

Competitive Programming Notebook

Programadores Roblox

Contents

1 String	6.7 Acha Pontes	10
1.1 Trie	6.8 Edmonds-karp	10
1.2 Hashing	6.9 Kruskal	10
1.3 Z Function	6.10 Bellman Ford	10
1.4 Kmp	6.11 Lca Jc	11
2 DS	6.12 Lca	11
2.1 Seg Lazy Pa	6.13 Kosaraju	11
2.2 Segtree Iterativa	6.14 Pega Ciclo	12
2.3 Merge Sort Tree	6.15 Min Cost Max Flow	12
2.4 Ordered Set E Map	7 Primitives	13
2.5 Sparse Table	8 DP	13
2.6 Psum 2d	8.1 Lis	13
2.7 Segtree Lazy	8.2 Edit Distance	13
2.8 Min Queue	8.3 Bitmask	13
2.9 Dsu	8.4 Lcs	13
2.10 Bit	8.5 Digit	13
3 Search and sort	8.6 Knapsack	13
3.1 Merge Sort	8.7 Lis Seg	14
3.2 Monotonic Stack	8.8 Disjoint Blocks	14
4 Stress	9 General	14
4.1 Gen	9.1 Brute Choose	14
5 Math	9.2 Struct	14
5.1 Combinatorics	9.3 Mex	14
5.2 Equacao Diofantina	9.4 Count Permutations	14
5.3 Multiplicacao Matriz	9.5 Bitwise	14
5.4 Discrete Log	10 Geometry	15
5.5 Segment Sieve	10.1 Convex Hull	15
5.6 Totient	10.2 Inside Polygon	16
5.7 Menor Fator Primo	10.3 Point Location	16
5.8 Exgcd	10.4 Lattice Points	16
5.9 Fexp		
5.10 Divisores		
5.11 Crivo		
5.12 Mod Inverse		
5.13 Base Calc		
5.14 Fft		
6 Graph	8	
6.1 Dijkstra	6.1 Dijkstra	8
6.2 Floyd Warshall	6.2 Floyd Warshall	8
6.3 Eulerian Path	6.3 Eulerian Path	8
6.4 Dinitz	6.4 Dinitz	9
6.5 Khan	6.5 Khan	9
6.6 Topological Sort	6.6 Topological Sort	10

1 String

1.1 Trie

```

1 // Trie por array
2 int trie[MAXN][26];
3 int tot_nos = 0;
4 vector<bool> acaba(MAXN, false);
5 vector<int> contador(MAXN, 0);
6
7 void insere(string s) {
8     int no = 0;
9     for(auto &c : s) {
10         if(trie[no][c - 'a'] == 0) {
11             trie[no][c - 'a'] = ++tot_nos;
12         }
13         no = trie[no][c - 'a'];
14         contador[no]++;
15     }
16     acaba[no] = true;
17 }
18
19 bool busca(string s) {
20     int no = 0;
21     for(auto &c : s) {
22         if(trie[no][c - 'a'] == 0) {
23             return false;
24         }
25         no = trie[no][c - 'a'];
26     }
27     return acaba[no];
28 }
29
30 int isPref(string s) {
31     int no = 0;
32     for(auto &c : s) {
33         if(trie[no][c - 'a'] == 0) {
34             return -1;
35         }
36         no = trie[no][c - 'a'];
37     }
38     return contador[no];
39 }
```

1.2 Hashing

```

1 // String Hash template
2 // constructor(s) - O(|s|)
3 // query(l, r) - returns the hash of the range [l,r] from
4 // left to right - O(1)
5 // query_inv(l, r) from right to left - O(1)
6 // patrocinado por tiagodfs
7 mt19937 rng(time(nullptr));
8
9 struct Hash {
10     const int X = rng();
11     const int MOD = 1e9+7;
12     int n; string s;
13     vector<int> h, hi, p;
14     Hash() {}
15     Hash(string s): s(s), n(s.size()), h(n), hi(n), p(n) {
16         for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1) % MOD;
17         for (int i=0;i<n;i++)
18             h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD;
19         for (int i=n-1;i>=0;i--)
20             hi[i] = (s[i] + (i+1<n ? hi[i+1]:0) * X) % MOD;
21     }
22     int query(int l, int r) {
23         int hash = (h[r] - (l ? h[l-1]*p[r-l+1]%MOD : 0));
24         return hash < 0 ? hash + MOD : hash;
25     }
26     int query_inv(int l, int r) {
27         int hash = (hi[l] - (r+1 < n ? hi[r+1]*p[r-l+1] % MOD
28 : 0));
29         return hash < 0 ? hash + MOD : hash;
30     }
}
```

1.3 Z Function

```

1 vector<int> z_function(string s) {
2     int n = s.size();
```

```

3     vector<int> z(n);
4     int l = 0, r = 0;
5     for(int i = 1; i < n; i++) {
6         if(i < r) {
7             z[i] = min(r - i, z[i - 1]);
8         }
9         while(i + z[i] < n && s[z[i]] == s[i + z[i]]) {
10             z[i]++;
11         }
12         if(i + z[i] > r) {
13             l = i;
14             r = i + z[i];
15         }
16     }
17     return z;
18 }
```

1.4 Kmp

```

1 vector<int> kmp(string &s) {
2     int m = s.size();
3     vector<int> lsp(m, 0);
4     for (int i = 1, j = 0; i < m; i++) {
5         while (j > 0 && s[j] != s[i]) j = lsp[j - 1];
6         if (s[i] == s[j]) j++;
7         lsp[i] = j;
8     }
9     return lsp;
10 }
```

2 DS

2.1 Seg Lazy Pa

```

1 /* Notas
2  PA eh da forma a0 (a) e razÄo (d)
3  na hora de propagar o lazy
4  aplica no no S = (a0 + (a0 + (n - 1) * d)) * n / 2 ( variante da soma total do no)
5  pros filhos, o da esquerda eh normal
6  lazy_a[esq] += lazy_a[x]
7  lazy_d[esq] += lazy_d[x]
8  pro da direita tem que mudar o a (que eh o elemento inicial
naquele no da direita)
9  lazy_a[dir] += a + len_esq * (d)
10 lazy_d[dir] += lazy_d[x]
11 */
12
13 int gauss(int n, int a, int d) {
14     // (a0 + an) * n / 2
15     if (n <= 0)
16         return 0;
17     return (a + (a + (n - 1) * d)) * n / 2;
18 }
19
20 struct SegTree {
21     int n;
22     vector<int> v, lazy_a, lazy_d, tree;
23     SegTree(vector<int> &a) : v(a), n(a.size()) {
24         tree.resize(4 * n);
25         lazy_a.resize(4 * n, 0);
26         lazy_d.resize(4 * n, 0);
27         build(1, 0, n - 1);
28     }
29     void build(int x, int lx, int rx) {
30         if (lx == rx) {
31             tree[x] = v[lx];
32             return;
33         }
34         int mid = (lx + rx) / 2;
35         build(2 * x, lx, mid);
36         build(2 * x + 1, mid + 1, rx);
37         tree[x] = tree[2 * x] + tree[2 * x + 1];
38     }
39     int query(int x, int lx, int rx, int l, int r) {
40         push(x, lx, rx);
41         if (lx >= l && rx <= r)
42             return tree[x];
43         if (lx > r || rx < l)
44             return 0;
45         int mid = (lx + rx) / 2;
46         return query(2 * x, lx, mid, l, r) + query(2 * x + 1, mid
+ 1, rx, l, r);
```

```

47 }
48 int query(int l, int r) {
49   return query(1, 0, n - 1, l, r);
50 }
51 void push(int x, int lx, int rx) {
52   if (lazy_a[x] && lazy_d[x]) {
53     int tam = rx - lx + 1;
54     tree[x] += gauss(tam, lazy_a[x], lazy_d[x]);
55     if (lx != rx) {
56       int mid = (lx + rx) / 2;
57       int tam_esq = mid - lx + 1;
58       lazy_a[2 * x] += lazy_a[x];
59       lazy_d[2 * x] += lazy_d[x];
60       lazy_a[2 * x + 1] += (lazy_a[x] + tam_esq * lazy_d[x]
61     });
62     lazy_d[2 * x + 1] += lazy_d[x];
63   }
64   lazy_a[x] = lazy_d[x] = 0;
65 }
66 void update(int x, int lx, int rx, int l, int r, int a, int d) {
67   push(x, lx, rx);
68   if (lx >= l && rx <= r) {
69     lazy_a[x] += a + (lx - 1) * d;
70     lazy_d[x] += d;
71     push(x, lx, rx);
72   }
73   if (lx > r || rx < l)
74     return;
75   int mid = (lx + rx) / 2;
76   update(2 * x, lx, mid, l, r, a, d);
77   update(2 * x + 1, mid + 1, rx, l, r, a, d);
78   tree[x] = tree[2 * x] + tree[2 * x + 1];
79 }
80 void update(int l, int r, int a, int d) {
81   update(1, 0, n - 1, l, r, a, d);
82 }
83 }
84 
```

