(), edges.end());
44     for (Edge e : edges) {
45         if (dsu.find(e.u) != dsu.find(e.v)) {
46             mst.push_back(e);
47             dsu.join(e.u, e.v);
48         }
49     }
50     return mst;
51 }

```

## 6.10 Bellman Ford

```

1  struct Edge {
2      int u, v, w;
3  };
4
5  // se x = -1, não tem ciclo
6  // se x != -1, pegar pais de x pra formar o ciclo
7
8  int n, m;
9  vector<Edge> edges;
10 vector<int> dist(n);
11 vector<int> pai(n, -1);
12
13 for (int i = 0; i < n; i++) {
14     x = -1;
15     for (Edge &e : edges) {
16         if (dist[e.u] + e.w < dist[e.v]) {
17             dist[e.v] = max(-INF, dist[e.u] + e.w);
18             pai[e.v] = e.u;
19             x = e.v;
20         }
21     }
22 }
23
24 // achando caminho (se precisar)
25 for (int i = 0; i < n; i++) x = pai[x];
26
27 vector<int> ciclo;
28 for (int v = x;; v = pai[v]) {
29     cycle.push_back(v);
30     if (v == x && ciclo.size() > 1) break;
31 }
32 reverse(ciclo.begin(), ciclo.end());

```

## 6.11 Lca Jc

```

1  const int MAXN = 200005;
2  int N;
3  int LOG;
4
5  vector<vector<int>> adj;
6  vector<int> profundidade;
7  vector<vector<int>> cima; // cima[v][j] é o 2^j-
8                          //ésimo ancestral de v
9
10 void dfs(int v, int p, int d) {
11     profundidade[v] = d;
12     cima[v][0] = p; // o pai direto é o 2^0-ésimo
13     ancestral

```

```

12     for (int j = 1; j < LOG; j++) {
13         // se o ancestral 2^(j-1) existir, calculamos
14         // o 2^j
15         if (cima[v][j - 1] != -1) {
16             cima[v][j] = cima[cima[v][j - 1]][j - 1];
17         } else {
18             cima[v][j] = -1; // não tem ancestral
19             superior
20         }
21     }
22     for (int nei : adj[v]) {
23         if (nei != p) {
24             dfs(nei, v, d + 1);
25         }
26     }
27 }
28 void build(int root) {
29     LOG = ceil(log2(N));
30     profundidade.assign(N + 1, 0);
31     cima.assign(N + 1, vector<int>(LOG, -1));
32     dfs(root, -1, 0);
33 }
34 int get_lca(int a, int b) {
35     if (profundidade[a] < profundidade[b]) {
36         swap(a, b);
37     }
38     // sobe 'a' até a mesma profundidade de 'b'
39     for (int j = LOG - 1; j >= 0; j--) {
40         if (profundidade[a] - (1 << j) >=
41             profundidade[b]) {
42             a = cima[a][j];
43         }
44     }
45     // se 'b' era um ancestral de 'a', então 'a'
46     // agora é igual a 'b'
47     if (a == b) {
48         return a;
49     }
50     // sobe os dois nós juntos até encontrar os
51     // filhos do LCA
52     for (int j = LOG - 1; j >= 0; j--) {
53         if (cima[a][j] != -1 && cima[a][j] != cima[b]
54             [j]) {
55             a = cima[a][j];
56             b = cima[b][j];
57         }
58     }
59     return cima[a][0];
60 }

```

## 6.12 Lca

```

1  // LCA - CP algorithm
2  // preprocessing O(NlogN)
3  // lca O(logN)
4  // Uso: criar LCA com a quantidade de vértices (n) e
5  // lista de adjacência (adj)
6  // chamar a função de preprocess com a raiz da árvore
7
8  struct LCA {
9      int n, l, timer;
10     vector<vector<int>> adj;
11     vector<int> tin, tout;
12     vector<vector<int>> up;
13
14     LCA(int n, const vector<vector<int>>& adj) : n(n)
15     , adj(adj) {}
16
17     void dfs(int v, int p) {
18         tin[v] = ++timer;

```

