

DMf90Factor: A FORTRAN Program for Experimental WIMP Analysis

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Model-Independent WIMP Scattering Responses and Event Rates

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This is the manual for the FORTRAN version of the model-independent WIMP scattering response and event rate code, which was originally written in Mathematica and described in arXiv:1308.6288.

1 Quickstart guide: Fortran interface

This program primarily computes two quantities. The first is the WIMP-nucleus differential event rate spectra:

$$\frac{dR_D}{dE_R} = \frac{dR_D}{d\vec{q}^2}(q) = N_T \frac{\rho_\chi}{m_\chi} \int_{v_{min}}^{v_{escape}} \frac{2m_T}{4\pi v^2} \frac{1}{2j_\chi + 1} \frac{1}{2j_T + 1} \sum_{spins} |\mathcal{M}(v, q)|^2 \tilde{f}(\vec{v}) v d^3v \quad (1)$$

This quantity has units of events/GeV and is implicitly multiplied by an effective exposure of 1 Kilogram-Day of target nuclei. This is done by taking $N_t = 1 \text{ kilogram} \cdot \text{day} / m_T$, where m_T is the mass of the target nucleus in *GeV*. Recoil energies E_R are given in keV.

The cross section is determined using a user-defined WIMP-nucleus interaction within a non-relativistic effective field theory (EFT) framework. The interaction is specified by 16 coupling coefficients defining an interaction:

$$\sum_{x=p,n} \sum_{i=1}^{16} c_i^x \mathcal{O}_i \quad (2)$$

The second is the integral of the first over either energy or momentum-transfer, for a range specified by the user.

1.1 Required files

1. Input file OR interactive inputs from user
2. Control file (.control)
3. Nuclear density matrix file (.dres)
4. Model space file (.sps) (Will not be required in future release)

1.2 Event rate spectra (events per GeV)

The program will prompt the user for the minimum necessary inputs to run a calculation with default parameter values, including the name of a control file which contains the EFT coefficients, and optionally, additional customizations to the calculation parameters.

After selecting the option to compute an event rate spectra, there are six further lines of input. These will be explained by an example:

```
Enter the target proton number
54
Enter the target neutron number
77
Enter name of control file (.control):
xe131
...
Enter shell-model space file name (.sps)
```

GCN5082

```
...
Enter name of one-body density file (.dres)
xe131gcn
...
What is the range of recoil energies in kev?
Enter starting energy, stoping energy, step size:
0.0001 250. 1.0
```

The first two entries are self-evident: we specify the number of protons and neutrons in the target nucleus. In this case, 54 and 74, respectively, for ^{131}Xe .

Third is the name of the control file containing the EFT coefficients and other, optional, settings. The '.control' file extension is omitted. This contents of this file will be explained in more detail later.

Fourth is a file which gives context for the Shell Model used to describe the nuclear wave functions. Future releases of this code will infer this information, but for now the user must provide the filename containing the single-particle space quantum numbers. The '.sps' file extension is omitted.

Fifth is the file containing the nuclear wave functions in the form of one-body density matrices. Only the ground-state need be included. The '.dres' file extension is omitted.

Sixth and finally are three numbers specifying the range of recoil energies E_R that the differential scattering rate should be computed for.

The event rate spectra will be written to a file, and as a side effect of the calculation, the total event rate for the energy range requested will be estimated by numerical integration. Note that the accuracy of this result will depend on the choice of the step size.

1.3 Control file

Each EFT parameter is written on its own line in [mycontrolfile].control, with four values: the keyword "coefnonrel", the operator number (integer 1..16), the coupling type ("p"=proton, "n"=neutron, "s"=scalar, "v"=vector), and the coefficient value. For example,

```
coefnonrel    1    s    3.1
```

would set $c_1^0 = 3.1$. We take the isospin convention:

$$\begin{aligned} c^0 &= c^p + c^n \\ c^1 &= c^p - c^n \end{aligned} \tag{3}$$

Thus, the previous example is equivalent to:

```
coefnonrel    1    p    1.55
coefnonrel    1    n    1.55
```