2.2 Segtree Iterativa

```

1 // Exemplo de uso:
2 // SegTree<int> st(vetor);
3 // range_query e point_update
4 template <typename T>
5 struct SegTree {
6   int n;
7   vector<T> tree;
8   T neutral_value = 0;
9   T combine(T a, T b) {
10     return a + b;
11   }
12
13 SegTree(const vector<T>& data) {
14   n = data.size();
15   tree.resize(2 * n, neutral_value);
16
17   for (int i = 0; i < n; i++)
18     tree[n + i] = data[i];
19
20   for (int i = n - 1; i > 0; --i)
21     tree[i] = combine(tree[i * 2], tree[i * 2 + 1]);
22 }
23 T range_query(int l, int r) {
24   T res_l = neutral_value, res_r = neutral_value;
25
26   for (l += n, r += n + 1; l < r; l >>= 1, r >>= 1) {
27     if (l & 1) res_l = combine(res_l, tree[l++]);
28     if (r & 1) res_r = combine(tree[-r], res_r);
29   }
30
31   return combine(res_l, res_r);
32 }
33 void update(int pos, T new_val) {
34   tree[pos += n] = new_val;
35   for (pos >>= 1; pos > 0; pos >>= 1)
36     tree[pos] = combine(tree[2 * pos], tree[2 * pos +
37   1]);
38 }

```

2.3 Merge Sort Tree

```

1 #define all(x) x.begin(), x.end()
2
3 struct MST {
4   int n;
5   vector<vector<int>> tree;
6   MST(vector<int> &a) {
7     n = a.size();
8     tree.resize(4 * n);
9     build(1, 0, n - 1, a);
10 }
11 void build(int x, int lx, int rx, vector<int> &a) {
12   if (lx == rx) {
13     tree[x] = {a[lx]};
14     return;
15   }
16   int mid = lx + (rx - lx) / 2;
17   build(2 * x, lx, mid, a);
18   build(2 * x + 1, mid + 1, rx, a);
19   auto &L = tree[2 * x], &R = tree[2 * x + 1];
20   tree[x].resize(L.size() + R.size());
21   merge(all(L), all(R), tree[x].begin());
22 }
23 int query(int x, int lx, int rx, int l, int r, int val) {
24   if (lx > r || rx < l) return 0;
25   if (lx >= l && rx <= r) {
26     auto &v = tree[x];
27     return lower_bound(all(v), val) - v.begin();
28   }
29   int mid = lx + (rx - lx) / 2;
30   return query(2 * x, lx, mid, l, r, val) + query(2 * x +
31   1, mid + 1, rx, l, r, val);
32 }
33 int query(int l, int r, int val) {
34   if (l > r) return 0;
35   return query(1, 0, n - 1, l, r, val);
36 }
37
38 /* mst.query(l, r, 1) retorna quantos caras distintos no
range
39 map<int, int> last;
40 for (int i = 0; i < n; i++) {
41   if (last.count(a[i])) {
42     esq[i] = last[a[i]];
43   } else {
44     esq[i] = -1;
45   }
46   last[a[i]] = i;
47 }
48 MST mst(esq);
49 jogar vetor de ultima aparicao na seg
50 */

```

2.4 Ordered Set E Map

```

1
2 #include<ext/pb_ds/assoc_container.hpp>
3 #include<ext/pb_ds/tree_policy.hpp>
4 using namespace __gnu_pbds;
5 using namespace std;
6
7 template<typename T> using ordered_multiset = tree<T,
8           null_type, less_equal<T>, rb_tree_tag,
9           tree_order_statistics_node_update>;
10 template <typename T> using o_set = tree<T, null_type, less<T>,
11           rb_tree_tag, tree_order_statistics_node_update>;
12 template <typename T, typename R> using o_map = tree<T, R,
13           less<T>, rb_tree_tag, tree_order_statistics_node_update
14           >;
15
16 int main() {
17   int i, j, k, n, m;
18   o_set<int> st;
19   st.insert(1);
20   st.insert(2);
21   cout << *st.find_by_order(0) << endl; // k-esimo elemento
22   cout << st.order_of_key(2) << endl; // numero de elementos
23   menores que k
24   o_map<int, int> mp;
25   mp.insert({1, 10});
26   mp.insert({2, 20});
27   cout << mp.find_by_order(0)->second << endl; // k-esimo
28   elemento
29   cout << mp.order_of_key(2) << endl; // numero de elementos
30   (chave) menores que k
31   return 0;
32 }

```

24 }

2.5 Sparse Table

```

1 // 0-index, O(1)
2 struct SparseTable {
3     vector<vector<int>> st;
4     int max_log;
5     SparseTable(vector<int>& arr) {
6         int n = arr.size();
7         max_log = floor(log2(n)) + 1;
8         st.resize(n, vector<int>(max_log));
9         for (int i = 0; i < n; i++) {
10             st[i][0] = arr[i];
11         }
12         for (int j = 1; j < max_log; j++) {
13             for (int i = 0; i + (1 << j) <= n; i++) {
14                 st[i][j] = max(st[i][j - 1], st[i + (1 << (j
15                     - 1))][j - 1]);
16             }
17         }
18     }
19     int query(int L, int R) {
20         int tamanho = R - L + 1;
21         int k = floor(log2(tamanho));
22         return max(st[L][k], st[R - (1 << k) + 1][k]);
23     }

```

2.6 Psum 2d

```

1 vector<vector<int>> psum(h+1, vector<int>(w+1, 0));
2 for (int i=1; i<=h; i++){
3     for (int j=1; j<=w; j++){
4         cin >> psum[i][j];
5         psum[i][j] += psum[i-1][j]+psum[i][j-1]-psum[i-1][j
-1];
6     }
7 }
8 // retorna a psum2d do intervalo inclusivo [(a, b), (c, d)]
9 int retangulo(int a, int b, int c, int d){
10    c = min(c, h), d = min(d, w);
11    a = max(0, a-1), b = max(0, b-1);
12    return v[c][d]-v[a][d]-v[c][b]+v[a][b];
13 }

```

2.7 Segtree Lazy

```

1 /*
2 Seg com double Lazy de soma e de set
3 tipo 1 - soma em range
4 tipo 2 - set em range
5 */
6 struct SegTree {
7     int n;
8     vector<int> v, tree;
9     vector<int> lazy_soma, lazy_set;
10    SegTree(vector<int> &a) : v(a), n(a.size()) {
11        tree.resize(4 * n);
12        lazy_soma.resize(4 * n, 0);
13        lazy_set.resize(4 * n, -1);
14        build(1, 0, n - 1);
15    };
16    void build(int x, int lx, int rx) {
17        if (lx == rx) {
18            tree[x] = v[lx];
19            return;
20        }
21        int mid = (lx + rx) / 2;
22        build(2 * x, lx, mid);
23        build(2 * x + 1, mid + 1, rx);
24        tree[x] = tree[2 * x] + tree[2 * x + 1];
25    }
26    void seta(int x, int lx, int rx, int val) {
27        tree[x] = val * (rx - lx + 1);
28        lazy_set[x] = val;
29        lazy_soma[x] = 0;
30    }
31    void soma(int x, int lx, int rx, int val) {
32        tree[x] += val * (rx - lx + 1);
33        if (lazy_set[x] != -1) {
34            lazy_set[x] += val;
35        } else {

```

```

36            lazy_soma[x] += val;
37        }
38    }
39    void push(int x, int lx, int rx) {
40        int mid = (lx + rx) / 2;
41        if (lazy_set[x] != -1) {
42            if (lx != rx) {
43                seta(2 * x, lx, mid, lazy_set[x]);
44                seta(2 * x + 1, mid + 1, rx, lazy_set[x]);
45            }
46            lazy_set[x] = -1;
47        }
48        if (lazy_soma[x] != 0) {
49            if (lx != rx) {
50                soma(2 * x, lx, mid, lazy_soma[x]);
51                soma(2 * x + 1, mid + 1, rx, lazy_soma[x]);
52            }
53            lazy_soma[x] = 0;
54        }
55    }
56    void update(int x, int lx, int rx, int l, int r, int val,
57                int type) {
58        push(x, lx, rx);
59        if (lx >= l && rx <= r) {
60            if (type == 1) soma(x, lx, rx, val);
61            else seta(x, lx, rx, val);
62            push(x, lx, rx);
63            return;
64        }
65        if (lx > r || rx < l) return;
66        int mid = (lx + rx) / 2;
67        update(2 * x, lx, mid, l, r, val, type);
68        update(2 * x + 1, mid + 1, rx, l, r, val, type);
69        tree[x] = tree[2 * x] + tree[2 * x + 1];
70    }
71    void update(int l, int r, int val, int type) {
72        update(1, 0, n - 1, l, r, val, type);
73    }
74    int query(int x, int lx, int rx, int l, int r) {
75        push(x, lx, rx);
76        if (lx >= l && rx <= r) return tree[x];
77        if (lx > r || rx < l) return 0;
78        int mid = (lx + rx) / 2;
79        return query(2 * x, lx, mid, l, r) + query(2 * x + 1, mid
+ 1, rx, l, r);
80    }
81    int query(int l, int r) {
82        return query(1, 0, n - 1, l, r);
83    }

```

2.8 Min Queue

```

1 struct MinQueue {
2     deque<pair<int, int>> dq;
3     void push(int val, int idx) {
4         while (!dq.empty() && dq.back().second >= val) dq.
5         pop_back();
6         dq.emplace_back(val, idx);
7     }
8     void pop(int idx) {
9         if (!dq.empty() && dq.front().second == idx) {
10            dq.pop_front();
11        }
12        int get() {
13            return dq.front().first;
14        }
15        bool empty() {
16            return dq.empty();
17        }
18    };
19    /*
20     considerando janela de tamanho K
21     mq.push(v[i], i);
22     if (i >= k) {
23         mq.pop(i - k);
24     }
25     if (i >= k - 1) {
26         result.push_back(mq.get());
27     }
28 */