```

17     up[v][0] = p;
18     for (int i = 1; i <= l; ++i)
19         up[v][i] = up[up[v][i-1]][i-1];
20
21     for (int u : adj[v]) {
22         if (u != p)
23             dfs(u, v);
24     }
25
26     tout[v] = ++timer;
27 }
28
29 bool is_ancestor(int u, int v) {
30     return tin[u] <= tin[v] && tout[u] >= tout[v];
31 };
32
33 int lca(int u, int v) {
34     if (is_ancestor(u, v))
35         return u;
36     if (is_ancestor(v, u))
37         return v;
38     for (int i = l; i >= 0; --i) {
39         if (!is_ancestor(up[u][i], v))
40             u = up[u][i];
41     }
42     return up[u][0];
43 }
44
45 void preprocess(int root) {
46     tin.resize(n);
47     tout.resize(n);
48     timer = 0;
49     l = ceil(log2(n));
50     up.assign(n, vector<int>(l + 1));
51     dfs(root, root);
52 }
53 };

```

### 6.13 Kosaraju

```

1 bool vis[MAXN];
2 vector<int> order;
3 int component[MAXN];
4 int N, m;
5 vector<int> adj[MAXN], adj_rev[MAXN];
6
7 // dfs no grafo original para obter a ordem (pÃ¶ss-
8 // order)
9 void dfs1(int u) {
10     vis[u] = true;
11     for (int v : adj[u]) {
12         if (!vis[v]) {
13             dfs1(v);
14         }
15     }
16     order.push_back(u);
17 }
18
19 // dfs o grafo reverso para encontrar os SCCs
20 void dfs2(int u, int c) {
21     component[u] = c;
22     for (int v : adj_rev[u]) {
23         if (component[v] == -1) {
24             dfs2(v, c);
25         }
26     }
27 }
28
29 int kosaraju() {
30     order.clear();
31     fill(vis + 1, vis + N + 1, false);
32     for (int i = 1; i <= N; i++) {

```

```

32         if (!vis[i]) {
33             dfs1(i);
34         }
35     }
36     fill(component + 1, component + N + 1, -1);
37     int c = 0;
38     reverse(order.begin(), order.end());
39     for (int u : order) {
40         if (component[u] == -1) {
41             dfs2(u, c++);
42         }
43     }
44     return c;
45 }

```

### 6.14 Pega Ciclo

```

1 // encontra um ciclo em g (direcionado ou nÃ£o)
2 // g[u] = vector<pair<id_aresta, vizinho>>
3 // rec_arestas: true -> retorna ids das arestas do
4 // ciclo; false -> retorna vÃ©rtices do ciclo
5 // directed: grafo direcionado?
6
7 const int MAXN = 5 * 1e5 + 2;
8 vector<pair<int, int>> g[MAXN];
9 int N;
10 bool DIRECTED = false;
11 vector<int> color(MAXN), parent(MAXN, -1), edgein(
12     MAXN, -1); // color: 0,1,2 ; edgein[v] = id da
13 // aresta que entra em v
14 int ini_ciclo = -1, fim_ciclo = -1, back_edge_id =
15     -1;
16
17 bool dfs(int u, int pai_edge) {
18     color[u] = 1; // cinza
19     for (auto [id, v] : g[u]) {
20         if (!DIRECTED && id == pai_edge) continue; //
21         // ignorar aresta de volta ao pai em nÃ£o-dir
22         if (color[v] == 0) {
23             parent[v] = u;
24             edgein[v] = id;
25             if (dfs(v, id)) return true;
26         } else if (color[v] == 1) {
27             // back-edge u -> v detectado
28             ini_ciclo = u;
29             fim_ciclo = v;
30             back_edge_id = id;
31             return true;
32         }
33         // se color[v] == 2, ignora
34     }
35     color[u] = 2; // preto
36     return false;
37 }
38
39 // retorna ids das arestas do ciclo (vazio se nÃ£o
40 // hÃ¡)
41 vector<int> pega_ciclo(bool rec_arestas) {
42     for (int u = 1; u <= N; u++) {
43         if (color[u] != 0) continue;
44         if (dfs(u, -1)) {
45             // reconstrÃ¶i caminho u -> ... -> v via
46             parent
47             vector<int> path;
48             int cur = ini_ciclo;
49             path.push_back(cur);
50             while (cur != fim_ciclo) {
51                 cur = parent[cur];
52                 path.push_back(cur);
53             }
54             // path = [u, ..., v] -> inverter para [v
55             // ..., u]

```

