

# **Circuit Theory and Electronics Fundamentals**

Department of Electrical and Computer Engineering, Técnico, University of Lisbon Mestrado em Engenharia Aeroespacial

Laboratory 2 Report

Group 7

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## 1 Introduction

The objective of this laboratory assignment is to study a circuit containing a dependent voltage source  $(V_c)$  and independent  $(I_d, V_a)$  current and voltage sources, connected to resistors  $(R_1 \text{ to } R_7)$  and to a capacitor (C). The circuit and its organization can be seen in Figure 1.

In Section 2, a theoretical analysis of the circuit is presented. In Section 3, the circuit is analysed by simulation, and the results are compared to the theoretical results obtained in Section 2. The conclusions of this study are outlined in Section 4.

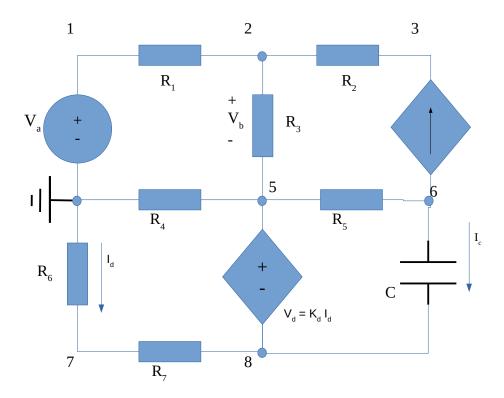


Figure 1: Circuit topography

## 2 Theoretical Analysis

In this section, the circuit shown in Figure 1 is analysed theoretically, through the method of Node Analysis.

## 2.1 Node analysis for t<0

The results obtained after implementing the KNL in Octave can be seen in Tables 1 and 2:

| Name  | Value [V] |
|-------|-----------|
| $V_0$ | 0.000000  |
| $V_1$ | 5.103557  |
| $V_2$ | 4.832610  |
| $V_3$ | 4.274744  |
| $V_5$ | 4.870590  |
| $V_6$ | 5.723435  |
| $V_7$ | -1.944932 |
| $V_8$ | -2.897433 |

Table 1: Voltages obtained in the theoretical analysis in Octave.

The currents derived from the results of the node analysis are found in Table 2.

| Name   | Value [A] |
|--------|-----------|
| $@I_1$ | -0.000261 |
| $@I_2$ | -0.000273 |
| $@I_3$ | -0.000013 |
| $@I_4$ | 0.001203  |
| $@I_5$ | 0.000273  |
| $@I_6$ | -0.000942 |
| $@I_7$ | -0.000942 |

Table 2: Currents obtained in the theoretical analysis in Octave.

#### 2.2 Node Analysis for t≥0 (Natural solution)

Here, we made use of Node Analysis to determine the current that passed through the capacitor. By short-circuting the independent voltage source  $V_s$  and by swapping the capacitor with a voltage source  $V_x = V_6$  -  $V_8$  we were able to calculate the current that flowed through the capacitor and the equivalent resistance. We short-circuted the independent voltage source because we are using the thevenin/norton theorems to calculate the resistence as seen by the

capacitor and we swapped the capacitor with a voltage source as at t = 0 the capacitor begins discharging and it has a voltage of  $V_x$  (since it's voltage is at a peak). Node analysis matrix:

$$R_e q = (V_x/I_x) \tag{3}$$

| Name     | Value [A], [V], [Ohm] |
|----------|-----------------------|
| $@I_x$   | 0.002765              |
| $V_x$    | 8.620868              |
| $R_{eq}$ | 3118.377902           |

Table 3: Equivalent current, voltage and resistor obtained in the theoretical analysis in Octave.

$$V_n = V_x * exp(-t/(R_eq * C)) \tag{4}$$

With the results obtained before we ploted the natural solution in Figure 2.

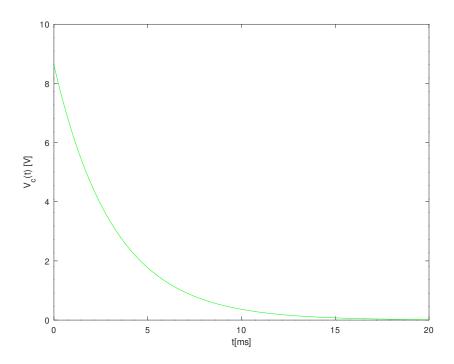


Figure 2: Natural solution for capacitor.

## 2.3 Node Analysis for t≥0 (Forced solution)

To determine the forced solution we used a phasor voltage source  $V_s = 1 \text{ V}$  and then we applied the Node analysis (in which C was replaced by its impedance).

Node analysis matrix:

| Name  | Value [V]            |
|-------|----------------------|
| $V_0$ | 0.000000+0.000000i   |
| $V_1$ | 0.540302+-0.841471i  |
| $V_2$ | 1.362896+-2.122584i  |
| $V_3$ | 2.907933+-4.528837i  |
| $V_5$ | 1.468083+-2.286404i  |
| $V_6$ | -0.111259+-0.457661i |
| $V_7$ | 0.325933+-0.507611i  |
| $V_8$ | 0.166312+-0.259016i  |

Table 4: Complex voltages obtained in the theoretical analysis in Octave.

