

## EEE321 Lab Work 1

### Introduction

In this lab work we are going to work on digital signals, which are discrete and quantized. It is expected to work on discrete cosine signals. The property of discrete cosine signals are that they are only defined over integers. This property is not peculiar to discrete cosine signals, all the discrete signals are defined over integer variables. The general formula of discrete cosine signal is given below.

$$x[n] = A * \cos[\omega n + \phi], n \in \mathbb{Z}$$

In the formula above  $A$  represents the maximum amplitude of the signal,  $\omega$  represents normalized frequency (in radians) and  $\phi$  represents the phase shift (in radians) of the function.

In the lab manual there are 12 different discrete cosine signals and few questions that some of these questions are about the given cosine signals and the others are general questions. In this lab report all the things indicated in the lab manual will be shown and the codes will be attached to the appendix part.

## Questions & Results

1-)

$$x_1[n] = \cos[0.14\pi n]$$

1-a)

The wanted files are created and the retrieved from directory for all 12 questions, the related codes are shown in appendix part.

Quantization means that the transformation of a continuous signal to a finite interval of discrete values. This process happens when we try to transfer the mathematical continuous functions to digital environment. Normally, there are infinitely many values of the signal that corresponds to wanted interval; however, computers cannot store infinite amount of data since there is no infinite space. To handle this problem, the data is divided equally to wanted number of points, and some approximations are done when there are irrational numbers that corresponds to wanted variables.

When  $x_1$  is stored by computer, it had to be quantized. It is because  $x_1$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_1[2] : 0.905
x_1[8] : -0.998
x_1[111] : -0.309
x_1[127] : 0.426
```

1-b)

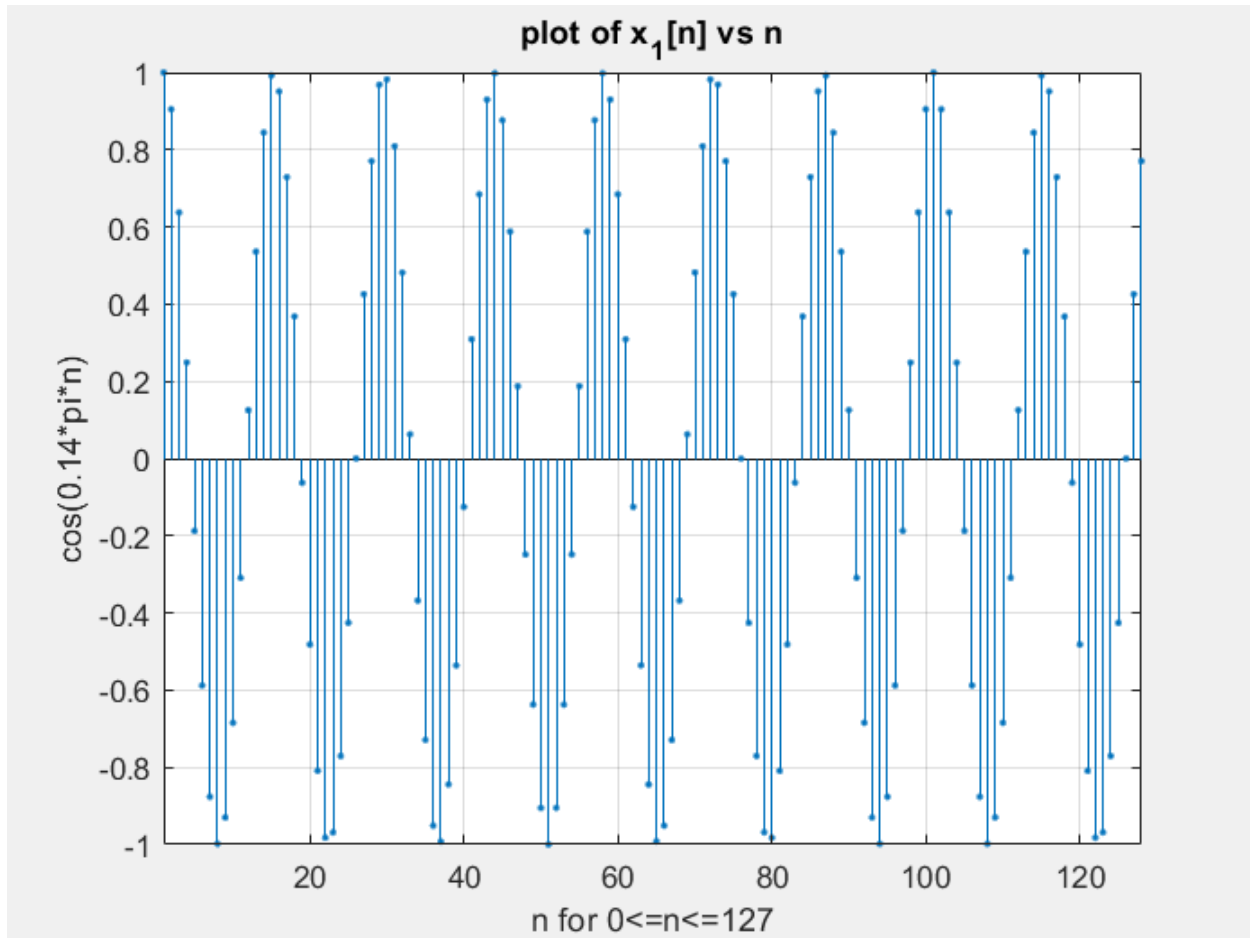


Figure-1) Plot of  $x_1[n]$  vs  $n$

The value of  $\omega$  is  $0.14\pi$  rad.

2-)

$$x_2[n] = \cos[2.3\pi n]$$

2-a)

When  $x_2$  is stored by computer, it had to be quantized. It is because  $x_2$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_2[2] : 0.588  
x_2[8] : 0.951  
x_2[111] : -1.000  
x_2[127] : 0.809
```

2-b)

