Machine Learning Engineer Nanodegree Udacity

Capstone Project

Report

Ognian Dantchev

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1. Definition

Project Overview

Time series forecasting is applied when scientific predictions are needed based on historical data with time component. Time series forecasting has many applications in various industries. Companies use everything from simple spreadsheets to complex financial planning software in an attempt to accurately forecast future business outcomes such as product demand, resource needs, crops yield, traffic or financial performance. Beyond business, applications include healthcare, medical, environmental studies, social studies and other forecasting.

There are many classical time series forecasting methods, based on autoregressive (AR) models, exponential smoothing, Fourier Transform, etc.

Models based on Neural Networks are able to handle more complex nonlinear patterns. They have less restrictions and make less assumptions; have high predictive power and can be easily automated. Their cons – they require more data; can be more difficult to interpret, and it is more difficult to derive confidence intervals for the forecast.

In this project, three different Neural Networks were implemented for time series forecasting. A Recurrent Neural Network (RNN) with Gated Recurrent Unit (GRU) from the Keras API, as described in the TensorFlow Tutorials in [1]. Second is a Dilated Causal CNN, I implemented in the past in [2] and as originally described in [6] by Aaron van den Oord, Sander Dieleman et al. Both 1st and 2nd models use Keras and TensorFlow 2.5. The third model implemented is based on the DeepAR+ algorithm of Amazon Forecast by AWS.

Problem Statement

The purpose of this project is to implement model based on the DeepAR+ algorithm by Amazon and deploy it to AWS. As a secondary target, I try to compare the results to other NN models for

time series. Own dataset with 45 years of local meteorology data was used, but no meteorology domain claims whatsoever.

The implementation was split into 5 smaller Jupyter Notebooks:

- 1. Generate and download the raw dataset at https://www.ncdc.noaa.gov/. Data import and exploration; Changing some of the labels using the Inventory file. Data cleaning and preprocessing; Feature engineering and data transformation add day-of-year (between 1 and 366) and the hour-of-day (between 0 and 23); Save the clean data in compact new format for use in next notebooks.
- 2. Split the data into training, validation, and testing sets; Define and train a Gated Recurrent Unit (GRU) RNN Model.
- 3. Split the data into training, validation, and testing sets; Define and train a Dilated Causal CNN Model. (model and model2 are the same, but use different way of building with Keras functional API as an experiment).
- 4. Connect AWS API session, create IAM role for Amazon Forecast, create S3 bucket; upload the dataset to AWS S3 bucket; Define and train a model from AWS Amazon Forecast Amazon DeepAR+ algorithm. I deviated from the original plan to use the open-source Gluon Time Series (GluonTS) toolkit by AWS Labs, in favor of the Amazon DeepAR+ algorithm, as it is state-of-the-art and used by amazon.com; Deployed the later model to AWS.
- 5. Discussion, TODO, Cleanup of AWS resources and References. Evaluate and compare the models, to the extend possible.

Metrics

Common metrics for Time Series Analysis are Mean Absolute Error (MAE), Mean Squared Error (MSE), Mean Absolute Percentage Error (MAPE), Weighted Average Percentage Error (WAPE, also referred to as the MAD/Mean ratio.

$$MSE = \sum_{j=0}^{n} (y_i - \widehat{y}_i)$$

Mean Squared Error (MSE) will be used as the loss-function that will be minimized and used as a metric. This measures how closely the model's output matches the true output signals.

At the beginning of a sequence, the model has only seen input-signals for a few time-steps, so its generated output may be very inaccurate. Therefore, the model will be given a "warmup-period" of 50 time-steps where we don't use its accuracy in the loss-function, in hope of improving the accuracy for later time-steps, see [1]

Amazon Forecast DeepAR+ uses RMSE and WAPE metrics, RMSD Wikipedia article

I'm using this relation to compare the metrics for the Dilated Causal CNN and the Amazon DeepAR+ model: $RMSE = \sqrt{MSE}$

The re-sampled data will be used to create "future" period by shifting the target-data.