```

2.9 Dsu

```

1 struct DSU {
2   vector<int> par, rank, sz;
3   int c;
4   DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n + 1, 1), c(n) {
5     for (int i = 1; i <= n; ++i) par[i] = i;
6   }
7   int find(int i) {
8     return (par[i] == i ? i : (par[i] = find(par[i])));
9   }
10  bool same(int i, int j) {
11    return find(i) == find(j);
12  }
13  int get_size(int i) {
14    return sz[find(i)];
15  }
16  int count() {
17    return c; // quantos componentes conexos
18  }
19  int merge(int i, int j) {
20    if ((i = find(i)) == (j = find(j))) return -1;
21    else --c;
22    if (rank[i] > rank[j]) swap(i, j);
23    par[i] = j;
24    sz[j] += sz[i];
25    if (rank[i] == rank[j]) rank[j]++;
26    return j;
27  }
28 };

```

2.10 Bit

```

1 struct BIT {
2   int n;
3   vector<int> bit;
4   BIT(int n = 0): n(n), bit(n + 1, 0) {}
5   void add(int i, int delta) {
6     for(; i <= n; i += i & -i) bit[i] += delta;
7   }
8   int sum(int i) {
9     int r = 0;
10    for(; i > 0; i -= i & -i) r += bit[i];
11    return r;
12  }
13  int range_sum(int l, int r) {
14    if (r < l) return 0;
15    return sum(r) - sum(l - 1);
16  }
17 };

```

3 Search and sort

3.1 Merge Sort

```

1 int mergeAndCount(vector<int>& v, int l, int m, int r) {
2   int x = m - l + 1;
3   int y = r - m;
4   vector<int> left(x), right(y);
5   for (int i = 0; i < x; i++) left[i] = v[l + i];
6   for (int j = 0; j < y; j++) right[j] = v[m + 1 + j];
7   int i = 0, j = 0, k = l;
8   int swaps = 0;
9   while (i < x && j < y) {
10     if (left[i] <= right[j]) {
11       v[k++] = left[i++];
12     } else {
13       v[k++] = right[j++];
14       swaps += (x - i);
15     }
16   }
17   while (i < x) v[k++] = left[i++];
18   while (j < y) v[k++] = right[j++];
19   return swaps;
20 }
21
22 int mergeSort(vector<int>& v, int l, int r) {
23   int swaps = 0;
24   if (l < r) {
25     int m = l + (r - 1) / 2;
26     swaps += mergeSort(v, l, m);
27     swaps += mergeSort(v, m + 1, r);
28     swaps += mergeAndCount(v, l, m, r);
29   }

```

3.2 Monotonic Stack

```

30   return swaps;
31 }

1 vector<int> find_esq(vector<int> &v, bool maior) {
2   int n = v.size();
3   vector<int> result(n);
4   stack<int> s;
5   for (int i = 0; i < n; i++) {
6     while (!s.empty() && (maior ? v[s.top()] <= v[i] : v[s.top()] >= v[i])) {
7       s.pop();
8     }
9     if (s.empty()) {
10       result[i] = -1;
11     } else {
12       result[i] = v[s.top()];
13     }
14     s.push(i);
15   }
16   return result;
17 }

20 vector<int> find_dir(vector<int> &v, bool maior) {
21   int n = v.size();
22   vector<int> result(n);
23   stack<int> s;
24   for (int i = n - 1; i >= 0; i--) {
25     while (!s.empty() && (maior ? v[s.top()] <= v[i] : v[s.top()] >= v[i])) {
26       s.pop();
27     }
28     if (s.empty()) {
29       result[i] = -1;
30     } else {
31       result[i] = v[s.top()];
32     }
33     s.push(i);
34   }
35   return result;
36 }

```

4 Stress

4.1 Gen

```

1 // pre-compilar os headers:
2 // compilar template com g++ -H e procurar onde esta stdc++.h
3 // criar a pasta bits e incluir com "" ou inves de <>
4 // compilar stress com: g++ -pipe -O3 -fno -march=native -mtune=native gen.ccp
5 // faz bastante diferen a no runtime
6
7 #include <bits/stdc++.h>
8 #include <cstdlib>
9 #include <ctime>
10 using namespace std;
11
12 int randi(int L, int R) { return L + rand() % (R - L + 1); }
13 char randc(char L, char R) { return char(L + rand() % (R - L + 1)); }
14
15 int main(int argc, char** argv) {
16   if (argc > 1) srand(atoi(argv[1]));
17   else srand(time(0));
18
19   int n = randi(1, 100);
20   cout << n << '\n';
21   for (int i = 0; i < n; i++) {
22     cout << randi(-10, 20) << ' ';
23   }
24   cout << '\n';
25 }

```

5 Math

5.1 Combinatorics

```

1 const int MAXN_FATORIAL = 200005;
2 const int MOD = 1e9 + 7;
3 // DEFINE INT LONG LONG PLMDS
4 int fat[MAXN_FATORIAL], fati[MAXN_FATORIAL];
5
6 // (a^b) % m em O(log b)
7 // coloque o fexp
8
9 int inv(int n) { return fexp(n, MOD - 2); }
10
11 void precalc() {
12     fat[0] = 1;
13     fati[0] = 1;
14     for (int i = 1; i < MAXN_FATORIAL; i++) fat[i] = (fat[i - 1] * i) % MOD;
15     fati[MAXN_FATORIAL - 1] = inv(fat[MAXN_FATORIAL - 1]);
16     for (int i = MAXN_FATORIAL - 2; i >= 0; i--) fati[i] = (fati[i + 1] * (i + 1)) % MOD;
17 }
18
19 int choose(int n, int k) {
20     if (k < 0 || k > n) return 0;
21     return (((fat[n] * fati[k]) % MOD) * fati[n - k]) % MOD;
22 }
23
24 // n! / (n-k)!
25 int perm(int n, int k) {
26     if (k < 0 || k > n) return 0;
27     return (fat[n] * fati[n - k]) % MOD;
28 }
29
30 // C_n = (1 / (n+1)) * C(2n, n)
31 int catalan(int n) {
32     if (n < 0 || 2 * n >= MAXN_FATORIAL) return 0;
33     int c2n_n = choose(2 * n, n);
34     return (c2n_n * inv(n + 1)) % MOD;
35 }

```

5.2 Equacao Diofantina

```

1 int extended_gcd(int a, int b, int& x, int& y) {
2     if (a == 0) {
3         x = 0;
4         y = 1;
5         return b;
6     }
7     int x1, y1;
8     int gcd = extended_gcd(b % a, a, x1, y1);
9     x = y1 - (b / a) * x1;
10    y = x1;
11    return gcd;
12 }
13
14 bool solve(int a, int b, int c, int& x0, int& y0) {
15     int x, y;
16     int g = extended_gcd(abs(a), abs(b), x, y);
17     if (c % g != 0) {
18         return false;
19     }
20     x0 = x * (c / g);
21     y0 = y * (c / g);
22     if (a < 0) x0 = -x0;
23     if (b < 0) y0 = -y0;
24     return true;
25 }

```

5.3 Multiplicacao Matriz

```

1 // multiplica matrizes de tamanhos variados, resultando em
2 // uma matriz N*M
3 vector<vector<int>> mm(vector<vector<int>> A, vector<vector<int>> B) {
4     int N = A.size(), M = B[0].size(), K = B.size();
5     vector<vector<int>> C(N, vector<int>(M));
6
7     for (int i = 0; i < N; ++i)
8         for (int j = 0; j < M; ++j)
9             for (int k = 0; k < K; ++k)
10                 C[i][j] = (C[i][j] + A[i][k] * B[k][j] % mod) %
11                     mod;
12
13     return C;
14 }

```

5.4 Discrete Log

```

1 // returns minimum x for which a^x = b (mod m), a and m are
2 // coprime.
3 // if the answer dont need to be greater than some value, the
4 // vector<int> can be removed
5 int discrete_log(int a, int b, int m) {
6     a %= m, b %= m;
7     int n = sqrt(m) + 1;
8
9     int an = 1;
10    for (int i = 0; i < n; ++i)
11        an = (an * 1ll * a) % m;
12
13    unordered_map<int, vector<int>> vals;
14    for (int q = 0, cur = b; q <= n; ++q) {
15        vals[cur].push_back(q);
16        cur = (cur * 1ll * a) % m;
17    }
18
19    int res = LLONG_MAX;
20
21    for (int p = 1, cur = 1; p <= n; ++p) {
22        cur = (cur * 1ll * an) % m;
23        if (vals.count(cur)) {
24            for (int q: vals[cur]){
25                int ans = n * p - q;
26                res = min(res, ans);
27            }
28        }
29    }
30
31    return res;
32 }

```

5.5 Segment Sieve

```

1 // Retorna quantos primos tem entre [l, r] (inclusivo)
2 // precisa de um vetor com os primos ate sqrt(r)
3 int seg_sieve(int l, int r){
4     if (l > r) return 0;
5     vector<bool> is_prime(r - l + 1, true);
6     if (l == 1) is_prime[0] = false;
7
8     for (int p : primos){
9         if (p * p > r) break;
10        int start = max(p * p, (l + p - 1) / p * p);
11        for (int j = start; j <= r; j += p){
12            if (j >= l) {
13                is_prime[j - 1] = false;
14            }
15        }
16    }
17
18    return accumulate(all(is_prime), 0ll);
19 }