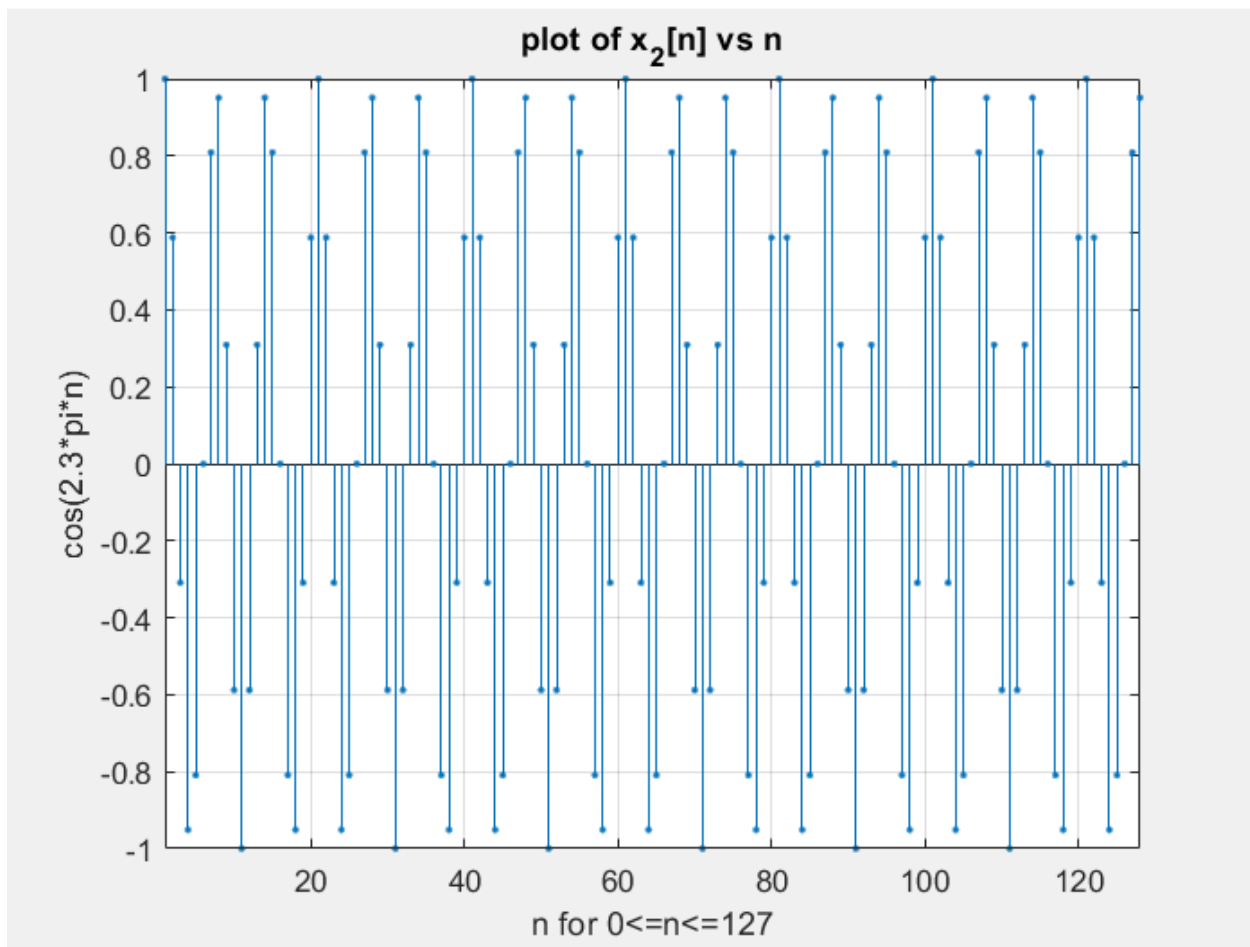


Figure-2) Plot of  $x_2[n]$  vs  $n$

The value of  $\omega$  is  $2.3 \pi$  rad.

3-)

$$x_3[n] = \cos[-1.7\pi n]$$

3-a)

When  $x_3$  is stored by computer, it had to be quantized. It is because  $x_3$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_3[2] : 0.588  
x_3[8] : 0.951  
x_3[111] : -1.000  
x_3[127] : 0.809
```

3-b)

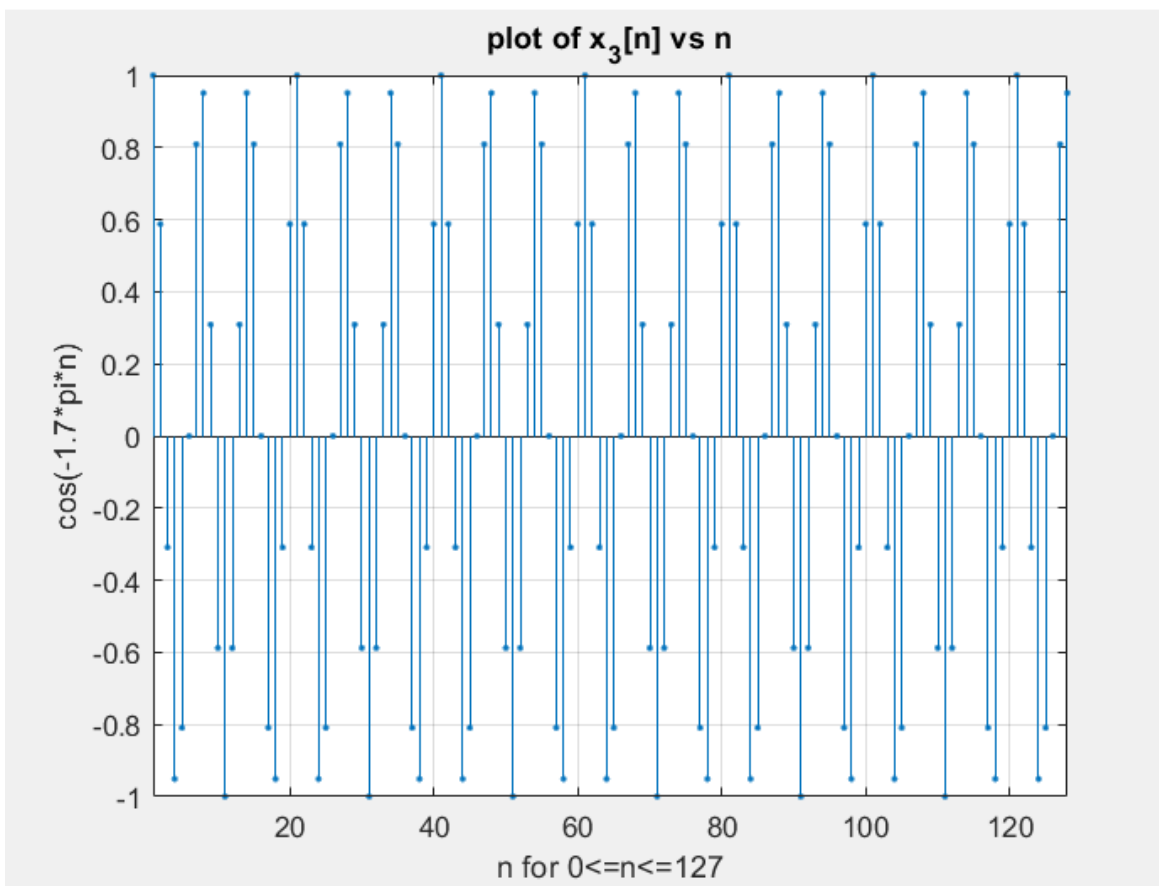


Figure-3) Plot of  $x_3[n]$  vs  $n$

The value of  $\omega$  is  $-1.7\pi$  rad.

### **Comparison of 2 and 3:**

It is known that

$$\cos(a) = \cos(a + 2\pi k); k \in \mathbb{Z}$$

Using this fact, it can be seen that

$$\cos(-1.7\pi n) = \cos(-1.7\pi n + 2\pi * 2) = \cos(2.3\pi n)$$

That has been shown that  $x_2$  and  $x_3$  are equal to each other for any values of  $n$ .

4-)

$$x_4[n] = \cos[0.24\pi n]$$

4-a)

When  $x_4$  is stored by computer, it had to be quantized. It is because  $x_4$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_4[2] : 0.729  
x_4[8] : 0.536  
x_4[111] : 0.309  
x_4[127] : 0.729
```

4-b)