#### 2.4 Final Solution

The final solution is:

$$V_t = V_6 - V_8, for \ t < 0 \tag{6}$$

$$V_t = V_n + abs(v_6) * cos(2 * pi * f * t + acos(Re(v_6)/abs(v_6))), for t >= 0$$
(7)

The plot of  $V_t$  and  $V_s$  is in Figure 3.

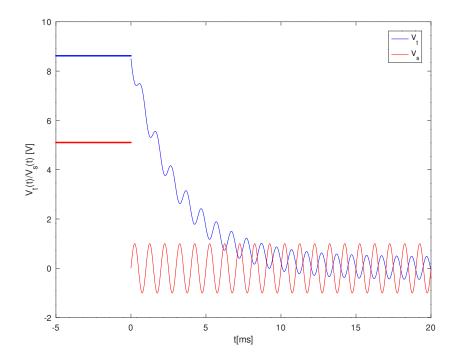


Figure 3: Final solution for  $V_s$  and  $V_t$ 

Here, the model used is one in which, as can be seen in Figure 3, the natural solution of the capacitor tends to diminish into the forced solution given by the sinusoidal excitation of the voltage source  $V_s$ . Finally, at the end of the period studied (t=20ms),it can be observed that the phase of the voltage on the capacitor differs Pi from the phase of voltage source.

#### 2.5 Frequency responses

In this subsection we present the frequency responses graphics. Since both  $V_6$  and  $V_c$  have its amplitude, and therefore magnitude, dependent of frequency, we can observe that with the frequency increase comes a magnitude decrease of both signals. On the contrary, the amplitude of  $V_s$  does not depend on the frequency, and is constant and equal to 1, we can then observe it remains constant and equals to 0, as  $log_{10}(1)$ =0.

As can be seen in Figure 5, when the frequency increases the phase tends to negative values. It is therefore according to what was to be expected.

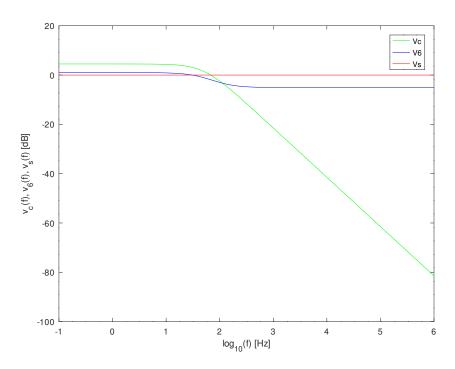


Figure 4: Theoretical analysis of magnitude in response to frequency changes.

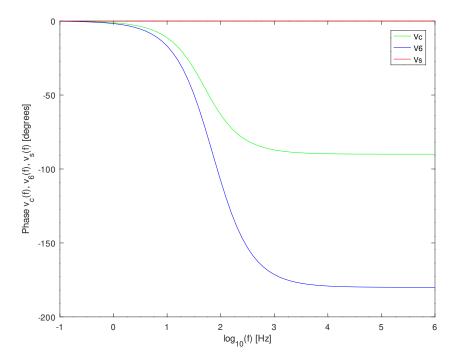


Figure 5: Theoretical analysis of phase in response to frequency changes.

## 3 Simulation Analysis

#### 3.1 Operating Point Analysis for t<0

While using Ngspice we encountered some problems with the use of current-controlled voltage sources. To overcome them, we introduced a dummy 0V voltage source between the resistors 6 and 7. The voltage source  $V_c$  depends on the current  $I_c$ , which is the current on  $R_6$ . However, since Ngspice could not take the current in  $R_6$ , we introduced the null voltage source, since the current there will be  $I_c$ , which is the current that  $V_c$  depends on.

Table 5 shows the simulated operating point results for the circuit under analysis. Compared to the theoretical analysis results, one notices the following differences: describe and explain the differences.

Comparing the Tables 1 and 2 with Table 5, we see that the difference between the different voltages and currents is apromixametly null.

| Name    | Value [A or V] |
|---------|----------------|
| @cd[i]  | 0.000000e+00   |
| @gib[i] | -2.73490e-04   |
| @rr1[i] | 2.609385e-04   |
| @rr2[i] | -2.73490e-04   |
| @rr3[i] | -1.25516e-05   |
| @rr4[i] | 1.202716e-03   |
| @rr5[i] | -2.73490e-04   |
| @rr6[i] | 9.417776e-04   |
| @rr7[i] | 9.417776e-04   |
| v(1)    | 5.103557e+00   |
| v(2)    | 4.832610e+00   |
| v(3)    | 4.274744e+00   |
| v(5)    | 4.870590e+00   |
| v(6)    | 5.723435e+00   |
| v(7)    | -1.94493e+00   |
| v(8)    | -2.89743e+00   |
| v(9)    | 0.000000e+00   |

Table 5: Operating point. A variable preceded by @ is of type *current* and expressed in Ampere; other variables are of type *voltage* and expressed in Volt.