```

49         reverse(path.begin(), path.end());
50         if (!rec_arestas) return path;
51         // converte para ids das arestas: edgein[
node] Ã a aresta que entra em node
52         vector<int> edges;
53         for (int i = 1; i < path.size(); i++)
edges.push_back(edgein[path[i]]);
54         // adiciona a aresta de retorno u -> v
55         edges.push_back(back_edge_id);
56         return edges;
57     }
58 }
59 return {};
60 }

```

## 6.15 Min Cost Max Flow

```

1 // Encontra o menor custo para passar K de fluxo em
um grafo com N vertices
2 // Funciona com multiplas arestas para o mesmo par de
vertices
3 // Para encontrar o min cost max flow Ã sÃ fazer K
= infinito
4
5 struct Edge {
6     int from, to, capacity, cost, id;
7 };
8
9 vector<vector<array<int, 2>>> adj;
10 vector<Edge> edges; // arestas pares sÃo as normais
e suas reversas sÃo as impares
11
12 const int INF = LLONG_MAX;
13
14 void shortest_paths(int n, int v0, vector<int>& dist,
vector<int>& edge_to) {
15     dist.assign(n, INF);
16     dist[v0] = 0;
17     vector<bool> in_queue(n, false);
18     queue<int> q;
19     q.push(v0);
20     edge_to.assign(n, -1);
21
22     while (!q.empty()) {
23         int u = q.front();
24         q.pop();
25         in_queue[u] = false;
26         for (auto [v, id] : adj[u]) {
27             if (edges[id].capacity > 0 && dist[v] >
dist[u] + edges[id].cost) {
28                 dist[v] = dist[u] + edges[id].cost;
29                 edge_to[v] = id;
30                 if (!in_queue[v]) {
31                     in_queue[v] = true;
32                     q.push(v);
33                 }
34             }
35         }
36     }
37 }
38
39 void add_edge(int from, int to, int capacity, int
cost){
40     edges.push_back({from, to, capacity, cost, (int)
edges.size()});
41     edges.push_back({to, from, 0, -cost, (int)edges.
size()}); // reversa
42 }
43
44 int min_cost_flow(int N, int K, int s, int t) {
45     adj.assign(N, vector<array<int, 2>>());
46
47     for (Edge e : edges) {

```

```

48         adj[e.from].push_back({e.to, e.id});
49     }
50
51     int flow = 0;
52     int cost = 0;
53     vector<int> dist, edge_to;
54     while (flow < K) {
55         shortest_paths(N, s, dist, edge_to);
56         if (dist[t] == INF)
57             break;
58
59         // find max flow on that path
60         int f = K - flow;
61         int cur = t;
62         while (cur != s) {
63             f = min(f, edges[edge_to[cur]].capacity);
64             cur = edges[edge_to[cur]].from;
65         }
66
67         // apply flow
68         flow += f;
69         cost += f * dist[t];
70         cur = t;
71         while (cur != s) {
72             int edge = edge_to[cur];
73             int rev_edge = edge^1;
74
75             edges[edge].capacity -= f;
76             edges[rev_edge].capacity += f;
77             cur = edges[edge].from;
78         }
79
80         if (flow < K)
81             return -1;
82         else
83             return cost;
84     }
85 }

```

## 7 Primitives

## 8 DP

### 8.1 Lis