```

5.6 Totient

```

1 // phi(n) = n * (1 - 1/p1) * (1 - 1/p2) * ...
2 int phi(int n) {
3     int result = n;
4     for (int i = 2; i * i <= n; i++) {
5         if (n % i == 0) {
6             while (n % i == 0)
7                 n /= i;
8             result -= result / i;
9         }
10    }
11    if (n > 1) // SE n sobrou, ele Ã' um fator primo
12        result -= result / n;
13    return result;
14 }
15
16 // crivo phi
17 const int MAXN_PHI = 1000001;
18 int phiv[MAXN_PHI];
19 void phi_sieve() {
20     for (int i = 0; i < MAXN_PHI; i++) phiv[i] = i;
21     for (int i = 2; i < MAXN_PHI; i++) {
22         if (phiv[i] == i) {
23             for (int j = i; j < MAXN_PHI; j += i) phiv[j] =
24                 phiv[j] / i;
25         }
26     }

```

5.7 Menor Fator Primo

```

1 const int MAXN = 1000001;
2 int spf[MAXN];
3 vector<int> primos;
4
5 void crivo() {
6     for (int i = 0; i < MAXN; i++) spf[i] = [i];
7     for (int i = 2; i * i < MAXN; i++) {
8         if (spf[i] == i) {
9             for (int j = i * i; j < MAXN; j += i) {
10                 if (spf[j] == j) {
11                     spf[j] = i;
12                 }
13             }
14         }
15     }
16     for (int i = 2; i < MAXN; i++) {
17         if (spf[i] == i) {
18             primos.push_back(i);
19         }
20     }
21 }
22
23 map<int, int> fatora(int n) {
24     map<int, int> fatores;
25     while (n > 1) {
26         fatores[spf[n]]++;
27         n /= spf[n];
28     }
29     return fatores;
30 }
31
32 int numero_de_divisores(int n) {
33     if (n == 1) return 1;
34     map<int, int> fatores = fatorar(n);
35     int nod = 1;
36     for (auto &[primo, expoente] : fatores) nod *= (expoente
37         + 1);
38     return nod;
39 }
40 // DEFINE INT LONG LONG
41 int soma_dos_divisores(int n) {
42     if (n == 1) return 1;
43     map<int, int> fatores = fatorar(n);
44     int sod = 1;
45     for (auto &[primo, expoente] : fatores) {
46         int termo_soma = 1;
47         int potencia_primo = 1;
48         for (int i = 0; i < expoente; i++) {
49             potencia_primo *= primo;
50             termo_soma += potencia_primo;
51         }
52         sod *= termo_soma;
53     }
54     return sod;
55 }
56 }
```

5.8 Exgcd

```

1 // O retorno da funcao eh {n, m, g}
2 // e significa que gcd(a, b) = g e
3 // n e m sao inteiros tais que an + bm = g
4 array<ll, 3> exgcd(int a, int b) {
5     if (b == 0) return {1, 0, a};
6     auto [m, n, g] = exgcd(b, a % b);
7     return {n, m - a / b * n, g};
8 }
```

5.9 Fexp

```

1 // a^e mod m
2 // O(log n)
3
4 int fexp(int a, int e, int m) {
5     a %= m;
6     int ans = 1;
7     while (e > 0) {
8         if (e & 1) ans = ans*a % m;
9         a = a*a % m;
10        e /= 2;
11    }
12 }
```

```

12     return ans%m;
13 }
```

5.10 Divisores

```

1 // Retorna um vetor com os divisores de x
2 // eh preciso ter o crivo implementado
3 // O(divisores)
4
5 vector<int> divs(int x){
6     vector<int> ans = {1};
7     vector<array<int, 2>> primos; // {primo, expoente}
8
9     while (x > 1) {
10         int p = crivo[x], cnt = 0;
11         while (x % p == 0) cnt++, x /= p;
12         primos.push_back({p, cnt});
13     }
14
15     for (int i=0; i<primos.size(); i++){
16         int cur = 1, len = ans.size();
17
18         for (int j=0; j<primos[i][1]; j++){
19             cur *= primos[i][0];
20             for (int k=0; k<len; k++)
21                 ans.push_back(cur*ans[k]);
22         }
23     }
24
25     return ans;
26 }
```

5.11 Crivo

```

1 // O(n*log(log(n)))
2 bool composto[MAX]
3 for(int i = 1; i <= n; i++) {
4     if(composto[i]) continue;
5     for(int j = 2*i; j <= n; j += i)
6         composto[j] = 1;
7 }
```

5.12 Mod Inverse

```

1 array<int, 2> extended_gcd(int a, int b) {
2     if (b == 0) return {1, 0};
3     auto [x, y] = extended_gcd(b, a % b);
4     return {y, x - (a / b) * y};
5 }
6
7 int mod_inverse(int a, int m) {
8     auto [x, y] = extended_gcd(a, m);
9     return (x % m + m) % m;
10 }
```

5.13 Base Calc

```

1 int char_to_val(char c) {
2     if (c >= '0' && c <= '9') return c - '0';
3     else return c - 'A' + 10;
4 }
5
6 char val_to_char(int val) {
7     if (val >= 0 && val <= 9) return val + '0';
8     else return val - 10 + 'A';
9 }
10
11 int to_base_10(string &num, int bfrom) {
12     int result = 0;
13     int pot = 1;
14     for (int i = num.size() - 1; i >= 0; i--) {
15         if (char_to_val(num[i]) >= bfrom) return -1;
16         result += char_to_val(num[i]) * pot;
17         pot *= bfrom;
18     }
19     return result;
20 }
21
22 string from_base_10(int n, int bto) {
23     if (n == 0) return "0";
24     string result = "";
25     while (n > 0) {
```

```

26     result += val_to_char(n % bto);
27     n /= bto;
28 }
29 reverse(result.begin(), result.end());
30 return result;
31 }
32
33 string convert_base(string &num, int bfrom, int bto) {
34     int n_base_10 = to_base_10(num, bfrom);
35     return from_base_10(n_base_10, bto);
36 }
```

5.14 Fft

```

1 // multiplica dois polinomios em O(NlogN)
2
3 using cd = complex<double>;
4 const double PI = acos(-1);
5
6 void fft(vector<cd> &A, bool invert) {
7     int N = size(A);
8
9     for (int i = 1, j = 0; i < N; i++) {
10        int bit = N >> 1;
11        for (; j & bit; bit >>= 1)
12            j ^= bit;
13        j ^= bit;
14
15        if (i < j)
16            swap(A[i], A[j]);
17    }
18
19    for (int len = 2; len <= N; len <= 1) {
20        double ang = 2 * PI / len * (invert ? -1 : 1);
21        cd wlen(cos(ang), sin(ang));
22        for (int i = 0; i < N; i += len) {
23            cd w(1);
24            for (int j = 0; j < len/2; j++) {
25                cd u = A[i+j], v = A[i+j+len/2] * w;
26                A[i+j] = u + v;
27                A[i+j+len/2] = u - v;
28                w *= wlen;
29            }
30        }
31    }
32
33    if (invert) {
34        for (auto &x : A)
35            x /= N;
36    }
37 }
38
39 vector<int> multiply(vector<int> const &A, vector<int> const &
40     B) {
41     vector<cd> fa(begin(A), end(A)), fb(begin(B), end(B));
42     int N = 1;
43     while (N < size(A) + size(B))
44         N *= 2;
45     fa.resize(N);
46     fb.resize(N);
47
48     fft(fa, false);
49     fft(fb, false);
50     for (int i = 0; i < N; i++)
51         fa[i] *= fb[i];
52     fft(fa, true);
53
54     vector<int> result(N);
55     for (int i = 0; i < N; i++)
56         result[i] = round(fa[i].real());
57 }
```

6 Graph

6.1 Dijkstra

```

1 // SSP com pesos positivos.
2 // O((V + E) log V).
3
4 vector<int> dijkstra(int S) {
5     vector<bool> vis(MAXN, 0);
6     vector<ll> dist(MAXN, LLONG_MAX);
```

```

7     dist[S] = 0;
8     priority_queue<pii, vector<pii>, greater<pii>> pq;
9     pq.push({0, S});
10    while(pq.size()) {
11        ll v = pq.top().second;
12        pq.pop();
13        if(vis[v]) continue;
14        vis[v] = 1;
15        for(auto &[peso, vizinho] : adj[v]) {
16            if(dist[vizinho] > dist[v] + peso) {
17                dist[vizinho] = dist[v] + peso;
18                pq.push({dist[vizinho], vizinho});
19            }
20        }
21    }
22    return dist;
23 }
```

6.2 Floyd Warshall

```

1 // SSP e acha ciclos.
2 // Bom com constraints menores.
3 // O(n^3)
4
5 int dist[501][501];
6
7 void floydWarshall() {
8     for(int k = 0; k < n; k++) {
9         for(int i = 0; i < n; i++) {
10             for(int j = 0; j < n; j++) {
11                 dist[i][j] = min(dist[i][j], dist[i][k] +
12                     dist[k][j]);
13             }
14         }
15     }
16 void solve() {
17     int m, q;
18     cin >> n >> m >> q;
19     for(int i = 0; i < n; i++) {
20         for(int j = i; j < n; j++) {
21             if(i == j) {
22                 dist[i][j] = dist[j][i] = 0;
23             } else {
24                 dist[i][j] = dist[j][i] = linf;
25             }
26         }
27     }
28     for(int i = 0; i < m; i++) {
29         int u, v, w;
30         cin >> u >> v >> w; u--; v--;
31         dist[u][v] = min(dist[u][v], w);
32         dist[v][u] = min(dist[v][u], w);
33     }
34     floydWarshall();
35     while(q--) {
36         int u, v;
37         cin >> u >> v; u--; v--;
38         if(dist[u][v] == linf) cout << -1 << '\n';
39         else cout << dist[u][v] << '\n';
40     }
41 }
```