The control file also serves a more general but optional function: to set any parameter in the program to a custom value. Simply add an entry to the control file with two values: the first should be the keyword for the parameter and the second should be the value to set that parameter to. For example, to set the velocity of the earth in the galactic frame to 240 *km/s*, you should add the line:

vearth 240.0

1.4 Total integrated events

Inputs 2 - 6 for this calculation will be almost identical to those required for the event rate spectra calculation. The main difference is in the sixth and final input:

```
Using adaptive numerical integration to determine total integrated event rate.  
What are the limits of integration for recoil energies in kev?  
Enter starting energy, stoping energy, relative error:  
0.0 250.0 0.001
```

Here, we have again been asked for a starting and stopping recoil energy, but this time the third value is the desired relative error of the integrated spectra. In this example, 0.001 corresponds to a desired uncertainty of 0.1%.

An important difference between this calculation and the event rate spectra calculation is that in this evaluation, the spectra is not written to file. This is because an adaptive integration routine is used to keep the number of function evaluations to a minimum. As a result, this calculation will be much faster than computing the entire spectra.

2 Quickstart Guide: Python interface

We provide two generic API's for interacting with the Fortran program through a python interface. They are: **runCustomControl** and **runCustomInput**. The former runs the Fortran code with a control file which has been programatically modified by the API then returns the results to the calling environment. The latter does the same, except with a custom input file, rather than a custom control file.

2.1 Example: using runCustomInput to generate a weighted sum of event-rate spectra

In this example we will construct a simple python script using the runCustomInput API to compute the differential event rate spectra for several isotopes of Xe, and compute the weighted sum according to the natural abundances of each isotope.

Firt, examining the API for runCustomInput:

```
1 def runCustomInput(exec_name, input_template, param_dict,
2   workdir='', label='runCustom', resultfile='eventrate_spectra.dat'):
3
4   """
5   Author: Oliver Gorton, 2020
6
7   This is a function for running an executable program with a custom
8   input file by replacing keywords in a template used by the executed
9   code.
10
11   exec_name: (string) containing the path to and name of the
12   executable you want to run
13   input_template: (string) this is an input or control file used by the
14   executable and which will be edited by this function
15   param_dict: (dictionary) of keywords and the values to which those
16   keywords will be changed. The keywords are strings which should
17   appear in the input_template file.
18   workdir: (string) name of the working directory where you want to
19   call the executable and send the output.
20   label: (string) name for this job, to label the input and output
21   files generated by this function.
22
23   """
```

The first three inputs are mandatory while the last three are optional, having default values defined in the function. We begin constructing our script by creating the generic inputs for the executatble name and the directory where the calculations will be done (this is where the required files for the calculation should be). We also specify the atomic number and natural abundances for Xenon isotopes:

```
1 import os
2 import matplotlib.pyplot as plt
3 import runCustomInput
4
5 exec_name = "dmf90factor.x"
6 workdir = os.getcwd()
```

```

7
8 Z = 54
9 isotopes = [128, 129, 130, 131, 132, 134, 136]
10 weights = [.01910, .26401, .04071, .21232, .26909, .10436, .08857]
11 weightedsum = 0.0

```

Now, we will need the input-file template. Having created the template file, for example:

```

1
54
NEUTRONS
xe
GCN5082
xeAAAgcN
1. 1000. 1.0

```

with our arbitrary choice of keywords "NEUTRONS" and "AAA", let's loop over our isotopes, and for each assemble the dictionary of keywords which the API will replace with values:

```

1 input_template = "input.xeAAA"
2 for i, isotope in enumerate(isotopes):
3     N = isotope - Z
4     label = "xe"+str(isotope)
5     param_dict = { "NEUTRONS" : N, "AAA" : isotope }