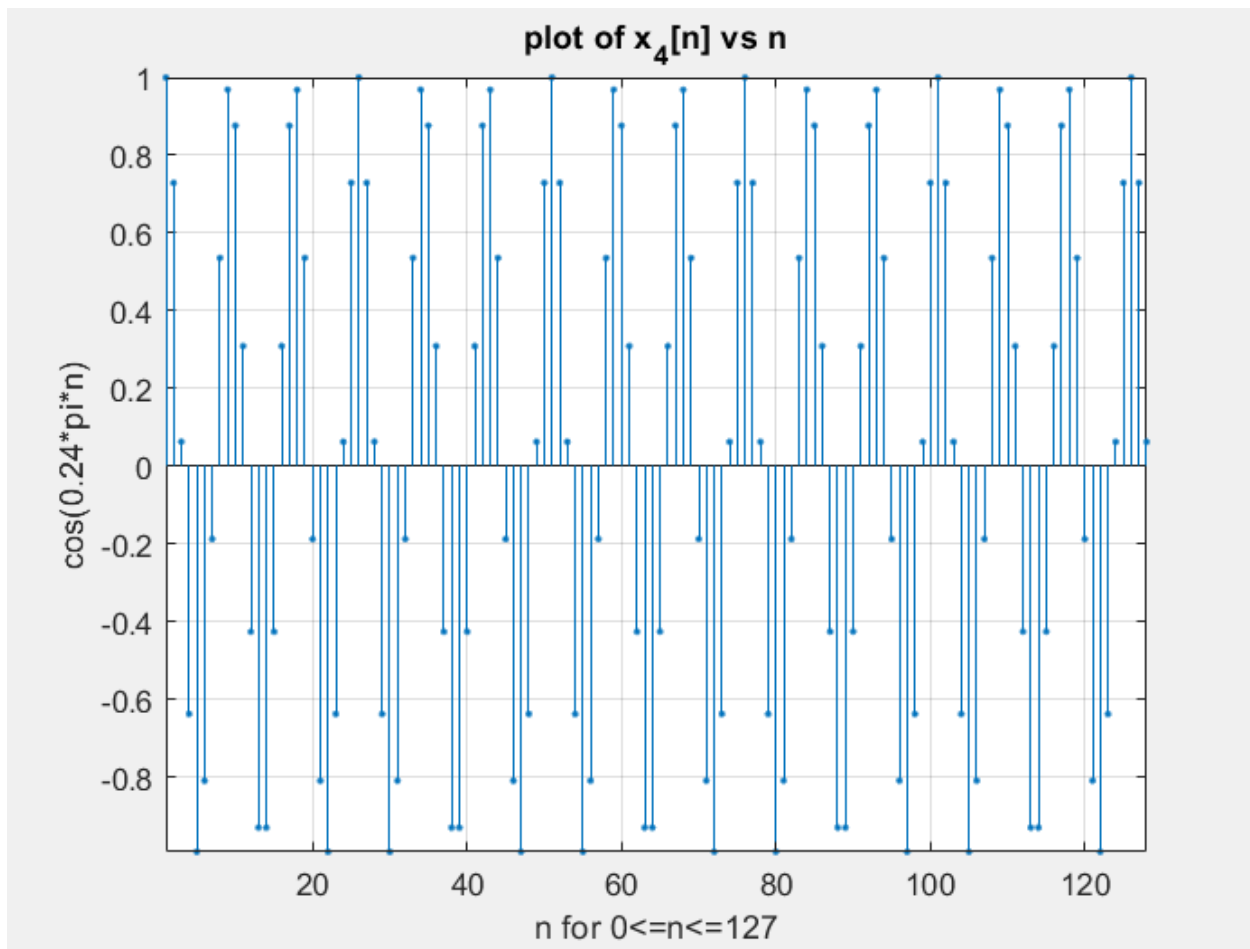


Figure-4) Plot of  $x_4[n]$  vs  $n$

The value of  $\omega$  is  $0.24\pi$  rad.

5-)

$$x_5[n] = \cos[0.24\pi n + 0.4]$$

5-a)

When  $x_5$  is stored by computer, it had to be quantized. It is because  $x_5$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_5[2] : 0.405  
x_5[8] : 0.822  
x_5[111] : -0.086  
x_5[127] : 0.405
```

5-b)

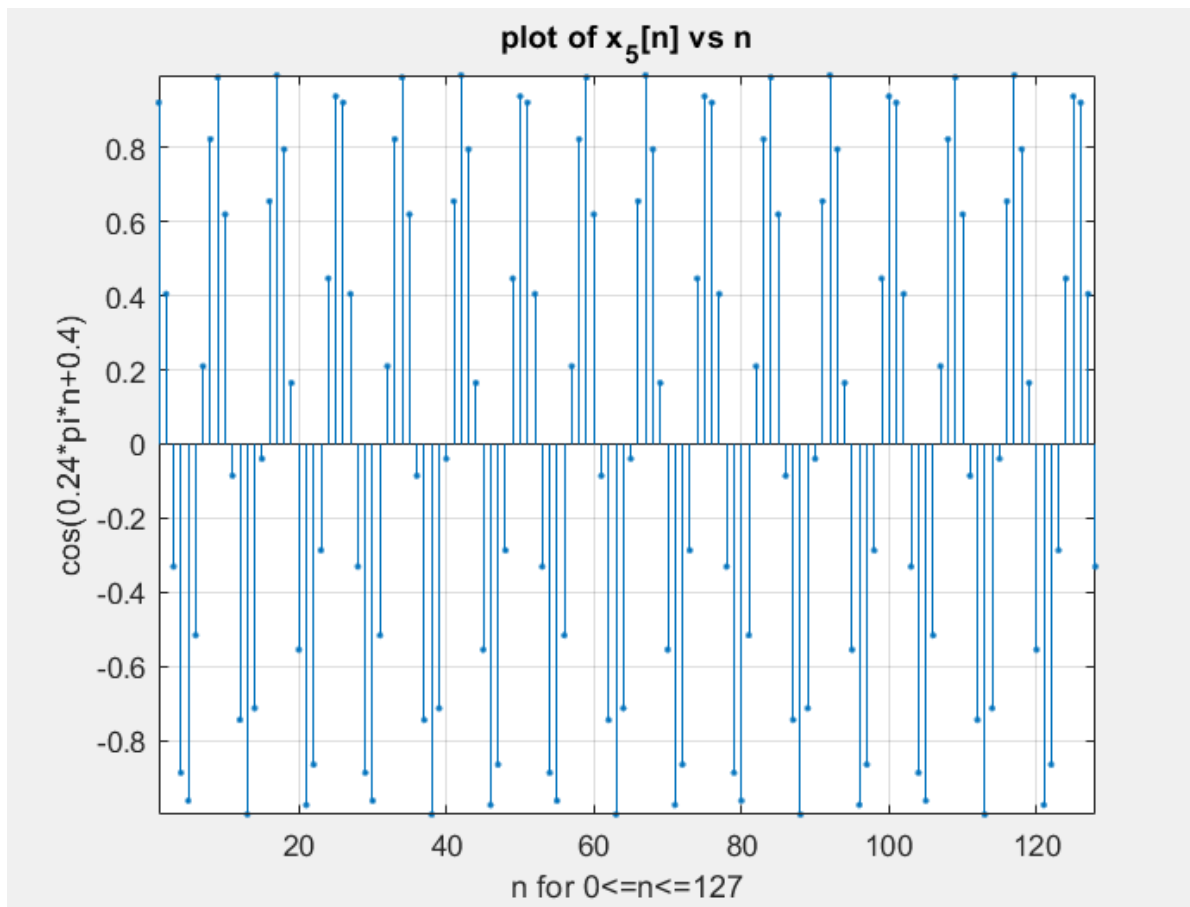


Figure-5) Plot of  $x_5[n]$  vs  $n$



The value of  $\omega$  is  $0.24\pi$  rad.

### **Comparison of 4 and 5:**

Normally it is known that adding constant value to inside of a function is just shifting, so if these functions were continuous functions, 5 would be the shifting version of 4 to the left. However, these functions are discrete. Even if 5 is shifted version of 4 to the left, it cannot be said that 5 is perfectly shifted version of 4. It is because the shifting value (phase) is not an integer (0.4) and that's why values of these functions cannot be matched with this shifting.

6-)

$$x_6[n] = \cos[0.38\pi n]$$

6-a)

When  $x_6$  is stored by computer, it had to be quantized. It is because  $x_6$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_6[2] : 0.368
x_6[8] : -0.482
x_6[111] : 0.809
x_6[127] : 0.930
```

6-b)