```

1 int lis_nlogn(vector<int> &v) {
2     vector<int> lis;
3     lis.push_back(v[0]);
4     for (int i = 1; i < v.size(); i++) {
5         if (v[i] > lis.back()) {
6             // estende a LIS.
7             lis.push_back(v[i]);
8         } else {
9             // encontra o primeiro elemento em lis
que Ã >= v[i].
10             // subsequÃncia de mesmo comprimento,
mas com um final menor.
11             auto it = lower_bound(lis.begin(), lis.
end(), v[i]);
12             *it = v[i];
13         }
14     }
15     return lis.size();
16 }
17
18 // LIS NA ARVORE
19 const int MAXN_TREE = 100001;
20 vector<int> adj[MAXN_TREE];
21 int values[MAXN_TREE];
22 int ans = 0;
23

```



```

24
25 void dfs(int u, int p, vector<int>& tails) {
26     auto it = lower_bound(tails.begin(), tails.end(),
27         values[u]);
28     int prev = -1;
29     bool coloquei = false;
30     if (it == tails.end()) {
31         tails.push_back(values[u]);
32         coloquei = true;
33     } else {
34         prev = *it;
35         *it = values[u];
36     }
37     ans = max(ans, (int)tails.size());
38     for (int v : adj[u]) {
39         if (v != p) {
40             dfs(v, u, tails);
41         }
42     }
43     if (coloquei) {
44         tails.pop_back();
45     } else {
46         *it = prev;
47     }
48 }

```

## 8.2 Edit Distance

```

1 vector<vector<int>> dp(n+1, vector<int>(m+1, LINF
2 ));
3 for(int j = 0; j <= m; j++) {
4     dp[0][j] = j;
5 }
6
7 for(int i = 0; i <= n; i++) {
8     dp[i][0] = i;
9 }
10
11 for(int i = 1; i <= n; i++) {
12     for(int j = 1; j <= m; j++) {
13         if(a[i-1] == b[j-1]) {
14             dp[i][j] = dp[i-1][j-1];
15         } else {
16             dp[i][j] = min({dp[i-1][j] + 1, dp[i-1][j-1] + 1, dp[i][j-1] + 1});
17         }
18     }
19 }
20
21 cout << dp[n][m];

```

## 8.3 Bitmask

```

1 // dp de intervalos com bitmask
2 int prox(int idx) {
3     return lower_bound(S.begin(), S.end(), array<int>,
4         4>{S[idx][1], 011, 011, 011}) - S.begin();
5 }
6
7 int dp[1002][(int)(111 << 10)];
8
9 int rec(int i, int vis) {
10     if (i == (int)S.size()) {
11         if (__builtin_popcountll(vis) == N) return 0;
12         return LLONG_MIN;
13     }
14     if (dp[i][vis] != -1) return dp[i][vis];
15     int ans = rec(i + 1, vis);
16     ans = max(ans, rec(prox(i), vis | (111 << S[i][3])) + S[i][2]);
17     return dp[i][vis] = ans;
18 }

```

```

17 }

```

## 8.4 Lcs

```

1 string s1, s2;
2 int dp[1001][1001];
3
4 int lcs(int i, int j) {
5     if (i < 0 || j < 0) return 0;
6     if (dp[i][j] != -1) return dp[i][j];
7     if (s1[i] == s2[j]) {
8         return dp[i][j] = 1 + lcs(i - 1, j - 1);
9     } else {
10        return dp[i][j] = max(lcs(i - 1, j), lcs(i, j - 1));
11    }
12 }

```

## 8.5 Digit

```

1 vector<int> digits;
2
3 int dp[20][10][2][2];
4
5 int rec(int i, int last, int flag, int started) {
6     if (i == (int)digits.size()) return 1;
7     if (dp[i][last][flag][started] != -1) return dp[i][last][flag][started];
8     int lim;
9     if (flag) lim = 9;
10    else lim = digits[i];
11    int ans = 0;
12    for (int d = 0; d <= lim; d++) {
13        if (started && d == last) continue;
14        int new_flag = flag;
15        int new_started = started;
16        if (d > 0) new_started = 1;
17        if (!flag && d < lim) new_flag = 1;
18        ans += rec(i + 1, d, new_flag, new_started);
19    }
20    return dp[i][last][flag][started] = ans;
21 }

```

## 8.6 Knapsack

