

Competitive Programming Notebook

Programadores Roblox

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1 String

1.1 Trie Ponteiros

```
1 // Trie por ponteiros
2 // InserÃgÃčo, busca e consulta de prefixo em O(N)
4 struct Node {
       Node *filhos[26] = \{\};
      bool acaba = false;
       int contador = 0;
8 };
void insere(string s, Node *raiz) {
      Node *cur = raiz;
       for(auto &c : s) {
13
          cur -> contador++;
           if(cur->filhos[c - 'a'] != NULL) {
14
               cur = cur->filhos[c - 'a'];
               continue;
16
17
          }
           cur->filhos[c - 'a'] = new Node();
18
           cur = cur->filhos[c - 'a'];
19
20
      cur -> contador++:
21
22
       cur -> a caba = true;
23 }
24
25 bool busca(string s, Node *raiz) {
      Node *cur = raiz;
26
       for(auto &c : s) {
          if (cur->filhos[c - 'a'] != NULL) {
28
               cur = cur->filhos[c - 'a'];
29
               continue;
3.0
31
          return false;
      }
33
34
      return cur->acaba:
35 }
_{\rm 37} // Retorna se {\rm \tilde{A}}{\rm l'} prefixo e quantas strings tem s como ^{12}
       prefixo
38 int isPref(string s, Node *raiz) {
       Node *cur = raiz;
3.9
      for(auto &c : s) {
          if (cur->filhos[c - 'a'] != NULL) {
41
               cur = cur->filhos[c - 'a'];
42
               continue;
43
          }
44
          return -1;
      }
46
       return cur->contador;
47
48 }
  1.2 Trie
1 // Trie por array
2 // InserÃgÃčo, busca e consulta de prefixo em O(N)
4 int trie[MAXN][26];
5 int tot_nos = 0;
6 vector < bool > acaba(MAXN, false);
7 vector < int > contador (MAXN, 0);
9 void insere(string s) {
     int no = 0;
10
      for(auto &c : s) {
11
          if(trie[no][c - 'a'] == 0) {
               trie[no][c - 'a'] = ++tot_nos;
1.3
14
```

no = trie[no][c - 'a'];

contador[no]++;

1.5

16

```
1.7
18
       acaba[no] = true;
19 }
20
21 bool busca(string s) {
     int no = 0;
22
       for(auto &c : s) {
23
           if(trie[no][c - 'a'] == 0) {
2.4
               return false;
25
26
           no = trie[no][c - 'a'];
27
28
       }
29
       return acaba[no];
30 }
31
32 int isPref(string s) {
33
       int no = 0;
       for(auto &c : s) {
3.4
           if(trie[no][c - 'a'] == 0){
36
               return -1;
37
38
           no = trie[no][c - 'a'];
3.9
       return contador[no];
40
41 }
```

1.3 Hashing

```
1 // String Hash template
_2 // constructor(s) - O(|s|)
3 // query(1, r) - returns the hash of the range [1,r]
       from left to right - 0(1)
4 // query_inv(l, r) from right to left - O(1)
5 // patrocinado por tiagodfs
 7 struct Hash {
      const int X = 2147483647;
       const int MOD = 1e9+7;
 9
       int n; string s;
       vector < int > h , hi , p;
       Hash() {}
       Hash(string s): s(s), n(s.size()), h(n), hi(n), p
1.3
           for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1)
14
        % MOD;
           for (int i=0;i<n;i++)</pre>
               h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD;
16
           for (int i=n-1;i>=0;i--)
17
               hi[i] = (s[i] + (i+1 < n ? hi[i+1]:0) * X)
18
       % MOD;
       }
19
       int query(int 1, int r) {
20
           int hash = (h[r] - (1 ? h[1-1]*p[r-1+1]%MOD :
21
        0)):
           return hash < 0 ? hash + MOD : hash;</pre>
23
       int query_inv(int 1, int r) {
24
           int hash = (hi[1] - (r+1 < n ? hi[r+1]*p[r-1
       +1] % MOD : 0));
           return hash < 0 ? hash + MOD : hash;</pre>
26
27
28 };
```

1.4 Lcs

```
int lcs(string &s1, string &s2) {
   int m = s1.size();
   int n = s2.size();

vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
```

```
for (int i = 1; i <= m; ++i) {</pre>
          for (int j = 1; j \le n; ++ j) {
               if (s1[i - 1] == s2[j - 1])
                                                             1.7 Kmp
                   dp[i][j] = dp[i - 1][j - 1] + 1;
                                                           vector < int > kmp(string s) {
                   dp[i][j] = max(dp[i - 1][j], dp[i][j
12
                                                                int n = (int)s.length();
       - 1]);
                                                                 vector < int > p(n+1);
          }
                                                                 p[0] = -1;
14
                                                                 for (int i = 1; i < n; i++) {</pre>
                                                                     int j = p[i-1];
      return dp[m][n];
16
                                                                     while (j \ge 0 \&\& s[j] != s[i-1])
17 }
                                                                         j = p[j-1];
                                                                     p[i] = j+1;
  1.5 Countpermutations
                                                          10
                                                                 return p;
                                                          11
1 // Returns the number of distinct permutations
_{2} // that are lexicographically less than the string t
3 // using the provided frequency (freq) of the
                                                                  String copy
      characters
4 // O(n*freq.size())
5 int countPermLess(vector < int > freq, const string &t)
                                                             2.1
                                                                   Trie Ponteiros
      int n = t.size();
                                                           1 // Trie por ponteiros
      int ans = 0;
                                                           _2 // InserÃğÃčo, busca e consulta de prefixo em O(N)
9
      vector < int > fact(n + 1, 1), invfact(n + 1, 1);
                                                           4 struct Node {
      for (int i = 1; i <= n; i++)</pre>
10
                                                                 Node *filhos[26] = \{\};
          fact[i] = (fact[i - 1] * i) % MOD;
11
                                                                 bool acaba = false:
       invfact[n] = fexp(fact[n], MOD - 2, MOD);
                                                                 int contador = 0;
      for (int i = n - 1; i >= 0; i--)
13
           invfact[i] = (invfact[i + 1] * (i + 1)) % MOD 8 };
14
                                                          10 void insere(string s, Node *raiz) {
1.5
                                                               Node *cur = raiz;
      // For each position in t, try placing a letter
                                                                 for(auto &c : s) {
      smaller than t[i] that is in freq
                                                                     cur->contador++;
                                                          1.3
      for (int i = 0; i < n; i++) {</pre>
                                                                     if(cur->filhos[c - 'a'] != NULL) {
                                                          14
           for (char c = 'a'; c < t[i]; c++) {
                                                                         cur = cur->filhos[c - 'a'];
                                                          15
               if (freq[c - 'a'] > 0) {
19
                                                                          continue;
                                                          16
                   freq[c - 'a']--;
                   int ways = fact[n - i - 1];
21
                                                                     cur->filhos[c - 'a'] = new Node();
                                                          1.8
                   for (int f : freq)
                                                                     cur = cur->filhos[c - 'a'];
                       ways = (ways * invfact[f]) % MOD; 19
                                                                 }
                                                          20
                   ans = (ans + ways) \% MOD;
                                                                 cur -> contador ++;
                                                          21
                   freq[c - 'a']++;
                                                          22
                                                                 cur->acaba = true;
              }
26
                                                          23 }
                                                          24
           if (freq[t[i] - 'a'] == 0) break;
                                                          25 bool busca(string s, Node *raiz) {
          freq[t[i] - 'a']--;
                                                          26
                                                                 Node *cur = raiz;
      }
30
                                                          27
                                                                 for(auto &c : s) {
31
      return ans;
                                                                     if (cur->filhos[c - 'a'] != NULL) {
                                                          28
32 }
                                                                          cur = cur->filhos[c - 'a'];
                                                          29
                                                                          continue;
                                                          30
  1.6 Z Function
                                                                     }
                                                          31
                                                          32
                                                                     return false;
vector<int> z_function(string s) {
                                                          33
      int n = s.size();
                                                          34
                                                                 return cur->acaba;
      vector < int > z(n);
                                                          35 }
      int 1 = 0, r = 0;
                                                          36
      for(int i = 1; i < n; i++) {</pre>
                                                          37 // Retorna se Ãľ prefixo e quantas strings tem s como
          if(i < r) {</pre>
                                                                  prefixo
              z[i] = min(r - i, z[i - 1]);
                                                          38 int isPref(string s, Node *raiz) {
                                                                 Node *cur = raiz;
           while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])_{40}
                                                                 for(auto &c : s) {
                                                                     if (cur->filhos[c - 'a'] != NULL) {
                                                          41
               z[i]++;
                                                                          cur = cur->filhos[c - 'a'];
10
                                                          43
                                                                          continue:
          if(i + z[i] > r) {
                                                          44
              1 = i;
                                                                     return -1;
                                                          45
               r = i + z[i];
14
                                                          46
                                                                 return cur->contador;
15
                                                          47
      }
                                                          48 }
16
      return z;
```