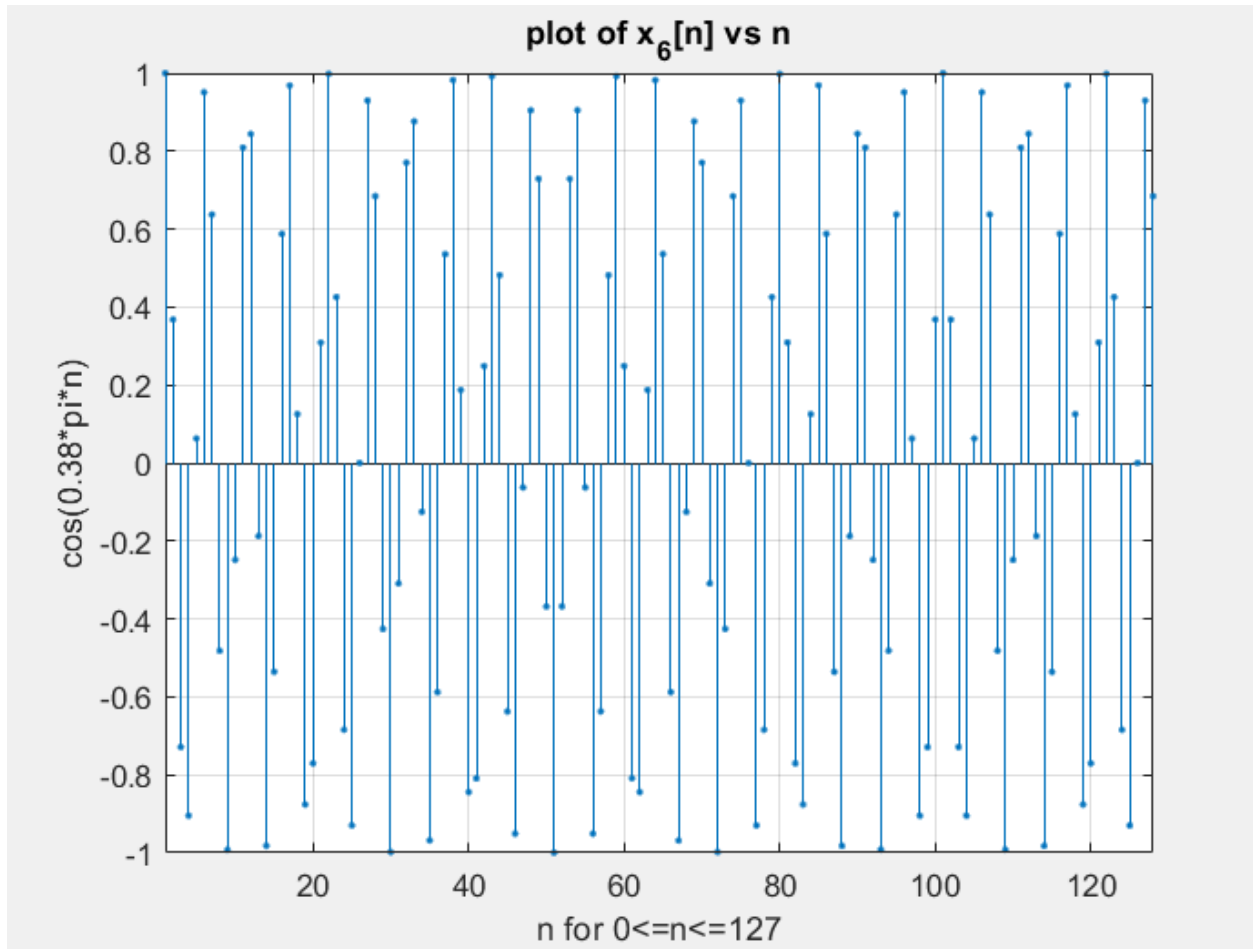


Figure-6) Plot of  $x_6[n]$  vs  $n$

The value of  $\omega$  is  $0.38\pi$  rad.

7-)

$$x_7[n] = \cos[0.01\pi n]$$

7-a)

When  $x_7$  is stored by computer, it had to be quantized. It is because  $x_7$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_7[2] : 1.000  
x_7[8] : 0.976  
x_7[111] : -0.951  
x_7[127] : -0.685
```

7-b)

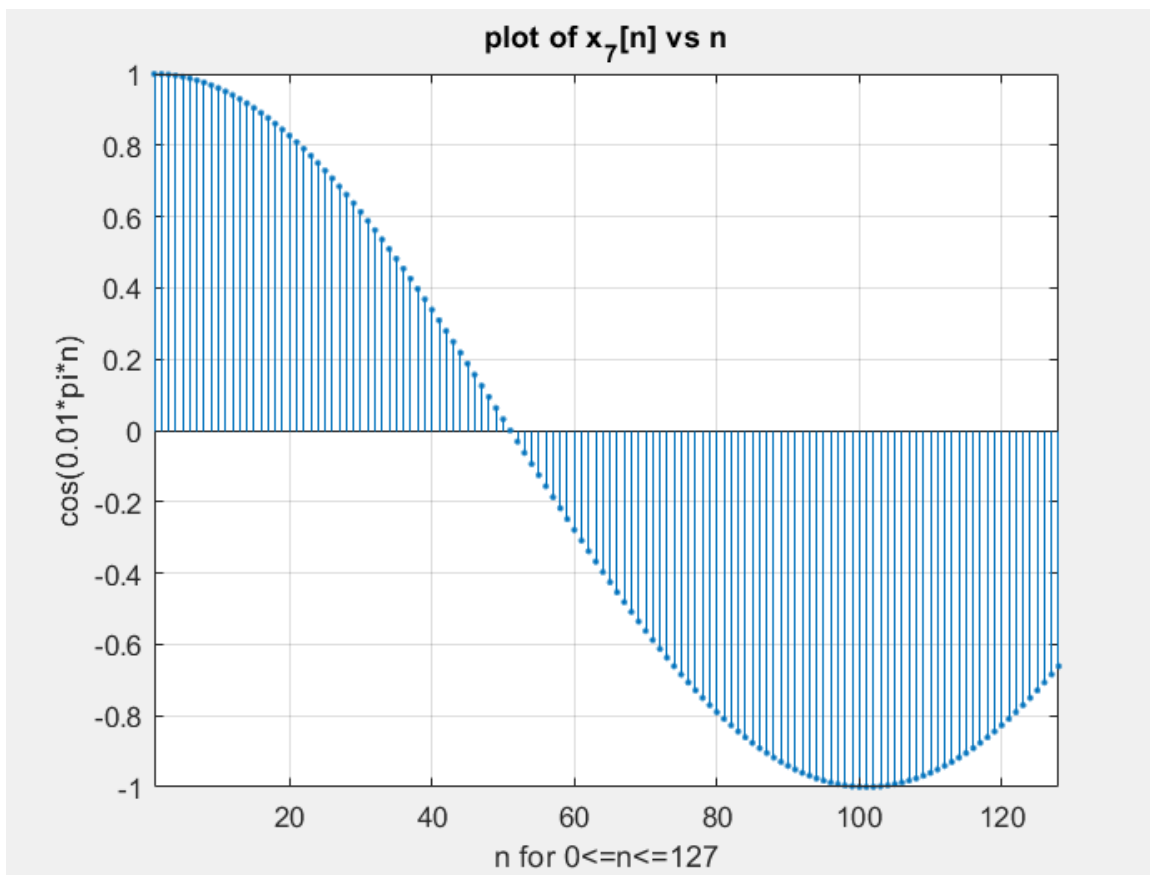


Figure-7) Plot of  $x_7[n]$  vs n

The value of  $\omega$  is  $0.01\pi$  rad.

8-)

$$x_8[n] = \cos[\pi n]$$

8-a)

When  $x_8$  is stored by computer, it had to be quantized. It is because  $x_8$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_8[2] : -1.000  
x_8[8] : -1.000  
x_8[111] : 1.000  
x_8[127] : 1.000
```

8-b)

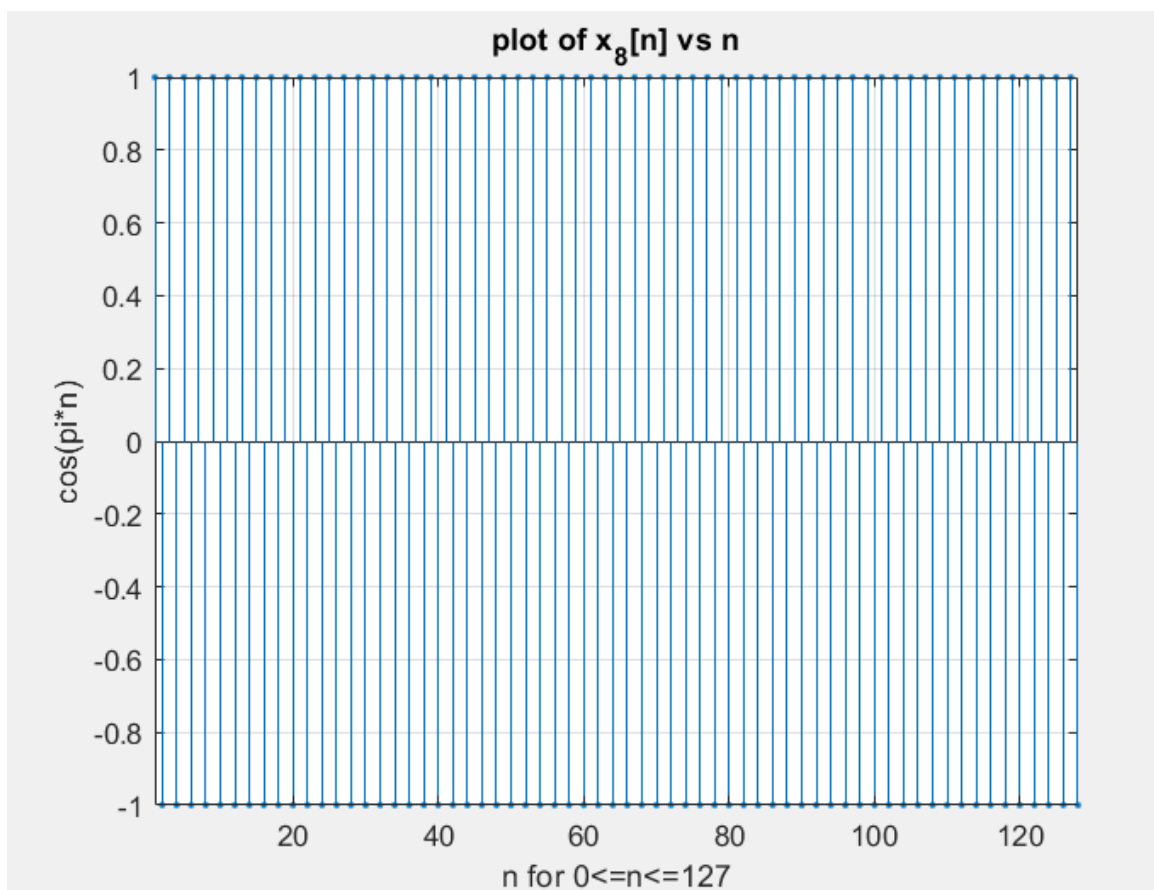


Figure-8) Plot of  $x_8[n]$  vs  $n$

The value of  $\omega$  is  $\pi$  rad.