#### 3.2 Operating Point Analysis for t>0 (natural solution)

By short-circuting the independent voltage source  $V_s$  and by swapping the capacitor with a voltage source  $V_x = V_6$  -  $V_8$  we were able to calculate the current that flowed through the capacitor and the equivalent resistance. We short-circuted the independent voltage source because we are using the thevenin/norton theorems to calculate the resistence as seen by the capacitor and we swapped the capacitor with a voltage source as at t=0 the capacitor begins discharging and it has a voltage of  $V_x$  (since it's voltage is at a peak).

The current source  $I_x$  and voltage  $V_6$  can be found in table 6.

| Name    | Value [A or V] |
|---------|----------------|
| @rr5[i] | -2.76454e-03   |
| v(6)    | 8.620868e+00   |

Table 6: Operating point of point 2 of the simulation. A variable preceded by @ is of type *current* and expressed in Ampere; other variables are of type *voltage* and expressed in Volt.

The graphic for the natural solution,  $V_6(t)$ , (using transient analysis) can be seen in Figure 6. Comparing Table 3 with 6, we can see that the difference between current and voltage obtained is nearly null. Moreover, looking at Figures 2 and 6 we can easily observe the similarities between graphics. This points us to the fact that the theorical model used approximates very well the simulations.

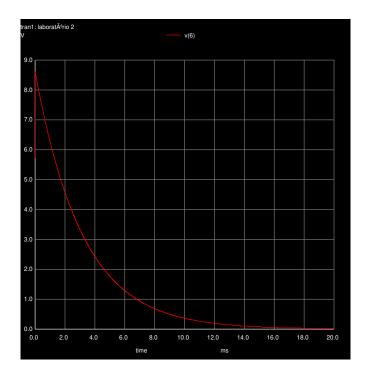


Figure 6: Natural solution for capacitor.

### 3.3 Operating Point Analysis for t>0 (natural and forced solution)

The graphic for the natural and forced responses on  $V_6(t)$  and on  $V_1$  (voltage source) can be observed in Figure 9. Once again, we can conclude that the natural response of the capacitor tends to fade, while the forced response starts to prevail. At the end of the period in study, we can observe that capacitor has a difference of Pi in phase with the voltage source.

Comparing Figure 3 and Figure 7, from Octave and Ngspice respectively, we can observe that the results are identical, which is to be expected, since the circuit is composed by linear components only.

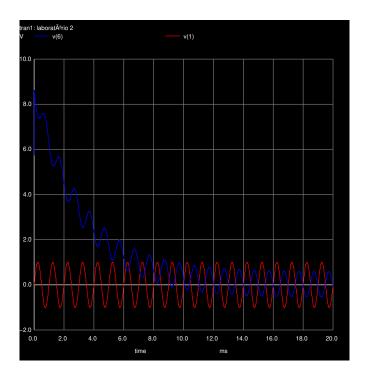


Figure 7: Forced solution of voltage source and capacitor.

#### 3.4 Frequency response

The graphics for the frequency response are seen in Figure 8 and 9. As can be seen in the graph,  $V_c$ 's magnitude is constant, since it is independent from the frequency.  $V_c$  and  $V_6$  are dependent of the frequency and this leads  $V_c$  to 0, since  $V_c$  is inversely proporcional to the frequency. Octave's (Figure 4) and ngspice's (Figure 8) graphs are similiar. Since the circuit is linear, this was expected, so it can be concluded that the model used is a very good aproximation. Once again, we can observe that the phase drops when the frequency increases, pointing out the very similar results in Figure 5 and Figure 9.

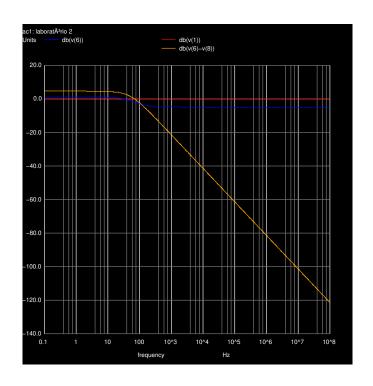


Figure 8: Magnitude in response to frequency changes.

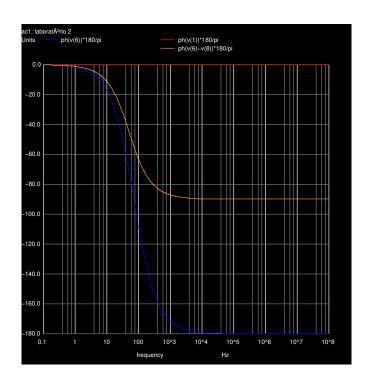


Figure 9: Phase in response to frequency changes.

### 4 Conclusion

The objective of this laboratory assignment as been accomplished as can be seen by the results obtained. The Ngspice simulator is a very powerful tool, as we can see by aproximating very acurately the theorical model.

As can be seen by comparing the tables and figures, both Octave maths tool and circuit simulator Ngspice data match, almost perfectly, the differences are explained by the rounding of the last decimal case. Once again, the model used can be seen to accurately describe the results we obtain, as it was to be expected.