2. Analysis

Data Exploration

Here's the sequence to acquire, clean and reshape the data:

- * generate the raw data set at https://www.ncdc.noaa.gov/
 (https://www7.ncdc.noaa.gov/CDO/cdoselect.cmd the old data request form)
- * review the original dataset files
- * resample data and helper functions z
- * remove data (where gaps are too big)
- * add data (linearly interpolated from the neighboring values)
- * save the clean, resampled data to a binary file.

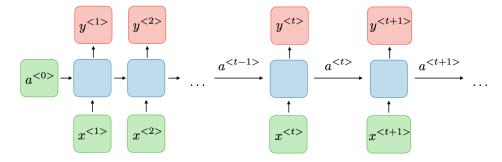
This was done in Jupyter notebook 01, and then the clean data was saved in Python standard binary file format.

The raw dataset was uploaded in ZIP to GitHub, for review, at the project proposal stage: https://github.com/ogniandantchev/ML_engineer_nd009_capstone

Algorithms and APIs

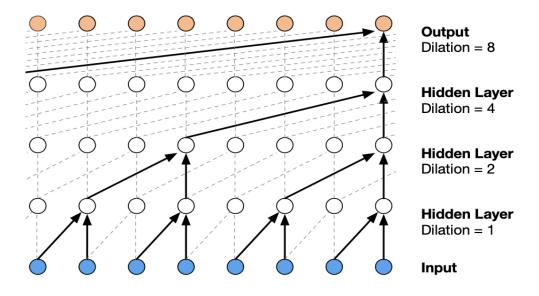
Recurrent neural networks (RNN) are a class of neural networks that is powerful for modeling sequence data such as time series or natural language. The 1st model will be based RNN with Gated Recurrent Unit (GRU). The 2nd one, I used in the past in [2], will be based on Dilated Causal CNN, often used for audio processing [6].

Here's a typical diagram of RNNs (from Stanford CS 230):



RNN

Here's a diagram of a Dilated Causal CNN, from the original WaveNet article [6]:

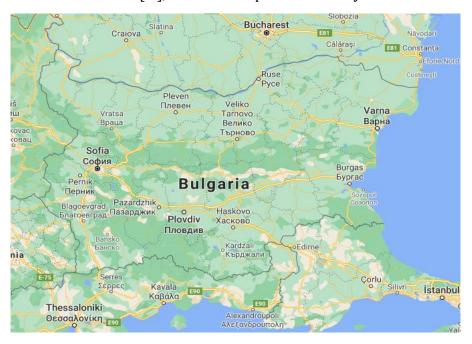


Dilated Causal CNN

3. Methodology

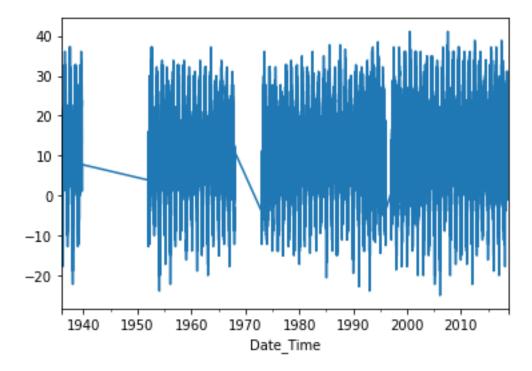
Data Preprocessing

Weather data for the period 1936-2018 will be used for four cities in Bulgaria – Ruse, Sofia, Varna and Veliko Tarnovo. After struggling with the format of some of the local sources, I found that the National Centers for Environmental Information of the National Oceanic and Atmospheric Administration https://www.ncei.noaa.gov/ provide an access to a global source of climatic data. It was also used in [1], and one can pick almost any location in the world.



Bulgaria Map

Since weather data is most diligently collected at airports, cities are encoded with their USAF codes. A function to convert these codes to names was prepared, as well as one that converts deg F to deg C.



Sofia Temperature, 1936 to 2018

There are some gaps in the data, so I removed some period, and at the end I only use 1973 to 2018 – i.e. 45 years of data vs the original 82 years, but still more than enough. Removed 2 of the cities with bigger gaps, so only Sofia and Varna time series left in the clean dataset. After that, the series were re-sampled, so an hourly frequency can be used for the entire period (data was collected only 2 times a day in the 1930ies, then 3 times, then 6, and currently more than 24 times).