9-)

$$x_9[n] = \cos[1.06\pi n]$$

9-a)

When  $x_9$  is stored by computer, it had to be quantized. It is because  $x_9$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_9[2] : -0.982  
x_9[8] : -0.249  
x_9[111] : -0.309  
x_9[127] : 0.187
```

9-b)

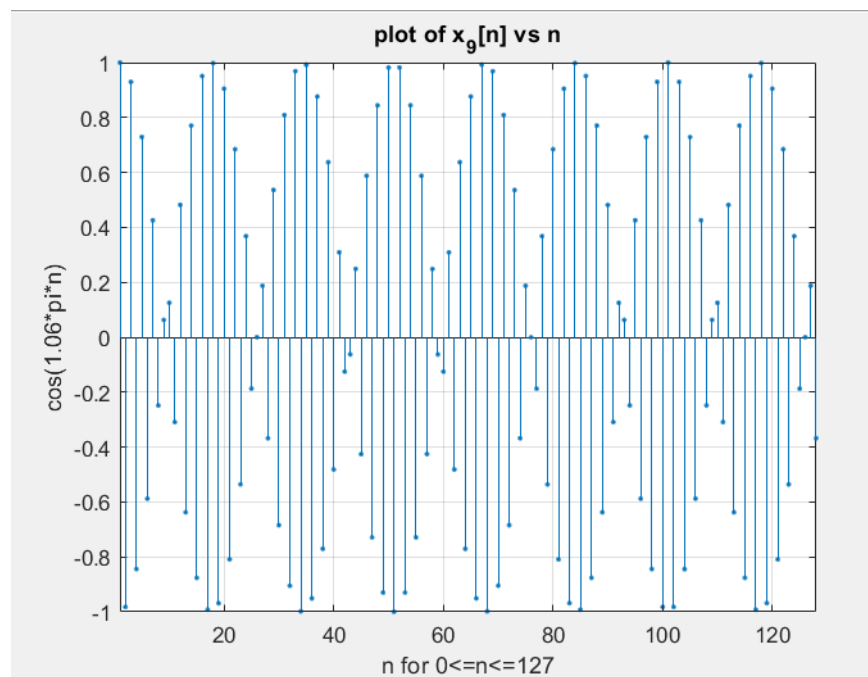


Figure-9) Plot of  $x_9[n]$  vs n

The value of  $\omega$  is  $1.06\pi$  rad.

10-)

$$x_{10}[n] = \cos[0.94\pi n]$$

10-a)

When  $x_{10}$  is stored by computer, it had to be quantized. It is because  $x_{11}$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_10[2] : -0.982
x_10[8] : -0.249
x_10[111] : -0.309
x_10[127] : 0.187
```

10-b)

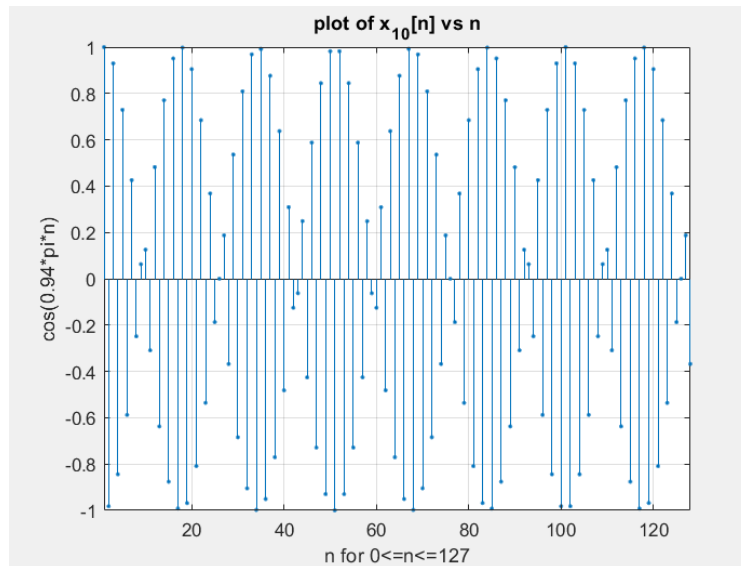


Figure-10) Plot of  $x_{10}[n]$  vs  $n$

The value of  $\omega$  is  $0.94\pi$  rad.

### **Comparison of 9 and 10:**

It is known that

$$\cos(a) = \cos(a + 2\pi k); k \in \mathbb{Z}$$

and

$$\cos(b) = \cos(-b)$$

Using these facts, it can be seen that

$$\cos(0.94\pi n) = \cos(-0.94\pi n) = \cos(-0.94\pi n + 2\pi n) = \cos(1.06\pi n)$$

It has been shown that  $x_9$  and  $x_{10}$  are equal to each other for any values of  $n$

11-)

$$x_{11}[n] = \cos[n]$$

11-a)

When  $x_{11}$  is stored by computer, it had to be quantized. It is because  $x_{11}$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.

Read and printed Results are:

```
x_11[2] : 0.540
x_11[8] : 0.754
x_11[111] : -0.999
x_11[127] : 0.944
```

11-b)

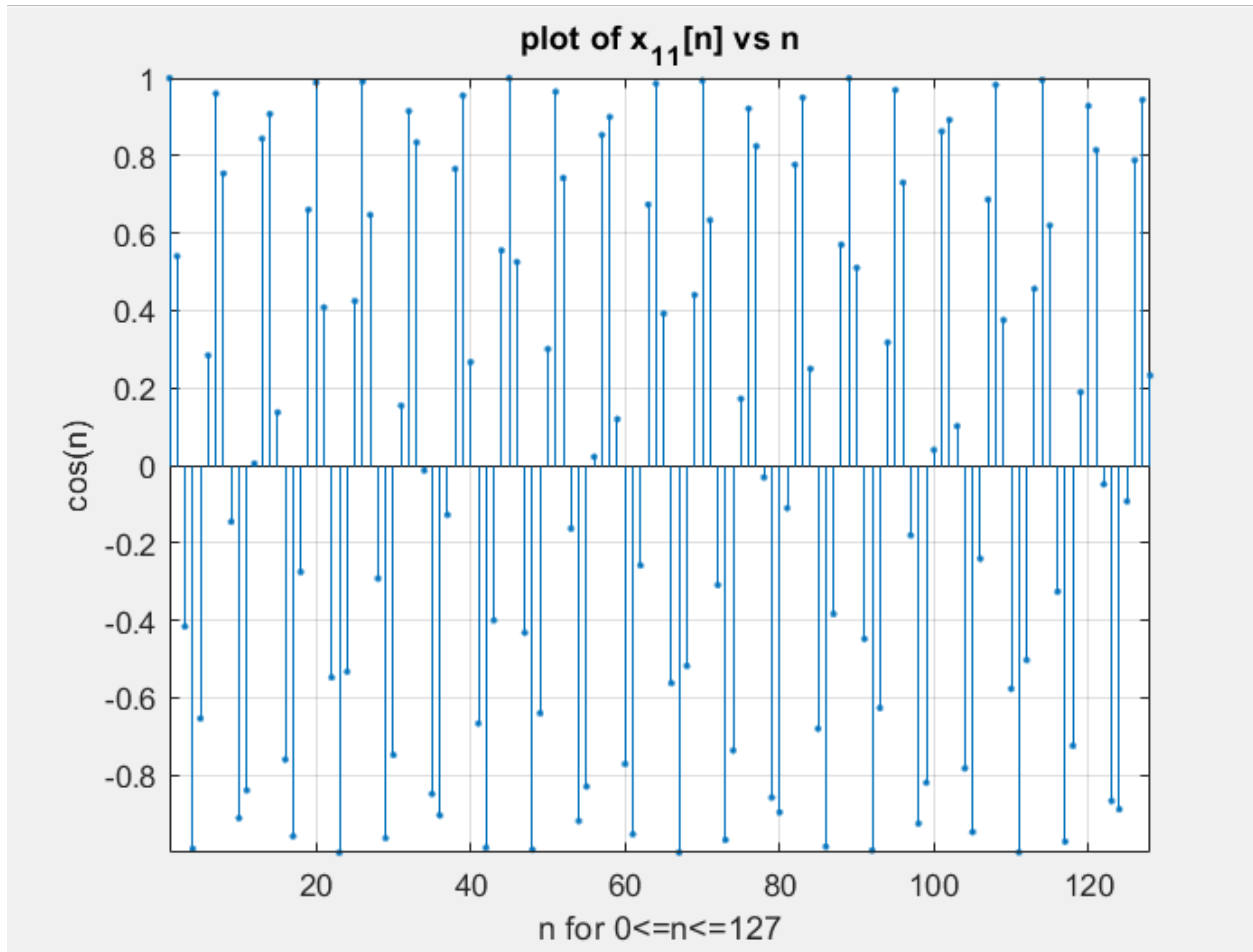


Figure-11) Plot of  $x_{11}[n]$  vs n

The value of  $\omega$  is 1 rad.