18 }

```
2.2
        Hashing
                                                              9
                                                                    vector < int > fact(n + 1, 1), invfact(n + 1, 1);
                                                                    for (int i = 1; i <= n; i++)</pre>
                                                             10
1 // String Hash template
                                                                         fact[i] = (fact[i - 1] * i) % MOD;
_2 // constructor(s) - O(|s|)
_{\rm 3} // query(1, r) - returns the hash of the range [1,r] ^{\rm 12}
                                                                    invfact[n] = fexp(fact[n], MOD - 2, MOD);
                                                                    for (int i = n - 1; i >= 0; i --)
      from left to right - 0(1)
                                                             13
                                                                         invfact[i] = (invfact[i + 1] * (i + 1)) % MOD
                                                             14
4 // query_inv(l, r) from right to left - O(1)
5 // patrocinado por tiagodfs
                                                             15
                                                                    // For each position in t, try placing a letter
                                                             16
7 mt19937 rng(time(nullptr));
                                                                    smaller than t[i] that is in freq
                                                                    for (int i = 0; i < n; i++) {</pre>
9 struct Hash {
                                                                         for (char c = 'a'; c < t[i]; c++) {
                                                             18
      const int X = rng();
1.0
                                                                             if (freq[c - 'a'] > 0) {
                                                             19
       const int MOD = 1e9+7;
                                                                                  freq[c - 'a']--;
                                                             2.0
       int n; string s;
                                                                                  int ways = fact[n - i - 1];
                                                             21
       vector < int > h , hi , p;
13
                                                                                  for (int f : freq)
       Hash() {}
                                                                                      ways = (ways * invfact[f]) % MOD;
       \label{eq:hash_string_s} \texttt{Hash}(\texttt{string} \ \texttt{s}): \ \texttt{s(s)}, \ \texttt{n(s.size())}, \ \texttt{h(n)}, \ \texttt{hi(n)}, \ \texttt{p}^{\,23}
15
                                                                                  ans = (ans + ways) % MOD;
                                                                                  freq[c - 'a']++;
           for (int i=0;i<n;i++) p[i] = (i ? X*p[i-1]:1) 25</pre>
       % MOD;
                                                                         }
           for (int i=0;i<n;i++)</pre>
                                                                         if (freq[t[i] - 'a'] == 0) break;
               h[i] = (s[i] + (i ? h[i-1]:0) * X) % MOD; 28
18
                                                                         freq[t[i] - 'a']--;
           for (int i=n-1; i>=0; i--)
                                                                    }
               hi[i] = (s[i] + (i+1 < n ? hi[i+1]:0) * X) 30
20
                                                             31
                                                                    return ans;
       % MOD;
                                                             32 }
21
       int query(int 1, int r) {
           int hash = (h[r] - (1 ? h[1-1]*p[r-1+1]%MOD : 2.5 Z Function
        0));
          return hash < 0 ? hash + MOD : hash;</pre>
24
                                                              vector<int> z_function(string s) {
                                                                   int n = s.size();
25
       int query_inv(int 1, int r) {
                                                                    vector < int > z(n);
26
           int hash = (hi[1] - (r+1 < n ? hi[r+1]*p[r-1]
                                                                    int 1 = 0, r = 0;
       +1] % MOD : 0));
                                                                    for(int i = 1; i < n; i++) {</pre>
           return hash < 0 ? hash + MOD : hash;</pre>
                                                                         if(i < r) {</pre>
29
                                                                             z[i] = min(r - i, z[i - 1]);
30 };
                                                                         }
                                                                         while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
  2.3 Lcs
                                                                             z[i]++;
                                                             10
int lcs(string &s1, string &s2) {
                                                                         if(i + z[i] > r) {
                                                             12
       int m = s1.size();
                                                             13
                                                                             1 = i;
       int n = s2.size();
                                                                             r = i + z[i];
                                                             14
                                                             15
       vector < vector < int >> dp(m + 1, vector < int > (n + 1,
                                                                    }
                                                             17
                                                                    return z;
       for (int i = 1; i <= m; ++i) {</pre>
           for (int j = 1; j <= n; ++j) {
                                                                     Kmp
                                                                2.6
                if (s1[i - 1] == s2[j - 1])
9
                    dp[i][j] = dp[i - 1][j - 1] + 1;
                                                              vector < int > kmp (string s) {
                    dp[i][j] = max(dp[i - 1][j], dp[i][j
                                                              int n = (int)s.length();
       - 1]);
                                                                    vector < int > p(n+1);
           }
13
                                                                    p[0] = -1;
14
                                                                    for (int i = 1; i < n; i++) {</pre>
1.5
                                                                         int j = p[i-1];
       return dp[m][n];
                                                                         while (j \ge 0 \&\& s[j] != s[i-1])
17 }
                                                                             j = p[j-1];
                                                                         p[i] = j+1;
                                                              9
  2.4 Countpermutations
                                                             10
                                                             11
                                                                    return p;
1 // Returns the number of distinct permutations
_{2} // that are lexicographically less than the string t
                                                                3
                                                                     DS
3 // using the provided frequency (freq) of the
       characters
4 // O(n*freq.size())
                                                                       Segtree Iterativa
5 int countPermLess(vector<int> freq, const string &t)
       int n = t.size();
                                                              _{1} // Exemplo de uso:
       int ans = 0;
                                                              2 // SegTree < int > st(vetor);
```

```
void update(int node, int start, int end, int idx
3 // range query e point update
                                                          2.3
                                                                 , int value) {
                                                                     if (start == end) {
5 template <typename T>
                                                          24
6 struct SegTree {
                                                          25
                                                                         tree[node] = value;
      int n;
                                                          26
                                                                     } else {
      vector < T > tree;
                                                                         int mid = (start + end) / 2;
                                                          27
      T neutral_value = 0;
                                                                         if (idx <= mid) {</pre>
                                                          28
      T combine(T a, T b) \{
                                                                             update(2 * node + 1, start, mid, idx,
1.0
                                                          29
          return a + b;
                                                                  value):
                                                                         } else {
                                                          30
                                                                             update(2 * node + 2, mid + 1, end,
13
                                                          31
14
      SegTree(const vector < T > & data) {
                                                                 idx, value);
         n = data.size();
1.5
                                                          32
                                                                        }
                                                                         tree[node] = gcd(tree[2 * node + 1], tree
          tree.resize(2 * n, neutral_value);
16
                                                          33
17
                                                                 [2 * node + 2]);
          for (int i = 0; i < n; i++)
18
                                                          34
               tree[n + i] = data[i];
                                                          35
20
                                                          36
           for (int i = n - 1; i > 0; --i)
                                                                 int query(int node, int start, int end, int 1,
              tree[i] = combine(tree[i * 2], tree[i * 2
                                                                 int r) {
       + 1]);
                                                                     if (r < start || 1 > end) {
                                                          38
                                                                         return 0;
23
                                                          39
24
                                                          40
      T range_query(int 1, int r) {
                                                                     if (1 <= start && end <= r) {</pre>
          T res_l = neutral_value, res_r =
                                                                         return tree[node];
26
                                                          42
      neutral_value;
                                                                     }
                                                          43
                                                                     int mid = (start + end) / 2;
                                                          44
           for (1 += n, r += n + 1; 1 < r; 1 >>= 1, r
                                                                     int left_gcd = query(2 * node + 1, start, mid
28
                                                          45
      >>= 1) {
                                                                    int right_gcd = query(2 * node + 2, mid + 1,
              if (1 & 1) res_l = combine(res_l, tree[1 46
29
      ++]);
                                                                 end, 1, r);
              if (r & 1) res_r = combine(tree[--r],
                                                                     return gcd(left_gcd, right_gcd);
3.0
      res_r);
                                                          48
31
          }
                                                          50 public:
32
           return combine(res_1, res_r);
                                                                 SegmentTreeGCD(const vector<int>& arr) {
                                                          51
                                                                    n = arr.size();
3.4
                                                          5.2
35
                                                          53
                                                                     tree.resize(4 * n);
      void update(int pos, T new_val) {
                                                                     build(arr, 0, 0, n - 1);
                                                          54
          tree[pos += n] = new_val;
3.7
                                                          55
                                                          56
                                                                 void update(int idx, int value) {
          for (pos >>= 1; pos > 0; pos >>= 1)
                                                                     update(0, 0, n - 1, idx, value);
39
                                                          5.7
              tree[pos] = combine(tree[2 * pos], tree[2 58
40
       * pos + 1]);
                                                          5.9
                                                                 int query(int 1, int r) {
                                                                     return query(0, 0, n - 1, 1, r);
41
                                                          60
42 };
                                                          61
                                                          62 };
  3.2 Segtree Gcd
                                                             3.3 Merge Sort Tree
int gcd(int a, int b) {
                                                          1 struct SegTree {
2
```

```
if (b == 0)
          return a;
      return gcd(b, a % b);
7 class SegmentTreeGCD {
                                                           6
8 private:
      vector < int > tree;
      int n;
                                                           10
      void build(const vector<int>& arr, int node, int 11
12
      start, int end) {
          if (start == end) {
1.3
               tree[node] = arr[start];
          } else {
1.5
                                                           14
               int mid = (start + end) / 2;
16
17
               build(arr, 2 * node + 1, start, mid);
                                                           16
               build(arr, 2 * node + 2, mid + 1, end); 17
18
               tree[node] = gcd(tree[2 * node + 1], tree 18
      [2 * node + 2]);
                                                           1.9
                                                           20
      }
21
                                                           21
```

22

```
vector < vector < int >> tree;
SegTree(vector<int> &a) {
    n = a.size();
    tree.resize(4 * n);
    build(1, 0, n - 1, a);
void build(int x, int lx, int rx, vector<int> &a)
    if (lx == rx) {
        tree[x] = { a[lx] };
        return;
    int mid = lx + (rx - lx)/2;
    build(2 * x, lx, mid, a);
    build(2 * x + 1, mid + 1, rx, a);
    auto &L = tree[2 * x], &R = tree[2 * x + 1];
    tree[x].resize(L.size() + R.size());
    merge(L.begin(), L.end(), R.begin(), R.end(),
 tree[x].begin());
```

```
}
                                                          1 // 1 - index, 0(1)
                                                          2 struct SparseTable {
23
      int query(int x, int lx, int rx, int l, int r) {
                                                               vector < vector < int >> st;
24
          if (1x >= 1 && rx <= r) {
                                                               int max_log;
25
              auto &v = tree[x];
                                                              SparseTable(vector<int>& arr) {
               return v.end() - upper_bound(v.begin(), v 6
                                                                   int n = arr.size();
27
      .end(), r);
                                                                    max_log = floor(log2(n)) + 1;
                                                                    st.resize(n, vector<int>(max_log));
         }
                                                                    for (int i = 0; i < n; i++) {</pre>
          if (rx < 1 || lx > r) {
              return 0;
                                                                        st[i][0] = arr[i];
                                                                    }
31
                                                         11
          int mid = lx + (rx - lx)/2;
                                                                    for (int j = 1; j < max_log; j++) {</pre>
                                                                        for (int i = 0; i + (1 << j) <= n; i++) {
          return query(2 * x, lx, mid, l, r) + query(2 13
33
                                                                            st[i][j] = max(st[i][j - 1], st[i +
      * x + 1, mid + 1, rx, l, r);
                                                         14
34
                                                                (1 << (j - 1))][j - 1]);
35
                                                         15
      int query(int 1, int r) {
                                                                    }
        return query(1, 0, n - 1, 1, r);
3.7
                                                         18
                                                                int query(int L, int R) {
39 }
                                                                    int tamanho = R - L + 1;
                                                         19
                                                                    int k = floor(log2(tamanho));
40
                                                         20
_{41} // Checar se o range 	ilde{\mathtt{Al}} todo distinto
                                                                    return max(st[L][k], st[R - (1 << k) + 1][k])</pre>
                                                         21
_{42} // Cada cara e sua pr	ilde{\mathtt{A}}şxima apari	ilde{\mathtt{A}}ğ	ilde{\mathtt{A}}čo a direita,
      conta quantos caras que a prÃşxima apariÃğÃčo a
      direita ta dentro do range ainda
                                                         23 }:
43 vector < int > nr(n);
44 map < int , int > mp;
                                                                  Psum 2d
45 for (int i = n - 1; i >= 0; i--) {
      auto it = mp.find(a[i]);
                                                          vector < vector < int >> psum(h+1, vector < int > (w+1, 0));
      nr[i] = it != mp.end() ? it->second : n;
47
      mp[a[i]] = i;
48
                                                          3 for (int i=1; i<=h; i++){</pre>
49 }
                                                                for (int j=1; j<=w; j++){</pre>
50 SegTree seg(nr);
                                                                    cin >> psum[i][j];
                                                                    psum[i][j] += psum[i-1][j]+psum[i][j-1]-psum[
  3.4 Ordered Set E Map
                                                                i-1][j-1];
                                                          8 }
2 #include < ext/pb_ds/assoc_container.hpp>
#include < ext/pb_ds/tree_policy.hpp>
                                                         10 // retorna a psum2d do intervalo inclusivo [(a, b), (
4 using namespace __gnu_pbds;
                                                                c, d)]
5 using namespace std;
                                                         int retangulo(int a, int b, int c, int d){
                                                                c = min(c, h), d = min(d, w);
a = max(0LL, a-1), b = max(0LL, b-1);
      null_type, less_equal <T>, rb_tree_tag,
                                                         14
      tree_order_statistics_node_update>;
                                                                return v[c][d]-v[a][d]-v[c][b]+v[a][b];
, less<T>, rb_tree_tag,
      tree_order_statistics_node_update>;
                                                            3.7 Segtree Sum
9 template <typename T, typename R> using o_map = tree<</pre>
      T, R, less<T>, rb_tree_tag,
      tree_order_statistics_node_update>;
                                                          1 struct SegTree {
                                                               ll merge(ll a, ll b) { return a + b; }
10
11 int main() {
                                                                const ll neutral = 0;
                                                                int n;
   int i, j, k, n, m;
                                                                vector<11> t, lazy;
  o_set<<del>int</del>>st;
                                                                vector < bool > replace;
14
   st.insert(1):
                                                                inline int lc(int p) { return p * 2; }
    st.insert(2);
15
                                                                inline int rc(int p) { return p * 2 + 1; }
    cout << *st.find_by_order(0) << endl; /// k-esimo</pre>
16
                                                                void push(int p, int 1, int r) {
     elemento
                                                                    if (replace[p]) {
   cout << st.order_of_key(2) << endl; ///numero de</pre>
                                                         10
     elementos menores que k
                                                                        t[p] = lazy[p] * (r - l + 1);
                                                         11
                                                                        if (1 != r) {
    o_map < int , int > mp;
                                                         12
18
    mp.insert({1, 10});
                                                                            lazy[lc(p)] = lazy[p];
                                                         13
19
    mp.insert({2, 20});
                                                                            lazy[rc(p)] = lazy[p];
20
                                                                            replace[lc(p)] = true;
    cout << mp.find_by_order(0) -> second << endl; /// k - 15
                                                         16
                                                                            replace[rc(p)] = true;
     esimo elemento
    cout << mp.order_of_key(2) << endl; /// numero de</pre>
                                                                    } else if (lazy[p] != 0) {
     elementos (chave) menores que k
                                                         18
                                                                        t[p] += lazy[p] * (r - l + 1);
    return 0;
                                                                        if (1 != r) {
24 }
                                                         20
                                                                            lazy[lc(p)] += lazy[p];
        Sparse Table
                                                                            lazy[rc(p)] += lazy[p];
                                                         22
```