Implementation

The Keras API and TensorFlow 2.5 was used to create the first 2 models, notebooks 02 and 03.

Gated Recurrent Unit (GRU) RNN Model Implementation

Loss function calculates MSE, but after ignoring some "warmup" part of the sequences:

```
warmup_steps = 50
```

Later on these are visualized in gray in the Forecast plots.

model.summary()

Model: "sequential"

Layer (type)	Output Shape	Param #	
gru (GRU)	(None, None, 512)	798720	
dense (Dense)	(None, None, 1)	513	

Total params: 799,233 Trainable params: 799,233 Non-trainable params: 0

Dilated Causal CNN Model Implementation

```
# Keras Sequential definition -- var model2
p='causal'
# this only works in TF 1.12+ -- December 2018+
# 2021: works with TensorFlow 2.5 too
model2 = Sequential([
    Conv1D(filters=32, input_shape=( None, num_x_signals ),
           kernel size=2, padding='causal', dilation rate=1),
    Conv1D(filters=32, kernel_size=2, padding=p, dilation_rate=2),
    Conv1D(filters=32, kernel_size=2, padding=p, dilation_rate=4),
    Conv1D(filters=32, kernel size=2, padding=p, dilation rate=8),
    Conv1D(filters=32, kernel_size=2, padding=p, dilation_rate=16),
    Conv1D(filters=32, kernel_size=2, padding=p, dilation_rate=32),
    Conv1D(filters=32, kernel_size=2, padding=p, dilation_rate=64),
    Conv1D(filters=32, kernel_size=2, padding=p, dilation_rate=128),
    Dense(128, activation=tf.nn.relu),
    Dropout(.2),
    Dense(1, activation="tanh")
])
model2.compile(Adam(), loss='mean absolute error')
Using Standard MSE as loss here loss='mean absolute error'.
```

model2.summary()

Model: "sequential_1"

Output Shape	Param #
(None, None, 32)	416
(None, None, 32)	2080
(None, None, 128)	4224
(None, None, 128)	0
(None, None, 1)	129
	(None, None, 32) (None, None, 128)