12-)

$$x_{12}[n] = \cos[0.8n + 0.3]$$

12-a)

When  $x_{12}$  is stored by computer, it had to be quantized. It is because  $x_{12}$  is a continuous function in normal circumstances and some of their values are irrational. To store it in a small space it has been quantized.



Read and printed Results are:

```
x_12[2] : 0.454  
x_12[8] : 0.927  
x_12[111] : 0.944  
x_12[127] : 0.842
```

12-b)

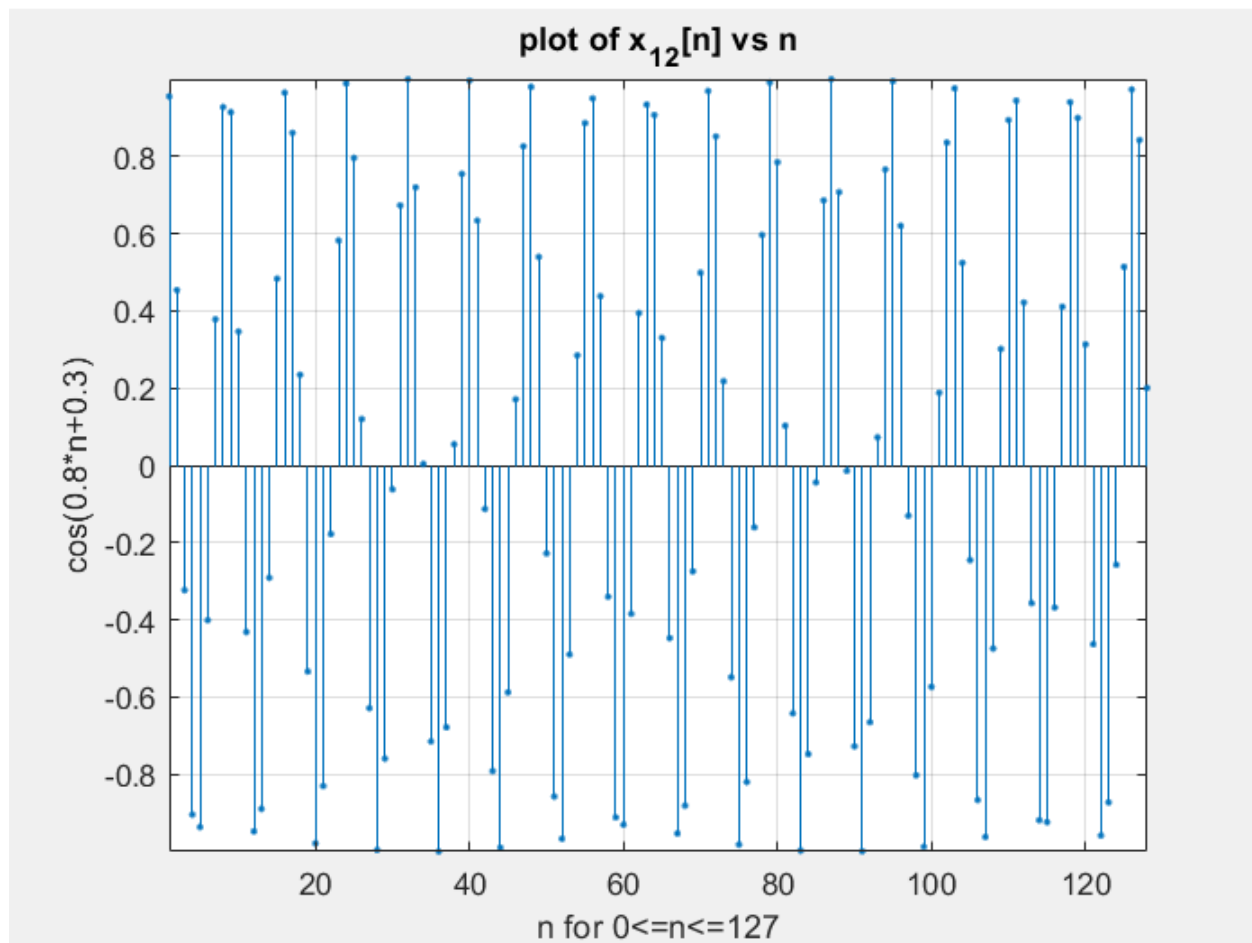


Figure-12) Plot of  $x_{12}[n]$  vs  $n$

The value of  $\omega$  is 0.8 rad.

Before answering question 13, question 14 is going to be answered and using the answer to question 14, fundamental periods of signals will be found for question 13.

14)

In the lab manual the information below was given.

A discrete signal  $x[n]$  is said to be *periodic* if an integer  $N$  can be found, such that,  $x[n + N] = x[n]$  for all  $n$ ; in that case,  $N$  is a *period* of  $x[n]$ . Note that  $N$ , is not unique if it exists; minimum positive  $N$  is called the *fundamental period*. If a period cannot be found, as defined above, then the signal is not a periodic signal.

Then using the Euler's formula, we know that real part of complex function is a cosine function, which is  $X_i$  in this lab.

$$X_i[n] = \text{Re}\{e^{j\omega n}\} = X_i[n + N] = \text{Re}\{e^{j\omega(n+N)}\} = \text{Re}\{e^{j\omega N} e^{j\omega n}\}$$

The equation above gives that

$$e^{j\omega n} = e^{j\omega n} * e^{j\omega N}$$

Using this equation, we got the equation below.

$$e^{j\omega N} = 1$$

It is known that  $\exp(2\pi * a) = 1$ , it implies that  $\omega N = 2\pi a$ ,  $a \in Z$

$$\frac{\omega}{2\pi} = \frac{a}{N}$$

The last equation gives the needed information us, to have a period the equation must be satisfied. Since the right-hand side of the equation is rational number (both  $a$  and  $N$  are integer), the left-hand side must be rational as well. So must be in a such form that  $\omega = \pi * b$ ,  $b \in R$ . This is the needed condition for  $\omega$  to satisfy the periodicity.

The minimum  $N$  that satisfies the last equation is the fundamental period of the signal.

13)

$$13.1) x_1[n] = \cos[0.14\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / 0.14\pi = 100a / 7 = N$ . The smallest integer N that satisfies this condition is 100. Then it is seen that the fundamental period of  $x_1$  is 100.

$$13.2) x_2[n] = \cos[2.3\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / 2.3\pi = 20a / 23 = N$ . The smallest integer N that satisfies this condition is 20. Then it is seen that the fundamental period of  $x_2$  is 20.

$$13.3) x_3[n] = \cos[-1.7\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / -1.7\pi = 20a / -17 = N$ . The smallest integer N that satisfies this condition is 20. Then it is seen that the fundamental period of  $x_3$  is 20.

$$13.4) x_4[n] = \cos[0.24\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / 0.24\pi = 25a / 6 = N$ . The smallest integer N that satisfies this condition is 25. Then it is seen that the fundamental period of  $x_4$  is 25.

$$13.5) x_5[n] = \cos[0.24\pi n + 0.4]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / 0.24\pi = 25a / 6 = N$ . The smallest integer  $N$  that satisfies this condition is 25. Then it is seen that the fundamental period of  $x_5$  is 25.

$$13.6) x_6[n] = \cos[0.38\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / 0.38\pi = 19 = N$ . The smallest integer  $N$  that satisfies this condition is 100. Then it is seen that the fundamental period of  $x_6$  is 100.