23

1, 1), c(n) {

for (int i = 1; i <= n; ++i) par[i] = i;</pre>

```
int find(int i) {
24
                                                          7
          replace[p] = false;
                                                                     return (par[i] == i ? i : (par[i] = find(par[
25
                                                                 il))):
26
          lazy[p] = 0;
                                                                 }
      void build(int p, int l, int r, const vector<ll> 10
                                                                 bool same(int i, int j) {
      &v) {
                                                                    return find(i) == find(j);
                                                          11
          if (1 == r) {
                                                          12
              t[p] = v[1];
                                                                 int get_size(int i) {
3.0
                                                          1.3
          } else {
                                                                     return sz[find(i)];
31
                                                          14
               int mid = (1 + r) / 2;
                                                          15
               build(lc(p), 1, mid, v);
                                                                 int count() {
33
                                                          16
               build(rc(p), mid + 1, r, v);
                                                          17
                                                                     return c; // quantos componentes conexos
3.5
               t[p] = merge(t[lc(p)], t[rc(p)]);
                                                          18
                                                                 int merge(int i, int j) {
                                                          19
                                                                     if ((i = find(i)) == (j = find(j))) return
3.7
      }
                                                          20
      void build(int _n) {
38
39
          n = _n;
          t.assign(n * 4, neutral);
                                                                     if (rank[i] > rank[j]) swap(i, j);
40
                                                          22
          lazy.assign(n * 4, 0);
                                                                     par[i] = j;
          replace.assign(n * 4, false);
                                                                     sz[j] += sz[i];
42
                                                          24
                                                          25
                                                                     if (rank[i] == rank[j]) rank[j]++;
43
      void build(const vector<11> &v) {
                                                          26
44
          n = (int)v.size();
                                                          27
45
          t.assign(n * 4, neutral);
                                                          28 };
          lazy.assign(n * 4, 0);
47
           replace.assign(n * 4, false);
                                                            3.9
                                                                   Bit
48
           build(1, 0, n - 1, v);
49
50
                                                          1 class BIT {
      void build(ll *bg, ll *en) {
51
                                                                vector < int > bit;
          build(vector<ll>(bg, en));
52
                                                                 int n:
53
                                                                 int sum(int idx) {
                                                          4
      11 query(int p, int 1, int r, int L, int R) {
5.4
                                                                     int result = 0;
          push(p, 1, r);
5.5
                                                                     while (idx > 0) {
           if (1 > R || r < L) return neutral;</pre>
                                                                         result += bit[idx];
           if (1 >= L && r <= R) return t[p];</pre>
57
                                                                         idx -= idx & -idx;
           int mid = (1 + r) / 2;
                                                          9
           auto ql = query(lc(p), l, mid, L, R);
59
                                                          10
                                                                     return result;
           auto qr = query(rc(p), mid + 1, r, L, R);
60
                                                          11
           return merge(ql, qr);
61
      }
62
      ll query(int l, int r) { return query(1, 0, n - 13 public:
63
                                                                 BIT(int size) {
      1, l, r); }
      void update(int p, int 1, int r, int L, int R, 11^{15}
                                                                    n = size;
64
                                                                     bit.assign(n + 1, 0); // BIT indexada em 1
       val, bool repl = 0) {
                                                          17
          push(p, 1, r);
65
                                                                 void update(int idx, int delta) {
                                                          18
           if (1 > R || r < L) return;</pre>
                                                                     while (idx <= n) {</pre>
                                                          19
           if (1 >= L && r <= R) {
67
                                                                         bit[idx] += delta;
                                                          2.0
               lazy[p] = val;
                                                          2.1
                                                                         idx += idx & -idx;
               replace[p] = repl;
69
                                                          22
               push(p, 1, r);
70
                                                          23
          } else {
71
                                                                 int query(int idx) {
              int mid = (1 + r) / 2;
72
                                                                     return sum(idx):
               update(lc(p), l, mid, L, R, val, repl);
               update(rc(p), mid + 1, r, L, R, val, repl ^{26}
7.4
                                                                 int range_query(int 1, int r) {
      );
                                                          28
                                                                     return sum(r) - sum(l - 1);
               t[p] = merge(t[lc(p)], t[rc(p)]);
          }
                                                          30 }:
      }
78
      void sumUpdate(int 1, int r, 11 val) { update(1,
                                                          82 BIT fenwick(n);
      0, n - 1, l, r, val, 0); }
                                                          33 for(int i = 1; i <= n; i++) {
      void assignUpdate(int 1, int r, 11 val) { update
                                                          34
                                                                 fenwick.update(i, arr[i]);
      (1, 0, n - 1, 1, r, val, 1); }
                                                          35
80 } segsum;
  3.8 Dsu
                                                                 Search and sort
1 struct DSU {
                                                                 Pilha Monotonic
                                                            4.1
      vector < int > par, rank, sz;
      int c;
```

 $DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n + 1) vector < int > find_esq(vector < int > &v, bool maior) \{ (int n) : par(n + 1), rank(n + 1, 0), sz(n + 1) vector < int > (int n) \}$

int n = v.size();

stack<int> s;

vector < int > result(n);

```
// Adiciona os elementos restantes do subarray
                                                            2.7
6
       for (int i = 0; i < n; i++) {</pre>
                                                                   esquerdo (se houver).
           while (!s.empty() && (maior ? v[s.top()] <= v 28</pre>
                                                                   while (i < x) v[k++] = left[i++];</pre>
       [i] : v[s.top()] >= v[i])) {
               s.pop();
                                                                   // Adiciona os elementos restantes do subarray
           }
                                                                   direito (se houver).
9
           if (s.empty()) {
                                                                   while (j < y) v[k++] = right[j++];</pre>
10
               result[i] = -1;
                                                            3.2
           } else {
                                                                   return swaps; // Retorna o numero total de
12
                                                            33
               result[i] = v[s.top()];
                                                                   trocas realizadas.
                                                            34 }
14
15
           s.push(i);
                                                            35
      }
16
                                                            36 int mergeSort(vector<int>& v, int 1, int r) {
       return result;
                                                            37
                                                                   int swaps = 0;
17
18 }
                                                            38
                                                                   if (1 < r) {</pre>
19
                                                            39
20 // maior = true -> encontra o primeiro maior Ãă
                                                                       // Encontra o ponto medio para dividir o
      direita
                                                                   vetor.
21 vector<int> find_dir(vector<int> &v, bool maior) {
                                                                       int m = 1 + (r - 1) / 2;
      int n = v.size();
22
                                                            42
       vector < int > result(n);
                                                                       // Chama merge sort para a metade esquerda.
                                                            43
       stack < int > s;
                                                                       swaps += mergeSort(v, 1, m);
24
                                                            44
       for (int i = n - 1; i >= 0; i--) {
                                                                       // Chama merge sort para a metade direita.
25
                                                            45
           while (!s.empty() && (maior ? v[s.top()] <= v 46</pre>
                                                                       swaps += mergeSort(v, m + 1, r);
       [i] : v[s.top()] >= v[i])) {
                                                            47
               s.pop();
                                                                       // Mescla as duas metades e conta as trocas.
                                                            48
           }
                                                                       swaps += mergeAndCount(v, 1, m, r);
28
                                                            49
           if (s.empty()) {
29
                                                            50
               result[i] = -1;
                                                            51
30
                                                                   return swaps; // Retorna o numero total de
           } else {
3.1
                                                            5.2
               result[i] = v[s.top()];
                                                                   trocas no vetor.
32
           }
                                                            53 }
3.3
34
           s.push(i);
35
       }
                                                              5
                                                                    Math
       return result;
36
37 }
```

4.2 Mergeandcount

```
2 // Realiza a mesclagem de dois subarrays e conta o
      nÞmero de trocas necessÃąrias.
3 int mergeAndCount(vector<int>& v, int 1, int m, int r 6 // (a^b) % m em 0(log b)
      ) {
      int x = m - 1 + 1; // Tamanho do subarray
4
      int y = r - m; // Tamanho do subarray direito.
                                                          10
      // Vetores temporarios para os subarray esquerdo 12
      e direito.
      vector<int> left(x), right(y);
      for (int i = 0; i < x; i++) left[i] = v[l + i];</pre>
      for (int j = 0; j < y; j++) right[j] = v[m + 1 +</pre>
      i];
      int i = 0, j = 0, k = 1;
13
      int swaps = 0;
1.5
      while (i < x && j < y) {
16
          if (left[i] <= right[j]) {</pre>
                                                          21
              // Se o elemento da esquerda for menor ou
18
       igual, coloca no vetor original.
              v[k++] = left[i++];
19
20
           } else {
              // Caso contrario, coloca o elemento da 25 int perm(int n, int k) {
      direita e conta as trocas.
              v[k++] = right[j++];
               swaps += (x - i);
23
          }
      }
25
26
```