6.3 Eulerian Path

```

1 /**
2 * versao que assume: #define int long long
3 *
4 * Retorna um caminho/ciclo euleriano em um grafo (se existir).
5 * - g: lista de adjacencia (vector<vector<int>>).
6 * - directed: true se o grafo for dirigido.
7 * - s: vertice inicial.
8 * - e: vertice final (opcional). Se informado, tenta caminho
8 * de s ate e.
9 * - O(Nlog(N))
10 * Retorna vetor com a sequencia de vertices, ou vazio se
11 * impossivel.
12 */
13 vector<int> eulerian_path(const vector<vector<int>>& g, bool
14     directed, int s, int e = -1) {
15     int n = (int)g.size();
16     // copia das adjacencias em multiset para permitir
17     remoção especifica
```

```

15  vector<multiset<int>> h(n);
16  vector<int> in_degree(n, 0);
17  vector<int> result;
18  stack<int> st;
19  // preencher h e indegrees
20  for (int u = 0; u < n; ++u) {
21      for (auto v : g[u]) {
22          ++in_degree[v];
23          h[u].emplace(v);
24      }
25  }
26  st.emplace(s);
27  if (e != -1) {
28      int out_s = (int)h[s].size();
29      int out_e = (int)h[e].size();
30      int diff_s = in_degree[s] - out_s;
31      int diff_e = in_degree[e] - out_e;
32      if (diff_s * diff_e != -1) return {};
33  }
34  for (int u = 0; u < n; ++u) {
35      if (e != -1 && (u == s || u == e)) continue;
36      int out_u = (int)h[u].size();
37      if (in_degree[u] != out_u || (!directed && (in_degree
38 [u] & 1))) {
39          return {};
40      }
41  while (!st.empty()) {
42      int u = st.top();
43      if (h[u].empty()) {
44          result.emplace_back(u);
45          st.pop();
46      } else {
47          int v = *h[u].begin();
48          auto it = h[u].find(v);
49          if (it != h[u].end()) h[u].erase(it);
50          --in_degree[v];
51          if (!directed) {
52              auto it2 = h[v].find(u);
53              if (it2 != h[v].end()) h[v].erase(it2);
54              --in_degree[u];
55          }
56          st.emplace(v);
57      }
58  }
59  for (int u = 0; u < n; ++u) {
60      if (in_degree[u] != 0) return {};
61  }
62  reverse(result.begin(), result.end());
63  return result;
64 }

```

6.4 Dinitz

```

1 // Complexidade: O(V^2E)
2
3 struct FlowEdge {
4     int from, to;
5     long long cap, flow = 0;
6     FlowEdge(int from, int to, long long cap) : from(from),
7               to(to), cap(cap) {}
7 };
8
9 struct Dinic {
10    const long long flow_inf = 1e18;
11    vector<FlowEdge> edges;
12    vector<vector<int>> adj;
13    int n, m = 0;
14    int s, t;
15    vector<int> level, ptr;
16    queue<int> q;
17
18    Dinic(int n, int s, int t) : n(n), s(s), t(t) {
19        adj.resize(n);
20        level.resize(n);
21        ptr.resize(n);
22    }
23
24    void add_edge(int from, int to, long long cap) {
25        edges.emplace_back(from, to, cap);
26        edges.emplace_back(to, from, 0);
27        adj[from].push_back(m);
28        adj[to].push_back(m + 1);
29        m += 2;
30    }
31

```

```

32    bool bfs() {
33        while (!q.empty()) {
34            int from = q.front();
35            q.pop();
36            for (int id : adj[from]) {
37                if (edges[id].cap == edges[id].flow)
38                    continue;
39                if (level[edges[id].to] != -1)
40                    continue;
41                level[edges[id].to] = level[from] + 1;
42                q.push(edges[id].to);
43            }
44        }
45        return level[t] != -1;
46    }
47
48    long long dfs(int from, long long pushed) {
49        if (pushed == 0)
50            return 0;
51        if (from == t)
52            return pushed;
53        for (int& cid = ptr[from]; cid < (int)adj[from].size
54 (); cid++) {
55            int id = adj[from][cid];
56            int to = edges[id].to;
57            if (level[from] + 1 != level[to])
58                continue;
59            long long tr = dfs(to, min(pushed, edges[id].cap
60 - edges[id].flow));
61            if (tr == 0)
62                continue;
63            edges[id].flow += tr;
64            edges[id ^ 1].flow -= tr;
65            return tr;
66        }
67        return 0;
68    }
69
70    long long flow() {
71        long long f = 0;
72        while (true) {
73            fill(level.begin(), level.end(), -1);
74            level[s] = 0;
75            q.push(s);
76            if (!bfs())
77                break;
78            fill(ptr.begin(), ptr.end(), 0);
79            while (long long pushed = dfs(s, flow_inf)) {
80                f += pushed;
81            }
82        }
83    }
84 }

```

6.5 Khan

```

1 // topo-sort DAG
2 // lexicograficamente menor.
3 // N: numero de Vértices (1-indexado)
4 // adj: lista de adjacencia do grafo
5
6 const int MAXN = 5 * 1e5 + 2;
7 vector<int> adj[MAXN];
8 int N;
9
10 vector<int> kahn() {
11     vector<int> indegree(N + 1, 0);
12     for (int u = 1; u <= N; u++) {
13         for (int v : adj[u]) {
14             indegree[v]++;
15         }
16     }
17     priority_queue<int, vector<int>, greater<int>> pq;
18     for (int i = 1; i <= N; i++) {
19         if (indegree[i] == 0) {
20             pq.push(i);
21         }
22     }
23     vector<int> result;
24     while (!pq.empty()) {
25         int u = pq.top();
26         pq.pop();
27         result.push_back(u);
28         for (int v : adj[u]) {

```

```

29         indegree[v]--;
30         if (indegree[v] == 0) {
31             pq.push(v);
32         }
33     }
34     if (result.size() != N) {
35         return {};
36     }
37     return result;
38 }

6.6 Topological Sort

1 vector<int> adj[MAXN];
2 vector<int> estado(MAXN); // 0: nao visitado 1: processamento
   2: processado
3 vector<int> ordem;
4 bool temCiclo = false;
5
6 void dfs(int v) {
7     if(estado[v] == 1) {
8         temCiclo = true;
9         return;
10    }
11    if(estado[v] == 2) return;
12    estado[v] = 1;
13    for(auto &nei : adj[v]) {
14        if(estado[v] != 2) dfs(nei);
15    }
16    estado[v] = 2;
17    ordem.push_back(v);
18}
19}

6.7 Acha Pontes

1 vector<int> d, low, pai;      // d[v] Tempo de descoberta ( discovery time)
2 vector<bool> vis;
3 vector<int> pontos_articulacao;
4 vector<pair<int, int>> pontes;
5 int tempo;
6
7 vector<vector<int>> adj;
8
9 void dfs(int u) {
10    vis[u] = true;
11    tempo++;
12    d[u] = low[u] = tempo;
13    int filhos_dfs = 0;
14    for (int v : adj[u]) {
15        if (v == pai[u]) continue;
16        if (vis[v]) { // back edge
17            low[u] = min(low[u], d[v]);
18        } else {
19            pai[v] = u;
20            filhos_dfs++;
21            dfs(v);
22            low[u] = min(low[u], low[v]);
23            if (pai[u] == -1 && filhos_dfs > 1) {
24                pontos_articulacao.push_back(u);
25            }
26            if (pai[u] != -1 && low[v] >= d[u]) {
27                pontos_articulacao.push_back(u);
28            }
29            if (low[v] > d[u]) {
30                pontes.push_back({min(u, v), max(u, v)});
31            }
32        }
33    }
34}

6.8 Edmonds-karp

1 // Edmonds-Karp com scaling O(E log(F))
2
3 int n, m;
4 const int MAXN = 510;
5 vector<vector<int>> capacity(MAXN, vector<int>(MAXN, 0));
6 vector<vector<int>> adj(MAXN);
7
8 int bfs(int s, int t, int scale, vector<int>& parent) {
9
10    fill(parent.begin(), parent.end(), -1);
11    parent[s] = -2;
12    queue<pair<int, int>> q;
13    q.push({s, LLONG_MAX});
14
15    while (!q.empty()) {
16        int cur = q.front().first;
17        int flow = q.front().second;
18        q.pop();
19
20        for (int next : adj[cur]) {
21            if (parent[next] == -1 && capacity[cur][next] >=
22 scale) {
23                parent[next] = cur;
24                int new_flow = min(flow, capacity[cur][next]);
25
26                if (next == t)
27                    return new_flow;
28                q.push({next, new_flow});
29            }
30        }
31    }
32
33    int maxflow(int s, int t) {
34        int flow = 0;
35        vector<int> parent(MAXN);
36        int new_flow;
37        int scaling = 1ll << 62;
38
39        while (scaling > 0) {
40            while (new_flow = bfs(s, t, scaling, parent)) {
41                if (new_flow == 0) continue;
42                flow += new_flow;
43                int cur = t;
44                while (cur != s) {
45                    int prev = parent[cur];
46                    capacity[prev][cur] -= new_flow;
47                    capacity[cur][prev] += new_flow;
48                    cur = prev;
49                }
50            }
51            scaling /= 2;
52        }
53
54    return flow;
55 }

6.9 Kruskal

1 // Ordena as arestas por peso, insere se ja nao estiver no
   mesmo componente
2 // O(E log E)
3
4 struct Edge {
5     int u, v, w;
6     bool operator < (Edge const & other) {
7         return weight < other.weight;
8     }
9 }
10
11 vector<Edge> kruskal(int n, vector<Edge> edges) {
12     vector<Edge> mst;
13     DSU dsu = DSU(n + 1);
14     sort(edges.begin(), edges.end());
15     for (Edge e : edges) {
16         if (dsu.find(e.u) != dsu.find(e.v)) {
17             mst.push_back(e);
18             dsu.join(e.u, e.v);
19         }
20     }
21     return mst;
22 }

6.10 Bellman Ford

1 struct Edge {
2     int u, v, w;
3 };
4
5 // se x = -1, nao tem ciclo
6 // se x != -1, pegar pais de x pra formar o ciclo