```

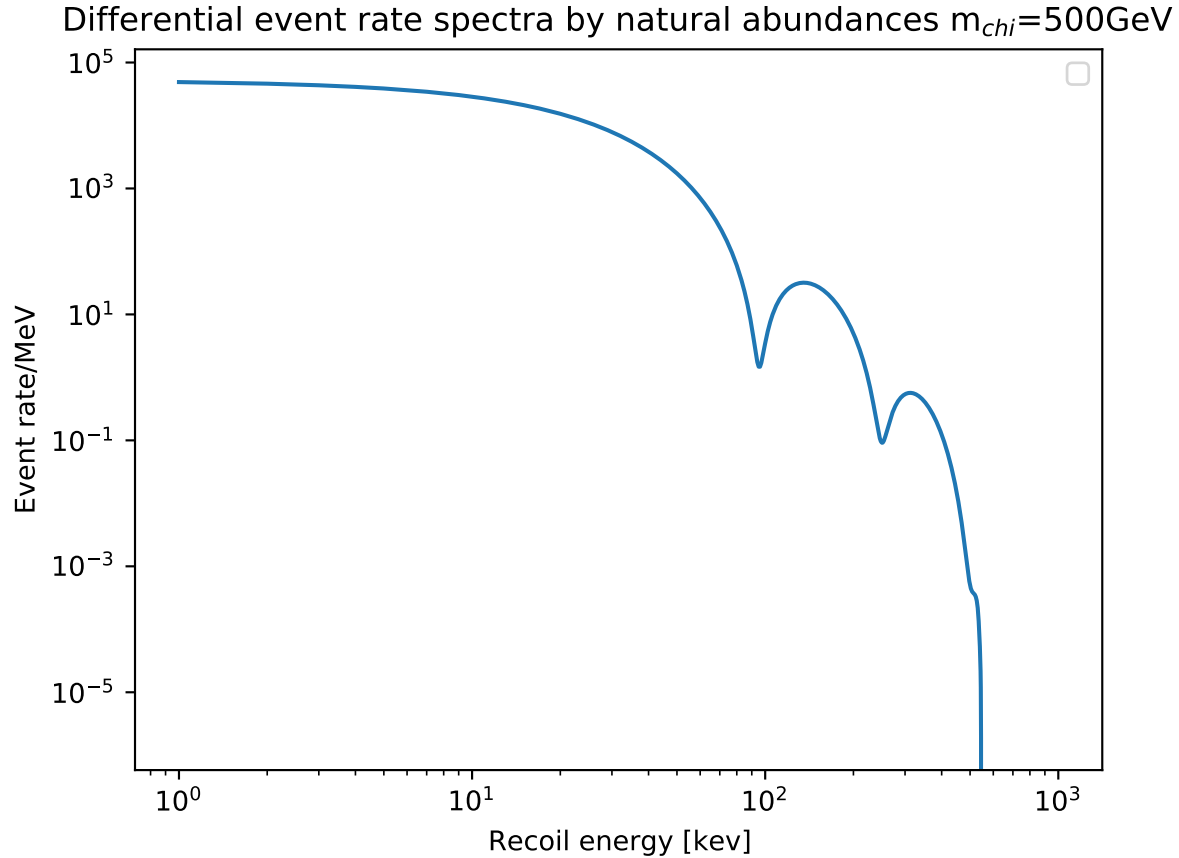
We now have all of the required arguments: `exec_name`, `input_template`, `param_dict`, `workdir`, and `label`. We are ready to call `runCustomInput`, which returns the event rate spectra vs recoil energy arrays. All-together now:

```

1 import os
2 import matplotlib.pyplot as plt
3 import runCustomInput
4
5 exec_name = "dmf90factor.x"
6 workdir = os.getcwd()
7
8 Z = 54
9 isotopes = [128, 129, 130, 131, 132, 134, 136]
10 weights = [.01910, .26401, .04071, .21232, .26909, .10436, .08857]
11 weightedsum = 0.0
12 input_template = "input.xeAAA"
13 for i, isotope in enumerate(isotopes):
14     N = isotope - Z
15     label = "xe"+str(isotope)
16     param_dict = { "NEUTRONS" : N, "AAA" : isotope }
17
18     RecoilE, EventRate = runCustomInput.runCustomInput(exec_name,
19                                                         input_template, param_dict, workdir, label)
20
21     weightedsum += EventRate * weights[i]

```

We now have the weighted sum of event rates stored in the variable `weightedsum`. Using `matplotlib`, we could produce the following plot:



2.2 Example: using runCustomControl to compare event-rate spectra for calculations with different WIMP masses

In this example we will construct a simple python script using the runCustomControl API to compute the differential event rate spectra for several values of the WIMP particle mass. This is very similar in implementation to the previous example, with the main difference being that the WIMP mass is edited by the user through the control file, rather than through the interactive input or input file. The appropriate API for this task is therefore **runCustomControl**:

```

1 def runCustomControl(exec_name, inputfile, control_template, param_dict,
2   workdir='', label='runCustom', resultfile='eventrate_spectra.dat'):
3
4   """
5   Author: Oliver Gorton, 2020
6
7   This is a function for running an executable program with a custom
8   control file by replacing keywords in a template used by the executed
9   code. The control file is one which is used indirectly (not a by a
10  command line pipe). For example, an interaction file for bigstick.
11
12  exec_name:

```

```

13         (string) containing the path to and name of the
14         executable you want to run
15     inputfile:
16         (string) this is an input file used by the executable
17     control_template:
18         (string) the base-name of a file ending in
19         '.control'. "<control_template>.template" is the template
20         file which the function will edit and copy into
21         <control_template>.
22     param_dict:
23         (dictionary) of keywords and the values to which those
24         keywords will be changed. The keywords are strings which should
25         appear in the input_template file.
26     workdir:
27         (string) name of the working directory where you want to call
28         the executable and send the output.
29     label:
30         (string) name for this job, to label the input and output files
31         generated by this function.
32
33     """

```

This API has the same inputs as `runCustomInput`, with ‘inputfile’ instead of ‘input_template’, and one additional argument: ‘control_template’.

We again start by constructing the necessary arguments:

```

1 import os
2 import matplotlib.pyplot as plt
3 import runCustomControl
4
5 exec_name = "dmf90factor.x"
6 inputfile = 'input.xe131'
7 control_template = "xe131.control"
8 workdir = os.getcwd()

```

As in the previous example, `inputfile` is a standard input file we have placed in the current working directory. This time, it is a complete input file with no replaceable keywords:

```

1
54
77
xe131
GCN5082
xe131gcn
1. 1000. 10.0

```

Alongside this standard input file, we also create a template control file called “xe131.control.template”. When the API replaces the keywords in this file, it will strip the .template filename extension, creating a file called “xe131.control”, which is referenced in the fourth line of the above input file. Within this template file, we find the line (along with other necessary and/or optional control commands not listed for brevity):