5.1 Combinatorics

```
1 const int MAXN_FATORIAL = 200005;
 2 const int MOD = 1e9 + 7;
 3 // DEFINE INT LONG LONG PLMDS
 4 int fat[MAXN_FATORIAL], fati[MAXN_FATORIAL];
 7 // coloque o fexp
 9 int inv(int n) { return fexp(n, MOD - 2); }
 void precalc() {
      fat[0] = 1;
       fati[0] = 1;
 13
        for (int i = 1; i < MAXN_FATORIAL; i++) fat[i] =</pre>
 14
       (fat[i - 1] * i) % MOD;
       fati[MAXN_FATORIAL - 1] = inv(fat[MAXN_FATORIAL -
        1]);
        for (int i = MAXN_FATORIAL - 2; i >= 0; i--) fati
 16
       [i] = (fati[i + 1] * (i + 1)) % MOD;
 17 }
 19 int choose(int n, int k) {
       if (k < 0 || k > n) return 0;
 20
       return (((fat[n] * fati[k]) % MOD) * fati[n - k])
        % MOD;
22 }
 24 // n! / (n-k)!
       if (k < 0 || k > n) return 0;
 26
       return (fat[n] * fati[n - k]) % MOD;
 27
 28 }
 30 // C_n = (1 / (n+1)) * C(2n, n)
 31 int catalan(int n) {
```

```
if (n < 0 || 2 * n >= MAXN_FATORIAL) return 0; 3 int seg_sieve(int 1, int r){
32
33
      int c2n_n = choose(2 * n, n);
                                                                 if (1 > r) return 0;
                                                           4
                                                                 vector < bool > is_prime(r - l + 1, true);
      return (c2n_n * inv(n + 1)) % MOD;
34
                                                           5
35
                                                                 if (1 == 1) is_prime[0] = false;
  5.2 Equação Diofantina
                                                                 for (int p : primos){
                                                                      if (p * p > r) break;
                                                                      int start = max(p * p, (1 + p - 1) / p * p);
                                                           10
int extended_gcd(int a, int b, int& x, int& y) {
                                                                      for (int j = start; j <= r; j += p){</pre>
                                                           11
      if (a == 0) {
                                                                          if (j >= 1) {
          x = 0;
3
                                                                              is_prime[j - 1] = false;
                                                           13
          y = 1;
4
                                                           14
                                                                          }
          return b;
                                                                      }
                                                           1.5
      }
                                                           16
      int x1, y1;
                                                           17
      int gcd = extended_gcd(b % a, a, x1, y1);
                                                                 return accumulate(all(is_prime), 011);;
                                                           18
      x = y1 - (b / a) * x1;
g
                                                           19 }
      y = x1;
10
      return gcd;
11
                                                                   Totient
                                                             5.5
12 }
13
14 bool solve(int a, int b, int c, int& x0, int& y0) {
                                                           _1 // phi(n) = n * (1 - 1/p1) * (1 - 1/p2) * ...
      int x, y;
                                                           2 int phi(int n) {
      int g = extended_gcd(abs(a), abs(b), x, y);
                                                                 int result = n;
      if (c % g != 0) {
17
                                                                  for (int i = 2; i * i <= n; i++) {
          return false;
                                                                      if (n % i == 0) {
      }
19
                                                                          while (n % i == 0)
      x0 = x * (c / g);
20
                                                                             n /= i;
      y0 = y * (c / g);
21
                                                                          result -= result / i;
      if (a < 0) x0 = -x0;
22
                                                                      }
      if (b < 0) y0 = -y0;
23
                                                                 }
                                                           10
      return true;
24
                                                                 if (n > 1) // SE n sobrou, ele \tilde{A}l' um fator primo
                                                           11
25 }
                                                                     result -= result / n;
                                                           12
                                                                 return result;
                                                           13
  5.3 Discrete Log
                                                           15
_{\rm 1} // Returns minimum x for which a^x = b (mod m), a and ^{\rm 16} // crivo phi
                                                           17 const int MAXN_PHI = 1000001;
       m are coprime.
                                                           18 int phiv[MAXN_PHI];
_{2} // if the answer dont need to be greater than some
      value, the vector < int > can be removed
                                                          19 void phi_sieve() {
                                                                 for (int i = 0; i < MAXN_PHI; i++) phiv[i] = i;
                                                          2.0
3 int discrete_log(int a, int b, int m) {
                                                           21
                                                                 for (int i = 2; i < MAXN_PHI; i++) {</pre>
      a \% = m, b \% = m;
                                                                      if (phiv[i] == i) {
                                                          22
5
      int n = sqrt(m) + 1;
                                                                          for (int j = i; j < MAXN_PHI; j += i)</pre>
                                                           23
                                                                 phiv[j] -= phiv[j] / i;
      int an = 1:
                                                                     }
      for (int i = 0; i < n; ++i)</pre>
                                                           24
                                                           25
          an = (an * 111 * a) % m;
                                                           26 }
10
11
      unordered_map < int , vector < int >> vals;
                                                                  Menor Fator Primo
      for (int q = 0, cur = b; q \le n; ++q) {
                                                             5.6
12
           vals[cur].push_back(q);
           cur = (cur * 111 * a) % m;
14
                                                           const int MAXN = 1000001; // Limite para o Crivo.
15
                                                           2 int spf[MAXN];
16
                                                           3 vector < int > primos;
      int res = LLONG_MAX;
                                                           5 void crivo() {
      for (int p = 1, cur = 1; p <= n; ++p) {</pre>
19
                                                                 for (int i = 2; i * i < MAXN; i++) {</pre>
                                                           6
           cur = (cur * 111 * an) % m;
                                                                      if (spf[i] == i) {
          if (vals.count(cur)) {
21
                                                                          for (int j = i * i; j < MAXN; j += i) {</pre>
               for (int q: vals[cur]){
22
                                                           9
                                                                              if (spf[j] == j) {
                   int ans = n * p - q;
                                                                                   spf[j] = i;
                                                           10
                   res = min(res, ans);
24
                                                           11
                                                                          }
                                                           12
          }
26
                                                           13
                                                                     }
27
                                                           14
28
       return res;
                                                                  for (int i = 2; i < MAXN; i++) {</pre>
                                                           15
29 }
                                                                      if (spf[i] == i) {
                                                           16
                                                           17
                                                                          primos.push_back(i);
  5.4 Segment Sieve
                                                                 }
1 // Retorna quantos primos tem entre [1, r] (inclusivo 20 }
2 // precisa de um vetor com os primos atÃľ sqrt(r)
                                                           22 map < int , int > fatora(int n) {
```

```
map <int , int > fatores;
                                                                while (x > 1) {
23
                                                         Q
      while (n > 1) {
                                                                    int p = crivo[x], cnt = 0;
24
                                                          10
                                                                     while (x \% p == 0) cnt++, x /= p;
         fatores[spf[n]]++;
25
                                                          11
          n /= spf[n];
                                                          12
                                                                     primos.push_back({p, cnt});
                                                          13
      return fatores;
28
                                                          14
29 }
                                                                 for (int i = 0; i < primos.size(); i++) {</pre>
                                                          15
                                                                     int cur = 1, len = ans.size();
3.0
                                                          16
31 int numero_de_divisores(int n) {
                                                         17
      if (n == 1) return 1;
                                                                     for (int j=0; j<primos[i][1]; j++){</pre>
      map < int , int > fatores = fatorar(n);
                                                                         cur *= primos[i][0];
33
                                                          19
      int nod = 1;
                                                                         for (int k=0; k<len; k++)</pre>
      for (auto &[primo, expoente] : fatores) nod *= ( _{21}
3.5
                                                                             ans.push_back(cur*ans[k]);
      expoente + 1);
36
      return nod;
37 }
                                                          24
                                                          25
                                                                 return ans;
39 // DEFINE INT LONG LONG
                                                          26 }
40 int soma_dos_divisores(int n) {
                                                            5.10 Crivo
      if (n == 1) return 1;
      map <int, int > fatores = fatorar(n);
42
      int sod = 1;
43
                                                         1 // O(n*log(log(n)))
      for (auto &[primo, expoente] : fatores) {
44
                                                         2 bool composto[MAX]
          int termo_soma = 1;
                                                          3 for(int i = 1; i <= n; i++) {</pre>
          int potencia_primo = 1;
46
                                                               if(composto[i]) continue;
          for (int i = 0; i < expoente; i++) {</pre>
47
                                                                for(int j = 2*i; j <= n; j += i)
                                                          5
               potencia_primo *= primo;
                                                                    composto[j] = 1;
               termo_soma += potencia_primo;
49
                                                          7 }
          }
          sod *= termo_soma;
5.1
                                                            5.11 Mod Inverse
52
5.3
      return sod;
                                                          1 array < int, 2 > extended_gcd(int a, int b) {
54 }
                                                                if (b == 0) return {1, 0};
                                                                 auto [x, y] = extended_gcd(b, a % b);
  5.7
        Exgcd
                                                          3
                                                          4
                                                                 return {y, x - (a / b) * y};
                                                          5 }
_{1} // O retorno da funcao eh {n, m, g}
2 // e significa que gcd(a, b) = g e
                                                          7 int mod_inverse(int a, int m) {
3 // n e m sao inteiros tais que an + bm = g
                                                                auto [x, y] = extended_gcd(a, m);
4 array<11, 3> exgcd(int a, int b) {
                                                                 return (x % m + m) % m;
     if(b == 0) return {1, 0, a};
                                                          10 }
      auto [m, n, g] = exgcd(b, a % b);
      return {n, m - a / b * n, g};
                                                            5.12 Base Calc
                                                          int char_to_val(char c) {
  5.8 Fexp
                                                                 if (c >= '0' && c <= '9') return c - '0';
                                                          2
                                                                 else return c - 'A' + 10;
                                                          3
_1 // a^e mod m
                                                          4 }
2 // O(log n)
                                                          6 char val_to_char(int val) {
4 int fexp(int a, int e, int m) {
                                                                 if (val >= 0 && val <= 9) return val + '0';</pre>
      a %= m;
                                                                 else return val - 10 + 'A';
                                                          8
      int ans = 1;
                                                          9 }
      while (e > 0){
                                                          1.0
          if (e & 1) ans = ans*a % m;
                                                          int to_base_10(string &num, int bfrom) {
          a = a*a \% m;
9
                                                                 int result = 0;
                                                          12
          e /= 2;
                                                                 int pot = 1;
                                                          13
      }
11
                                                                 for (int i = num.size() - 1; i >= 0; i--) {
      return ans%m;
12
                                                          15
                                                                    if (char_to_val(num[i]) >= bfrom) return -1;
13 }
                                                                     result += char_to_val(num[i]) * pot;
                                                          16
                                                          17
                                                                     pot *= bfrom;
  5.9 Divisores
                                                          18
                                                         19
                                                                 return result;
_{\scriptscriptstyle 1} // Retorna um vetor com os divisores de x
                                                         20 }
2 // eh preciso ter o crivo implementado
                                                          21
3 // O(divisores)
                                                          22 string from_base_10(int n, int bto) {
                                                          23
                                                                if (n == 0) return "0";
                                                                 string result = "";
5 vector<int> divs(int x){
      vector < int > ans = {1};
                                                                 while (n > 0) {
      vector<array<int, 2>> primos; // {primo, expoente 26
                                                                     result += val_to_char(n % bto);
                                                                     n /= bto;
                                                         27
```

```
reverse(result.begin(), result.end());
                                                                      cin >> u >> v >> w; u--; v--;
29
                                                           3.0
30
      return result;
                                                           31
                                                                      dist[u][v] = min(dist[u][v], w);
31 }
                                                                      dist[v][u] = min(dist[v][u], w);
                                                           32
32
                                                           33
  string convert_base(string &num, int bfrom, int bto) 34
                                                                  floydWarshall();
                                                                  while(q--) {
                                                           35
      int n_base_10 = to_base_10(num, bfrom);
                                                                      int u, v;
34
                                                                      cin >> u >> v; u--; v--;
      return from_base_10(n_base_10, bto);
3.5
                                                           3.7
                                                                      if(dist[u][v] == linf) cout << -1 << '\n';</pre>
36
                                                           38
                                                           39
                                                                      else cout << dist[u][v] << '\n';</pre>
       Graph
                                                           40
                                                           41 }
```

13

14

16

17

21

22

23

Dijkstra 6.1

```
1 // SSP com pesos positivos.
_2 // O((V + E) log V).
4 vector<int> dijkstra(int S) {
      vector < bool > vis(MAXN, 0);
       vector<ll> dist(MAXN, LLONG_MAX);
       dist[S] = 0;
      priority_queue < pii, vector < pii >, greater < pii >> pq 7 * - 8: VALIDICE INTOIGE.

8 * - e: vÄlrtice final (opcional). Se informado,
9
      pq.push({0, S});
10
       while(pq.size()) {
           11 v = pq.top().second;
           pq.pop();
12
           if(vis[v]) continue;
           vis[v] = 1;
14
           for(auto &[peso, vizinho] : adj[v]) {
15
                if(dist[vizinho] > dist[v] + peso) {
1.6
                    dist[vizinho] = dist[v] + peso;
                    pq.push({dist[vizinho], vizinho});
               }
19
           }
      }
21
                                                              18
       return dist;
22
                                                              19
23 }
                                                              20
```