```

```

7
8 int n, m;
9 vector<Edge> edges;
10 vector<int> dist(n);
11 vector<int> pai(n, -1);
12
13 for (int i = 0; i < n; i++) {
14     x = -1;
15     for (Edge &e : edges) {
16         if (dist[e.u] + e.w < dist[e.v]) {
17             dist[e.v] = max(-INF, dist[e.u] + e.w);
18             pai[e.v] = e.u;
19             x = e.v;
20         }
21     }
22 }
23
24 // achando caminho (se precisar)
25 for (int i = 0; i < n; i++) x = pai[x];
26
27 vector<int> ciclo;
28 for (int v = x;; v = pai[v]) {
29     cycle.push_back(v);
30     if (v == x && ciclo.size() > 1) break;
31 }
32 reverse(ciclo.begin(), ciclo.end());

```

6.11 Lca Jc

```

1 const int MAXN = 200005;
2 int N;
3 int LOG;
4
5 vector<vector<int>> adj;
6 vector<int> profundidade;
7 vector<vector<int>> cima; // cima[v][j] eh o 2^j-esimo
8 // ancestral de v
9
10 void dfs(int v, int p, int d) {
11     profundidade[v] = d;
12     cima[v][0] = p; // o pai direto eh o 2^0-Ãºltimo ancestral
13     for (int j = 1; j < LOG; j++) {
14         // se o ancestral 2^(j-1) existir, calculamos o 2^j
15         if (cima[v][j - 1] != -1) {
16             cima[v][j] = cima[cima[v][j - 1]][j - 1];
17         } else {
18             cima[v][j] = -1; // nao tem ancestral superior
19         }
20         for (int nei : adj[v]) {
21             if (nei != p) {
22                 dfs(nei, v, d + 1);
23             }
24     }
25 }
26
27 void build(int root) {
28     LOG = ceil(log2(N));
29     profundidade.assign(N + 1, 0);
30     cima.assign(N + 1, vector<int>(LOG, -1));
31     dfs(root, -1, 0);
32 }
33
34 int get_lca(int a, int b) {
35     if (profundidade[a] < profundidade[b]) {
36         swap(a, b);
37     }
38     // sobe 'a' ate a mesma profundidade de 'b'
39     for (int j = LOG - 1; j >= 0; j--) {
40         if (profundidade[a] - (1 << j) >= profundidade[b]) {
41             a = cima[a][j];
42         }
43     }
44     // se 'b' era um ancestral de 'a', entÃ£o 'a' agora Ã©
45     // igual a 'b'
46     if (a == b) {
47         return a;
48     }
49     // sobe os dois juntos ate encontrar os filhos do LCA
50     for (int j = LOG - 1; j >= 0; j--) {
51         if (cima[a][j] != -1 && cima[a][j] != cima[b][j]) {
52             a = cima[a][j];
53             b = cima[b][j];
54         }
55     }

```

```

55     return cima[a][0];
56 }

```

6.12 Lca

```

1 // LCA - CP algorithm
2 // preprocessing O(NlogN)
3 // lca O(logN)
4 // Uso: criar LCA com a quantidade de vertices (n) e lista de
5 // adjacencias (adj)
6 // chamar a funcao preprocess com a raiz da arvore
7
8 struct LCA {
9     int n, l, timer;
10    vector<vector<int>> adj;
11    vector<int> tin, tout;
12    vector<vector<int>> up;
13
14    LCA(int n, const vector<vector<int>>& adj) : n(n), adj(
15        adj) {}
16
17    void dfs(int v, int p) {
18        tin[v] = ++timer;
19        up[v][0] = p;
20        for (int i = 1; i <= l; ++i)
21            up[v][i] = up[up[v][i-1]][i-1];
22
23        for (int u : adj[v]) {
24            if (u != p)
25                dfs(u, v);
26        }
27
28        tout[v] = ++timer;
29    }
30
31    bool is_ancestor(int u, int v) {
32        return tin[u] <= tin[v] && tout[u] >= tout[v];
33    }
34
35    int lca(int u, int v) {
36        if (is_ancestor(u, v))
37            return u;
38        if (is_ancestor(v, u))
39            return v;
40        for (int i = l; i >= 0; --i) {
41            if (!is_ancestor(up[u][i], v))
42                u = up[u][i];
43        }
44        return up[u][0];
45    }
46
47    void preprocess(int root) {
48        tin.resize(n);
49        tout.resize(n);
50        timer = 0;
51        l = ceil(log2(n));
52        up.assign(n, vector<int>(l + 1));
53        dfs(root, root);
54    }

```

6.13 Kosaraju

```

1 bool vis[MAXN];
2 vector<int> order;
3 int component[MAXN];
4 int N, m;
5 vector<int> adj[MAXN], adj_rev[MAXN];
6
7 // dfs no grafo original para obter a ordem (pos-order)
8 void dfs1(int u) {
9     vis[u] = true;
10    for (int v : adj[u]) {
11        if (!vis[v]) {
12            dfs1(v);
13        }
14    }
15    order.push_back(u);
16}
17
18 // dfs o grafo reverso para encontrar os SCCs
19 void dfs2(int u, int c) {
20    component[u] = c;
21    for (int v : adj_rev[u]) {

```

```

22     if (component[v] == -1) {
23         dfs2(v, c);
24     }
25 }
26 }
27
28 int kosaraju() {
29     order.clear();
30     fill(vis + 1, vis + N + 1, false);
31     for (int i = 1; i <= N; i++) {
32         if (!vis[i]) {
33             dfs1(i);
34         }
35     }
36     fill(component + 1, component + N + 1, -1);
37     int c = 0;
38     reverse(order.begin(), order.end());
39     for (int u : order) {
40         if (component[u] == -1) {
41             dfs2(u, c++);
42         }
43     }
44     return c;
45 }

```

6.14 Pega Ciclo

```

1 // encontra um ciclo em g
2 // g[u] = vector<pair<id_aresta, vizinho>>
3 // rec_arestas: true -> retorna ids das arestas do ciclo;
4 // false -> retorna vertices do ciclo
5 // directed: grafo direcionado?
6 const int MAXN = 5 * 1e5 + 2;
7 vector<pair<int, int>> g[MAXN];
8 int N;
9 bool DIRECTED = false;
10 vector<int> color(MAXN), parent(MAXN, -1), edgein(MAXN, -1);
11 // color: 0,1,2 ; edgein[v] = id da aresta que entra em v
12 int ini_ciclo = -1, fim_ciclo = -1, back_edge_id = -1;
13
14 bool dfs(int u, int pai_edge){
15     color[u] = 1; // cinza
16     for (auto [id, v] : g[u]) {
17         if (!DIRECTED && id == pai_edge) continue; // ignorar
18         aresta_de_volta ao pai em n-dir
19         if (color[v] == 0) {
20             parent[v] = u;
21             edgein[v] = id;
22             if (dfs(v, id)) return true;
23         } else if (color[v] == 1) {
24             // back-edge u -> v detectado
25             ini_ciclo = u;
26             fim_ciclo = v;
27             back_edge_id = id;
28             return true;
29         } // se color[v] == 2, ignora
30     }
31     color[u] = 2; // preto
32     return false;
33 }
34
35 // retorna ids das arestas do ciclo
36 vector<int> pega_ciclo(bool rec_arestas) {
37     for (int u = 1; u <= N; u++) {
38         if (color[u] != 0) continue;
39         if (dfs(u, -1)) {
40             // caminho u -> ... -> v via parent
41             vector<int> path;
42             int cur = ini_ciclo;
43             path.push_back(cur);
44             while (cur != fim_ciclo) {
45                 cur = parent[cur];
46                 path.push_back(cur);
47             }
48             // path = [u, ..., v] -> inverter para [v, ..., u]
49             reverse(path.begin(), path.end());
50             if (!rec_arestas) return path;
51             // converte para ids das arestas: edgein[node] eh
52             a aresta que entra em node
53             vector<int> edges;

```

```

53         for (int i = 1; i < path.size(); i++) edges.
54             push_back(edgein[path[i]]);
55             // adiciona a aresta de retorno u -> v
56             edges.push_back(back_edge_id);
57         }
58     }
59     return {};
60 }