```

1 // dp[i][j] => i-esimo item com j-carga sobrando na
2 // mochila
3 // O(N * W)
4
5 for(int j = 0; j < MAXN; j++) {
6     dp[0][j] = 0;
7 }
8
9 for(int i = 1; i <= N; i++) {
10    for(int j = 0; j <= W; j++) {
11        if(items[i].first > j) {
12            dp[i][j] = dp[i-1][j];
13        } else {
14            dp[i][j] = max(dp[i-1][j], dp[i-1][j-items[i].first] + items[i].second);
15        }
16    }
17 }

```

## 8.7 Lis Seg

```

1 vector<int> a(n);
2 for (int i = 0; i < n; i++) cin >> a[i];
3 vector<int> sorted_a = a;
4 sort(sorted_a.begin(), sorted_a.end());
5 for (int i = 0; i < n; i++) {

```

```

6         a[i] = lower_bound(sorted_a.begin(), sorted_a
7         .end(), a[i]) - sorted_a.begin();
8     }
9     SegTreeMx segmx;
10    segmx.build(n);
11    vector<int> dp(n, 1);
12    for (int k = 0; k < n; k++) {
13        if (a[k] > 0) {
14            dp[k] = segmx.query(0, a[k] - 1) + 1;
15        }
16        segmx.update(a[k], dp[k]);
17    }
18    cout << *max_element(dp.begin(), dp.end()) << '\n'
19    ;

```

## 8.8 Disjoint Blocks

```

1 // Número máximo de subarrays disjuntos com soma x
2 // usando apenas
3 // prefixo até i (ou seja, considerando prefixo a
4 // [1..i]).
5 int disjointSumX(vector<int> &a, int x) {
6     int n = a.size();
7     map<int, int> best; // best[pref] = melhor dp
8     visto para esse pref
9     best[0] = 0;
10    int pref = 0;
11    vector<int> dp(n + 1, 0); // dp[0] = 0
12    for (int i = 1; i <= n; i++) {
13        pref += a[i - 1];
14        // não pegar subarray terminando em i
15        dp[i] = dp[i-1];
16        // pega se existir prefixo anterior e
17        atualiza best
18        auto it = best.find(pref - x);
19        if (it != best.end()) {
20            dp[i] = max(dp[i], it->second + 1);
21        }
22        best[pref] = max(best[pref], dp[i]);
23    }
24    return dp[n];
25 }

```

## 9 General

### 9.1 Brute Choose

```

1 vector<int> elements;
2 int N, K;
3 vector<int> comb;
4
5
6 void brute_choose(int i) {
7     if (comb.size() == K) {
8         for (int j = 0; j < comb.size(); j++) {
9             cout << comb[j] << ' ';
10        }
11        cout << '\n';
12        return;
13    }
14    if (i == N) return;
15    int r = N - i;
16    int preciso = K - comb.size();
17    if (r < preciso) return;
18    comb.push_back(elements[i]);
19    brute_choose(i + 1);
20    comb.pop_back();
21    brute_choose(i + 1);
22 }

```

### 9.2 Struct

```

1 struct Pessoa{
2     // Atributos
3     string nome;
4     int idade;
5
6     // Comparador
7     bool operator<(const Pessoa& other) const{
8         if(idade != other.idade) return idade > other
9         .idade;
10        else return nome > other.nome;
11    }

```

### 9.3 Mex

```

1 struct MEX {
2     map<int, int> f;
3     set<int> falta;
4     int tam;
5     MEX(int n) : tam(n) {
6         for (int i = 0; i <= n; i++) falta.insert(i);
7     }
8     void add(int x) {
9         f[x]++;
10        if (f[x] == 1 && x >= 0 && x <= tam) {
11            falta.erase(x);
12        }
13    }
14    void rem(int x) {
15        if (f.count(x) && f[x] > 0) {
16            f[x]--;
17            if (f[x] == 0 && x >= 0 && x <= tam) {
18                falta.insert(x);
19            }
20        }
21    }
22    int get() {
23        if (falta.empty()) return tam + 1;
24        return *falta.begin();
25    }
26 };

```

### 9.4 Bitwise