Floyd Warshall

```
1 // SSP e acha ciclos.
                                                               24
2 // Bom com constraints menores.
                                                               25
3 // O(n^3)
                                                               26
                                                                27
5 int dist[501][501];
                                                               2.8
                                                               29
7 void floydWarshall() {
                                                               3.0
       for(int k = 0; k < n; k++) {</pre>
                                                               31
            for(int i = 0; i < n; i++) {</pre>
                for(int j = 0; j < n; j++) {</pre>
10
                     dist[i][j] = min(dist[i][j], dist[i][33
       k] + dist[k][j]);
                                                                3.4
                }
                                                                3.5
           }
13
                                                                36
       }
14
                                                                37
15 }
16 void solve() {
                                                                38
       int m, q;
17
                                                                39
18
       cin >> n >> m >> q;
                                                                40
       for(int i = 0; i < n; i++) {</pre>
                                                               41
19
           for(int j = i; j < n; j++) {
                                                               42
                if(i == j) {
21
                                                               43
                    dist[i][j] = dist[j][i] = 0;
                                                               44
23
                } else {
                                                                45
                     dist[i][j] = dist[j][i] = linf;
                                                               46
24
                                                               47
           }
26
                                                                48
       for(int i = 0; i < m; i++) {</pre>
28
                                                               5.0
           int u, v, w;
                                                               51
29
```

