

## Algorithm Proof

The algorithm implemented runs in  $O(N+W+M^2)$  time complexity. First, the inputs are taken through `getline()` and stored in variables `key` and `hint`. `Key` and `hint` are then passed as parameters into the constructor of a `Password` object. The object's variables are set within the constructor and the method `showPattern` is called to identify the LPS array that aligns with the given hint. The method `showPattern` runs in  $O(W)$  as it loops through all  $W$  characters of `hint` once updating the LPS pattern each iteration. Next, the method `makediff` is run in  $O(N)$  time as it runs through each character of `key` and compares it to a character of `hint`. If the characters match, then the next character in each is compared; otherwise, a previous character in `hint` is compared to the character in `key` until either the first character of `hint` fails or a match is found. When a match occurs, the difference between the found index and the last index are stored in an integer array with the exception of the first index which is stored in a temp variable that is updated each time a match is found. Because of the comparisons with  $W$  hint characters and the fact that the hint index can only be decremented as far as it has been incremented between 0 and  $W-1$ , then the worst case time complexity for finding the differences is  $O(2*N)$  which is still  $O(N)$ . Next, an array that is the reverse of the previously found index differences is formed in  $O(M)$  time totaling  $O(N+W+M)$  time so far. Lastly, the method `diffid` is called to compare the arrays `diff` and `ffid` holding the differences in forward and reverse. A `Password` object containing the arrays, an empty string called `code`, the `key`, the `hint`, and a few other variables is passed into `diffid`. If the last integers of the array are equal, then the integer is added to the front of the recursively returned `code` and the object is returned to its previous call. If they are not equal, then the object is copied into two new temporary objects and the index of `diff` is decremented in the first one and the index of `ffid` is decremented and the longer of the codes between the two recursive output codes is returned to the previous call. In the worst case, every integer in each array is compared to every integer in the reverse array in  $O(M^2)$  time. This in total is  $O(N+W+M+M^2)$  which is still equivalent to  $O(N+W+M^2)$  time.