$$13.7) x_7[n] = \cos[0.01\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / 0.01\pi = 200a / 1 = N$ . The smallest integer  $N$  that satisfies this condition is 200. Then it is seen that the fundamental period of  $x_7$  is 200.

$$13.8) x_8[n] = \cos[\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a / \omega$ . According to this rule  $2\pi a / \pi = 2a / 1 = N$ . The smallest integer  $N$  that satisfies this condition is 2. Then it is seen that the fundamental period of  $x_8$  is 2.

$$13.9) x_9[n] = \cos[1.06\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a/\omega$ . According to this rule  $2\pi a/1.06\pi = 100a/53 = N$ . The smallest integer N that satisfies this condition is 100. Then it is seen that the fundamental period of  $x_9$  is 100.

$$13.10) x_{10}[n] = \cos[0.94\pi n]$$

According to rule found while answering question 14,  $N = 2\pi a/\omega$ . According to this rule  $2\pi a/0.94\pi = 100a/47 = N$ . The smallest integer N that satisfies this condition is 100. Then it is seen that the fundamental period of  $x_{10}$  is 100.

$$13.11) x_{11}[n] = \cos[n]$$

According to rule found while answering question 14,  $N = 2\pi a/\omega$ . According to this rule  $2\pi a/1 = N$ . There is no integer N that satisfies this condition. Then it is seen that  $x_{11}$  is not periodic.

$$13.12) x_{12}[n] = \cos[0.8n+0.3]$$

According to rule found while answering question 14,  $N = 2\pi a/\omega$ . According to this rule  $2\pi a/0.8 = N$ . There is no integer N that satisfies this condition. Then it is seen that  $x_{12}$  is not periodic.

15)

It is known that  $2\pi$  is the natural and fundamental period of any cosine signal and using this fact it is easily can be said that  $2\pi/\omega = T$  (*period*) for any continuous cosine signal. Therefore, for a continuous cosine signal there is no periodicity condition. In other words, the period of a cosine signal is the interval between two maxima or two minima. However, if the signal is a discrete cosine signal, the period doesn't have to be the interval between two extrema. Instead of this rule there is another so that  $T$  must be integer and  $\omega * T$  must be a multiple of  $2\pi$ , mathematically  $\omega * T = 2\pi a$ ;  $a, T \in \mathbb{Z}$ , which was shown while answering question 14. This is because unlike continuous functions, all the variables that function can take is integer and so their intervals are integer as well. Since the period is one of those intervals, it must be an integer too.

## Appendix

```
n=[0:127];
```

```
disp("------(1.a)-----")
```

```
temp_x_1=cos(0.14*pi*n);
```

```
writematrix(temp_x_1,"x_1.csv");
```

```
x_1=readmatrix("x_1.csv");
```

```
fprintf("x_1[2] : %0.3f \nx_1[8] : %0.3f\nx_1[111] : %0.3f\nx_1[127] : %0.3f \n",  
x_1(2),x_1(8),x_1(111),x_1(127))
```

```
figure
```

```
stem(x_1, '.')
```

```
title('plot of x_1[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(0.14*pi*n)')
```

```
grid on
```

```
axis tight
```

```
fprintf("the value of w is %0.3f rad \n", 0.14*pi)
```

```
fprintf("the fundamental period is %0.f \n", 100)
```

```
disp("------(2.a)-----")
```

```
temp_x_2=cos(2.3*pi*n);
```

```
writematrix(temp_x_2,"x_2.csv");
```

```
x_2=readmatrix("x_2.csv");
```

```
fprintf("x_2[2] : %0.3f \nx_2[8] : %0.3f\nx_2[111] : %0.3f\nx_2[127] : %0.3f\n",  
x_2(2),x_2(8),x_2(111),x_2(127))
```

figure

```
stem(x_2, '.')
```

```
title('plot of x_2[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(2.3*pi*n)')
```

grid on

axis tight

```
fprintf("the value of w is %0.3f rad\n", 2.3*pi)
```

```
fprintf("the fundamental period is %0.f \n", 20)
```

```
disp("------(3.a)-----")
```

```
temp_x_3=cos(-1.7*pi*n);
```

```
writematrix(temp_x_3,"x_3.csv");
```

```
x_3=readmatrix("x_3.csv");
```

```
fprintf("x_3[2] : %0.3f \nx_3[8] : %0.3f\nx_3[111] : %0.3f\nx_3[127] : %0.3f\n",
```

```
x_3(2),x_3(8),x_3(111),x_3(127))
```



figure

stem(x\_3, 'r')

title('plot of x\_3[n] vs n')

xlabel('n for 0 ≤ n ≤ 127')

ylabel('cos(-1.7\*pi\*n)')

grid on

axis tight

fprintf("the value of w is %0.3f rad\n", -1.7\*pi)

fprintf("the fundamental period is %0.f \n", 20)

disp("-----Comparison (2) and (3)-----")

disp("it is known that  $\cos(a) = \cos(a + 2\pi k)$ ")

disp("using this fact, it can be seen that  $\cos(-1.7\pi n) = \cos(-$

$1.7\pi n + 2\pi(2n)) = \cos(2.3\pi n)$ ")

disp("it has been shown that x\_2 and x\_3 are equal to each other for any values of n")

disp("------(4.a)-----")

temp\_x\_4 = cos(0.24\*pi\*n);

writematrix(temp\_x\_4, "x\_4.csv");

x\_4 = readmatrix("x\_4.csv");

```
fprintf("x_4[2] : %0.3f \nx_4[8] : %0.3f\nx_4[111] : %0.3f\nx_4[127] : %0.3f\n",  
x_4(2),x_4(8),x_4(111),x_4(127))
```

figure

```
stem(x_4, '.')
```

```
title('plot of x_4[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(0.24*pi*n)')
```

grid on

axis tight

```
fprintf("the value of w is %0.3f rad\n", 0.24*pi)
```

```
fprintf("the fundamental period is %0.f \n", 25)
```

```
disp("------(5.a)-----")
```

```
temp_x_5=cos(0.24*pi*n+0.4);
```

```
writematrix(temp_x_5,"x_5.csv");
```

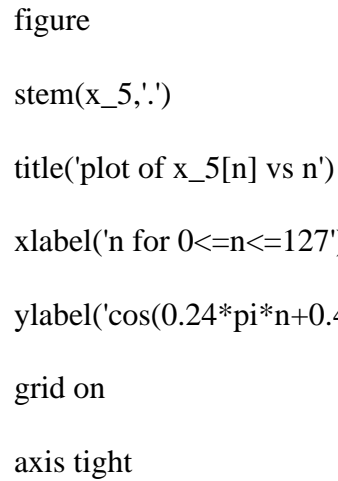
```
x_5=readmatrix("x_5.csv");
```

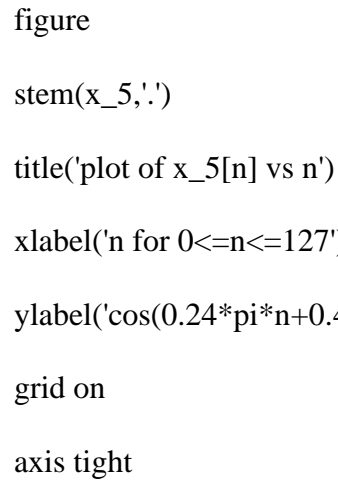
```
fprintf("x_5[2] : %0.3f \nx_5[8] : %0.3f\nx_5[111] : %0.3f\nx_5[127] : %0.3f\n",
```

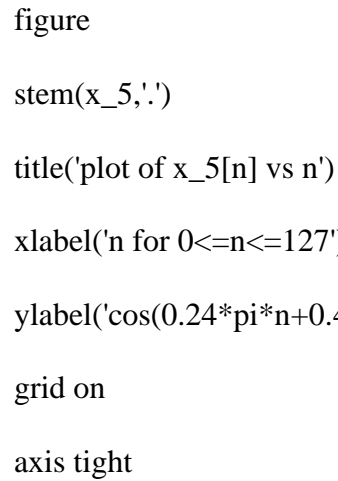
```
x_5(2),x_5(8),x_5(111),x_5(127))
```