6.3Eulerian Path

```
1 /**
* VersÃčo que assume: #define int long long
  * Retorna um caminho/ciclo euleriano em um grafo (se
4
      existir).
  * - g: lista de adjacÃłncia (vector<vector<int>>).
6 * - directed: true se o grafo for dirigido.
   * - s: vÃľrtice inicial.
      tenta caminho de s atÃľ e.
  * - 0(Nlog(N))
9
* Retorna vetor com a sequÃłncia de vÃľrtices, ou
      vazio se impossÃnvel.
11 */
12 vector <int> eulerian_path(const vector <vector <int>>&
      g, bool directed, int s, int e = -1) {
      int n = (int)g.size();
      // cÃşpia das adjacÃłncias em multiset para
      permitir remoÃğÃčo especÃŋfica
      vector<multiset<int>> h(n);
      vector < int > in_degree(n, 0);
      vector<int> result;
      stack < int > st;
      // preencher h e indegrees
      for (int u = 0; u < n; ++u) {</pre>
          for (auto v : g[u]) {
              ++in_degree[v];
              h[u].emplace(v);
      }
      st.emplace(s);
      if (e != -1) {
          int out_s = (int)h[s].size();
          int out_e = (int)h[e].size();
          int diff_s = in_degree[s] - out_s;
          int diff_e = in_degree[e] - out_e;
          if (diff_s * diff_e != -1) return {}; //
      impossÃŋvel
      for (int u = 0; u < n; ++u) {
          if (e != -1 && (u == s || u == e)) continue;
          int out_u = (int)h[u].size();
          if (in_degree[u] != out_u || (!directed && (
      in_degree[u] & 1))) {
              return {};
      }
      while (!st.empty()) {
          int u = st.top();
          if (h[u].empty()) {
              result.emplace_back(u);
              st.pop();
          } else {
              int v = *h[u].begin();
              auto it = h[u].find(v);
              if (it != h[u].end()) h[u].erase(it);
              --in_degree[v];
              if (!directed) {
```

```
int u = edges[id].u;
                    auto it2 = h[v].find(u);
52
                                                            5.5
                    if (it2 != h[v].end()) h[v].erase(it2 56
                                                                            if (level[v] + 1 != level[u])
      );
                                                                                 continue
                                                            5.7
54
                    --in_degree[u];
                                                                            long long tr = dfs(u, min(pushed, edges[
                                                            58
               }
                                                                   id].cap - edges[id].flow));
               st.emplace(v);
                                                                            if (tr == 0)
56
           }
                                                                                continue;
                                                                            edges[id].flow += tr;
       }
5.8
                                                            6.1
       for (int u = 0; u < n; ++u) {
                                                                            edges[id ^ 1].flow -= tr;
           if (in_degree[u] != 0) return {};
                                                                            return tr;
60
                                                            63
                                                                        }
61
                                                            64
62
       reverse(result.begin(), result.end());
                                                                        return 0;
63
       return result;
                                                            66
64 }
                                                            67
                                                            68
                                                                   long long flow() {
  6.4 Dinitz
                                                                        long long f = 0;
                                                            69
                                                            70
                                                                        while (true) {
                                                                            fill(level.begin(), level.end(), -1);
1 // Complexidade: O(V^2E)
                                                                            level[s] = 0;
struct FlowEdge {
                                                            7.3
                                                                            q.push(s);
                                                                            if (!bfs())
                                                            74
       int v, u;
       long long cap, flow = 0;
5
                                                                            fill(ptr.begin(), ptr.end(), 0);
       FlowEdge(int v, int u, long long cap) : v(v), u(u<sup>76</sup>
                                                                            while (long long pushed = dfs(s, flow_inf
       ), cap(cap) {}
                                                                   )) {
                                                                                f += pushed;
                                                            7.8
                                                                            }
9 struct Dinic {
                                                            79
                                                                        }
       const long long flow_inf = 1e18;
                                                            80
10
       vector < Flow Edge > edges;
                                                            81
                                                                        return f;
                                                                   }
       vector<vector<int>> adj;
                                                            82
                                                            83 }:
       int n, m = 0;
13
       int s, t;
14
                                                                     Khan
                                                               6.5
       vector < int > level, ptr;
15
       queue < int > q;
16
                                                             1 // topo-sort DAG
                                                           2 // lexicograficamente menor.
       Dinic(int n, int s, int t) : n(n), s(s), t(t) {
18
                                                             3 // N: nÞmero de vÃľrtices (1-indexado)
           adj.resize(n);
                                                             4 // adj: lista de adjacÃłncia do grafo
20
           level.resize(n);
           ptr.resize(n);
21
       }
                                                             6 const int MAXN = 5 * 1e5 + 2;
23
                                                             vector < int > adj [MAXN];
       void add_edge(int v, int u, long long cap) {
                                                             8 int N;
           edges.emplace_back(v, u, cap);
25
           edges.emplace_back(u, v, 0);
                                                            10 vector < int > kahn() {
26
27
           adj[v].push_back(m);
                                                            11
                                                                   vector < int > indegree(N + 1, 0);
                                                                   for (int u = 1; u \le N; u++) {
           adj[u].push_back(m + 1);
28
                                                            12
           m += 2;
                                                            13
                                                                        for (int v : adj[u]) {
       }
3.0
                                                            1.4
                                                                            indegree[v]++;
3.1
                                                            1.5
                                                                   }
       bool bfs() {
                                                            16
32
           while (!q.empty()) {
                                                                   priority_queue<int, vector<int>, greater<int>> pq
33
               int v = q.front();
                                                                   for (int i = 1; i <= N; i++) {</pre>
35
               q.pop();
                                                             18
               for (int id : adj[v]) {
                                                                        if (indegree[i] == 0) {
                                                            19
                    if (edges[id].cap == edges[id].flow) 20
3.7
                                                                            pq.push(i);
                        continue;
38
                                                            21
                    if (level[edges[id].u] != -1)
                                                                   vector < int > result;
40
                        continue
                                                            23
                    level[edges[id].u] = level[v] + 1;
                                                                   while (!pq.empty()) {
                                                            24
42
                    q.push(edges[id].u);
                                                            25
                                                                       int u = pq.top();
               }
                                                                        pq.pop();
                                                            26
43
           }
44
                                                            27
                                                                        result.push_back(u);
                                                                        for (int v : adj[u]) {
           return level[t] != -1;
                                                            28
45
46
       }
                                                            29
                                                                            indegree[v]--;
                                                                            if (indegree[v] == 0) {
47
                                                            3.0
       long long dfs(int v, long long pushed) {
48
                                                            31
                                                                                pq.push(v);
           if (pushed == 0)
49
                                                            32
                                                                        }
50
               return 0;
                                                            33
           if (v == t)
51
                                                            34
               return pushed;
                                                                   if (result.size() != N) {
52
                                                            3.5
           for (int& cid = ptr[v]; cid < (int)adj[v].</pre>
53
                                                            36
                                                                        return {};
                                                                   }
       size(); cid++) {
                                                            3.7
               int id = adj[v][cid];
                                                                   return result;
54
                                                            38
```

```
39 }
                                                                                                       6 vector < vector < int >> adj(MAXN);
               Topological Sort
    6.6
                                                                                                       8 int bfs(int s, int t, int scale, vector<int>& parent)
                                                                                                                 fill(parent.begin(), parent.end(), -1);
 vector < int > adj [MAXN];
                                                                                                                 parent[s] = -2;
                                                                                                      10
 vector < int > estado(MAXN); // 0: nao visitado 1:
                                                                                                                 queue < pair < int , int >> q;
          processamento 2: processado
                                                                                                                 q.push({s, LLONG_MAX});
 3 vector < int > ordem;
                                                                                                      13
 4 bool temCiclo = false;
                                                                                                                 while (!q.empty()) {
                                                                                                      14
                                                                                                                        int cur = q.front().first;
                                                                                                      15
6 void dfs(int v) {
                                                                                                                         int flow = q.front().second;
           if(estado[v] == 1) {
                                                                                                                         q.pop();
                  temCiclo = true;
                                                                                                     18
                  return;
9
                                                                                                     19
                                                                                                                        for (int next : adj[cur]) {
10
                                                                                                                               if (parent[next] == -1 && capacity[cur][
                                                                                                      20
           if(estado[v] == 2) return;
11
                                                                                                                  next] >= scale) {
           estado[v] = 1;
                                                                                                                                       parent[next] = cur;
           for(auto &nei : adj[v]) {
                                                                                                                                        int new_flow = min(flow, capacity[cur
                  if(estado[v] != 2) dfs(nei);
14
                                                                                                                 ][next]);
15
                                                                                                                                        if (next == t)
                                                                                                     23
           estado[v] = 2;
16
                                                                                                                                               return new_flow;
                                                                                                      24
           ordem.push_back(v);
17
                                                                                                                                        q.push({next, new_flow});
           return;
18
                                                                                                                                }
19 }
                                                                                                                         }
                                                                                                     27
                                                                                                      28
    6.7 Acha Pontes
                                                                                                     29
                                                                                                                  return 0;
                                                                                                     30
 vector < int > d, low, pai;
                                                      // d[v] Tempo de
                                                                                                     31 }
          descoberta (discovery time)
                                                                                                     3.2
 vector<bool> vis;
                                                                                                     33 int maxflow(int s, int t) {
 3 vector < int > pontos_articulação;
                                                                                                                 int flow = 0:
                                                                                                     3.4
 4 vector<pair<int, int>> pontes;
                                                                                                                  vector < int > parent(MAXN);
                                                                                                     3.5
5 int tempo;
                                                                                                     36
                                                                                                                 int new_flow;
                                                                                                                 int scalling = 111 << 62;</pre>
                                                                                                     37
7 vector < vector < int >> adj;
                                                                                                                 while (scalling > 0) {
                                                                                                     3.9
9 void dfs(int u) {
                                                                                                      40
                                                                                                                         while (new_flow = bfs(s, t, scalling, parent)
          vis[u] = true;
           tempo++;
11
                                                                                                                                 if (new_flow == 0) continue;
                                                                                                      41
           d[u] = low[u] = tempo;
12
                                                                                                      42
                                                                                                                                flow += new_flow;
           int filhos_dfs = 0;
                                                                                                                                 int cur = t;
                                                                                                      43
14
           for (int v : adj[u]) {
                                                                                                                                while (cur != s) {
                                                                                                     44
                   if (v == pai[u]) continue;
                                                                                                     45
                                                                                                                                       int prev = parent[cur];
                  if (vis[v]) { // back edge
16
                                                                                                                                        capacity[prev][cur] -= new_flow;
                                                                                                      46
                         low[u] = min(low[u], d[v]);
                                                                                                      47
                                                                                                                                        capacity[cur][prev] += new_flow;
                  } else {
18
                                                                                                                                        cur = prev;
                                                                                                      48
                         pai[v] = u;
19
                          filhos_dfs++;
20
                                                                                                                         }
                                                                                                      5.0
                          dfs(v);
21
                                                                                                                         scalling /= 2;
                                                                                                      51
                          low[u] = min(low[u], low[v]);
                                                                                                      52
                          if (pai[u] == -1 && filhos_dfs > 1) {
23
                                                                                                     53
                                 pontos_articulacao.push_back(u);
                                                                                                                 return flow;
25
                                                                                                     55
                          if (pai[u] != -1 && low[v] >= d[u]) {
                                 pontos_articulacao.push_back(u);
                                                                                                                   Kruskal
28
                                 pontes.push_back({min(u, v), max(u, v), max(
                          if (low[v] > d[u]) {
30
           )});
                                                                                                       2 // O(E log E)
                          }
31
32
                  }
                                                                                                       4 struct DSU {
33
                                                                                                                vector < int > par, rank, sz;
34 }
                                                                                                                 DSU(int n) : par(n + 1), rank(n + 1, 0), sz(n +
    6.8 Edmonds-karp
                                                                                                                 1, 1), c(n) {
                                                                                                                         for (int i = 1; i <= n; ++i) par[i] = i;</pre>
1 // Edmonds-Karp com scalling O(Ešlog(F))
                                                                                                       9
                                                                                                                 int find(int i) {
3 int n, m;
                                                                                                                        return (par[i] == i ? i : (par[i] = find(par[
 4 const int MAXN = 510;
                                                                                                                 i])));
_{5} vector < vector < int >> capacity ( MAXN , vector < int > ( MAXN , _{12}
           0));
                                                                                                                 bool same(int i, int j) {
```

```
return find(i) == find(j);
                                                             31 }
1.4
15
                                                             32 reverse(ciclo.begin(), ciclo.end());
       int get_size(int i) {
16
                                                               6.11 Lca Jc
           return sz[find(i)];
       }
       int count() {
19
                                                             1 const int MAXN = 200005;
           return c; // quantos componentes conexos
20
                                                             2 int N:
                                                             3 int LOG;
       int merge(int i, int j) {
22
           if ((i = find(i)) == (j = find(j))) return
                                                             5 vector < vector < int >> adj;
       -1:
                                                             6 vector < int > profundidade;
                                                              vector < vector < int >> cima; // cima[v][j] Ãi o 2^j-
           if (rank[i] > rank[j]) swap(i, j);
25
                                                                   Ãľsimo ancestral de v
           par[i] = j;
26
           sz[j] += sz[i];
27
                                                             9 void dfs(int v, int p, int d) {
           if (rank[i] == rank[j]) rank[j]++;
28
                                                                  profundidade[v] = d;
                                                             10
29
           return ;;
                                                                    cima[v][0] = p; // o pai direto <math>\tilde{A}l' o 2^0-\tilde{A}l'simo
3.0
                                                                    ancestral
31 };
                                                                    for (int j = 1; j < LOG; j++) {</pre>
                                                             12
32
                                                                        // se o ancestral 2^{(j-1)} existir, calculamos
                                                             13
33 struct Edge {
                                                                     o 2^j
      int u, v, w;
                                                                        if (cima[v][j - 1] != -1) {
                                                             14
       bool operator <(Edge const & other) {</pre>
3.5
                                                                            cima[v][j] = cima[cima[v][j - 1]][j - 1];
                                                             15
          return weight <other.weight;</pre>
                                                                        } else {
                                                             16
37
                                                                            cima[v][j] = -1; // n\tilde{A}čo tem ancestral
38 }
                                                                    superior
39
                                                                        }
40 vector < Edge > kruskal (int n, vector < Edge > edges) {
                                                                    }
                                                             19
       vector < Edge > mst;
                                                                    for (int nei : adj[v]) {
                                                             20
      DSU dsu = DSU(n + 1);
42
                                                                        if (nei != p) {
                                                             21
       sort(edges.begin(), edges.end());
43
                                                                            dfs(nei, v, d + 1);
                                                             22
44
       for (Edge e : edges) {
                                                             23
           if (dsu.find(e.u) != dsu.find(e.v)) {
45
                                                             24
               mst.push_back(e);
                                                             25 }
               dsu.join(e.u, e.v);
47
                                                             26
           }
48
                                                             27 void build(int root) {
      }
49
                                                                    LOG = ceil(log2(N));
50
      return mst;
                                                                    {\tt profundidade.assign(N+1,0);}
                                                             29
51 }
                                                                    cima.assign(N + 1, vector < int > (LOG, -1));
                                                             30
                                                             31
                                                                    dfs(root, -1, 0);
  6.10 Bellman Ford
                                                            32 }
                                                             33
1 struct Edge {
                                                             34 int get_lca(int a, int b) {
      int u, v, w;
                                                             35
                                                                    if (profundidade[a] < profundidade[b]) {</pre>
3 };
                                                             36
                                                                        swap(a, b);
                                                             3.7
_{5} // se x = -1, nÃčo tem ciclo
                                                                    // sobe 'a' atÃl a mesma profundidade de 'b'
                                                             38
_{6} // se x != -1, pegar pais de x pra formar o ciclo
                                                                    for (int j = LOG - 1; j >= 0; j--) {
                                                             39
                                                                        if (profundidade[a] - (1 << j) >=
8 int n, m;
                                                                    profundidade[b]) {
9 vector < Edge > edges;
                                                                            a = cima[a][j];
                                                             41
vector < int > dist(n);
                                                             42
11 vector < int > pai(n, -1);
                                                             43
                                                                    // se 'b' era um ancestral de 'a', entÃčo 'a'
                                                             44
      for (int i = 0; i < n; i++) {</pre>
                                                                    agora Ãľ igual a 'b'
1.3
           x = -1;
1.4
                                                                    if (a == b) {
           for (Edge &e : edges) {
15
                                                             46
                                                                        return a;
                if (dist[e.u] + e.w < dist[e.v]) {</pre>
16
                                                             47
                    \label{eq:dist_e.u} \mbox{dist[e.u] + e.w}_{\ 48}
      );
                                                                    // sobe os dois nÃşs juntos atÃl encontrar os
                                                             49
                    pai[e.v] = e.u;
18
                                                                    filhos do LCA
19
                    x = e.v;