```

6.15 Min Cost Max Flow

```

1 // Encontra o menor custo para passar K de fluxo em um grafo
2 // com N vertices
3 // Funciona com multiplas arestas para o mesmo par de
4 // vertices
5 // Para encontrar o min cost max flow eh so fazer K =
6 // infinito
7
8 struct Edge {
9     int from, to, capacity, cost, id;
10};
11
12 const int INF = LLONG_MAX;
13
14 void shortest_paths(int n, int v0, vector<int>& dist, vector<
15 int>& edge_to) {
16     dist.assign(n, INF);
17     dist[v0] = 0;
18     vector<bool> in_queue(n, false);
19     queue<int> q;
20     q.push(v0);
21     edge_to.assign(n, -1);
22
23     while (!q.empty()) {
24         int u = q.front();
25         q.pop();
26         in_queue[u] = false;
27         for (auto [v, id] : adj[u]) {
28             if (edges[id].capacity > 0 && dist[v] > dist[u] +
29                 edges[id].cost) {
30                 dist[v] = dist[u] + edges[id].cost;
31                 edge_to[v] = id;
32                 if (!in_queue[v]) {
33                     in_queue[v] = true;
34                     q.push(v);
35                 }
36             }
37         }
38     }
39
40 void add_edge(int from, int to, int capacity, int cost){
41     edges.push_back({from, to, capacity, cost, (int)edges.
42 size()});
43     edges.push_back({to, from, 0, -cost, (int)edges.size()});
44     // reversa
45 }
46
47 int min_cost_flow(int N, int K, int s, int t) {
48     adj.assign(N, vector<array<int, 2>>());
49
50     for (Edge e : edges) {
51         adj[e.from].push_back({e.to, e.id});
52     }
53
54     int flow = 0;
55     int cost = 0;
56     vector<int> dist, edge_to;
57     while (flow < K) {
58         shortest_paths(N, s, dist, edge_to);
59         if (dist[t] == INF)
60             break;
61
62         // find max flow on that path
63         int f = K - flow;
64         int cur = t;
65         while (cur != s) {
66             f = min(f, edges[edge_to[cur]].capacity);
67             cur = edges[edge_to[cur]].from;
68         }
69     }
70 }

```

```

67     // apply flow
68     flow += f;
69     cost += f * dist[t];
70     cur = t;
71     while (cur != s) {
72         int edge = edge_to[cur];
73         int rev_edge = edge^1;
74
75         edges[edge].capacity -= f;
76         edges[rev_edge].capacity += f;
77         cur = edges[edge].from;
78     }
79 }
80
81 if (flow < K)
82     return -1;
83 else
84     return cost;
85 }
```

7 Primitives

8 DP

8.1 Lis

```

1 int lis_nlogn(vector<int> &v) {
2     vector<int> lis;
3     lis.push_back(v[0]);
4     for (int i = 1; i < v.size(); i++) {
5         if (v[i] > lis.back()) {
6             // estende a lis
7             lis.push_back(v[i]);
8         } else {
9             // encontra o primeiro elemento em lis que >= v[i]
10            ].auto it = lower_bound(lis.begin(), lis.end(), v[i]);
11        });
12        *it = v[i];
13    }
14    return lis.size();
15 }
16
17 // lis na tree do problema da sub
18 const int MAXN_TREE = 100001;
19 vector<int> adj[MAXN_TREE];
20 int values[MAXN_TREE];
21 int ans = 0;
22
23 void dfs(int u, int p, vector<int>& tails) {
24     auto it = lower_bound(tails.begin(), tails.end(), values[u]);
25     int prev = -1;
26     bool coloquei = false;
27     if (it == tails.end()) {
28         tails.push_back(values[u]);
29         coloquei = true;
30     } else {
31         prev = *it;
32         *it = values[u];
33     }
34     ans = max(ans, (int)tails.size());
35     for (int v : adj[u]) {
36         if (v != p) {
37             dfs(v, u, tails);
38         }
39     }
40     if (coloquei) {
41         tails.pop_back();
42     } else {
43         *it = prev;
44     }
45 }
```

8.2 Edit Distance

```

1 vector<vector<int>> dp(n+1, vector<int>(m+1, LLONG_MIN));
2 for(int j = 0; j <= m; j++) dp[0][j] = j;
3 for(int i = 0; i <= n; i++) dp[i][0] = i;
4 for(int i = 1; i <= n; i++) {
```

```

5     for(int j = 1; j <= m; j++) {
6         if(a[i-1] == b[j-1]) {
7             dp[i][j] = dp[i-1][j-1];
8         } else {
9             dp[i][j] = min({dp[i-1][j] + 1, dp[i][j-1] +
10                1, dp[i-1][j-1] + 1});
11         }
12     }
13     cout << dp[n][m];
14 }
```

8.3 Bitmask

```

1 // dp de intervalos com bitmask
2 int prox(int idx) {
3     return lower_bound(S.begin(), S.end(), array<int, 4>{S[
4         idx][1], 0ll, 0ll, 0ll}) - S.begin();
5 }
6 int dp[1002][(int)(1ll << 10)];
7
8 int rec(int i, int vis) {
9     if (i == (int)S.size()) {
10         if (__builtin_popcountll(vis) == N) return 0;
11         return LLONG_MIN;
12     }
13     if (dp[i][vis] != -1) return dp[i][vis];
14     int ans = rec(i + 1, vis);
15     ans = max(ans, rec(prox(i), vis | (1ll << S[i][3])) + S[i]
16 [i][2]);
17     return dp[i][vis] = ans;
18 }
```

8.4 Lcs

```

1 string s1, s2;
2 int dp[1001][1001];
3 int lcs(int i, int j) {
4     if (i < 0 || j < 0) return 0;
5     if (dp[i][j] != -1) return dp[i][j];
6     if (s1[i] == s2[j]) return dp[i][j] = 1 + lcs(i - 1, j -
1);
7     else return dp[i][j] = max(lcs(i - 1, j), lcs(i, j - 1));
8 }
```

8.5 Digit

```

1 vector<int> digits;
2
3 int dp[20][10][2][2];
4
5 int rec(int i, int last, int flag, int started) {
6     if (i == (int)digits.size()) return 1;
7     if (dp[i][last][flag][started] != -1) return dp[i][last][
8         flag][started];
9     int lim;
10    if (flag) lim = 9;
11    else lim = digits[i];
12    int ans = 0;
13    for (int d = 0; d <= lim; d++) {
14        if (started && d == last) continue;
15        int new_flag = flag;
16        int new_started = started;
17        if (d > 0) new_started = 1;
18        if (!flag && d < lim) new_flag = 1;
19        ans += rec(i + 1, d, new_flag, new_started);
20    }
21    return dp[i][last][flag][started] = ans;
22 }
```

8.6 Knapsack

```

1 // dp[i][j] => i-esimo item com j-carga sobrando na mochila
2 // O(N * W)
3 vector<vector<int>> dp(N + 1, vector<int>(W + 1, 0));
4 for (int i = 1; i <= N; i++) dp[i][0] = 0;
5 for (int j = 0; j <= W; j++) dp[0][j] = 0;
6 for (int i = 1; i <= N; i++) {
7     for (int j = 0; j <= W; j++) {
8         dp[i][j] = dp[i - 1][j];
9         if (j >= items[i-1].first) {
10             dp[i][j] = max(dp[i][j], dp[i - 1][j - items[i
11 - 1].first] + items[i-1].second);
12         }
13     }
14 }
```

```

11     }
12   }
13 }
14 cout << dp[N][W] << '\n';

```

8.7 Lis Seg

```

1 // comprime coordenadas pra quando ai <= 1e9
2 vector<int> vals(a.begin(), a.end());
3 sort(vals.begin(), vals.end());
4 vals.erase(unique(vals.begin(), vals.end()), vals.end());
5 auto id = [&](int x) -> int {
6   return lower_bound(vals.begin(), vals.end(), x) - vals.
7   begin();
8 };
9 for (int i = 0; i < n; i++) a[i] = id(a[i]);
10 // fim da parte de compr
11 SegTree seg(n);
12 vector<int> dp(n, 1); // dp[i] = 1 base case
13 for (int i = 0; i < n; i++) {
14   if (a[i] > 0) dp[i] = seg.query(0, max(0LL, a[i] - 1)) +
15     1;
16   seg.update(a[i], dp[i]);
17 }
18 cout << *max_element(dp.begin(), dp.end()) << '\n';

```

8.8 Disjoint Blocks

```

1 // num max de subarrays disjuntos com soma x usando apenas
2 // prefixo i (ou seja, considerando prefixo a[1..i]).
3 int disjointSumX(vector<int> &a, int x) {
4   int n = a.size();
5   map<int, int> best; // best[pref] = melhor dp visto para
6   esse pref
6   best[0] = 0;
7   int pref = 0;
8   vector<int> dp(n + 1, 0); // dp[0] = 0
9   for (int i = 1; i <= n; i++) {
10     pref += a[i - 1];
11     dp[i] = dp[i - 1];
12     auto it = best.find(pref - x);
13     if (it != best.end()) {
14       dp[i] = max(dp[i], it->second + 1);
15     }
16     best[pref] = max(best[pref], dp[i]);
17   }
18   return dp[n];
19 }

```

9 General

9.1 Brute Choose

```

1 vector<int> elements;
2 int N, K;
3 vector<int> comb;
4
5 void brute_choose(int i) {
6   if (comb.size() == K) {
7     for (int j = 0; j < comb.size(); j++) {
8       cout << comb[j] << ' ';
9     }
10    cout << '\n';
11    return;
12  }
13  if (i == N) return;
14  int r = N - i;
15  int preciso = K - comb.size();
16  if (r < preciso) return;
17  comb.push_back(elements[i]);
18  brute_choose(i + 1);
19  comb.pop_back();
20  brute_choose(i + 1);
21 }

```

9.2 Struct

```

1 struct Pessoa{
2   // Atributos
3   string nome;

```

```

4   int idade;
5
6   // Comparador
7   bool operator<(const Pessoa& other) const{
8     if(idade != other.idade) return idade > other.idade;
9     else return nome > other.nome;
10  }
11 }