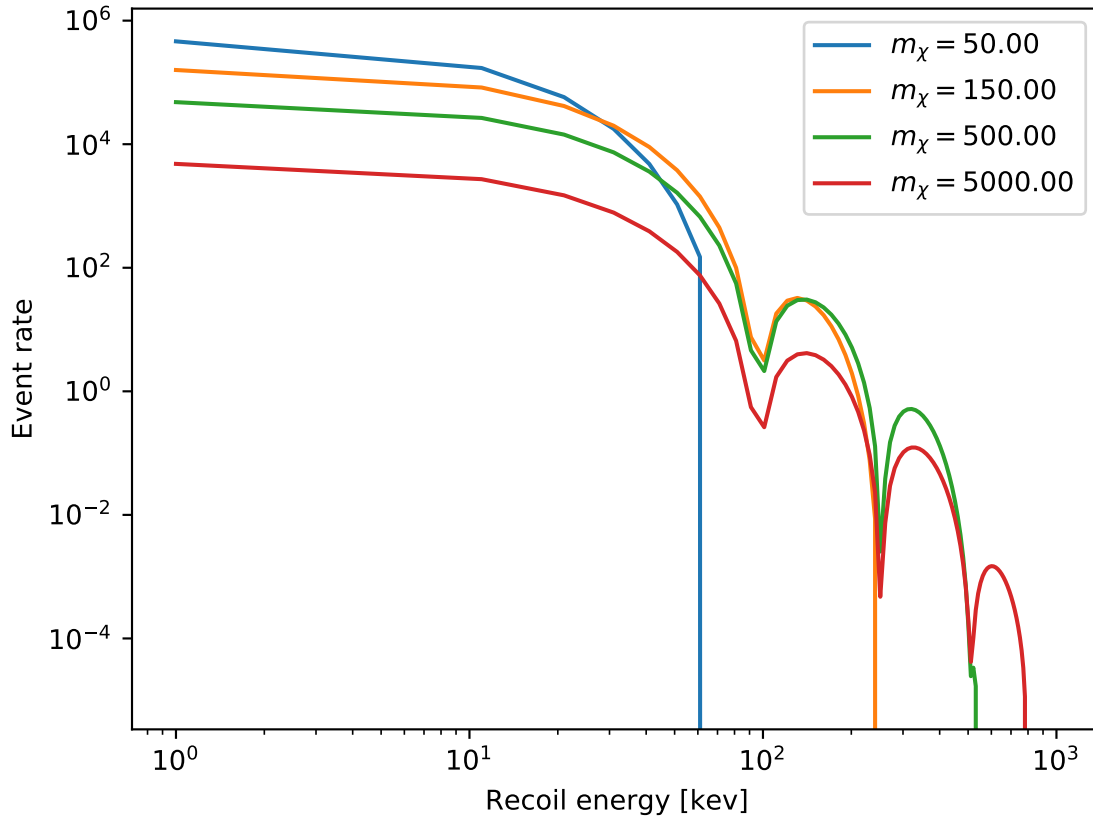
```
wimpmass MASS_KEYWORD
```


‘wimpmass’ is the keyword for setting the WIMP mass, and ‘MASS_KEYWORD’ is our arbitrary keyword for the Python API to replace.

We complete the script by looping over different WIMP masses, creating the dictionary or keywords to replace and their values, and finally call the runCustomControl API:

```
1 import os
2 import matplotlib.pyplot as plt
3 import runCustomControl
4
5 exec_name = "dmf90factor.x"
6 inputfile = 'input.xe131'
7 control_template = "xe131.control"
8 workdir = os.getcwd()
9 for wimp_mass in (50.,150.0, 500.,5000.):
10     param_dict = { "MASS_KEYWORD" : wimp_mass }
11     RecoilE, EventRate = runCustomControl.runCustomControl(exec_name,
12                                                             inputfile, control_template, param_dict, workdir)
```

We could, for example, plot the result at each iteration and construct the following plot:



3 Equations found in the code

3.1 Differential event rate

$$\frac{dR_D}{dE_R} = \frac{dR_D}{d\vec{q}^2}(q) = N_T n_\chi \int_{v_{min}}^{\infty} \frac{d\sigma(v, q)}{d\vec{q}^2} \tilde{f}(\vec{v}) v d^3v \quad (4)$$

where q is the WIMP-nucleon momentum transfer, N_T is the number of target nuclei, $n_\chi = \rho_\chi/m_\chi$ is the local dark matter number density, σ is the WIMP-nucleon cross section, and \tilde{f} is dark matter velocity distribution in the lab-frame. $\tilde{f}(\vec{v})$ is obtained by boosting the Galactic-frame distribution $f(\vec{v})$,

$$\tilde{f}(\vec{v}) = f(\vec{v} + \vec{v}_{earth}), \quad (5)$$

where \vec{v}_{earth} is the velocity of the earth in the galactic rest frame. The simplest model is a three-dimensional Maxwell distribution:

$$f(\vec{v}) \propto e^{-\vec{v}^2/v_0^2}, \quad (6)$$

where v_0 is some scaling factor (typically taken to be around 220 km/s).

In order to evaluate the integral in (4), we make the conversion to spherical coordinates, and take special care to deal with the velocity boost in (5). Assuming a $1/v^2$ velocity dependence of the cross section term (see section 3.2), we need to evaluate an integral of the form

$$I = \int_{v_{min}}^{v_{max}} d^3v \frac{f(\vec{v} + \vec{v}_{earth})}{v} = \int_{v_{min}}^{v_{max}} d^3v \frac{1}{v} e^{-(\vec{v} + \vec{v}_{earth})^2/v_0^2} \quad (7)$$