Total params: 19,329 Trainable params: 19,329 Non-trainable params: 0 Similarly, to the scheme above, most of the work is in preparing the dataset (one time series here) in the Amazon Forecast specific format, copy to the newly created S3 bucket and import to AWS Forecast. Here's the import result at the end:

```
forecast.describe_dataset_import_job(DatasetImportJobArn=ts_dataset_import_job_arn)
```

```
{'DatasetImportJobName': 'sof temperature forecast 1',
 'DatasetImportJobArn': 'arn:aws:forecast:eu-central-1:574930355514:dataset-import-
job/sof_temperature_forecast_1/sof_temperature_forecast_1',
 'DatasetArn': 'arn:aws:forecast:eu-central-
1:574930355514:dataset/sof temperature forecast 1',
 'TimestampFormat': 'yyyy-MM-dd hh:mm:ss',
 'UseGeolocationForTimeZone': False,
 'DataSource': {'S3Config': {'Path': 's3://forecast-test-0/t1.csv',
   'RoleArn': 'arn:aws:iam::574930355514:role/ForecastNotebookRole-Basic'}},
 'FieldStatistics': {'item_id': {'Count': 401784,
   'CountDistinct': 1,
   'CountNull': 0,
   'CountLong': 401784,
   'CountDistinctLong': 1,
   'CountNullLong': 0},
  'target_value': {'Count': 401784,
   'CountDistinct': 12756,
   'CountNull': 0,
   'CountNan': 0,
   'Min': '-25.0', 'Max': '41.11',
   'Avg': 10.1715268852146,
   'Stddev': 9.428677566143127,
   'CountLong': 401784,
   'CountDistinctLong': 12756,
   'CountNullLong': 0,
   'CountNanLong': 0},
  'timestamp': {'Count': 401784,
   'CountDistinct': 401784,
   'CountNull': 0,
   'Min': '1973-01-01T00:00:00Z',
   'Max': '2018-11-01T23:00:00Z',
   'CountLong': 401784,
   'CountDistinctLong': 401784,
   'CountNullLong': 0}},
 'DataSize': 0.012740140780806541,
 'Status': 'ACTIVE',
 'CreationTime': datetime.datetime(2021, 7, 29, 15, 58, 11, 748000,
tzinfo=tzlocal()),
 'LastModificationTime': datetime.datetime(2021, 7, 29, 16, 6, 20, 94000,
tzinfo=tzlocal()),
 'ResponseMetadata': {'RequestId': 'd73cb6b2-1910-4a59-b0ee-27c2667f66e7',
  'HTTPStatusCode': 200,
  'HTTPHeaders': {'content-type': 'application/x-amz-json-1.1',
   'date': 'Thu, 29 Jul 2021 13:06:35 GMT',
   'x-amzn-requestid': 'd73cb6b2-1910-4a59-b0ee-27c2667f66e7',
   'content-length': '1182',
```

```
'connection': 'keep-alive'},
  'RetryAttempts': 0}}
Then creating the model:
create_predictor_response = \
    forecast.create_predictor(PredictorName=predictor_name_deep_ar,
                              AlgorithmArn=algorithm arn deep ar plus,
                              ForecastHorizon=FORECAST LENGTH,
                              PerformAutoML=False,
                              PerformHPO=False,
                              InputDataConfig= {"DatasetGroupArn":
dataset_group_arn},
                              FeaturizationConfig= {"ForecastFrequency":
DATASET FREQUENCY }
                             )
forecast.describe_predictor(PredictorArn=predictor_arn_deep_ar)
{'PredictorArn': 'arn:aws:forecast:eu-central-
1:574930355514:predictor/sof temperature forecast 1 deep ar plus',
 'PredictorName': 'sof temperature forecast 1 deep ar plus',
 'AlgorithmArn': 'arn:aws:forecast:::algorithm/Deep_AR_Plus',
 'ForecastHorizon': 72,
 'ForecastTypes': ['0.1', '0.5', '0.9'],
 'PerformAutoML': False,
 'PerformHPO': False,
 'TrainingParameters': {'context length': '144',
  'epochs': '500',
  'learning_rate': '1E-3',
  'learning_rate_decay': '0.5',
  'likelihood': 'student-t',
  'max_learning_rate_decays': '0',
  'num_averaged_models': '1',
  'num_cells': '40',
  'num_layers': '2',
  'prediction length': '72'},
 'EvaluationParameters': {'NumberOfBacktestWindows': 1,
  'BackTestWindowOffset': 72},
 'InputDataConfig': {'DatasetGroupArn': 'arn:aws:forecast:eu-central-
1:574930355514:dataset-group/sof_temperature_forecast_1'},
 'FeaturizationConfig': {'ForecastFrequency': 'H',
  'Featurizations': [{'AttributeName': 'target value',
    'FeaturizationPipeline': [{'FeaturizationMethodName': 'filling',
      'FeaturizationMethodParameters': {'aggregation': 'sum',
       'backfill': 'zero',
       'frontfill': 'none',
       'middlefill': 'zero'}}]}]},
 'PredictorExecutionDetails': {'PredictorExecutions': [{'AlgorithmArn':
'arn:aws:forecast:::algorithm/Deep_AR_Plus',
    'TestWindows': [{'TestWindowStart': datetime.datetime(2018, 10, 30, 2, 0,
tzinfo=tzlocal()),
      'TestWindowEnd': datetime.datetime(2018, 11, 2, 2, 0, tzinfo=tzlocal()),
      'Status': 'ACTIVE'}]}]},
 'DatasetImportJobArns': ['arn:aws:forecast:eu-central-1:574930355514:dataset-
import-job/sof_temperature_forecast_1/sof_temperature_forecast_1'],
 'AutoMLAlgorithmArns': ['arn:aws:forecast:::algorithm/Deep_AR_Plus'],
 'Status': 'ACTIVE',
 'CreationTime': datetime.datetime(2021, 7, 29, 16, 9, 7, 637000,
tzinfo=tzlocal()),
```

```
'LastModificationTime': datetime.datetime(2021, 7, 29, 18, 39, 4, 691000,
tzinfo=tzlocal()),
 'ResponseMetadata': {'RequestId': 'c7dc6e9e-e288-4c08-8be5-b8e73d73df2e',
  'HTTPStatusCode': 200,
  'HTTPHeaders': {'content-type': 'application/x-amz-json-1.1',
   'date': 'Thu, 29 Jul 2021 18:51:42 GMT',
   'x-amzn-requestid': 'c7dc6e9e-e288-4c08-8be5-b8e73d73df2e',
   'content-length': '1567',
   'connection': 'keep-alive'},
  'RetryAttempts': 0}}
Creating forecast
forecast.describe forecast(ForecastArn=forecast arn deep ar)
{'ForecastArn': 'arn:aws:forecast:eu-central-
1:574930355514:forecast/sof temperature forecast 1 deep ar plus',
 'ForecastName': 'sof_temperature_forecast_1_deep_ar_plus',
 'ForecastTypes': ['0.1', '0.5', '0.9'],
 'PredictorArn': 'arn:aws:forecast:eu-central-
1:574930355514:predictor/sof temperature forecast 1 deep ar plus',
 'DatasetGroupArn': 'arn:aws:forecast:eu-central-1:574930355514:dataset-
group/sof_temperature_forecast_1',
 'Status': 'ACTIVE',
 'CreationTime': datetime.datetime(2021, 7, 29, 21, 57, 48, 160000,
tzinfo=tzlocal()),
 'LastModificationTime': datetime.datetime(2021, 7, 29, 22, 14, 22, 326000,
tzinfo=tzlocal()),
 'ResponseMetadata': {'RequestId': '9b374fe8-d03e-462a-a382-a0f18533c4d8',
  'HTTPStatusCode': 200,
  'HTTPHeaders': {'content-type': 'application/x-amz-json-1.1',
   'date': 'Thu, 29 Jul 2021 19:15:04 GMT',
   'x-amzn-requestid': '9b374fe8-d03e-462a-a382-a0f18533c4d8',
   'content-length': '505',
   'connection': 'keep-alive'},
  'RetryAttempts': 0}}
```

