EEE443 Neural Networks Homework 1 Report

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We can define error as error = yn-h(xn,w) = we have orpmin Z (error)2+BI w12 W= orgmax P(Wlenor) (Rule = orgmax P(error) P(W) = orgmax P(error | W) P(W)

W P(error) = orgmax P(error | W) P(W) lusing natural logarithm = orgmax ln(P(error/w)P(w)) = orgmax [en(P(error/w))+ln(P(w))] Finding agmox of ln(P(error lw))+ln(P(w)) is same or finding agmin of -ln (Plenor | w1)-ln (Plw1) thus, w= arg min T-ln (p(error lw1)-ln (p(W))] we are given that moximum a parteriori estimate for the network weights are obtained by solving: Organin [(error n) 2 + BIW12] Seeing the similarity between the moximum a porteriori estimate and the equation w=aremin [-ln(P(enor/w))-ln(P(w))] we can say that -ln(P(w))~ \$ \(\sum_{i2} = -ln(P(w)) = \(\begin{array}{c} \begin{array}{c} \begin{array}{c} \extrem{P(w)} & = \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \extrem{P(w)} & = \begin{array}{c} \begin{array}{ Therefore, $P(w)=e^{-\gamma \beta \sum w_i^2}$ $\sum w_i^2=WW^T$ $P(w)=e^{-\gamma \beta WW^T}$ prior probability dotribution of the network weights

Question 2)

In this question, we are to design a neural network with a single hidden layer with four input neurons (with binary inputs) and a single ouput neuron, assuming a step function as the activation function, to implement:

$$(X_1OR\ NOT\ X_2)\ XOR\ (NOT\ X_3OR\ NOT\ X_3)$$

which can also be written as

$$(X_1 + \bar{X}_2) \oplus (\bar{X}_3 + \bar{X}_4)$$

This function can be simplified as:

$$(X_1 + \bar{X}_2)\overline{(\bar{X}_3 + \bar{X}_4)} + \overline{(X_1 + \bar{X}_2)}(\bar{X}_3 + \bar{X}_4)$$

where OR operation refers to summation and AND to multiplication. Further simplifications:

$$[(X_1 + \bar{X}_2)(X_3X_4)] + [(\bar{X}_1X_2)(\bar{X}_3 + \bar{X}_4)]$$

$$[X_1X_2X_4 + \bar{X}_2X_3X_4] + [\bar{X}_1X_2\bar{X}_3 + \bar{X}_1X_2\bar{X}_4]$$

a) This simplified logic equation forms 4 neurons of hidden layer (AND operation). Truth tables of each neuron and calculation weights and biases of each neuron are shown below:

Truth Table for $X_1X_3X_4$

X1	Х3	X4	Output
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

Corresponding activation functions for each row of truth table is given on left, whereas the simplified constraints for step function as activation function are given on the right below:

$$f(-\theta) < 0 \qquad \theta > 0 \qquad \theta > 0$$

$$f(w_4 - \theta) < 0 \qquad \theta > w_4 \qquad \theta > w_3 + w_4 \qquad \theta > w_3 + w_4 \qquad \theta > w_3 + w_4 \qquad \theta > w_1 + w_4 \qquad \theta > w_1 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 + w_2 + w_3 + w_4 \qquad \theta > w_1 +$$

Weights and biases chosen arbitrarly, complying with the inequalities above are:

$$w_1 = 2$$
 $\theta = 4.5$
 $w_2 = 0$
 $w_3 = 2$
 $w_4 = 2$

			_		
Truth	Table	for	X_{2}	X_{2}	$X_{\mathbf{A}}$
			4 1	4 . 4	4 4

X2	Х3	X4	Output
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

Corresponding activation functions for each row of truth table is given on left, whereas the simplified constraints for step function as activation function are given on the right below:

$f(-\theta) < 0$	$\theta > 0$
$f(w_4 - \theta) < 0$	$\theta > w_4$
$f(w_3 - \theta) < 0$	$\theta > w_3$
$f(w_3 + w_4 - \theta) > 0$	$w_3 + w_4 > \theta$
$f(w_2 - \theta) < 0$	$\theta > w_2$
$f(w_2 + w_4 - \theta) < 0$	$\theta > w_2 + w_4$
$f(w_2 + w_3 - \theta) < 0$	$\theta > w_2 + w_3$
$f(w_2 + w_3 + w_4 - \theta) < 0$	$\theta < w_2 + w_3 + w_4$