```

1 int check_kth_bit(int x, int k) {
2     return (x >> k) & 1;
3 }
4
5 void print_on_bits(int x) {
6     for (int k = 0; k < 32; k++) {
7         if (check_kth_bit(x, k)) {
8             cout << k << ' ';
9         }
10    }
11    cout << '\n';
12 }
13
14 int count_on_bits(int x) {
15     int ans = 0;
16     for (int k = 0; k < 32; k++) {
17         if (check_kth_bit(x, k)) {
18             ans++;
19         }
20    }
21    return ans;
22 }
23
24 bool is_even(int x) {
25     return ((x & 1) == 0);
26 }
27
28 int set_kth_bit(int x, int k) {
29     return x | (1 << k);

```

```

30 }
31
32 int unset_kth_bit(int x, int k) {
33     return x & ~(1 << k);
34 }
35
36 int toggle_kth_bit(int x, int k) {
37     return x ^ (1 << k);
38 }
39
40 bool check_power_of_2(int x) {
41     return count_on_bits(x) == 1;
42 }

```

## 10 Geometry

### 10.1 Convex Hull

```

1 #include <bits/stdc++.h>
2
3 using namespace std;
4 #define int long long
5 typedef int cod;
6
7 struct point
8 {
9     cod x,y;
10     point(cod x = 0, cod y = 0): x(x), y(y)
11     {}
12
13     double modulo()
14     {
15         return sqrt(x*x + y*y);
16     }
17
18     point operator+(point o)
19     {
20         return point(x+o.x, y+o.y);
21     }
22     point operator-(point o)
23     {
24         return point(x - o.x , y - o.y);
25     }
26     point operator*(cod t)
27     {
28         return point(x*t, y*t);
29     }
30     point operator/(cod t)
31     {
32         return point(x/t, y/t);
33     }
34
35     cod operator*(point o)
36     {
37         return x*o.x + y*o.y;
38     }
39     cod operator^(point o)
40     {
41         return x*o.y - y * o.x;
42     }
43     bool operator<(point o)
44     {
45         if( x != o.x) return x < o.x;
46         return y < o.y;
47     }
48 };
49
50 int ccw(point p1, point p2, point p3)
51 {
52     cod cross = (p2-p1) ^ (p3-p1);
53     if(cross == 0) return 0;

```

```

55     else if(cross < 0) return -1;
56     else return 1;
57 }
58
59 vector <point> convex_hull(vector<point> p)
60 {
61     sort(p.begin(), p.end());
62     vector<point> L,U;
63
64     //Lower
65     for(auto pp : p)
66     {
67         while(L.size() >= 2 and ccw(L[L.size() - 2],
68             L.back(), pp) == -1)
69             // Ãr -1 pq eu nÃo quero excluir os
70             // colineares
71             L.pop_back();
72         L.push_back(pp);
73     }
74
75     reverse(p.begin(), p.end());
76
77     //Upper
78     for(auto pp : p)
79     {
80         while(U.size() >= 2 and ccw(U[U.size()-2], U
81             .back(), pp) == -1)
82             U.pop_back();
83         U.push_back(pp);
84     }
85
86     L.pop_back();
87     L.insert(L.end(), U.begin(), U.end()-1);
88     return L;
89 }
90
91 cod area(vector<point> v)
92 {
93     int ans = 0;
94     int aux = (int)v.size();
95     for(int i = 2; i < aux; i++)
96     {
97         ans += ((v[i] - v[0])^(v[i-1] - v[0]))/2;
98     }
99     ans = abs(ans);
100     return ans;
101 }
102
103 int bound(point p1 , point p2)
104 {
105     return __gcd(abs(p1.x-p2.x), abs(p1.y-p2.y));
106 }
107
108 //teorema de pick [pontos = A - (bound+points)/2 + 1]
109
110 int32_t main()
111 {
112
113     int n;
114     cin >> n;
115
116     vector<point> v(n);
117     for(int i = 0; i < n; i++)
118     {
119         cin >> v[i].x >> v[i].y;
120     }
121
122     vector <point> ch = convex_hull(v);
123
124     cout << ch.size() << '\n';

```