4. Results

Model Evaluation and Validation

The training results, times, and the forecast plots are as follows:

Recurrent Neural Network with GRU:

```
Epoch 00003: val loss improved from 0.00839 to 0.00464, saving model to
02 checkpoint.keras
Epoch 4/20
100/100 [============ ] - 60s 597ms/step - loss: 0.0056 -
val loss: 0.0060
Epoch 00004: val loss did not improve from 0.00464
Epoch 00004: ReduceLROnPlateau reducing learning rate to 0.00010000000474974513.
Epoch 5/20
100/100 [=============== ] - 60s 598ms/step - loss: 0.0041 -
val loss: 0.0038
Epoch 00005: val loss improved from 0.00464 to 0.00380, saving model to
02 checkpoint.keras
Epoch 6/20
100/100 [================ ] - 60s 597ms/step - loss: 0.0039 -
val loss: 0.0039
Epoch 00006: val loss did not improve from 0.00380
Epoch 00006: ReduceLROnPlateau reducing learning rate to 0.0001.
Epoch 7/20
100/100 [=============== ] - 60s 596ms/step - loss: 0.0039 -
val loss: 0.0038
Epoch 00007: val loss did not improve from 0.00380
Epoch 8/20
100/100 [============ ] - 60s 596ms/step - loss: 0.0039 -
val loss: 0.0038
Epoch 00008: val_loss improved from 0.00380 to 0.00378, saving model to
02 checkpoint.keras
Epoch 9/20
val loss: 0.0037
Epoch 00009: val_loss improved from 0.00378 to 0.00375, saving model to
02_checkpoint.keras
Epoch 10/20
100/100 [============= ] - 60s 597ms/step - loss: 0.0038 -
val loss: 0.0040
Epoch 00010: val loss did not improve from 0.00375
Epoch 11/20
100/100 [=============== ] - 60s 597ms/step - loss: 0.0038 -
val_loss: 0.0037
Epoch 00011: val_loss improved from 0.00375 to 0.00374, saving model to
02 checkpoint.keras
Epoch 12/20
100/100 [================ ] - 60s 598ms/step - loss: 0.0038 -
val loss: 0.0037
Epoch 00012: val_loss improved from 0.00374 to 0.00370, saving model to
02_checkpoint.keras
Epoch 13/20
100/100 [================= ] - 60s 598ms/step - loss: 0.0037 -
```