                                                                    for (int j = LOG - 1; j >= 0; j--) {
                                                             5.0
2.0
                                                                        if (cima[a][j] != -1 && cima[a][j] != cima[b
                                                             51
           }
                                                                    ][j]) {
22
                                                                             a = cima[a][i];
                                                             52
                                                                             b = cima[b][j];
24 // achando caminho (se precisar)
                                                                        }
                                                            5.4
25 for (int i = 0; i < n; i++) x = pai[x];</pre>
                                                             55
                                                            56
                                                                    return cima[a][0];
27 vector < int > ciclo;
                                                            57 }
28 for (int v = x;; v = pai[v]) {
       cycle.push_back(v);
29
                                                               6.12 Lca
       if (v == x && ciclo.size() > 1) break;
```

```
1 // LCA - CP algorithm
                                                           1.4
2 // preprocessing O(NlogN)
                                                           15
                                                                  order.push_back(u);
3 // lca O(logN)
                                                           16 }
4 // Uso: criar LCA com a quantidade de vÃl'rtices (n) e 17
       lista de adjacÃłncia (adj)
                                                           18 // dfs o grafo reverso para encontrar os SCCs
_5 // chamar a fun\tilde{A}g̃ãco preprocess com a raiz da Ãarvore 19 void dfs2(int u, int c) {
                                                                  component[u] = c;
                                                           20
7 struct LCA {
                                                                  for (int v : adj_rev[u]) {
      int n, 1, timer;
                                                                      if (component[v] == -1) {
                                                           22
      vector < vector < int >> adj;
                                                           23
                                                                           dfs2(v, c);
      vector < int > tin, tout;
10
                                                           24
      vector < vector < int >> up;
                                                           25
                                                           26 }
12
      LCA(int n, const vector < vector < int >> & adj) : n(n) 27
13
      , adj(adj) {}
                                                           28 int kosaraju() {
                                                                  order.clear();
14
                                                           29
      void dfs(int v, int p) {
15
                                                           30
                                                                  fill(vis + 1, vis + N + 1, false);
          tin[v] = ++timer;
                                                                  for (int i = 1; i <= N; i++) {</pre>
16
                                                           3.1
           up[v][0] = p;
                                                                      if (!vis[i]) {
           for (int i = 1; i <= 1; ++i)
                                                                          dfs1(i);
18
                                                           3.3
               up[v][i] = up[up[v][i-1]][i-1];
                                                           34
19
                                                                  }
                                                           35
20
           for (int u : adj[v]) {
                                                           36
                                                                 fill(component + 1, component + N + 1, -1);
21
               if (u != p)
                                                           37
                                                                  int c = 0;
                   dfs(u, v);
                                                                  reverse(order.begin(), order.end());
23
                                                           38
           }
                                                           39
                                                                  for (int u : order) {
24
                                                                      if (component[u] == -1) {
2.5
                                                           40
           tout[v] = ++timer;
                                                                          dfs2(u, c++);
26
                                                           41
      }
                                                           42
                                                                  }
28
                                                           43
      bool is_ancestor(int u, int v) {
                                                                  return c;
29
                                                           44
           return tin[u] <= tin[v] && tout[u] >= tout[v 45 }
30
                                                              6.14 Pega Ciclo
31
      }
32
      int lca(int u, int v) {
33
                                                            1 // encontra um ciclo em g (direcionado ou nÃčo)
           if (is_ancestor(u, v))
3.4
                                                            2 // g[u] = vector<pair<id_aresta, vizinho>>
35
               return u;
                                                            3 // rec_arestas: true -> retorna ids das arestas do
           if (is_ancestor(v, u))
                                                                  ciclo; false -> retorna vÃľrtices do ciclo
               return v;
3.7
                                                            4 // directed: grafo direcionado?
           for (int i = 1; i >= 0; --i) {
               if (!is_ancestor(up[u][i], v))
39
                                                            6 \text{ const int } MAXN = 5 * 1e5 + 2;
                   u = up[u][i];
40
                                                            7 vector < pair < int , int >> g[MAXN];
           }
41
                                                            8 int N;
           return up[u][0];
                                                           9 bool DIRECTED = false;
42
      }
43
                                                           vector < int > color(MAXN), parent(MAXN, -1), edgein(
44
                                                                  MAXN, -1); // color: 0,1,2; edgein[v] = id da
      void preprocess(int root) {
                                                                  aresta que entra em v
          tin.resize(n);
46
                                                           int ini_ciclo = -1, fim_ciclo = -1, back_edge_id =
47
           tout.resize(n);
                                                                  -1:
           timer = 0;
48
                                                           12
           1 = ceil(log2(n));
49
                                                           13
           up.assign(n, vector<int>(1 + 1));
                                                           14 bool dfs(int u, int pai_edge){
           dfs(root, root);
5.1
                                                                  color[u] = 1; // cinza
                                                           15
52
      }
                                                                  for (auto [id, v] : g[u]) {
                                                           16
53 };
                                                                      if (!DIRECTED && id == pai_edge) continue; //
                                                           17
                                                                   ignorar aresta de volta ao pai em nÃčo-dir
  6.13 Kosaraju
                                                                      if (color[v] == 0) {
                                                           18
                                                                          parent[v] = u;
                                                           19
1 bool vis[MAXN];
                                                           20
                                                                          edgein[v] = id;
                                                                          if (dfs(v, id)) return true;
vector<int> order;
                                                           21
                                                                      } else if (color[v] == 1) {
3 int component[MAXN];
                                                           22
                                                                          // back-edge u -> v detectado
4 int N, m;
                                                           23
5 vector < int > adj [MAXN], adj_rev[MAXN];
                                                                          ini_ciclo = u;
                                                                          fim_ciclo = v;
                                                           2.5
_{7} // dfs no grafo original para obter a ordem (pÃşs-
                                                           26
                                                                           back_edge_id = id;
      order)
                                                           27
                                                                           return true:
8 void dfs1(int u) {
                                                           28
      vis[u] = true;
                                                                      // se color[v] == 2, ignora
                                                           29
      for (int v : adj[u]) {
1.0
                                                           3.0
          if (!vis[v]) {
                                                                  color[u] = 2; // preto
                                                           31
               dfs1(v);
12
                                                           32
                                                                  return false;
           }
                                                           33 }
13
```

```
}
                                                           3.3
_{35} // retorna ids das arestas do ciclo (vazio se n	ilde{	ilde{A}}čo
                                                                           }
                                                           34
                                                                      }
      hÃą)
                                                           35
36 vector<int> pega_ciclo(bool rec_arestas) {
                                                           36
      for (int u = 1; u <= N; u++) {</pre>
                                                           37 }
          if (color[u] != 0) continue;
38
                                                           38
          if (dfs(u, -1)) {
                                                           39 void add_edge(int from, int to, int capacity, int
39
               // reconstr\tilde{A}și caminho u -> ... -> v via
40
                                                                  cost){
      parent
                                                                  edges.push_back({from, to, capacity, cost, (int)
               vector < int > path;
                                                                  edges.size()});
41
                                                                  edges.push_back({to, from, 0, -cost, (int)edges.
               int cur = ini_ciclo;
42
                                                           41
               path.push_back(cur);
                                                                  size()}); // reversa
44
               while (cur != fim_ciclo) {
                                                           42 }
                   cur = parent[cur];
45
                                                           43
46
                   path.push_back(cur);
                                                           44 int min_cost_flow(int N, int K, int s, int t) {
                                                                  adj.assign(N, vector<array<int, 2>>());
47
                                                           45
               // path = [u, ..., v] -> inverter para [v 46
                                                                  for (Edge e : edges) {
        ..., u]
                                                           47
                                                                       adj[e.from].push_back({e.to, e.id});
              reverse(path.begin(), path.end());
50
               if (!rec_arestas) return path;
                                                           49
               // converte para ids das arestas: edgein[50
      node] Ãľ a aresta que entra em node
                                                                  int flow = 0;
               vector<int> edges;
                                                                  int cost = 0:
52
                                                           5.2
                                                                  vector < int > dist, edge_to;
               for (int i = 1; i < path.size(); i++)</pre>
      edges.push_back(edgein[path[i]]);
                                                                  while (flow < K) {
                                                           5.4
               // adiciona a aresta de retorno u -> v
                                                           5.5
                                                                       shortest_paths(N, s, dist, edge_to);
54
5.5
               edges.push_back(back_edge_id);
                                                           56
                                                                       if (dist[t] == INF)
               return edges;
                                                                           break:
56
                                                           5.7
          }
57
                                                           58
      }
                                                                      // find max flow on that path
5.8
                                                           5.9
59
      return {};
                                                           60
                                                                       int f = K - flow;
60 }
                                                                       int cur = t;
                                                           61
                                                                       while (cur != s) {
                                                           62
  6.15 Min Cost Max Flow
                                                                           f = min(f, edges[edge_to[cur]].capacity);
                                                                           cur = edges[edge_to[cur]].from;
                                                           64
1 // Encontra o menor custo para passar K de fluxo em
      um grafo com N vertices
_2 // Funciona com multiplas arestas para o mesmo par de ^{67}
                                                                      // apply flow
                                                                      flow += f;
                                                                      cost += f * dist[t];
_3 // Para encontrar o min cost max flow \tilde{\mathtt{Al}} s\tilde{\mathtt{A}}ş fazer K ^{69}
                                                                       cur = t;
      = infinito
                                                                       while (cur != s) {
                                                                           int edge = edge_to[cur];
                                                           72
5 struct Edge {
                                                           7.3
                                                                           int rev_edge = edge^1;
      int from, to, capacity, cost, id;
                                                           74
                                                                           edges[edge].capacity -= f;
                                                                           edges[rev_edge].capacity += f;
9 vector < vector < array < int , 2>>> adj;
10 vector<Edge> edges; // arestas pares s\tilde{\text{A}}čo as normais ^{77}
                                                                           cur = edges[edge].from;
                                                                       }
      e suas reversas sÃčo as impares
                                                           7.8
                                                           79
                                                                  }
12 const int INF = LLONG_MAX;
                                                           80
                                                                  if (flow < K)
                                                           81
14 void shortest_paths(int n, int v0, vector<int>& dist, 82
                                                                      return -1;
       vector<int>& edge_to) {
                                                           83
                                                                       return cost;
      dist.assign(n, INF);
                                                           84
1.5
                                                           85 }
      dist[v0] = 0;
16
      vector < bool > in_queue(n, false);
      queue < int > q;
                                                              7
                                                                   Primitives
18
      q.push(v0);
20
      edge_to.assign(n, -1);
                                                              8
                                                                   DP
21
22
      while (!q.empty()) {
          int u = q.front();
23
                                                              8.1
                                                                   _{
m Lis}
          q.pop();
           in_queue[u] = false;
25
           for (auto [v, id] : adj[u]) {
                                                            int lis_nlogn(vector<int> &v) {
26
                                                                  vector < int > lis;
               if (edges[id].capacity > 0 && dist[v] >
27
      dist[u] + edges[id].cost) {
                                                                  lis.push_back(v[0]);
                   dist[v] = dist[u] + edges[id].cost;
                                                                  for (int i = 1; i < v.size(); i++) {</pre>
                   edge_to[v] = id;
                                                                      if (v[i] > lis.back()) {
29
                   if (!in_queue[v]) {
                                                                           // estende a LIS
                                                                           lis.push_back(v[i]);
3.1
                        in_queue[v] = true;
                                                                      } else {
                        q.push(v);
32
```

```
1 // dp de intervalos com bitmask
               // encontra o primeiro elemento em lis
      que \tilde{A}l' >= v[i].
                                                           2 int prox(int idx) {
              // subsequÃłncia de mesmo comprimento,
                                                                  return lower_bound(S.begin(), S.end(), array<int,</pre>
10
      mas com um final menor.
                                                                   4>{S[idx][1], Oll, Oll, Oll}) - S.begin();
               auto it = lower_bound(lis.begin(), lis.
                                                           4 }
      end(), v[i]);
                                                            6 int dp[1002][(int)(111 << 10)];</pre>
               *it = v[i];
           }
1.3
                                                            8 int rec(int i, int vis) {
14
      return lis.size();
                                                                  if (i == (int)S.size()) {
15
                                                           9
16 }
                                                                      if (__builtin_popcountll(vis) == N) return 0;
                                                           10
                                                                      return LLONG_MIN;
18 // LIS NA ARVORE
                                                           12
19 const int MAXN_TREE = 100001;
                                                                  if (dp[i][vis] != -1) return dp[i][vis];
                                                           13
                                                                  int ans = rec(i + 1, vis);
20 vector < int > adj [MAXN_TREE];
                                                           14
21 int values[MAXN_TREE];
                                                                  ans = max(ans, rec(prox(i), vis | (111 << S[i
                                                           15
22 int ans = 0;
                                                                  ][3])) + S[i][2]);
                                                                  return dp[i][vis] = ans;
23
                                                           16
25 void dfs(int u, int p, vector<int>& tails) {
      auto it = lower_bound(tails.begin(), tails.end(), 8.4 Lcs
26
       values[u]);
      int prev = -1;
                                                           string s1, s2;
      bool coloquei = false;
                                                           1 int dp [1001] [1001];
      if (it == tails.end()) {
29
           tails.push_back(values[u]);
3.0
                                                           4 int lcs(int i, int j) {
31
           coloquei = true;
                                                                 if (i < 0 || j < 0) return 0;
      } else {
32
                                                                  if (dp[i][j] != -1) return dp[i][j];
          prev = *it;
                                                                  if (s1[i] == s2[j]) {
                                                           7
           *it = values[u];
3.4
                                                                      return dp[i][j] = 1 + lcs(i - 1, j - 1);
35
                                                                  } else {
                                                           9
      ans = max(ans, (int)tails.size());
36
                                                                      return dp[i][j] = max(lcs(i - 1, j), lcs(i, j
                                                           10
      for (int v : adj[u]) {
37
                                                                   - 1));
           if (v != p) {
                                                           11
               dfs(v, u, tails);
39
                                                           12 }
40
4.1
                                                                   Digit
                                                              8.5
      if (coloquei) {
42
          tails.pop_back();
43
                                                           vector < int > digits;
      } else {
44
          *it = prev;
45
                                                           3 int dp[20][10][2][2];
46
47 }
                                                            5 int rec(int i, int last, int flag, int started) {
                                                                  if (i == (int)digits.size()) return 1;
       Edit Distance
                                                                  if (dp[i][last][flag][started] != -1) return dp[i
                                                                  [last][flag][started];
       vector<vector<int>> dp(n+1, vector<int>(m+1, LINF _8
1
                                                                  int lim;
                                                                  if (flag) lim = 9;
                                                                  else lim = digits[i];
                                                           10
      for(int j = 0; j <= m; j++) {</pre>
                                                                  int ans = 0;
           dp[0][j] = j;
                                                                  for (int d = 0; d <= lim; d++) {</pre>
                                                           12
                                                           13
                                                                      if (started && d == last) continue;
                                                                      int new_flag = flag;
                                                           14
      for(int i = 0; i <= n; i++) {</pre>
                                                                      int new_started = started;
                                                           15
          dp[i][0] = i;
                                                                      if (d > 0) new_started = 1;
                                                           16
9
                                                                      if (!flag && d < lim) new_flag = 1;</pre>
                                                           1.7
10
                                                                      ans += rec(i + 1, d, new_flag, new_started);
                                                           18
      for(int i = 1; i <= n; i++) {</pre>
                                                                  }
                                                           19
           for(int j = 1; j <= m; j++) {</pre>
12
                                                                  return dp[i][last][flag][started] = ans;
                                                           20
               if(a[i-1] == b[j-1]) {
13
                   dp[i][j] = dp[i-1][j-1];
14
15
                                                                   Knapsack
                   dp[i][j] = min({dp[i-1][j] + 1, dp[i]}
      [j-1] + 1, dp[i-1][j-1] + 1);
                                                            1 // dp[i][j] => i-esimo item com j-carga sobrando na
           }
18
                                                            2 // O(N * W)
19
20
                                                            4 for(int j = 0; j < MAXN; j++) {
       cout << dp[n][m];
                                                                  dp[0][j] = 0;
                                                           5
                                                            6 }
       \mathbf{Bitmask}
  8.3
                                                            7 for(int i = 1; i <= N; i++) {</pre>
                                                                  for(int j = 0; j <= W; j++) {</pre>
```

```
if(items[i].first > j) {
                                                                   for (int j = 0; j < comb.size(); j++) {</pre>
10
              dp[i][j] = dp[i-1][j];
                                                          9
                                                                        cout << comb[j] << ' ';
11
                                                         10
                                                                    cout << '\n';
          else {
12
              dp[i][j] = max(dp[i-1][j], dp[i-1][j-
                                                                    return:
      items[i].first] + items[i].second);
                                                         13
                                                                if (i == N) return;
                                                         14
                                                                int r = N - i;
1.5
                                                         1.5
16 }
                                                                int preciso = K - comb.size();
                                                         16
                                                                if (r < preciso) return;</pre>
                                                         17
  8.7 Lis Seg
                                                                comb.push_back(elements[i]);
                                                         18
                                                         19
                                                                brute_choose(i + 1);
                                                         20
                                                                comb pop_back();
      vector < int > a(n);
                                                                brute_choose(i + 1);
                                                         21
      for (int i = 0; i < n; i++) cin >> a[i];
                                                        22 }
      vector<int> sorted_a = a;
      sort(sorted_a.begin(), sorted_a.end());
                                                            9.2 Struct
      for (int i = 0; i < n; i++) {</pre>
          a[i] = lower_bound(sorted_a.begin(), sorted_a
      .end(), a[i]) - sorted_a.begin();
                                                          1 struct Pessoa{
                                                              // Atributos
      SegTreeMx segmx;
                                                               string nome;
      segmx.build(n);
                                                                int idade;
      vector < int > dp(n, 1);
      for (int k = 0; k < n; k++) {</pre>
11
                                                                // Comparador
          if (a[k] > 0) {
                                                               bool operator < (const Pessoa& other) const{
              dp[k] = segmx.query(0, a[k] - 1) + 1;
13
                                                                   if(idade != other.idade) return idade > other
                                                                .idade;
          segmx.update(a[k], dp[k]);
                                                                    else return nome > other.nome;
      }
16
      cout << *max_element(dp.begin(), dp.end()) << '\n 11 }</pre>
                                                            9.3 Bitwise
  8.8 Disjoint Blocks
                                                          int check_kth_bit(int x, int k) {
```

```
1 // NÞmero mÃąximo de subarrays disjuntos com soma x
      usando apenas
2 // prefixo atÃľ i (ou seja, considerando prefixo a
      [1..i]).
3 int disjointSumX(vector<int> &a, int x) {
      int n = a.size();
      map <int, int> best; // best[pref] = melhor dp
      visto para esse pref
      best[0] = 0;
      int pref = 0;
      vector < int > dp(n + 1, 0); // dp[0] = 0
      for (int i = 1; i <= n; i++) {
          pref += a[i - 1];
10
          // nÃčo pegar subarray terminando em i
          dp[i] = dp[i-1];
          // pega se existir prefixo anterior e
13
      atualiza best
          auto it = best.find(pref - x);
14
          if (it != best.end()) {
              dp[i] = max(dp[i], it->second + 1);
16
          best[pref] = max(best[pref], dp[i]);
1.8
19
      return dp[n];
20
21 }
```