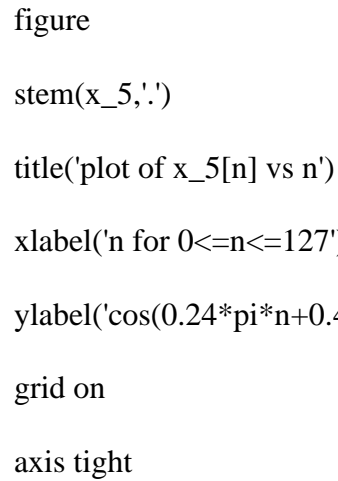
figure

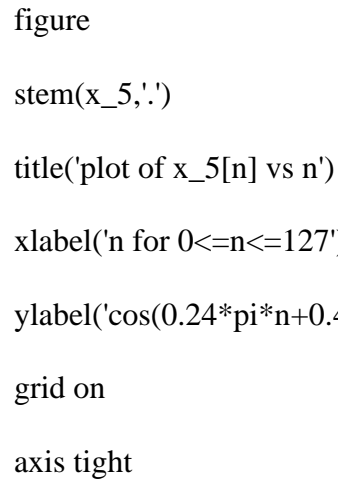
stem(x\_5, '.')

title('plot of  $x_5[n]$  vs  $n$ ')  


xlabel('n for  $0 \leq n \leq 127$ ')  


ylabel('cos( $0.24 \cdot \pi \cdot n + 0.4$ )')  


grid on  


axis tight  


fprintf("the value of  $w$  is  $0.3f$  rad\n",  $0.24 \cdot \pi$ )

fprintf("the fundamental period is  $0.f$  \n", 25)

disp("-----Comparison (4) and (5)-----")

disp("normally it is known that adding constant value to inside of a function is just shifting")

disp("so if these functions were continuous functions, 5 would be the shifting version of 4 to the left")

disp("however these functions are discrete")

disp("even if they have same period and of course same periods, it cannot be said that 5 is shifted version of 4")

disp("it is because the shifting value is not an integer (0.4) and that's why values of these functions cannot be matched with this shifting")

```
disp("------(6.a)-----")
```

```
temp_x_6=cos(0.38*pi*n);
```

```
writematrix(temp_x_6,"x_6.csv");
```

```
x_6=readmatrix("x_6.csv");
```

```
fprintf("x_6[2] : %0.3f \nx_6[8] : %0.3f \nx_6[111] : %0.3f \nx_6[127] : %0.3f \n",
```

```
x_6(2),x_6(8),x_6(111),x_6(127))
```

```
figure
```

```
stem(x_6,')
```

```
title('plot of x_6[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(0.38*pi*n)')
```

```
grid on
```

```
axis tight
```

```
fprintf("the value of w is %0.3f rad\n", 0.38*pi)
```

```
fprintf("the fundamental period is %0.f \n", 100)
```

```
disp("------(7.a)-----")
```

```
temp_x_7=cos(0.01*pi*n);
```

```
writematrix(temp_x_7,"x_7.csv");
```

```
x_7=readmatrix("x_7.csv");
```

```
fprintf("x_7[2] : %0.3f \nx_7[8] : %0.3f\nx_7[111] : %0.3f\nx_7[127] : %0.3f\n",
```

```
x_7(2),x_7(8),x_7(111),x_7(127))
```

```
figure
```

```
stem(x_7, '.')
```

```
title('plot of x_7[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(0.01*pi*n)')
```

```
grid on
```

```
axis tight
```

```
fprintf("the value of w is %0.3f rad\n", 0.01*pi)
```

```
fprintf("the fundamental period is %0.f \n", 200)
```

```
disp("------(8.a)-----")
```

```

temp_x_8=cos(pi*n);
writematrix(temp_x_8,"x_8.csv");
x_8=readmatrix("x_8.csv");
fprintf("x_8[2] : %0.3f \nx_8[8] : %0.3f\nx_8[111] : %0.3f\nx_8[127] : %0.3f\n",
x_8(2),x_8(8),x_8(111),x_8(127))

```

```

figure
stem(x_8,'.')
title('plot of x_8[n] vs n')
xlabel('n for 0<=n<=127')
ylabel('cos(pi*n)')
grid on
axis tight

```

```

fprintf("the value of w is %0.3f rad\n", pi)
fprintf("the fundamental period is %0.f \n", 2)

```

```

disp("------(9.a)-----")

```

```

temp_x_9=cos(1.06*pi*n);
writematrix(temp_x_9,"x_9.csv");

```

```

x_9=readmatrix("x_9.csv");

fprintf("x_9[2] : %0.3f \nx_9[8] : %0.3f\nx_9[111] : %0.3f\nx_9[127] : %0.3f\n",
x_9(2),x_9(8),x_9(111),x_9(127))

```

```

figure

stem(x_9,')

title('plot of x_9[n] vs n')

xlabel('n for 0<=n<=127')

ylabel('cos(1.06*pi*n)')

grid on

axis tight

```

```

fprintf("the value of w is %0.3f rad\n", 1.06*pi)

fprintf("the fundamental period is %0.f \n", 100)

```

```

disp("------(10.a)-----")

```

```

temp_x_10=cos(0.94*pi*n);

writematrix(temp_x_10,"x_10.csv");

x_10=readmatrix("x_10.csv");

```

```
fprintf("x_10[2] : %0.3f \nx_10[8] : %0.3f\nx_10[111] : %0.3f\nx_10[127] : %0.3f\n",  
x_10(2),x_10(8),x_10(111),x_10(127))
```

figure

```
stem(x_10, '.')
```

```
title('plot of x_1_0[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(0.94*pi*n)')
```

grid on

axis tight

```
fprintf("the value of w is %0.3f rad\n", 0.94*pi)
```

```
fprintf("the fundamental period is %0.f \n", 100)
```

```
disp("-----Comparison (9) and (10)-----")
```

```
disp("it is know that  $\cos(a)=\cos(a+2*\pi*k)$  and  $\cos(b)=\cos(-b)$ ")
```

```
disp("using these facts, it can be seen that  $\cos(0.94*\pi*n)=\cos(-0.94*\pi*n)=\cos(-$ 
```

```
 $0.94*\pi*n+2*\pi*n)=\cos(1.06*\pi*n)$ ")
```

```
disp("it has been shown that x_9 and x_10 are equal to each other for any values of n")
```

```
disp("----- (11.a) -----")
```



```

temp_x_11=cos(n);

writematrix(temp_x_11,"x_11.csv");

x_11=readmatrix("x_11.csv");

fprintf("x_11[2] : %0.3f \nx_11[8] : %0.3f\nx_11[111] : %0.3f\nx_11[127] : %0.3f\n",
x_11(2),x_11(8),x_11(111),x_11(127))

figure

stem(x_11, '.')

title('plot of x_1_1[n] vs n')

xlabel('n for 0<=n<=127')

ylabel('cos(n)')

grid on

axis tight

fprintf("the value of w is %0.3f rad\n", 1)

fprintf("it is not periodic since there is no integer k or period for the equation k*2*pi=period*n\n")

disp("------(12.a)-----")

temp_x_12=cos(0.8*n+0.3);

```

```
writematrix(temp_x_12,"x_12.csv");
```

```
x_12=readmatrix("x_12.csv");
```

```
fprintf("x_12[2] : %0.3f \nx_12[8] : %0.3f\nx_12[111] : %0.3f\nx_12[127] : %0.3f \n",
```

```
x_12(2),x_12(8),x_12(111),x_12(127))
```

```
figure
```

```
stem(x_12,'.')
```

```
title('plot of x_1_2[n] vs n')
```

```
xlabel('n for 0<=n<=127')
```

```
ylabel('cos(0.8*n+0.3)')
```

```
grid on
```

```
axis tight
```

```
fprintf("the value of w is %0.3f rad\n", 0.8)
```

```
fprintf("it is not periodic since there is no integer k or period for the equation  $k*2*\pi=0.8*period$ \n\n")
```

```
fprintf("14) to have a period for discrete signals w must satisfy that T(period) must be an integer\nand w*(T)period must be a multiple of  $2*\pi$  \n\n")
```

```
disp("15) it is known that  $2\pi$  is the natural and fundamental period of a cosine signal,")
```

```
disp("and using this fact it is easily can be said that  $2\pi/w=T(period)$  for a continuous cosine")
```

```
disp("so for continuous cosine signals there is no periodicity condition ")
```

```
disp("however if the signal is a discrete cosine signal period must be integer and so  $w \cdot T(\text{period})$   
must be a multiple of  $2\pi$ :  $w \cdot T = k \cdot 2\pi$ ;  $k$  and  $T$  are integers")
```

```
disp("this is because unlike continuous functions, all the units function can take is integer and so  
their intervals are integer as well")
```

```
disp("since the period is one of those intervals, it must be an integer as well")
```

```
save lab_1.mat
```

```
load lab_1.mat
```