Weights and biases chosen arbitrarly, complying with the inequalities above are:

$$w_1 = 0$$

 $w_2 = -1$
 $w_3 = 1$
 $w_4 = 2$
 $\theta = 2.25$

Truth Table for $\overline{X}_1X_2\overline{X}_3$

X1	X2	Х3	Output
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

Corresponding activation functions for each row of truth table is given on left, whereas the simplified constraints for step function as activation function are given on the right below:

$f(-\theta) < 0$	$\theta > 0$
$f(w_3 - \theta) < 0$	$\theta > w_3$
$f(w_2 - \theta) > 0$	$w_2 > \theta$
$f(w_2 + w_3 - \theta) < 0$	$w_2 + w_3 < \theta$
$f(w_1 - \theta) < 0$	$\theta > w_1$
$f(w_1 + w_3 - \theta) < 0$	$\theta > w_1 + w_3$
$f(w_1 + w_2 - \theta) < 0$	$\theta > w_1 + w_2$
$f(w_1 + w_2 + w_3 - \theta) < 0$	$\theta < w_1 + w_2 + w_3$

Weights and biases chosen arbitrarly, complying with the inequalities above are:

$$w_1 = -2$$

$$w_2 = 2$$

$$w_3 = -1$$

$$w_4 = 0$$

$$\theta = 1.75$$

Truth Table for $\overline{X}_1X_2\overline{X}_4$

X1	X2	X4	Output
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

Corresponding activation functions for each row of truth table is given on left, whereas the simplified constraints for step function as activation function are given on the right below:

$$\begin{split} f(-\theta) &< 0 & \theta > 0 \\ f(w_4 - \theta) &< 0 & \theta > w_4 \\ f(w_2 - \theta) &> 0 & w_2 > \theta \\ f(w_2 + w_4 - \theta) &< 0 & \theta > w_2 + w_4 \\ f(w_1 - \theta) &< 0 & \theta > w_1 \\ f(w_1 + w_4 - \theta) &< 0 & \theta > w_1 + w_4 \\ f(w_1 + w_2 - \theta) &< 0 & \theta > w_1 + w_2 \\ f(w_1 + w_2 + w_4 - \theta) &< 0 & \theta > w_1 + w_2 \\ \end{split}$$

Weights and biases chosen arbitrarly, complying with the inequalities above are:

$$w_1 = -1$$

 $w_2 = 2$
 $w_3 = 0$
 $w_4 = -1$
 $\theta = 1.25$

In the truth table below for the 4-input OR gate, Neuron 1 is $X_1X_3X_4$, Neuron 2 is $\bar{X}_2X_3X_4$, Neuron 3 is $\bar{X}_1X_2\bar{X}_3$ and Neuron 4 is $\bar{X}_1X_2\bar{X}_4$.

Truth Table for Neuron 1 + Neuron 2 + Neuron 3 + Neuron 4

Neuron 1	Neuron 2	Neuron 3	Neuron 4	Output
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

Corresponding activation functions for each row of truth table is given on left, whereas the simplified constraints for step function as activation function are given on the right below:

$f(-\theta) < 0$	$\theta > 0$
$f(w_4 - \theta) > 0$	$w_4 > \theta$
$f(w_3 - \theta) > 0$	$w_3 > \theta$
$f(w_3 + w_4 - \theta) > 0$	$\theta > w_3 + w_4$
$f(w_2 - \theta) > 0$	$\theta > w_2$
$f(w_2 + w_4 - \theta) > 0$	$\theta > w_2 + w_4$
$f(w_2 + w_3 - \theta) > 0$	$\theta > w_2 + w_3$
$f(w_2 + w_3 + w_4 - \theta) > 0$	$\theta > w_2 + w_3 + w_4$
$f(w_1 - \theta) > 0$	$w_1 > \theta$
$f(w_1 + w_4 - \theta) > 0$	$w_1 + w_4 > \theta$
$f(w_1 + w_3 - \theta) > 0$	$w_1 + w_3 > \theta$
$f(w_1 + w_3 + w_4 - \theta) > 0$	$w_1 + w_3 + w_4 > \theta$
$f(w_1 + w_2 - \theta) > 0$	$w_1 + w_2 > \theta$
$f(w_1 + w_2 + w_4 - \theta) > 0$	$w_1 + w_2 + w_4 > \theta$
$f(w_1 + w_2 + w_3 - \theta) > 0$	$w_1 + w_2 + w_3 > \theta$
$f(w_1 + w_2 + w_3 + w_4 - \theta) > 0$	$w_1 + w_2 + w_3 + w_4 > \theta$