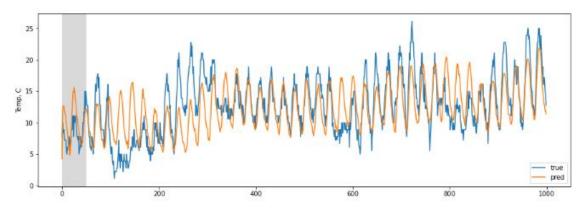
val loss: 0.0038

```
Epoch 00013: val loss did not improve from 0.00370
Epoch 14/20
100/100 [================ ] - 60s 599ms/step - loss: 0.0038 -
val_loss: 0.0037
Epoch 00014: val_loss did not improve from 0.00370
Epoch 15/20
100/100 [=============== ] - 60s 598ms/step - loss: 0.0037 -
val loss: 0.0036
Epoch 00015: val_loss improved from 0.00370 to 0.00363, saving model to
02 checkpoint.keras
Epoch 16/20
100/100 [=============== ] - 60s 598ms/step - loss: 0.0037 -
val loss: 0.0038
Epoch 00016: val_loss did not improve from 0.00363
Epoch 17/20
100/100 [=============== ] - 60s 598ms/step - loss: 0.0037 -
val loss: 0.0037
Epoch 00017: val loss did not improve from 0.00363
Epoch 18/20
100/100 [================ ] - 60s 599ms/step - loss: 0.0037 -
val_loss: 0.0038
```

Epoch 00018: val_loss did not improve from 0.00363

Epoch 00018: early stopping

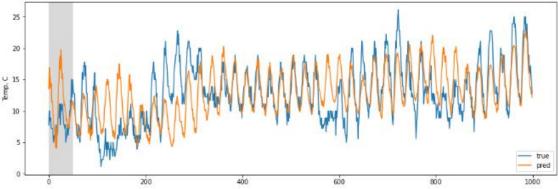
Wall time: 17min 54s



Gated Recurrent Unit (GRU) RNN Model forecast

Dilated Causal Convolutional Neural Network

```
Epoch 5/10
100/100 [================= ] - 18s 177ms/step - loss: 0.0542 -
val loss: 0.0482
Epoch 6/10
100/100 [=============== ] - 18s 178ms/step - loss: 0.0536 -
val loss: 0.0480
Epoch 7/10
100/100 [=============== ] - 18s 178ms/step - loss: 0.0533 -
val loss: 0.0490
Epoch 8/10
100/100 [================ ] - 18s 178ms/step - loss: 0.0528 -
val loss: 0.0479
Epoch 9/10
100/100 [================ ] - 18s 178ms/step - loss: 0.0523 -
val_loss: 0.0478
Epoch 10/10
100/100 [================ ] - 18s 179ms/step - loss: 0.0520 -
val loss: 0.0479
Wall time: 3min 1s
 25
```