Noting that $(\vec{v} + \vec{v}_{earth})^2 = \vec{v}^2 + \vec{v}_{earth}^2 + 2v v_{earth} \cos(\theta)$, with $|\vec{v}| \equiv v$ and θ defining the angle between the two vectors, it's convenient to make the substitution $d^3v = d\phi d(\cos \theta) v^2 dv$:

$$\begin{aligned} I &= \int_0^{2\pi} d\phi \int_{v_{min}}^{v_{max}} dv \int_{-1}^1 d(\cos \theta) e^{-2vv_{earth} \cos \theta / v_0^2} v^2 \frac{1}{v} e^{-(\vec{v}^2 + \vec{v}_{earth}^2)/v_0^2} \\ &= 2\pi \int_{v_{min}}^{v_{max}} dv v e^{-(\vec{v}^2 + \vec{v}_{earth}^2)/v_0^2} \left(-\frac{v_0^2}{2vv_{earth}} e^{-2vv_{earth} \cos \theta / v_0^2} \right)_{-1}^1 \\ &= \frac{\pi v_0^2}{v_{earth}} \int_{v_{min}}^{v_{max}} dv e^{-(\vec{v}^2 + \vec{v}_{earth}^2)/v_0^2} \left(-e^{-2vv_{earth}/v_0^2} + e^{+2vv_{earth}/v_0^2} \right) \\ &= \frac{\pi v_0^2}{v_{earth}} \int_{v_{min}}^{v_{max}} dv \left(-e^{(v+v_{earth})^2/v_0^2} + e^{(v-v_{earth})^2/v_0^2} \right) \\ &= \frac{\pi v_0^2}{v_{earth}} \int_{v_{min}}^{v_{max}} dv (g(v - v_{earth}) - g(v + v_{earth})) \end{aligned} \quad (8)$$

where in the last equality, we have defined a one-dimensional Gaussian form

$$g(v) \propto e^{-v^2/v_0^2}. \quad (9)$$

The final expression for I can be trivially generalized to other spherically- symmetric velocity-dependent forms of the differential cross section. What's important is the reduction of the velocity-boosted d^3v integral to a radial integral which can be carried out with one-dimensional quadrature:

$$\int_{v_{min}}^{v_{max}} d^3v \sigma(v) e^{-(\vec{v} + \vec{v}_{earth})^2 / v_0^2} = \frac{\pi v_0^2}{v_{earth}} \int_{v_{min}}^{v_{max}} dv \sigma(v) v^2 (g(v - v_{earth}) - g(v + v_{earth})). \quad (10)$$

The FORTRAN code uses equation (10) to evaluate the event rate integral in equation (4) with quadrature. Analytic solutions of (10) exist in the form of error functions; we use the above form since it makes easy to later modify the velocity distribution (as long as it remains spherically symmetric). For example, adding a velocity cut-off is as easy as changing the limit on the quadrature, with no need to write a whole new subroutine for the analytic forms found in the Mathematica script.

3.2 Differential cross section

$$\frac{d\sigma(v, E_R)}{dE_R} = 2m_T \frac{d\sigma(v)(v, \vec{q}^2)}{d\vec{q}^2} = 2m_T \frac{1}{4\pi v^2} T(v, q), \quad (11)$$

Where v is the velocity of the dark matter particles in the lab-frame, q is the momentum transfer of the scattering event, m_T is the mass of the target nucleus, and $T(v, q)$ is the transition or scattering probability. We can see here that the differential cross section has an explicit $1/v^2$ dependence, independent of any velocity dependence of $T(v, q)$.

3.3 Transition probability / Scattering probability

The scattering probability is

$$T(v, q) = \frac{1}{2j_\chi + 1} \frac{1}{2j_T + 1} \sum_{spins} |\mathcal{M}(v, q)|^2 \quad (12)$$

where j_χ is the spin of the WIMP, j_T is the spin angular momentum of the target nucleus, and \mathcal{M} Galilean invariant amplitude, which is defined by

$$T(v, q) = \frac{4\pi}{2j_T + 1} \frac{1}{(4m_\chi)^2} \sum_{x=p,n} \sum_{x'=p,n} \sum_{i=1}^8 R_i^{xx'}(v^2, q^2) W_i^{xx'}(q) \quad (13)$$

where m_χ is the mass of the dark matter particle and x is an index used to sum over isospin couplings. The coefficients $R_i^{x,x'}$ are dark matter particle response functions, to be define in another section. The operators $W_i^{xx'}(q)$ are nuclear response functions, which are sums over matrix elements of nuclear operators constructed from Bessel spherical harmonics and vector spherical harmonics.