Weights and biases chosen arbitrarly, complying with the inequalities above are:

$$w_1 = 1$$

 $w_2 = 1$
 $w_3 = 1$
 $w_4 = 1$
 $\theta = 0.75$

b) The output of the vector calcualted by MATLAB is:

```
The output of the network taking inputs in binary from 0 to 15 is the vector: 0 0 0 1 1 1 1 0 0 0 0 1 0 0 0 1
```

This output vector is correct, according to the truth table of the $(X_1 + \bar{X}_2) \oplus (\bar{X}_3 + \bar{X}_4)$ showing that the network achieves 100% performance in implementing the desired logic.

- c) To minimize the error caused by the Gaussian Noise and to make the network have the most robust decision boundary, I prefer to select biases in the exact middle of lower and higher values of the constraints. The values that are found this way give the optimal performance of the network.
- d) We are to generate 400 input samples by first concatenating 25 samples from each input vector and then, we generate a random noise vector of length 2 for each training sample, assuming a zero-mean Gaussian distribution with an std of 0.2.

	X_noise ×														
4:	x400 double														
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	0.0214	-0.1928	-0.4023	-0.0086	0.0687	-0.0381	-0.2448	7.9191e-04	0.8246	1.1965	0.8679	1.3464	1.0707	0.8175	1.3333
2	0.0499	0.0852	-0.3786	-0.2320	1.2463	1.0743	1.0667	1.0692	0.2451	0.0192	0.1308	-0.0207	1.1145	1.1054	0.9736
3	0.0220	0.3051	1.0021	0.8378	-0.0492	0.0232	1.3086	0.8269	-0.1032	-0.1079	1.2149	0.9537	-0.0269	0.0467	1.0221
4	-0.1406	0.9679	-0.0755	1.0600	0.0097	1.2080	-0.1400	0.9605	0.0657	1.1128	-0.0387	1.1104	0.1703	0.8278	0.3166
5															
6															

Figure 1: First 15 column of new X matrix with Gaussian noise

The classification performance of the non robust and robust networks on the validation samples is calculated by MATLAB:

```
Correctness percentage of not robust network is:
85

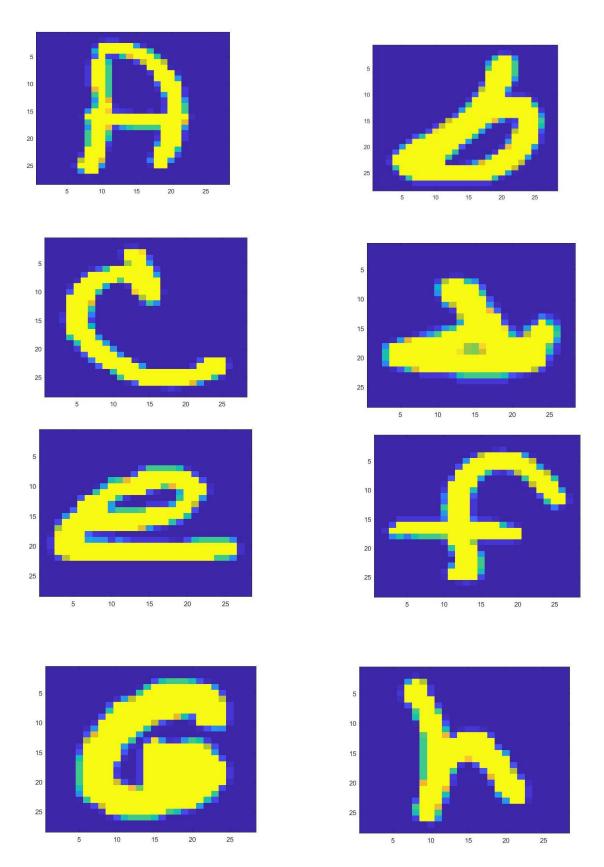
Correctness percentage of robust network is:
90.7500
```