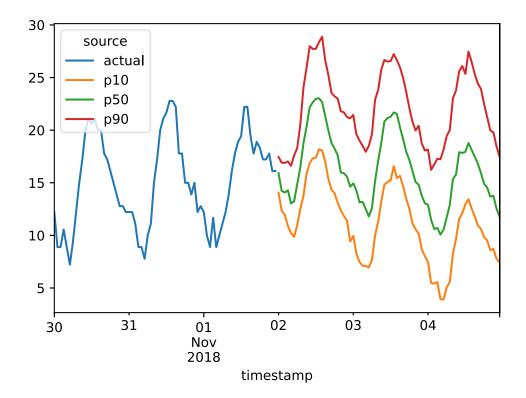


Dilated Causal CNN Model forecast

```
see describe_predictor above. here's the result of forecast.get_accuracy_metrics:
```

```
{'PredictorEvaluationResults': [{'AlgorithmArn':
'arn:aws:forecast:::algorithm/Deep AR Plus',
   'TestWindows': [{'EvaluationType': 'SUMMARY',
     'Metrics': {'RMSE': 2.8056032983401455,
      'WeightedQuantileLosses': [{'Quantile': 0.9,
        'LossValue': 0.0640613829623758},
       {'Quantile': 0.5, 'LossValue': 0.13991594321957088}, {'Quantile': 0.1, 'LossValue': 0.10678413658910633}],
      'ErrorMetrics': [{'ForecastType': 'mean',
        'WAPE': 0.14845030024660774,
        'RMSE': 2.8056032983401455}]}},
    {'TestWindowStart': datetime.datetime(2018, 10, 30, 2, 0, tzinfo=tzlocal()),
     'TestWindowEnd': datetime.datetime(2018, 11, 2, 2, 0, tzinfo=tzlocal()),
     'ItemCount': 1,
     'EvaluationType': 'COMPUTED',
     'Metrics': {'RMSE': 2.8056032983401455,
      'WeightedQuantileLosses': [{'Quantile': 0.9,
        'LossValue': 0.0640613829623758},
       {'Quantile': 0.5, 'LossValue': 0.13991594321957088},
       {'Quantile': 0.1, 'LossValue': 0.10678413658910633}],
      'ErrorMetrics': [{'ForecastType': 'mean',
        'WAPE': 0.14845030024660774,
        'RMSE': 2.8056032983401455}]}}]}],
 'ResponseMetadata': {'RequestId': '970b42fa-e957-4d00-bf67-2d334101dcc6',
```

```
'HTTPStatusCode': 200,
'HTTPHeaders': {'content-type': 'application/x-amz-json-1.1',
'date': 'Thu, 29 Jul 2021 18:55:57 GMT',
'x-amzn-requestid': '970b42fa-e957-4d00-bf67-2d334101dcc6',
'content-length': '950',
'connection': 'keep-alive'},
'RetryAttempts': 0}}
```



Amazon Forecast DeepAR+ forecast

5. Conclusion

Discussion

Two custom multivariate models were implemented: RNN with Gated Recurrent Unit (GRU) and a Dilated Causal CNN with Keras and TensorFlow. The 3rd based on Amazon Forecast DeepAR+ algorithm was implemented and deployed at AWS. An attempt was made to compare custom models to Amazon's own DeepAR+ model, but since they use different metrics, further work is required.

- The main goal was to learn how implement and deploy DeepAR+ model for time series forecast to AWS Amazon Forecast.
- The DeepAR+ model of Amazon Forecast (notebook 04) has RMSE of 2.806, while the custom Dilated Causal CNN (notebook 03) has an MSE 0.0037 (or $RMSE = \sqrt{MSE} = 0.061$). Of course, it is not fair to compare a model based on just one time series, to the multivariate custom model.
- the total cost of training and deploying the model at AWS Amazon Forecast was EUR 0.78 (USD 0.91) with the AWS free tier.

The state-of-the-art DeepAR+ model performs well, even though it was the only model using just one time series. The custom models are both multivariate, using temperature and pressure data for 2 cities + some engineered features to help make sense of time of day, and day of the year. All 3 models capture well the daily and seasonal variations in temperature.

Future improvements and TODO

- implement a multivariate version of the predictor, based on the Amazon Forecast advanced examples here, and add the additional data from the original dataset atmospheric pressure and temperature for other cities in the region
- at the moment metric for the model in 02 is MAE, in 03 metrics are MSE and MAPE, while Amazon Forecast uses RMSE and WAPE. need to have same for all 3 models.
- DeepAR+ of Amazon Forecast gives probabilistic Monte Carlo type evaluations, calculating P10, P50 and P90 the plot at the end of Notebook 04. I.e., a statistical confidence level for an estimate. TODO: understand the concept and implement for the first two models.

6. References

- 1. Magnus Erik Hvass Pedersen, TensorFlow-Tutorials / GitHub repo / Videos on YouTube
- 2. Ognian Dantchev, Multivariate Time Series Forecasting with Keras and TensorFlow, GitHub repo
- 3. Amazon Forecast resources, AWS website
- 4. Time Series Forecasting Principles with Amazon Forecast, Technical Guide
- 5. AWS Samples Amazon Forecast Samples GitHub repo
- 6. Aaron van den Oord, Sander Dieleman et al., WaveNet: A Generative Model for Raw Audio