3.4 Dark matter response functions

There are 8 dark matter response functions which group 15 operator coefficients c_i^x according to the pair of nuclear response functions which they multiply.

$$R_M^{xx'}(v, q) = \frac{1}{4}cl(j_\chi) \left((v^2 - (\frac{q}{2\mu_t})^2)(c_5^x c_5^{x'} q^2 + c_8^x c_8^{x'}) + c_{11}^x c_{11}^{x'} q^2 \right) \quad (14)$$

$$+ (c_1^x + c_2^x(v^2 - (\frac{q}{2\mu_t})^2))(c_1^{x'} + c_2^{x'}(v^2 - (\frac{q}{2\mu_t})^2)) \quad (15)$$

$$R_{\Sigma''}^{xx'}(v, q) = \frac{1}{16}cl(j_\chi) \left(c_6^x c_6^{x'} q^4 + (c_{13}^x c_{13}^{x'} q^2 + c_{12}^x c_{12}^{x'})(v^2 - q^2/(2\mu_T)^2) + 2c_4^x c_6^{x'} q^2 + c_4^x c_4^{x'} \right) + \frac{1}{4}c_{10}^x c_{10}^{x'} q^2 \quad (16)$$

$$R_{\Sigma'}^{xx'}(v, q) = \frac{1}{32}cl(j_\chi) \left(2c_9^x c_9^{x'} q^2 + (c_{15}^x c_{15}^{x'} q^4 + c_{14}^x c_{14}^{x'} q^2 - 2c_{12}^x c_{15}^{x'} q^2 + c_{12}^x c_{12}^{x'})(v^2 - q^2/(2\mu_T)^2) + 2c_4^x c_4^{x'} \right) \quad (17)$$

$$+ \frac{1}{8} \left(c_3^x c_3^{x'} q^2 + c_7^x c_7^{x'} \right) (v^2 - q^2/(2\mu_T)^2) \quad (18)$$

$$R_{\Phi''}^{xx'}(v, q) = \frac{q^2}{(4m_N)^2}cl(j_\chi) (c_{12}^x - c_{15}^x q^2) (c_{12}^{x'} - c_{15}^{x'} q^2) + \frac{q^2}{(4m_N)^2} q^2 c_3^x c_3^{x'} \quad (19)$$

$$R_{\Phi'}^{xx'}(v, q) = \frac{q^2}{(4m_N)^2}cl(j_\chi) (c_{12}^x c_{12}^{x'} q^2 + c_{12}^x c_{12}^{x'}) \quad (20)$$

$$R_{\Delta}^{xx'}(v, q) = \frac{q^2}{(2m_N)^2}cl(j_\chi) (c_5^x c_5^{x'} q^2 + c_8^x c_8^{x'}) + 2\frac{q^2}{m_N^2} c_2^x c_2^{x'} (v^2 - q^2/(2\mu_T)^2) \quad (21)$$

$$R_{\Delta\Sigma'}^{xx'}(v, q) = \frac{q^2}{(2m_N)^2}cl(j_\chi) (c_4^x c_5^{x'} - c_8^x c_9^{x'}) - \frac{q^2}{m_N} c_2^x c_3^{x'} (v^2 - q^2/(2\mu_T)^2) \quad (22)$$

$$R_{\Phi''M}^{xx'}(v, q) = \frac{q^2}{4m_N}cl(j_\chi) c_{11}^x (c_{12}^{x'} - c_{12}^{x'} q^2) + \frac{q^2}{m_N} c_3^{x'} (c_1^x + c_2^x(v^2 - q^2/(2\mu_T)^2)) \quad (23)$$