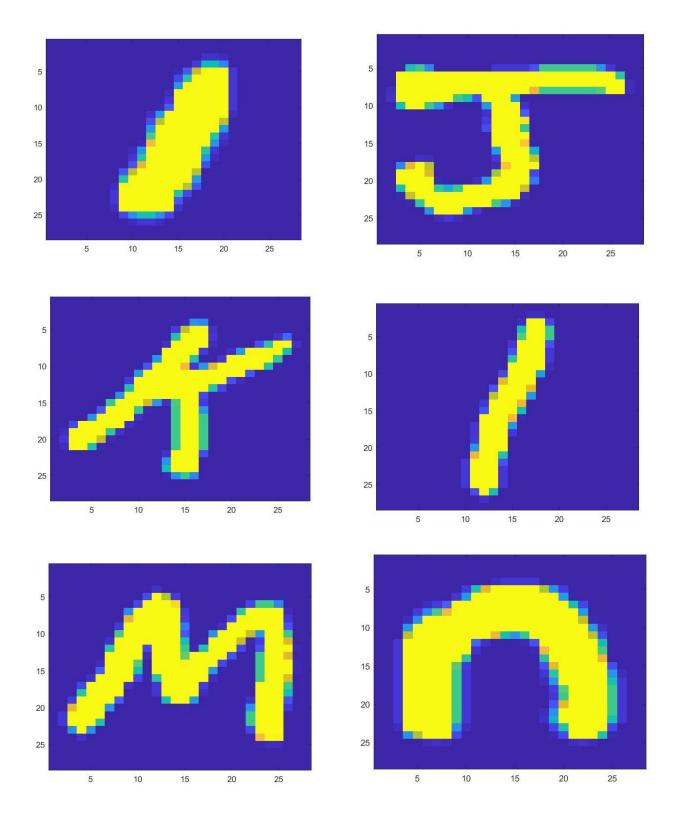
It can be seen that the performance of the network increases as it uses robust configuration of weights and biases. Therefore, using optimal weights and biases that make the network most robust increase the performance of the network.

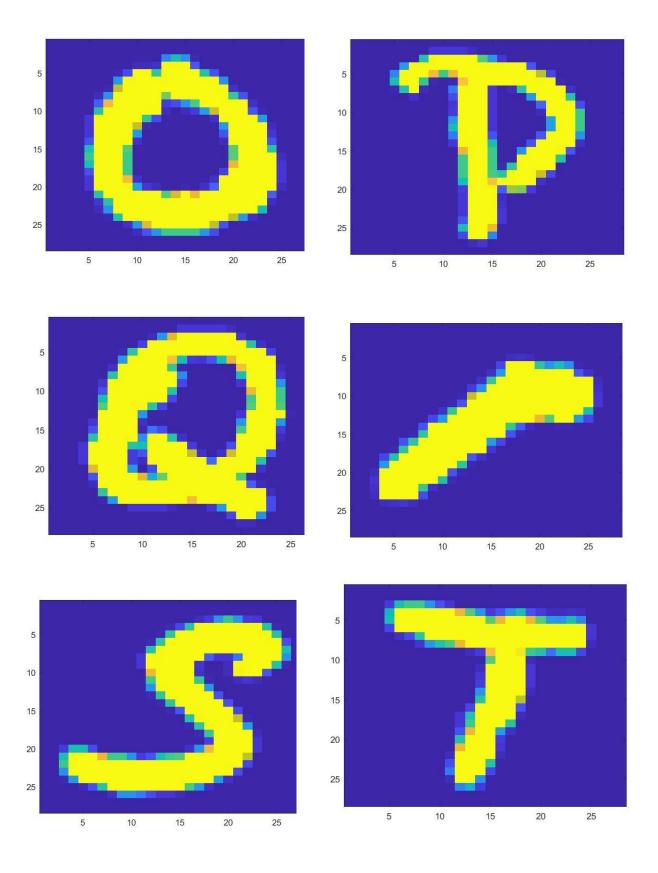
Question 3)

a)

Sample images from each class:







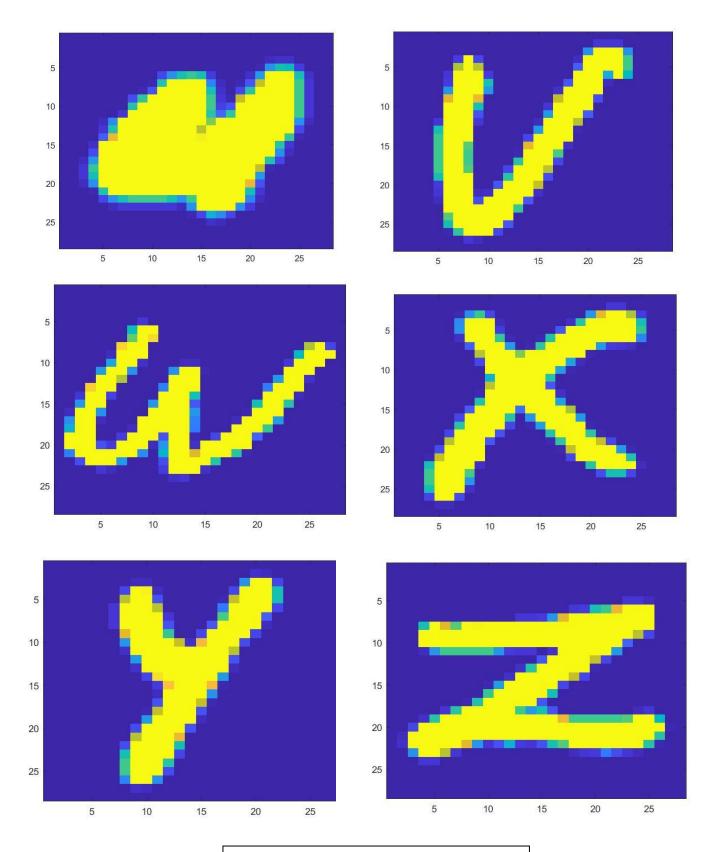


Figure 2: Letter Samples from English Alphabet

The first 15 columns of correlation coefficients matrix can be seen below. Diagonal of this matrix consists of 1's, as the correlation coefficient between two same images is 1.

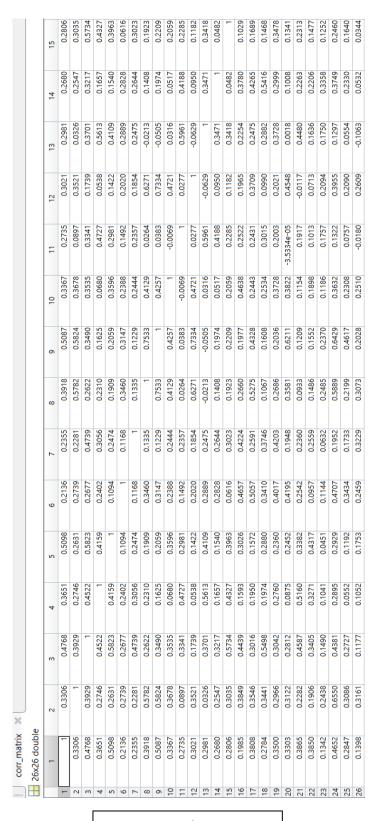


Figure 3: Correlation Matrix

The variability for within-class is lower than for across-class because the images in the same class are more similar than two images in different classes. This situation can also be observable in the correlation coefficient matrix below. In conclusion, for two images that are in the same class, their correlation is stronger than for two images that are in different class (across- class).

The correlation coefficient matrix can be visualised as below:

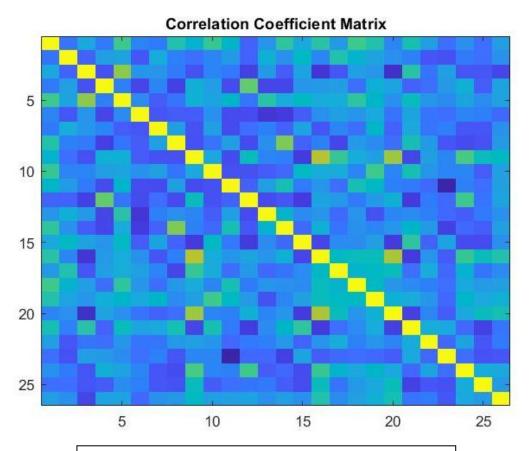


Figure 4: Correlation Matrix within Image Representation

b) Optimal learning rate is found to be around 0.1. The final network weights for each digit as a separate image can be seen below:

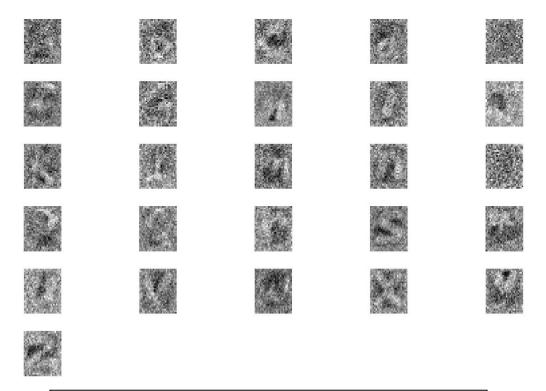
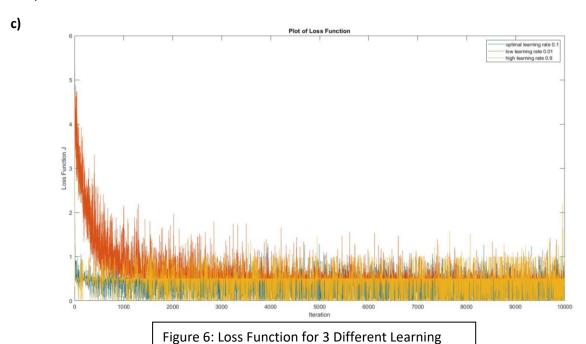


Figure 5: Final Network Weights for Each Digit as Separate Images

It can be seen that network predicts the letters in the alphabet with a moderate performance and accuracy. This is due to single layer perceptron architecture of network, which is more primitive compared to the multi layer neural networks, which maye give higher performance. The results are not perfect but letters can be read.



As it can be seen from the plot of the loss function for optimal learning rate, low learning rate and high learning rate, the most optimal minimization of loss function occurs for optimal learning rate.

d) The performance of the trained networks using all samples in the test data are evaluated using MATLAB and results for three different learning rates can be seen below:

```
The correctness for learning rate nu 0.1 is = 57.461538

The correctness for low learning rate nu 0.001 is = 14.230769

The correctness for high learning rate nu 0.9 is = 32.307692
```