```

125     for(auto p : ch) cout << p.x << " " << p.y << "\n" 48     else return 1; // inside
126     "; 49 }
127     return 0;
128 }

```

## 10.2 Inside Polygon

```

1 // Convex O(logn)
2
3 bool insideT(point a, point b, point c, point e){
4     int x = ccw(a, b, e);
5     int y = ccw(b, c, e);
6     int z = ccw(c, a, e);
7     return !((x==1 or y==1 or z==1) and (x==-1 or y
8     ==-1 or z==-1));
9 }
10
11 bool inside(vp &p, point e){ // ccw
12     int l=2, r=(int)p.size()-1;
13     while(l<r){
14         int mid = (l+r)/2;
15         if(ccw(p[0], p[mid], e) == 1)
16             l=mid+1;
17         else{
18             r=mid;
19         }
20     }
21     // bordo
22     // if(r==(int)p.size()-1 and ccw(p[0], p[r], e)
23     ==0) return false;
24     // if(r==2 and ccw(p[0], p[1], e)==0) return
25     false;
26     // if(ccw(p[r], p[r-1], e)==0) return false;
27     return insideT(p[0], p[r-1], p[r], e);
28 }
29
30 // Any O(n)
31
32 int inside(vp &p, point pp){
33     // 1 - inside / 0 - boundary / -1 - outside
34     int n = p.size();
35     for(int i=0; i<n; i++){
36         int j = (i+1)%n;
37         if(line({p[i], p[j]}).inside_seg(pp))
38             return 0;
39     }
40     int inter = 0;
41     for(int i=0; i<n; i++){
42         int j = (i+1)%n;
43         if(p[i].x <= pp.x and pp.x < p[j].x and ccw(p
44         [i], p[j], pp)==1)
45             inter++; // up
46         else if(p[j].x <= pp.x and pp.x < p[i].x and
47         ccw(p[i], p[j], pp)==-1)
48             inter++; // down
49     }
50     if(inter%2==0) return -1; // outside

```

## 10.3 Point Location

```

1
2 int32_t main(){
3     sws;
4
5     int t; cin >> t;
6
7     while(t--){
8
9         int x1, y1, x2, y2, x3, y3; cin >> x1 >> y1
10        >> x2 >> y2 >> x3 >> y3;
11
12        int deltax1 = (x1-x2), deltax2 = (x1-x3),
13        deltax3 = (x2-x3);
14        int compx = (x1-x3), compy = (y1-y3);
15
16        int ans = (deltax1*compy) - (compx*deltax2);
17
18        if(ans == 0){cout << "TOUCH\n"; continue;}
19        if(ans < 0){cout << "RIGHT\n"; continue;}
20        if(ans > 0){cout << "LEFT\n"; continue;}
21    }
22    return 0;

```

## 10.4 Lattice Points

```

1 ll gcd(ll a, ll b) {
2     return b == 0 ? a : gcd(b, a % b);
3 }
4 ll area_triangulo(ll x1, ll y1, ll x2, ll y2, ll x3,
5     ll y3) {
6     return abs(x1 * (y2 - y3) + x2 * (y3 - y1) + x3 *
7     (y1 - y2));
8 }
9 ll pontos_borda(ll x1, ll y1, ll x2, ll y2) {
10    return gcd(abs(x2 - x1), abs(y2 - y1));
11 }
12
13 int32_t main() {
14     ll x1, y1, x2, y2, x3, y3;
15     cin >> x1 >> y1;
16     cin >> x2 >> y2;
17     cin >> x3 >> y3;
18
19     ll area = area_triangulo(x1, y1, x2, y2, x3, y3);
20     ll tot_borda = pontos_borda(x1, y1, x2, y2) +
21     pontos_borda(x2, y2, x3, y3) + pontos_borda(x3,
22     y3, x1, y1);
23
24     ll ans = (area - tot_borda) / 2 + 1;
25     cout << ans << endl;
26
27     return 0;
28 }

```