```

9.3 Mex

```

1 struct MEX {
2   map<int, int> f;
3   set<int> falta;
4   int tam;
5   MEX(int n) : tam(n) {
6     for (int i = 0; i <= n; i++) falta.insert(i);
7   }
8   void add(int x) {
9     f[x]++;
10    if (f[x] == 1 && x >= 0 && x <= tam) {
11      falta.erase(x);
12    }
13  }
14  void rem(int x) {
15    if (f.count(x) && f[x] > 0) {
16      f[x]--;
17      if (f[x] == 0 && x >= 0 && x <= tam) {
18        falta.insert(x);
19      }
20    }
21  }
22  int get() {
23    if (falta.empty()) return tam + 1;
24    return *falta.begin();
25  }
26 };

```

9.4 Count Permutations

```

1 // Returns the number of distinct permutations
2 // that are lexicographically less than the string t
3 // using the provided frequency (freq) of the characters
4 // 0(freq.size())
5 int countPermLess(vector<int> freq, const string &t) {
6   int n = t.size();
7   int ans = 0;
8
9   vector<int> fact(n + 1, 1), invfact(n + 1, 1);
10  for (int i = 1; i <= n; i++)
11    fact[i] = (fact[i - 1] * i) % MOD;
12  invfact[n] = fexp(fact[n], MOD - 2, MOD);
13  for (int i = n - 1; i >= 0; i--)
14    invfact[i] = (invfact[i + 1] * (i + 1)) % MOD;
15
16  // For each position in t, try placing a letter smaller
17  // than t[i] that is in freq
18  for (int i = 0; i < n; i++) {
19    for (char c = 'a'; c < t[i]; c++) {
20      if (freq[c - 'a'] > 0) {
21        freq[c - 'a']--;
22        int ways = fact[n - i - 1];
23        for (int f : freq)
24          ways = (ways * invfact[f]) % MOD;
25        ans = (ans + ways) % MOD;
26        freq[c - 'a']++;
27      }
28      if (freq[t[i] - 'a'] == 0) break;
29      freq[t[i] - 'a']--;
30    }
31  }
32  return ans;

```

9.5 Bitwise

```

1 int check_kth_bit(int x, int k) {
2   return (x >> k) & 1;
3 }
4
5 void print_on_bits(int x) {
6   for (int k = 0; k < 32; k++) {
7     if (check_kth_bit(x, k)) {

```

```

8      cout << k << ' ';
9    }
10   cout << '\n';
11 }
12 }
13
14 int count_on_bits(int x) {
15   int ans = 0;
16   for (int k = 0; k < 32; k++) {
17     if (check_kth_bit(x, k)) {
18       ans++;
19     }
20   }
21   return ans;
22 }
23
24 bool is_even(int x) {
25   return ((x & 1) == 0);
26 }
27
28 int set_kth_bit(int x, int k) {
29   return x | (1 << k);
30 }
31
32 int unset_kth_bit(int x, int k) {
33   return x & (~(1 << k));
34 }
35
36 int toggle_kth_bit(int x, int k) {
37   return x ^ (1 << k);
38 }
39
40 bool check_power_of_2(int x) {
41   return count_on_bits(x) == 1;
42 }

```

10 Geometry

10.1 Convex Hull

```

1 #include <bits/stdc++.h>
2
3 using namespace std;
4 #define int long long
5 typedef int cod;
6
7 struct point
8 {
9   cod x,y;
10  point(cod x = 0, cod y = 0): x(x), y(y)
11  {}
12
13  double modulo()
14  {
15    return sqrt(x*x + y*y);
16  }
17
18  point operator+(point o)
19  {
20    return point(x+o.x, y+o.y);
21  }
22  point operator-(point o)
23  {
24    return point(x - o.x, y - o.y);
25  }
26  point operator*(cod t)
27  {
28    return point(x*t, y*t);
29  }
30  point operator/(cod t)
31  {
32    return point(x/t, y/t);
33  }
34
35  cod operator*(point o)
36  {
37    return x*o.x + y*o.y;
38  }
39  cod operator^(point o)
40  {
41    return x*o.y - y * o.x;
42  }
43  bool operator<(point o)
44  {

```

```

45      if( x != o.x) return x < o.x;
46      return y < o.y;
47    }
48  };
49 }
50
51 int ccw(point p1, point p2, point p3)
52 {
53   cod cross = (p2-p1) ^ (p3-p1);
54   if(cross == 0) return 0;
55   else if(cross < 0) return -1;
56   else return 1;
57 }
58
59 vector<point> convex_hull(vector<point> p)
60 {
61   sort(p.begin(), p.end());
62   vector<point> L,U;
63
64   //Lower
65   for(auto pp : p)
66   {
67     while(L.size() >= 2 and ccw(L[L.size()-2], L.back(),
68       pp) == -1)
69     {
70       // If -1 pq eu nÃ£o quero excluir os colineares
71       L.pop_back();
72     }
73   L.push_back(pp);
74 }
75 reverse(p.begin(), p.end());
76
77 //Upper
78 for(auto pp : p)
79 {
80   while(U.size() >= 2 and ccw(U[U.size()-2], U.back(),
81     pp) == -1)
82   {
83     U.pop_back();
84   U.push_back(pp);
85 }
86 L.pop_back();
87 L.insert(L.end(), U.begin(), U.end()-1);
88 return L;
89 }
90
91 cod area(vector<point> v)
92 {
93   int ans = 0;
94   int aux = (int)v.size();
95   for(int i = 2; i < aux; i++)
96   {
97     ans += ((v[i] - v[0])^(v[i-1] - v[0]))/2;
98   }
99   ans = abs(ans);
100  return ans;
101 }
102
103 int bound(point p1 , point p2)
104 {
105   return __gcd(abs(p1.x-p2.x), abs(p1.y-p2.y));
106 }
107
108 //teorema de pick [pontos = A - (bound+points)/2 + 1]
109
110 int32_t main()
111 {
112
113   int n;
114   cin >> n;
115
116   vector<point> v(n);
117   for(int i = 0; i < n; i++)
118   {
119     cin >> v[i].x >> v[i].y;
120   }
121
122   vector<point> ch = convex_hull(v);
123
124   cout << ch.size() << '\n';
125   for(auto p : ch) cout << p.x << " " << p.y << "\n";
126
127   return 0;
128 }

```

10.2 Inside Polygon

```

1 // Convex O(logn)
2
3 bool insideT(point a, point b, point c, point e){
4     int x = ccw(a, b, e);
5     int y = ccw(b, c, e);
6     int z = ccw(c, a, e);
7     return !(x==1 or y==1 or z==1) and (x==-1 or y==-1 or z
8         ==-1));
9 }
10
11 bool inside(vp &p, point e){ // ccw
12     int l=2, r=(int)p.size()-1;
13     while(l<r){
14         int mid = (l+r)/2;
15         if(ccw(p[0], p[mid], e) == 1)
16             l=mid+1;
17         else{
18             r=mid;
19         }
20     }
21     // bordo
22     // if(r==(int)p.size()-1 and ccw(p[0], p[r], e)==0)
23     //     return false;
24     // if(r==2 and ccw(p[0], p[1], e)==0) return false;
25     // if(ccw(p[r], p[r-1], e)==0) return false;
26     // return insideT(p[0], p[r-1], p[r], e);
27 }
28
29 // Any O(n)
30
31 int inside(vp &p, point pp){
32     // 1 - inside / 0 - boundary / -1 - outside
33     int n = p.size();
34     for(int i=0;i<n;i++){
35         int j = (i+1)%n;
36         if(line({p[i], p[j]}).inside_seg(pp))
37             return 0;
38     }
39     int inter = 0;
40     for(int i=0;i<n;i++){
41         int j = (i+1)%n;
42         if(p[i].x <= pp.x and pp.x < p[j].x and ccw(p[i], p[j],
43             pp)==1)
44             inter++; // up
45         else if(p[j].x <= pp.x and pp.x < p[i].x and ccw(p[i],
46             p[j], pp)==-1)
47             inter++; // down
48     }
49     if(inter%2==0) return -1; // outside
50     else return 1; // inside
51 }
```

10.3 Point Location

```

1 int32_t main(){
2     sws;
3
4     int t; cin >> t;
5
6     while(t--){
7
8         int x1, y1, x2, y2, x3, y3; cin >> x1 >> y1 >> x2 >>
9             y2 >> x3 >> y3;
10
11        int deltax1 = (x1-x2), deltay1 = (y1-y2);
12
13        int compx = (x1-x3), compy = (y1-y3);
14
15        int ans = (deltax1*compy) - (compx*deltay1);
16
17        if(ans == 0){cout << "TOUCH\n"; continue;}
18        if(ans < 0){cout << "RIGHT\n"; continue;}
19        if(ans > 0){cout << "LEFT\n"; continue;}
20    }
21
22 }
```

10.4 Lattice Points

```

1 ll gcd(ll a, ll b) {
2     return b == 0 ? a : gcd(b, a % b);
3 }
4 ll area_triangulo(ll x1, ll y1, ll x2, ll y2, ll x3, ll y3) {
5     return abs(x1 * (y2 - y3) + x2 * (y3 - y1) + x3 * (y1 -
6         y2));
7 }
8 ll pontos_borda(ll x1, ll y1, ll x2, ll y2) {
9     return gcd(abs(x2 - x1), abs(y2 - y1));
10 }
11 int32_t main() {
12     ll x1, y1, x2, y2, x3, y3;
13     cin >> x1 >> y1;
14     cin >> x2 >> y2;
15     cin >> x3 >> y3;
16     ll area = area_triangulo(x1, y1, x2, y2, x3, y3);
17     ll tot_borda = pontos_borda(x1, y1, x2, y2) +
18         pontos_borda(x2, y2, x3, y3) + pontos_borda(x3, y3, x1,
19         y1);
20     ll ans = (area - tot_borda) / 2 + 1;
21     cout << ans << endl;
22 }
23 }
```