APPFNDIX

```
function oguz altan 21600966 hw1(question)
clc
close all
switch question
    case '1'
        disp('1')
        %% question 1 code goes here
        disp('The answer of this question is analytical
and can be found on the report.');
    case '2'
        disp('2')
        %% question 2 code goes here
        %hidden layer (AND gate) input weights and bias
        w1 = [2 \ 0 \ 2 \ 2];
        w2 = [0 -1 1 2];
        w3 = [-2 \ 2 \ -1 \ 0];
        w4 = [-1 \ 2 \ 0 \ -1];
        theta = [4.5 \ 2.25 \ 1.75 \ 1.25];
        W hidden = [w1; w2; w3; w4];
        disp('hidden layer input weights matrix is: ');
        disp(W hidden);
        disp('hidden layer bias weight vector is: ');
        disp(theta);
        %output layer (OR gate) input weigths and bias
        W \text{ or } = [1 \ 1 \ 1 \ 1];
        theta or = 0.75;
        disp('output layer input weights vector is: ')
        disp(W or);
        disp('output layer bias weight is: ');
        disp(theta or);
```

```
bina input = decimalToBinaryVector(0:15); %creates
matrix of binary equivalents of 0 to 15
        disp('Matrix of binary equivalents of decimal 0 to
15: ');
        disp(bina input);
        %calculates the network output: hidden layer takes
weights and theta and uses
        %weighted sum minus bias and puts the result in
activation
        %function. Output layer makes similar calculation
using OR layer
        %weights, which are outputs of hidden layer and
again puts the result into activation function. The
        %result is nn out
        nn out =
unitStep(W or*unitStep(W hidden*bina input'-theta')-
theta or);
        disp('The output of the network taking inputs in
binary from 0 to 15 is the vector: ')
        disp(nn out)
        %generate 400 input samples by concatenating 25
samples from each input vector
        %and adds gaussian noise with std of 0.2
        std = 0.2;
        new X = repmat(bina input', 1, 25);
        noise = std*randn(4,400);
        X \text{ noise} = \text{new } X + \text{noise};
        disp('New X matrix with Gaussian noise:');
        disp(X noise);
        %not robust network
        %calculates network output using the same way that
is explained for
        %nn out
        nn out tt =
unitStep(W or*unitStep(W hidden*new X-theta')-theta or);
        nn out noised =
unitStep(W or*unitStep(W hidden*X noise-theta')-theta or);
        notrobustcorrect = sum(nn out tt ==
nn out noised) /4; %compares the original vs noised network
        disp('Correctness percentage of not robust network
is: ')
        disp(notrobustcorrect);
```

```
%robust network
        robust hidden theta = [5 2.5 1.5 1.5];
        robust theta or = 0.5;
        nn out tt robust =
unitStep(W or*unitStep(W hidden*new X-
robust hidden theta')-robust theta or);
        nn out noised robust =
unitStep(W or*unitStep(W hidden*X noise-
robust hidden theta')-robust theta or);
        %compares the original vs noised network and
divides the number of times
        %that they are equal by 4 to find the correctness
percentage
        robustcorrect = sum(nn out tt robust ==
nn out noised robust) /4;
        disp('Correctness percentage of robust network is:
')
        disp(robustcorrect);
    case '3'
        disp('3')
        %% question 3 code goes here
        load('assign1 data1.mat')
        %part a
        %find random indexes for each class
        rand vector = [];
        for i = 1:26
            rand vector = [rand vector randi([(i-1)*200]
i*200])];
        end
        rand vector;
        %print sample images for each class
        for i = 1:26
            figure;
            image(trainims(:,:,rand vector(i)));
        end
        figure;
        image(trainims(:,:,randi([5000 5200])))
        %construct correlation matrix for each pair of
images
        bina input = [];
```

```
for i = 1:26
            matt = trainims(:,:,rand vector(i));
            col vec = matt(:); %reshapes the image matrix
into a column vector
            bina input = [bina input col vec];
        end
        bina input = double(bina input);
        corr matrix = corrcoef(bina input);
        disp('The correlation coefficient matrix: ');
        disp(corr matrix);
        imagesc(corr matrix);
        title('Correlation Coefficient Matrix');
        %using one hot encoding for labels to make them
appropriate
        %to use in error calculation
        onehot = zeros(26,5200);
        for i = 1:5200
            onehot(trainlbls(i),i) = 1;
        end
        %constructing weights and learning rate (nu)
matrices
        std = 0.1;
        W = 0.1*randn(785,26); %Gaussian noise weights
        nu opt = 0.1; %learning rate
        W low = W;
        W high = W;
        loss vec = [];
        %10000 iterations and updates using gradient
descent
        for i = 1:10000
            rand image index = randi([1 5200]); %randomly
selects an index in [1 5200]
            trainims in matrix =
trainims(:,:,rand image index); %creates image matrix from
trainims dataset
            x = double(trainims in matrix(:)); %casting
uint8 to double
            x = [x; -1]; %adding bias to the weights
matrix
            x = x/255; %normalization
            v = W'*x; %weighted sum
```

```
y = sigmoid(v); %applying activation function
to v
            der act = sigmoid(v) .* (1 - sigmoid(v));
%derivative of the sigmoid function
            error = (onehot(:,rand image index)-y);
%difference between the desired and realized output of the