As a shorthand we have introduced the notation

$$cl(j) = 4j(j+1)/3. \quad (24)$$

3.5 Nuclear response functions

There are eight nuclear response functions $W_i^{xx'}(y)$ considered here. The unit-less variable y is defined

$$y = \left(\frac{qb}{2} \right)^2, \quad (25)$$

in terms of the harmonic oscillator size parameter b , which has a default value of

$$b^2 = 41.467/(45A^{-1/3} - 25A^{-2/3}) fm^2. \quad (26)$$

$$W_M^{xx'}(y) = \sum_{\text{even } J} \langle j_T | M_{Jx}(y) | j_T \rangle \langle j_T | M_{Jx'}(y) | j_T \rangle \quad (27)$$

$$W_{\Sigma''}^{xx'}(y) = \sum_{\text{odd } J} \langle j_T | \Sigma''_{Jx}(y) | j_T \rangle \langle j_T | \Sigma''_{Jx'}(y) | j_T \rangle \quad (28)$$

$$W_{\Sigma'}^{xx'}(y) = \sum_{\text{odd } J} \langle j_T | \Sigma'_{Jx}(y) | j_T \rangle \langle j_T | \Sigma'_{Jx'}(y) | j_T \rangle \quad (29)$$

$$W_{\Phi''}^{xx'}(y) = \sum_{\text{even } J} \langle j_T | \Phi''_{Jx}(y) | j_T \rangle \langle j_T | \Phi''_{Jx'}(y) | j_T \rangle \quad (30)$$

$$W_{\tilde{\Phi}'}^{xx'}(y) = \sum_{\text{even } J} \langle j_T | \tilde{\Phi}'_{Jx}(y) | j_T \rangle \langle j_T | \tilde{\Phi}'_{Jx'}(y) | j_T \rangle \quad (31)$$

$$W_{\Delta}^{xx'}(y) = \sum_{\text{odd } J} \langle j_T | \Delta_{Jx}(y) | j_T \rangle \langle j_T | \Delta_{Jx'}(y) | j_T \rangle \quad (32)$$

$$W_{\Delta\Sigma'}^{xx'}(y) = \sum_{\text{odd } J} \langle j_T | \Delta_{Jx}(y) | j_T \rangle \langle j_T | \Sigma'_{Jx'}(y) | j_T \rangle \quad (33)$$

$$W_{\Phi''M}^{xx'}(y) = \sum_{\text{even } J} \langle j_T | \Phi''_{Jx}(y) | j_T \rangle \langle j_T | M_{Jx'}(y) | j_T \rangle \quad (34)$$

3.6 Nuclear operators and their matrix elements

of which there are six, are nuclear operators constructed from Bessel spherical harmonics and vector spherical harmonics, and are evaluated here on the ground state of the target nucleus.

4 Control file keywords

Keyword	Symbol	Meaning	Units	Default
dmdens	ρ_χ	Local dark matter density.	GeV/cm ³	0.3
dmspin	j_χ	Intrinsic spin of WIMP particles.	\hbar	$\frac{1}{2}$
fillnuclearcore		Logical flag (enter 0 for False, 1 for True) to fill the inert-core single-particle orbitals in the nuclear level densities. Phenomenological shell model calculations typically provide only the density matrices for the active valence-space orbitals, leaving it to the user to infer the core-orbital densities. This option automatically assigns these empty matrix elements assuming a totally filled core.		1 (true)

intpoints		Number of lattice points in the numerical quadrature. More lattice points results in a more accurate integral, at the cost of runtime.		1000
maxwellv0	v_0	Maxwell-Boltzman velocity distribution scaling factor.	km/s	220.0
mnucleon	m_N	Mass of a nucleon. It's assumed that $m_p \approx m_n$.	GeV	0.938272
ntscale	N_t	Effective number of target nuclei scaling factor. The differential event rate is multiplied by this constant in units of kilogram-days. For example, if the detector had a total effective exposure of 2500 kg days, one might enter 2500 for this value.	kg days	1.0
useenergyfile		Logical flag (enter 0 for False, 1 for True) to read energy grid used for calculation from a user-provided file instead of specifying a range.		0 (false)
usemomentum		Logical flag (enter 0 for False, 1 for True) to use momentum transfer instead of recoil energy as the independent variable.		0 (false)
vearth	v_{earth}	Speed of the earth in the galactic frame.	km/s	232.0
vescape	v_{escape}	Galactic escape velocity. Particles moving faster than this speed will escape the galaxy, thus setting an upper limit on the WIMP velocity distribution.	km/s	$12 \times v_{scale}$
weakmscale	m_v	Weak interaction mass scale. User defined EFT coefficients are divided by m_v^2 .	GeV	246.2
wimpmass	m_χ	WIMP particle mass.	GeV	50.0