9 General

9.1 Brute Choose

```
1 vector < int > elements;
2 int N, K;
3 vector < int > comb;
4
5
6 void brute_choose(int i) {
7    if (comb.size() == K) {
```

```
2 return (x >> k) & 1;
 5 void print_on_bits(int x) {
 6 for (int k = 0; k < 32; k++) {</pre>
     if (check_kth_bit(x, k)) {
         cout << k << ' ';
10 }
11
     cout << '\n';
12 }
14 int count_on_bits(int x) {
int ans = 0;
16 for (int k = 0; k < 32; k++) {
     if (check_kth_bit(x, k)) {
17
18
         ans++;
       }
19
20 }
21
    return ans;
22 }
24 bool is_even(int x) {
return ((x & 1) == 0);
26 }
27
28 int set_kth_bit(int x, int k) {
    return x | (1 << k);
29
30 }
3.1
32 int unset_kth_bit(int x, int k) {
33
    return x & (~(1 << k));
34 }
36 int toggle_kth_bit(int x, int k) {
    return x ^ (1 << k);
38 }
39
```

```
40 bool check_power_of_2(int x) {
return count_on_bits(x) == 1;
```

Geometry 10

Convex Hull 10.1

```
1 #include <bits/stdc++.h>
3 using namespace std;
 4 #define int long long
5 typedef int cod;
7 struct point
8 {
       cod x,y;
       point(cod x = 0, cod y = 0): x(x), y(y)
1.0
       {}
12
       double modulo()
13
14
15
           return sqrt(x*x + y*y);
16
1.7
       point operator+(point o)
18
19
           return point(x+o.x, y+o.y);
20
21
       }
22
       point operator - (point o)
23
            return point(x - o.x , y - o.y);
24
25
       point operator*(cod t)
27
           return point(x*t, y*t);
29
       point operator/(cod t)
30
31
           return point(x/t, y/t);
32
34
       cod operator*(point o)
35
36
37
           return x*o.x + y*o.y;
       }
       cod operator^(point o)
39
40
41
           return x*o.y - y * o.x;
       }
42
       bool operator < (point o)</pre>
43
44
            if( x != o.x) return x < o.x;</pre>
45
46
           return y < o.y;</pre>
47
49 };
50
51 int ccw(point p1, point p2, point p3)
52 {
       cod cross = (p2-p1) ^ (p3-p1);
53
       if(cross == 0) return 0;
54
55
       else if(cross < 0) return -1;</pre>
56
       else return 1;
57 }
59 vector <point> convex_hull(vector<point> p)
60 {
       sort(p.begin(), p.end());
6.1
       vector < point > L,U;
62
       //Lower
64
```

```
for(auto pp : p)
6.5
66
            while(L.size() >= 2 and ccw(L[L.size() - 2],
67
       L.back(), pp) == -1)
68
                // Ãľ -1 pq eu nÃčo quero excluir os
        colineares
                L.pop_back();
71
            L.push_back(pp);
73
74
75
       reverse(p.begin(), p.end());
76
7.7
        //Upper
78
        for(auto pp : p)
79
            while(U.size() >= 2 and ccw(U[U.size()-2], U
80
        .back(), pp) == -1)
8.1
            {
                U.pop_back();
82
83
            U.push_back(pp);
84
85
86
87
       L.pop_back();
       L.insert(L.end(), U.begin(), U.end()-1);
88
        return L;
89
90 }
9.1
92 cod area(vector<point> v)
93 {
        int ans = 0;
94
95
       int aux = (int)v.size();
       for(int i = 2; i < aux; i++)</pre>
96
97
            ans += ((v[i] - v[0])^(v[i-1] - v[0]))/2;
9.8
99
100
       ans = abs(ans);
       return ans;
102 }
103
104 int bound(point p1 , point p2)
105 {
        return __gcd(abs(p1.x-p2.x), abs(p1.y-p2.y));
106
107 }
108 //teorema de pick [pontos = A - (bound+points)/2 + 1]
110 int32_t main()
111 {
112
        int n;
113
        cin >> n;
114
115
116
       vector < point > v(n);
       for(int i = 0; i < n; i++)</pre>
118
            cin >> v[i].x >> v[i].y;
119
120
121
122
       vector <point> ch = convex_hull(v);
123
        cout << ch.size() << '\n';
124
        for(auto p : ch) cout << p.x << " " << p.y << " \n
        return 0;
127
128 }
```

10.2 Inside Polygon

1 // Convex O(logn)

10.3 Point Location

```
3 bool insideT(point a, point b, point c, point e){
       int x = ccw(a, b, e);
                                                             2 int32_t main(){
4
       int y = ccw(b, c, e);
5
                                                                   sws;
       int z = ccw(c, a, e);
       return ! ((x==1 \text{ or } y==1 \text{ or } z==1) and (x==-1 \text{ or } y
                                                                  int t; cin >> t;
      ==-1 \text{ or } z==-1));
                                                                   while(t - -) {
g
10 bool inside(vp &p, point e){ // ccw
                                                                        int x1, y1, x2, y2, x3, y3; cin >> x1 >> y1
      int 1=2, r=(int)p.size()-1;
                                                                   >> x2 >> y2 >> x3 >> y3;
       while(1<r){
12
                                                             10
13
           int mid = (1+r)/2;
                                                                        int deltax1 = (x1-x2), deltay1 = (y1-y2);
14
           if(ccw(p[0], p[mid], e) == 1)
                                                             12
               l = mid + 1;
                                                                        int compx = (x1-x3), compy = (y1-y3);
15
                                                             13
           else{
16
                                                            14
               r = mid;
                                                                        int ans = (deltax1*compy) - (compx*deltay1);
17
                                                             15
18
           }
                                                                        if(ans == 0){cout << "TOUCH\n"; continue;}</pre>
19
                                                                        if(ans < 0){cout << "RIGHT\n"; continue;}</pre>
      // bordo
      // if(r==(int)p.size()-1 and ccw(p[0], p[r], e)
                                                                        if(ans > 0){cout << "LEFT\n"; continue;}</pre>
21
                                                            19
                                                                   }
       ==0) return false;
                                                            20
       // if(r==2 and ccw(p[0], p[1], e)==0) return
                                                            21
                                                                   return 0;
       false:
                                                            22 }
       // if(ccw(p[r], p[r-1], e) == 0) return false;
23
       return insideT(p[0], p[r-1], p[r], e);
                                                               10.4 Lattice Points
24
25 }
26
                                                             1 ll gcd(ll a, ll b) {
27
                                                                   return b == 0 ? a : gcd(b, a % b);
                                                             2
28 // Any O(n)
                                                             3 }
29
                                                             4 ll area_triangulo(11 x1, 11 y1, 11 x2, 11 y2, 11 x3,
30 int inside(vp &p, point pp){
                                                                   11 y3) {
      // 1 - inside / 0 - boundary / -1 - outside
3.1
                                                                   return abs(x1 * (y2 - y3) + x2 * (y3 - y1) + x3 *
       int n = p.size();
32
                                                                    (y1 - y2));
       for (int i=0; i < n; i++) {</pre>
                                                             6 }
           int j = (i+1)%n;
34
                                                             7 ll pontos_borda(ll x1, ll y1, ll x2, ll y2) {
           if(line({p[i], p[j]}).inside_seg(pp))
                                                                   return gcd(abs(x2 - x1), abs(y2 - y1));
                                                             8
36
               return 0:
                                                             9 }
37
                                                            10
       int inter = 0;
                                                             11 int32_t main() {
       for (int i = 0; i < n; i + +) {</pre>
39
                                                                   ll x1, y1, x2, y2, x3, y3;
                                                            12
40
           int j = (i+1)%n;
                                                                   cin >> x1 >> y1;
                                                             13
           if(p[i].x \le pp.x and pp.x \le p[j].x and ccw(p)
41
                                                                   cin >> x2 >> y2;
       [i], p[j], pp)==1)
                                                                   cin >> x3 >> y3;
                                                             15
42
               inter++; // up
                                                                   11 area = area_triangulo(x1, y1, x2, y2, x3, y3);
           else if(p[j].x \le pp.x and pp.x \le p[i].x and ^{16}
43
                                                                   11 tot_borda = pontos_borda(x1, y1, x2, y2) +
                                                            17
       ccw(p[i], p[j], pp)==-1)
                                                                   pontos_borda(x2, y2, x3, y3) + pontos_borda(x3,
               inter++; // down
44
                                                                   y3, x1, y1);
                                                            18
46
                                                                   11 ans = (area - tot_borda) / 2 + 1;
                                                            19
       if(inter%2==0) return -1; // outside
47
                                                                   cout << ans << endl;</pre>
                                                            20
       else return 1; // inside
                                                            21
49 }
                                                                   return 0:
                                                            22
                                                            23 }
```