network
            grad = x * (error .* der act)'; %gradient for
gradient descent
            W = W + nu opt * grad; %updating weights
matrix
            loss = 1/2 * error' * error; %Mean Square
Error
            loss vec = [loss vec loss]; %storing loss for
each iteration into a vector
        end
        figure;
        for k = 1:26
            subplot (6,5,k), imshow (reshape (W(2:785,k),[28]
28]), [min(W(2:785,k)) max(W(2:785,k))]);
        end
        %testing the trained network using test images
        W test = W;
        correct = 0;
        output tot = [];
        max value = [];
        for i = 1:1300
            rand image index = i; %randomly selects an
index in [1 5200]
            testims in matrix =
testims(:,:,rand image index);
            x test = double(testims in matrix(:));
%casting uint8 to double
            x test = [x test;-1]; %adding bias
            x \text{ test} = x \text{ test/255};
            output test = sigmoid(W test.'*x test);
            [max value, label index] = max(output test);
            if (testlbls(i) == label index)
                correct = correct+1;
            end
        end
        fprintf('The correctness for optimal learning rate
nu 0.1 is = f \in (1300 \times 100);
```

```
nu low = 0.001;
        loss vec low = [];
        for i = 1:10000
            rand image index = randi([1 5200]); %randomly
selects an index in [1 5200]
            trainims in matrix =
trainims(:,:,rand image index); %creates image matrix from
trainims dataset
            x = double(trainims in matrix(:)); %casting
uint8 to double
            x = [x; -1]; %adding bias to the weights
matrix
            x = x/255; %normalization
            v = W low'*x ; %weighted sum
            y = sigmoid(v); %applying activation function
to v
            der act = sigmoid(v) .* (1 - sigmoid(v));
%derivative of the sigmoid function
            error = (onehot(:,rand image index)-y);
%difference between the desired and realized output of the
network
            grad = x * (error .* der act)'; %gradient for
gradient descent
            W low = W low + nu low * grad; %updating
weights matrix
            loss low = 1/2 * error' * error; %Mean
Squarred Error
            loss vec low = [loss vec low loss low];
%storing loss for each iteration into a vector
        end
        W test low = W low;
        correct low = 0;
        output tot low = [];
        max value low = [];
        for i = 1:1300
            rand image index = i;
            testims in matrix =
testims(:,:,rand image index);
            x test = double(testims in matrix(:));
            x \text{ test} = [x \text{ test}; -1];
            x \text{ test} = x \text{ test/255};
            output test = sigmoid(W test low.'*x test);
            [max value low, label index] =
max(output test);
            if (testlbls(i) == label index)
```

```
correct low = correct_low+1;
           end
        end
        fprintf('The correctness for low learning rate nu
0.001 is = f \in \text{orrect low}/1300*100;
        nu high = 0.9;
        loss vec high = [];
        for i = 1:10000
            rand image index = randi([1 5200]); %randomly
selects an index in [1 5200]
           trainims in matrix =
trainims(:,:,rand image index); %creates image matrix from
trainims dataset
           x = double(trainims in matrix(:)); %casting
uint8 to double
           x = [x; -1]; %adding bias to the weights
matrix
           x = x/255; %normalization
           v = W high'*x ; %weighted sum
           y = sigmoid(v); %applying activation function
to v
           der act = sigmoid(v) .* (1 - sigmoid(v));
%derivative of the sigmoid function
           error = (onehot(:,rand image index)-y);
%difference between the desired and realized output of the
network
           grad = x * (error .* der act)'; %gradient for
gradient descent
            W high = W high + nu high * grad; %updating
weights matrix
            loss high = 1/2 * error' * error; %Mean
Squarred Error
            loss vec high = [loss vec high loss high];
%storing loss for each iteration into a vector
        end
        W test high= W high;
        correct high = 0;
        output tot high = [];
        max value high = [];
        for i = 1:1300
            rand image index = i;
```

```
testims in matrix =
testims(:,:,rand image index);
            x test = double(testims in matrix(:));
             x \text{ test} = [x \text{ test}; -1];
            x \text{ test} = x \text{ test}/255;
             output test = sigmoid(W test high.'*x test);
             [max value high, label index] =
max(output test);
             if (testlbls(i) == label index)
                 correct high = correct high+1;
            end
        end
        fprintf('The correctness for high learning rate nu
0.9 is = f^{n'}, correct high/1300*100);
        %plotting loss functions for three different
learning rates on the
        %same figure to compare easily
        iter = [1:10000];
        figure;
        plot(iter,loss vec);
        hold on;
        plot(iter, loss vec low);
        plot(iter, loss vec high);
        title('Plot of Loss Function');
        legend('optimal learning rate 0.1', 'low learning
rate 0.01', 'high learning rate 0.9');
        xlabel('Iteration');
        ylabel('Loss Function J');
end
end
function outStep = unitStep(t)
outStep = t >= 0;
end
function sigmoidOut = sigmoid(v)
sigmoidOut = 1./(1+exp(-v));
end
```